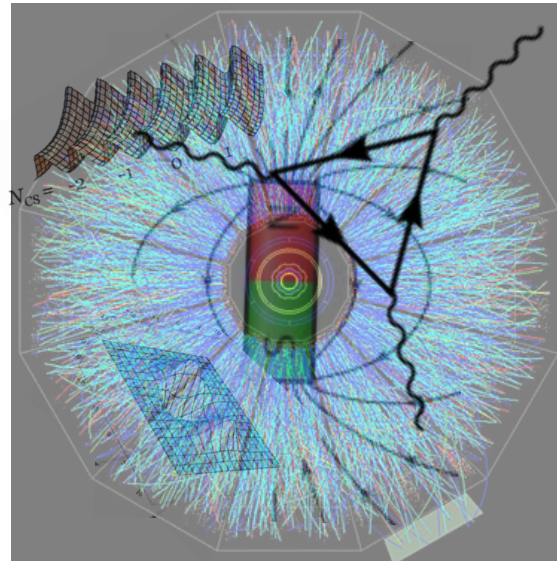


# Vorticity and Magnetic Fields in Collisions at BES/FAIR/NICA Energies



**Jinfeng Liao**



**BEST**  
COLLABORATION

# Outline

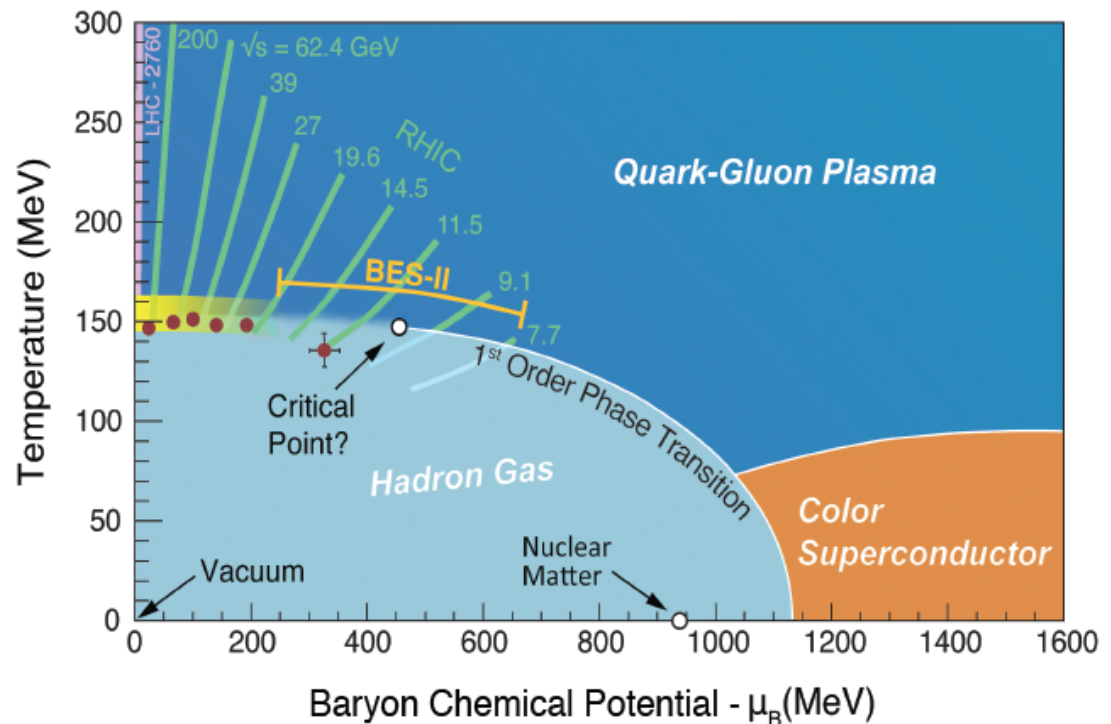
- *Brief Introduction*
- *Vorticity and Spin Polarization*
- *Magnetic Field at Low Collision Energy*
- *Discussions & Outlook*

# INT Program 2020

## *Chirality and Criticality: Novel Phenomena in Heavy Ion Collisions*

*May 11 — June 5, 2020*

*Organizers: J. Liao, M. Stephanov, H.-U. Yee, Z. Xu*



# An Upcoming Review

## Mapping the Phases of Quantum Chromodynamics with Beam Energy Scan

Adam Bzdak<sup>a</sup>, Shin'ichi Esumi<sup>b</sup>, Volker Koch<sup>c</sup>, Jinfeng Liao<sup>d,f</sup>, Mikail Stephanov<sup>e</sup>, Nu Xu<sup>f,c</sup>

<sup>a</sup>AGH University of Science and Technology, Faculty of Physics and Applied Computer Science, 30-059 Krakow, Poland

<sup>b</sup>Tomonaga Center for the History of the Universe, University of Tsukuba, Tsukuba, Ibaraki 305, Japan

<sup>c</sup>Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

<sup>d</sup>Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

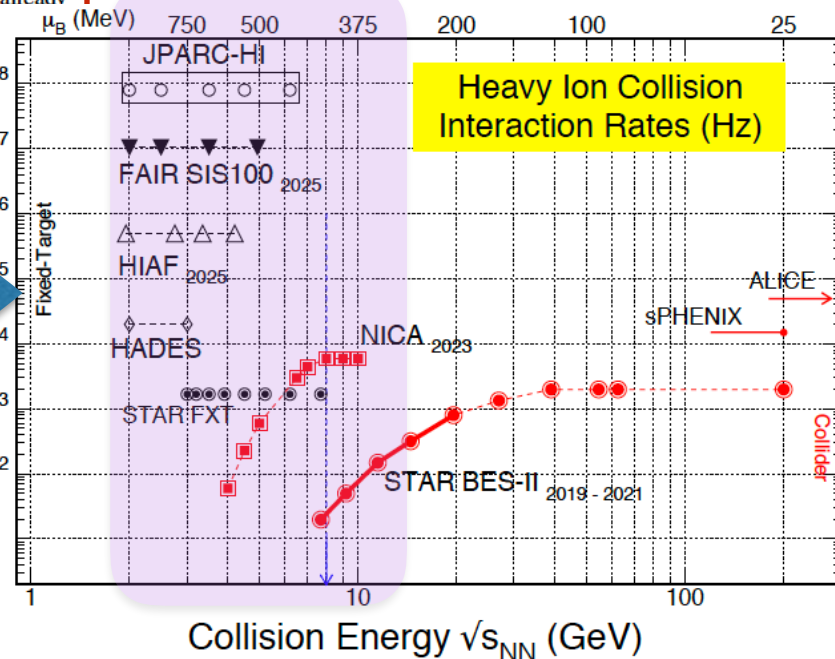
<sup>e</sup>Physics Department, University of Illinois at Chicago, W. Taylor St., Chicago IL 60607-7059, USA

<sup>f</sup>Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan, 430079, China

### Abstract

We review the present status of the search for a QCD phase transition and critical point, as well as anomalous transport phenomena with an emphasis on the Beam Energy Scan program at the relativistic heavy ion collider at Brookhaven National Laboratory. We present the conceptual framework and discuss the observables deemed most sensitive to a phase transition, QCD critical point, and anomalous transport focusing on fluctuation and correlation measurements. The presently available experimental results for these observables together with those characterizing the global properties of the systems created in heavy ion collisions will be presented. We will then discuss what can be already learned from the presently available data about the QCD critical point and anomalous transport and what measurements and theoretical developments are needed in order to discover these phenomena.

**Future of nuclear collisions:  
high baryon density region!**



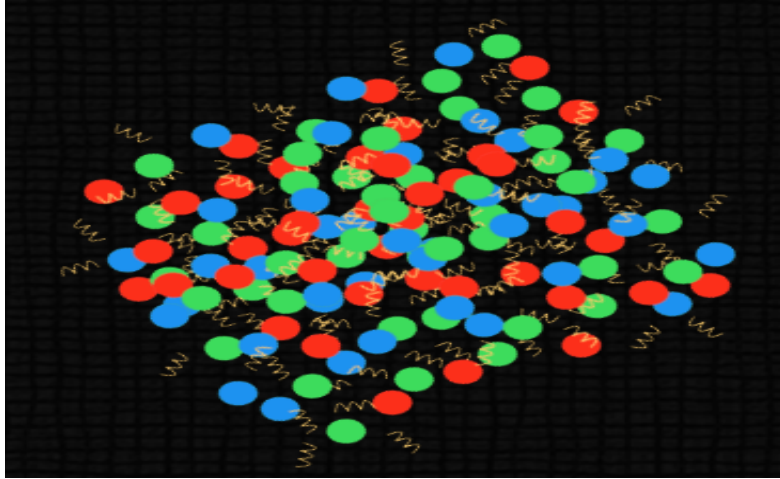
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# Introduction

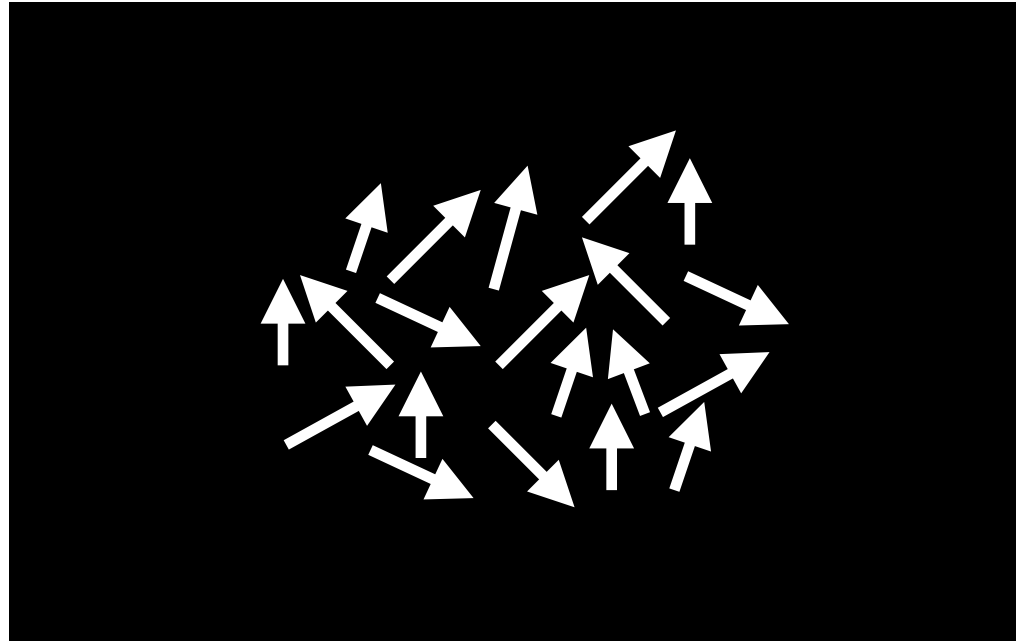
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# A Fluid of Spin

*A nearly perfect fluid*

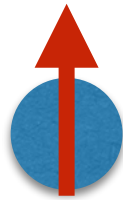


*What happens to the spin  
DoF in the fluid???*

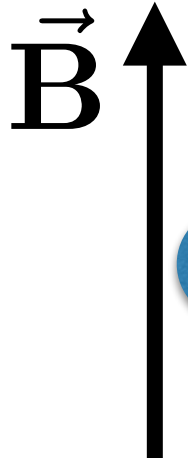


# Manipulating the Spin

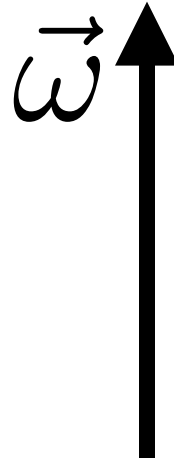
*SPIN  
UP*



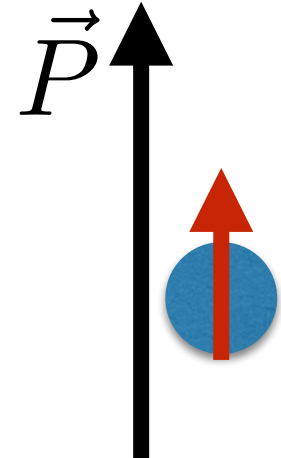
*SPIN  
DOWN*



**Magnetic  
Polarization**



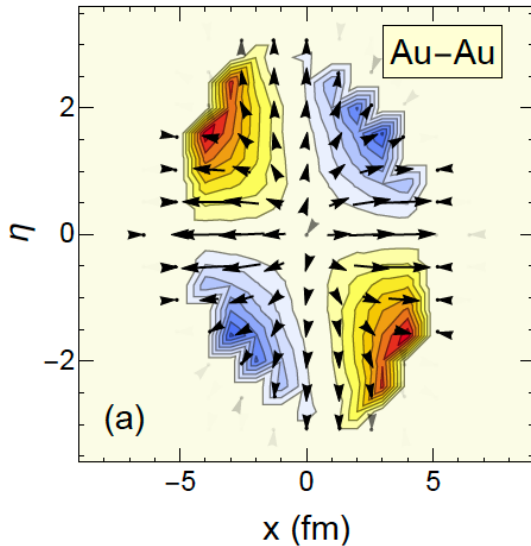
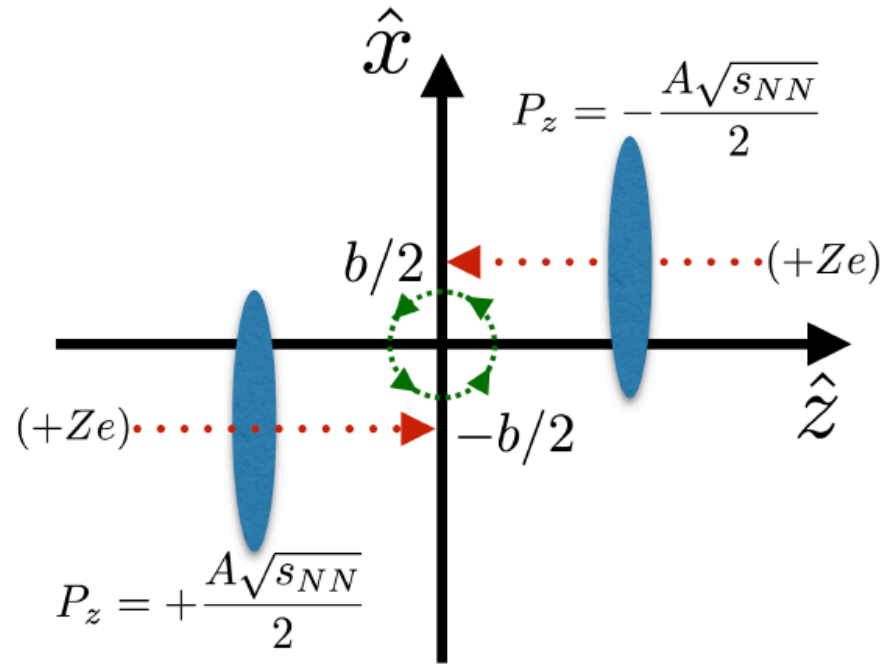
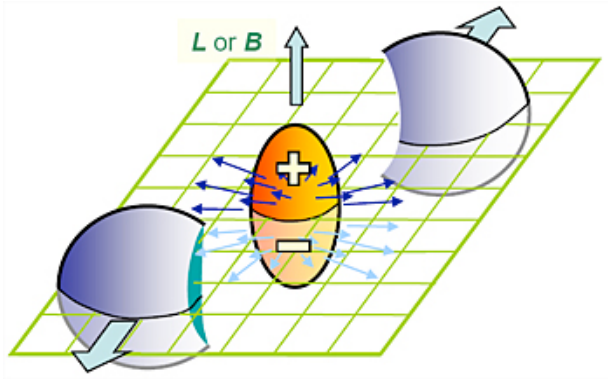
**Rotational  
Polarization**



**Chirality  
Polarization**

Interesting interplay  $\rightarrow$  highly nontrivial phenomena!

# Extreme Vorticity & EM Fields

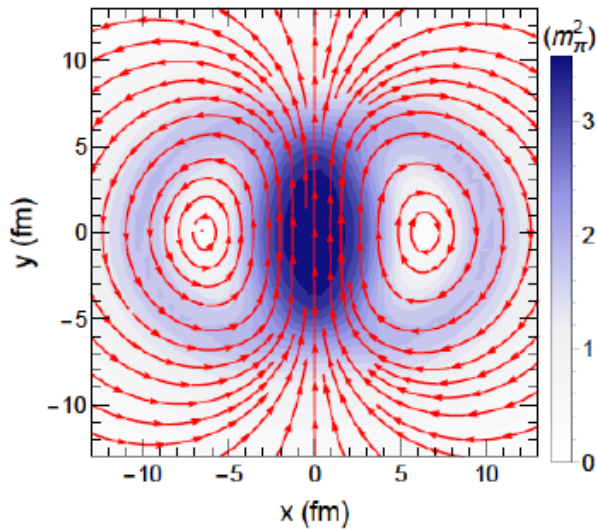
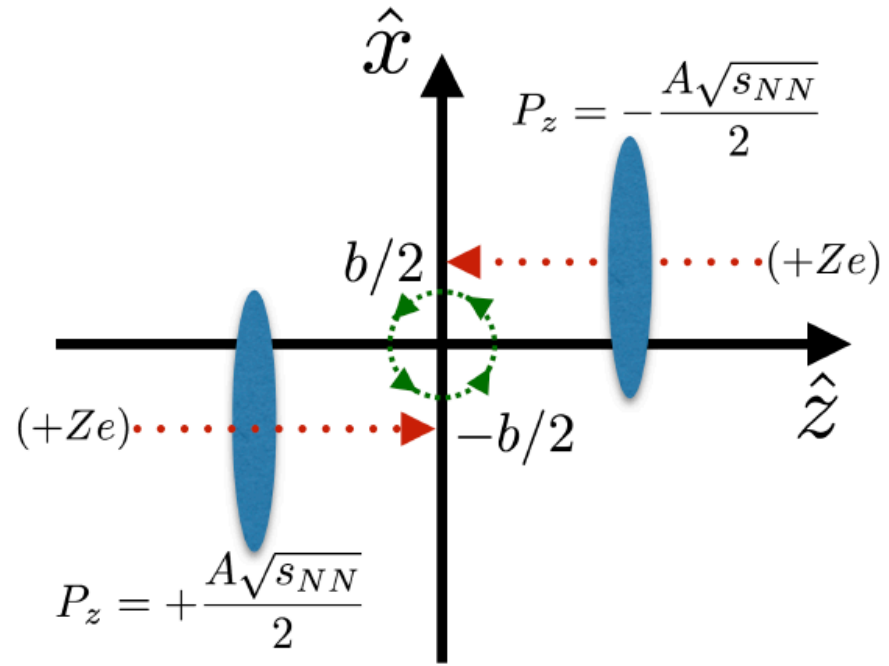
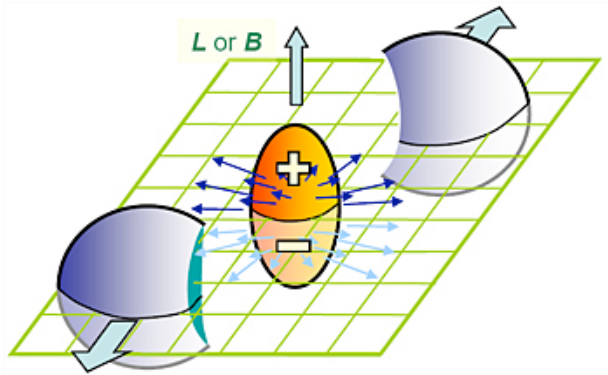


$$L_y = \frac{Ab\sqrt{s}}{2} \sim 10^{4\sim 5} \hbar$$

**Large angular momentum  $\rightarrow$  the most vortical fluid**



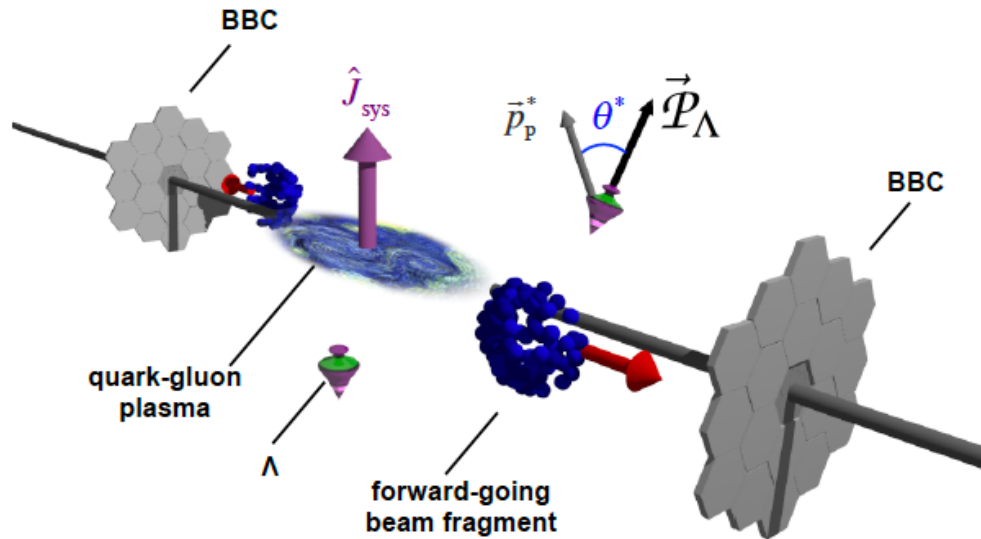
# Extreme Vorticity & EM Fields



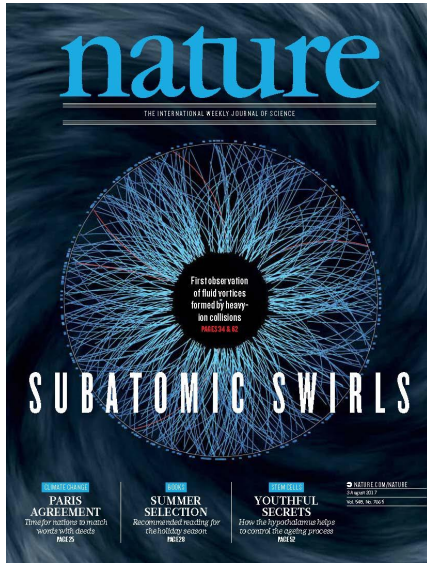
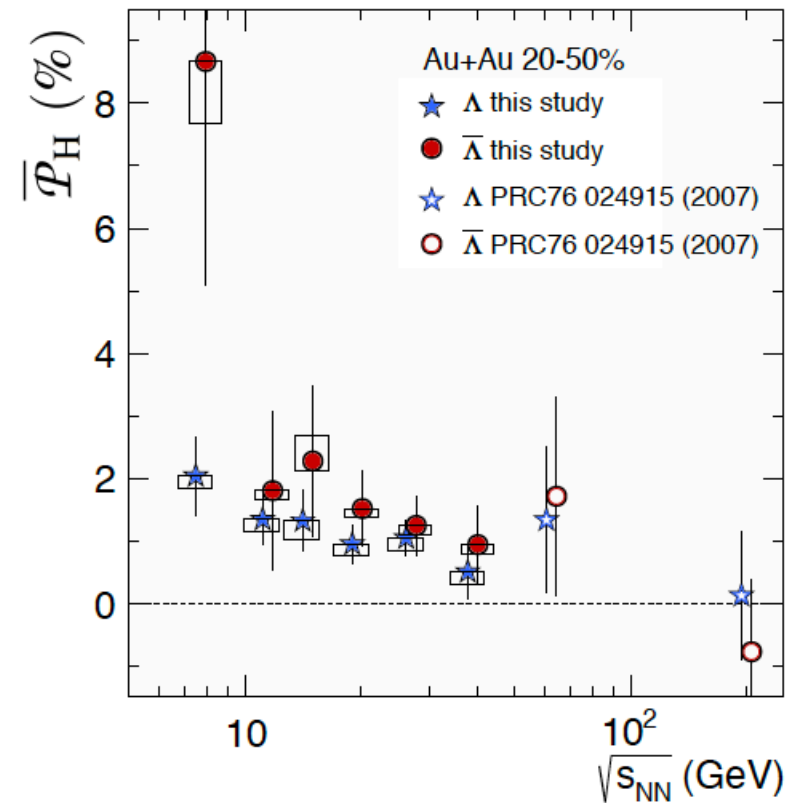
$$E, B \sim \gamma \frac{Z\alpha_{EM}}{R_A^2} \sim 3m_\pi^2$$

**The angular momentum together with large (+Ze) nuclear charge  
 → the strongest magnetic field!**

# Novel Phenomena: “Fluid Spintronics”

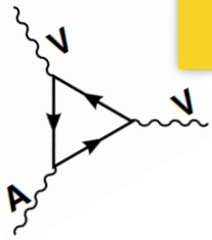


## Rotation-induced Spin Polarization

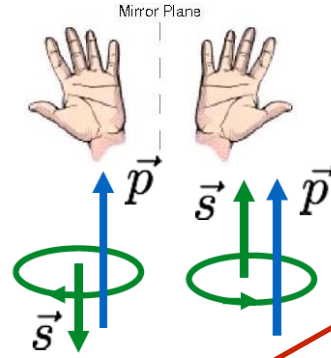


STAR Collaboration, Nature 2017

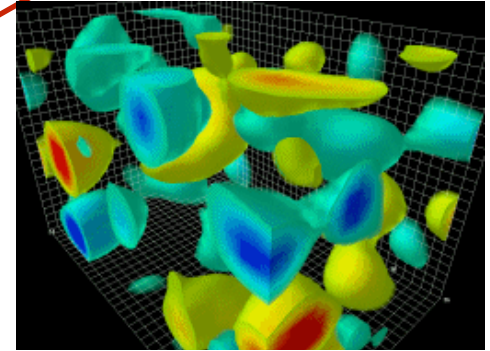
# Chiral Magnetic Effect (CME)



Chirality & Anomaly



Chirality & Topology



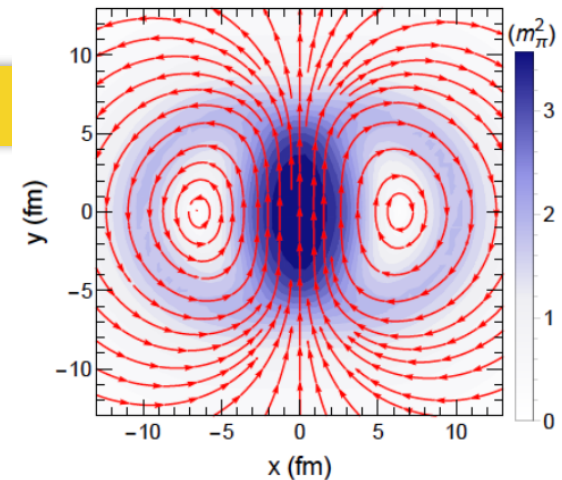
$$N_R - N_L = N_5 = 2Q_w$$

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

Anomalous Electric Current

Magnetic Field

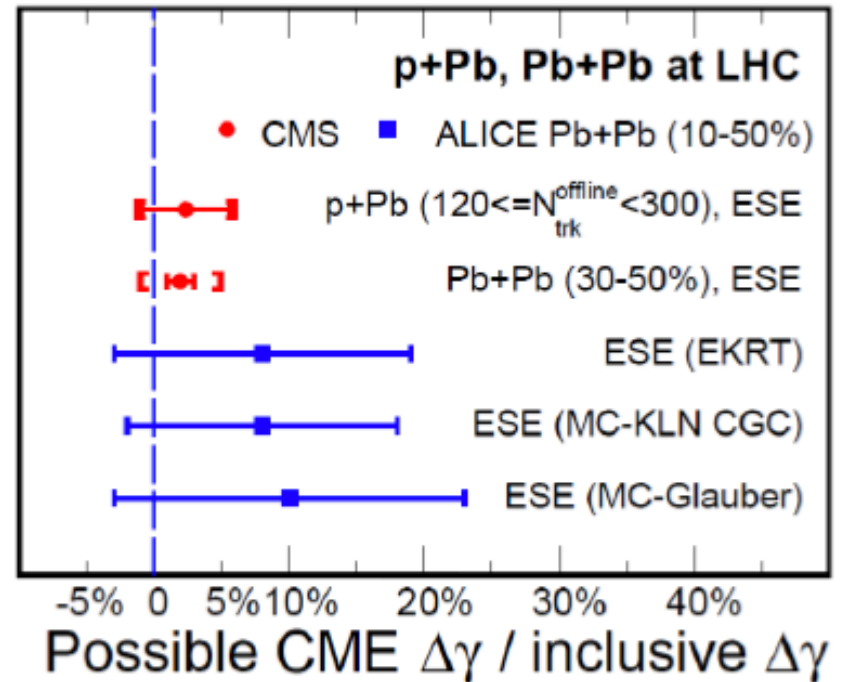
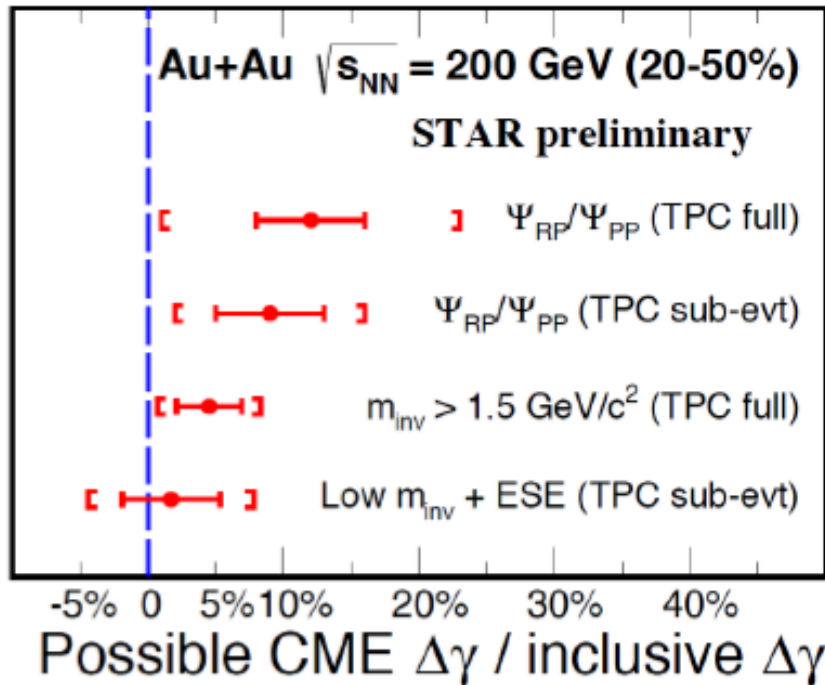
Q.M. Transport



***CME  $\leftrightarrow$  macroscopic chiral anomaly***  
***CME: a new type of (quantum) electricity***

# Exp. Search for CME

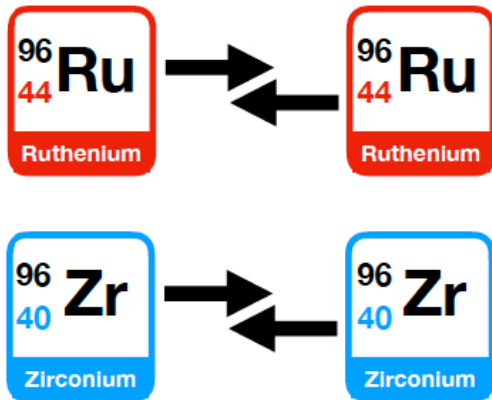
**Most measurements based on:  
gamma correlator + certain procedure to fight backgrounds**



**Slide from Fuqiang Wang @ Chirality 2019**

# Isobaric Collisions @ RHIC

*New opportunity of potential discovery: Isobaric Collision @ RHIC*



***Charge Asymmetry  
Correlation Measurement***

Background

Signal

**RuRu**

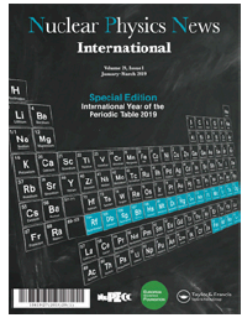
Background

Signal

**ZrZr**

*~2 billion data collected successfully in RHIC 2018 run;  
processing and analysis underway!*

# Real Near-Term Opportunity: Isobaric Collisions



Nuclear Physics News



ISSN: 1061-9127 (Print) 1931-7336 (Online) Journal homepage: <https://www.tandfonline.com/loi/gnpn20>

feature article

## Isobar Collisions at RHIC to Test Local Parity Violation in Strong Interactions

D. E. KHARZEEV<sup>1,2</sup> AND J. LIAO<sup>3</sup>

versus the background level (horizontal axis). One expects that a  $5\sigma$  observation of the local parity violation will be possible if the background contributes less than two thirds of the measured correlation.

This decisive experiment for the search of CME had just begun in the spring 2018 RHIC run. If a conclusive observation of CME is achieved, it would amount to the experimental discovery of the restoration of chiral symmetry in hot QCD matter and to the first direct experimental observation of the topological fluctuations in QCD. We will be holding our breath awaiting the outcome of this groundbreaking experiment.



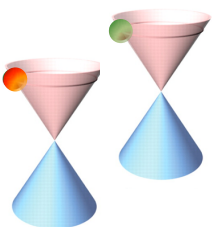
D. E. KHARZEEV



J. LIAO

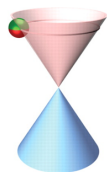
# Interdisciplinary Interests

**Weyl semimetal**  
(non-degenerated bands)

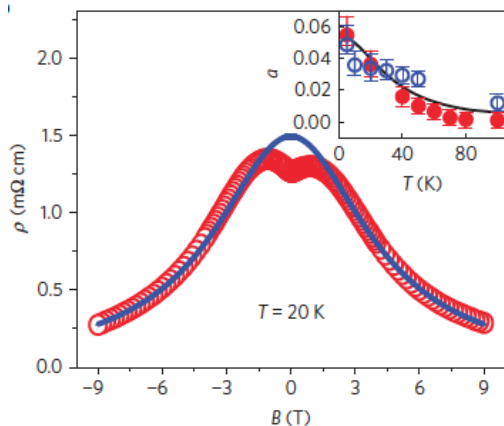


TaAs  
NbAs  
NbP  
TaP

**Dirac semimetal**  
(doubly degenerated bands)

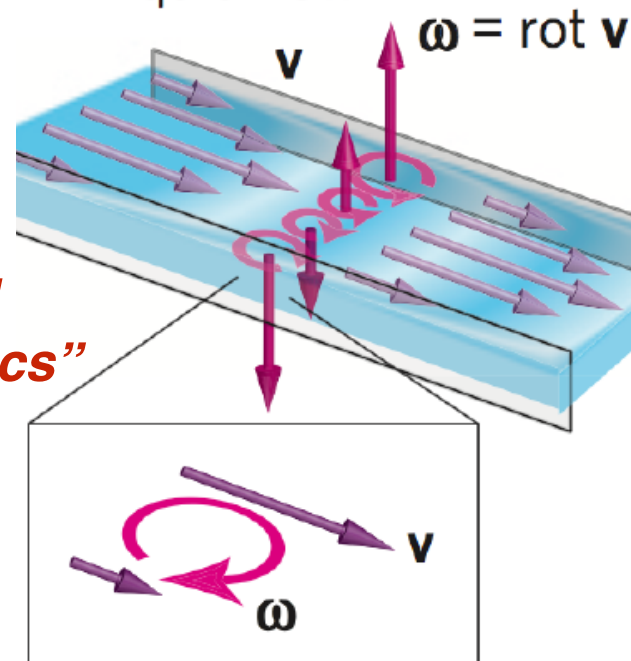


ZrTe<sub>5</sub>  
Na<sub>3</sub>Bi,  
Cd<sub>3</sub>As<sub>2</sub>



“Spin hydrodynamic generation”  
Takahashi, *et al.* Nat. Phys. (2016)

Liquid flow



“Fluid Spintronics”

nature  
physics

LETTERS

PUBLISHED ONLINE: 8 FEBRUARY 2016 | DOI: 10.1038/NPHYS3648

Chiral magnetic effect in ZrTe<sub>5</sub>

Qiang Li<sup>1\*</sup>, Dmitri E. Kharzeev<sup>2,3\*</sup>, Cheng Zhang<sup>1</sup>, Yuan Huang<sup>4</sup>, I. Pletikosić<sup>1,5</sup>, A. V. Fedorov<sup>6</sup>,  
R. D. Zhong<sup>1</sup>, J. A. Schneeloch<sup>1</sup>, G. D. Gu<sup>1</sup> and T. Valla<sup>1\*</sup>

**Condensed matter, cold atomic gases, neutron stars,  
cosmology, plasma physics, etc**

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# Vorticity & Spin Polarization

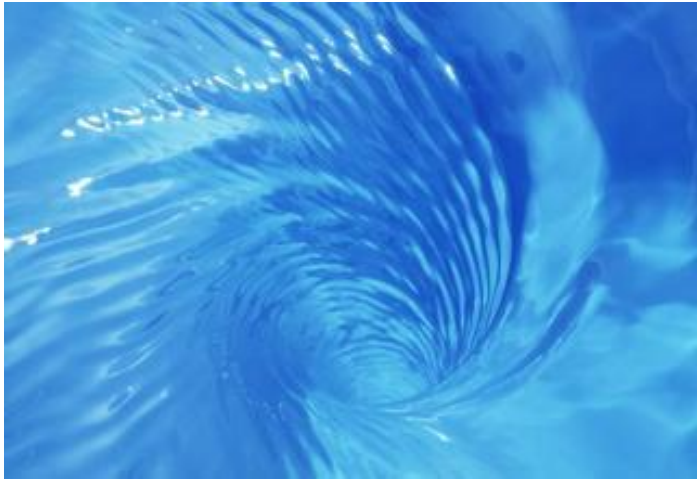
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# Fluid with Angular Momentum

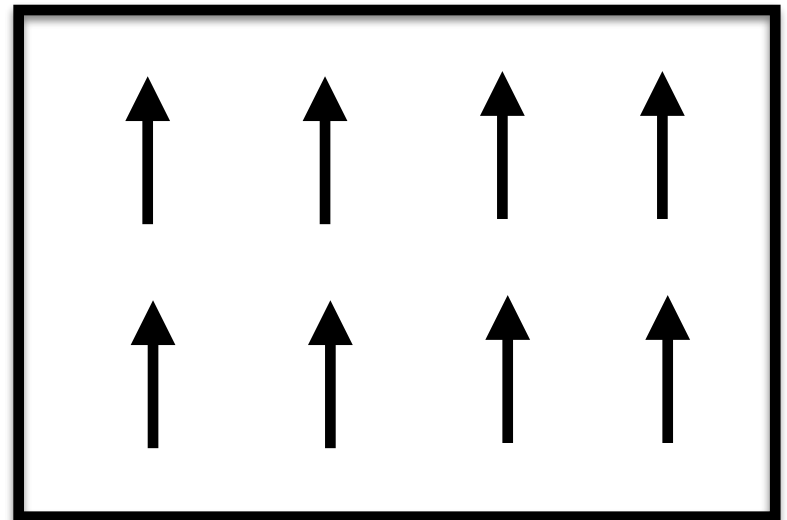
*How does a many-body system cope with a sizable angular momentum?*

*Orbital motion (vorticity);  
Spin alignment (polarization).*



**Fluid vorticity**

**Macroscopic**



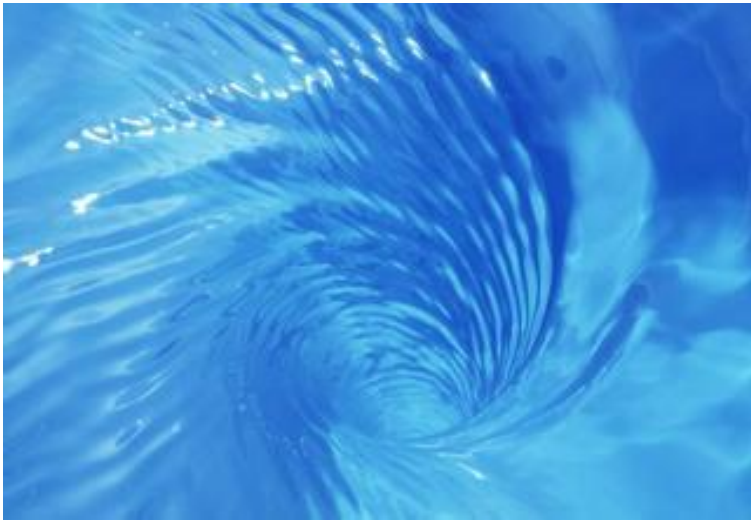
**Individual spin**

**Microscopic**

???

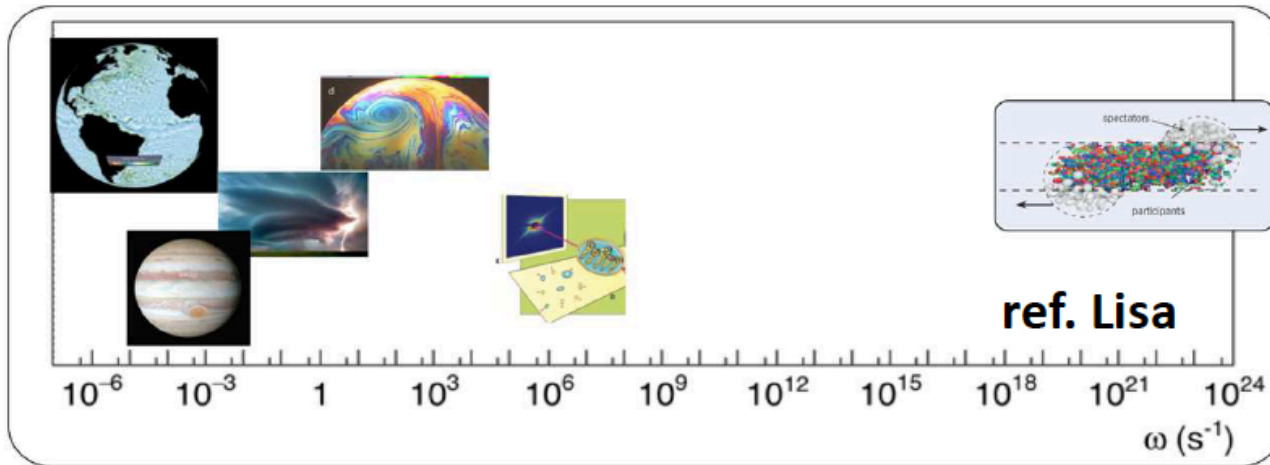


# Quantifying Fluid Rotation



**NR**  $\vec{\omega} = \frac{1}{2} \nabla \times \vec{v}$

**UR**  $\Omega_{\mu\nu} = \frac{1}{2} (\partial_\nu u_\mu - \partial_\mu u_\nu)$



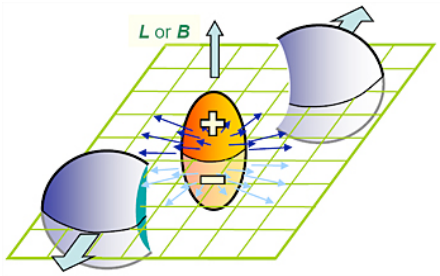
**Heavy ion collisions:**

$v \sim 0.1 c$

$\partial \sim \text{fm}^{-1}$

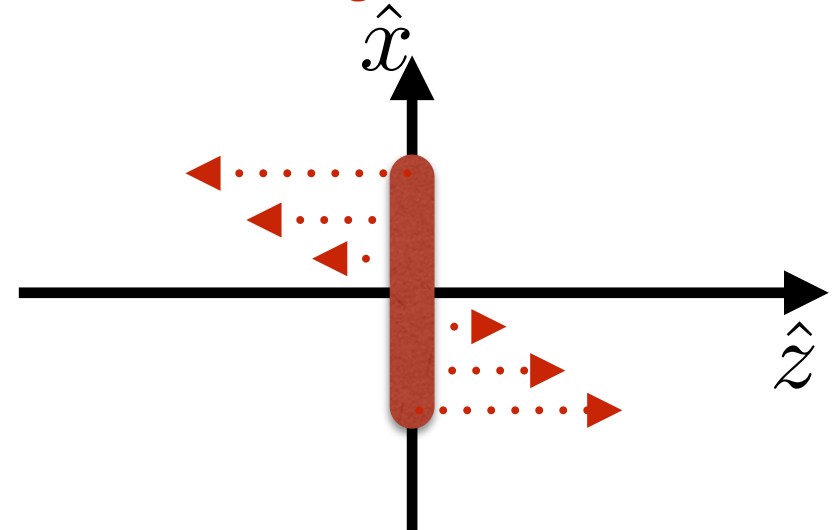
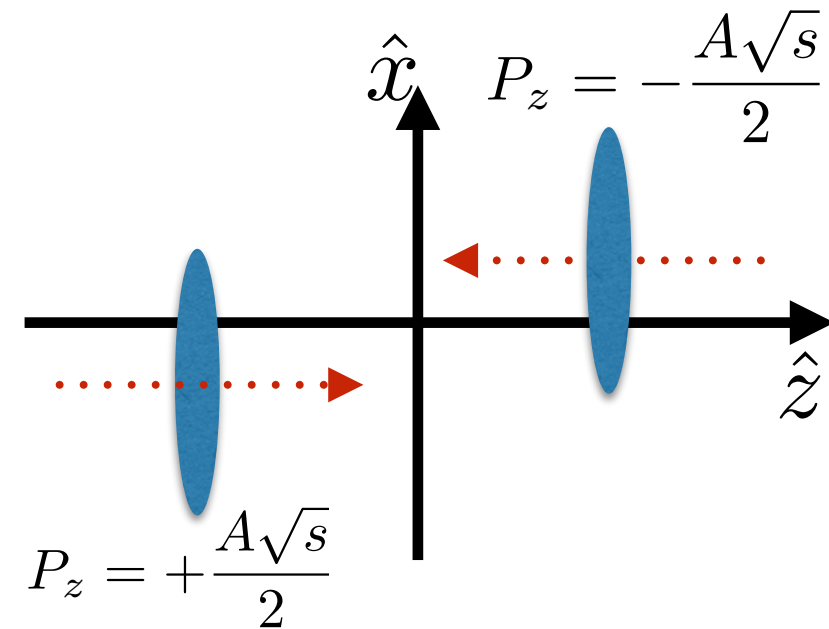
$\omega \sim 10^{22} \text{ s}^{-1}$

# Rotating Quark-Gluon Plasma (1/3)



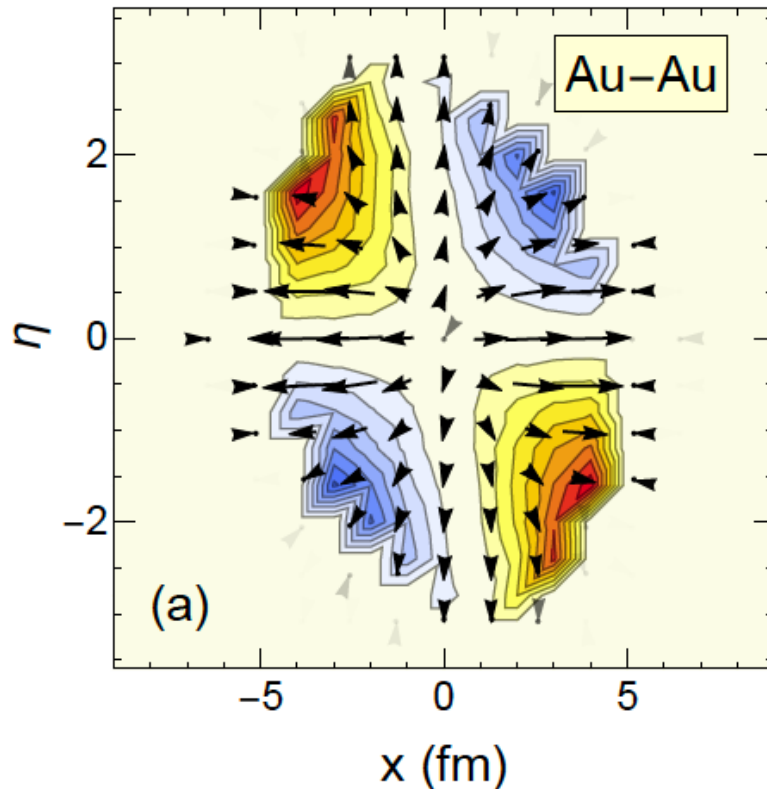
$$L_y = \frac{Ab\sqrt{s}}{2} \sim 10^{4\sim 5} \hbar$$

*QGP's way of accommodating this angular momentum*



*Issue: Spectators taking away lots of L ?!  
(will come back to this point later)*

# Rotating Quark-Gluon Plasma (2/3)



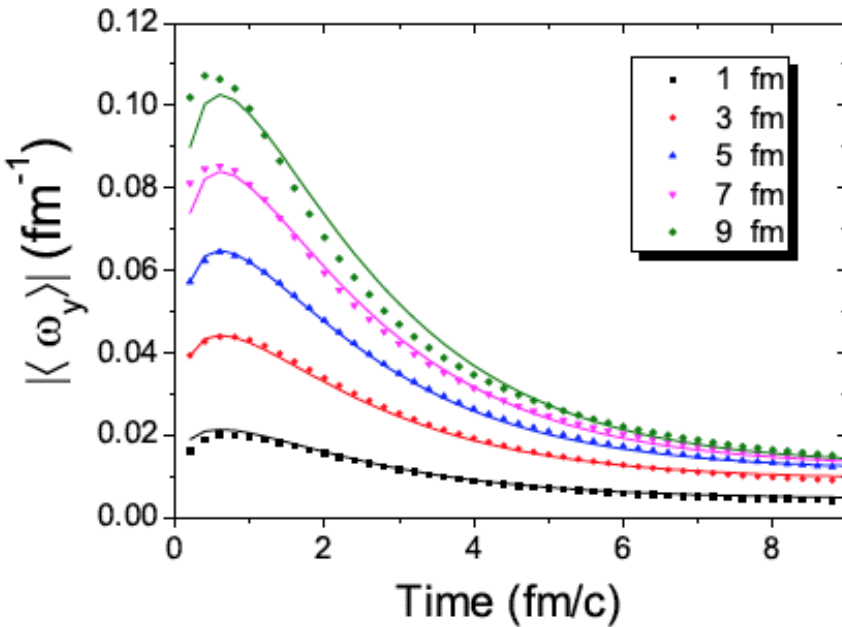
$$\vec{v}(\rho, \phi, \eta) = \hat{e}_\rho v_0(\rho, \eta) [1 + 2c_2(\rho, \eta) \cos 2\phi]$$

$$\begin{aligned} \omega_y &= \frac{\partial v_\rho}{\partial z} \cos \phi \\ &= \frac{2}{t} (ch\eta)^2 \partial_\eta (v_0 + 2v_0 c_2 \cos 2\phi) \cos \phi \\ &= \frac{2}{t} (ch\eta)^2 \left( \frac{x}{\rho} \right) \partial_\eta \left[ v_0 + 2v_0 c_2 \left( 2\frac{x^2}{\rho^2} - 1 \right) \right] \end{aligned}$$

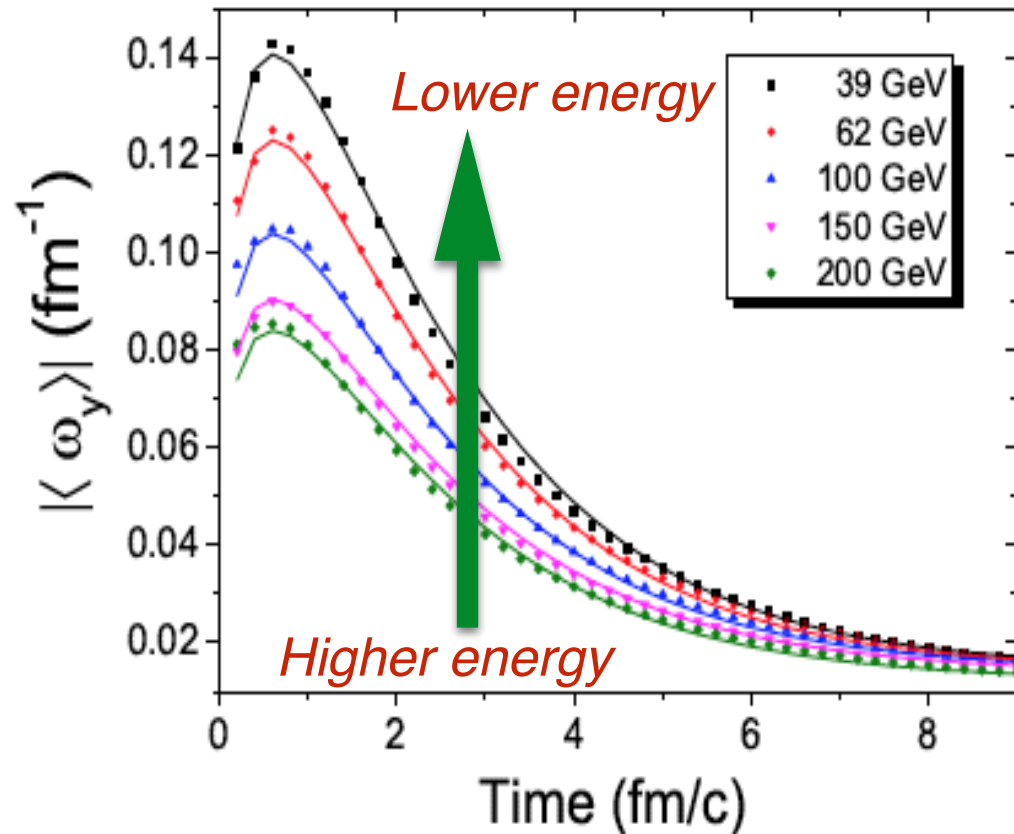
***The local vorticity pattern is strongly influenced by the bulk flow.  
The averaged vorticity reflects the global orbital angular momentum.***

**Yin Jiang, Zi-Wei Lin, JL, PRC2016**

# Rotating Quark-Gluon Plasma (3/3)



**Centrality trend**



**Beam Energy  
Dependence  
Nontrivial !!**

Yin Jiang, Zi-Wei Lin, JL, PRC2016

# Rotational Polarization (1/3)

*Dirac Lagrangian in rotating frame:*

$$g_{\mu\nu} = \begin{pmatrix} 1 - \vec{v}^2 & -v_1 & -v_2 & -v_3 \\ -v_1 & -1 & 0 & 0 \\ -v_2 & 0 & -1 & 0 \\ -v_3 & 0 & 0 & -1 \end{pmatrix}$$

$$\vec{v} = \vec{\omega} \times \vec{x}.$$

$$\bar{\gamma}^\mu = e_a^\mu \gamma^a$$

$$\Gamma_\mu = \frac{1}{4} \times \frac{1}{2} [\gamma^a, \gamma^b] \Gamma_{ab\mu}$$



$$\mathcal{L} = \bar{\psi} [i\bar{\gamma}^\mu (\partial_\mu + \Gamma_\mu) - m] \psi$$

*Under slow rotation:*

$$\mathcal{L} = \psi^\dagger \left[ i\partial_0 + i\gamma^0 \vec{\gamma} \cdot \vec{\partial} + (\vec{\omega} \times \vec{x}) \cdot (-i\vec{\partial}) + \vec{\omega} \cdot \vec{S}_{4 \times 4} \right] \psi$$

$$\hat{H} = \gamma^0 (\vec{\gamma} \cdot \vec{p} + m) - \vec{\omega} \cdot (\vec{x} \times \vec{p} + \vec{S}_{4 \times 4}) = \hat{H}_0 - \vec{\omega} \cdot \hat{\vec{J}}$$

**Rotational  
polarization effect!**

# Rotational Polarization (2/3)

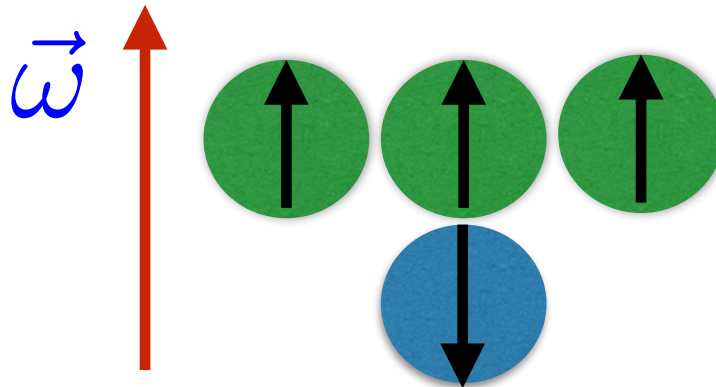
$$\hat{H} = \gamma^0(\vec{\gamma} \cdot \vec{p} + m) - \vec{\omega} \cdot (\vec{x} \times \vec{p} + \vec{S}_{4 \times 4}) = \hat{H}_0 - \vec{\omega} \cdot \hat{J}$$

**Rotational  
polarization effect!**

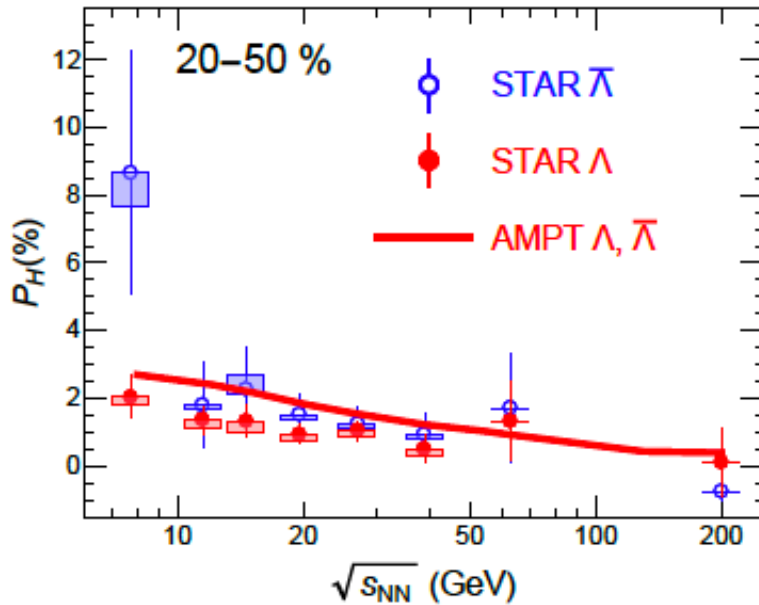


**For thermally produced particles:  
“equal-partition” of angular momentum**

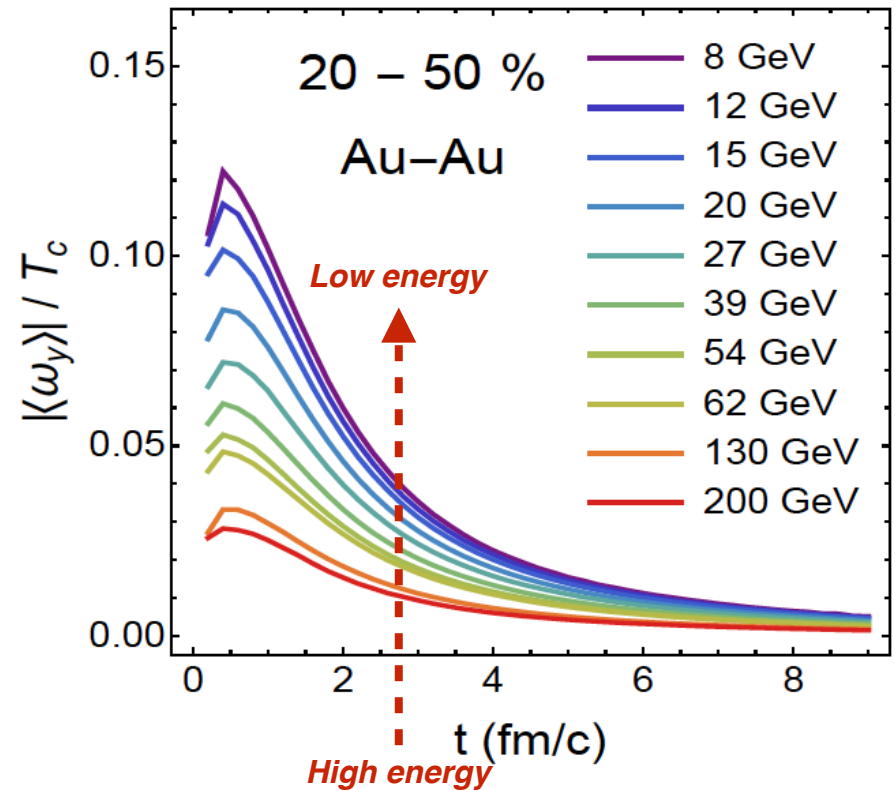
$$dN \propto e^{\frac{\vec{\omega} \cdot \vec{J}}{T}}$$



# Rotational Polarization (3/3)



Jiang, Lin, JL, PRC2016;  
Shi, Li, JL, PLB2019



$$\omega \approx (9 \pm 1) \times 10^{21} \text{ s}^{-1}$$

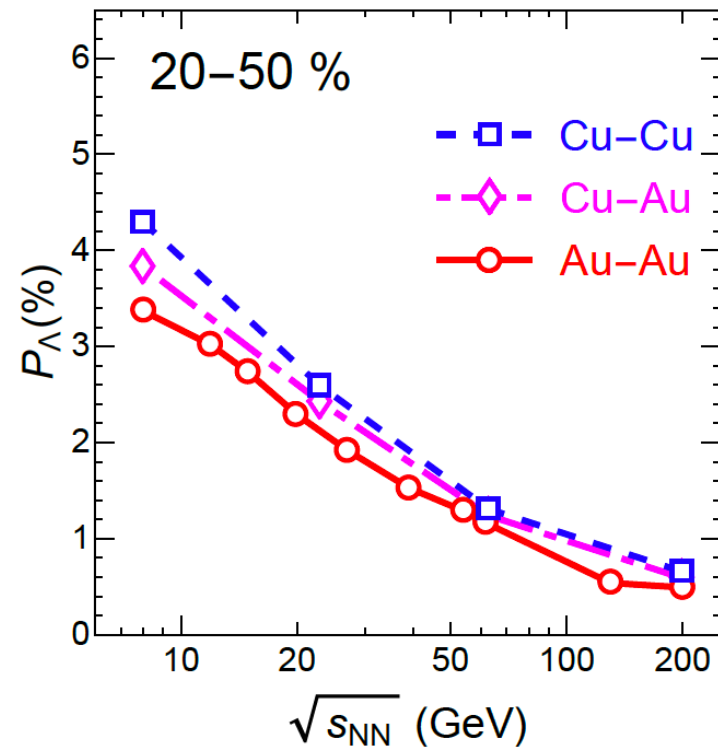
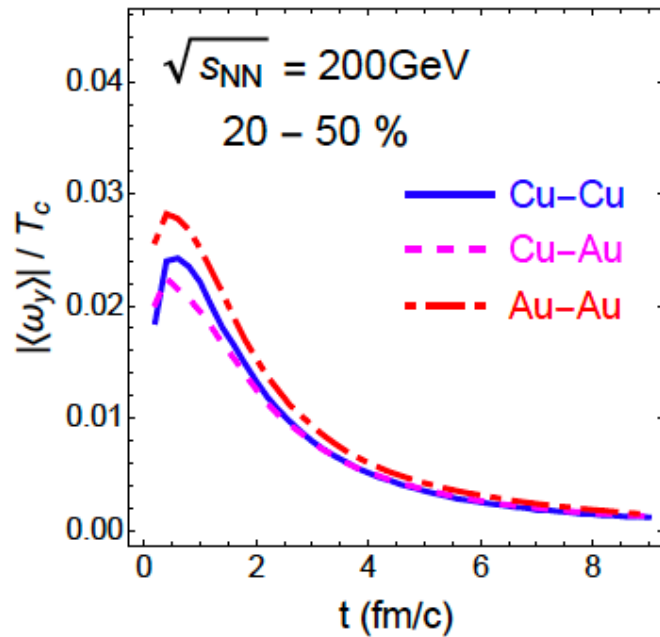
**The most vortical fluid!**

- \* Important at low collision energy!!
- \* Puzzle: why difference in hyperons and anti-hyperons??



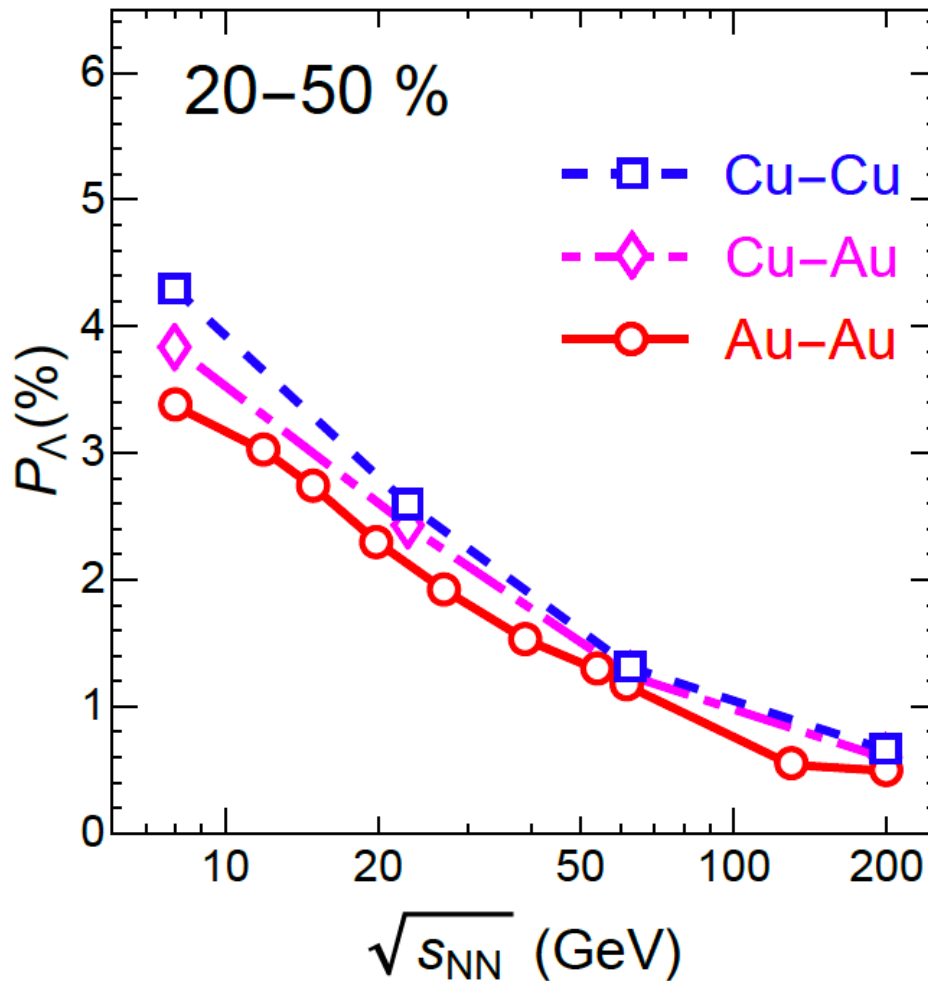
# Predictions for Smaller Systems

**Polarization effect in CuCu and CuAu collisions should be sizable!**



Shuzhe Shi, Kangle Li, JL, PLB2019.

# Prediction for Polarization in CuCu and AuAu



Our surprising finding of  
the signal hierarchy:  
CuCu > CuAu > AuAu !

WHY SO?

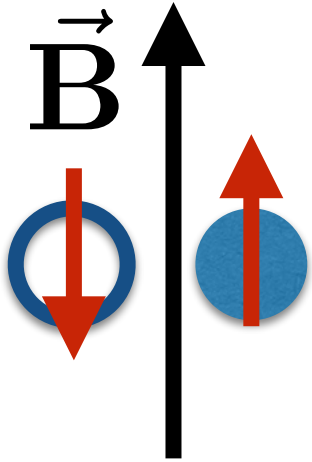
Shuzhe Shi, Kangle Li, JL, arXiv:1712.00878.

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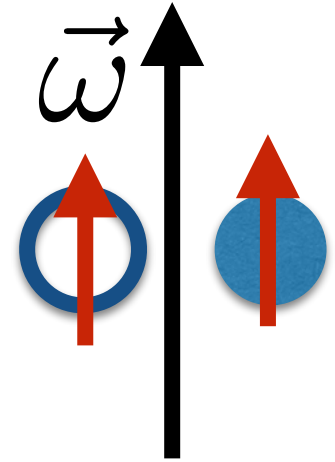
# Magnetic Field at Low Collision Energy

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# Magnetic Field Induced Polarization



$$S^\mu = -\frac{1}{8m} \epsilon^{\mu\nu\rho\sigma} p_\nu \varpi_{\rho\sigma}$$



For Lambda:

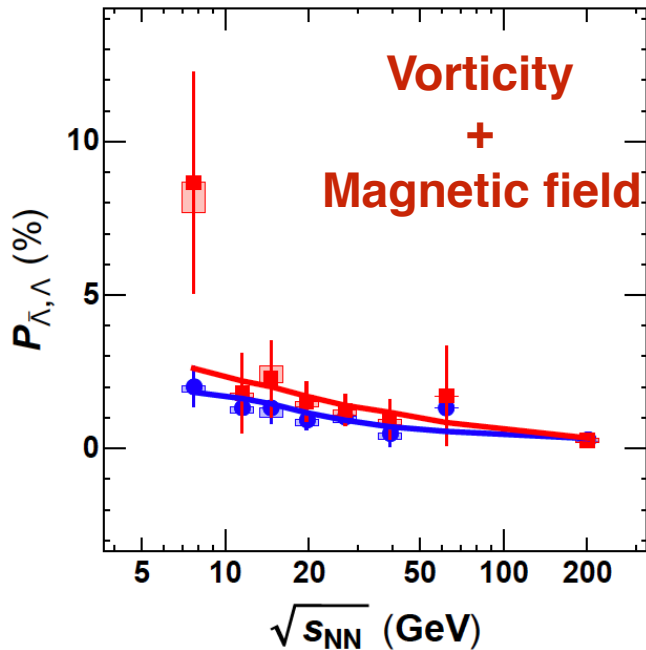
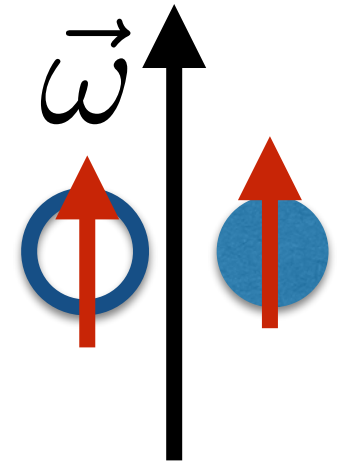
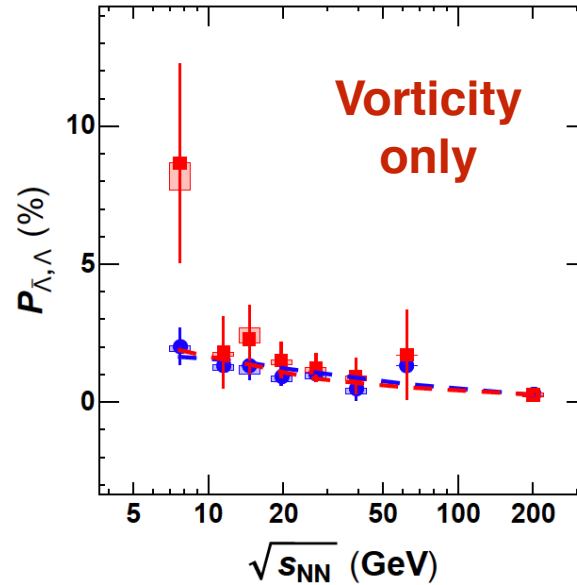
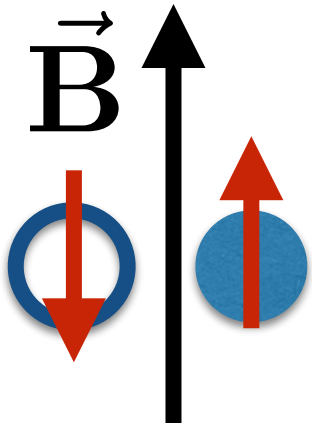
$$\varpi_{\rho\sigma} \rightarrow \left[ \varpi_{\rho\sigma} - 2 \left( \frac{0.61}{2M_p} \right) \frac{eF_{\rho\sigma}}{T} \right]$$

For anti-Lambda:

$$\varpi_{\rho\sigma} \rightarrow \left[ \varpi_{\rho\sigma} + 2 \left( \frac{0.61}{2M_p} \right) \frac{eF_{\rho\sigma}}{T} \right]$$

*[Yu Guo, Shengqin Feng, Shuzhe Shi, JL, in preparation.]*

# Magnetic Field Induced Polarization

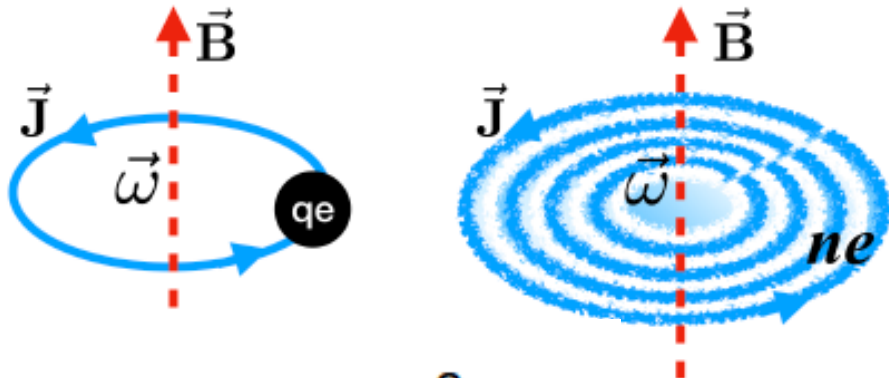


**For this to work:  
Requires long-lived late time  
magnetic field.**

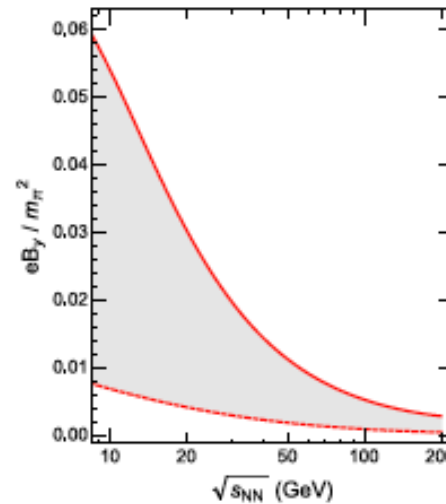
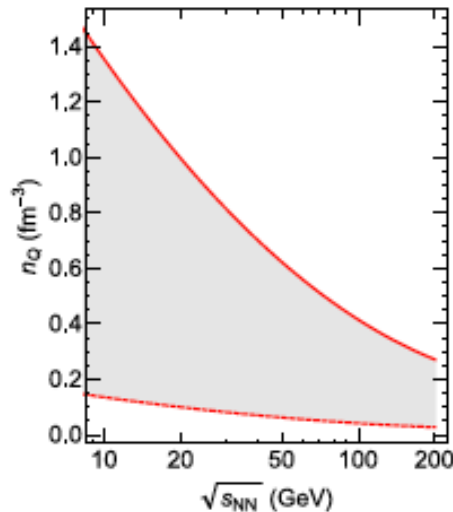
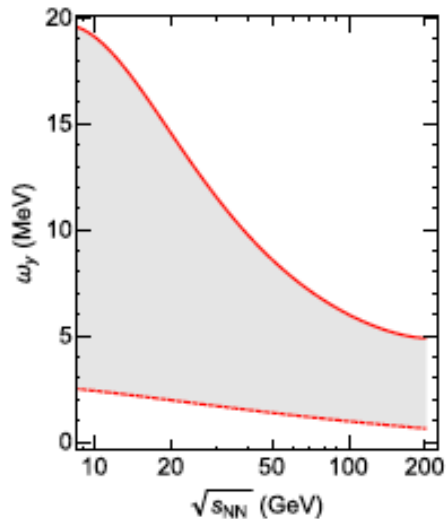
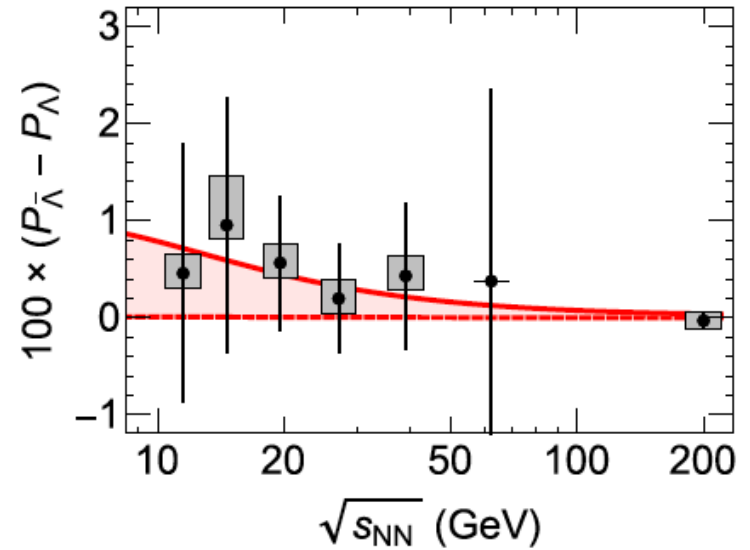
**Where does that come from??**

**[Yu Guo, Shengqin Feng, Shuzhe Shi, JL, in preparation.]**

# Connecting Magnetic Field and Fluid Rotation



$$e\bar{B} = \frac{e^2}{4\pi} nA\bar{\omega}$$



**Important at  
low beam  
energy!**

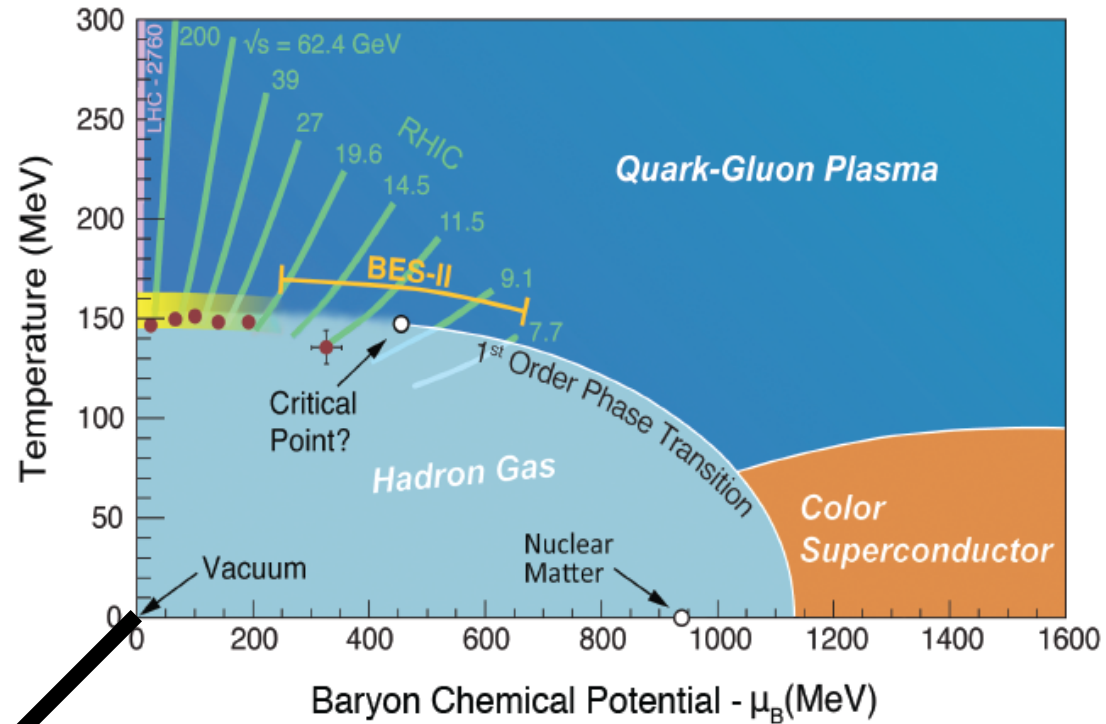
**[X. Guo, et al, arXiv:1904.04704]**

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# Discussions & Outlook

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# QCD Phase Structures under Extreme Fields



$\vec{B}$   
 $\vec{\omega}$



# Rotational Suppression of Scalar Pairing

*Let us consider pairing phenomenon in fermion systems.*

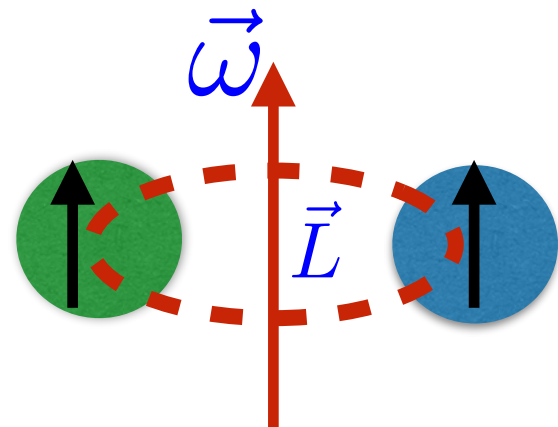
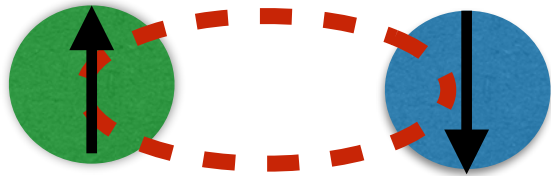
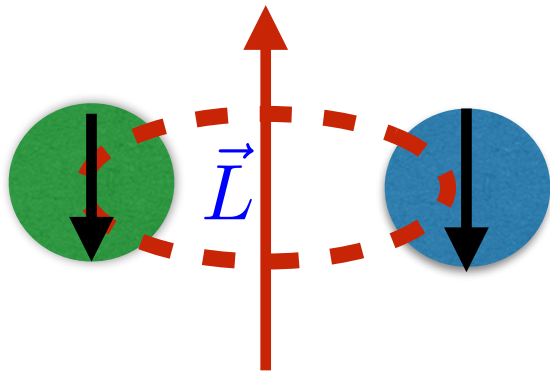
*There are many examples:*

*superconductivity, superfluidity, chiral condensate, diquark, ...*

We consider scalar pairing state, with  $J=0$ .

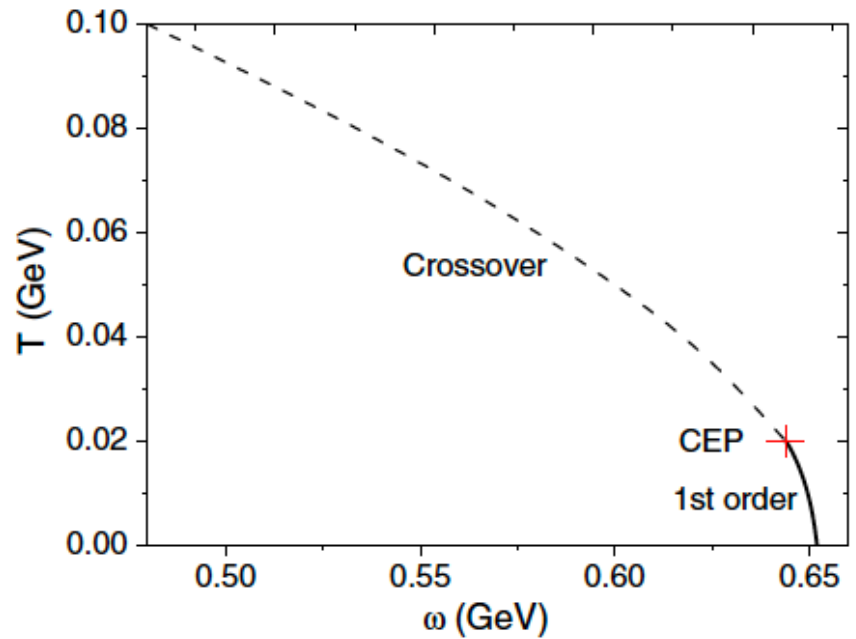
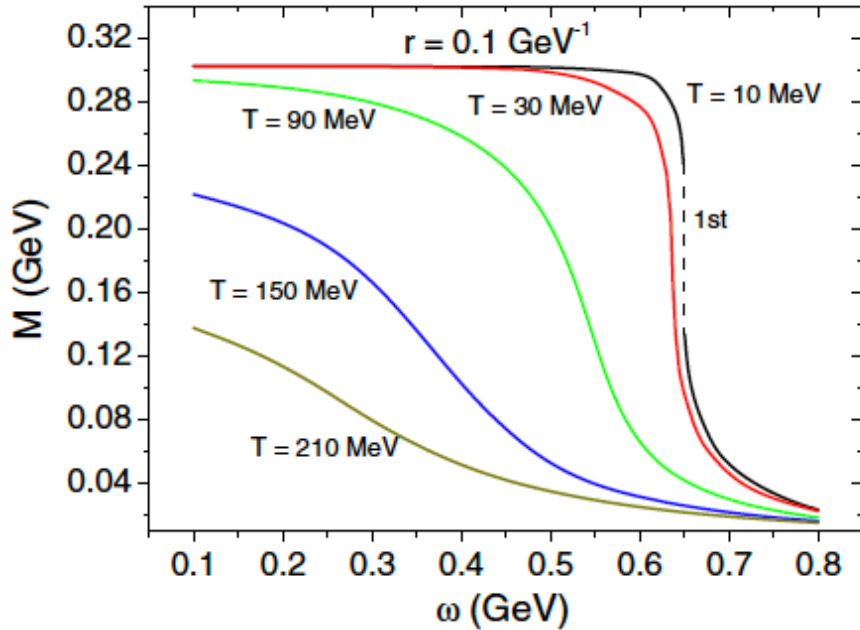
$$\vec{S} = \vec{s}_1 + \vec{s}_2 \quad \vec{J} = \vec{L} + \vec{S}$$

Rotation tends to polarize ALL angular momentum, both L and S, thus suppressing scalar pairing.



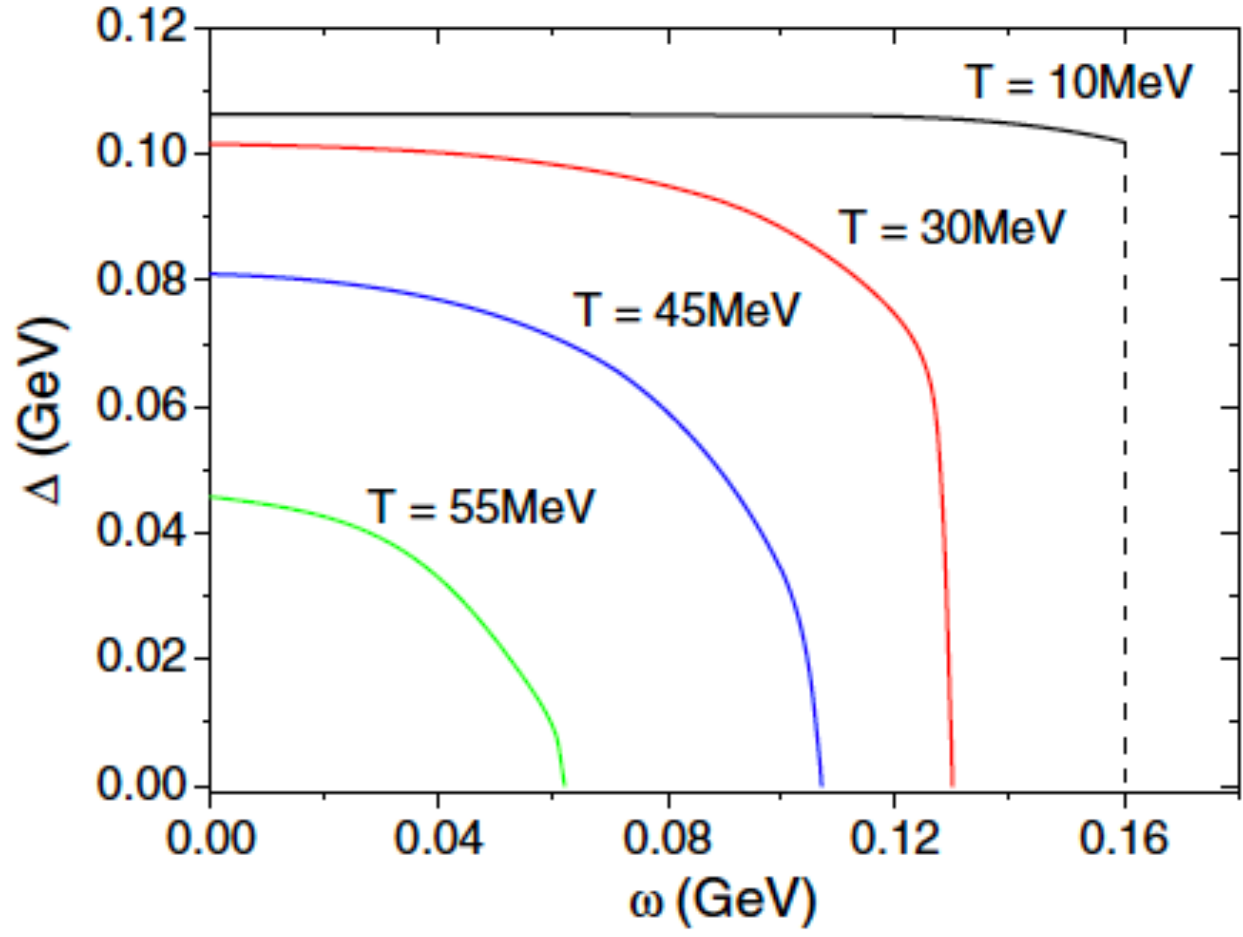
[Yin Jiang, JL, PRL2016]

# Chiral Phase Transition



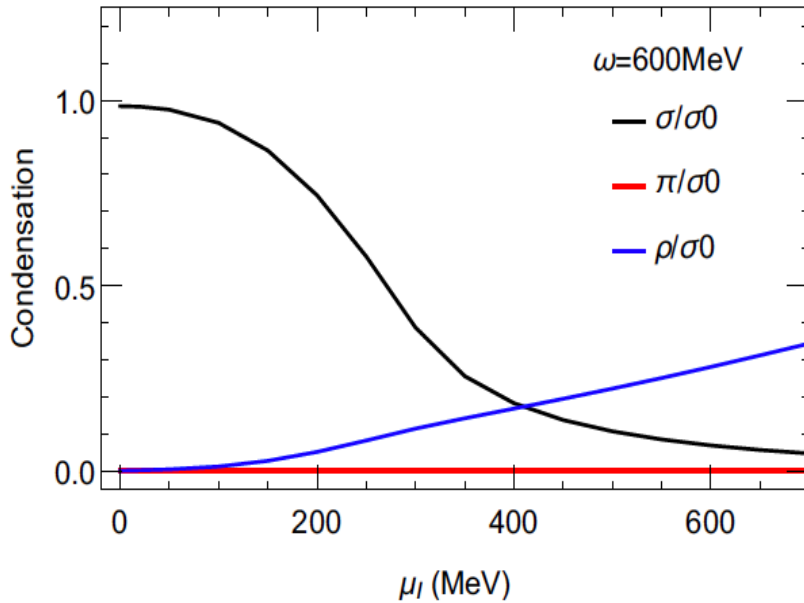
***Maybe in low energy collisions:  
In-medium mass correction due to rotation??***

# Color Superconducting Pairing



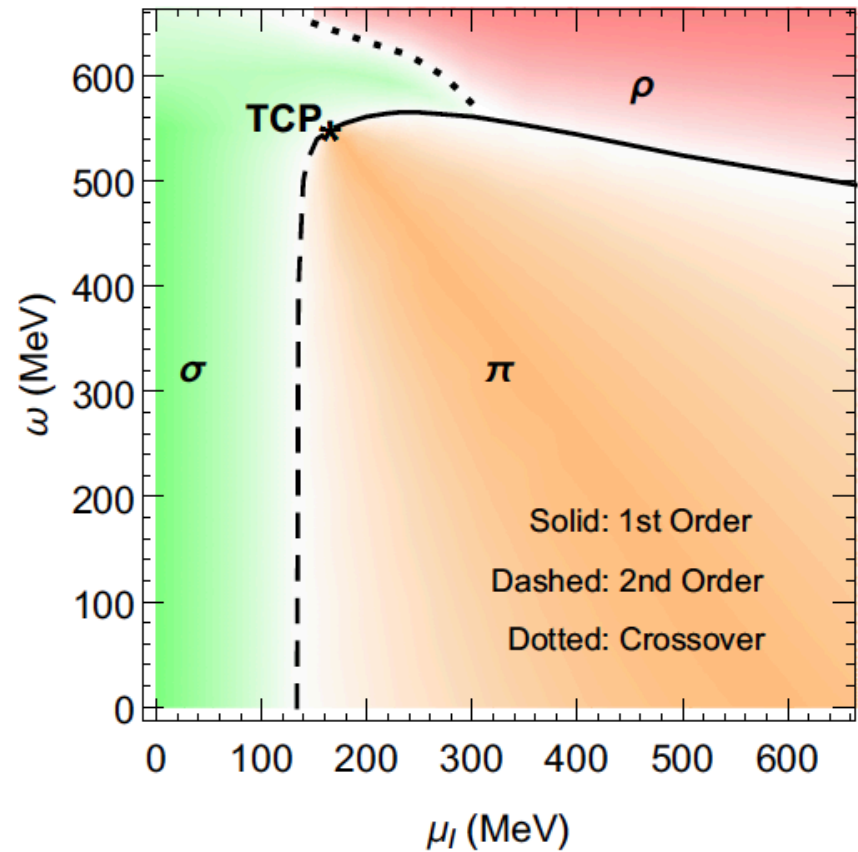
*Maybe also for nucleon-pairing?!*

# Isospin Matter



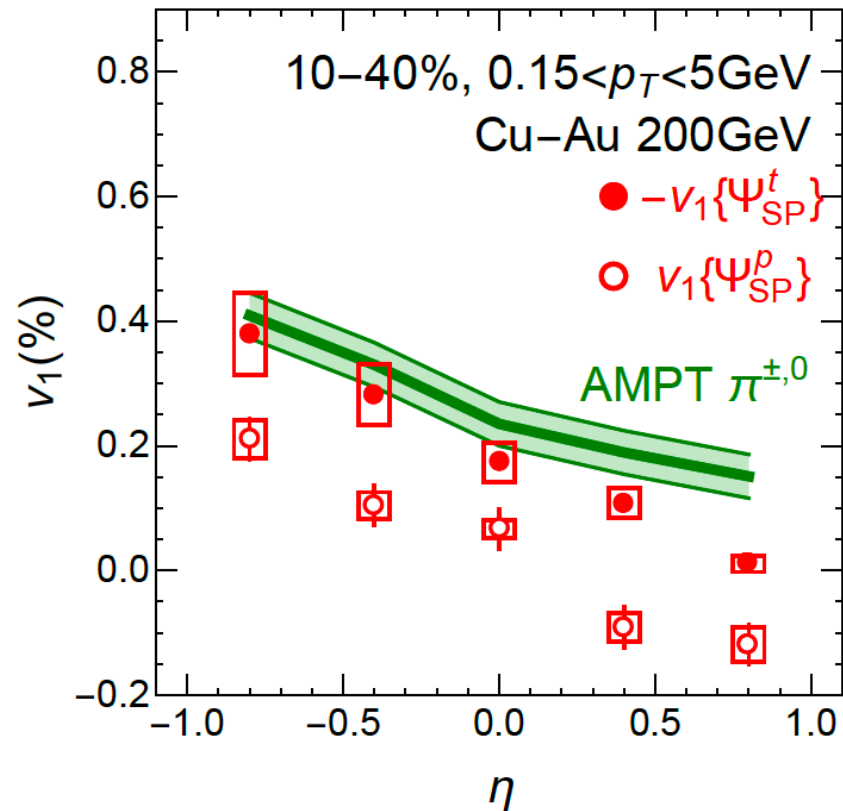
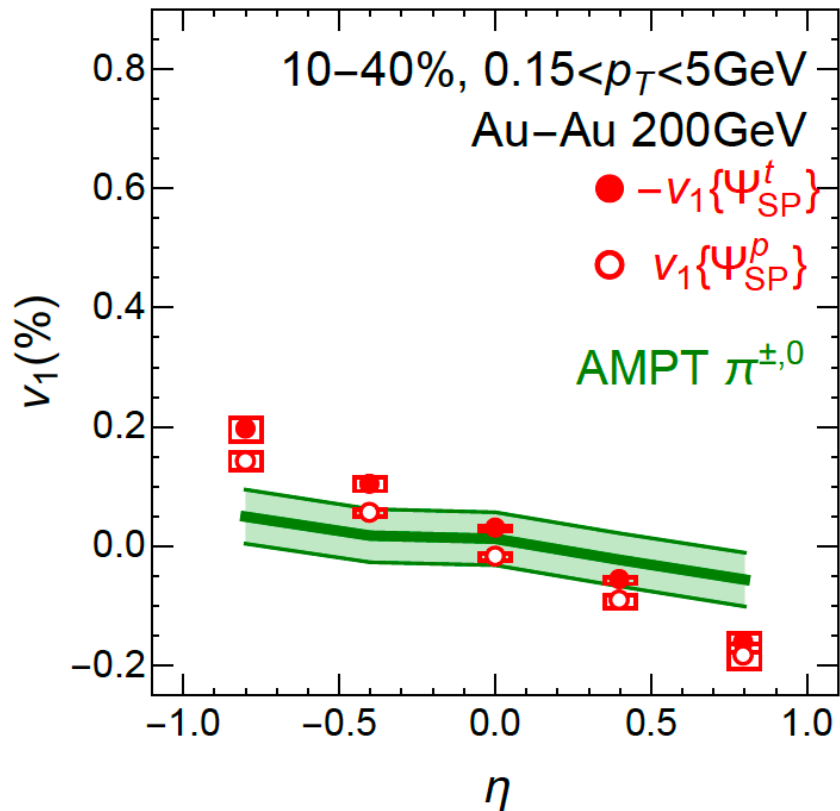
**Spin-1 Rho condensation  
is favored by rotation!**

[Hui Zhang, Defu Hou, JL,  
arXiv: 1812.11787.]



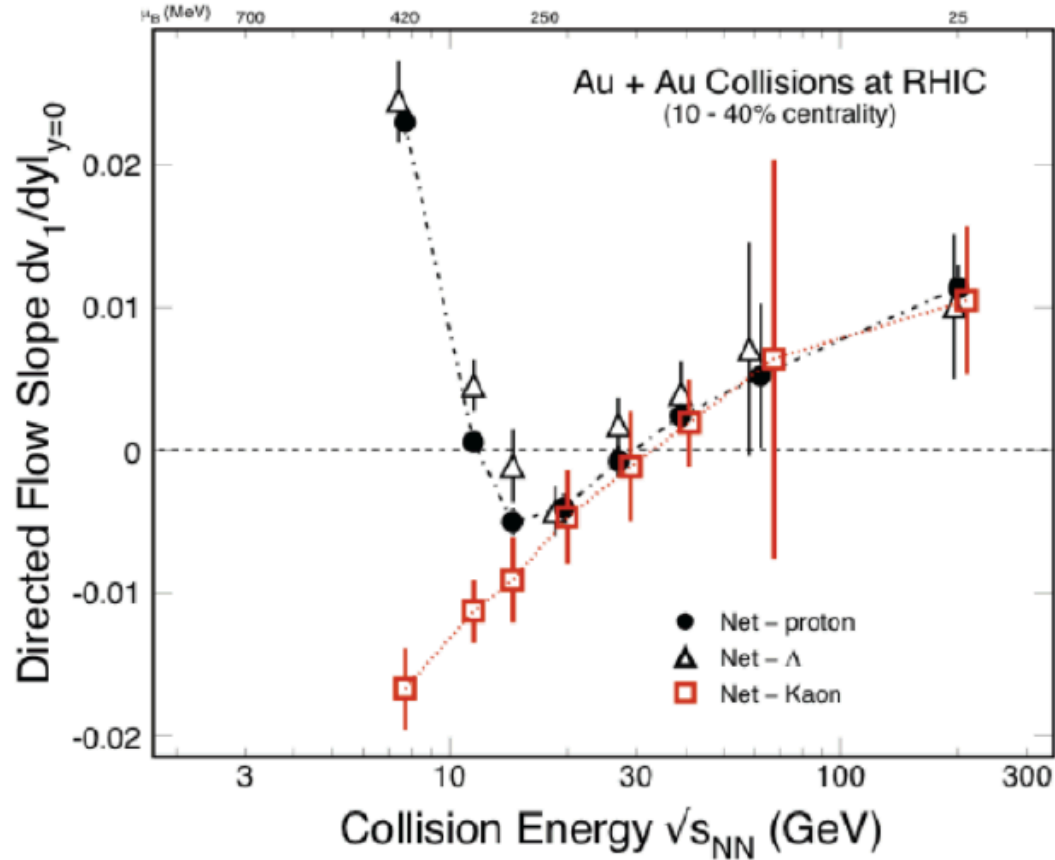
**Large isospin density in low energy collision:  
Possible effect from rotation?**

# Directed Flow



It is important to understand directed flow and vorticity simultaneously.

# Directed Flow



***Possible nontrivial implications for vorticity/rotation at very low beam energy??***

***Forward/backward vorticity & polarization?!***

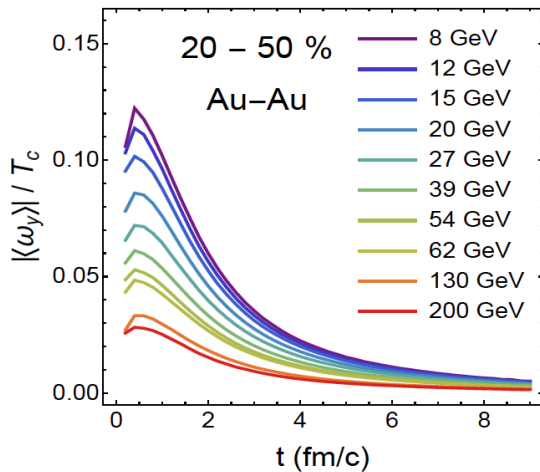
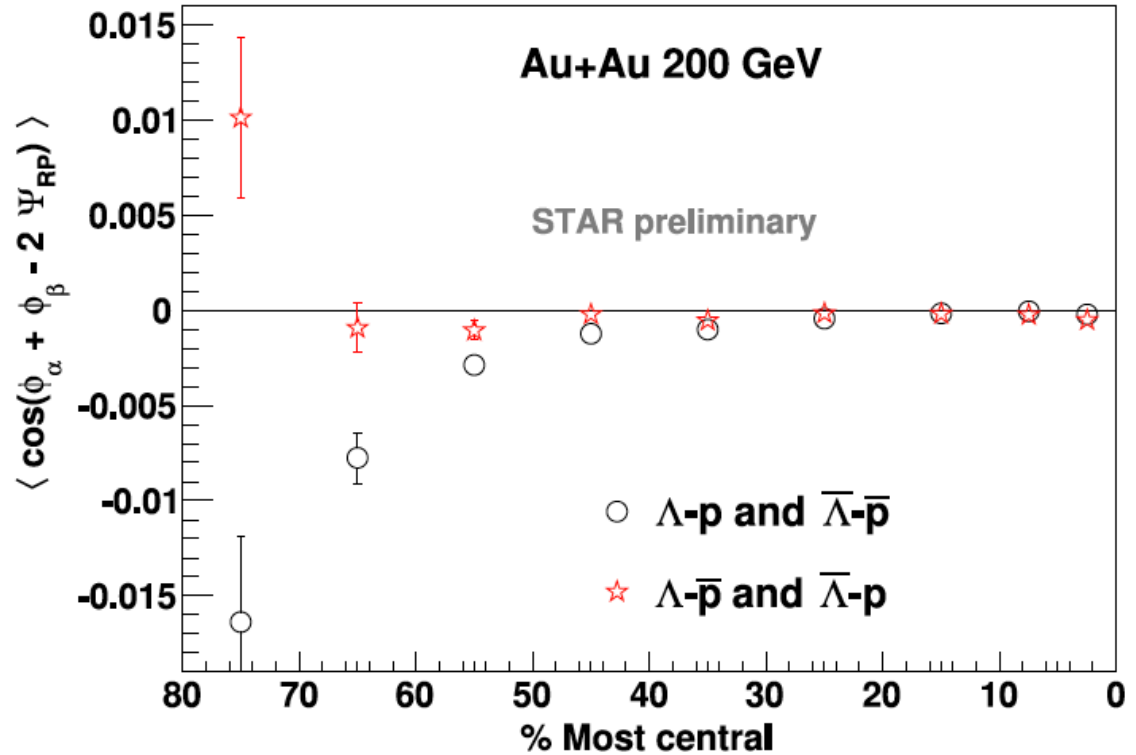
# Potential Signal of Chiral Vortical Effect (CVE)

QM2014

**CVE → Baryon separation across reaction plane.**

$$\vec{J}_Q^{2f} = \frac{N_c \mu_5}{2\pi^2} \left[ \frac{5}{9} (e\vec{B}) + \frac{2}{9} (\mu_B \vec{\omega}) \right]$$

$$\vec{J}_B^{2f} = \frac{N_c \mu_5}{2\pi^2} \left[ \frac{1}{9} (e\vec{B}) + \frac{4}{9} (\mu_B \vec{\omega}) \right]$$



**Vortical effects at low energy ?!**

# Outlook

**Nuclear matter under extreme fields  
(magnetic field and fluid rotation):  
Possibility of a very interesting and novel  
physics topical line at FAIR/NICA?!**

- *Vorticity structure and directed flow*
- *Magnetic field from rotation*
- *Vorticity-induced transport effects*
- *Mass shift / phase line shift due to extreme fields*
- *Isospin matter*
- *Hadronic level effects*

