

(Semi-)leptonic charm decays at BESIII

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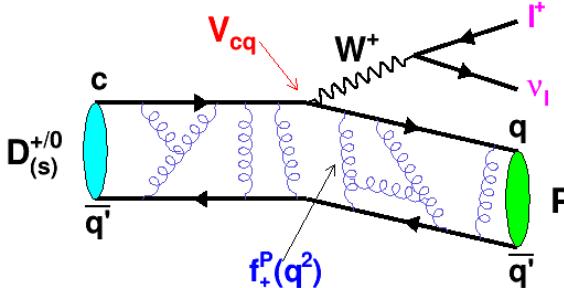
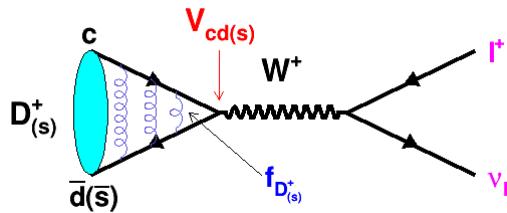
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Introduction

$c \rightarrow s/d e^+ \nu$ 跃迁中强、弱作用能够很好分离



$$\Gamma(D_{(s)}^+ \rightarrow l^+ \bar{\nu}_l) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

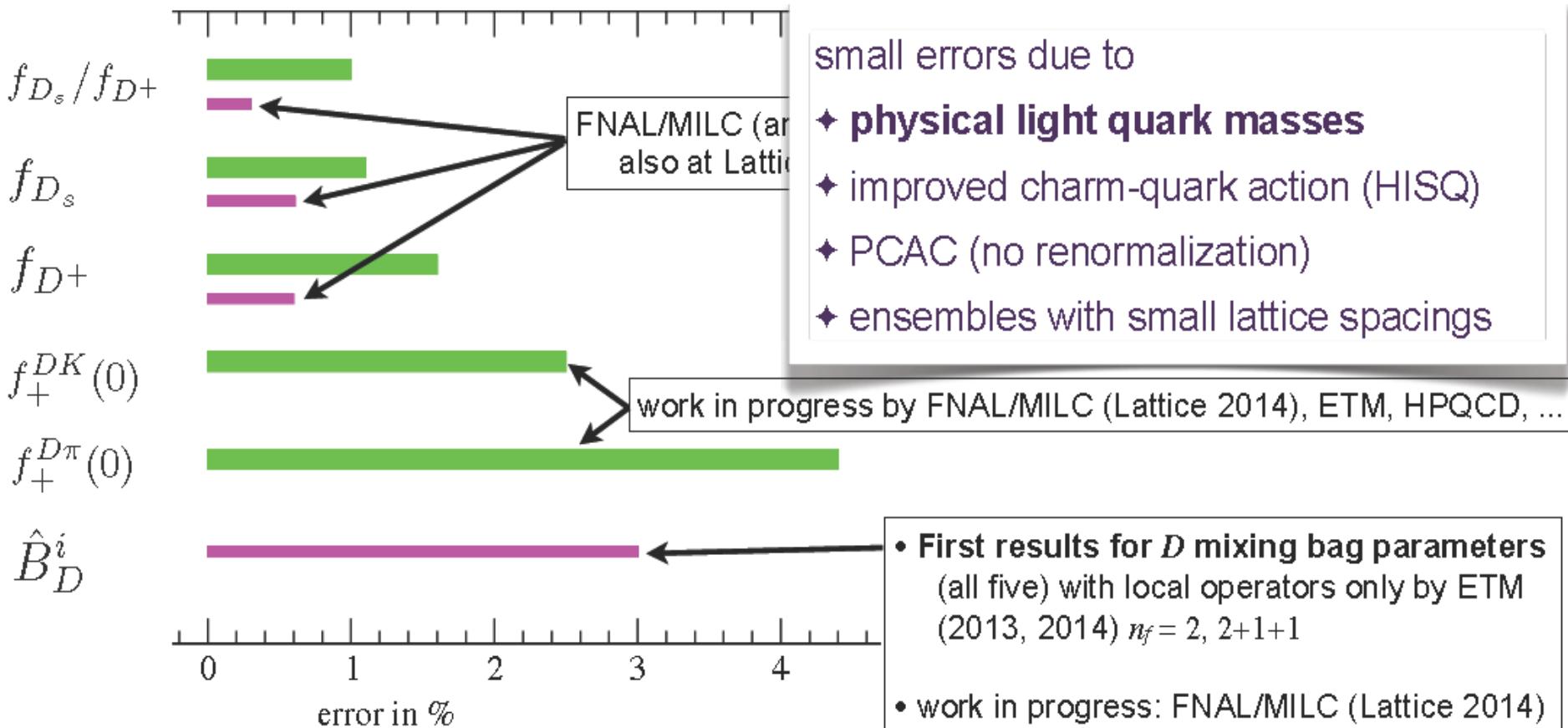
$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

状态: 2001年, $|V_{cs(d)}|$ 精度7(16)%。人们寄望D半轻衰变精密测量 $|V_{cs(d)}|$ 。至2012年, 精度大约2.5(4.8)%。但长期以来, 半轻测量受制于LQCD对形状因子计算精度。

- 测定CKM矩阵元 $|V_{cs}|$ 和 $|V_{cd}| \rightarrow$ 检验CKM矩阵幺正性
- 测定衰变常数 $f_{D(s)+}$, 形状因子 $f_+^{D \rightarrow h}(0) \dots \rightarrow$ 检验LQCD计算
- 测定(微分)衰变率 \rightarrow 检验 $e-\mu$ 和 $\mu-\tau$ 轻子普适性
- 寻找 $D \rightarrow S e \bar{\nu}$ 或 $A e \bar{\nu}$ \rightarrow 探讨标量介子S和轴矢量介子A性质

Progress of LQCD before BESIII

errors (in %) comparison: **FLAG-2 averages** vs. **new results**



review by C. Bouchard @ Lattice 2014

■ 2018年, FNAL/MILC对 $f_{D(s)}$ 计算精度达到0.2%

Recent $D^0(+)$, D_s^+ and Λ_c^+ samples

Taking from Longke Li's talk at joint workshop of BESIII/Belle/LHCb at Nankai

Experiment	Machine	C.M	Lumin.	$N(D)$	efficiency	advantage/disadvantage	
	CLEO (e^+e^-)	3.77 GeV	0.8 fb^{-1}	2.9×10^6	$\sim 10\text{-}30\%$	<ul style="list-style-type: none"> ⊕ extremely clean environment ⊕ pure D-beam, almost no bkg ⊕ quantum coherence ⊖ no CM boost, no T-dep analyses 	
		4.17 GeV	0.6 fb^{-1}	$2.3 \times 10^6 (D^\pm)$			
	BEPC-II (e^+e^-)	3.77 GeV	2.92 fb^{-1}	0.6×10^6			
		4.18 GeV	3 fb^{-1}	10.5×10^6			
		4.6 GeV	0.567 fb^{-1}	$8.4 \times 10^6 D_0^+$			
				D_s^+			
				3×10^6			
				Λ_c^+			
				★		★★★	
	KEKB (e^+e^-)	10.58 GeV	1 ab^{-1}	1.3×10^9	$\sim 5\text{-}10\%$	<ul style="list-style-type: none"> ⊕ clear event environment ⊕ high trigger efficiency ⊕ high-efficiency detection of neutrals ⊕ many high-statistics control samples ⊕ time-dependent analysis ⊖ smaller cross-section than pp colliders 	
		10.58 GeV	0.5 ab^{-1}	6.5×10^8			
	PEP-II (e^+e^-)			★★		★★	
	Tevatron ($p\bar{p}$)	1.96 TeV	9.6 fb^{-1}	1.3×10^{11}	<0.5%	<ul style="list-style-type: none"> ⊕ large production cross-section ⊕ large boost: excellent time resolution ⊖ dedicated trigger required ⊖ hard to do neutrals and neutrinos 	
		7 TeV	1.0 fb^{-1}	5.0×10^{12}			
	LHC (pp)	8 TeV	2.0 fb^{-1}				
				★★★	★		

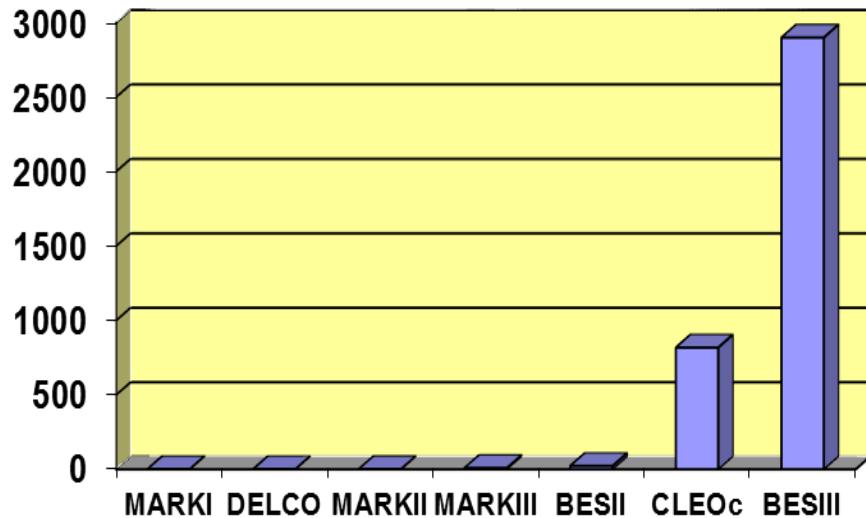
■ CLEOc, Belle和BaBar实验开展了粲介子纯轻半轻衰变测量

世界上最大的近阈粲强子样本

■ 2010-2011年: 2.9 fb^{-1} @3.773 GeV

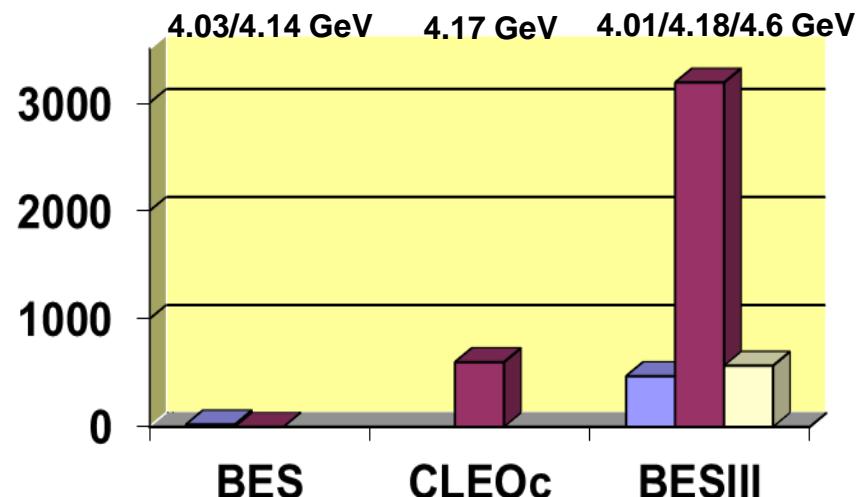
D^0 、 D^+

约11月

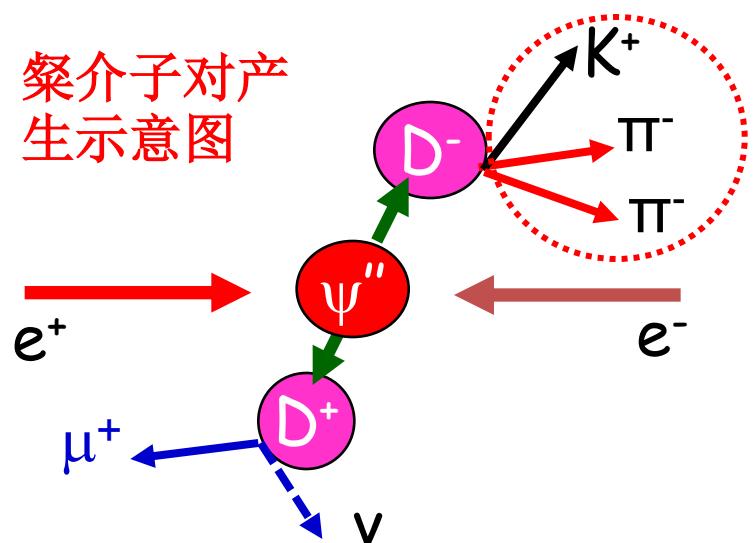


■ 2014年: 0.6 fb^{-1} @4.6 GeV Λ_c^+

■ 2016年: 3.2 fb^{-1} @4.18 GeV D_s^+



粲介子对产生示意图



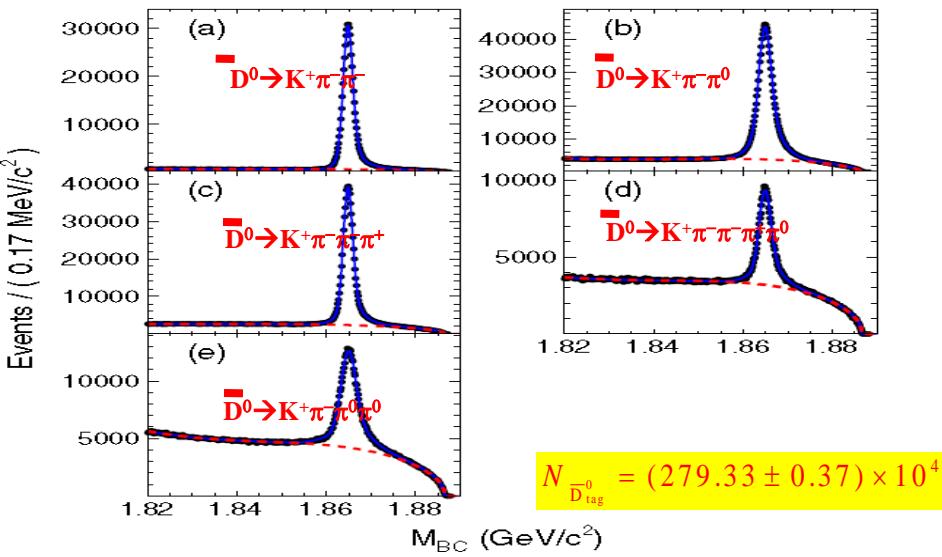
优势: 产额大、背景低、系统误差小, 可测量绝对分支比

$$B_{\text{sig}} = \frac{N_{\text{DT}}^{\text{tot}}}{N_{\text{ST}}^{\text{tot}} \times \bar{\epsilon}_{\text{sig}}}$$

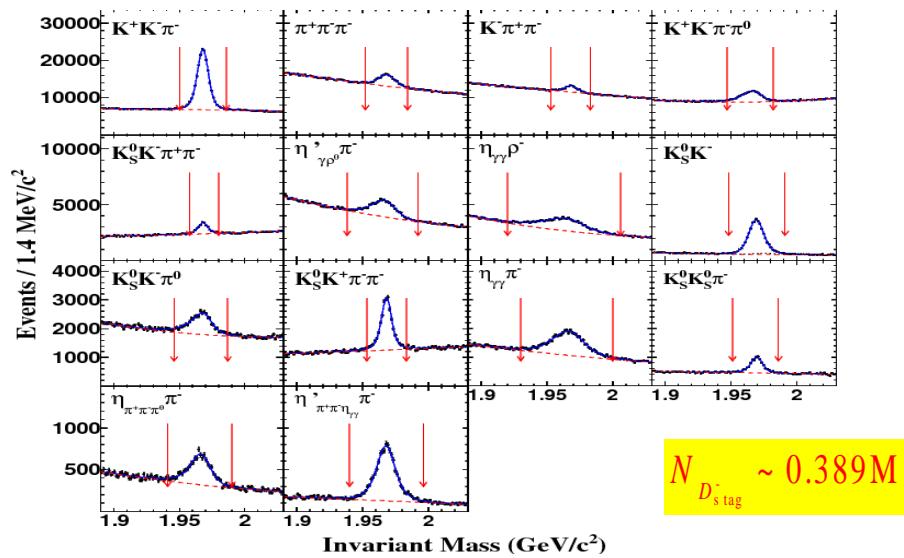
■ BESIII实验研究需增加统计量、发挥近阈优势、改进系统误差

单标记 $D^0(+)$ 、 D_s^+ 和 Λ_c^+ 样本

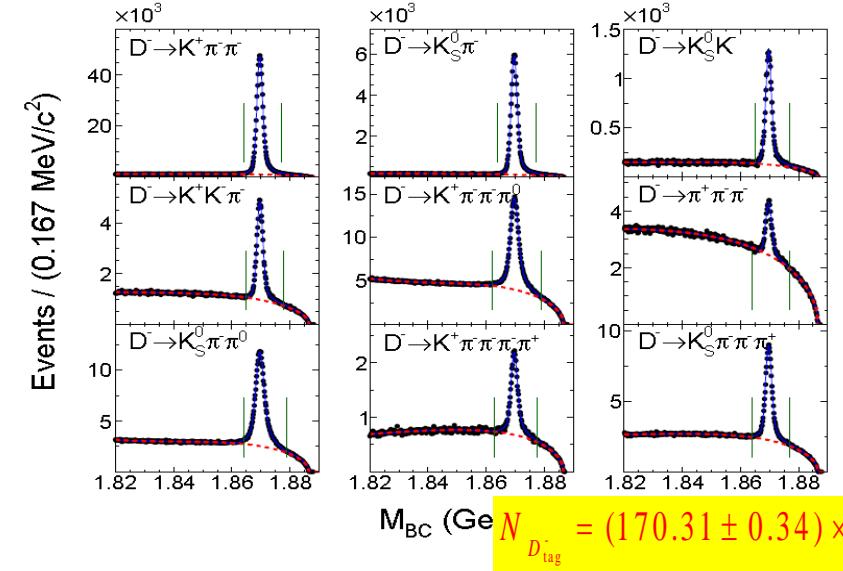
$e^+e^- \rightarrow D^0\bar{D}^0 @ 3.773 \text{ GeV}$



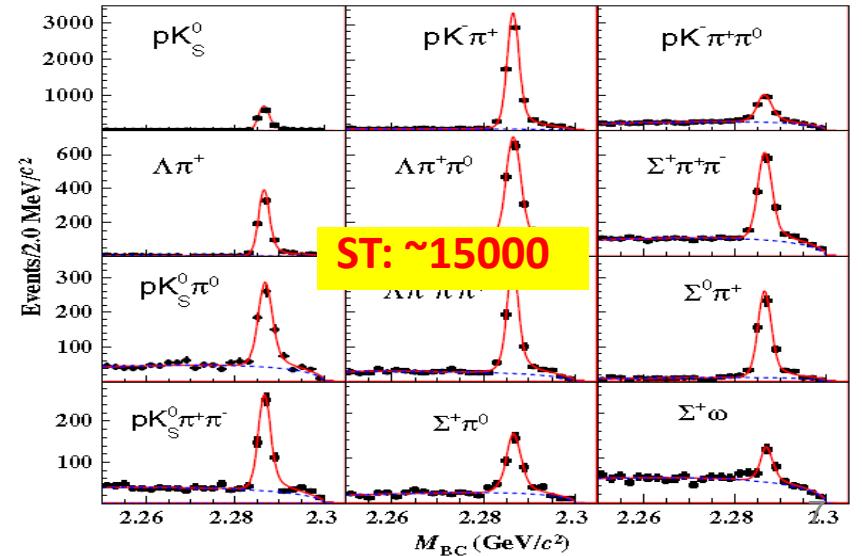
$e^+e^- \rightarrow D_s^{*+}D_s^- + \text{c.c.} @ 4.18 \text{ GeV}$



$e^+e^- \rightarrow D^+D^- @ 3.773 \text{ GeV}$

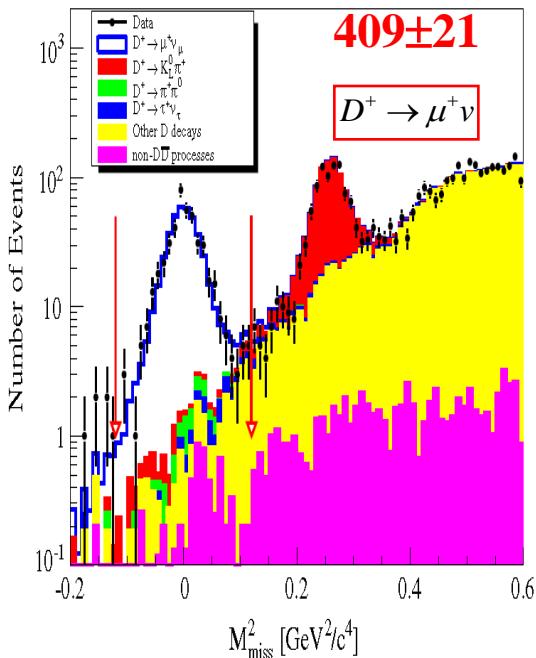


$e^+e^- \rightarrow \Lambda_s^+\Lambda_s^- + \text{c.c.} @ 4.18 \text{ GeV}$



纯轻衰变 $D^+ \rightarrow l^+ \nu$ 研究

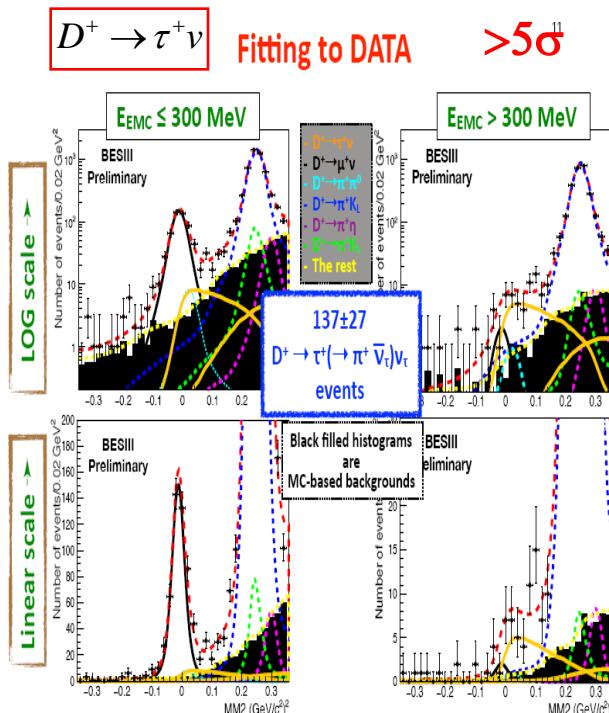
PRD89(2014)051104



$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} |V_{cd}| = 46.7 \pm 1.2 \pm 0.4 \text{ MeV}$$

BESIII初步结果



$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24_{\text{stat}}) \times 10^{-3}$$

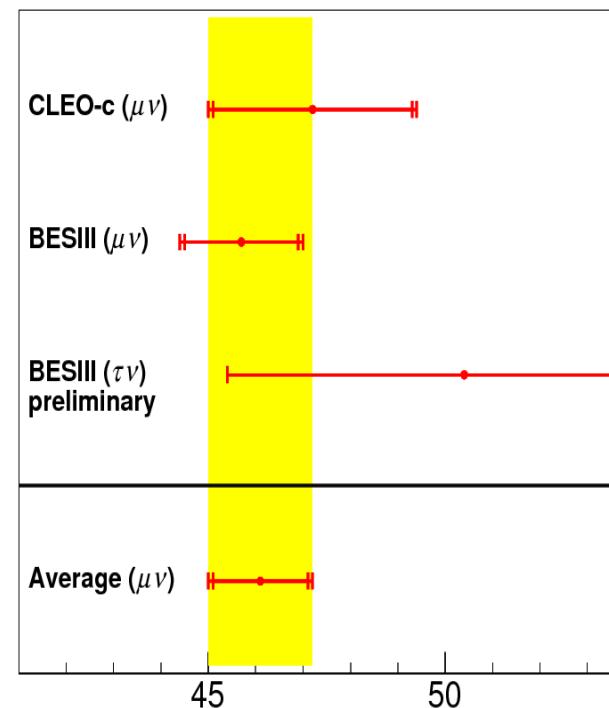
$$f_{D^+} |V_{cd}| = 50.4 \pm 5.0_{\text{stat}} \text{ MeV}$$

统计误差主导

BESIII首次提出使用 D^+ 纯轻衰变测量 $|V_{cd}|$

New inputs from PDG2018:

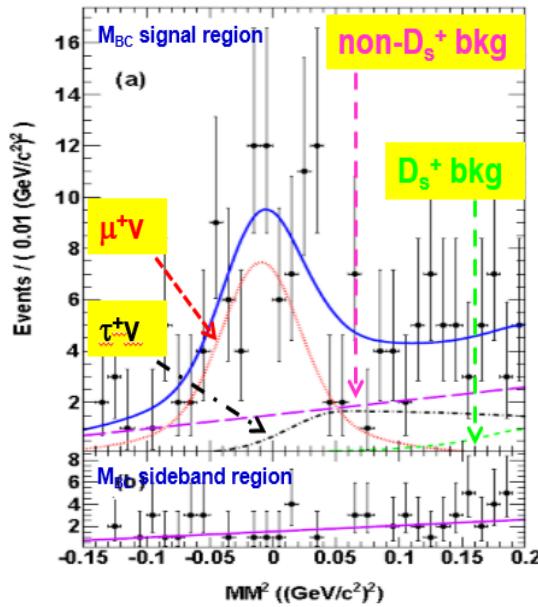
	value
m_μ	$0.1056583745(24) \text{ GeV}$
m_τ	$1.77686(12) \text{ GeV}$
m_{D^+}	$1.86965(5) \text{ GeV}$
τ_{D^+}	$1.040(7) \text{ ps}$
G_F	$1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$



纯轻衰变 $D_s^+ \rightarrow l^+ \nu$ 研究

0.48 fb^{-1} data @ 4.01 GeV

PRD94(2016)072004



$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.17 \pm 0.75 \pm 0.21) \times 10^{-3}$$

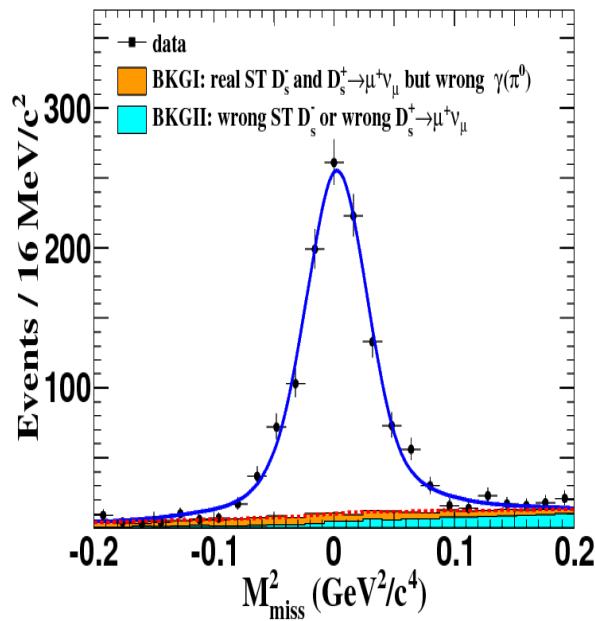
$$B[D_s^+ \rightarrow \tau^+ \nu] = (3.28 \pm 1.83 \pm 0.37)\%$$

$$f_{D_s^+} | V_{cs}| = 239 \pm 17 \pm 5 \text{ MeV} [\mu]$$

$$f_{D_s^+} | V_{cs}| = 193 \pm 54 \pm 11 \text{ MeV} [\tau]$$

3.19 fb^{-1} data @ 4.178 GeV

PRL122(2019)071802

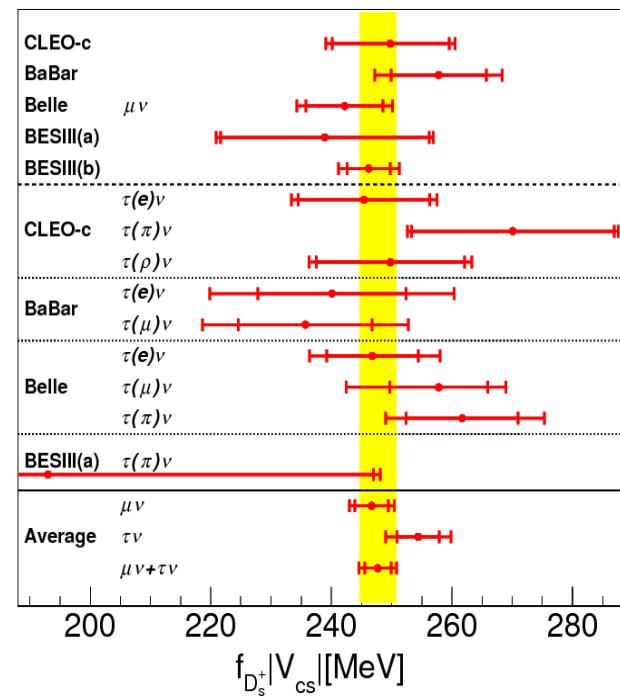


$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.49 \pm 0.16 \pm 0.15) \times 10^{-3}$$

$$f_{D_s^+} | V_{cs}| = 242.5 \pm 3.5 \pm 3.7 \text{ MeV} [\mu]$$

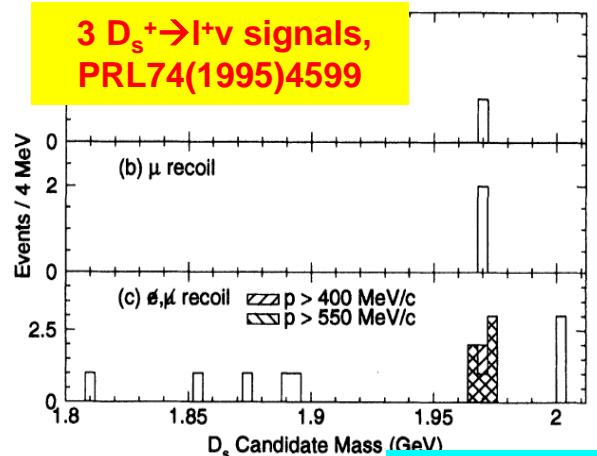
New inputs from PDG2018:

	value
m_μ	$0.1056583745(24) \text{ GeV}$
m_τ	$1.77686(12) \text{ GeV}$
$m_{D_s^+}$	$1.96834(7) \text{ GeV}$
$\tau_{D_s^+}$	$504(4) \text{ ps}$
G_F	$1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$



30年来，北京谱仪D_(s)纯轻衰变研究

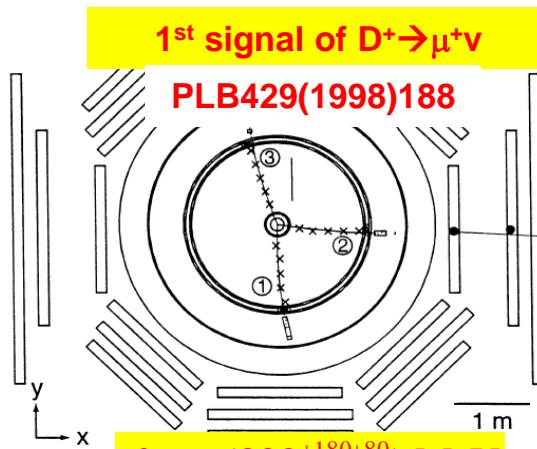
■ BESI, 22.3 pb⁻¹@4.03GeV



$$f_{D_s^+} = (430^{+150+40}_{-130-40}) \text{ MeV}$$

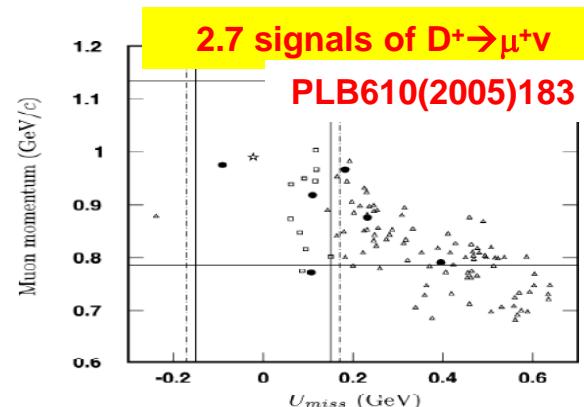
First absolute measurement

■ BESI, 22.3 pb⁻¹@4.03GeV



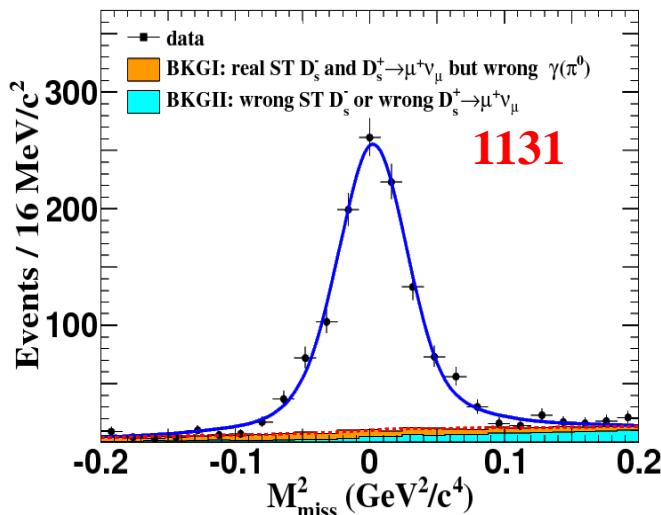
$$f_{D^+} = (300^{+180+80}_{-150-40}) \text{ MeV}$$

■ BESII, 33 pb⁻¹@ψ''

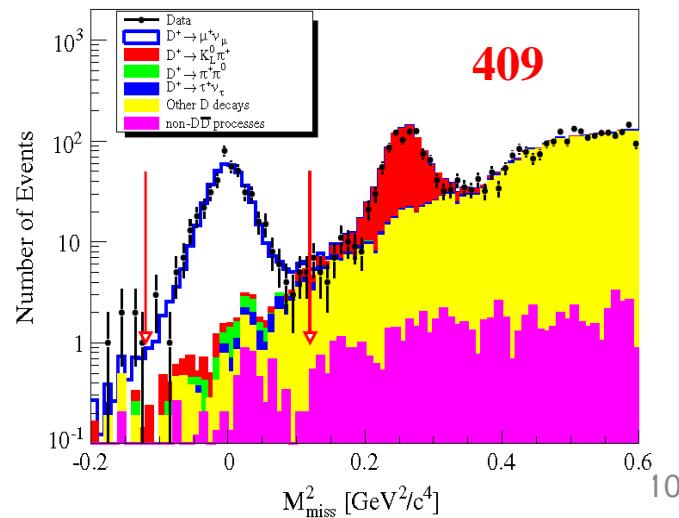


$$f_{D^+} = (371^{+129}_{-119} \pm 25) \text{ MeV}$$

BESIII: 3.19 fb⁻¹@4.178GeV

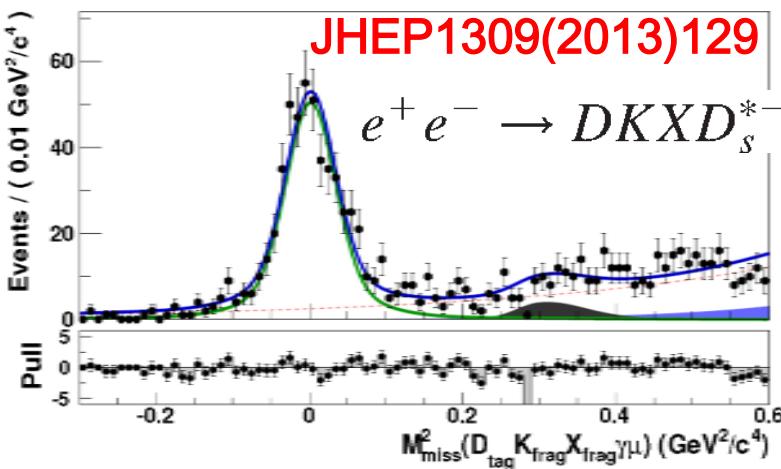


BESIII: 2.93 fb⁻¹@3.773GeV

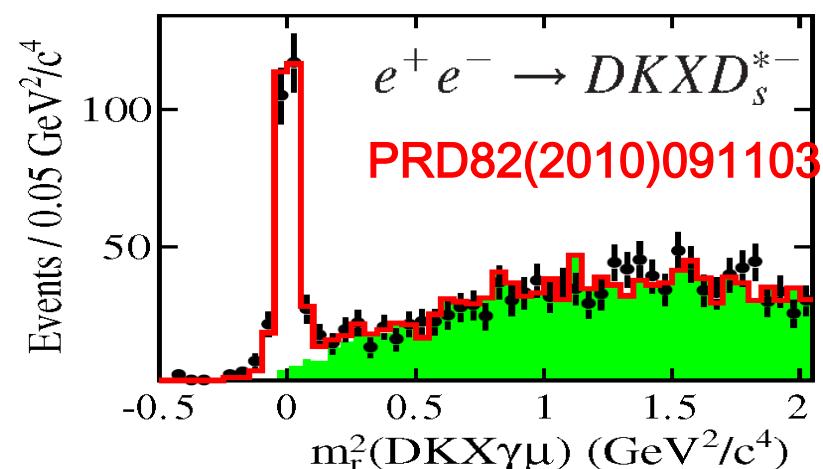


近20年，不同实验对 $D_s \rightarrow \mu^+ \nu$ 纯轻的研究

■ Belle, 913 fb^{-1} at 10.58 GeV

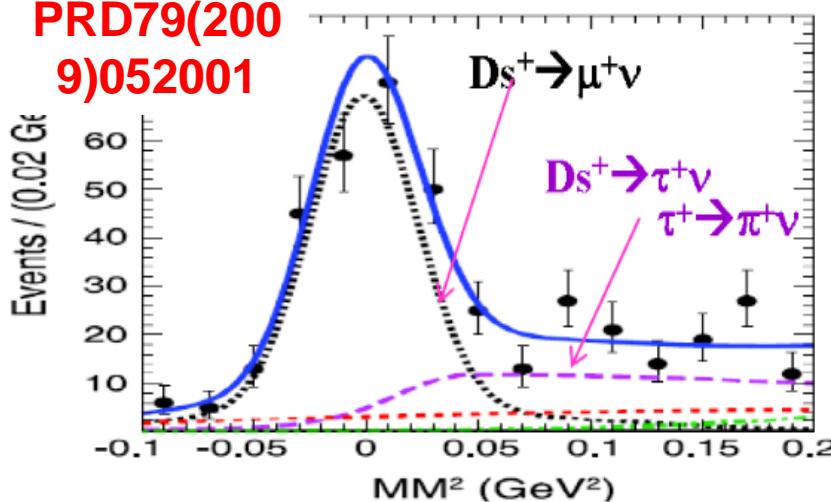


■ Babar, 521 fb^{-1} at 10.58 GeV

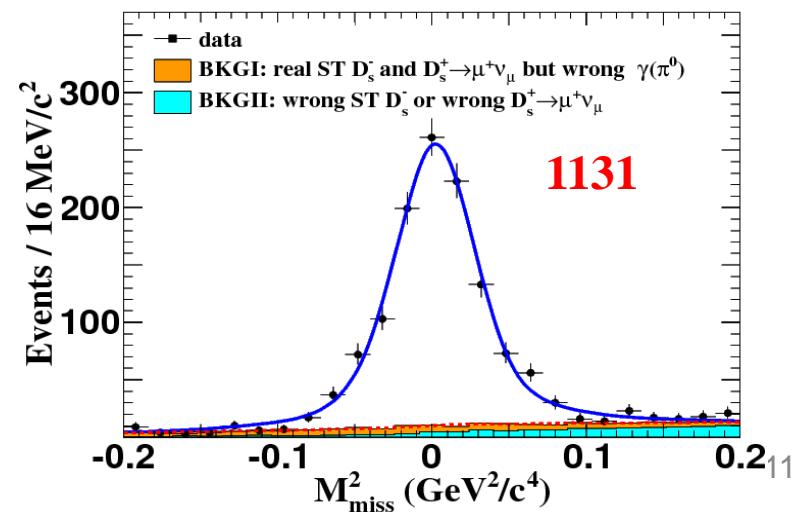


■ CLEOc: 600 pb^{-1} @ 4.17 GeV

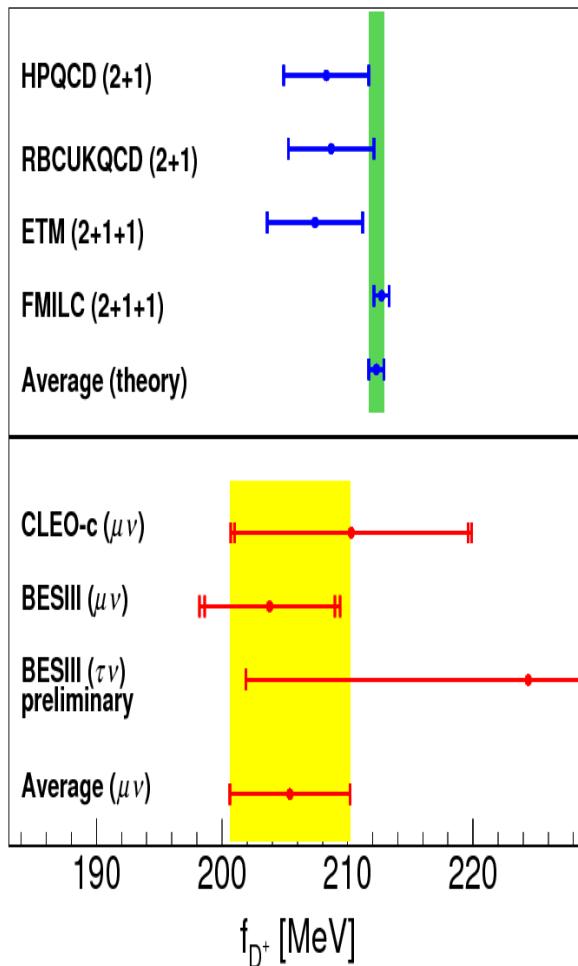
PRD79(2009)052001



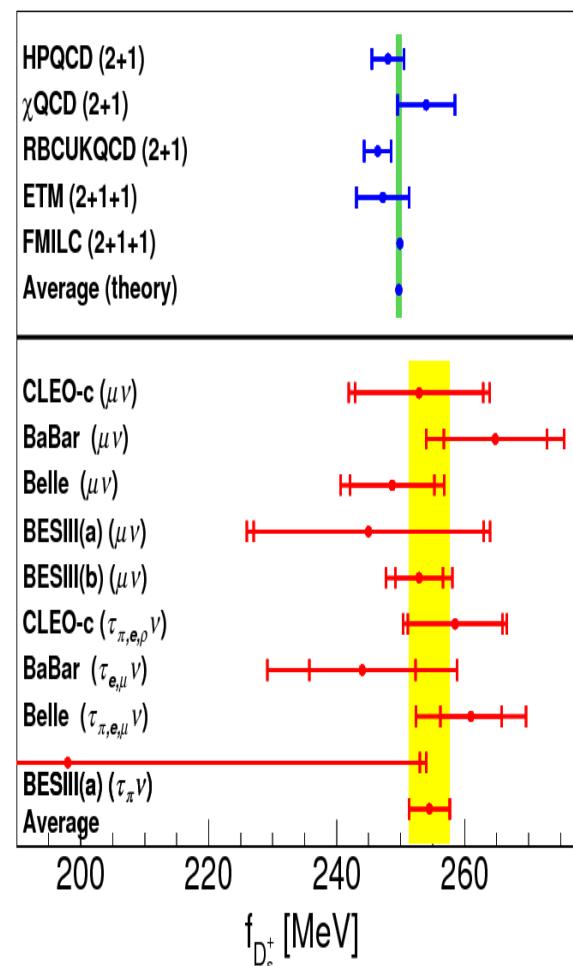
BESIII: 3.19 fb^{-1} @ 4.178 GeV



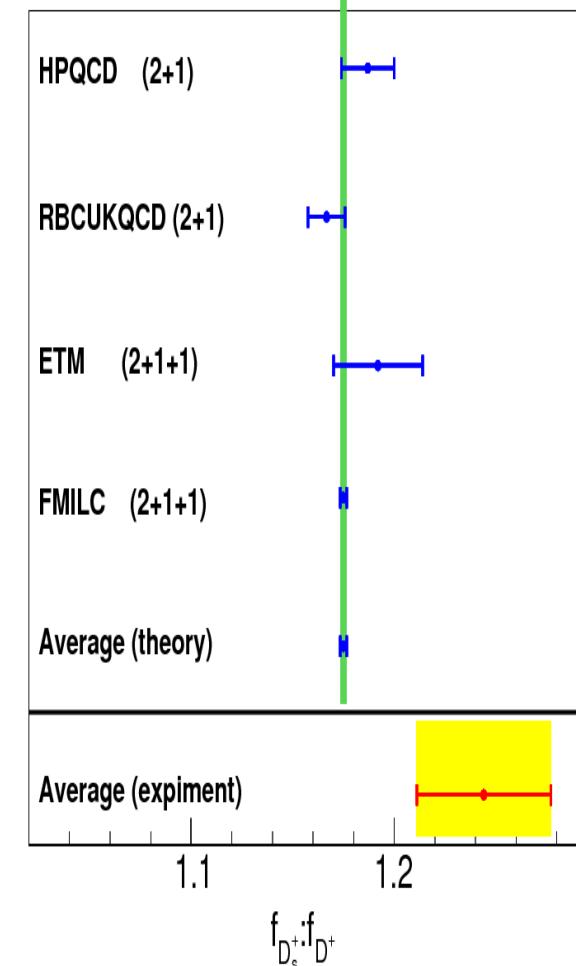
f_{D^+} 、 $f_{D_s^+}$ 、 $f_{D_s^+}:f_{D^+}$ 实验和理论比较



-1.4 σ 差异



+1.5 σ 差异



2 σ 差异

半轻衰变D→Peν动力学研究

Form factor parameterization

– Single pole form

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$$

– Modified pole

$$f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{\text{pole}}^2})(1 - \alpha \frac{q^2}{M_{\text{pole}}^2})}$$

– ISGW2

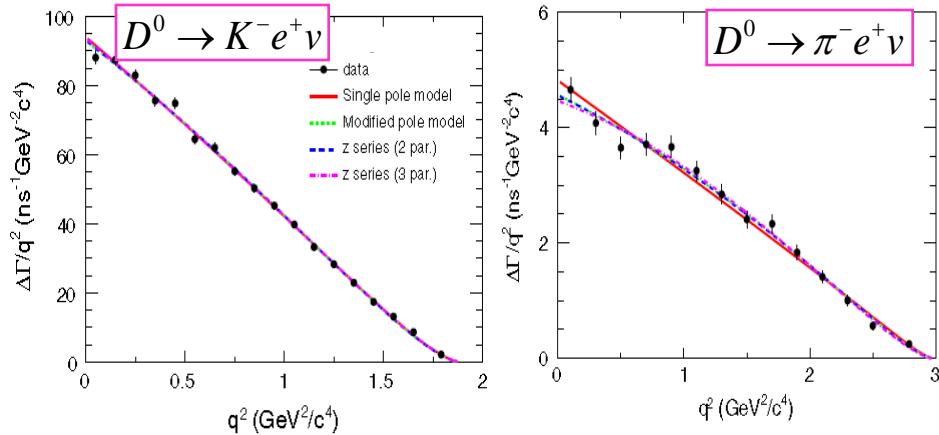
$$f_+(q^2) = f_+(q_{\max}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\max}^2 - q^2)\right)^{-2}$$

– Series expansion

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

The shown results are based on 2nd order series expansion

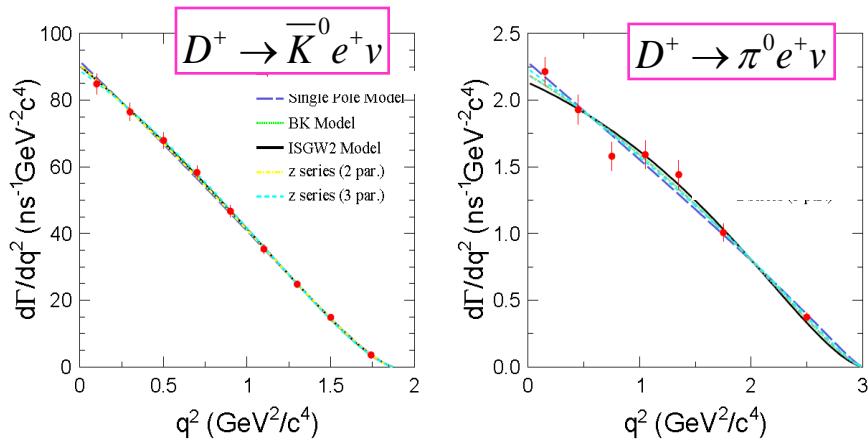
PRD92(2015)072012



$$|f_+^K(0)| V_{cs} | = 0.717(03)(04)$$

$$|f_+^\pi(0)| V_{cd} | = 0.144(02)(01)$$

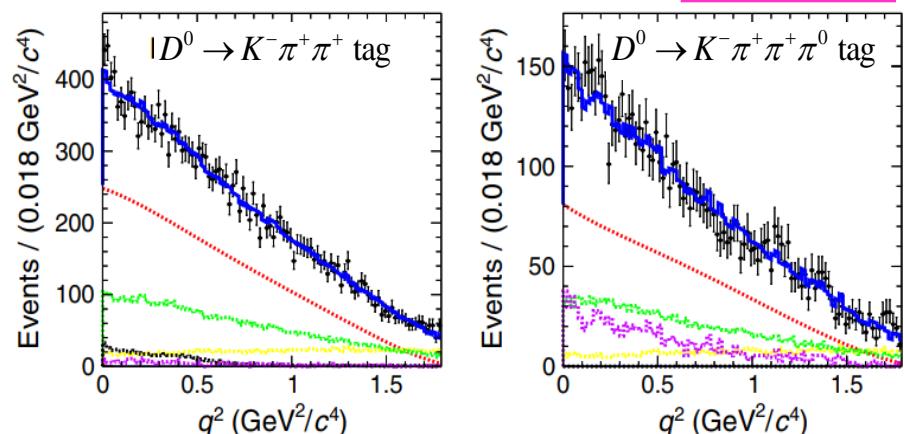
PRD96(2017)012002



$$|f_+^K(0)| V_{cs} | = 0.705(04)(11)$$

$$|f_+^\pi(0)| V_{cd} | = 0.140(03)(01)$$

PRD92(2015)112008



$$|f_+^K(0)| V_{cs} | = 0.728(06)(11)$$

半轻衰变 $D^0 \rightarrow K^- \mu^+ \nu$ 动力学研究

Differential partial widths

$$\begin{aligned} \frac{d\Gamma}{dq^2} = & \frac{G_F^2 |V_{cs}|^2}{8\pi^3 m_D} |\vec{p}_K| |f_+^K(q^2)|^2 \left(\frac{W_0 - E_K}{F_0} \right)^2 \\ & \times \left[\frac{1}{3} m_D |\vec{p}_K|^2 + \frac{m_\ell^2}{8m_D} (m_D^2 + m_K^2 + 2m_D E_K) \right. \\ & + \frac{1}{3} m_\ell^2 \frac{|\vec{p}_K|^2}{F_0} + \frac{1}{4} m_\ell^2 \frac{m_D^2 - m_K^2}{m_D} \text{Re}\left(\frac{f_-^K(q^2)}{f_+^K(q^2)}\right) \\ & \left. + \frac{1}{4} m_\ell^2 F_0 \left| \frac{f_-^K(q^2)}{f_+^K(q^2)} \right|^2 \right] \end{aligned}$$

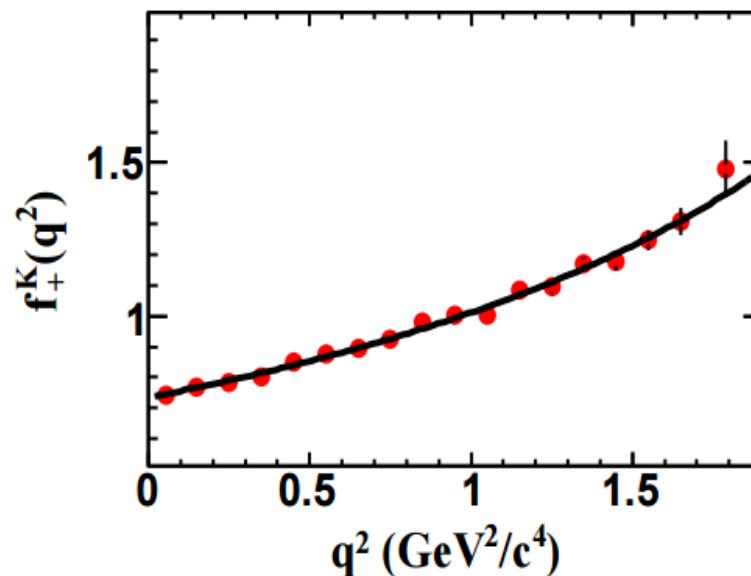
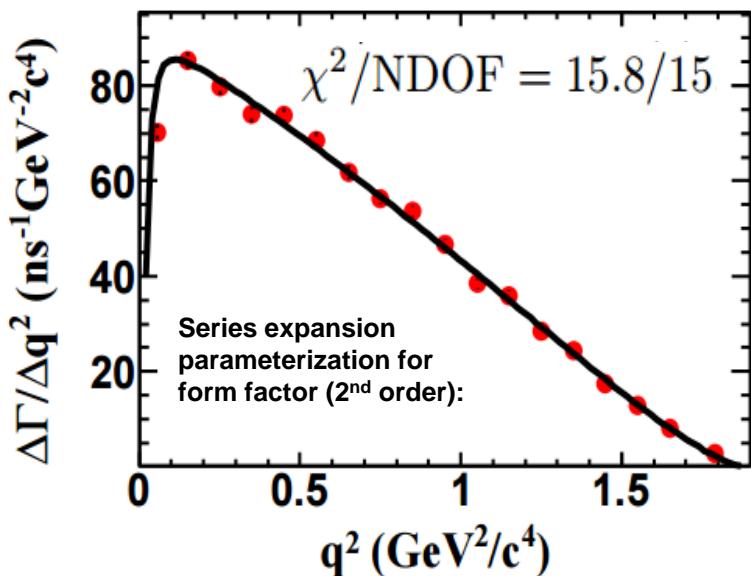
Assumed to be independent of q^2 following FOCUS's treatment
(PLB607(2005)233)

$$q = p_\mu + p_\nu$$

$$W_0 = (m_D^2 + m_K^2 - m_\ell^2)/2m_D$$

$$F_0 = W_0 - E_K + m_\ell^2/2m_D$$

PRL122(2019)011804



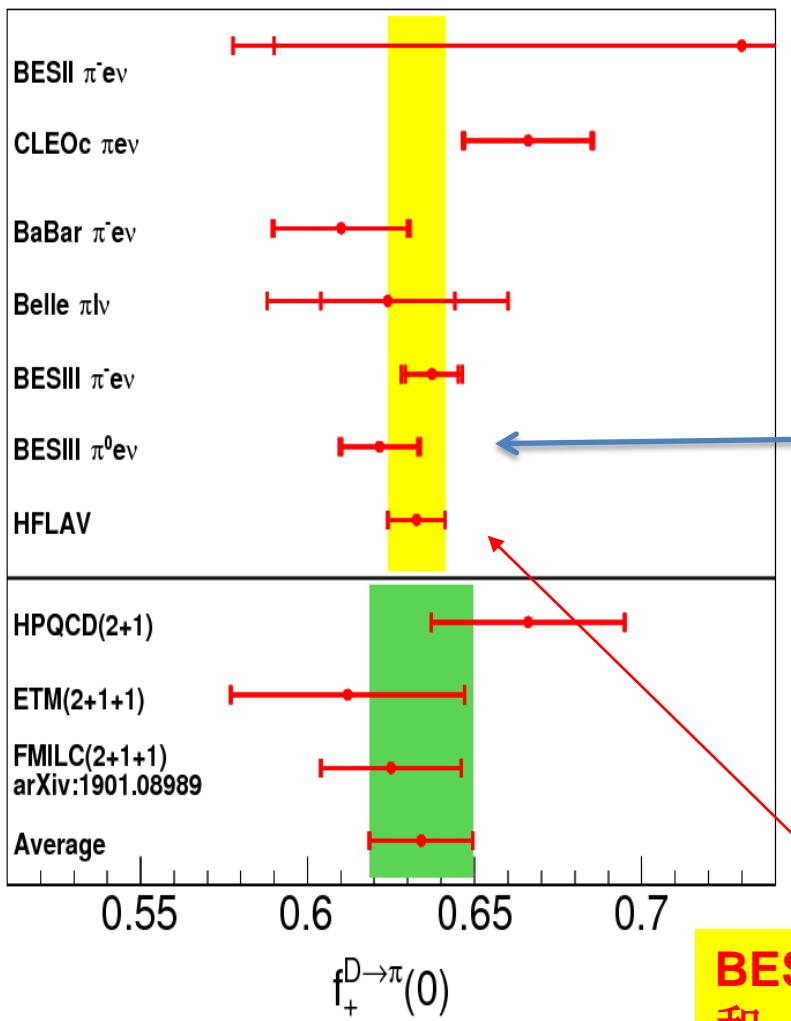
$f_+^K(0) | V_{cs} | = 0.7148(38)(29)$

形状因子 $f_+^{K(\pi)}(0)$ 实验和理论比较

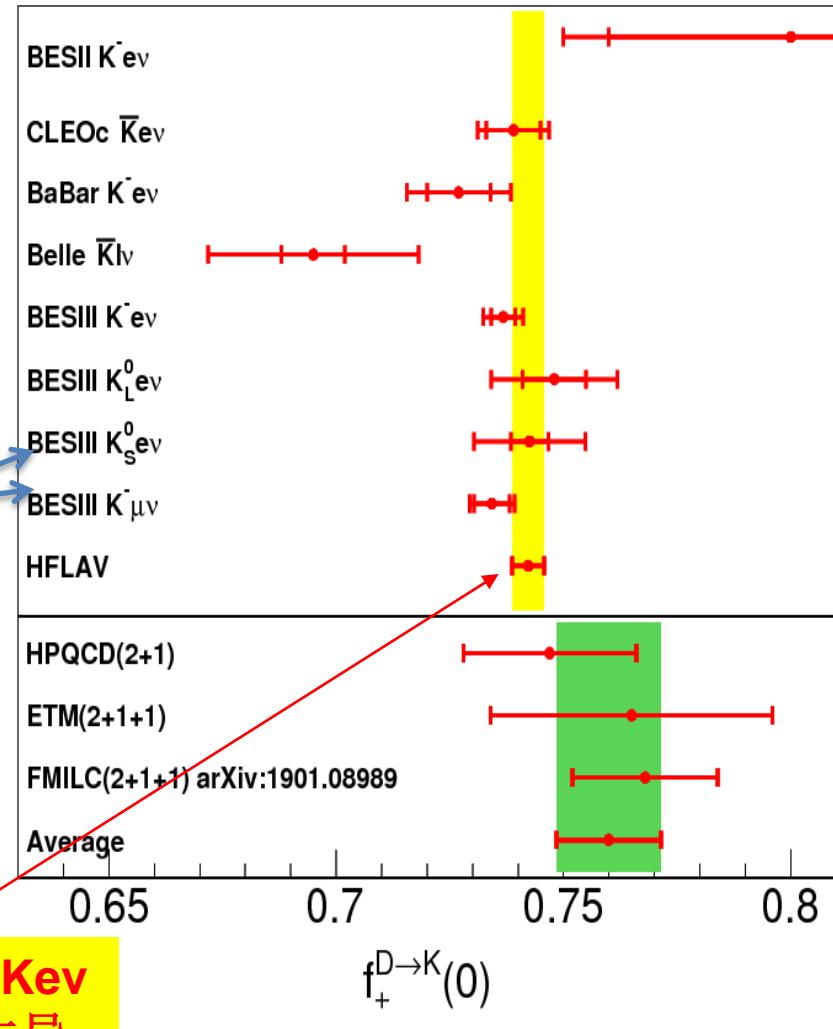
HFLAV16 averages based on a combined analysis of all
 $D \rightarrow K(\pi)l\nu$ measurements before 2016 using series expansion

$$f_+^K(0) | V_{cs} | = 0.7226(22)(26)$$

$$f_+^\pi(0) | V_{cd} | = 0.1426(17)(08)$$



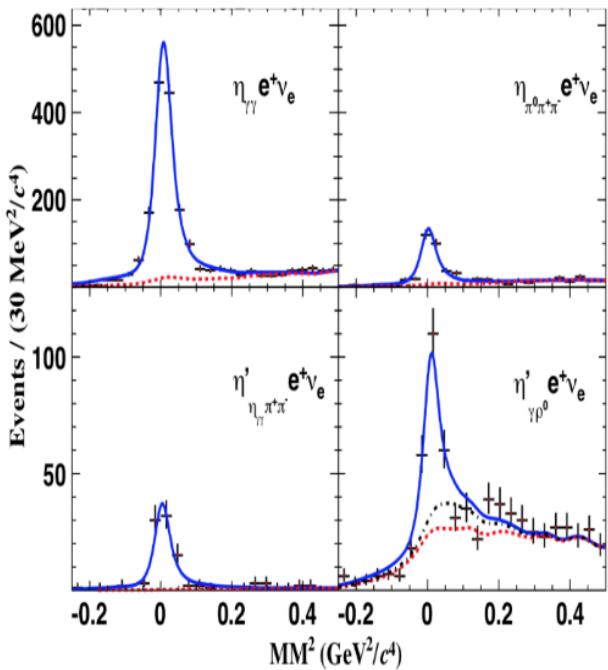
**BESIII $D^0 \rightarrow K e\nu$
和 $\pi e\nu$ 结果主导**



半轻衰变 $D \rightarrow \eta^{(\prime)} e^+ \nu$ 动力学研究

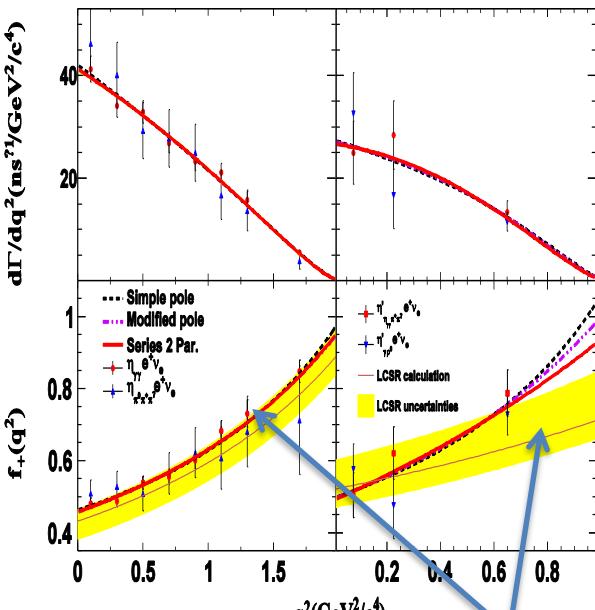
改进 $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$ 分支比，首次测定形状因子

3.19 fb^{-1} data@4.178 GeV



PRL122(2019)121801

微分跃迁率拟合



PRD88, 034023

$$f_+^{D_s^+ \rightarrow \eta}(0) = 0.446 \pm 0.005 \pm 0.004$$

$$f_+^{D_s^+ \rightarrow \eta'}(0) = 0.477 \pm 0.049 \pm 0.011$$

$D^+ \rightarrow \eta^{(\prime)} e^+ \nu$ 衰变研究

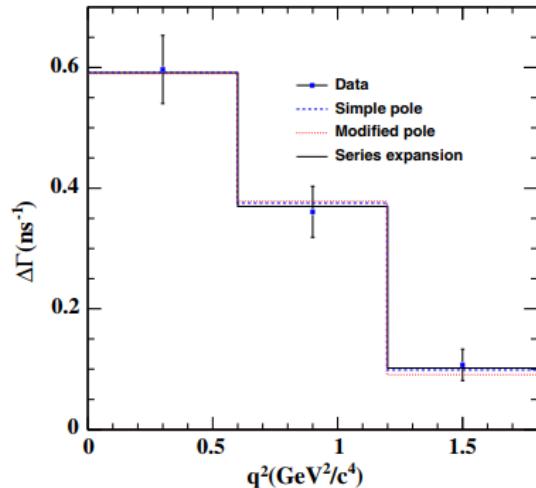
PRD97(2018)092009

分支比测量:

$$B[D^+ \rightarrow \eta e^+ \nu] = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$$

$$B[D^+ \rightarrow \eta' e^+ \nu] = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$$

$D^+ \rightarrow \eta e^+ \nu$ 跃迁率拟合:



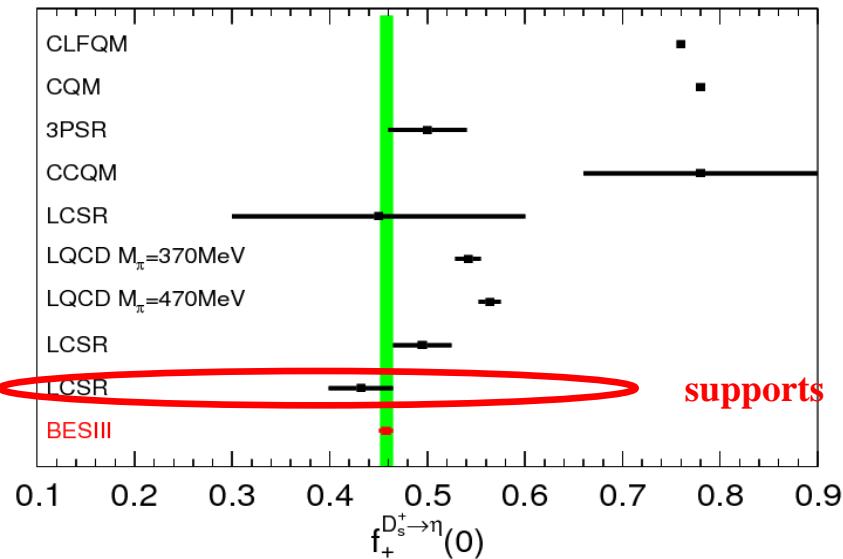
$$f_+^{D^+ \rightarrow \eta}(0) |V_{cd}| = (7.84 \pm 0.64 \pm 0.21) \%$$

$$B[D_s^+ \rightarrow \eta e^+ \nu] = (2.32 \pm 0.06 \pm 0.06) \%$$

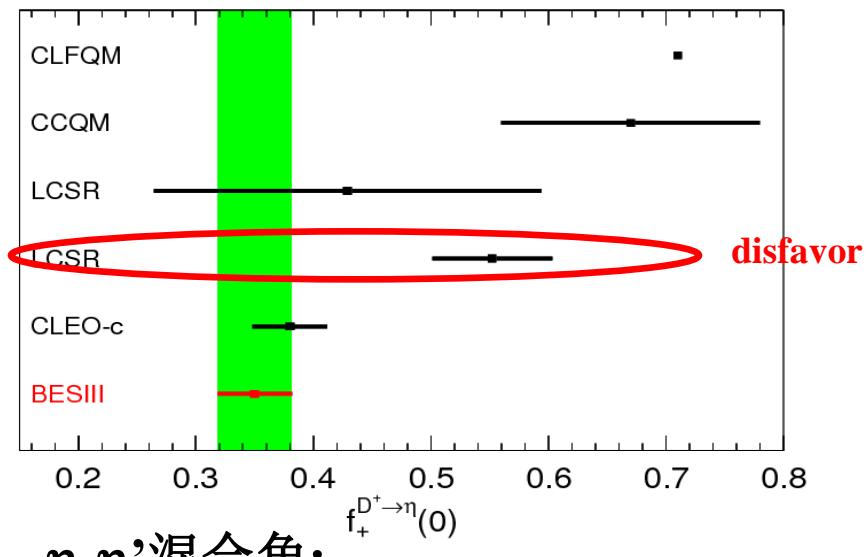
$$B[D_s^+ \rightarrow \eta' e^+ \nu] = (0.82 \pm 0.07 \pm 0.03) \%$$

形状因子和 $\eta-\eta'$ 混合角比较

$f_{+}^{D_s \rightarrow \eta(0)}$ 实验和理论比较



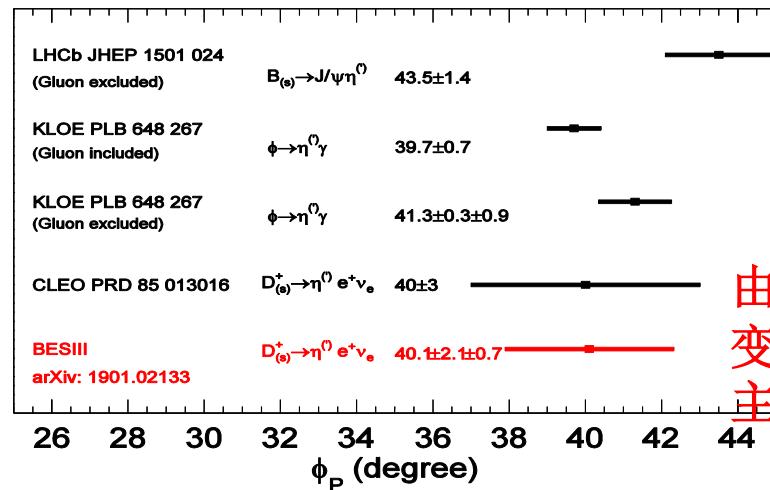
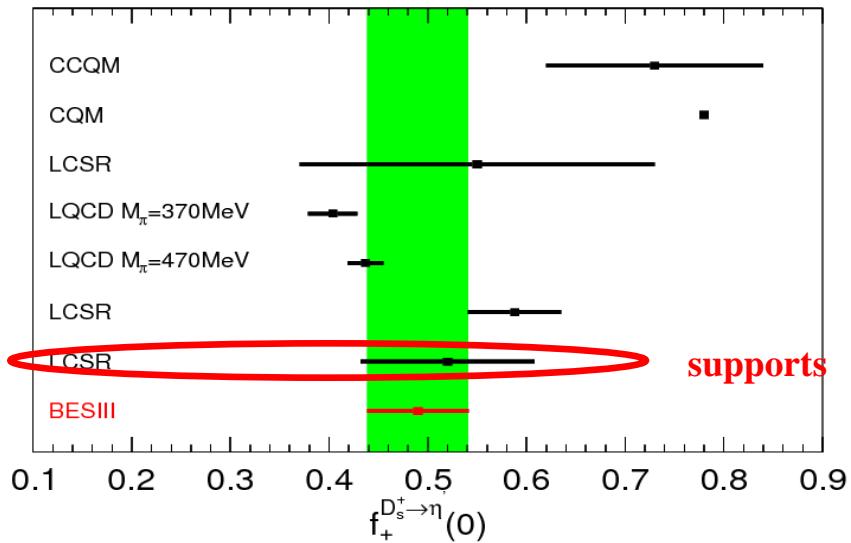
$f_{+}^{D^+ \rightarrow \eta(0)}$ 实验和理论比较



$\eta-\eta'$ 混合角:

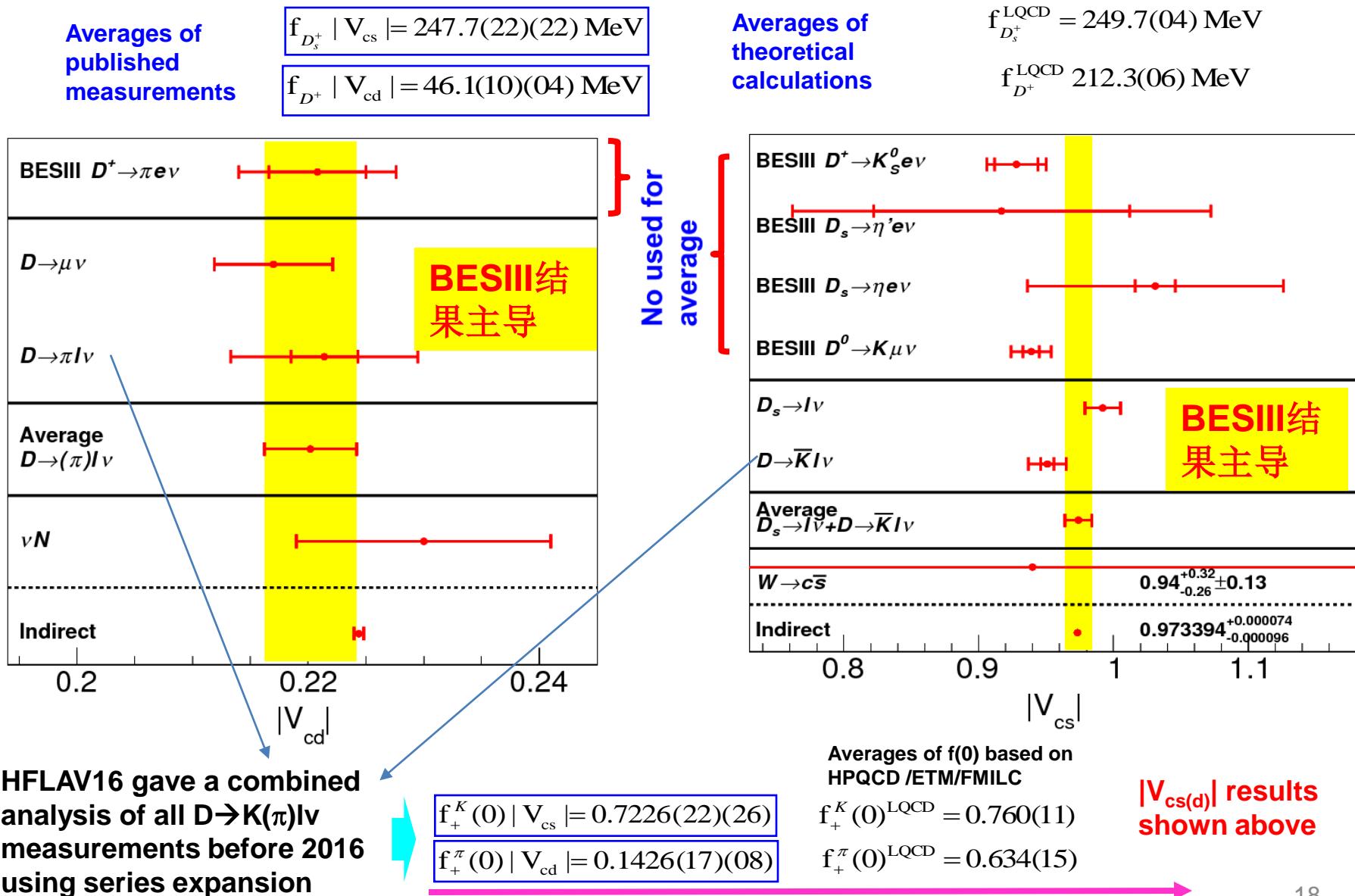
$$\frac{\Gamma(D_s^+ \rightarrow \eta'e^+\nu)/\Gamma(D_s^+ \rightarrow \eta e^+\nu)}{\Gamma(D^+ \rightarrow \eta'e^+\nu)/\Gamma(D^+ \rightarrow \eta e^+\nu)} \simeq \cot^4 \phi_P$$

With the BFs in
PRD97, 092009 &
arXiv:1901.02133



由 D^+ 衰变误差主导

CKM矩阵元 $|V_{cs}|$ 和 $|V_{cd}|$ 比较

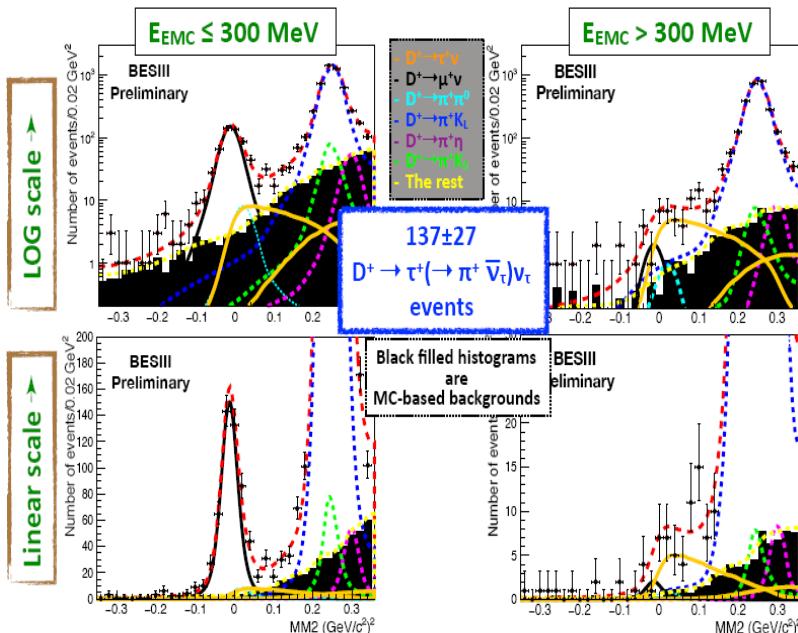


$D_{(s)}^+ \rightarrow l^+ \nu$ 衰变检验轻子普适性

>5 σ

Fitting to DATA

11



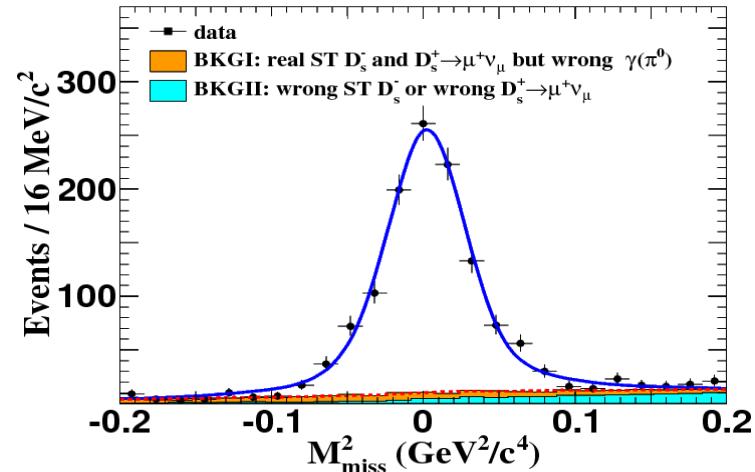
$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24_{\text{stat}}) \times 10^{-3}$$

$$\frac{B[D^+ \rightarrow \tau^+ \nu]}{B[D^+ \rightarrow \mu^+ \nu]} = 3.21 \pm 0.64_{\text{stat}}$$

SM预期: 2.66

PRL122(2019)071802



$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.49 \pm 0.16 \pm 0.15) \times 10^{-3}$$

Combined results:

$$\bar{B}[D_s^+ \rightarrow \mu^+ \nu] = (5.49 \pm 0.17) \times 10^{-3}$$

$$B^{\text{PDG}}[D_s^+ \rightarrow \tau^+ \nu] = (5.49 \pm 0.17) \times 10^{-3}$$

$$\frac{B[D_s^+ \rightarrow \tau^+ \nu]}{B[D_s^+ \rightarrow \mu^+ \nu]} = 9.98 \pm 0.52$$

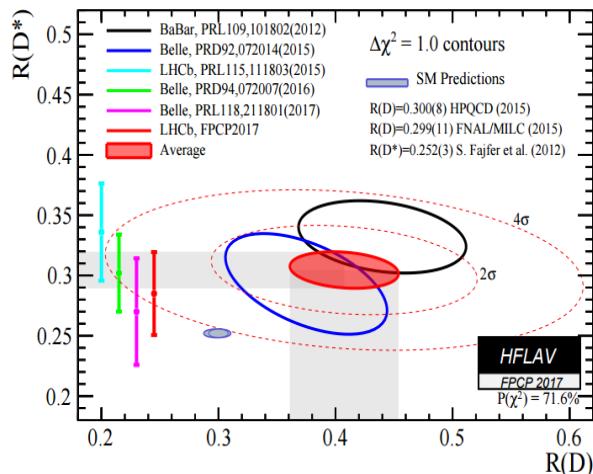
SM预期: 9.74

$D^0(+) \rightarrow \pi^+ \nu$ 衰变检验轻子普适性

B物理研究中：

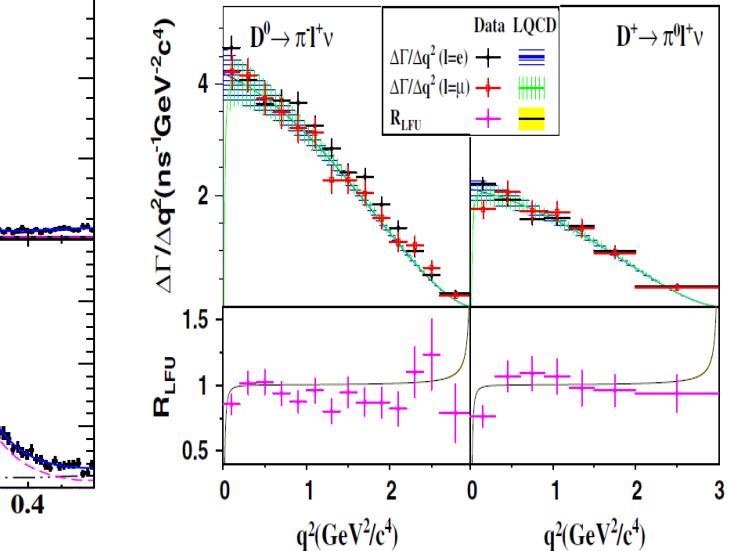
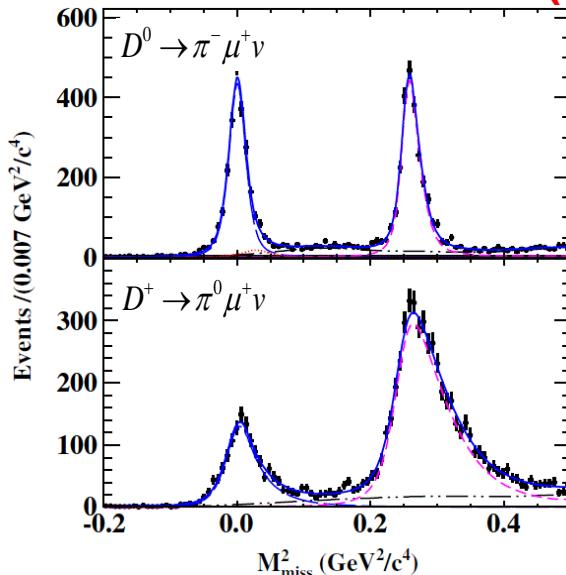
$$R(D^{(*)}) = \frac{B(B \rightarrow D^{(*)} \tau \nu)}{B(B \rightarrow D^{(*)} l \nu)}$$

与LFU预期有 3.9σ 偏离



BESIII:

$$\begin{aligned} B[D^0 \rightarrow \pi^- \mu^+ \nu] &= (0.272 \pm 0.008 \pm 0.006)\% \\ B[D^+ \rightarrow \pi^0 \mu^+ \nu] &= (0.350 \pm 0.011 \pm 0.010)\% \\ B[D^0 \rightarrow \pi^- e^+ \nu] &= (0.295 \pm 0.004 \pm 0.003)\% \\ B[D^+ \rightarrow \pi^0 e^+ \nu] &= (0.363 \pm 0.008 \pm 0.005)\% \end{aligned}$$



$$\frac{\Gamma[D^0 \rightarrow \pi^- \mu^+ \nu]}{\Gamma[D^0 \rightarrow \pi^- e^+ \nu]} = 0.922 \pm 0.030 \pm 0.022 \quad (1.7\sigma)$$

$$\frac{\Gamma[D^+ \rightarrow \pi^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \pi^0 e^+ \nu]} = 0.964 \pm 0.037 \pm 0.026 \quad (0.5\sigma)$$

SM预期: 0.985

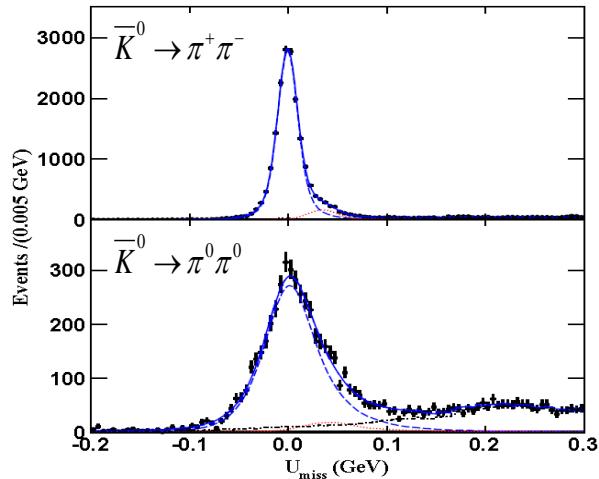
$$\frac{\Gamma^{\text{PDG}}[D^0 \rightarrow \pi^- \mu^+ \nu]}{\Gamma^{\text{PDG}}[D^0 \rightarrow \pi^- e^+ \nu]} = 0.82 \pm 0.08 \quad (2.1\sigma)$$

$$B^{\text{PDG}}[D^+ \rightarrow \pi^0 \mu^+ \nu] = (0.272 \pm 0.024)\%$$

PRL121(2018)171803

D $\rightarrow\bar{K}l^+\nu$ 衰变检验轻子普适性

EPJC76(2016)369



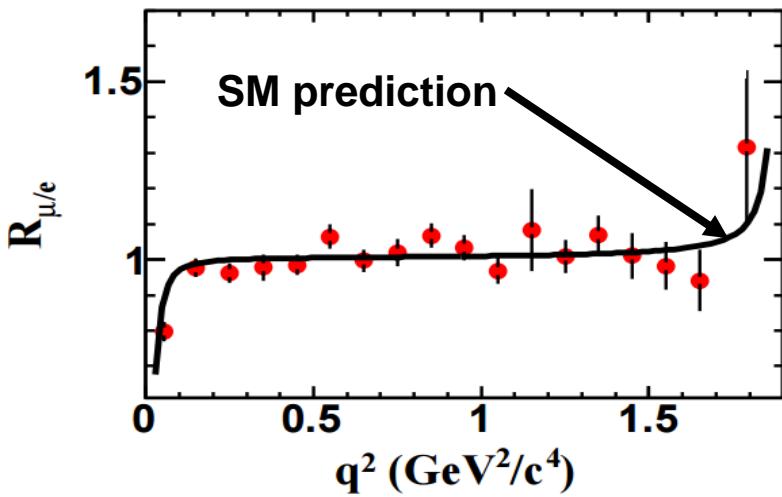
$$B[D^+ \rightarrow \bar{K}^0 \mu^+ \nu] = (8.72 \pm 0.07 \pm 0.18)\%$$

$$B^{\text{PDG}}[D^+ \rightarrow \bar{K}^0 e^+ \nu] = (8.74 \pm 0.19)\%$$

SM预期: 0.97

$$\frac{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 1.00 \pm 0.03$$

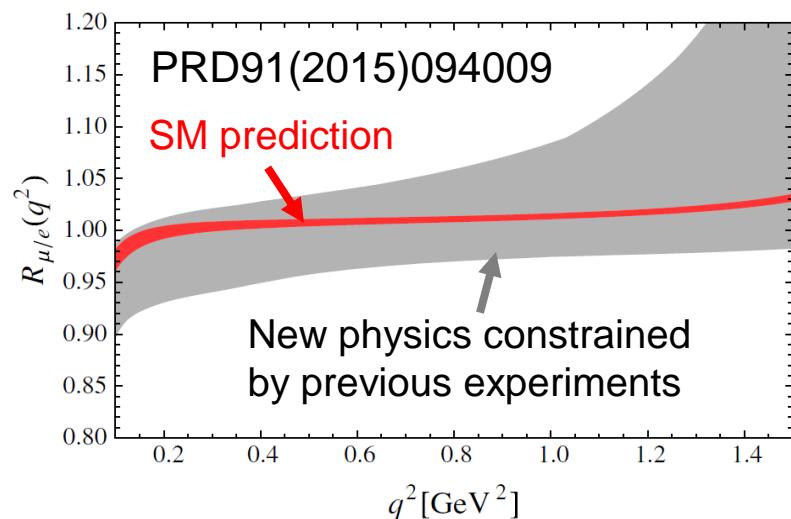
PRL122(2019)011804



$$B[D^0 \rightarrow K^- \mu^+ \nu] = (3.413 \pm 0.019 \pm 0.035)\%$$

$$B^{\text{BESIII}}[D^0 \rightarrow K^- e^+ \nu] = (3.505 \pm 0.014 \pm 0.033)\%$$

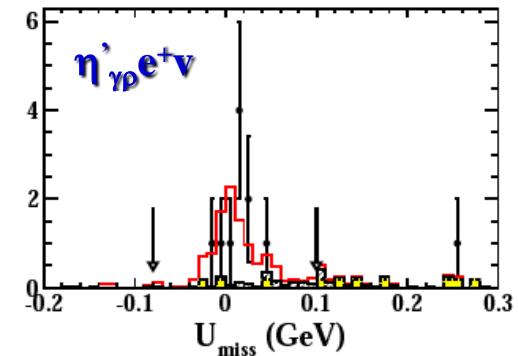
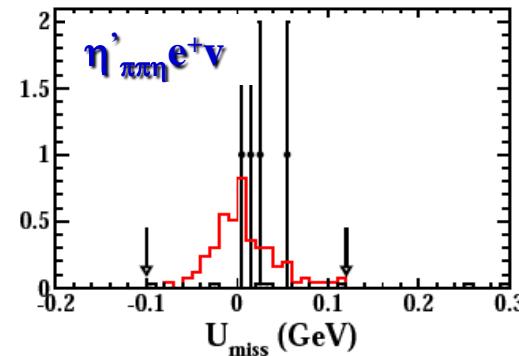
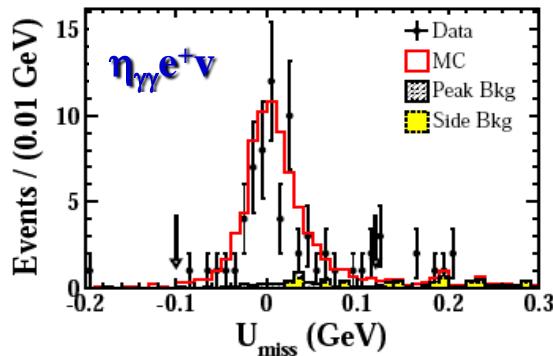
$$\frac{\Gamma[D^0 \rightarrow K^- \mu^+ \nu]}{\Gamma[D^0 \rightarrow K^- e^+ \nu]} = 0.978 \pm 0.007 \pm 0.012$$



LFU test with $D_s^+ \rightarrow \phi/\eta(\prime) l^+ \nu$ decays

PRD94(2016)112003

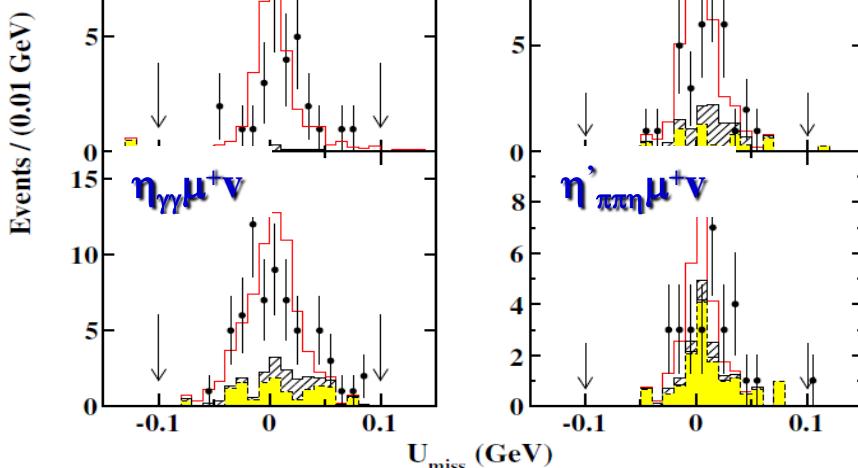
0.48 fb⁻¹ data@4.01 GeV



$$B[D_s^+ \rightarrow \eta e^+ \nu] = (2.30 \pm 0.31 \pm 0.08)\%$$

$$B[D_s^+ \rightarrow \eta' e^+ \nu] = (0.93 \pm 0.30 \pm 0.05)\%$$

PRD97(2018)012006



$$B[D_s^+ \rightarrow \phi e^+ \nu] = (2.26 \pm 0.45 \pm 0.09)\%$$

$$B[D_s^+ \rightarrow \phi \mu^+ \nu] = (1.94 \pm 0.53 \pm 0.09)\%$$

$$B[D_s^+ \rightarrow \eta \mu^+ \nu] = (2.42 \pm 0.46 \pm 0.11)\%$$

$$B[D_s^+ \rightarrow \eta' \mu^+ \nu] = (1.06 \pm 0.54 \pm 0.07)\%$$

First measurements

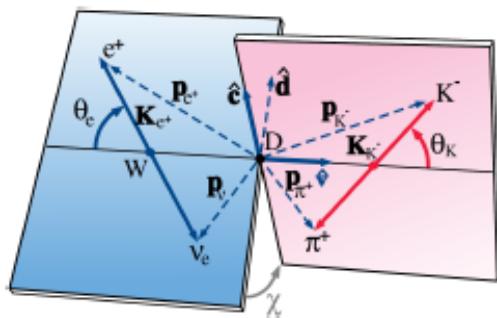
$$\frac{\Gamma[D_s^+ \rightarrow \phi \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \phi e^+ \nu]} = 0.86 \pm 0.29$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta e^+ \nu]} = 1.05 \pm 0.24$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta' \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta' e^+ \nu]} = 1.14 \pm 0.68$$

半轻衰变 $D \rightarrow V e^+ \bar{v}$ 形状因子测量

因 $D \rightarrow V \mu \nu$ 形状因子和背景更加复杂，目前完成了一些 $D \rightarrow V e \bar{v}$ 研究



- $m^2 = (p_{\pi^+} + p_{K^-})^2$
- $\cos(\theta_K) = \frac{\hat{D} \cdot \mathbf{K}_{K^-}}{|\mathbf{K}_{K^-}|}$
- $\cos(\chi) = \hat{e} \cdot \hat{d}$
- $q^2 = (p_{e^+} + p_{\nu_e})^2$
- $\cos(\theta_e) = -\frac{\hat{D} \cdot \mathbf{K}_{e^+}}{|\mathbf{K}_{e^+}|}$
- $\sin(\chi) = (\hat{e} \times \hat{D}) \cdot \hat{d}$

Decay rate depend on 5 variables and 3 form factors

$$d^5\Gamma = \frac{G_F^2 |V_{cs}|^2}{(4\pi)^6 m_D^2} X \beta \mathcal{I}(m^2, q^2, \theta_K, \theta_e, \chi) dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi$$

- $X = p_{K\pi} m_D$, $p_{K\pi}$ is the momentum of the $K\pi$ system in the D rest frame
- $\beta = 2p^+/m$, p^+ is the breakup momentum of the $K\pi$ system in its rest frame
- \mathcal{I} can be expressed in terms of helicity amplitudes $H_{0,\pm}$:

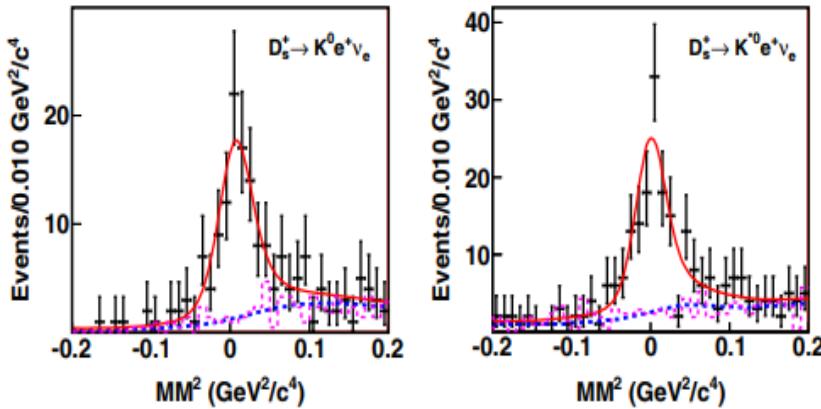
$$H_0(q^2) = \frac{1}{2m_q} \left[(m_D^2 - m^2 - q^2)(m_D + m) \textcolor{red}{A}_1(q^2) - 4 \frac{m_D^2 p_{K\pi}^2}{m_D + m} \textcolor{red}{A}_2(q^2) \right]$$

$$H_{\pm}(q^2) = (m_D + m) \textcolor{red}{A}_1(q^2) \mp \frac{2m_D p_{K\pi}}{m_D + m} \textcolor{red}{V}(q^2)$$

- Vector form factor: $\textcolor{red}{V}(q^2) = \frac{V(0)}{1 - q^2/m_V^2}$; or: FF ratio $r_V = V(0)/A_1(0)$
- Axial-vector form factor: $\textcolor{red}{A}_1(q^2) = \frac{A_1(0)}{1 - q^2/m_A^2}$, $\textcolor{red}{A}_2(q^2) = \frac{A_2(0)}{1 - q^2/m_A^2}$; or: FF ratio $r_2 = A_2(0)/A_1(0)$

$D_s^+ \rightarrow K^{(*)0} e^+ \nu$ 衰变的研究

PRL122(2019)061801



改进测定分支比:

$$B_{D_s^+ \rightarrow K^0 e^+ \nu} = (3.25 \pm 0.38 \pm 0.16) \times 10^{-3} \quad \text{理论: } 2.0-3.9 \times 10^{-3}$$

$$B_{D_s^+ \rightarrow K^{*0} e^+ \nu} = (2.37 \pm 0.26 \pm 0.20) \times 10^{-3} \quad \text{理论: } 1.7-2.3 \times 10^{-3}$$

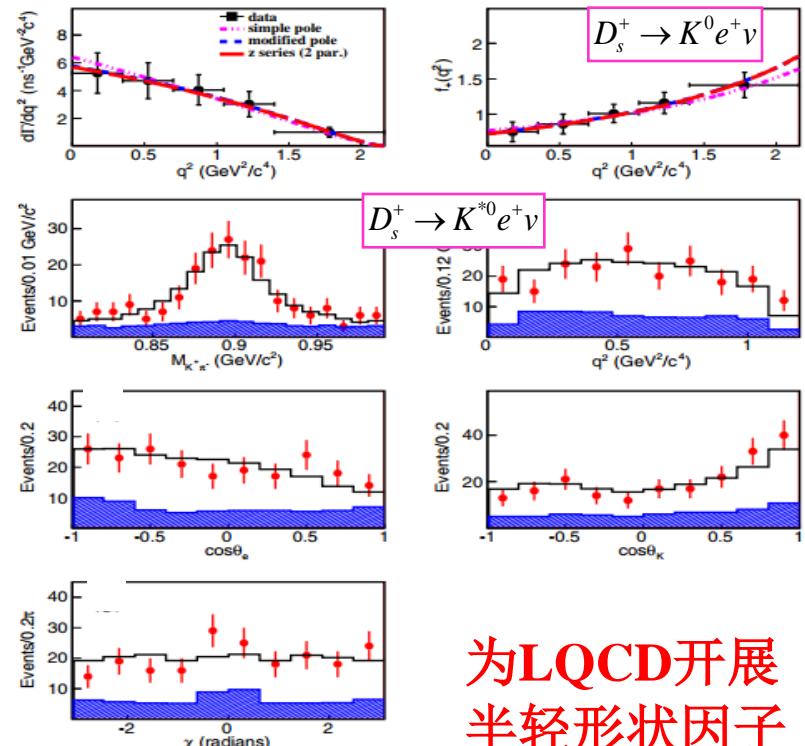
首次测定形状因子:

$$D_s^+ \rightarrow K^0 e^+ \nu \quad f_+^{D_s \rightarrow K}(0) = 0.720 \pm 0.084 \pm 0.013$$

$$D_s^+ \rightarrow K^{*0} e^+ \nu \quad r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

微分跃迁率拟合投影



为LQCD开展半轻形状因子计算提供了重要参照依据

形状因子比值:

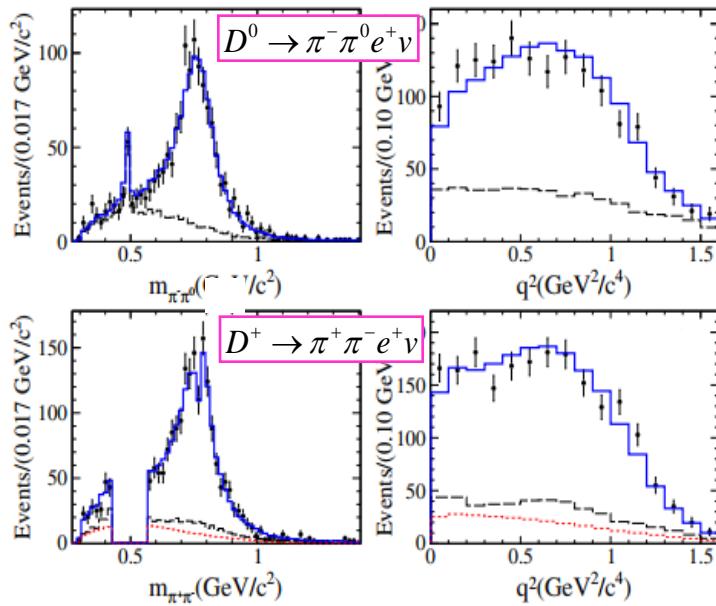
$$f_+^{D_s \rightarrow K}(0) / f_+^{D^+ \rightarrow \pi}(0) = 1.16 \pm 0.14 \pm 0.02$$

$$r_V^{D_s \rightarrow K^{*0}} / r_V^{D^+ \rightarrow \rho^0} = 1.13 \pm 0.26 \pm 0.11$$

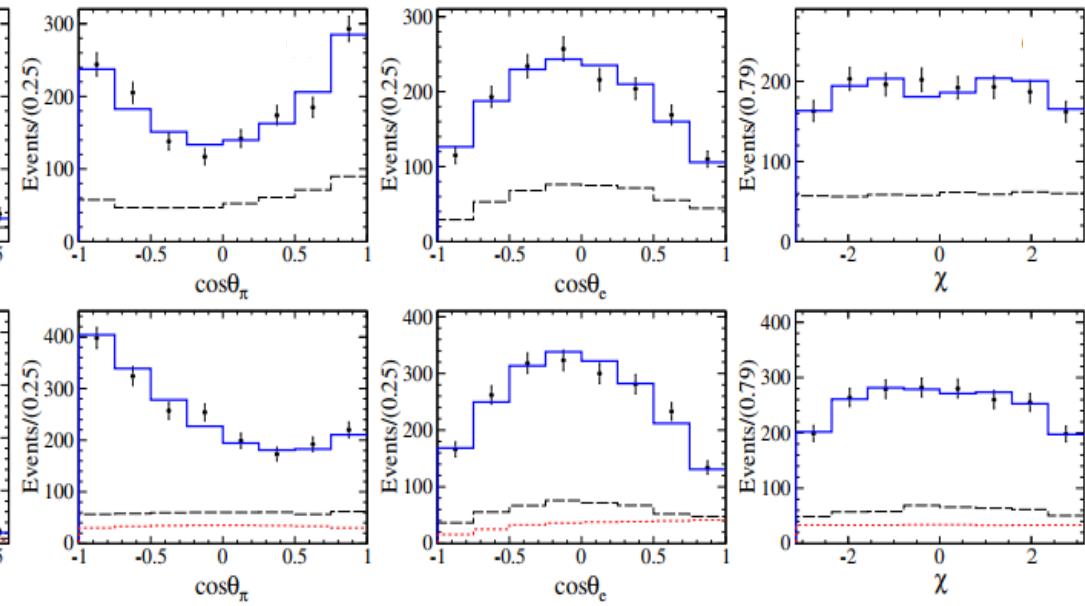
$$r_2^{D_s \rightarrow K^{*0}} / r_2^{D^+ \rightarrow \rho^0} = 0.93 \pm 0.36 \pm 0.10$$

$D^0(+) \rightarrow \pi\pi e^+\nu$ 衰变的研究

PRL122(2019)062001



微分跃迁率拟合投影



结果显示，该过程由 $D \rightarrow \rho e \nu$ 主导，并首次观测到 $D^+ \rightarrow f_0(500) e^+ \nu$ ($> 10\sigma$)

Signal mode	This analysis ($\times 10^{-3}$)
$D^0 \rightarrow \pi^- \pi^0 e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^+ \rightarrow \pi^+ \pi^+ e^+ \nu_e$	$2.449 \pm 0.074 \pm 0.073$
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$1.860 \pm 0.070 \pm 0.061$
$D^+ \rightarrow \omega e^+ \nu_e$	$2.05 \pm 0.66 \pm 0.30$
$D^+ \rightarrow f_0(500) e^+ \nu_e, f_0(500) \rightarrow \pi^+ \pi^-$	$0.630 \pm 0.043 \pm 0.032$
$D^+ \rightarrow f_0(980) e^+ \nu_e, f_0(980) \rightarrow \pi^+ \pi^-$	< 0.028

改进测定形状因子

$$r_V = 1.695 \pm 0.083 \pm 0.051$$

$$r_2 = 0.845 \pm 0.056 \pm 0.039$$

理论预期：如果轻标量介子是两(四)夸克态，则 $R=1(3)$ ，有助于探讨其夸克成分

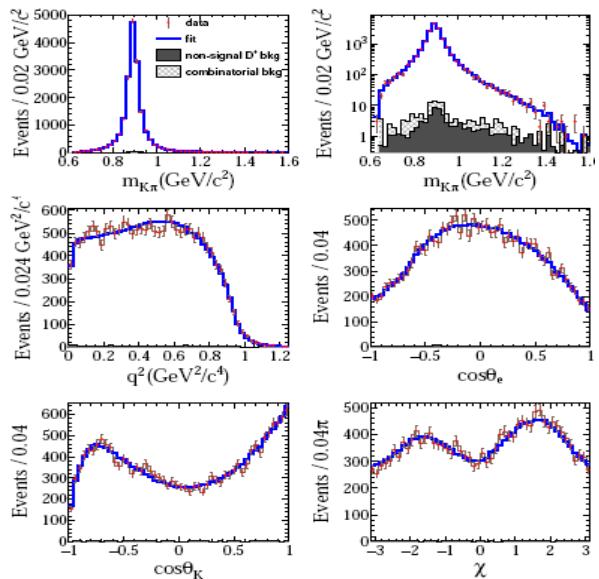
$$R = [B_{D^+ \rightarrow f_0(980)^0 e^+ \nu_e} + B_{D^+ \rightarrow f_0(500)^0 e^+ \nu_e}] / B_{D^+ \rightarrow a_0(980)^0 e^+ \nu_e}$$

BESIII测得 $R > 2.7$ ，倾向支持四夸克态

D \rightarrow $\bar{K}\pi e^+\nu$ 和 $\omega e^+\nu$ 衰变的研究

PRD94(2016)032001

改进测量 D $^+$ \rightarrow K $^-\pi^+e^+\nu$



$$B_{D^+ \rightarrow K^- \pi^+ e^+ \nu} = (3.77 \pm 0.03 \pm 0.08)\%$$

$$f_{S\text{-wave}} = (6.05 \pm 0.22 \pm 0.18)\%$$

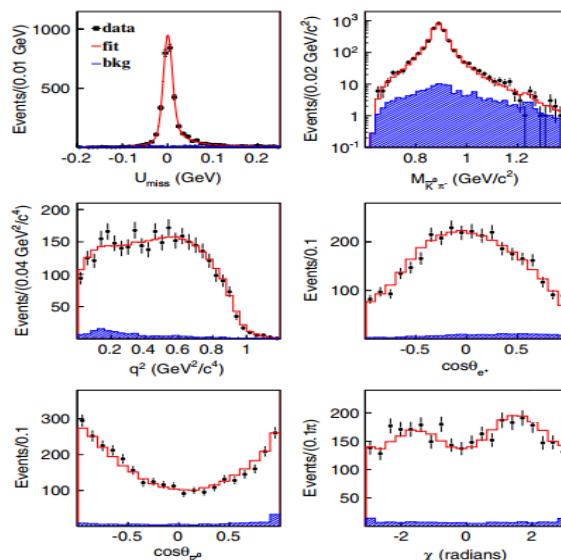
$$r_V = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = 0.788 \pm 0.042 \pm 0.008$$

$$A_1(0) = 0.589 \pm 0.010 \pm 0.012$$

PRD99(2018)011103

D $^0 \rightarrow K_S^0 \pi^- e^+ \nu$



精密测量分支比，并
首次测量形状因子

$$B_{D^0 \rightarrow \bar{K}^0 \pi^- e^+ \nu} = (1.43 \pm 0.03 \pm 0.03)\%$$

原分支比测量来自**BESII**

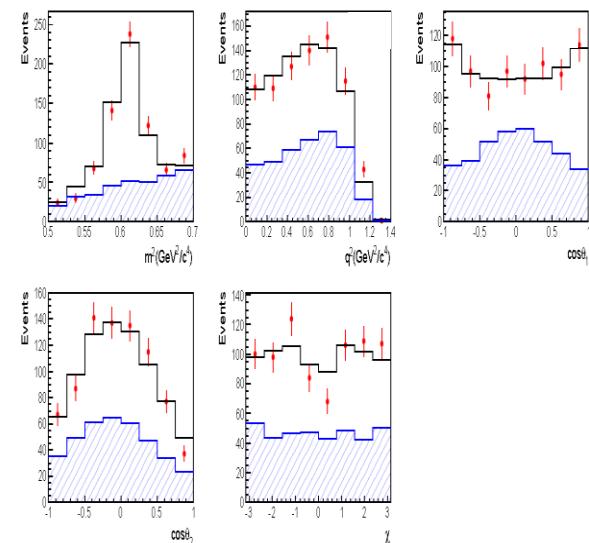
$$f_{S\text{-wave}} = (5.51 \pm 0.97 \pm 0.62)\%$$

$$r_V = 1.46 \pm 0.07 \pm 0.02$$

$$r_2 = 0.67 \pm 0.06 \pm 0.01$$

PRD92(2015)071101

D $^+ \rightarrow \omega e^+ \nu$



精密测量分支比，并
首次测量形状因子

$$B_{D^+ \rightarrow \omega e^+ \nu} = (1.63 \pm 0.11 \pm 0.08) \times 10^{-3}$$

$$r_V = 1.24 \pm 0.09 \pm 0.06$$

$$r_2 = 1.06 \pm 0.15 \pm 0.05$$

半轻衰变 $D^0(+) \rightarrow a_0(980) e^+ \nu$ 首次观测

- Explore the nontrivial internal structure of light hadron mesons, traditional $q\bar{q}$ states, tetra quark system
- With chiral unitarity approach in the coupled channels, BF is predicted to be order of $5(6) \times 10^{-5}$ for $D^0(+) \rightarrow a_0(980)$ decays

- Improve understanding of classification of light scalar mesons

$$R \equiv \frac{B(D^+ \rightarrow f_0 l^+ \nu) + B(D^+ \rightarrow \sigma l^+ \nu)}{B(D^+ \rightarrow a_0 l^+ \nu)}$$

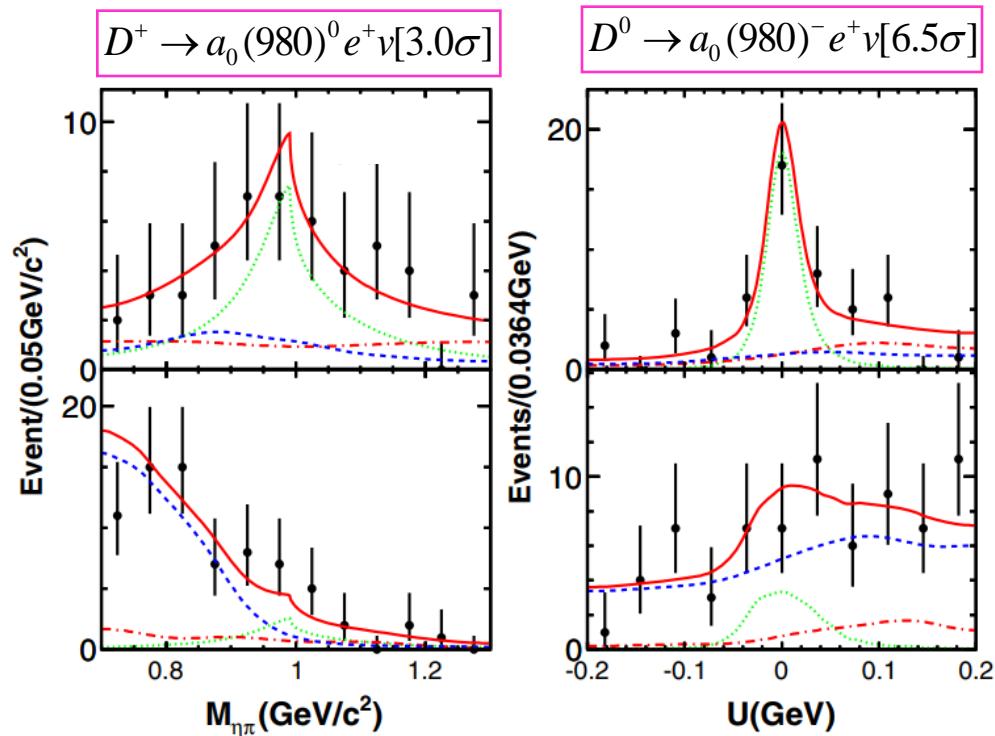
$R=1(3)$ if traditional qq (tetra quark) system

首次测出联合分支比

$$B_{D^+ \rightarrow a_0(980)^0 e^+ \nu} B_{a_0(980)^0 \rightarrow \eta \pi^0} = (1.66^{+0.81}_{-0.66}) \times 10^{-4}$$

$$B_{D^0 \rightarrow a_0(980)^- e^+ \nu} B_{a_0(980)^- \rightarrow \eta \pi^-} = (1.33^{+0.33}_{-0.29}) \times 10^{-4}$$

PRL121(2018)081802



$$\frac{\Gamma_{D^0 \rightarrow a_0(980)^- e^+ \nu}}{\Gamma_{D^+ \rightarrow a_0(980)^0 e^+ \nu}} = 2.05 \pm 0.95 \pm 0.06$$

与同位旋守恒预期一致

半轻衰变 $D^+ \rightarrow K_1(1270)^0 e^+ \nu$ 首次观测

粲介子P波半轻跃迁
已预期30年^{PRD52, 2783}，
但仍无实验确认

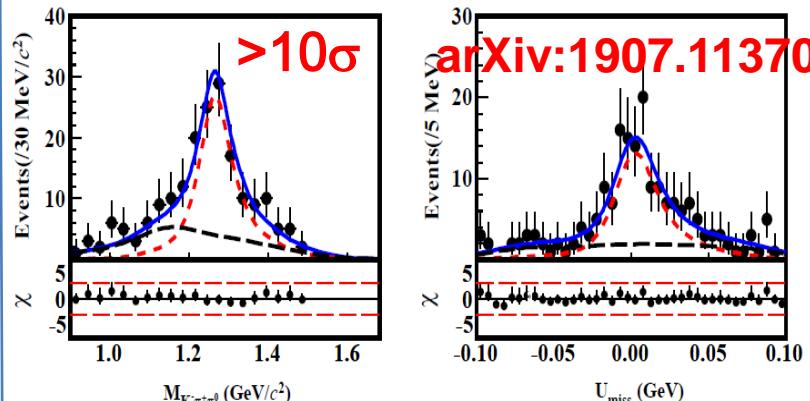
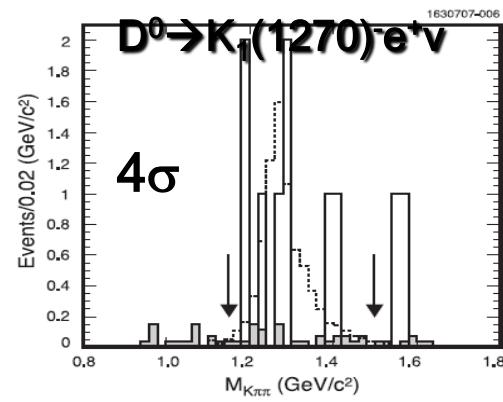
在忽略 $K_1 [K_1(1270) - K_1(1400)]$ 混合时，夸克
模型暗示 B_{D^0} 约0.12%/
 B_{D^+} 约0.34%

从 τ/D 强子/B衰变，理论
提取 K_1 混合角： $33^\circ - 35^\circ$ 或
 $57^\circ - 55^\circ$ 、 45° 、 60° 、 35°
 $- 65^\circ$ 有很大争议

粲介子半轻衰变探讨 K_1 混合及粒子参数理想窗口

CLEOc, PRL99(2007)91801

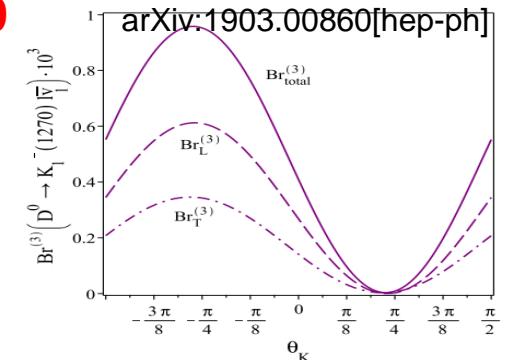
Evidence with 281 pb⁻¹



BESIII首次观测到 $D^+ \rightarrow A e \nu$

$$B_{D^+ \rightarrow K_1(1270)^- e^+ \nu} = (2.30 \pm 0.26 \pm 0.18 \pm 0.25) \times 10^{-4}$$

近期理论计算BFs
强烈依赖 K_1 混合角



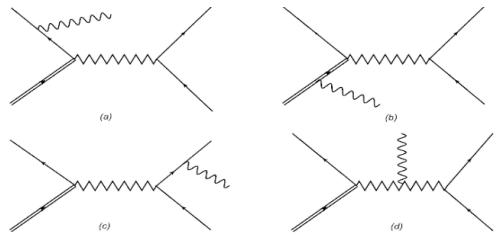
B与 K_1 混合角依赖示意图

支持混合角约
 33° 或 57° 的计算

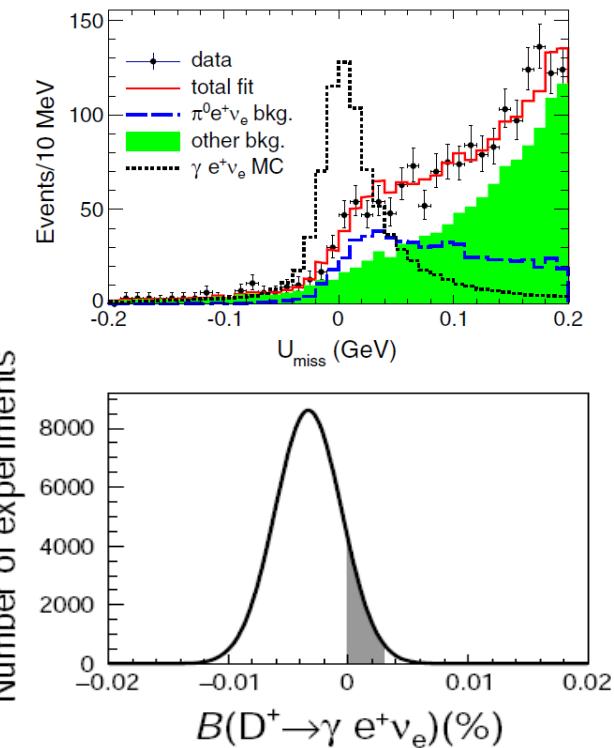
更大样本→形状因子；轴矢量粒子性质；
寻找夸克模型预期的BF更小的其它衰变

$$B_{D^0 \rightarrow K_1(1270)^- e^+ \nu} = (7.6^{+4.1}_{-3.0} \pm 0.6 \pm 0.7) \times 10^{-4}$$

寻找D辐射半轻衰变或 β 衰变



PRD95(2017)071102

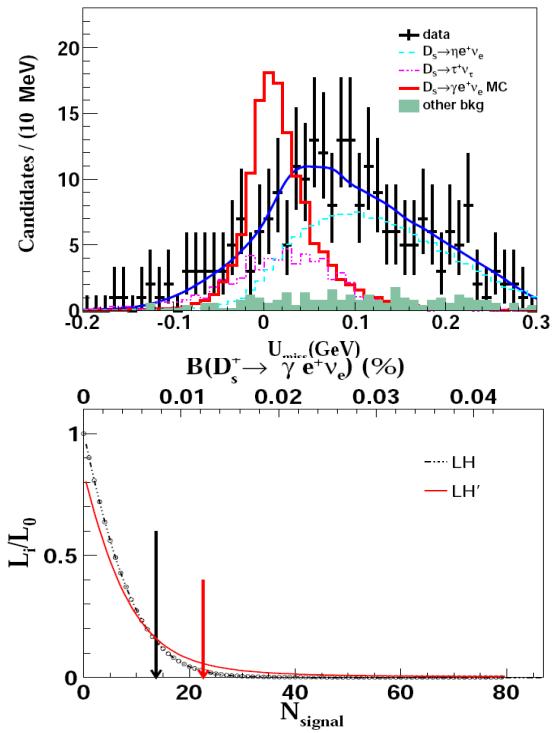


$B[D^+ \rightarrow \gamma e^+ \nu] |_{E_\gamma > 10 \text{ MeV}} < 3.0 \times 10^{-4}$
@90% C.L.

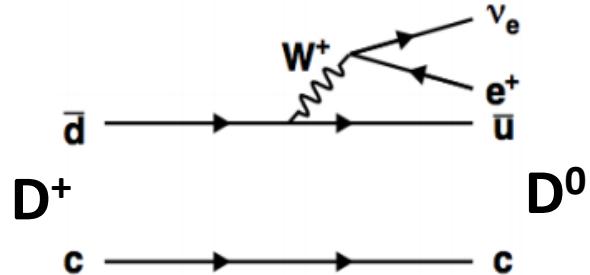
BF expected to be
less than 10^{-3}

Detectable if BF at
level of 10^{-4}

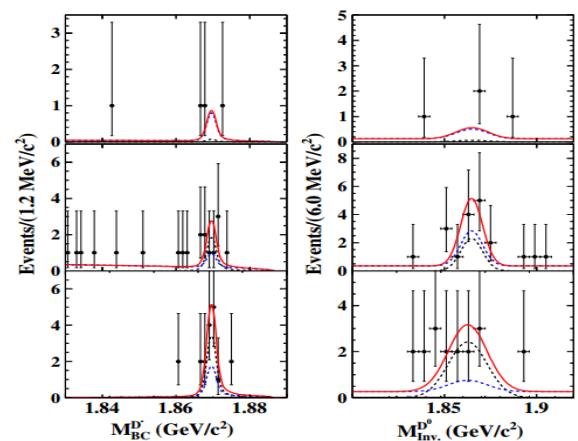
PRD99(2019)072002



$B[D_s^+ \rightarrow \gamma e^+ \nu] |_{E_\gamma > 10 \text{ MeV}} < 1.2 \times 10^{-4}$
@90% C.L.



PRD96(2017)092002

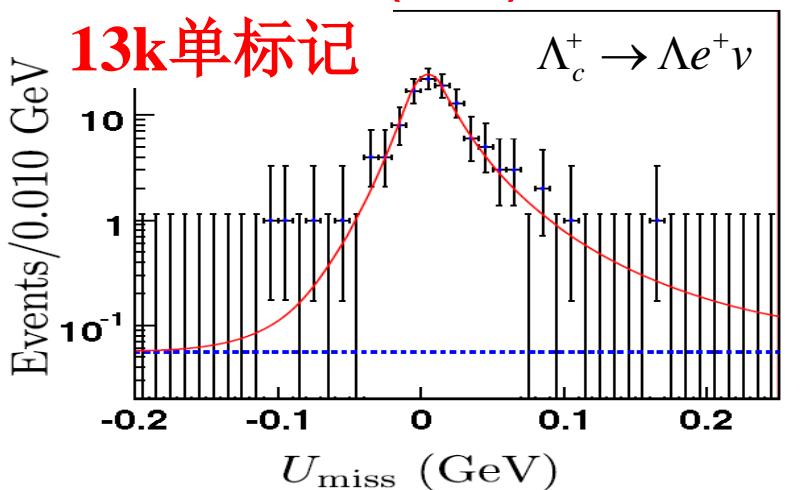


$B[D^+ \rightarrow D^0 e^+ \nu] < 1 \times 10^{-4}$
@90% C.L.

粲重子 Λ_c^+ $\rightarrow\Lambda l^+\nu$ 绝对分支比

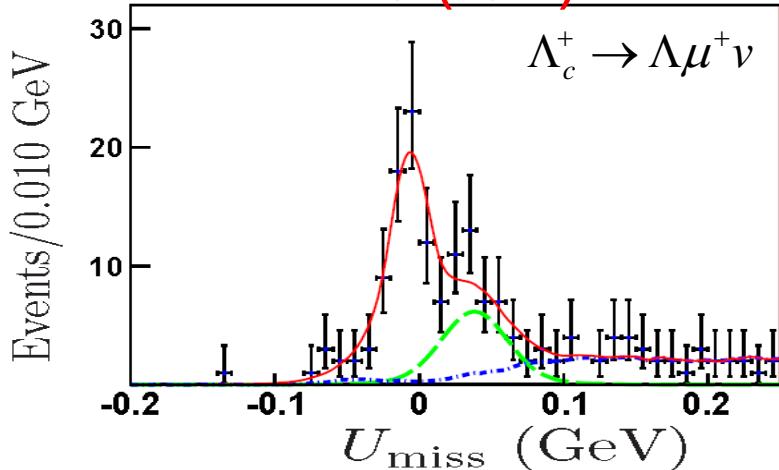
PRL115(2015)221805

13k单标记



$$B[\Lambda_c^+ \rightarrow \Lambda e^+ \nu] = (3.63 \pm 0.38 \pm 0.20)\%$$

PLB767(2017)42



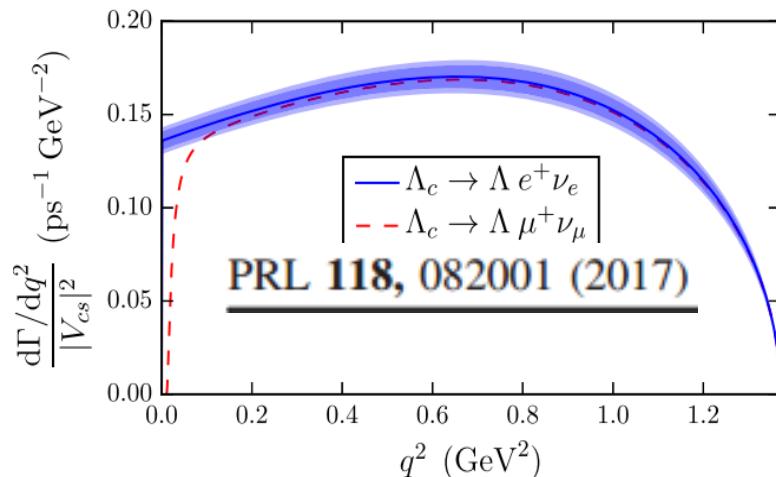
$$B[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu] = (3.49 \pm 0.46 \pm 0.26)\%$$

大大限定理论计算：原有理论计算
(1.4–9.2)%较大范围内

轻子谱适性检验：

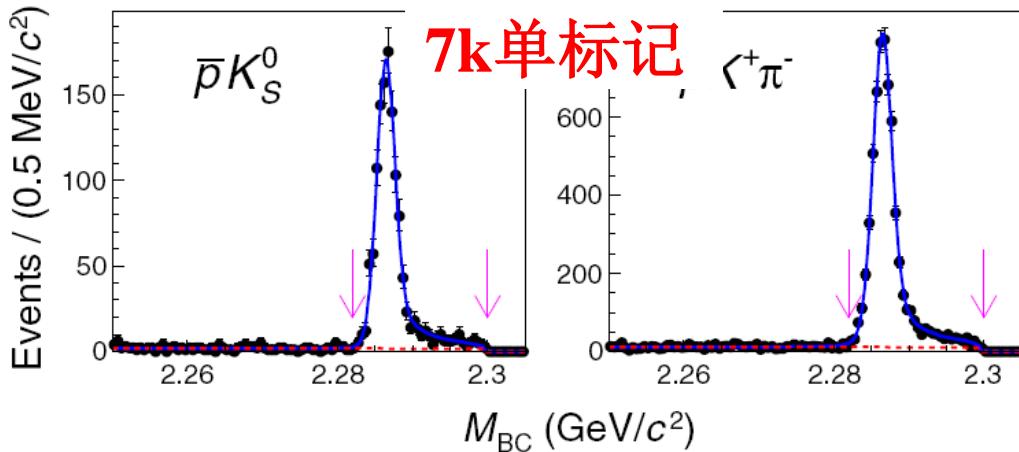
$$\frac{\Gamma[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu]}{\Gamma[\Lambda_c^+ \rightarrow \Lambda e^+ \nu]} = 0.96 \pm 0.16 \pm 0.04$$

引发LQCD计算：BF与BESIII一致



更多数据有望开展形状因子研究

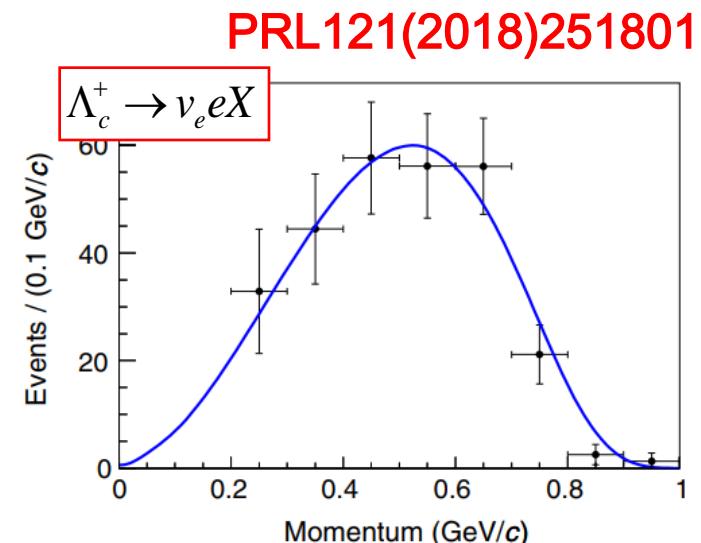
粲重子 Λ_c^+ $\rightarrow e\nu_e X$ 绝对分支比



$$B_{\Lambda_c^+ \rightarrow e\nu_e X} = (3.95 \pm 0.34 \pm 0.09)\%$$

精度显著改进

Result	$\Lambda_c^+ \rightarrow X e^+ \nu_e$	$\frac{\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)}{\Gamma(D \rightarrow X e^+ \nu_e)}$
BESIII	3.95 ± 0.35	1.26 ± 0.12
MARK II [11]	4.5 ± 1.7	1.44 ± 0.54
Effective-quark method [8,9]		1.67
Heavy-quark expansion [10]		1.2



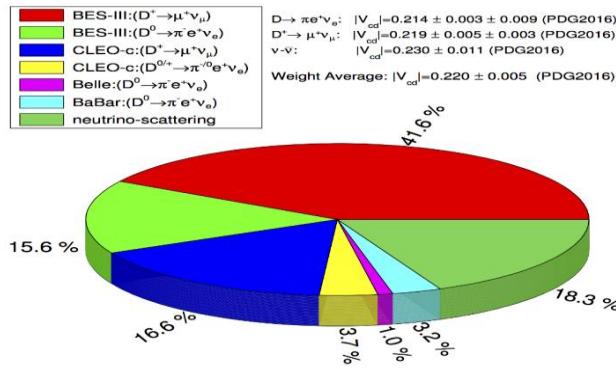
与单举粲介子分宽度之比，能够精密刻度理论预期

Decay channel	\mathcal{B} (%)	Model
$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$	3.63 ± 0.43 [5]	$F_1^V(q^2)$ $= 2.52/5.09 - q^2$ [28]
$\Lambda_c^+ \rightarrow \Lambda(1405) e^+ \nu_e$	0.38 ± 0.38 [30]	PYTHIA [29]
$\Lambda_c^+ \rightarrow n e^+ \nu_e$	0.27 ± 0.27 [31]	PYTHIA [29]

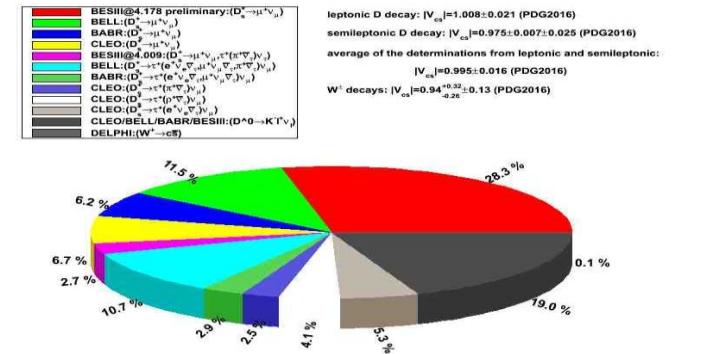
结果表明，没有其他大的遍举电子半轻衰变

Summary and prospect

BESIII实验在粲介子衰变常数、半轻形状因子、轻子普适性检验、 $|V_{cs(d)}|$ 测量和 Λ_c^+ 绝对分支比测量等方面取得重要成果。



$$|V_{cd}|: 4.8 \rightarrow 2.3\%$$



$$|V_{cs}|: 2.5 \rightarrow 1.5\%$$

-- 半轻测量 $|V_{cs(d)}|$ 寄望LQCD大幅改进计算精度

$$|V_{cs}| \rightarrow 1\%$$

-- 现有4.13-4.23 GeV数据，增加约1倍 D_s

-- 未来10 fb^{-1} $\psi(3770)$ 数据：Sev, Aev形状因子研究

$$|V_{cd}| \rightarrow \sim 1.2\%$$

-- 2020年，3-5 fb^{-1} Λ_c^+ @4.6-4.7 GeV： Λ lv形状因子，新衰变

谢谢！