

# BLR Dynamical Modeling in Reverberation Mapping

Yan-Rong Li  
Institute of High Energy Physics

SEMAMBH collaboration  
MAHA collaboration

“Mapping Central Regions of Active Galactic Nuclei”  
Guilin China, 2019-09-20

# Outline

- I. An introduction to BLR dynamical modeling
- II. Application to Mrk 142
- III. Application to NGC 3227
- IV. Future improvements

# All efforts of RM analysis

To obtain the transfer function/velocity-delay map from the integral equation

$$L(\mathbf{v}, t) = \int \Psi(\mathbf{v}, \tau) C^{1+\gamma}(t - \tau) d\tau$$

For small continuum variations, the linearized equation is

$$\Delta L(\mathbf{v}, t) = \int \Psi(\mathbf{v}, \tau) \Delta C(t - \tau) d\tau$$

$$\Delta L(\mathbf{v}, t) = L(\mathbf{v}, t) - L_0$$

$$\Delta C(t) = C(t) - C_0$$

# All efforts of RM analysis

To obtain the transfer function/velocity-delay map from the integral equation

$$L(v, t) = \int \Psi(v, \tau) C^{1+\gamma}(t - \tau) d\tau$$

Methods:

- ✓ Fourier transformation: Blandford & McKee 1982
- ✓ Regularized linear inversion: Krolik & Done 1995; Skielboe+2015
- ✓ Maximum entropy technique: Horne 1994
- ✓ **BLR dynamical modeling**: Pancoast et al. 2011, 2014; Li et al. 2013, 2018

# All efforts of RM analysis

Dynamical modeling approach explores the best solution with input BLR models

$$L(v, t) = \int \Psi(v, \tau) C^{1+\gamma} (t - \tau) d\tau$$



BLR dynamical model

# Early attempts: computing $\Psi(v, \tau)$

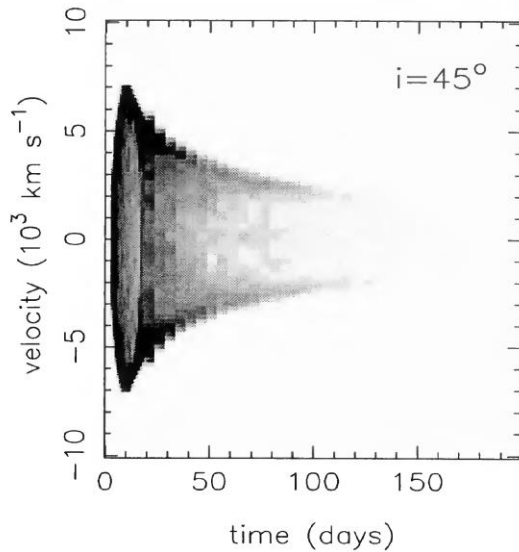
## The response of the broad emission line region to ionizing continuum variations – III. An atlas of transfer functions

E. Pérez,<sup>1</sup> A. Robinson<sup>2</sup> and L. de la Fuente<sup>1</sup>

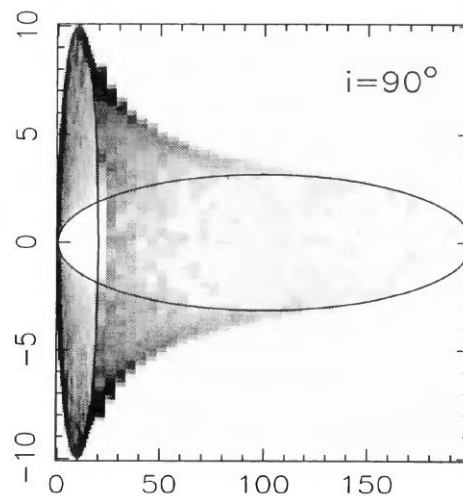
<sup>1</sup>Instituto de Astrofísica de Canarias, 38200 La Laguna, Tenerife

<sup>2</sup>Institute of Astronomy, Madingley Road, Cambridge, CB3 0HA

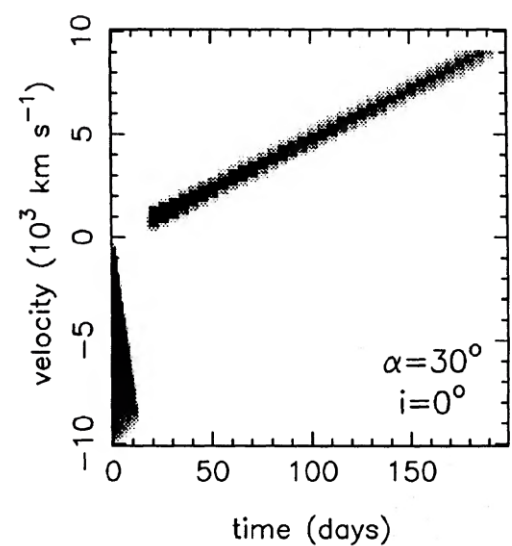
Perez et al. 1992, MNRAS, 256, 103



inclined disk



edge-on disk



bi-conical outflow

# Early attempts: computing $\Psi(v, \tau)$

## Response functions as diagnostics of the broad-line region in active galactic nuclei – II. Anisotropic line emission

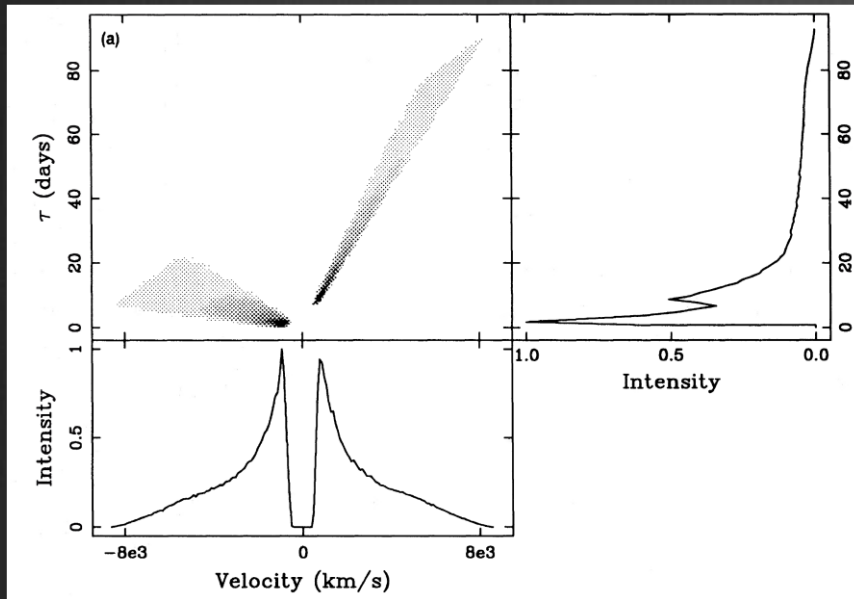
P. T. O'Brien,<sup>1,2</sup> M. R. Goad<sup>1</sup> and P. M. Gondhalekar<sup>3</sup>

<sup>1</sup>Department of Physics & Astronomy, University College London, Gower Street, London WC1E 6BT

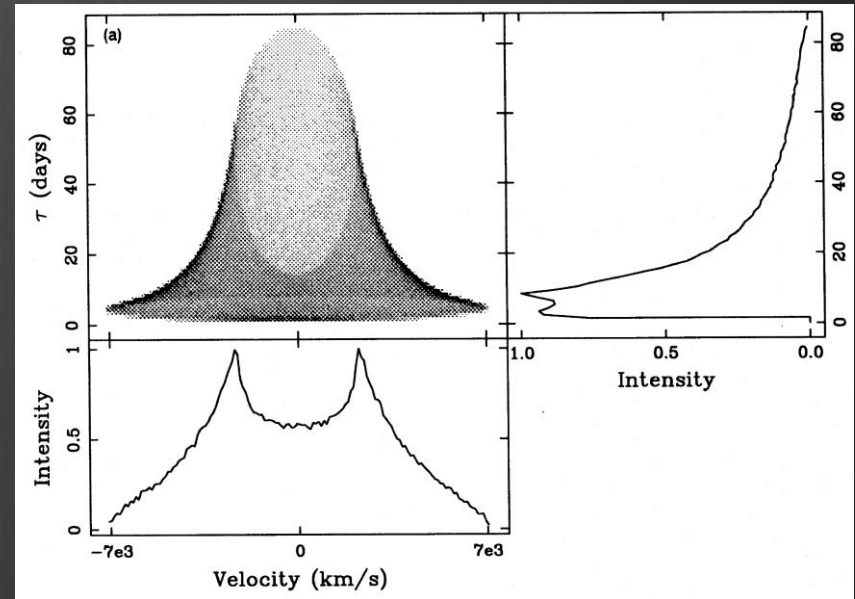
<sup>2</sup>Astrophysics, Department of Physics, Oxford University, Keble Road, Oxford OX1 3RH

<sup>3</sup>Rutherford Appleton Laboratory, Chilton, Didcot, Oxon OX11 0QX

O'Brien et al. 1994, MNRAS, 268, 845



outflow



inclined disk

# Bottorff et al. (1997): hydromagnetic wind model

## DYNAMICS OF BROAD EMISSION-LINE REGION IN NGC 5548: HYDROMAGNETIC WIND MODEL VERSUS OBSERVATIONS

MARK BOTTORFF, KIRK T. KORISTA, AND ISAAC SHLOSMAN

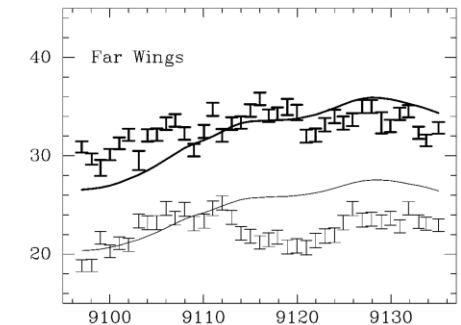
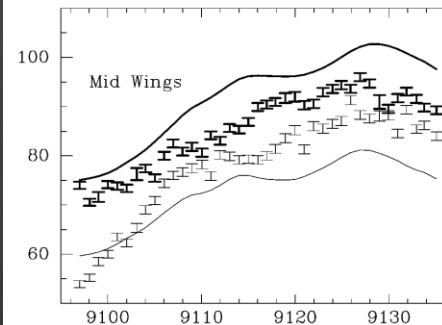
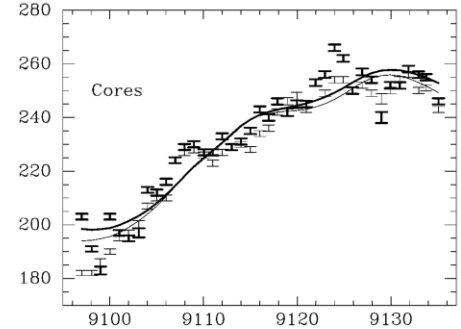
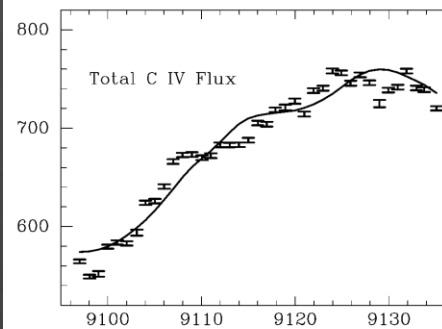
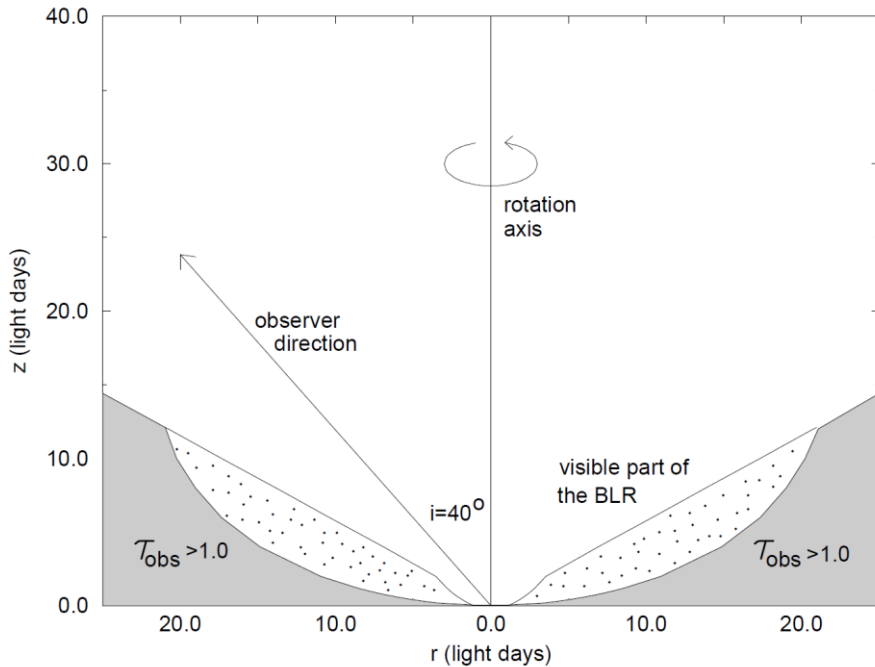
Department of Physics and Astronomy, University of Kentucky, Lexington, KY 40506-0055; bottorff@pa.uky.edu, korista@pa.uky.edu, shlosman@pa.uky.edu

AND

ROGER D. BLANDFORD

Theoretical Astrophysics 130-33, California Institute of Technology, Pasadena, CA 91125; rdb@tapir.caltech.edu

BH mass estimated:  
 $\sim 3 \times 10^7 M_{\odot}$



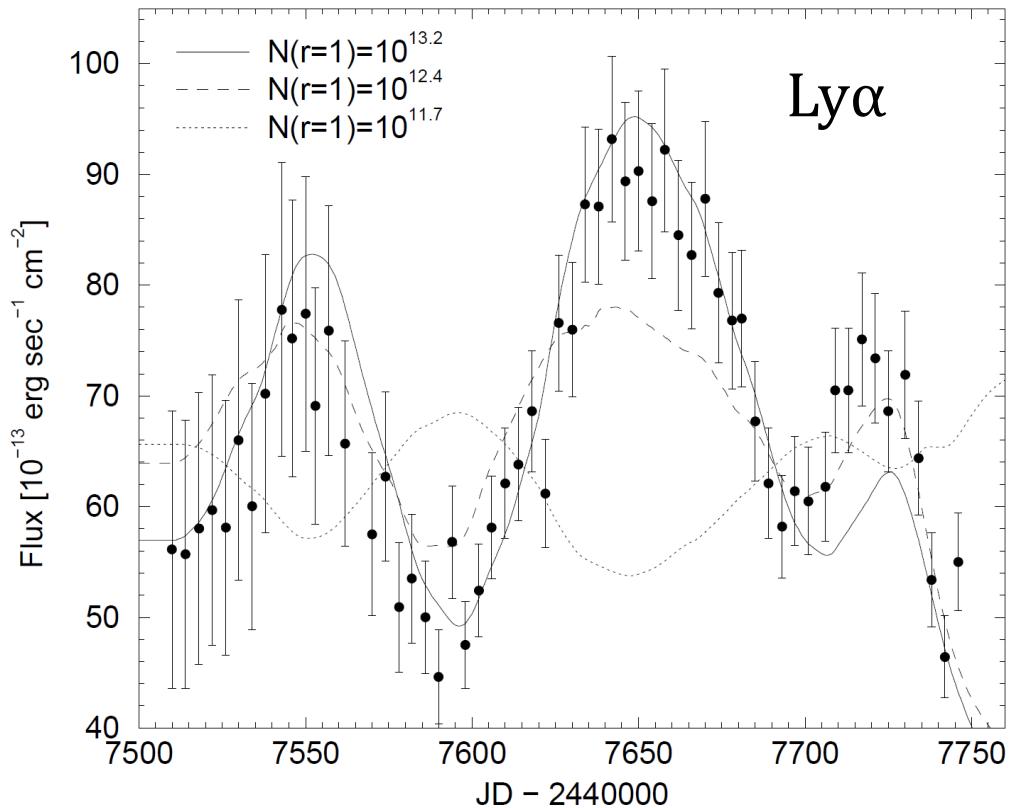


# Kaspi & Netzer (1999): spherical BLRs

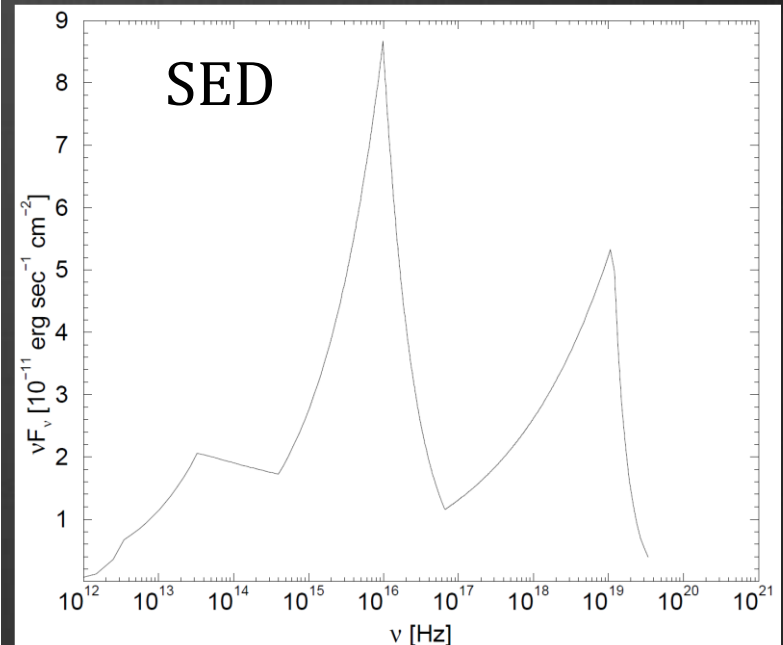
## MODELING VARIABLE EMISSION LINES IN ACTIVE GALACTIC NUCLEI: METHOD AND APPLICATION TO NGC 5548

SHAI KASPI AND HAGAI NETZER

School of Physics and Astronomy and the Wise Observatory, The Raymond and Beverly Sackler Faculty of Exact Sciences,  
Tel-Aviv University, Tel-Aviv 69978, Israel; shai@wise.tau.ac.il, netzer@wise.tau.ac.il



Photoionization included,  
but velocity-unresolved

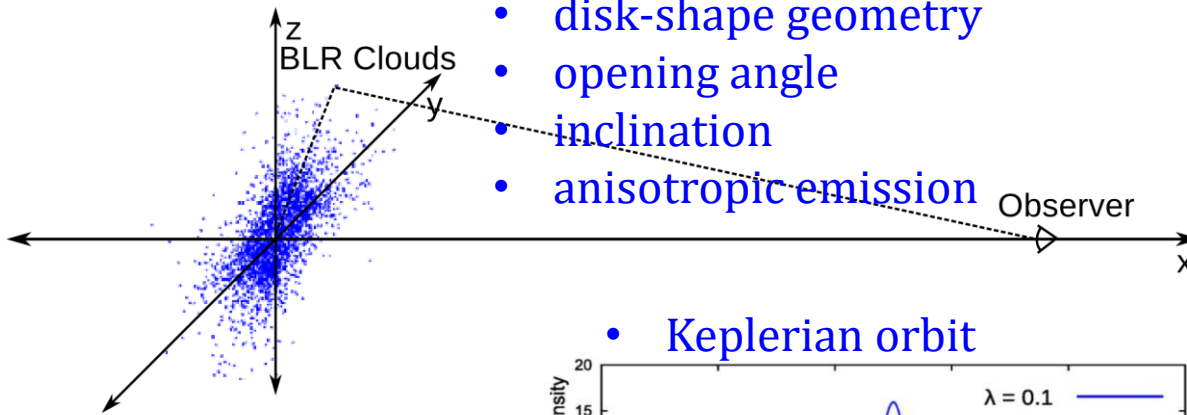


# Pancoast et al. (2011): modern version

## GEOMETRIC AND DYNAMICAL MODELS OF REVERBERATION MAPPING DATA

ANNA PANCOAST, BRENDON J. BREWER, AND TOMMASO TREU<sup>1</sup>

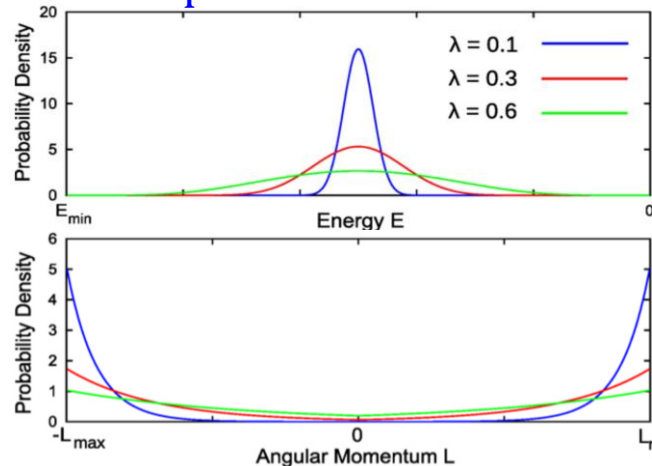
Department of Physics, University of California, Santa Barbara, CA 93106-9530, USA; [pancoast@physics.ucsb.edu](mailto:pancoast@physics.ucsb.edu)



- disk-shape geometry
- opening angle
- inclination
- anisotropic emission

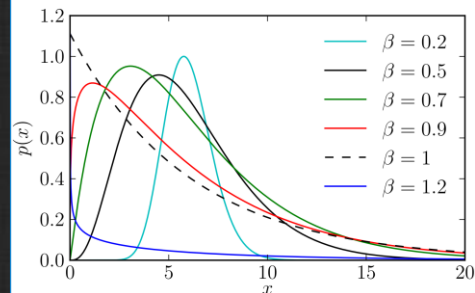
- position: Gamma distribution

- Keplerian orbit



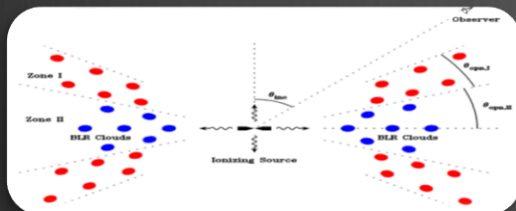
$$p(\boldsymbol{\theta} | \mathbf{D}, I) \propto p(\boldsymbol{\theta} | I) p(\mathbf{D} | \boldsymbol{\theta}, I)$$

- Bayesian inference
- Sophisticated sampling algorithm
- Fully explore parameter space

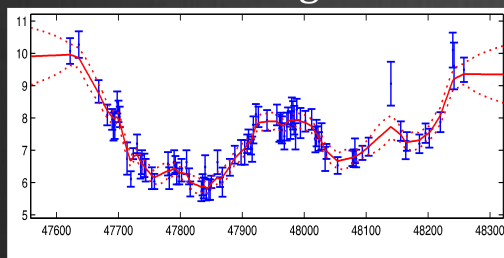


# BLR dynamical modeling: generic flowchart

BLR model

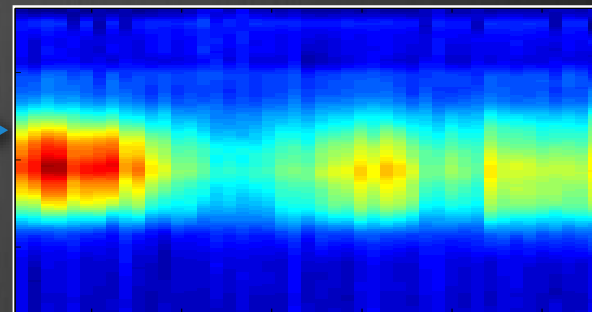


Continuum light curve

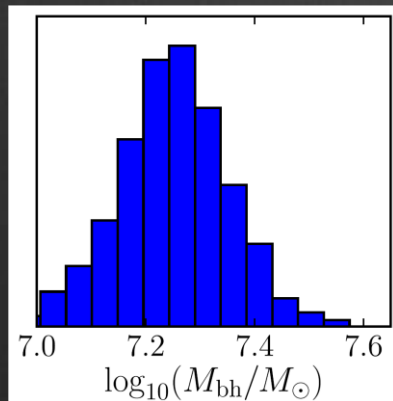


posterior probability  
Markov-Chain Monte Carlo

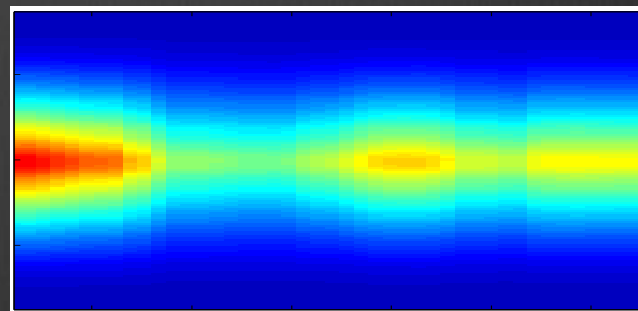
Broad-line data



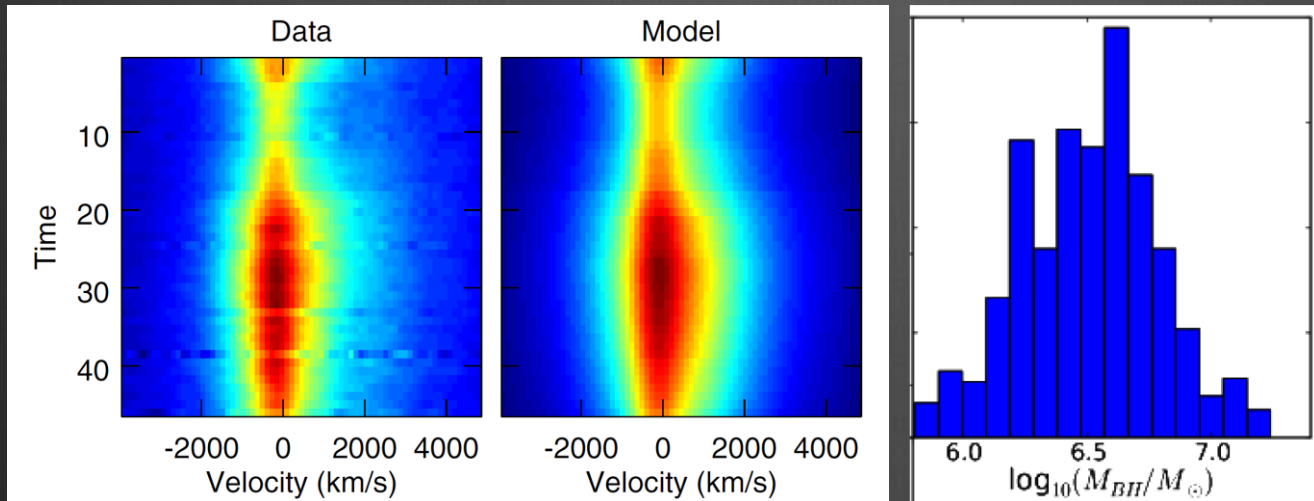
BH mass



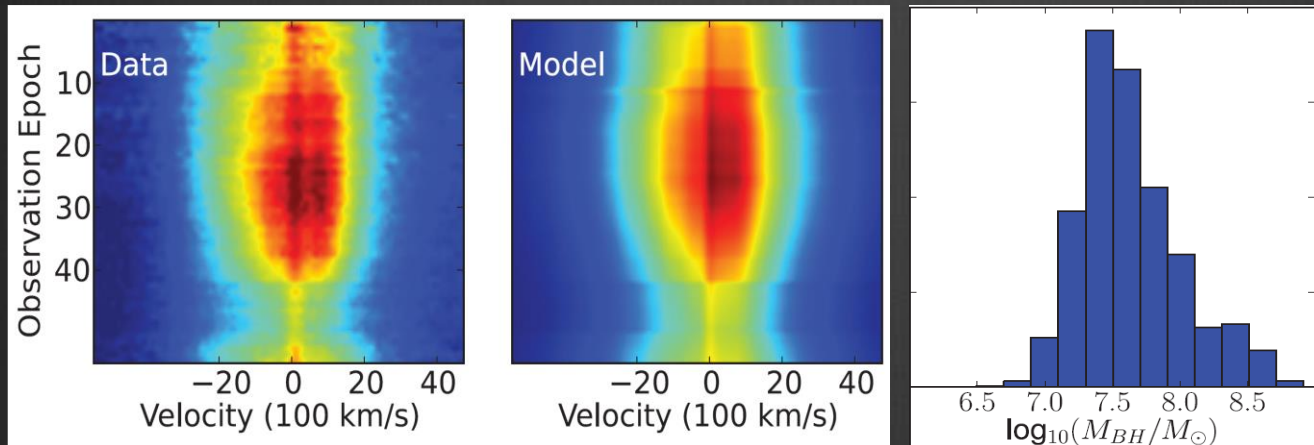
Reconstructed line



## Arp 151 (Brewer et al. 2011)



## Mrk 50 (Pancoast et al. 2012)



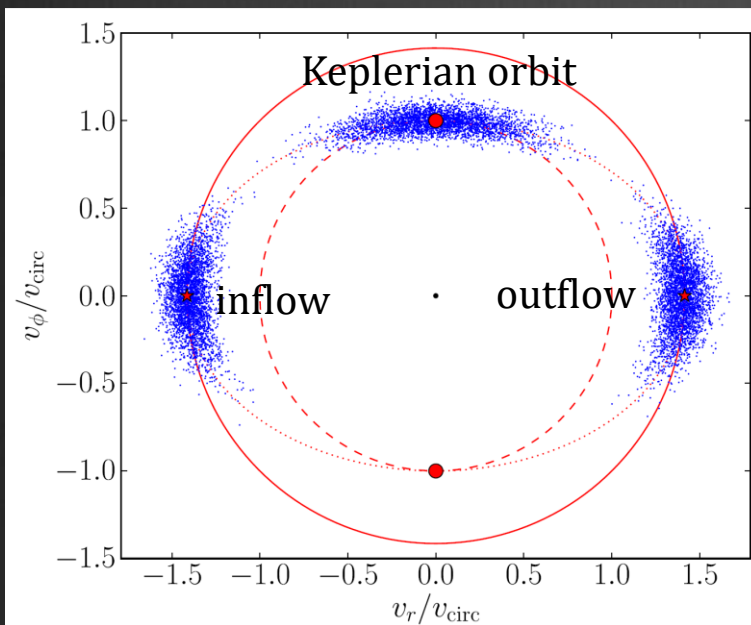
# Pancoast et al. (2014): further improvements

## Modelling reverberation mapping data – I. Improved geometric and dynamical models and comparison with cross-correlation results

Anna Pancoast,<sup>1</sup>★ Brendon J. Brewer<sup>2</sup> and Tommaso Treu<sup>1</sup>†

<sup>1</sup>Department of Physics, University of California, Santa Barbara, CA 93106, USA

<sup>2</sup>Department of Statistics, The University of Auckland, Private Bag 92019, Auckland 1142, New Zealand



velocity sampling

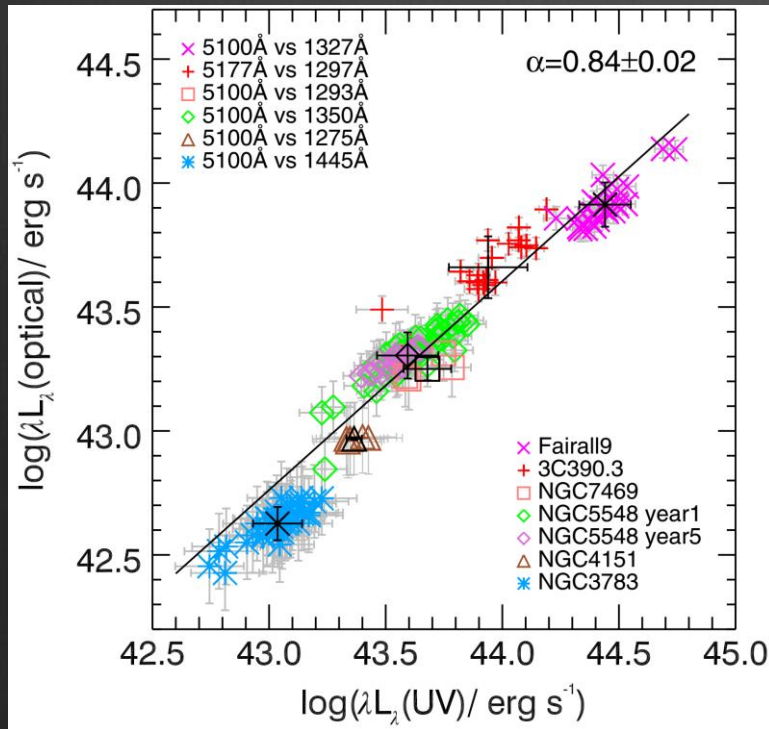
- Better velocity sampling of BLR clouds
- Inflow/outflows
- Improved anisotropic treatments

see Peter Williams' talk

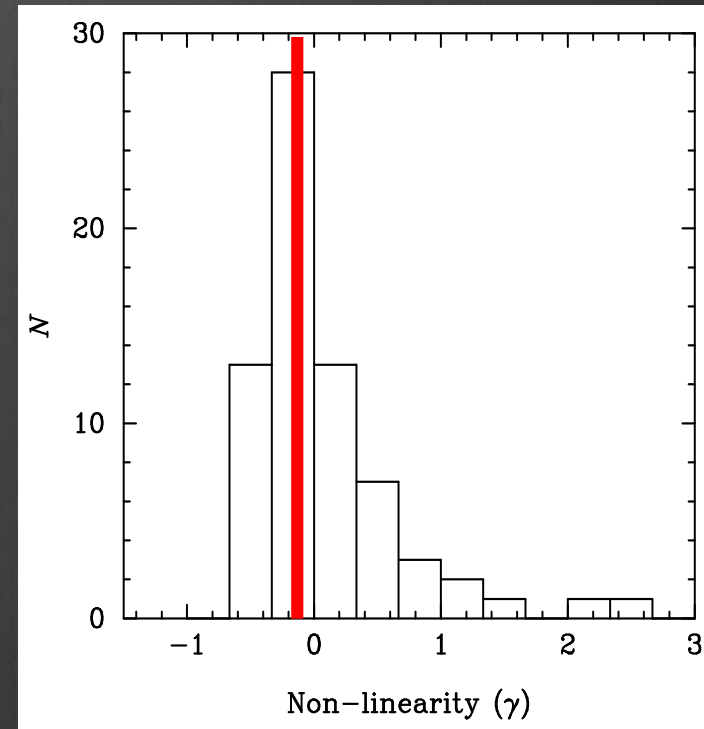
# Li et al. (2013, 2018): independent approach

Following Pancoast et al.'s work, but include two additional points:

✓ Includes non-linear response of broad lines:  $L(\nu, t) \propto C^{1+\gamma}(t - \tau)$



Kilerci Eser et al. 2015



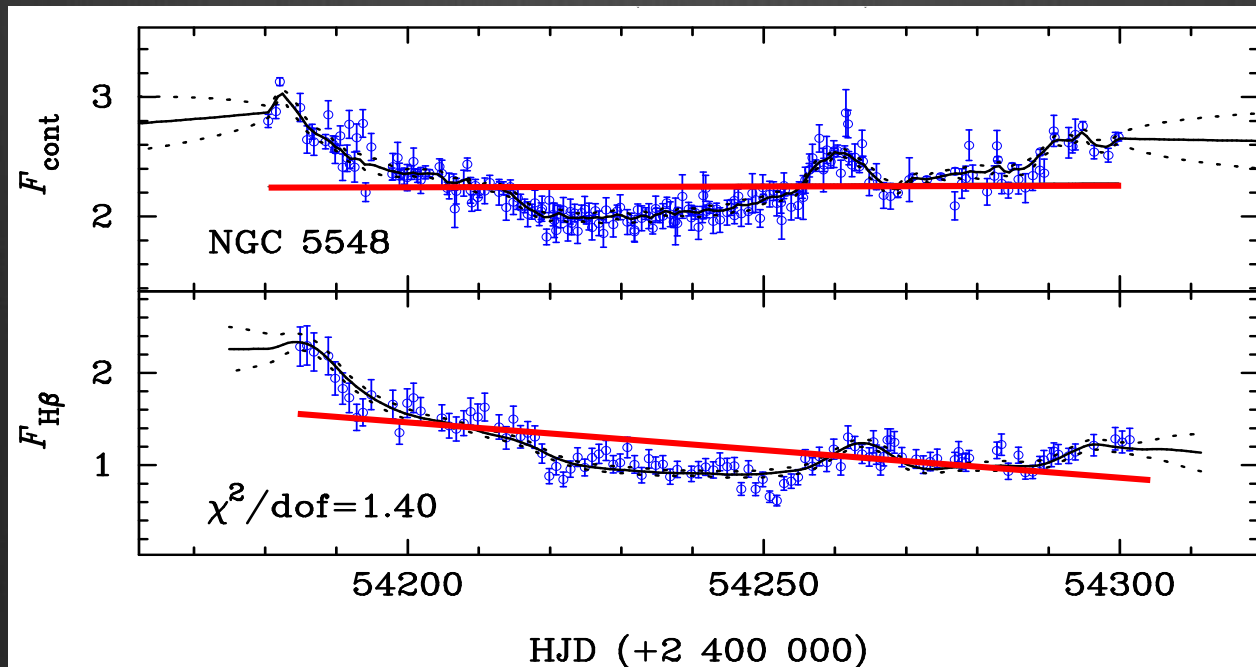
Li et al. 2013



# Li et al. (2013, 2018): independent approach

Following Pancoast et al.'s work, but include two additional points:

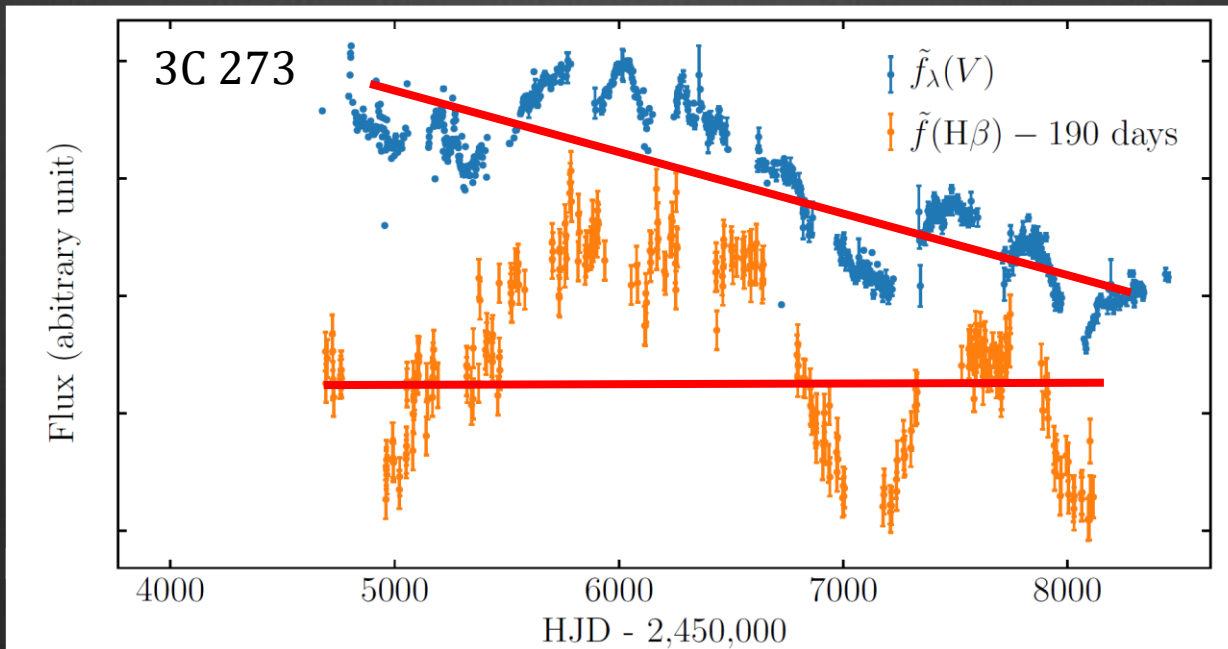
- ✓ Includes non-linear response of broad lines:  $L(\nu, t) \propto C^{1+\gamma}(t - \tau)$
- ✓ Long-term detrending



# Li et al. (2013, 2018): independent approach

Following Pancoast et al.'s work, but include two additional points:

- ✓ Includes non-linear response of broad lines:  $L(\nu, t) \propto C^{1+\gamma}(t - \tau)$
- ✓ Long-term detrending





# Software: BRAINS

## BLR Reverberation-mapping Analysis Integrated with Nested Sampling

- C Language, MPI parallel interface
- Diffusive nested sampling
- Publicly available at <https://github.com/LiyrAstroph/BRAINS>

### BRAINS

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Bayesian Reverberation-mapping Analysis Integrated with Nested Sampling

A package for dynamically modeling broad-line regions and analyzing reverberation mapping data, and measuring the black hole mass.

**References:**

- Li, Y.-R., Songshen, Y.-Y., Qiu, J., et al. 2018, ApJ, 869, 137.
- Li, Y.-R., Wang, J.-M., Ho, L. C. et al. 2013, ApJ, 779, 110.

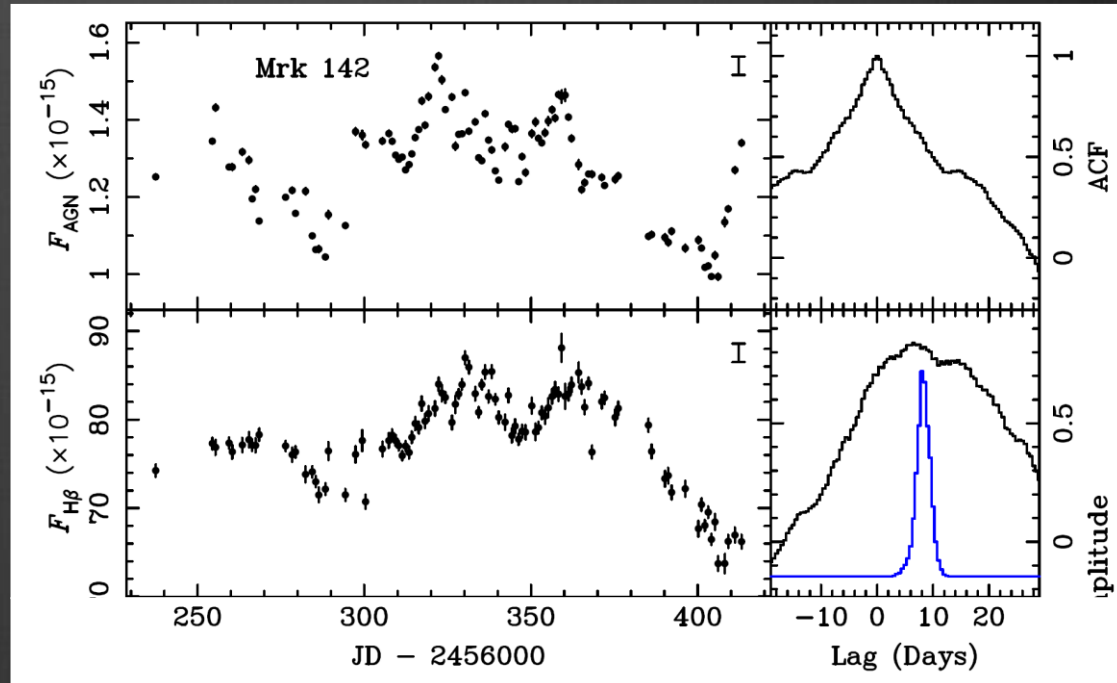
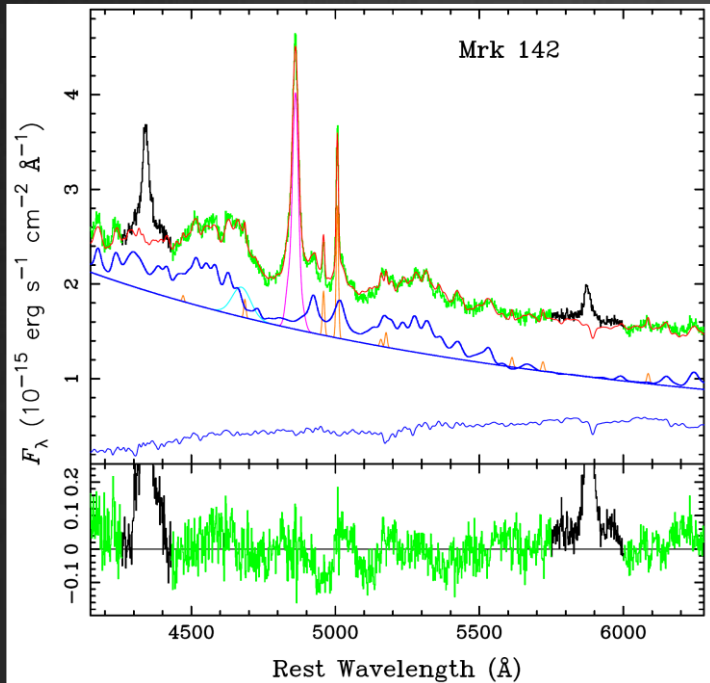
docs passing

Read [the documentation](#).

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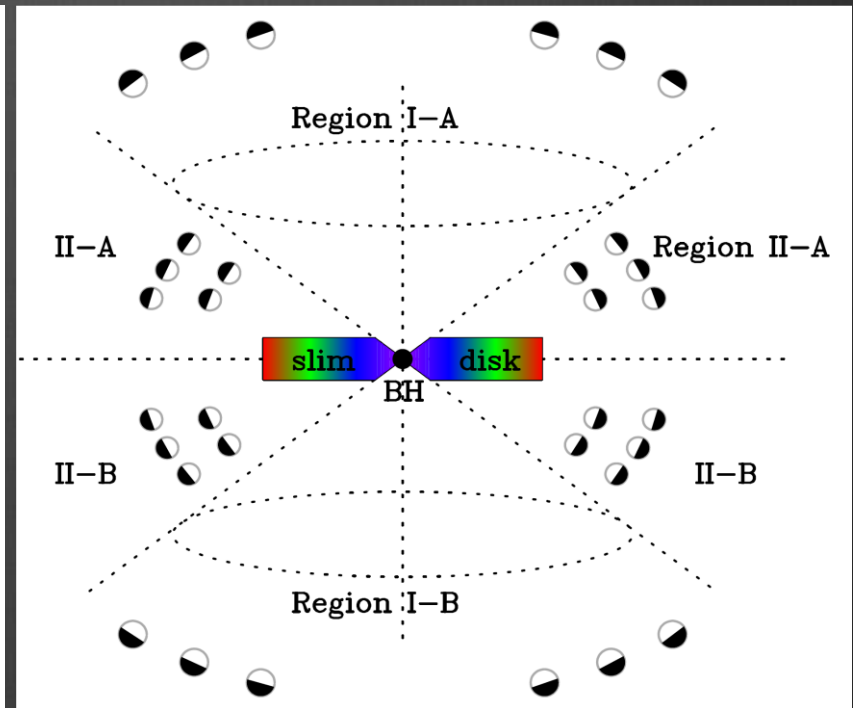
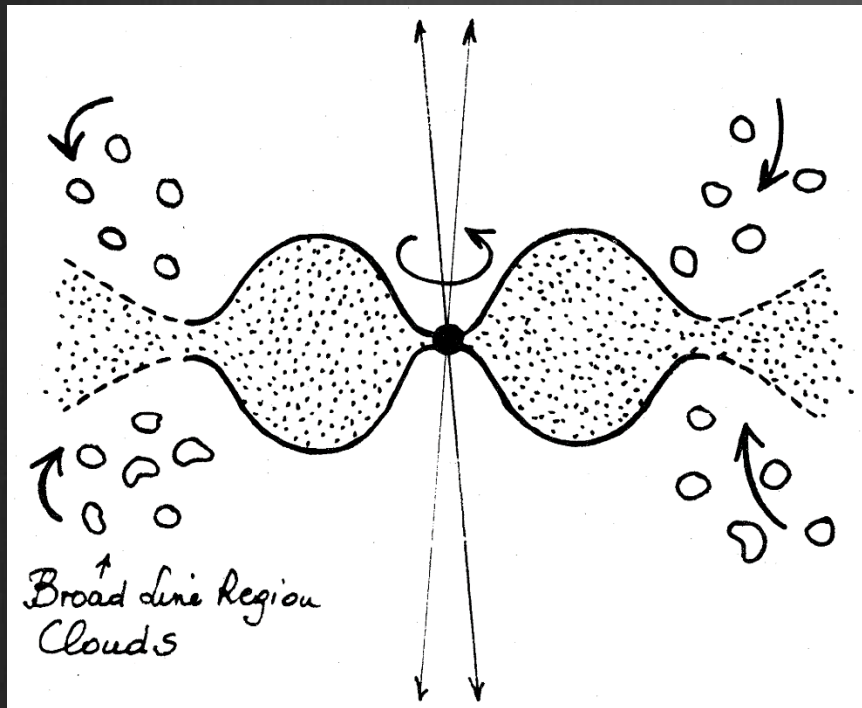
# Our application to Mrk 142

- Mrk 142 is a narrow-line Seyfert I galaxy
- Monitored by SEAMBH project (Lijiang 2.4m Telescope) between 2012-2013
- Dimensionless accretion rate  $\dot{\mathcal{M}} = \dot{M}c^2/L_{Edd} \approx 45$



# Our application to Mrk 142

- For super-Eddington accretion, self-shadowing effect is important

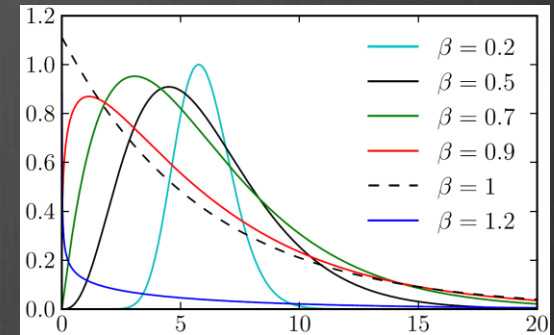
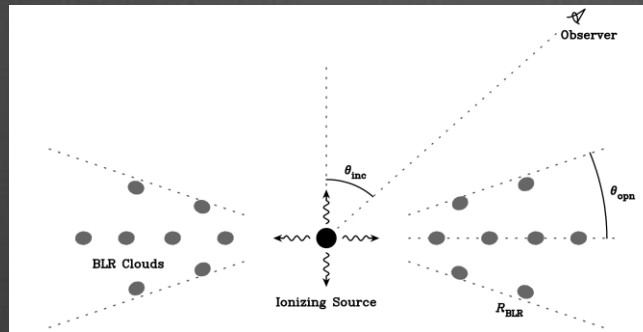


Wang et al. 2014

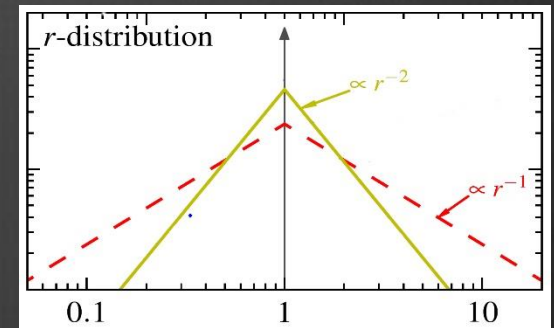
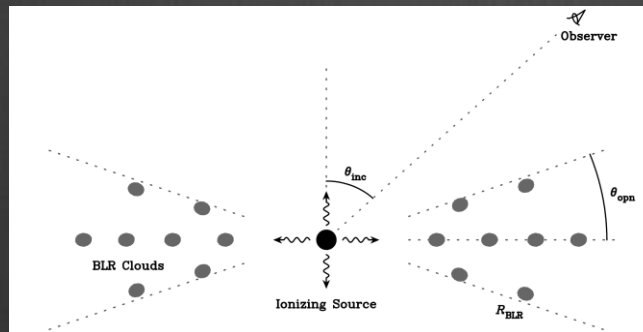
# Our application to Mrk 142

## Three models

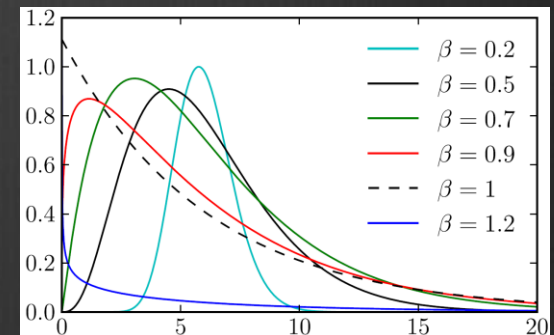
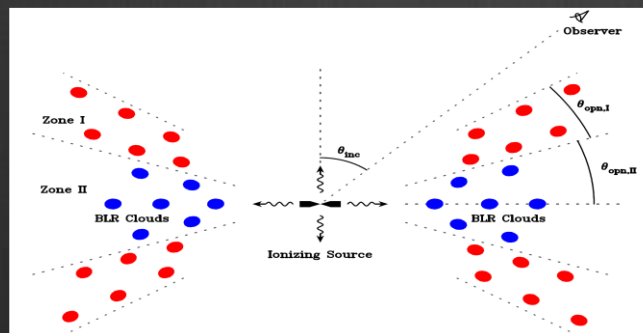
M1



M2

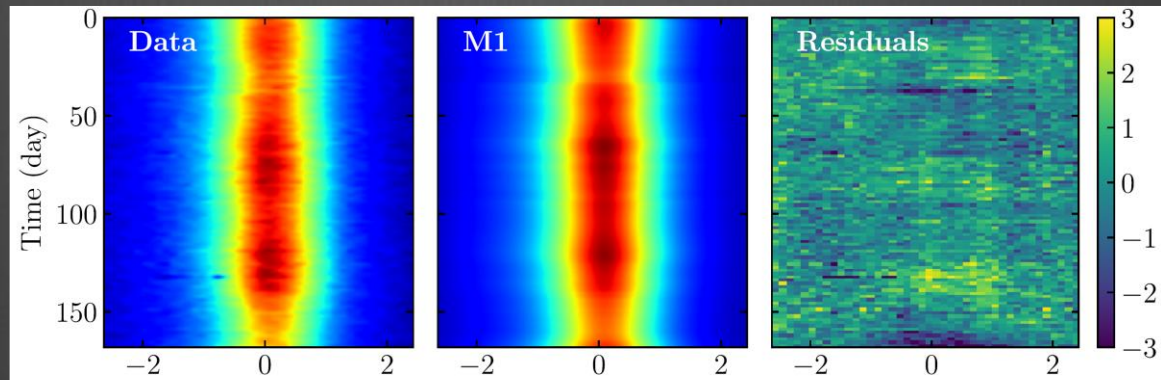


M3

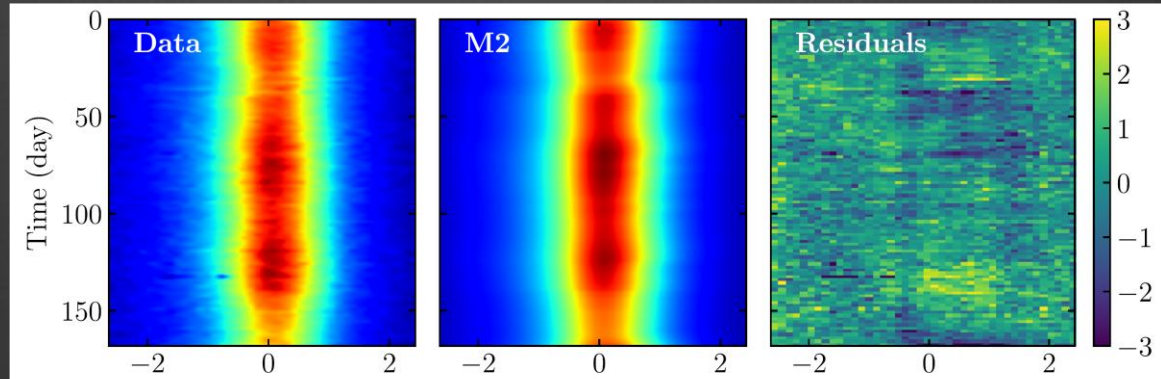


# Our application to Mrk 142

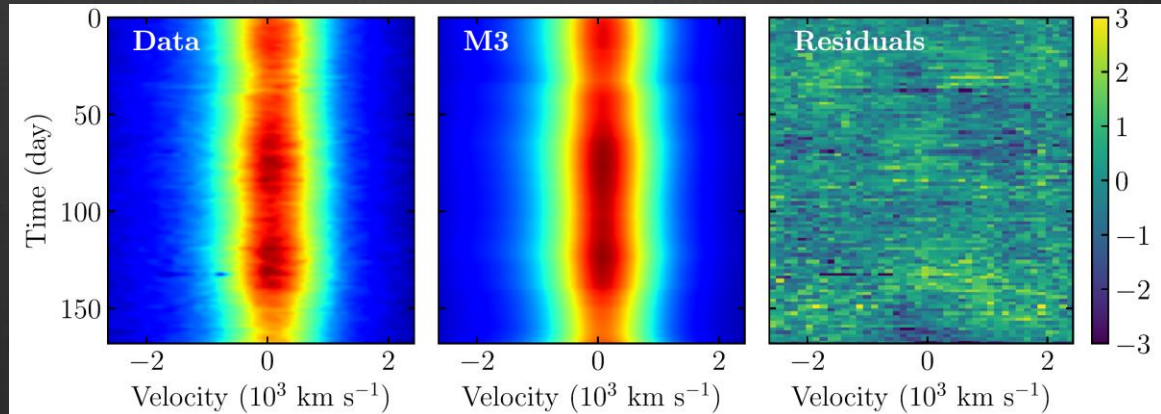
M1



M2



M3

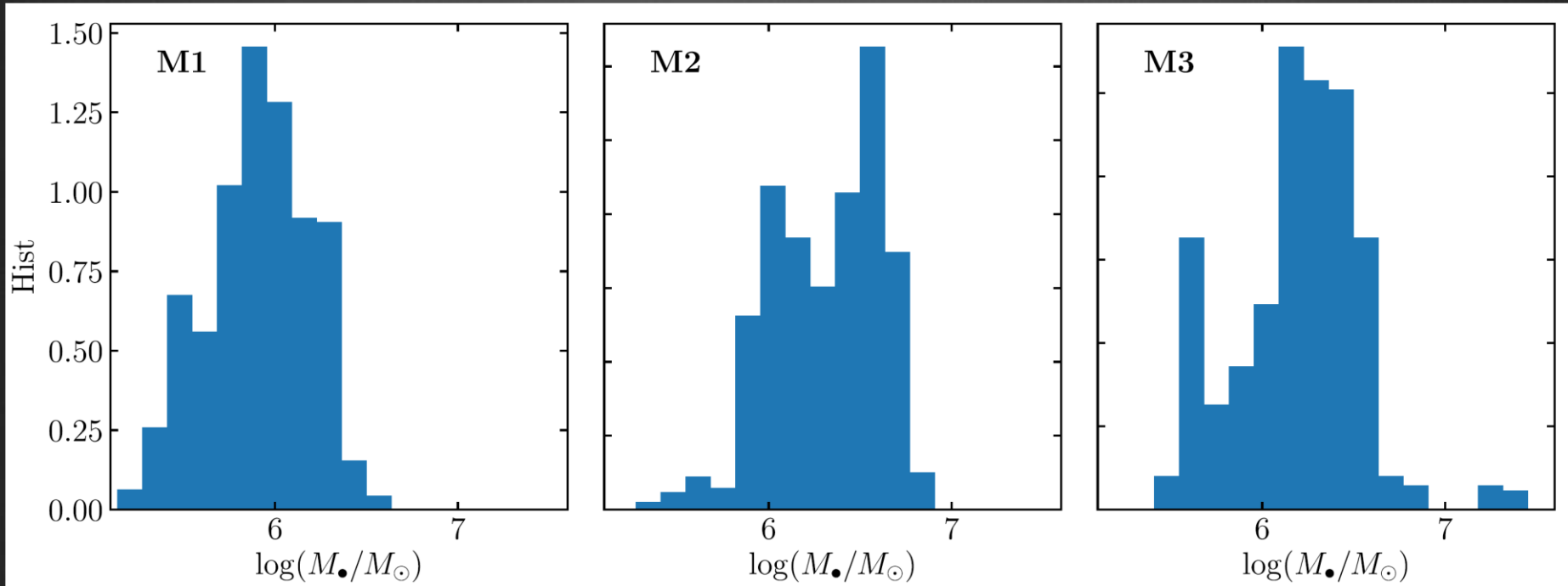


## Model comparison: M3 is the most probable

	<i>M1</i>	<i>M2</i>	<i>M3</i>
$\ln \mathcal{L}_{\max}$	0	-280	164
BIC	0	288	-105
AIC	0	562	-313
$\log K$	0	-118	68



# Our application to Mrk 142

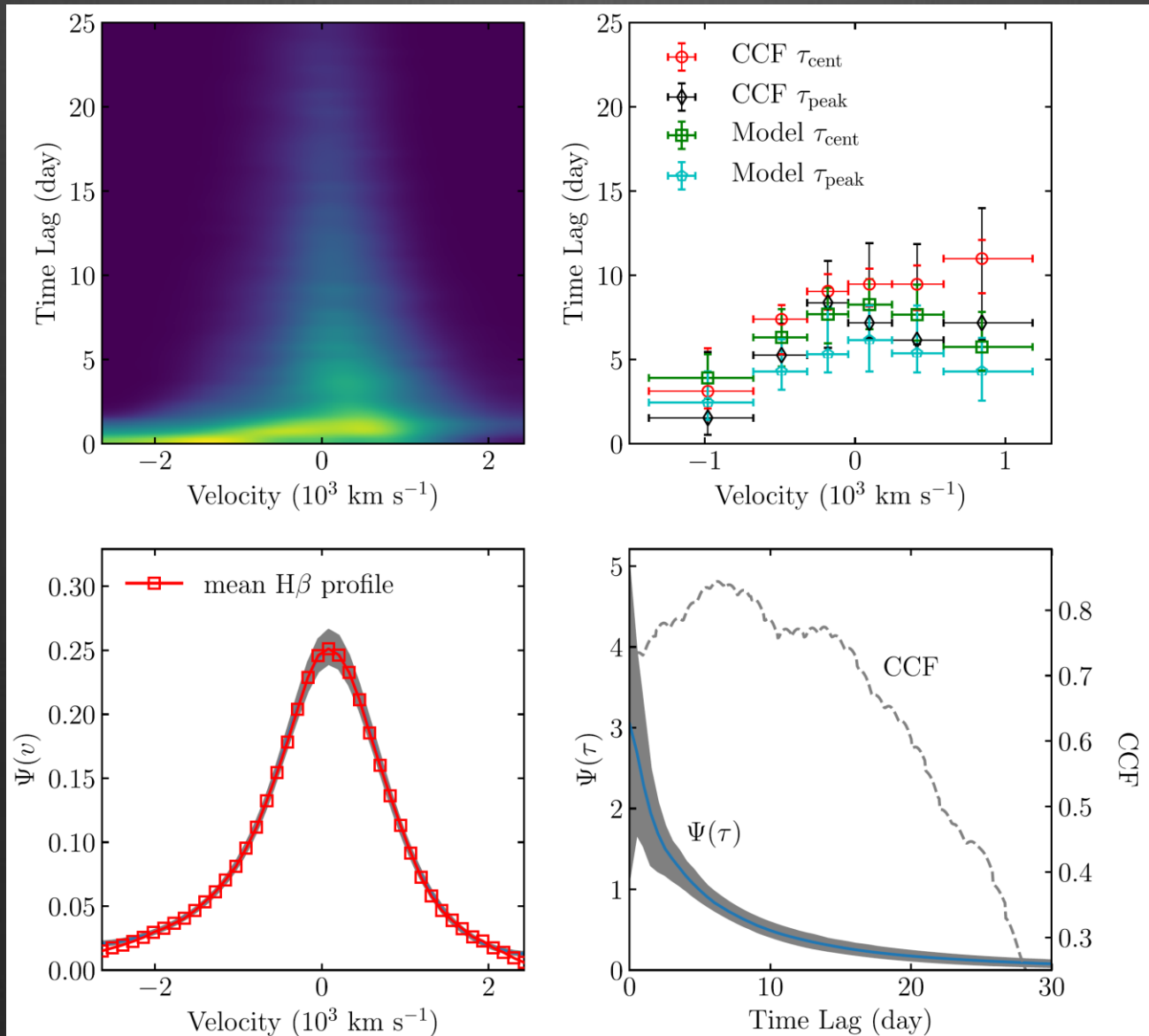


$$\log(M_{\bullet}/M_{\odot}) = 6.23^{+0.26}_{-0.45}$$

$$\log f = -0.36^{+0.33}_{-0.54}$$

FWHM of the mean spectrum  
Consistent with the calibration of  
Ho & Kim 2014 for pseudo-bulges

# Our application to Mrk 142

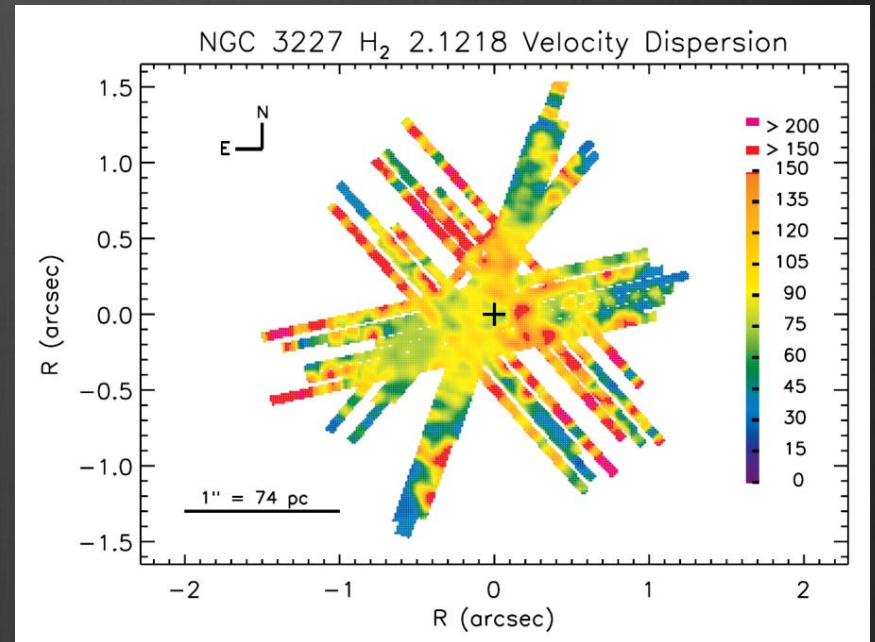
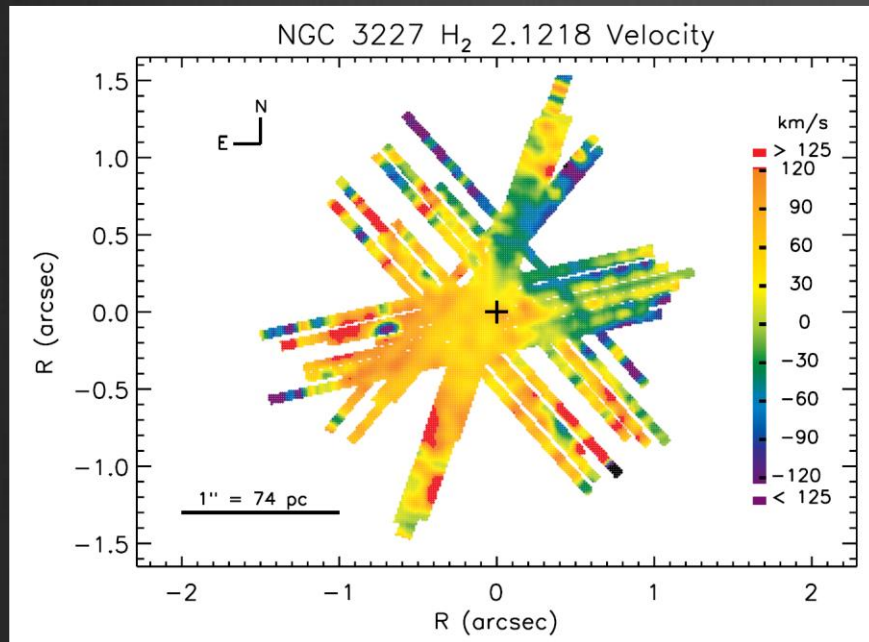




# Our application to NGC 3227

CIRCUMNUCLEAR GAS IN SEYFERT 1 GALAXIES: MORPHOLOGY, KINEMATICS,  
AND DIRECT MEASUREMENT OF BLACK HOLE MASSES

ERIN K. S. HICKS<sup>1,2</sup> AND MATTHEW A. MALKAN<sup>1</sup>

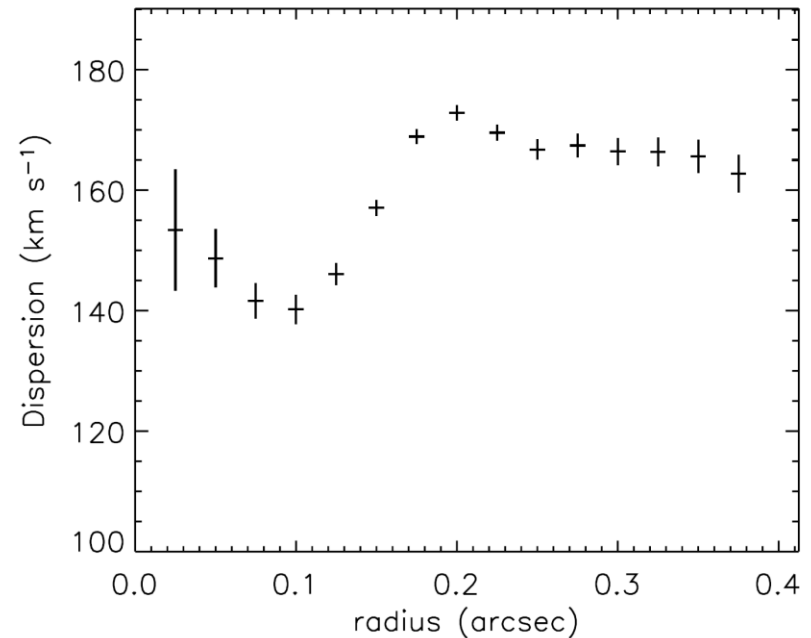
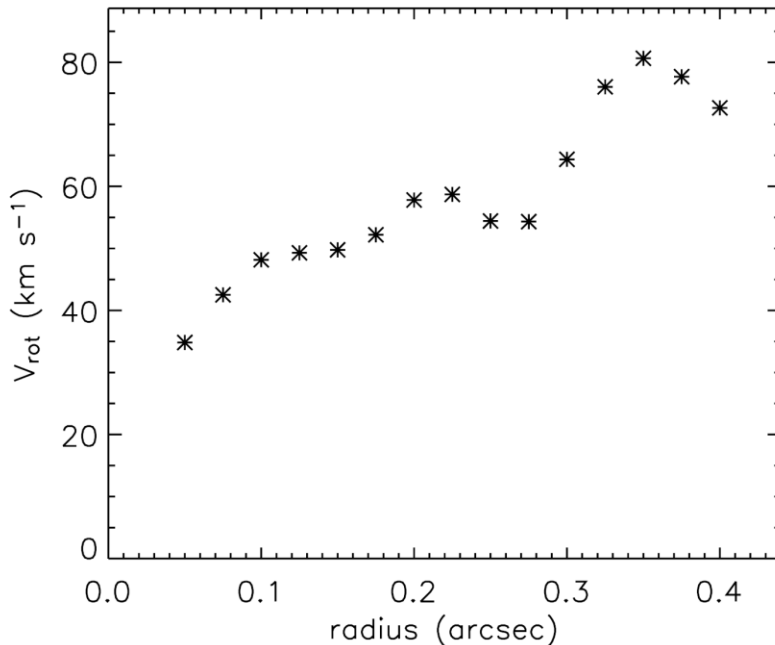


gas dynamics yields:  $M_{\bullet} = 2.0^{+1.0}_{-0.4} \times 10^7 M_{\odot}$

# Our application to NGC 3227

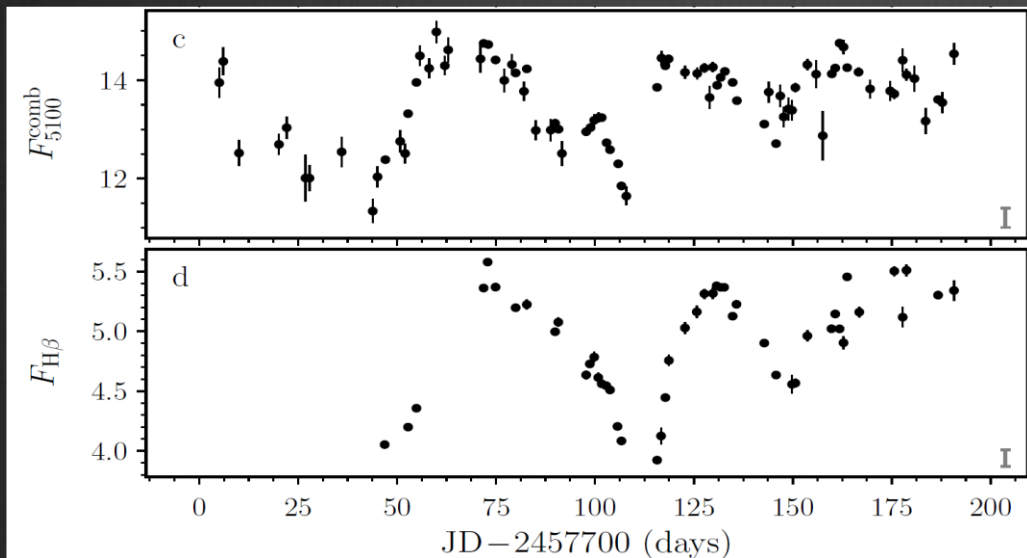
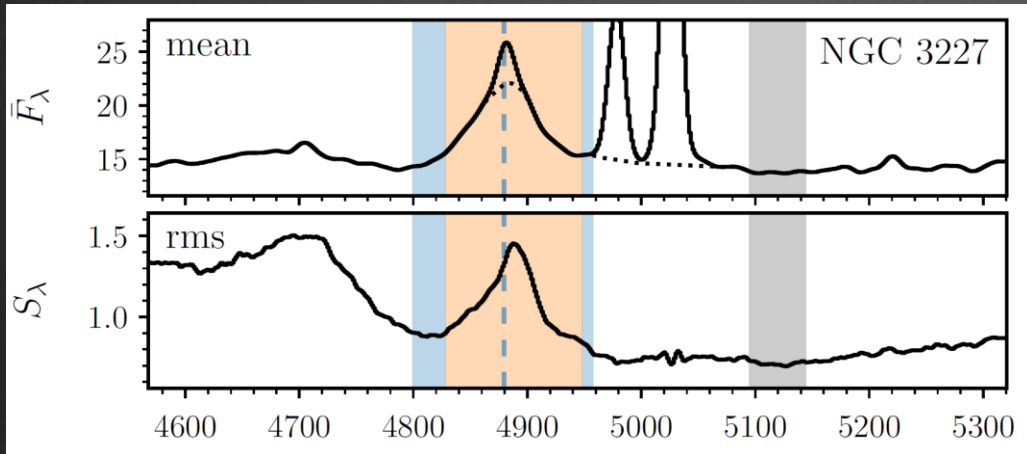
## THE STAR-FORMING TORUS AND STELLAR DYNAMICAL BLACK HOLE MASS IN THE SEYFERT 1 NUCLEUS OF NGC 3227<sup>1</sup>

R. I. DAVIES,<sup>2</sup> J. THOMAS,<sup>2,3</sup> R. GENZEL,<sup>2,4</sup> F. MUELLER SÁNCHEZ,<sup>2</sup> L. J. TACCONI,<sup>2</sup> A. STERNBERG,<sup>5</sup>  
F. EISENHAUER,<sup>2</sup> R. ABUTER,<sup>2</sup> R. SAGLIA,<sup>2,3</sup> AND R. BENDER<sup>2,3</sup>



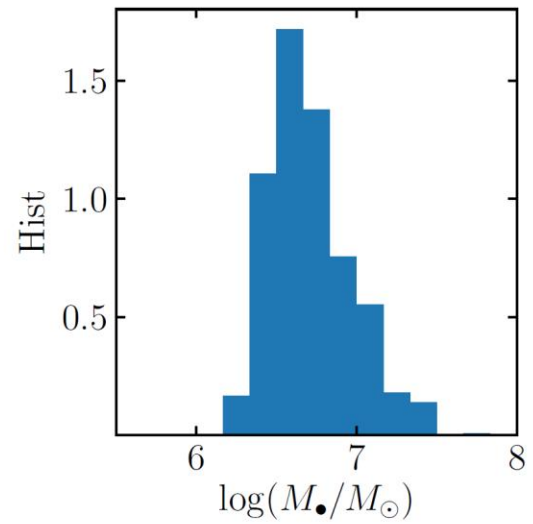
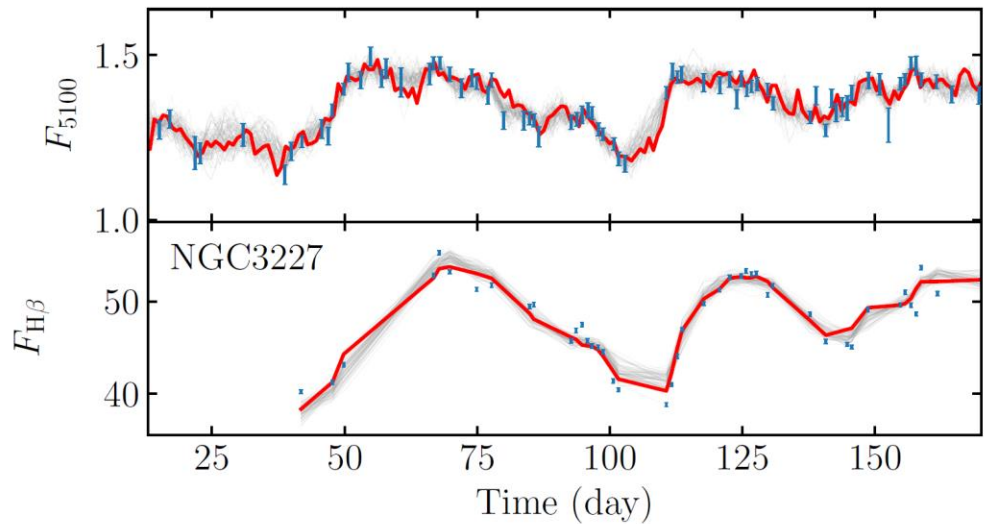
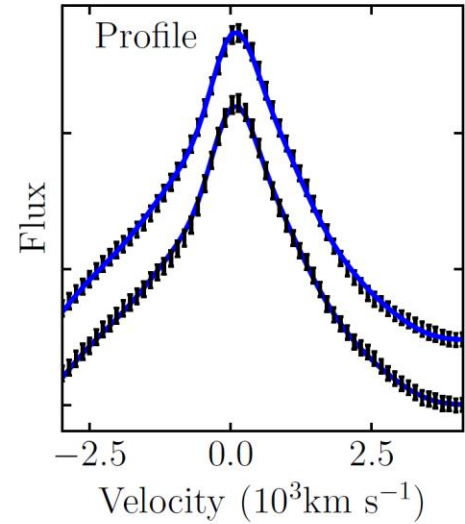
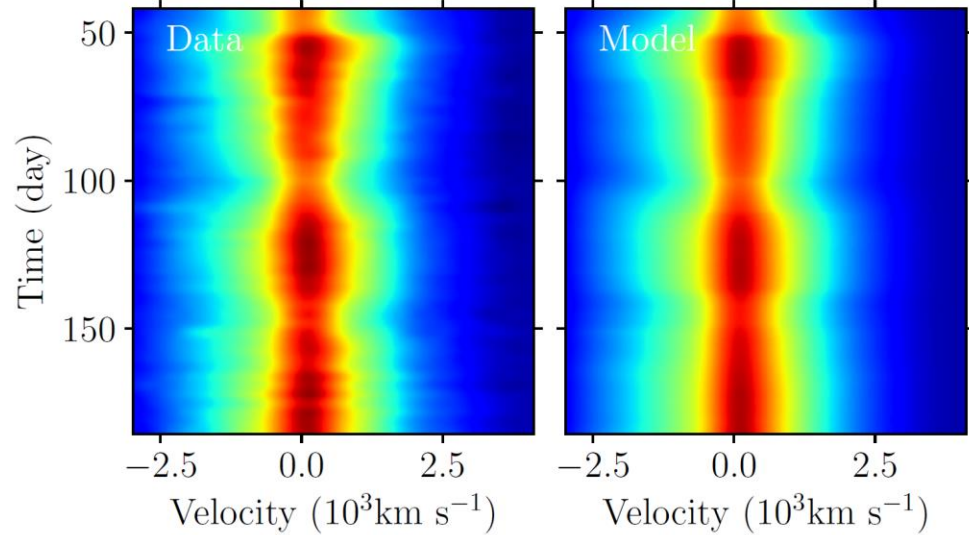
stellar dynamics yields:  $M_{\bullet} = (7 \times 10^6 - 2 \times 10^7) M_{\odot}$

# Our application to NGC 3227

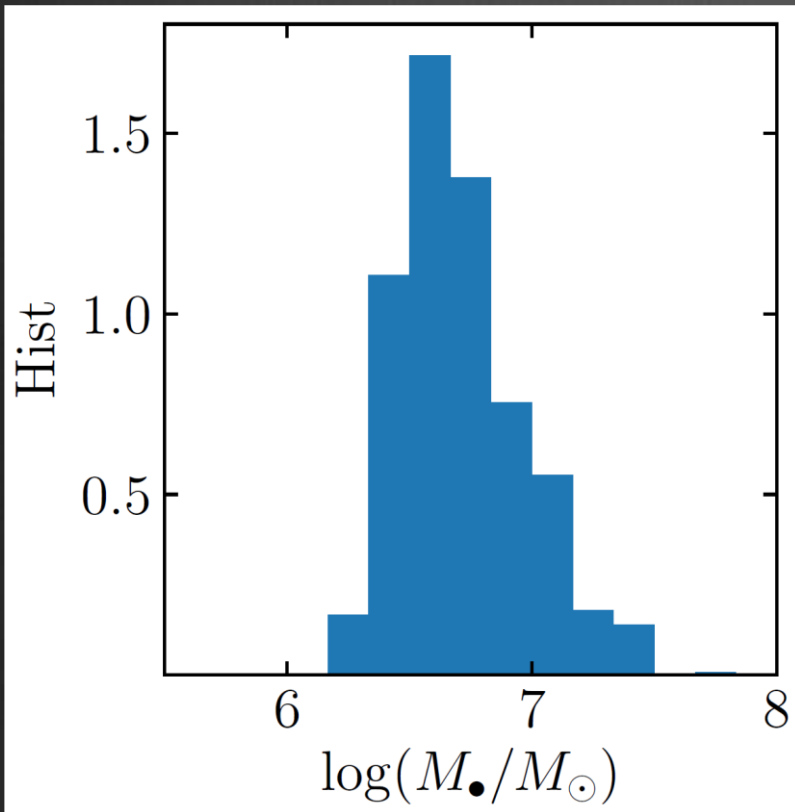


- monitored by MAHA project (WIRO 2.3m telescope) between 2016-2017
- see Mike Brotherton's talk and Jacob McLane's talk

# Our application to NGC 3227



# Our application to NGC 3227



Method	BH Mass ( $10^6 M_{\odot}$ )
Gas dynamics	$20^{+10}_{-4}$
Stellar dynamics	7-20
BLR dynamical modeling	$5.2^{+4.5}_{-2.2}$

## Future improvements

- Systematic errors of BLR dynamical modeling  
comparison with other independent methods
  - ✓ Stellar/gas dynamics (NGC 3227, NGC 4151)
  - ✓ Spectro-interferometry (3C 273)

see Yuyang Songsheng's talk
- Compare with other BLR models (e.g, disk wind)
- Include photoionization processes

# Summary

- We developed BLR dynamical code “BRAINS”, publicly available at <https://github.com/LiyraAstroph/BRAINS>
- Application to Mrk 142 shows a two-zone BLR
- Application to NGC 3227 shows a consistent BH mass measurement with other independent methods

**Thank You**