

第17届全国重味物理与CP破坏研讨会



Weak Decays of Anti-triplet Charmed Baryon

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2019. 7. 31

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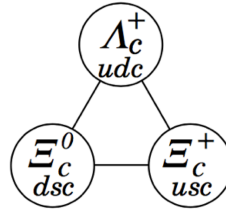


Introduction

新瓶

Review: Talk by 耿朝强

$2286.46 \pm 0.14 \text{ MeV}$
 $(2.00 \pm 0.06) \times 10^{-13} \text{ s (S = 1.6)}$



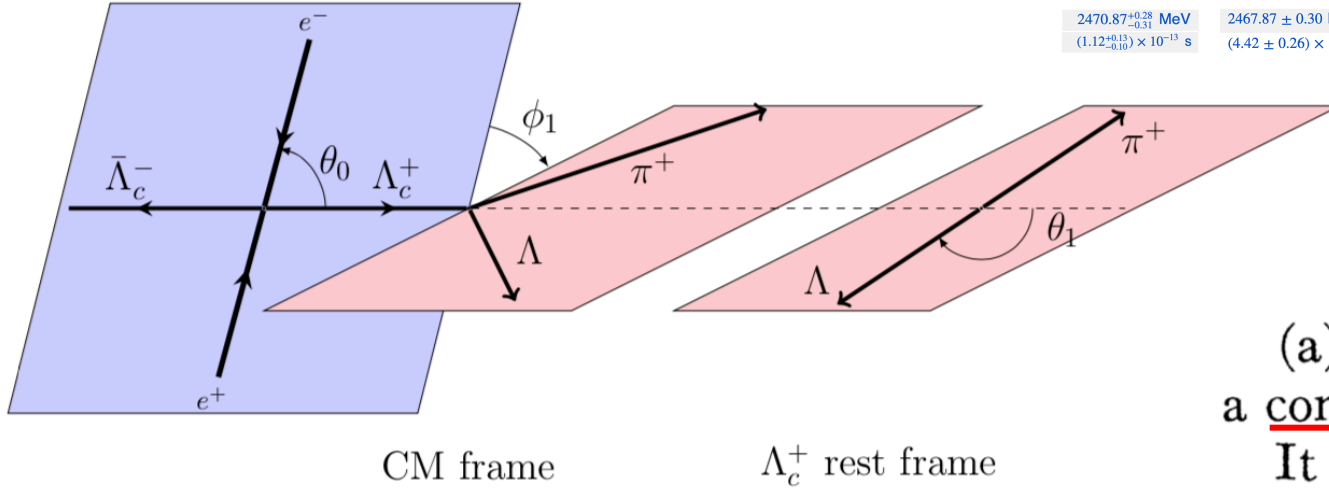
$2470.87^{+0.28}_{-0.31} \text{ MeV}$
 $(1.12^{+0.13}_{-0.10}) \times 10^{-13} \text{ s}$

$2467.87 \pm 0.30 \text{ MeV (S = 1.1)}$
 $(4.42 \pm 0.26) \times 10^{-13} \text{ s (S = 1.3)}$

旧酒

Branching fraction

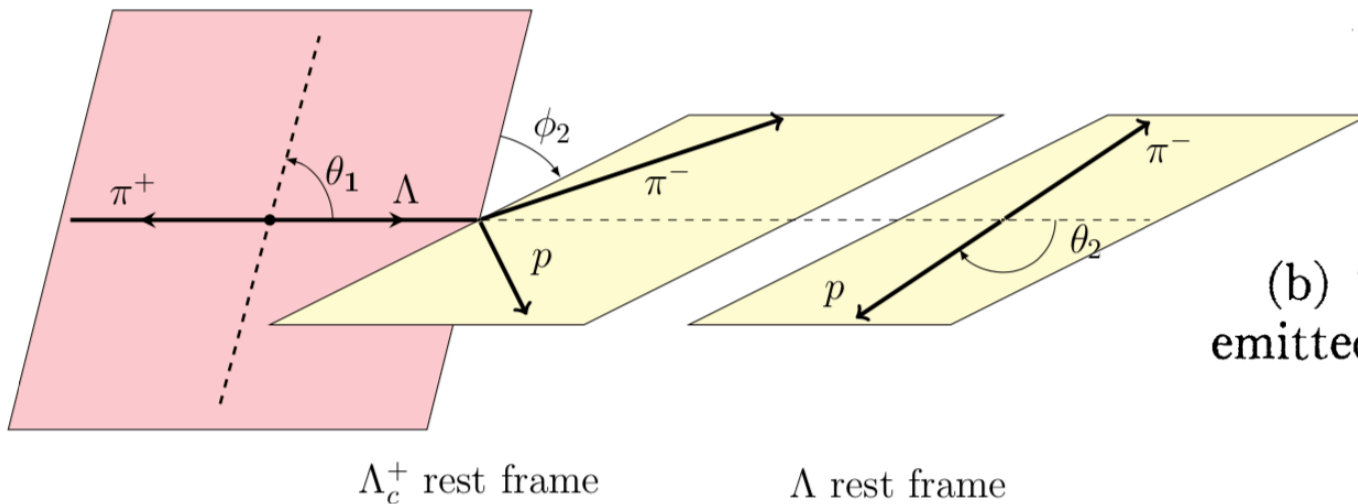
Polarization



(a) The angular distribution of the decay pion from a completely polarized hyperon at rest.

It has been pointed out before¹ that the distribution is proportional to

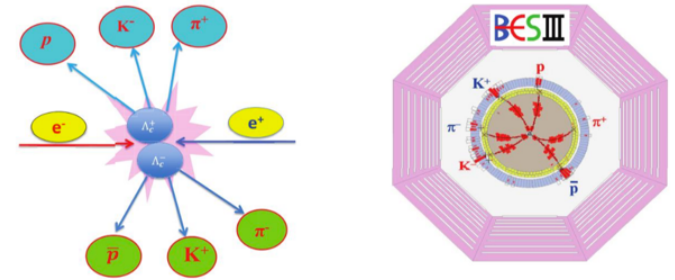
$$[1 + \alpha \cos \chi] d\Omega, \quad (1)$$



(b) The longitudinal polarization of the nucleon emitted in the decay of unpolarized hyperons at rest.

Lee-Yang, 1957

Λ_c^+ @ BESIII 4.6 GeV, 567/pb



- $\mathcal{B}(\Lambda_c^+ \rightarrow pK^- \pi^+)$

- ARGUS + CLEO : $(5.0 \pm 1.3)\%$ PDG 2014

- Belle: $(6.84 \pm 0.24^{+0.21}_{-0.27})\%$
Belle, PRL 113 (2014), 042002

- BESIII: $(5.84 \pm 0.27 \pm 0.23)\%$
BESIII, PRL 116 (2016) , 052001



PDG 2016: $(6.35 \pm 0.33)\%$

- 12 modes measured by BESIII

Mode	This work (%)	PDG (%)
pK_S^0	$1.52 \pm 0.08 \pm 0.03$	1.15 ± 0.30
$pK^- \pi^+$	$5.84 \pm 0.27 \pm 0.23$	5.0 ± 1.3
$pK_S^0 \pi^0$	$1.87 \pm 0.13 \pm 0.05$	1.65 ± 0.50
$pK_S^0 \pi^+ \pi^-$	$1.53 \pm 0.11 \pm 0.09$	1.30 ± 0.35
$pK^- \pi^+ \pi^0$	$4.53 \pm 0.23 \pm 0.30$	3.4 ± 1.0
$\Lambda \pi^+$	$1.24 \pm 0.07 \pm 0.03$	1.07 ± 0.28
$\Lambda \pi^+ \pi^0$	$7.01 \pm 0.37 \pm 0.19$	3.6 ± 1.3
$\Lambda \pi^+ \pi^- \pi^+$	$3.81 \pm 0.24 \pm 0.18$	2.6 ± 0.7
$\Sigma^0 \pi^+$	$1.27 \pm 0.08 \pm 0.03$	1.05 ± 0.28
$\Sigma^+ \pi^0$	$1.18 \pm 0.10 \pm 0.03$	1.00 ± 0.34
$\Sigma^+ \pi^+ \pi^-$	$4.25 \pm 0.24 \pm 0.20$	3.6 ± 1.0
$\Sigma^+ \omega$	$1.56 \pm 0.20 \pm 0.07$	2.7 ± 1.0

PDG values for Λ_c^+ decay BF's before 2016 version become obsolete

Λ_c^+ @ BESIII **4.6 GeV, 567/pb**

- Singly-Cabibbo-suppressed decay has been measured

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\eta) = (1.24 \pm 0.28(\text{stat.}) \pm 0.10(\text{syst.})) \times 10^{-3}$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^0) < 2.7 \times 10^{-4}$$

BESIII, PRD 95 (2017), 111102

- Neutral mode can be measured

$$\mathcal{B}(\Lambda_c^+ \rightarrow nK_S^0\pi^+) = (1.82 \pm 0.23(\text{stat}) \pm 0.11(\text{syst}))\%. \quad \text{BESIII, PRL 118 (2016), 112001}$$

- More decay asymmetries can be measured

$$\alpha_{\Lambda\pi^+} \sim 10\%, \quad \alpha_{\Sigma^0\pi^+} \sim (19 - 66)\%$$

D. Wang, R.-G. Ping, L. Li, X.-R. Lyu, Y.-H. Zheng, Chin. Phys. C 41 (2017) 023106

$$\alpha_{\Lambda\pi^+} = -0.80 \pm 0.11 \pm 0.02$$

$$\alpha_{\Sigma^+\pi^0} = -0.57 \pm 0.10 \pm 0.07$$

BESIII, 1905.04707

$$\alpha_{\Sigma^0\pi^+} = -0.73 \pm 0.17 \pm 0.07$$

Λ_c^+ @ BESIII

4.6 GeV, 567/pb

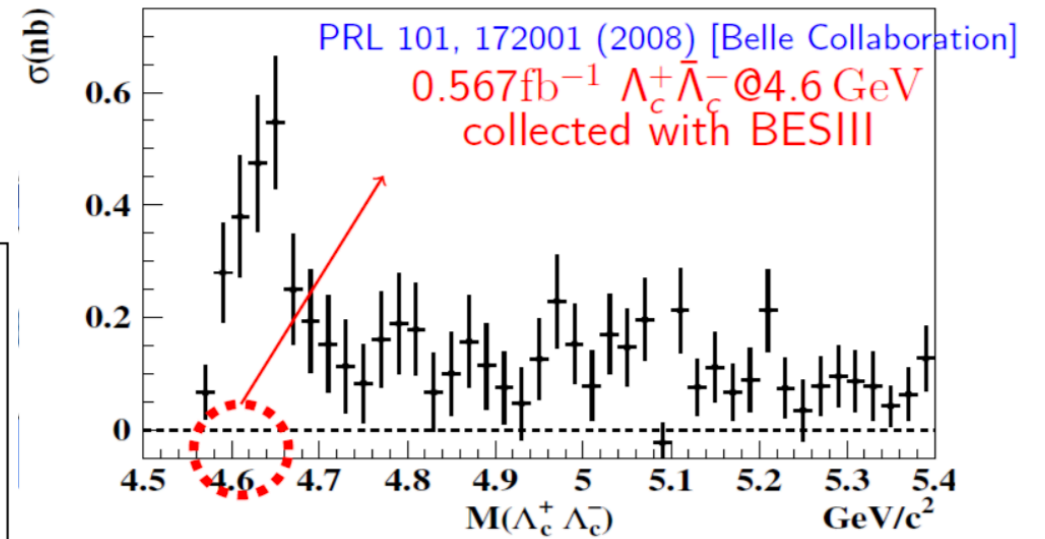
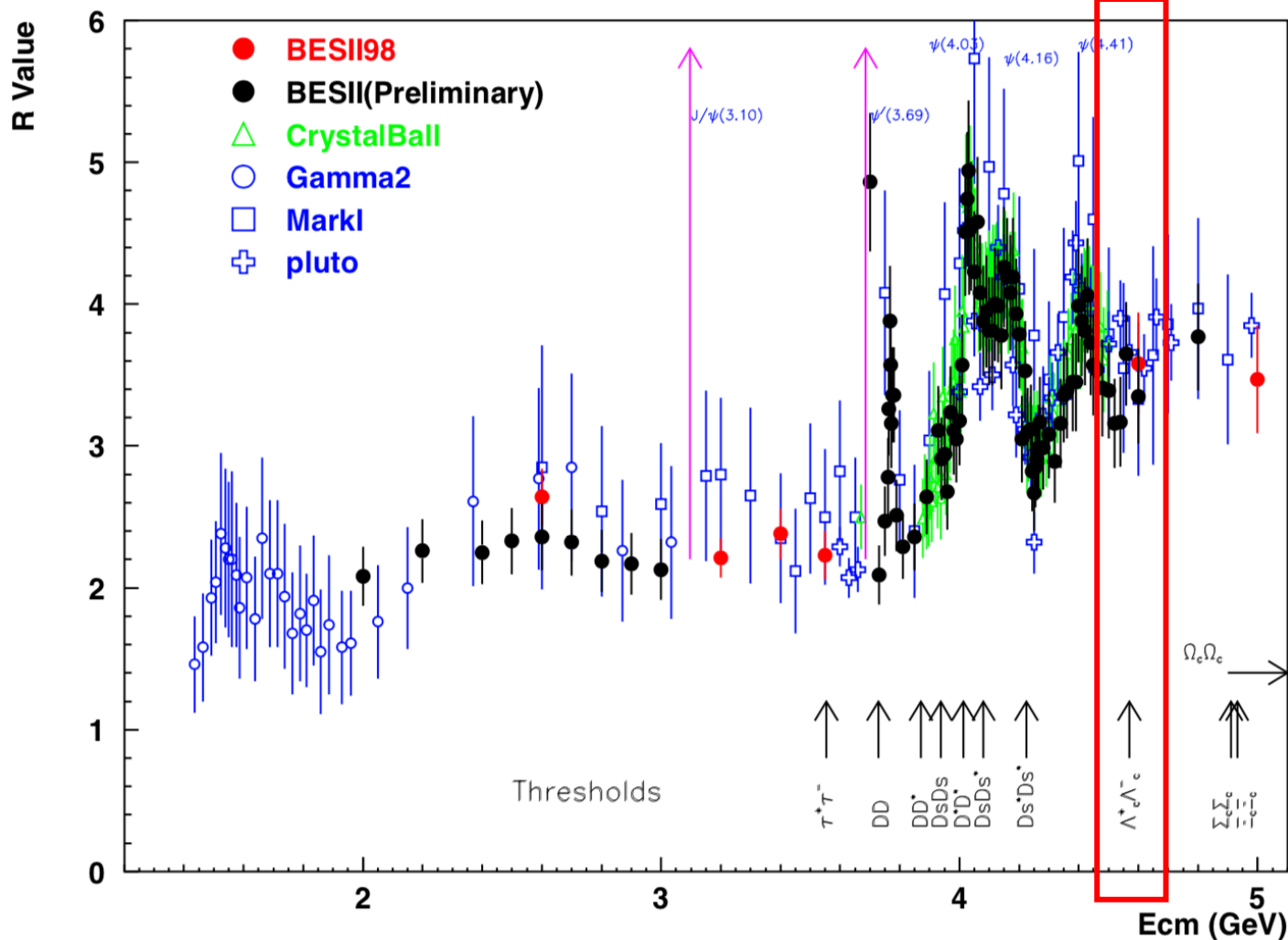
- More precise measurement of Cabibbo-favored process

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+) = (5.90 \pm 0.86 \pm 0.39) \times 10^{-3} \quad \text{BESIII, PLB 783 (2018), 200-206}$$

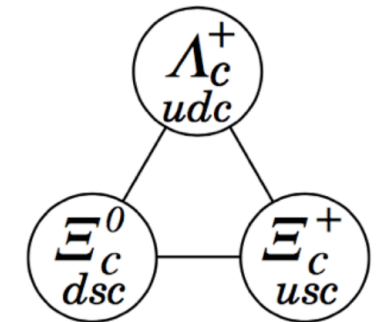
$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = (0.41 \pm 0.19 \pm 0.05)\% (< 0.68\%)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = (1.34 \pm 0.53 \pm 0.21)\% (< 1.9\%) \quad \text{BESIII, 1811.08028}$$

The future of Λ_c^+



2286.46 ± 0.14 MeV
 (2.00 ± 0.06) × 10⁻¹³ s (S = 1.6)



2470.87^{+0.28}_{-0.31} MeV
 (1.12^{+0.13}_{-0.10}) × 10⁻¹³ s

2467.87 ± 0.30 MeV (S = 1.1)
 (4.42 ± 0.26) × 10⁻¹³ s (S = 1.3)

● Beam energy

- Ebeam = 2.3 → 2.35 GeV in 2019
- Ebeam = 2.35 → 2.45 GeV in 2020-21

Ξ_c @ Belle (772 ± 11) × 10⁶ B \bar{B} pair

Talk by 沈成平

- First measurement of $\Xi_c^0 \rightarrow \Xi^- \pi^+$

$$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0) = [9.51 \pm 2.10(\text{stat.}) \pm 0.88(\text{syst.})] \times 10^{-4}$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = [1.80 \pm 0.50(\text{stat.}) \pm 0.14(\text{syst.})]\%$$

Belle, PRL 122 (2019) 082001

- The branching fraction of $\Xi_c^+ \rightarrow \Xi^0 \pi^+$

$$\mathcal{B}(\bar{B}^0 \rightarrow \bar{\Lambda}_c^- \Xi_c^+) = [1.16 \pm 0.42(\text{stat.}) \pm 0.15(\text{syst.})] \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+) = (2.86 \pm 1.21 \pm 0.38) \times 10^{-2} \quad \text{Belle, 1904.12093}$$

$$\Gamma(\Xi_c^+ \rightarrow \Xi^0 \pi^+) / \Gamma(\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+) = (0.55 \pm 0.13 \pm 0.09) \quad \text{CLEO, PLB373(1996)261}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+) = (1.57 \pm 0.83)\%$$

Lifetimes @ LHCb

$$\tau_{\Lambda_c^+} = 203.5 \pm 1.0 \pm 1.3 \pm 1.4 \text{ fs},$$

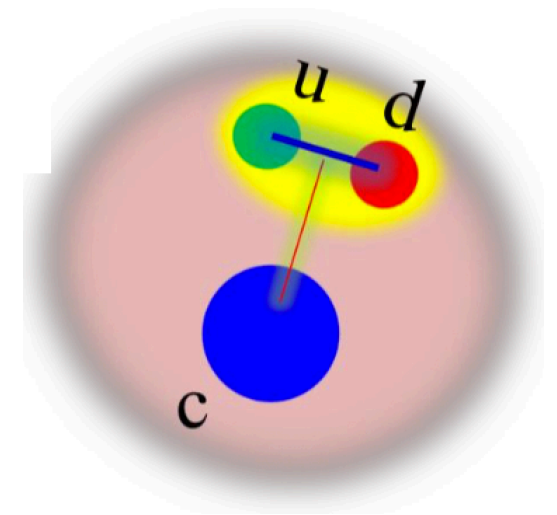
$$\tau_{\Xi_c^+} = 456.8 \pm 3.5 \pm 2.9 \pm 3.1 \text{ fs},$$

$$\tau_{\Xi_c^0} = 154.5 \pm 1.7 \pm 1.6 \pm 1.0 \text{ fs}, \quad 3.3 \sigma \text{ larger}$$

LHCb, 1906.08350

Theory issues of charmed baryon

- Meaning of weak decays of charmed baryon
 - Examination of weak interaction
 - Exploration of strong interaction
- Difficulty in charmed baryon study
 - heavy to apply ChPT
 - light to apply HQET
 - **Model estimation** cannot avoid



BF of Cabbibo-favored decays in 1990s

	RQM	Pole	Pole		RQM	Pole	C.A.		
Decay	Körner, Krämer [8]	Xu, Kamal [9]	Cheng, Tseng [10]	CA	Pole	Ivanov et al [11]	Żenczykowski [12]	Sharma, Verma [13]	Expt. [7]
$\Lambda_c^+ \rightarrow \Lambda \pi^+$	input	1.62	1.46	0.88	0.79	0.52	1.12	1.30 ± 0.07	
$\Lambda_c^+ \rightarrow p \bar{K}^0$	input	1.20	3.64	1.26	2.06	1.71	1.64	3.16 ± 0.16	
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	0.32	0.34	1.76	0.72	0.88	0.39	1.34	1.29 ± 0.07	
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	0.32	0.34	1.76	0.72	0.88	0.39	1.34	1.24 ± 0.10	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.16				0.11	0.90	0.57	0.70 ± 0.23	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	1.28				0.12	0.11	0.10		
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	0.26	0.10			0.31	0.34	0.13	0.50 ± 0.12	

- Non-factorizable contributions play an essential role
 - $\Lambda_c^+ \rightarrow \Xi^0 K^+$: only proceed through W-exchange
 - $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0, \Sigma^+ \eta, \Sigma^+ \eta'$: proceed through W-exchange or internal W-emission
- Except current algebra, predictions are generally below experiment

BF of Cabbibo-favored decays in 1990s

Decay	RQM	Pole	Pole		RQM	Pole	C.A.	Expt. [6]
	Körner, Krämer [16]	Xu, Kamal [18]	Cheng, Tseng [19] CA	Pole	Ivanov et al [17]	Żenczykowski [20]	Sharma, Verma [21]	
$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	6.45	0.44	0.04	0.84	3.08	1.56	0.04	
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	3.54	3.36	0.84	3.93	4.40	1.59	0.53	1.57 ± 0.83
$\Xi_c^0 \rightarrow \Lambda \bar{K}^0$	0.12	0.37	1.0	0.27	0.42	0.35	0.54	
$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	1.18	0.10	0.02	0.13	0.20	0.11	0.07	
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	0.12	0.12			0.27	0.36	0.12	
$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	0.03	0.56	1.25	0.28	0.04	0.69	0.87	
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	1.04	1.74	0.83	1.25	1.22	0.61	2.46	1.80 ± 0.52
$\Xi_c^0 \rightarrow \Xi^0 \eta$	0.24				0.28	0.69	0.09	
$\Xi_c^0 \rightarrow \Xi^0 \eta'$	0.85				0.31	0.01	0.14	

new

new

- No channel contains pure factorizable contributions
- Nonfactorizable contributions play an essential role
 - $\Xi_c^0 \rightarrow \Sigma^+ K^-$, $\Xi_c^0 \rightarrow \Xi^0 \pi^0$, $\Xi_c^0 \rightarrow \Xi^0 \eta$: only contain nonfactorizable contribution
 - Others contain both two parts of contributions

Decay asymmetry α of Cabibbo-favored decays in 1990s

	RQM	Pole	Pole	RQM	Pole	C.A.		
Decay	Körner, Krämer [8]	Xu, Kamal [9]	Cheng, Tseng [10] CA Pole	Ivanov et al [11]	Żenczykowski [12]	Sharma, Verma [13]	Expt. [7]	BESIII
✓ $\Lambda_c^+ \rightarrow \Lambda \pi^+$	-0.70	-0.67	-0.99	-0.95	-0.99	-0.99	-0.91 ± 0.15	$-0.80 \pm 0.11 \pm 0.02$
$\Lambda_c^+ \rightarrow p \bar{K}^0$	-1.0	0.51	-0.90	-0.49	-0.97	-0.66	-0.99	
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	0.70	0.92	-0.49	0.78	0.43	0.39	-0.31	$-0.73 \pm 0.17 \pm 0.07$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	0.70	0.92	-0.49	0.78	0.43	0.39	-0.45 ± 0.32	$-0.57 \pm 0.10 \pm 0.07$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.33				0.55	0	-0.91	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	-0.45				-0.05	-0.91	0.78	
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	0	0			0	0	0	

■ $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$

- CLEO ('95) measured $\alpha = -0.45 \pm 0.31 \pm 0.06$
- Pole model & RQM predict positive α
- Current algebra leads to negative α
- The sign of α has been confirmed by BESIII

■ $\Lambda_c^+ \rightarrow \Xi^0 K^+$

- theory: small s-wave $\Rightarrow \alpha = 0$
 - Can be improved
- Experiment ?

BESIII, PLB 783 (2018), 200-206

Decay asymmetry α of Cabibbo-favored decays in 1990s

Decay	RQM	Pole	Pole		RQM	Pole	C.A.	Expt. [6]
	Körner, Krämer [16]	Xu, Kamal [18]	Cheng, Tseng [19] CA	Pole	Ivanov et al [17]	Żenczykowski [20]	Sharma, Verma [21]	
$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	-1.0	0.24	0.43	-0.09	-0.99	1.0	0.54	
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	-0.78	-0.81	-0.77	-0.77	-0.97	1.0	-0.27	
$\Xi_c^0 \rightarrow \Lambda \bar{K}^0$	-0.76	1.00	-0.88	-0.73	-0.75	-0.29	-0.79	
$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	-0.96	-0.99	0.85	-0.59	-0.55	-0.50	0.48	
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	0	0			0	0	0	
$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	0.92	0.92	-0.78	-0.54	0.94	0.21	-0.80	
✓ $\Xi_c^0 \rightarrow \Xi^- \pi^+$	-0.38	-0.38	-0.47	-0.99	-0.84	-0.79	-0.97	-0.6 ± 0.4
$\Xi_c^0 \rightarrow \Xi^0 \eta$	-0.92				-1.0	0.21	-0.37	
$\Xi_c^0 \rightarrow \Xi^0 \eta'$	-0.38				-0.32	-0.04	0.56	

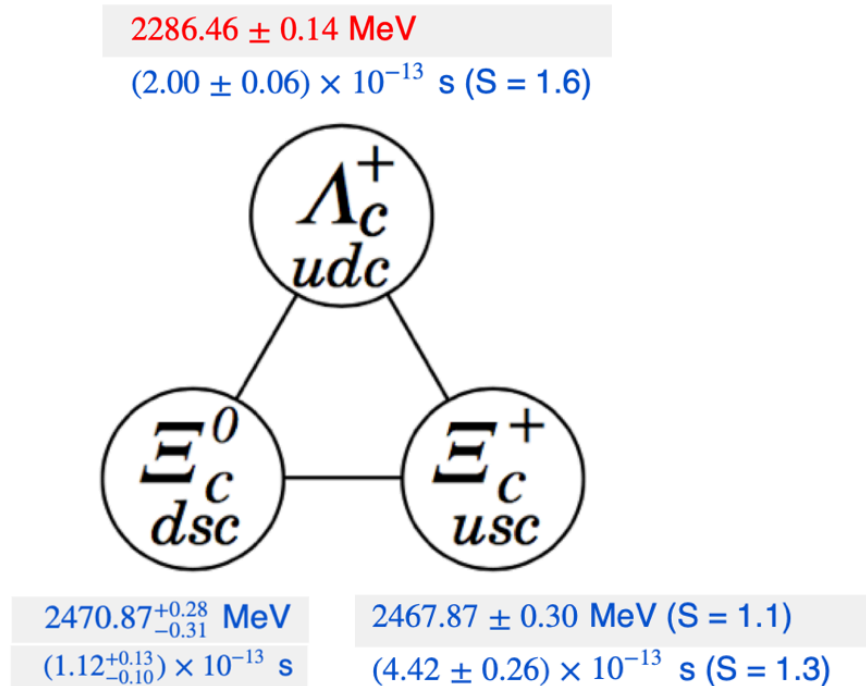
■ $\Xi_c^+ \rightarrow \Xi^- \pi^+$:

- CLEO ('96) measured $\alpha = -0.6 \pm 0.4$
- All model estimations predict correct sign of α

■ Could Belle/Belle II provide α measurement ?

Our strategy

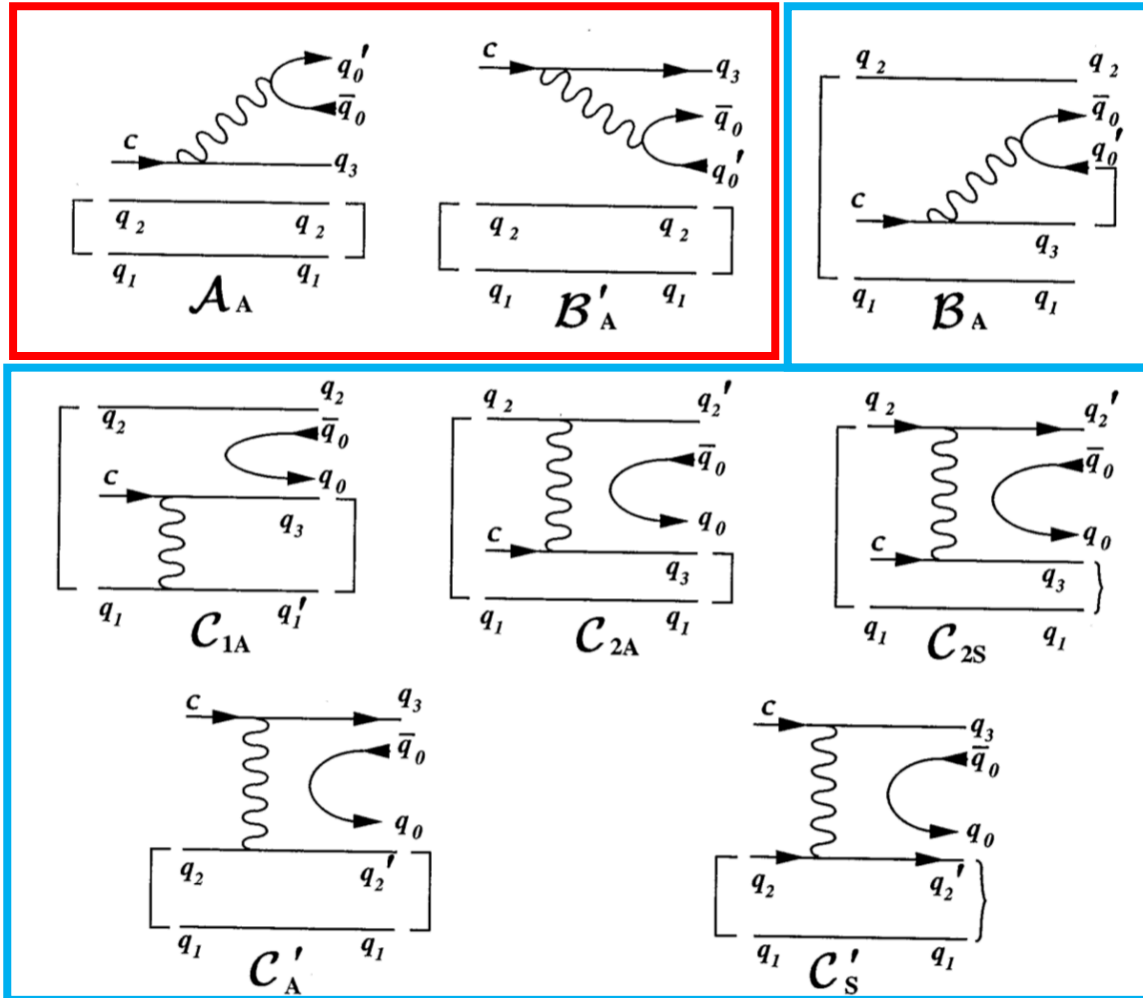
- Non-factorizable contribution is incorporated
- Methodology: Pole model + current algebra





Theoretical framework

Topological diagram approach



$$M(\mathcal{B}_i \rightarrow \mathcal{B}_f P) = i\bar{u}_f(A - B\gamma_5)u_i$$

$$A = A^{\text{fac}} + A^{\text{nf}}$$

$$B = B^{\text{fac}} + B^{\text{nf}}$$

Factorizable part: naïve factorization

$$A^{\text{fac.}} = \frac{G_F}{\sqrt{2}} a_{1,2} V_{ud}^* V_{cs} f_P (m_{\mathcal{B}_c} - m_{\mathcal{B}}) f_1(q^2)$$

$$B^{\text{fac.}} = -\frac{G_F}{\sqrt{2}} a_{1,2} V_{ud}^* V_{cs} f_P (m_{\mathcal{B}_c} + m_{\mathcal{B}}) g_1(q^2)$$

- The choice of $a_{1,2}$ depends on the meson in final states
- Effective N_c included in $a_{1,2}$ is determined by experiment

$$a_2 = c_2 + \frac{c_1}{N_c}$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\phi) = (1.04 \pm 0.21) \times 10^{-3}$$



$$N_c^{\text{eff}} \approx 7$$

BESIII, Phys. Rev. Lett. 117, 232002 (2016).

Factorizable part: form factor

- FF sign issue
- MIT bag model estimation

Static limit

$$f_1^{B_f B_i}(q_{\max}^2) = \langle B_f \uparrow | b_{q_1}^\dagger b_{q_2} | B_i \uparrow \rangle \int d^3 \mathbf{r} (u_{q_1} u_{q_2} + v_{q_1} v_{q_2})$$

$$g_1^{B_f B_i}(q_{\max}^2) = \langle B_f \uparrow | b_{q_1}^\dagger b_{q_2} \sigma_z | B_i \uparrow \rangle \int d^3 \mathbf{r} (u_{q_1} u_{q_2} - \frac{1}{3} v_{q_1} v_{q_2})$$

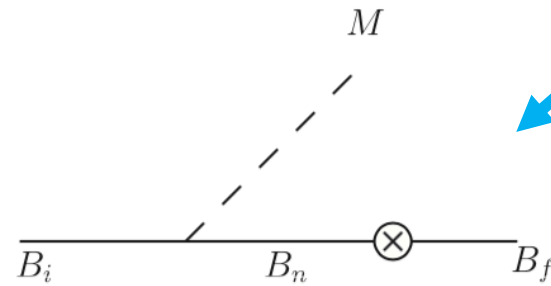
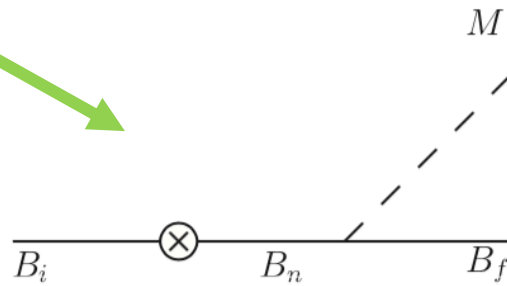
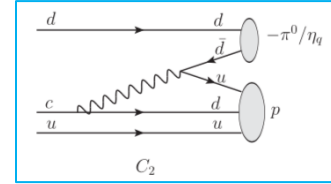
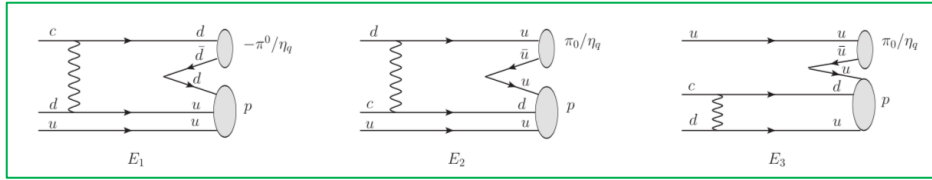
Run

$$f_i(q^2) = \frac{f_i(0)}{(1 - q^2/m_V^2)^2}, \quad g_i(q^2) = \frac{g_i(0)}{(1 - q^2/m_A^2)^2}$$

- More efforts on FF required

modes	$(c\bar{q})$	$f_1(q_{\max}^2)$	$f_1(m_P^2)/f_1(q_{\max}^2)$	$g_1(q_{\max}^2)$	$g_1(m_P^2)/g_1(q_{\max}^2)$
$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	$(c\bar{s})$	$-\frac{\sqrt{6}}{2} Y_1$	0.44907	$-\frac{\sqrt{6}}{2} Y_2$	0.60286
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	$(c\bar{s})$	$-\frac{\sqrt{6}}{2} Y_1^s$	0.49628	$-\frac{\sqrt{6}}{2} Y_2^s$	0.63416
$\Xi_c^0 \rightarrow \Lambda \bar{K}^0$	$(c\bar{s})$	$\frac{1}{2} Y_1$	0.38700	$\frac{1}{2} Y_2$	0.55337
$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	$(c\bar{s})$	$\frac{\sqrt{3}}{2} Y_1$	0.44929	$\frac{\sqrt{3}}{2} Y_2$	0.60304
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	$(c\bar{s})$	$-\frac{\sqrt{6}}{2} Y_1^s$	0.49911	$-\frac{\sqrt{6}}{2} Y_2^s$	0.63636
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	$(c\bar{d})$	$\frac{\sqrt{3}}{2} Y_1$	0.36045	$\frac{\sqrt{3}}{2} Y_2$	0.52523
$\Xi_c^+ \rightarrow \Lambda \pi^+$	$(c\bar{d})$	$-\frac{1}{2} Y_1$	0.30260	$-\frac{1}{2} Y_2$	0.47622
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	$(c\bar{d})$	$-\frac{\sqrt{6}}{2} Y_1$	0.35774	$-\frac{\sqrt{6}}{2} Y_2$	0.52294
$\Xi_c^+ \rightarrow \Sigma^+ \eta_8$	$(c\bar{d})$	$-\frac{\sqrt{6}}{2} Y_1$	0.41371	$-\frac{\sqrt{6}}{2} Y_2$	0.57735
$\Xi_c^+ \rightarrow \Xi^0 K^+$	$(c\bar{s})$	$-\frac{\sqrt{6}}{2} Y_1^s$	0.55058	$-\frac{\sqrt{6}}{2} Y_2^s$	0.68080
$\Xi_c^0 \rightarrow \Lambda \eta_8$	$(c\bar{s}), (c\bar{d})$	$\frac{1}{2} Y_1$	0.39685, 0.34715	$\frac{1}{2} Y_2$	0.56286, 0.52343
$\Xi_c^0 \rightarrow \Sigma^0 \eta_8$	$(c\bar{s}), (c\bar{d})$	$\frac{\sqrt{3}}{2} Y_1$	0.46073, 0.41395	$\frac{\sqrt{3}}{2} Y_2$	0.61338, 0.57754
$\Xi_c^0 \rightarrow \Lambda \pi^0$	$(c\bar{d})$	$\frac{1}{2} Y_1$	0.30019	$\frac{1}{2} Y_2$	0.47410
$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	$(c\bar{d})$	$\frac{\sqrt{3}}{2} Y_1$	0.35795	$\frac{\sqrt{3}}{2} Y_2$	0.52311
$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	$(c\bar{d})$	$\frac{\sqrt{6}}{2} Y_1$	0.36183	$\frac{\sqrt{6}}{2} Y_2$	0.52638
$\Xi_c^0 \rightarrow \Xi^- K^+$	$(c\bar{s})$	$-\frac{\sqrt{6}}{2} Y_1^s$	0.55371	$-\frac{\sqrt{6}}{2} Y_2^s$	0.68316

Non-factorizable part: pole model



S-wave: $1/2^-$:

$$A^{\text{pole}} = - \sum_{B_n^*(1/2^-)} \left[\frac{g_{B_f B_n^*} P b_{n^* i}}{m_i - m_{n^*}} + \frac{b_{f n^*} g_{B_n^* B_i} P}{m_f - m_{n^*}} \right]$$

P-wave: $1/2^+$:

$$B^{\text{pole}} = \sum_{B_n} \left[\frac{g_{B_f B_n} P a_{n i}}{m_i - m_n} + \frac{a_{f n} g_{B_n B_i} P}{m_f - m_n} \right].$$

$$\langle \mathcal{B}_i | H_{\text{eff}} | \mathcal{B}_j \rangle = \bar{u}_i (a_{ij} - b_{ij} \gamma_5) u_j, \quad \langle \mathcal{B}_i^*(1/2^-) | H_{\text{eff}}^{\text{PV}} | \mathcal{B}_j \rangle = i b_{i^* j} \bar{u}_i u_j.$$

Non-factorizable part: current algebra

- Advance: avoid $\frac{1}{2}^-$

$$A^{\text{com}} = -\frac{\sqrt{2}}{f_{P^a}} \langle B_f | [Q_5^a, H_{\text{eff}}^{PV}] | B_i \rangle = \frac{\sqrt{2}}{f_{P^a}} \langle B_f | [Q^a, H_{\text{eff}}^{PC}] | B_i \rangle$$

$$B^{\text{pole}} = \frac{\sqrt{2}}{f_{P^a}} \sum_{B_n} \left[g_{B_f B_n}^A \frac{m_f + m_n}{m_i - m_n} a_{ni} + a_{fn} \frac{m_i + m_n}{m_f - m_n} g_{B_n B_i}^A \right]$$

- S-wave: commutator

$$A^{\text{com}}(B_i \rightarrow B_f K^\pm) = \frac{1}{f_K} \langle B_f | [V_\mp, H_{\text{eff}}^{PC}] | B_i \rangle$$



- P-wave: generalized Goldberg-Treinman relation

$$g_{B' B P^a} = \frac{\sqrt{2}}{f_{P^a}} (m_{B'} + m_B) g_{B' B}^A$$

$$\begin{aligned} V_+ \Lambda &= -\frac{\sqrt{6}}{2} p \\ V_+ \Sigma^0 &= -\frac{\sqrt{2}}{2} p \\ V_+ \Xi^- &= -\frac{\sqrt{2}}{2} \Sigma^0 - \frac{\sqrt{6}}{2} \Lambda \end{aligned}$$

Baryon matrix elements & axial form factors

- MIT bag model estimation

$$a_{B'B} \equiv \langle B' | \mathcal{H}_{\text{eff}}^{\text{PC}} | B \rangle = \frac{G_F}{2\sqrt{2}} \sum_{q=d,s} V_{cq} V_{uq}^* c_- \langle B' | O_-^q | B \rangle$$

$$O_{\pm}^q = O_1^q \pm O_2^q = (\bar{q}c)(\bar{u}q) \pm (\bar{q}q)(\bar{u}c)$$

$$c_- = c_1 - c_2$$

$$g_{B'B}^{A(P)} = \langle B' \uparrow | b_{q_1}^\dagger b_{q_2} \sigma_z | B \uparrow \rangle \int d^3\mathbf{r} \left(u_{q_1} u_{q_2} - \frac{1}{3} v_{q_1} v_{q_2} \right)$$

Hard working ...



Results for anti-triplet decays

Λ_c^+ decays

TABLE II. The predicted S - and P -wave amplitudes of singly Cabibbo-suppressed decays $\Lambda_c^+ \rightarrow \mathcal{B} + P$ in units of $G_F 10^{-2} \text{ GeV}^2$. Branching fractions and the asymmetry parameter α are shown in the last three columns. Experimental results are taken from [7,19].

Channel	A^{fac}	A^{com}	A^{tot}	B^{fac}	B^{ca}	B^{tot}	$\mathcal{B}_{\text{theo}}$	$\mathcal{B}_{\text{expt}}$	α_{theo}
$\Lambda_c^+ \rightarrow p\pi^0$	-0.41	0.81	0.40	0.87	-1.57	-0.70	0.75×10^{-4}	$< 2.7 \times 10^{-4}$	-0.95
$\Lambda_c^+ \rightarrow p\eta$	<u>0.96</u>	<u>1.11</u>	2.08	-1.93	-1.24	-3.17	1.28×10^{-3}	$(1.24 \pm 0.29) 10^{-3}$	-0.56
$\Lambda_c^+ \rightarrow n\pi^+$	<u>-1.64</u>	<u>1.15</u>	-0.50	3.45	-1.57	1.88	2.66×10^{-4}		-0.90
$\Lambda_c^+ \rightarrow \Lambda K^+$	-1.66	0.09	-1.57	4.43	-0.54	3.70	1.06×10^{-3}	$(6.1 \pm 1.2) 10^{-4}$	-0.96
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	0	-1.48	-1.48	0	2.30	2.30	7.18×10^{-4}	$(5.2 \pm 0.8) 10^{-4}$	-0.73
$\Lambda_c^+ \rightarrow \Sigma^+ K^0$	0	-2.10	-2.10	0	3.25	3.25	1.44×10^{-3}		-0.74

- $\Lambda_c^+ \rightarrow p\pi^0, \Lambda_c^+ \rightarrow p\eta$: consistent well with BESIII experiment
- $\Lambda_c^+ \rightarrow n\pi^+$: wait for new result from BESIII
- $\Lambda_c^+ \rightarrow \Lambda K^+$: may resort to form factor

Ξ_c decays: CF

TABLE III. The Cabibbo-favored decays $\Xi_c \rightarrow \mathcal{B}_f P$ in units of $10^{-2} G_F \text{GeV}^2$. Branching fractions (in percent) and the up-down spin asymmetry α in theory and experiment are shown in the last four columns.

Channel	A^{fac}	A^{com}	A^{tot}	B^{fac}	B^{ca}	B^{tot}	$\mathcal{B}_{\text{theo}}$	\mathcal{B}_{exp}	α_{theo}	α_{exp}
$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	2.98	-4.42	-1.44	-9.95	12.33	2.38	0.18	—	-0.83	—
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	-7.41	5.43	-1.98	28.07	-13.97	14.11	1.66	1.57 ± 0.83	-0.76	—
$\Xi_c^0 \rightarrow \Lambda \bar{K}^0$	-1.11	-5.49	-6.60	3.66	6.70	10.36	0.98	—	-0.85	—
$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	-2.11	3.17	1.06	7.05	-9.36	-2.30	0.03	—	-0.94	—
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	0	-0.06	-0.06	0	-11.48	-11.48	0.24	—	0.03	—
$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	0	-7.68	-7.68	0	11.77	11.77	1.36	—	-0.76	—
$\Xi_c^0 \rightarrow \Xi^0 \eta_8$	0	-10.95	-10.95	0	-5.99	-5.99	2.00	—	0.29	—
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	-7.42	-5.43	-12.85	28.24	2.68	30.92	4.77	1.80 ± 0.52	-0.95	-0.6 ± 0.4

$\Xi_c^+ \rightarrow \Xi^0 \pi^+$: consistent well with Belle experiment

$\Xi_c^0 \rightarrow \Xi^- \pi^+$: has a tension with Belle experiment

Comparison of FF

TABLE VI. MBM predictions for the bare form factors evaluated at $q^2=0$ of the $c \rightarrow s$ decays. The upper value corresponds to monopole approximation and the lower one to dipole approximation.

$B_1 \rightarrow B_2 + e + \nu_e$	f_1	f_2	f_3	g_1	g_2	g_3
$\Xi_{cc}^{++} \rightarrow \Xi_c^{A+}$	0.97	-0.06	-0.45	0.28	-0.01	-0.92
	0.68	-0.04	-0.32	0.22	-0.00	-0.73
$\Xi_{cc}^{++} \rightarrow \Xi_c^+$	0.48	1.19	-0.02	0.79	-0.02	-2.64
	0.34	0.84	-0.02	0.63	-0.02	-2.08
$\Xi_{cc}^+ \rightarrow \Xi_c^0$	0.52	1.29	-0.06	0.84	0.03	-2.83
	0.39	0.97	-0.04	0.70	0.03	-2.34
$\Omega_{cc}^+ \rightarrow \Omega_c^0$	0.75	1.94	-0.11	1.20	0.06	-4.51
	0.56	1.46	-0.08	0.99	0.05	-3.72
$\Xi_{cc}^+ \rightarrow \Xi_c^{A0}$	0.97	-0.06	-0.45	0.28	-0.01	-0.92
	0.68	-0.04	-0.32	0.22	-0.00	-0.73
$\Sigma_c^0 \rightarrow \Sigma^-$	0.80	-0.78	-0.37	-0.20	0.03	0.22
	0.51	-0.50	-0.24	-0.15	0.02	0.16
$\Xi_c^0 \rightarrow \Xi^-$	0.57	-0.56	-0.27	-0.14	0.02	0.18
	0.38	-0.37	-0.18	-0.11	0.01	0.14
$\Xi_c^{A0} \rightarrow \Xi^-$	0.84	0.44	-0.04	0.80	-0.07	-0.93
	0.59	0.31	-0.03	0.63	-0.05	-0.74
$\Lambda_c^+ \rightarrow \Lambda$	0.66	0.27	0.00	0.64	-0.07	-0.56
	0.46	0.19	0.00	0.50	-0.05	-0.44
$\Xi_c^{A+} \rightarrow \Xi^0$	0.84	0.44	-0.04	0.80	-0.07	-0.93
	0.58	0.31	-0.03	0.63	-0.05	-0.73
$\Sigma_c^+ \rightarrow \Sigma^0$	0.80	-0.78	-0.37	-0.20	0.03	0.22
	0.52	-0.50	-0.24	-0.15	0.02	0.16
$\Xi_c^+ \rightarrow \Xi^0$	0.61	-0.58	-0.28	-0.15	0.01	0.18
	0.43	-0.41	-0.20	-0.12	0.01	0.14
$\Sigma_c^{++} \rightarrow \Sigma^+$	0.80	-0.78	-0.37	-0.20	0.03	0.21
	0.52	-0.50	-0.24	-0.15	0.02	0.16

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Ξ_c decays: SCS

TABLE IV. The singly Cabibbo-suppressed decays $\Xi_c \rightarrow \mathcal{B}_f P$ in units of $10^{-2} G_F \text{GeV}^2$. Branching fractions (in unit of 10^{-4}) and the asymmetry parameter α are shown in the last three columns.

Channel	A^{fac}	A^{com}	A^{tot}	B^{fac}	B^{ca}	B^{tot}	$\mathcal{B}_{\text{theo}}$	$\mathcal{B}_{\text{expt}}$	α_{theo}
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	-0.90	-0.99	-1.89	3.29	0.76	4.05	41.59	—	-0.96
$\Xi_c^+ \rightarrow \Lambda \pi^+$	0.46	-1.52	-1.05	-1.69	2.16	0.47	8.50	—	-0.33
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	1.27	0.99	2.26	-4.63	1.59	-3.04	46.67	—	-0.77
$\Xi_c^+ \rightarrow p \bar{K}^0$	0	-2.10	-2.10	0	2.63	2.63	38.02	—	-0.84
$\Xi_c^+ \rightarrow \Sigma^+ \eta_8$	-0.74	1.41	0.67	2.58	-2.21	0.37	3.02	—	0.34
$\Xi_c^+ \rightarrow \Xi^0 K^+$	0.82	1.15	1.97	-3.00	-6.14	-9.14	68.72	—	-0.97
$\Xi_c^0 \rightarrow \Lambda \eta_8$	0.27	1.53	1.80	-0.94	-1.54	-2.48	6.72	—	-0.78
$\Xi_c^0 \rightarrow \Sigma^0 \eta_8$	0.53	-1.00	-0.47	-1.83	-0.81	-2.64	1.55	—	0.85
$\Xi_c^0 \rightarrow \Lambda \pi^0$	-0.46	1.07	0.61	1.68	-0.95	0.73	0.85	—	0.75
$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	-0.90	-0.70	-1.60	3.28	1.37	4.65	9.82	—	-1.00
$\Xi_c^0 \rightarrow \Xi^0 K^0$	0	2.11	2.11	0	-4.16	-4.16	9.73	—	-0.84
$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	-1.28	-1.40	-2.68	4.67	0.24	4.91	19.13	—	-0.90
$\Xi_c^0 \rightarrow \Xi^- K^+$	0.82	-0.96	-0.14	-3.02	0.69	-2.33	0.73	—	0.40
$\Xi_c^0 \rightarrow p K^-$	0	-0.01	-0.01	0	-1.88	-1.88	1.11	—	0.025
$\Xi_c^0 \rightarrow n \bar{K}^0$	0	-2.11	-2.11	0	2.94	2.94	10.26	—	-0.88
$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$	0	0	0	0	2.50	2.50	1.43	—	0

$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$: vanished α ; only nonfactorizable p-wave amplitudes contributes.

Summary

- Weak decays of anti-triplet of charmed baryons are predicted.
- The sign of form factors can be discriminated.
- Several Λ_c^+ decays are in agreement with BESIII.
- One mode of Ξ_c^+ decay agree well with Belle, tension exists in Ξ_c^0 decay.
- Wait for more BESIII data to examine Λ_c^+ decay theory.

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