

# CP VIOLATION AND THE BARYON ASYMMETRY

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第17届重味物理与CP破坏研讨会

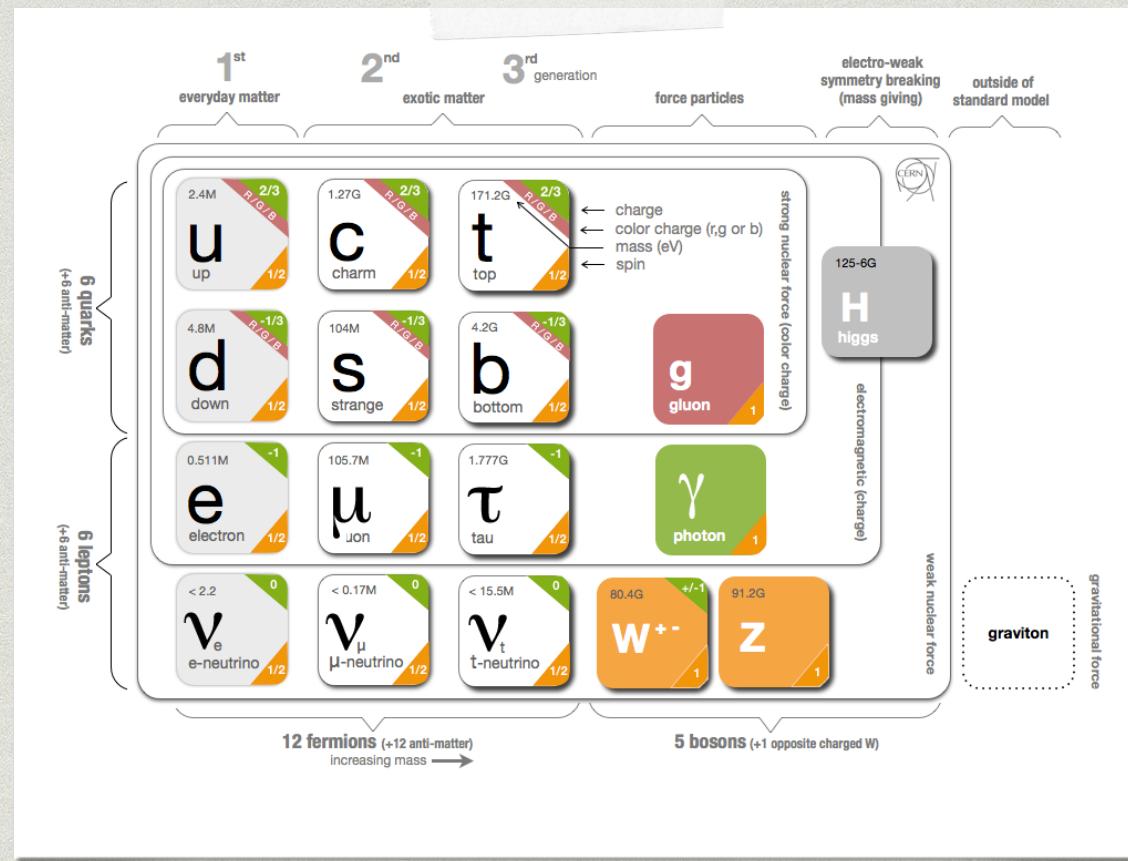
# Outline&preview

- \* Introduction to the baryon asymmetry;
- \* Brief overview of the EWBG;
- \* CP violation @finite temperature;
- \* EWBG from the spontaneous CPV.

## Preview

- ◆ *Show you how to generate the baryon asymmetry of the universe with a spontaneous CPV at the finite temperature.*
- ◆ *Show you how to avoid the constraint on the EWBG arising from the EDM measurement.*

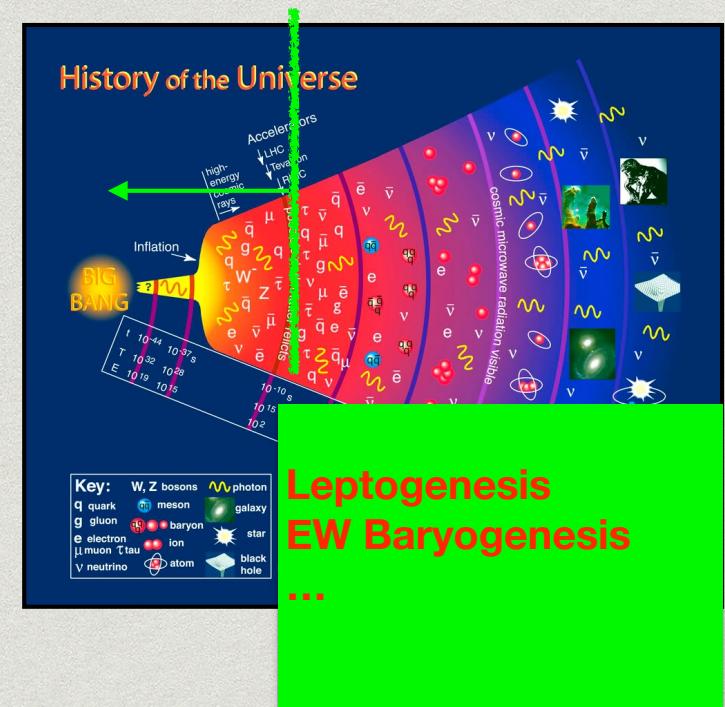
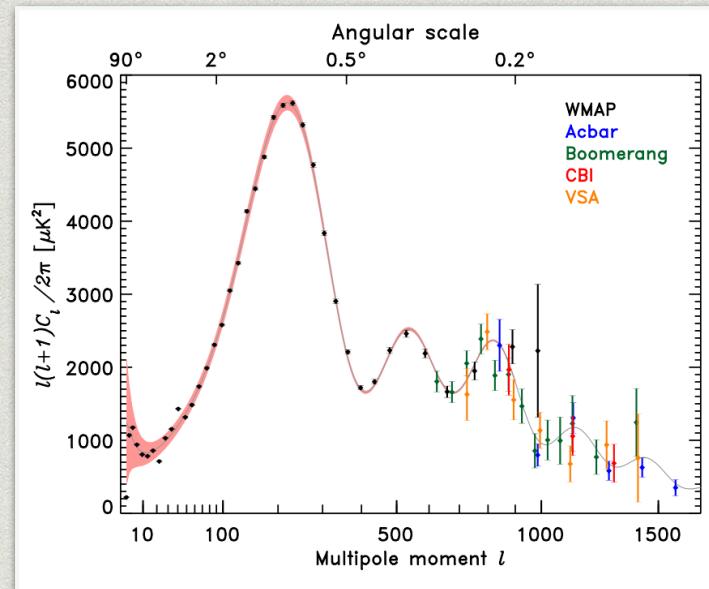
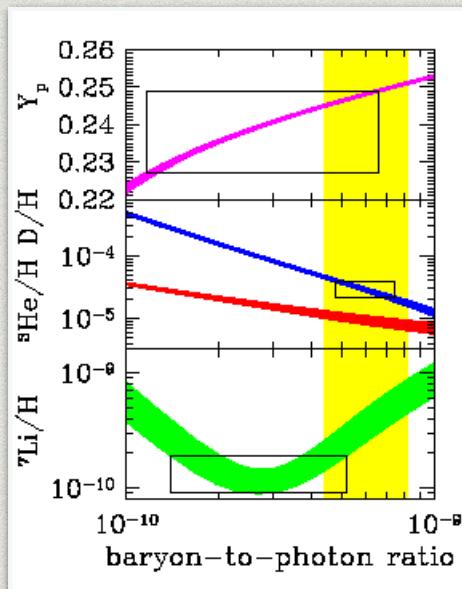
# Particle Zoo



- \* Neutrino masses
- \* Dark matter
- \* Baryon asymmetry

# Baryon asymmetry

- \* No anti-galaxy was observed
- \* The abundance of the primordial elements and the height of the CMB power spectrum depend on the ratio of baryon to photons



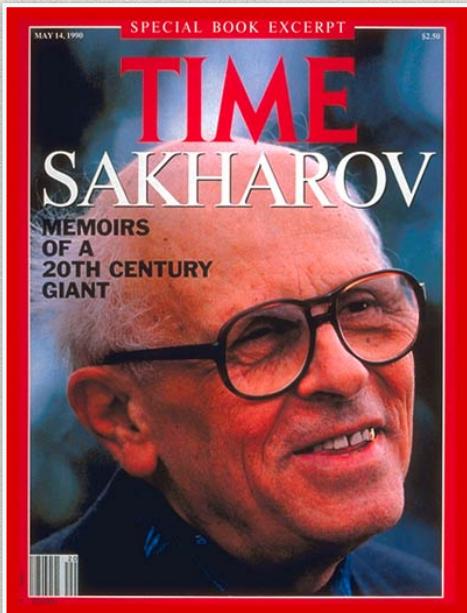
**Baryon asymmetry:**

$$Y_B = \frac{\rho_B}{s} = (8.59 \pm 0.11) \times 10^{-11}$$

(Planck 2015)

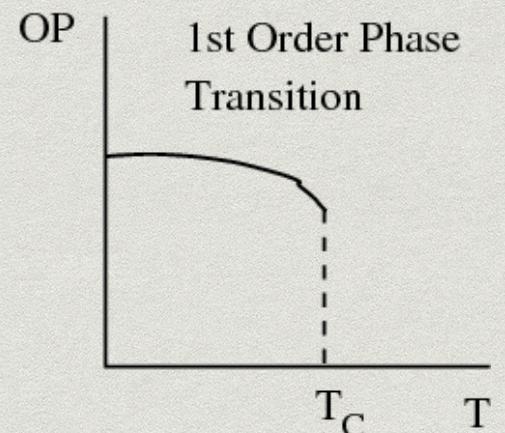
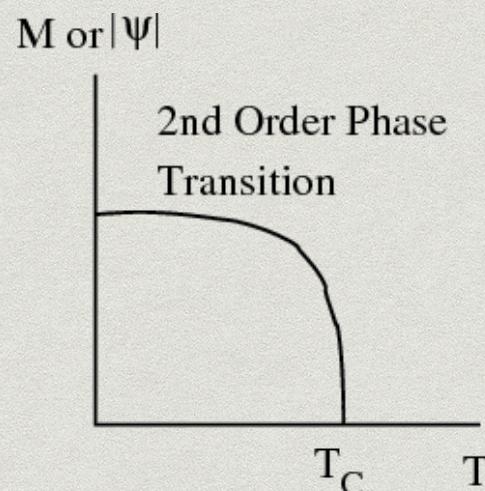
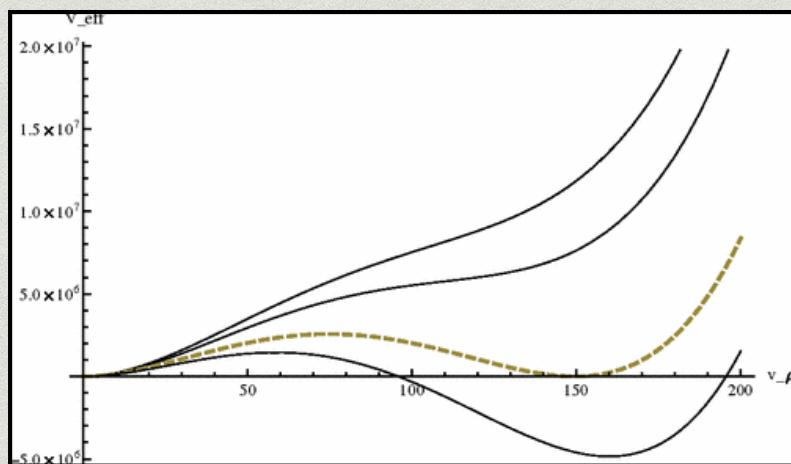
# BAU from First order EWPT

BAU might be generated during the electroweak phase transition



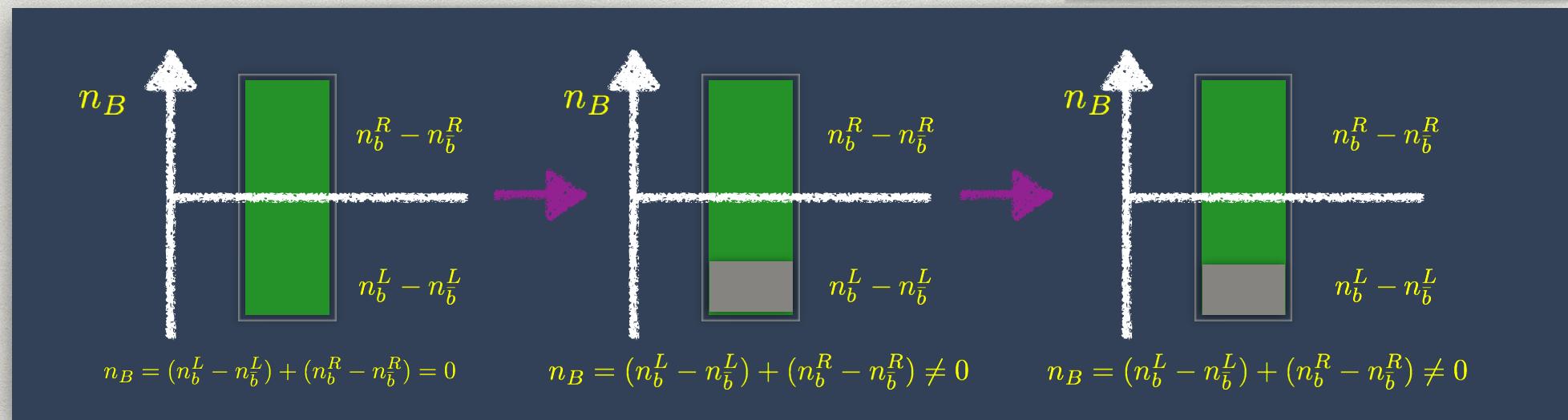
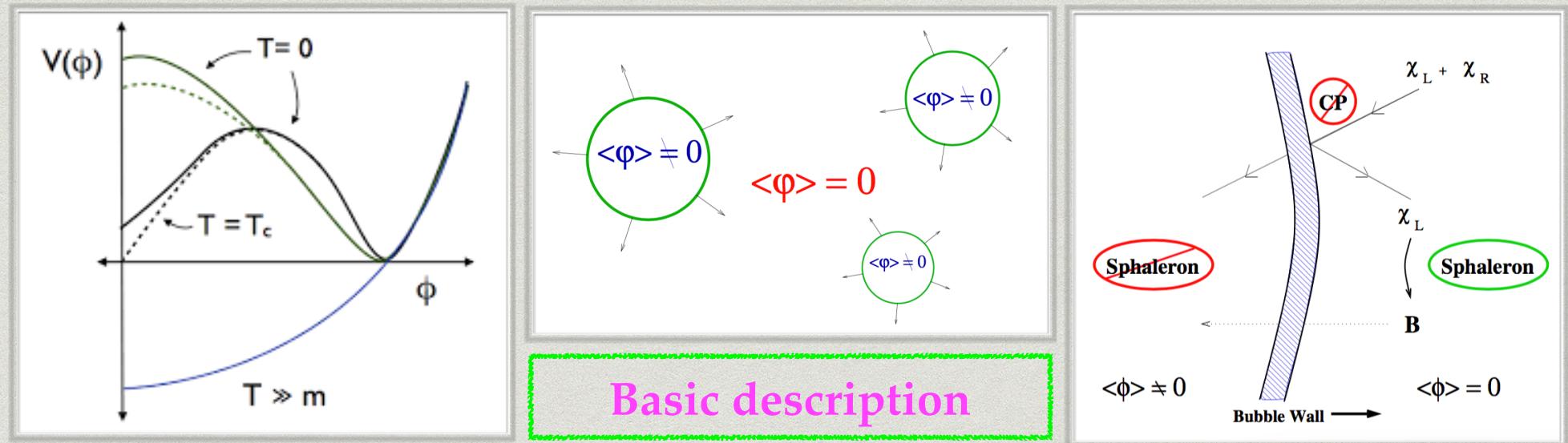
- ★ Baryon number violation
- ★ C&CP violation
- ★ Departure from thermal equilibrium

First order electroweak phase transition if baryon asymmetry is generated during the EWPT without CPT violation.



# Electroweak Baryogenesis

- \* Generate BAU during the electroweak phase transition



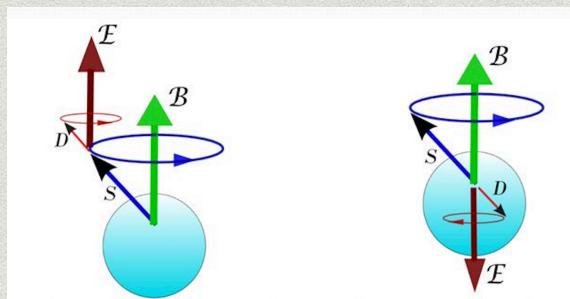
# Fate of the EWBG

## Three Detectives

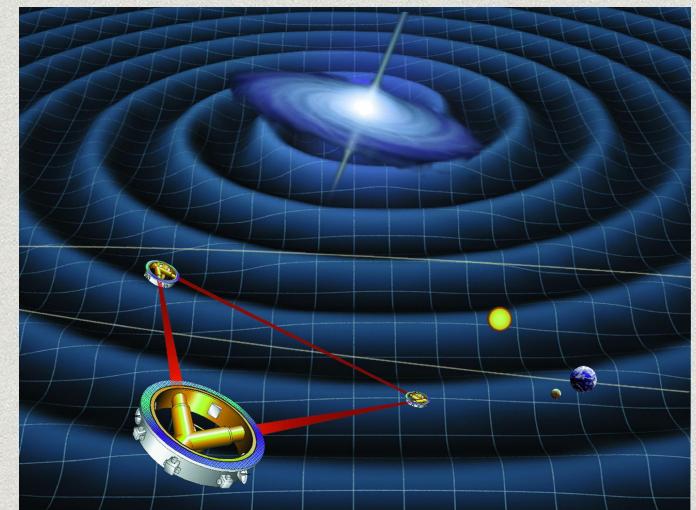
LHC



EDM



GW



Conventional EWBG mechanism might be found or excluded in the near future when these three detection methods are combined.

A typical example: Wino-catalyzed EWBG is excluded by the ACME result(intensity frontier) and the Higgs search results at the LHC(energy frontier).

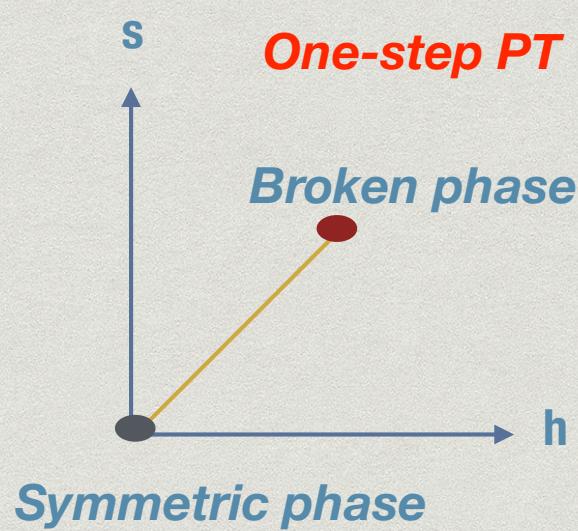
Questions: Is there a mechanism of electroweak baryogenesis that can escape from these hunters?

# Our little aim: a EWBG with less signature

Exploring the scenario of electroweak baryogenesis that may escape from the combined detection of the cosmic, energy and intensity frontiers.

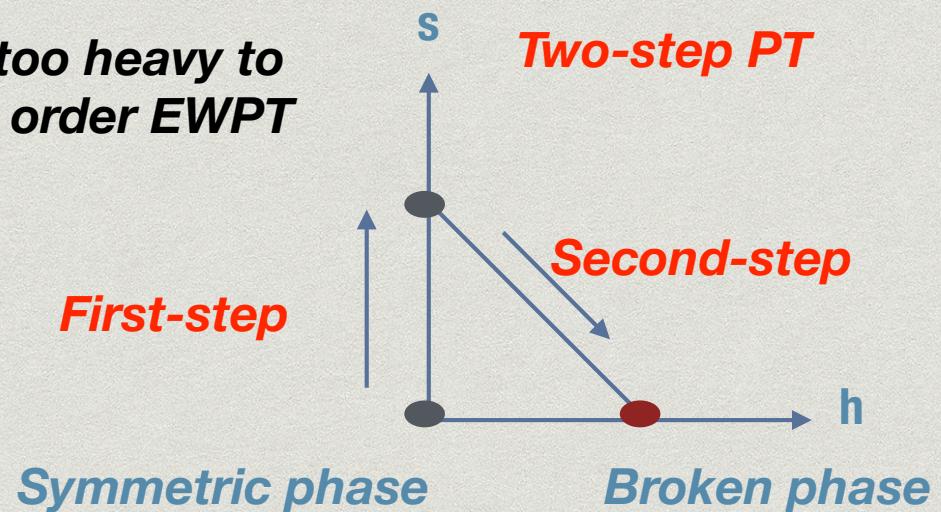
One observation:

A two-step phase transition may avoid constraint arising from Higgs searches at the LHC



The barrier between the symmetric and the broken phase usually comes from radiative corrections

$$V_{\text{eff}}(\phi, T) = \mathcal{A}(T)\phi^2 + \mathcal{B}(T)\phi^3 + \mathcal{C}(T)\phi^4 + \dots$$



The barrier exists at the tree-level  
Merits:  
1. No mixing with the SM Higgs  
2. Correlated with the dark matter

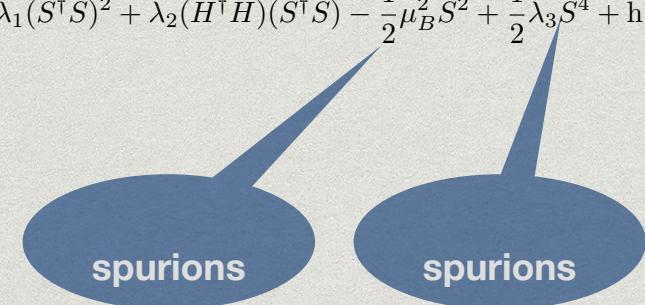
# Our little aim: a EWBG with less signature

Another observation:

There exists spontaneous CP phase in the scalar singlet sector

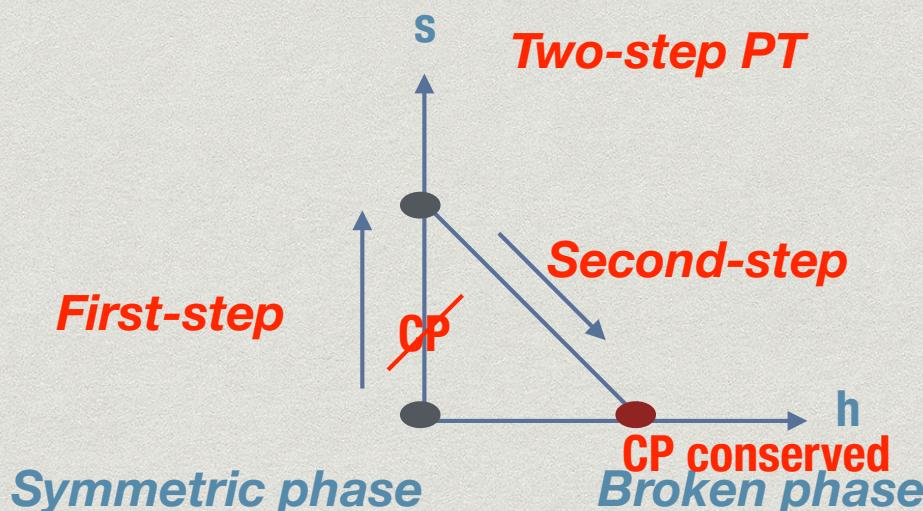
**Lemma:** Haber, Surujon, 2012  
*spontaneous CP violation in the theory of one complex scalar field may occur only when the related U(1) is explicitly broken by at least two spurions whose U(1) charges are different in magnitude*

$$V = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 - \mu_A^2(S^\dagger S) + \lambda_1(S^\dagger S)^2 + \lambda_2(H^\dagger H)(S^\dagger S) - \frac{1}{2}\mu_B^2 S^2 + \frac{1}{2}\lambda_3 S^4 + \text{h.c.}$$



A possible strategy:

There might be spontaneous CPV phase only at finite T!



$$\varphi = \pm \frac{1}{2} \arccos \left[ \frac{\lambda_1 - \lambda_3}{2\lambda_3} \frac{m_\beta^2 - m_\alpha^2}{\lambda_2 v^2 - m_\alpha^2 - m_\beta^2 + 2\Pi_\alpha} \right]$$

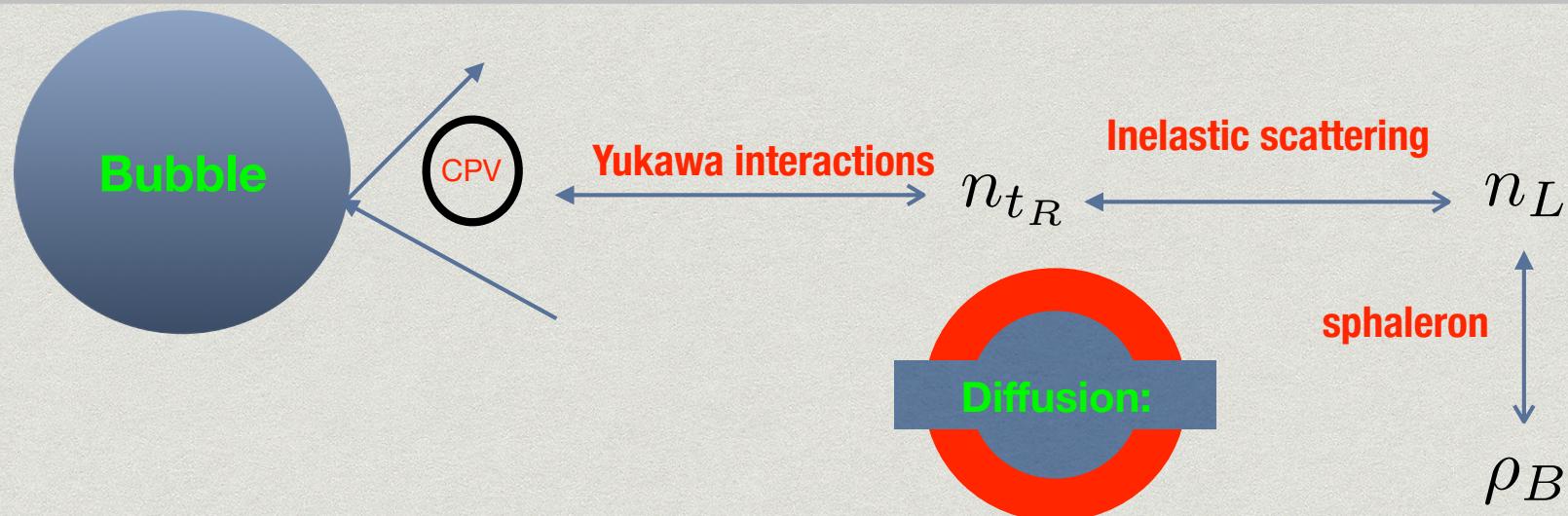
NO constraint of EDM and Higgs search!

# Sketch of the mechanism

## Basic description

- Sakharov:
- {
- \*  $\mathcal{B}$
  - \*  $\mathcal{C} \& \mathcal{CP}$
  - \* First order EWPT

Sphaleron
Spontaneous CPV
Two-step PT



Transport equation:

$$\partial_t \rho_B(x) - D \nabla^2 \rho_B(x) = -\Gamma_{ws} F_{ws}(x)[n_L(x) - R\rho_B(x)]$$

# The model:

**SM+ complex scalar singlets**

**Potential:**

$$V = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 - \mu_A^2(S^\dagger S) + \lambda_1(S^\dagger S)^2 + \lambda_2(H^\dagger H)(S^\dagger S) - \frac{1}{2}\mu_B^2 S^2 + \frac{1}{2}\lambda_3 S^4 + \text{h.c.}$$

**Yukawa:**

$$-\mathcal{L} \sim \frac{1}{\Lambda} \overline{Q}_L \tilde{H} S t_R + \text{h.c.}$$

$$-\mathcal{L} \sim \eta \overline{T}_L S t_R + M \overline{T}_L T_R + \text{h.c.}$$

**$T_{L,R}$ : vector-like top quark**

$$J_{B(F)}(x) = \int_0^\infty dt t^2 \ln \left( 1 \mp \exp \{-\sqrt{t^2 + x}\} \right)$$

$$V_T = \frac{T^4}{2\pi^2} \left\{ \sum_{i \in B} n_i J_B \left[ \frac{m_i^2(h, s, \xi)}{T^2} \right] - \sum_{j \in F} n_j J_F \left[ \frac{m_j^2(h)}{T^2} \right] - \sum_{k \in G} n_k J_B \left[ \frac{m_k^2(h, s, \xi)}{T^2} \right] \right\}$$

\*  **$V_0$ :** The tree-level potential

$$V_{\text{eff}} = V_0 + V_{\text{CW}} + V_T + V_{\text{Daisy}}$$

\*  **$V_{\text{cw}}$ :** Coleman-Weinberg term

$$V_{\text{CW}} = \frac{1}{64\pi^2} \sum_i (-1)^{2s_i} n_i m_i^4(h, s, \xi) \left[ \log \frac{m_i^2(h, s, \xi)}{\mu^2} - C_i \right]$$

\*  **$V_T$ :** Finite temperature contribution

\*  **$V_{\text{ring}}$ :** The ring contribution

$$V_T^{\text{ring}} = \frac{T}{12\pi} \sum_i n_i \left\{ (m_i^2(h, s))^{3/2} - (M_i^2(h, s, T))^{3/2} \right\}$$

# Bubble dynamics

## 1. Bubble nucleation

**Euclidean equation of motion**

$$\frac{d^2\phi}{dr^2} + \frac{2}{r} \frac{d\phi}{dr} - V''(\phi) = 0$$

**Euclidean action for the solution of EoM**

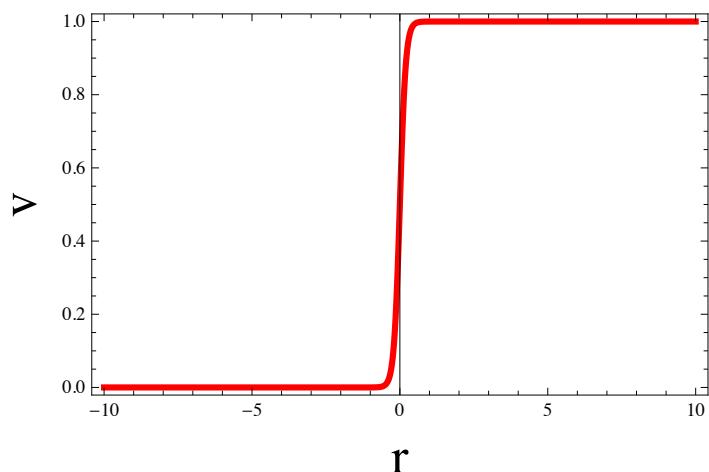
$$S_3 = 4\pi \int r^2 dr \left[ \frac{1}{2} \left( \frac{d\phi}{dr} \right)^2 + V(\phi) \right]$$

**Bubble nucleation rate per unit time per unit volume**

$$\Gamma_n(T) \approx T^4 \left( \frac{S_3(T)}{2\pi T} \right)^{3/2} \exp \left[ -\frac{S_3(T)}{T} \right]$$

**Bounce solution to the background field**

$$V(z) = \frac{1}{2} v(T) \left[ 1 + \tanh \left( 3 \frac{z}{L_w} \right) \right]$$



Vacuum expectation value

$$\overbrace{\qquad\qquad\qquad}^{\langle \phi \rangle \neq 0} \qquad \overbrace{\qquad\qquad\qquad}^{\langle \phi \rangle = 0}$$

bubble  
wall

sound  
shell

$$\overbrace{\qquad\qquad\qquad}^{V_r \approx 0} \qquad \overbrace{\qquad\qquad\qquad}^{V_r > 0} \qquad \overbrace{\qquad\qquad\qquad}^{V_r = 0}$$

Fluid velocity

# Bubble dynamics

## 2. Typical temperatures

**Critical temperature  $T_c$ :**

**Bubble nucleation Temperature  $T_n$ :**

**PT completed Temperature  $T_d$ :**

★**Relationships**

$$T_c > T_n > T_d$$

$$V_{\text{eff}}(\phi_{\text{symmetric}}, T)|_{T_C} = V_{\text{eff}}(\phi_{\text{broken}}, T)|_{T_C}$$

$$\int_0^{t_n} \Gamma V_H(t) dt = \int_{T_n}^{\infty} \frac{dT}{T} \left( \frac{2\zeta M_{\text{pl}}}{T} \right)^4 e^{-S_3/T} = \mathcal{O}(1),$$

$\Gamma$	<b>Bubble nucleation rate</b>
$V_H(t)$	<b>One-horizon volume</b>

$$f(T_d) = \frac{4\pi}{3} \int_{T_d}^{T_c} \frac{dT}{T} \frac{\Gamma(T)}{H(T)^4} v_w^3 \left(1 - \frac{T_d}{T}\right)^3 \equiv 1$$

$H(T)$	<b>Hubble constant</b>
$v_w$	<b>Bubble wall velocity</b>
$f(T)$	<b>Friction of the universe covered by the broken phase</b>

# Bubble dynamics

## 3. Physical parameters relating to PT

$v_w$	<i>Bubble wall velocity</i>	<i>calculated numerically</i>
$l_w$	<i>Bubble wall width</i>	<i>calculated numerically</i>
$\alpha$	<i>Released energy to radiation energy</i>	$\alpha = \Lambda / \rho_{\text{rad}}$
$\kappa$	<i>The efficiency factor</i>	$\kappa = \frac{3}{\varepsilon v_w^3} \int w(\xi) v^2 \gamma^2 \xi^2 d\xi$
$\Lambda$	<i>Latent heat</i>	$\Lambda = \Delta \left( V - \frac{dV}{dt} T \right)$

$v_w$
$l_w$

Relevant to the calculation of baryon number density generated during the EWPT

$\alpha$
$\kappa$
$\Lambda$

Relevant to the calculation of stochastic gravitational wave spectrum emitted during the EWPT

# CP phase and bubble wall width

**EoM for three background fields:**

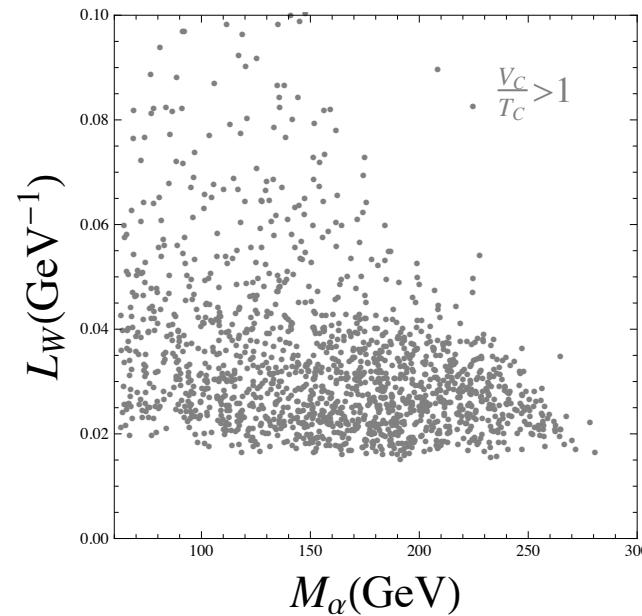
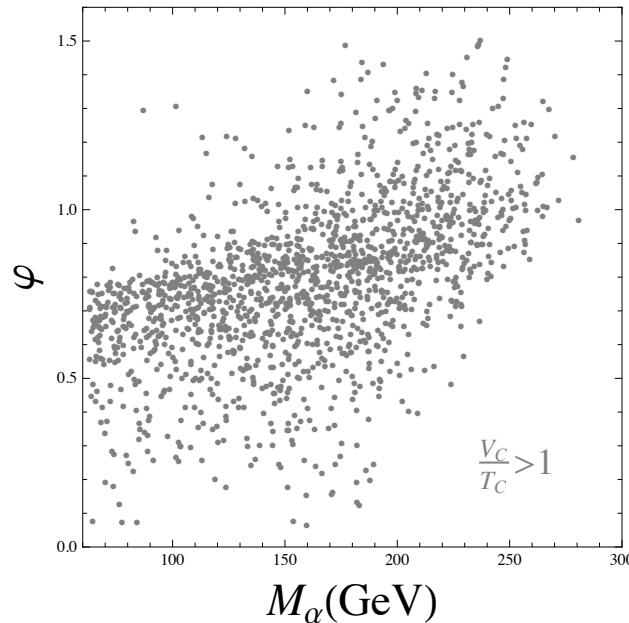
$$\frac{d^2\phi_i}{dr^2} + \frac{2}{r} \frac{d\phi_i}{dr} = \bar{V}'(\vec{\phi})$$

**Bubble wall width:**

$$L_w^2 \approx 1.35 \frac{\lambda + \sqrt{\lambda\lambda_\varrho}}{(\lambda_2 - 2\sqrt{\lambda\lambda_\varrho})[\lambda v_0^2 - \Pi_h(T_C^2)]} \times \left(1 + \sqrt{\frac{\lambda_2^2}{4\lambda\lambda_\varrho}}\right)$$

**Spontaneous CP phase:**

$$\varphi = \pm \frac{1}{2} \arccos \left[ \frac{\lambda_1 - \lambda_3}{2\lambda_3} \frac{m_\beta^2 - m_\alpha^2}{\lambda_2 v^2 - m_\alpha^2 - m_\beta^2 + 2\Pi_\alpha} \right] .$$



# Transport equations

EWBG

*Transport equation*

$$\frac{\partial n}{\partial t} + \nabla \cdot j(x) = - \int d^3z \int_{-\infty}^{x_0} dz^0 \text{Tr}[\Sigma^>(x, z)S^<(z, x) - S^>(x, z)\Sigma^<(z, x) \\ + S^<(x, z)\Sigma^>(z, x) - \Sigma^<(x, z)S^>(z, x)]$$

**Source term:**

$$S_{\text{top}}^{\text{CPV}} = -2\zeta^2 v_s^2 \dot{\varphi} \int \frac{k^2 dk}{\pi^2 \omega_L \omega_R} \text{Im} \left\{ (\varepsilon_L \varepsilon_R^* - k^2) \frac{n(\varepsilon_L) - n(\varepsilon_R^*)}{(\varepsilon_L - \varepsilon_R^*)^2} + (\varepsilon_L \varepsilon_R + k^2) \frac{n(\varepsilon_L) + n(\varepsilon_R)}{(\varepsilon_L + \varepsilon_R)^2} \right\}$$



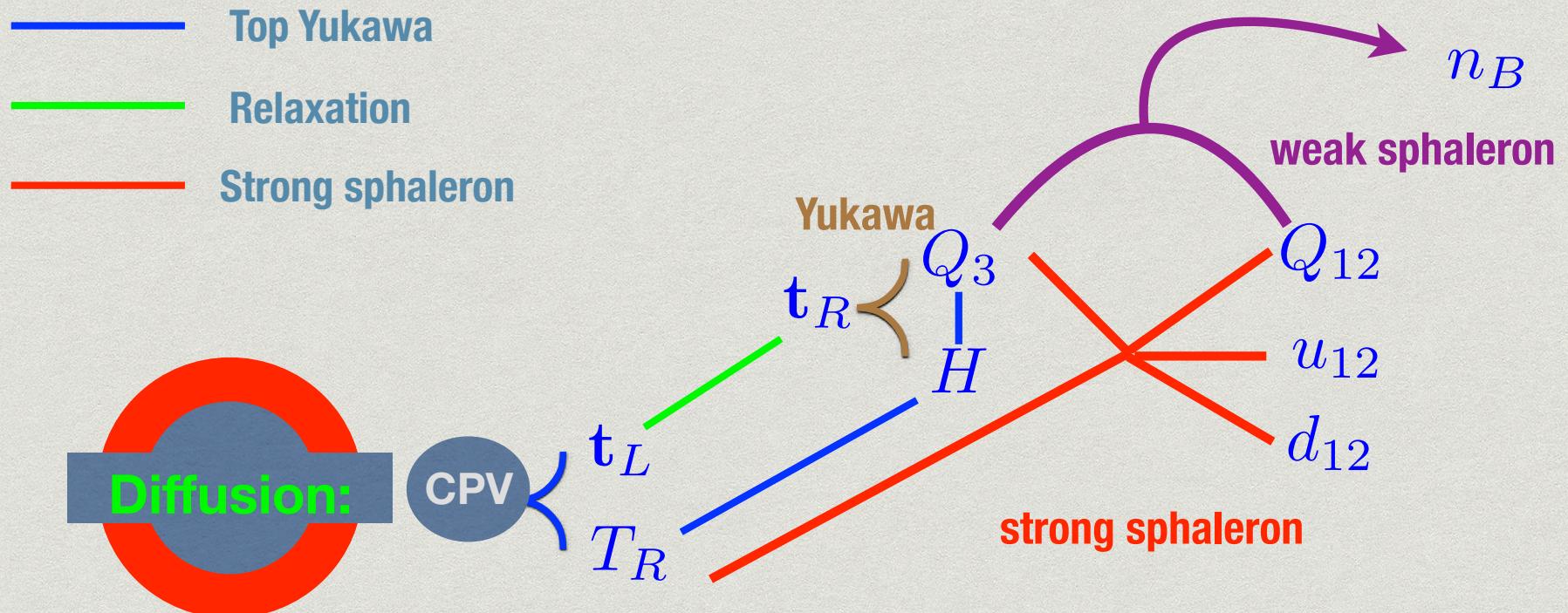
$$\zeta \overline{\mathfrak{t}_L} St_R + (M_{\mathfrak{t}}) \overline{\mathfrak{t}_L} \mathfrak{t}_R + \text{h.c.} \longrightarrow \frac{y_t \zeta}{\Lambda} \overline{Q_3} \tilde{H} St_R$$

**All equations**

$$\begin{aligned} \partial^\mu Q_\mu &= +\Gamma_{m_t} \mathcal{R}_T^- + \Gamma_{Y_t} \delta_t + \Gamma_{y'} \delta_{\mathfrak{t}'} + 2\Gamma_s \delta_s \\ \partial^\mu T_\mu &= -\Gamma_{m_t} \mathcal{R}_T^- - \Gamma_{Y_t} \delta_t - \Gamma_s \delta_s - \Gamma_\zeta \delta_{\mathfrak{t}} \\ &\quad + \Gamma_{\mathfrak{t}}^+ \mathcal{R}_{\mathfrak{t}}^+ + \Gamma_{\mathfrak{t}}^- \mathcal{R}_{\mathfrak{t}}^- + S_{\text{top}}^{\text{CPV}} \\ \partial^\mu \mathfrak{t}_\mu &= +\Gamma_{m_t} \mathcal{R}_\Lambda^- - \Gamma_{\mathfrak{t}}^+ \mathcal{R}_{\mathfrak{t}}^+ - \Gamma_{\mathfrak{t}}^- \mathcal{R}_{\mathfrak{t}}^- + \Gamma_\zeta \delta_{\mathfrak{t}} - S_{\text{top}}^{\text{CPV}} \\ \partial^\mu \mathfrak{t}'_\mu &= -\Gamma_{m_t} \mathcal{R}_\Lambda^- - \Gamma_{y'} \delta_{\mathfrak{t}'} \\ \partial^\mu S_\mu &= -\Gamma_\zeta \delta_{\mathfrak{t}} \\ \partial^\mu H_\mu &= -\Gamma_{Y_t} \delta_t - \Gamma_{y'} \delta_{\mathfrak{t}'} \end{aligned} \tag{13}$$

# Diffusions

EWBG



**Baryon number density:**

$$\hat{n}_B = -\frac{3\Gamma_{ws}}{2D_Q\lambda_+} \int_{-\infty}^{-L_w/2} dz n_L(z) e^{-\lambda_- z}$$

# Damping of the domain wall

EWBG

*Problems*

$$+\varphi + -\varphi = 0$$

*No BAU left*

*Solution: Adding a  $Z_2$  breaking term to the Higgs potential:  $\Delta s + h.c.$*

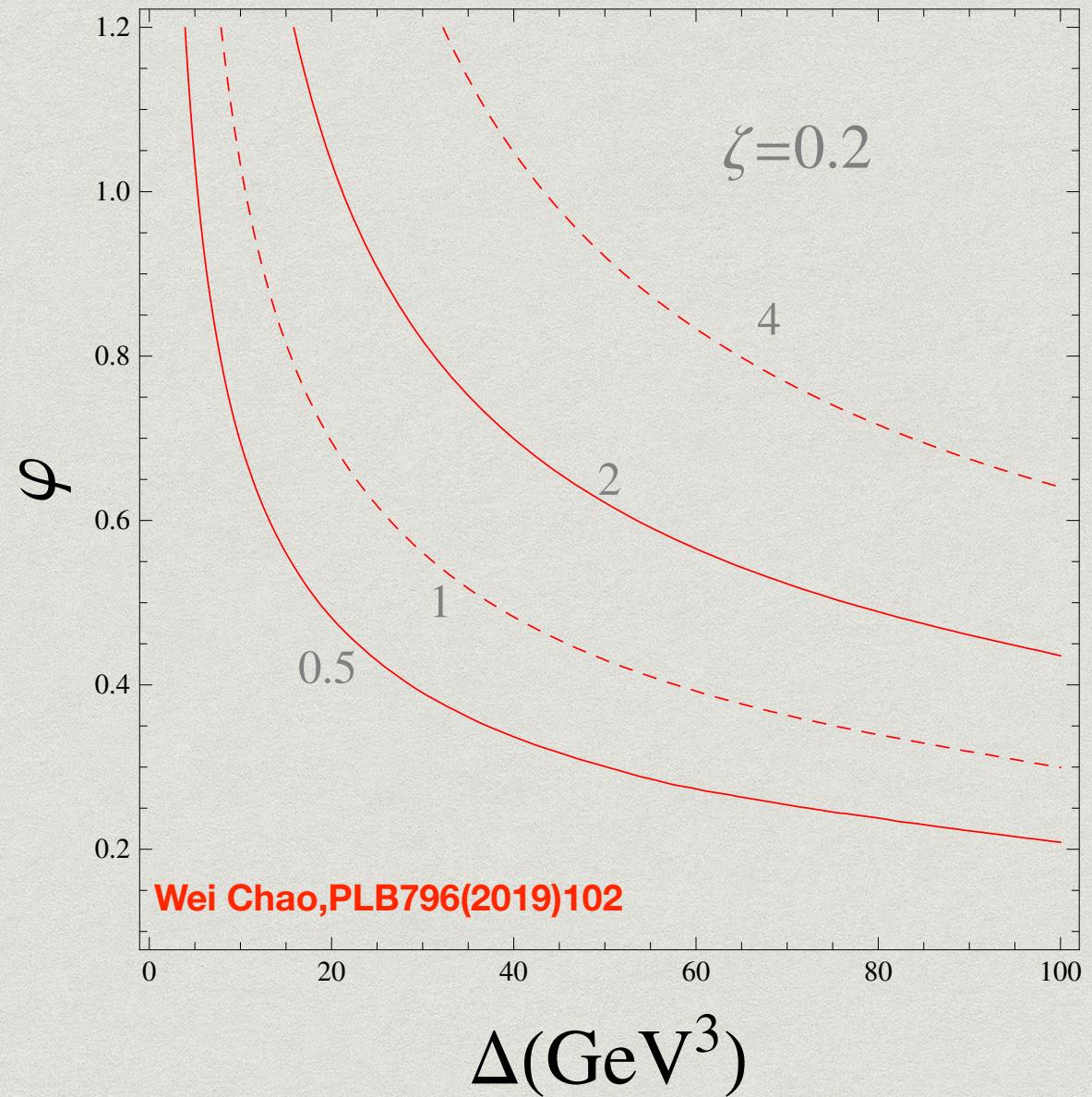
*Ratio of bubbles*

$$\frac{N_+}{N_-} = \exp\left(\frac{\Delta F}{T}\right)$$

*Final BAU*

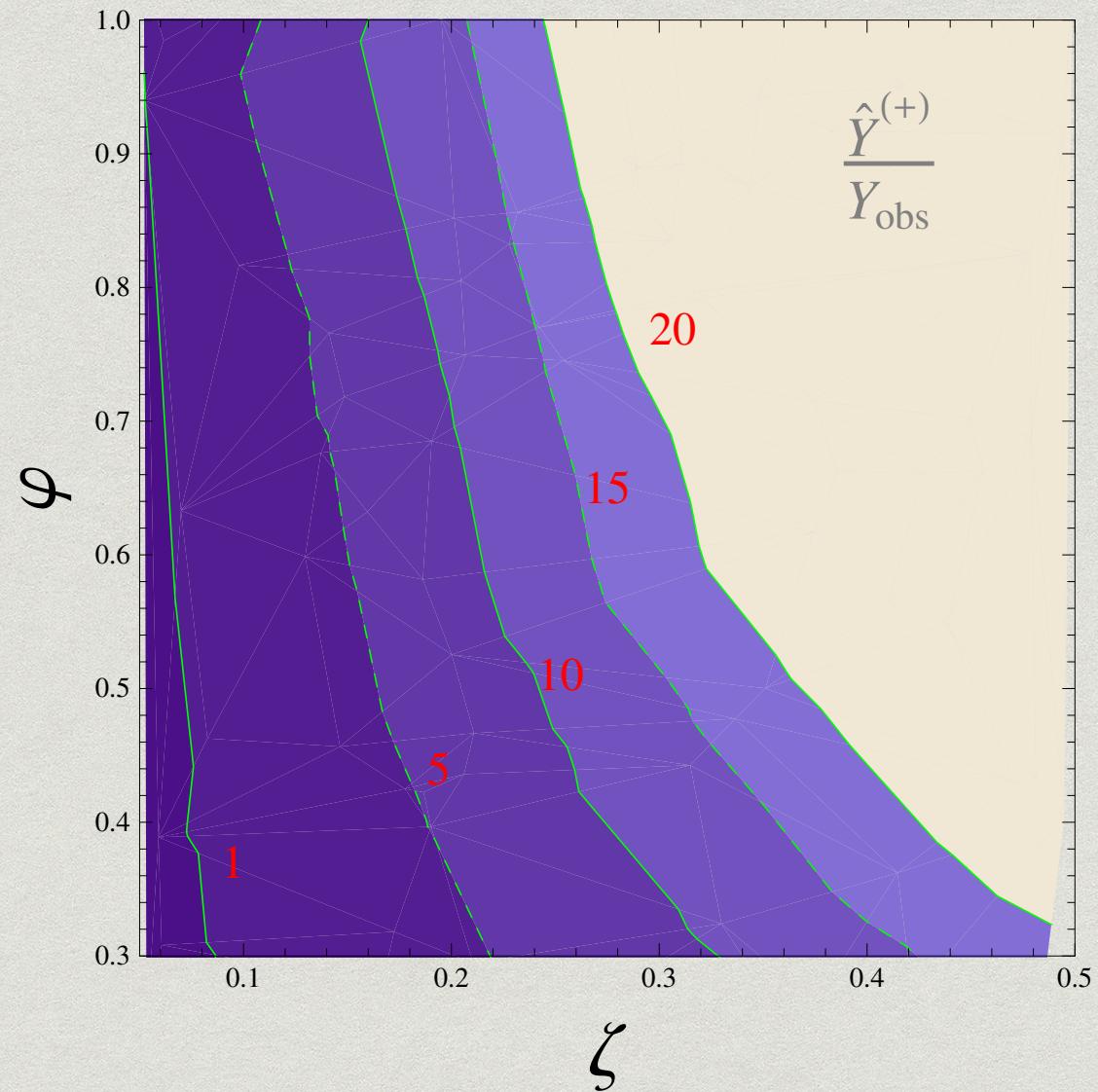
$$n_B = \hat{n}_B^{(+)} \frac{N_+ - N_-}{N_+ + N_-}$$

# Numerical results



# Numerical results

Wei Chao,PLB796(2019)102



# Summary

- ◆ Physics relevant to electroweak phase transition are briefly reviewed.
- ◆ The baryon asymmetry of the universe generated during the first order EWPT is discussed, especially I showed how to generate sufficient BAU with the spontaneous CP phase and a two-step EWPT.

# Advertisement

## 第三届北师大暗物质研讨会

6-9 December 2019  
Asia/Shanghai timezone

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Overview

Scientific Programme

Timetable

Registration

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Participant List

暗物质是具有确凿实验证据的超出标准模型的新物理，也是当前高能物理实验和理论研究的前沿热点课题。近年来，暗物质的实验研究不断取得突破性进展，暗物质-核子弹性散射截面的排除线精度不断提高、COHERENT实验观测到中微子-核子相干弹性散射（暗物质直接探测的主要背景）、XENON1T实验观测到双 $\beta$ 衰变。此外，WIMP的直接探测也进入了关键时期，各种新的针对轴子和Sub-GeV暗物质的直接探测思想不断涌现。这些都为中国的暗物质研究提供了机遇和挑战。

为了促进国内高能物理界学术交流、推动我国暗物质理论和实验研究的发展、寻求高能物理与其他学科领域交叉的可能性，北京师范大学和北京大学高能物理研究中心将于2019年12月07日至09日在北京师范大学珠海校区联合举办第三届北师大暗物质研讨会。会议主题将针对所有暗物质相关的课题。诚挚邀请您参加此次会议。

会议地点：北师大珠海校区，珠海市  
注册费：1200元（老师和博士后），600元（学生）  
注册截止：2019年10月31日。

主办单位：北京师范大学、北京大学高能物理研究中心  
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会务联系人：  
杨硕尧（北京师范大学）： yangshuoya@bnu.edu.cn

Starts Dec 6, 2019 08:00  
Ends Dec 9, 2019 18:00  
Asia/Shanghai

<https://indico.ihep.ac.cn/event/10365/>



**Thank you**