Large v_2 with small cross section

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Int. Workshop on "Partonic and Hadronic Transport Approaches for Relativistic Heavy Ion Collisions"

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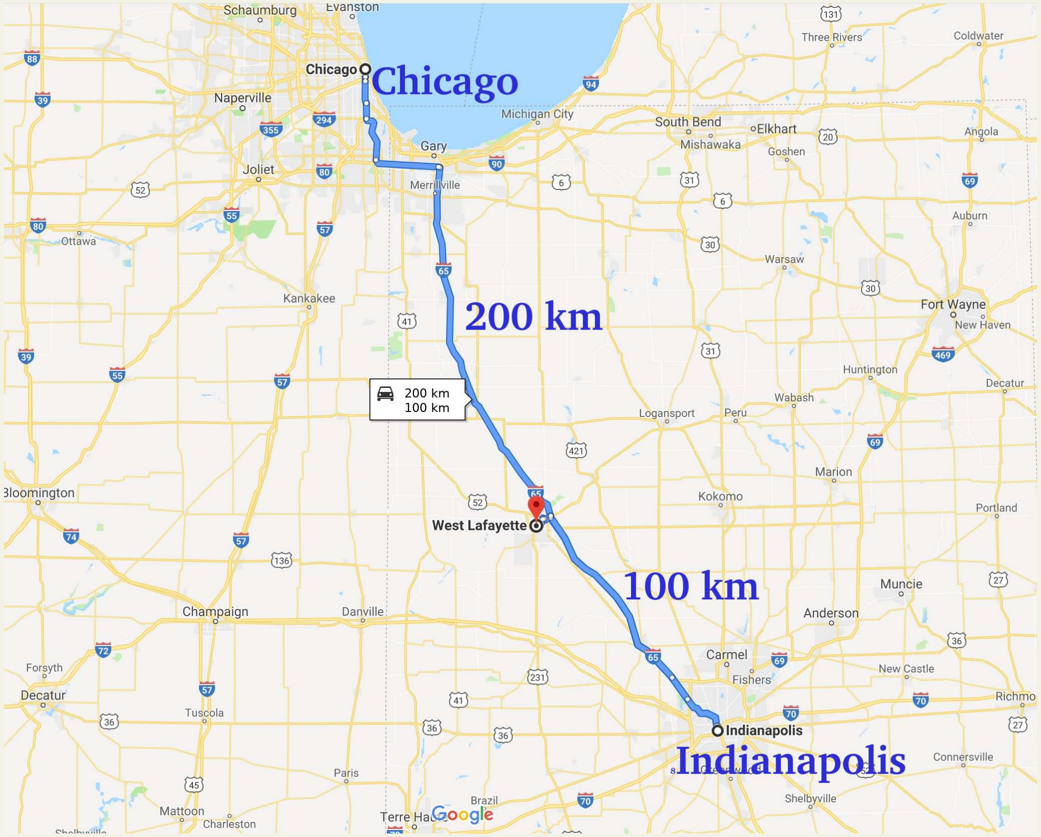


Purdue University

→ **www.purdue.edu**

∼ **2 hrs to Chicago (QM2017)**
∼ **1 hr to Indianapolis (F1 racing)**

- ∼ **50 000 students**
- ∼ **150 physics grad students**
- ∼ **60 physics professors**

High-E Nuclear Physics Group

→ **Fuqiang Wang, Wei Xie, DM**

Outline

I. AMPT puzzle (hydro vs small cross sections)

II. Covariant transport and MPC

III. Understanding AMPT through MPC comparisons

IV. Summary - how small cross sections can work

A Multi-Phase Transport

Lin, Ko et al, PRC72 ('05)

full-fledged multicomponent event generator

$$\text{AMPT} \approx \text{Lund string model (HIJING)} + 2 \to 2 \text{ parton cascade (ZPC)} + \text{hadron transport (ART)}$$

version with "string melting":

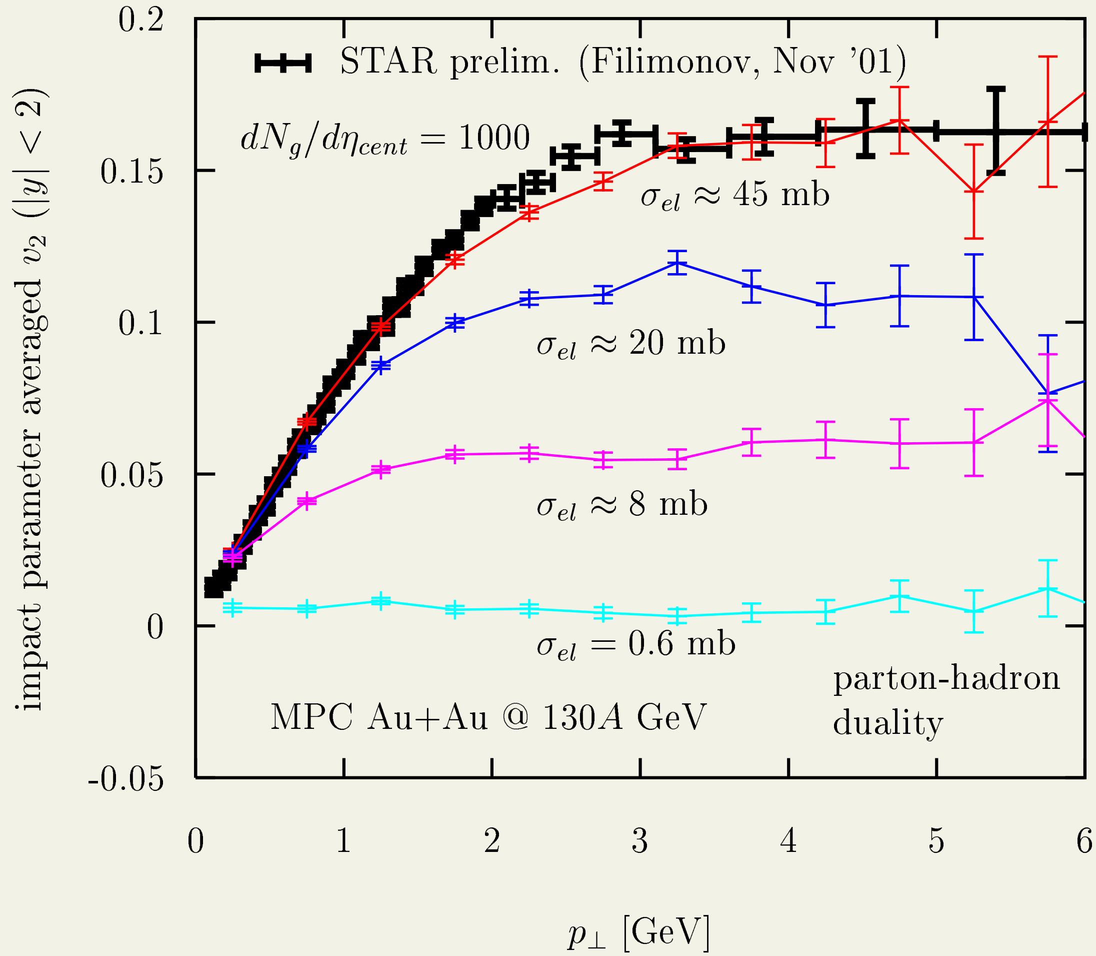
- **energy density in strings converted to quanta (quarks/antiquarks)**
- $\to$ **fluctuating initial geometry (random nucleon positions)**
- **hadronization via coalescence**

explains quite well a wide range of A+A observables

- **using small ~ 3 mb partonic cross sections (!?)**

Parton opacity puzzle

DM & Gyulassy, NPA 697 ('02): **$v_2(p_T, \chi)$ in Au+Au at RHIC**



parton transport model MPC

$2 \to 2$ only, forward-peaked

$\sigma_{tr} \approx 0.3\sigma_{tot}$

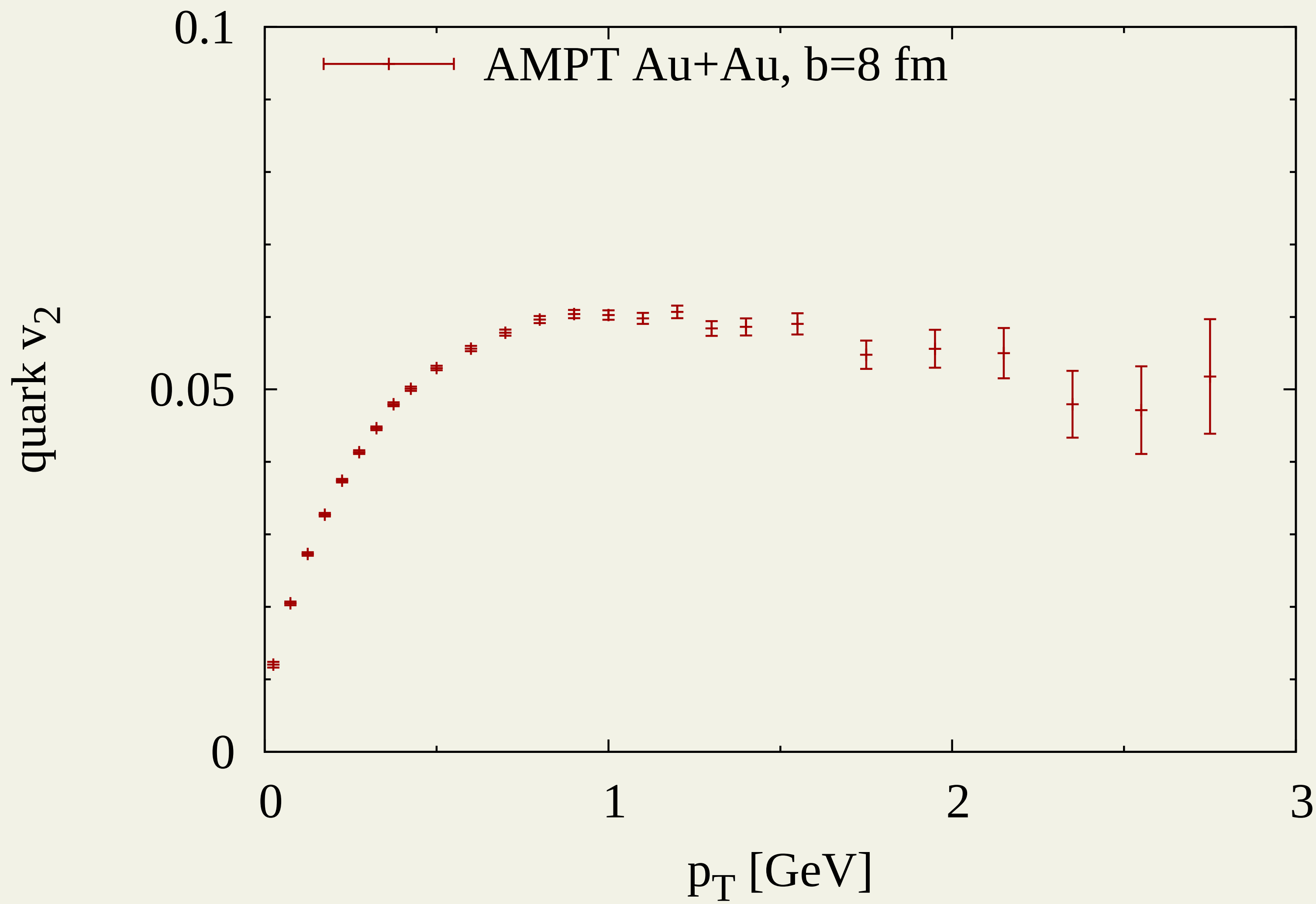
Au+Au @ 130 GeV, $b = 8$ fm

- minijet initconds
- 1 parton $\to$ 1 π hadronization

perturbative $\sigma_{gg\to gg} \approx 3$ mb gives $v_2 \approx 2\%$ $\to$ need $15\times$ higher opacity

radiative $gg \leftrightarrow ggg$ helps (e.g., BAMPS)... but AMPT has pure elastic $2 \to 2$

quark v_2 from AMPT for 200-GeV Au+Au, b=8 fm



$v_2 \approx 6\%$ **with only** $\sigma_{qq} = 3$ **mb... yet** $\sim$**15% hadron** v_2 **(30% centrality)**

v_2 amplified by coalescence

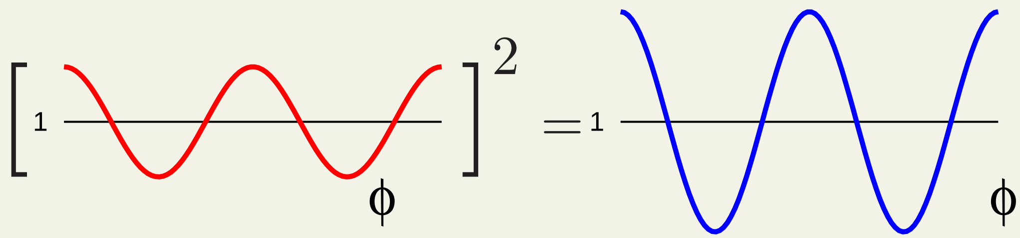
Ko, Lin, Voloshin, DM, Greco, Levai, Mueller, Fries, Bass, Nonaka, Asakawa ...

coalescence of comoving quarks: $q\bar{q} \Rrightarrow\longrightarrow M \qquad 3q \Rrightarrow\Longrightarrow B$

DM & Voloshin, PRL91 ('03)

$$\frac{dN_M(p_T)}{d\phi} \propto \left[\frac{dN_q(p_T/2)}{d\phi}\right]^2$$

$$\frac{dN_B(p_T)}{d\phi} \propto \left[\frac{dN_q(p_T/3)}{d\phi}\right]^3$$

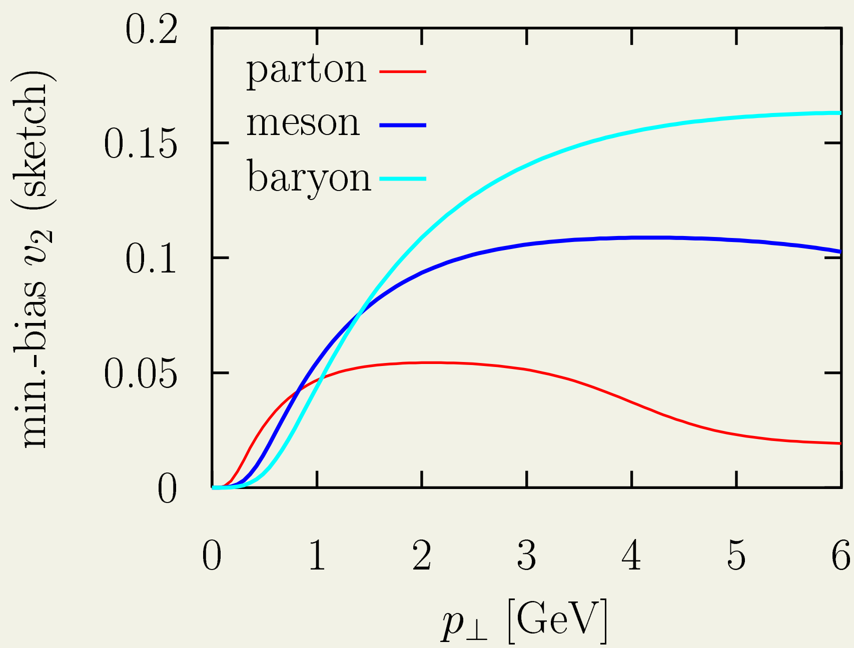


squared/cubed probability $\rightarrow$ amplified v_2

$$v_2^{hadron}(p_\perp) \approx n \times v_2^{quark}(p_\perp/n)$$

$3\times$ **for baryons**
$2\times$ **for mesons** } **50% larger v_2 for baryons**

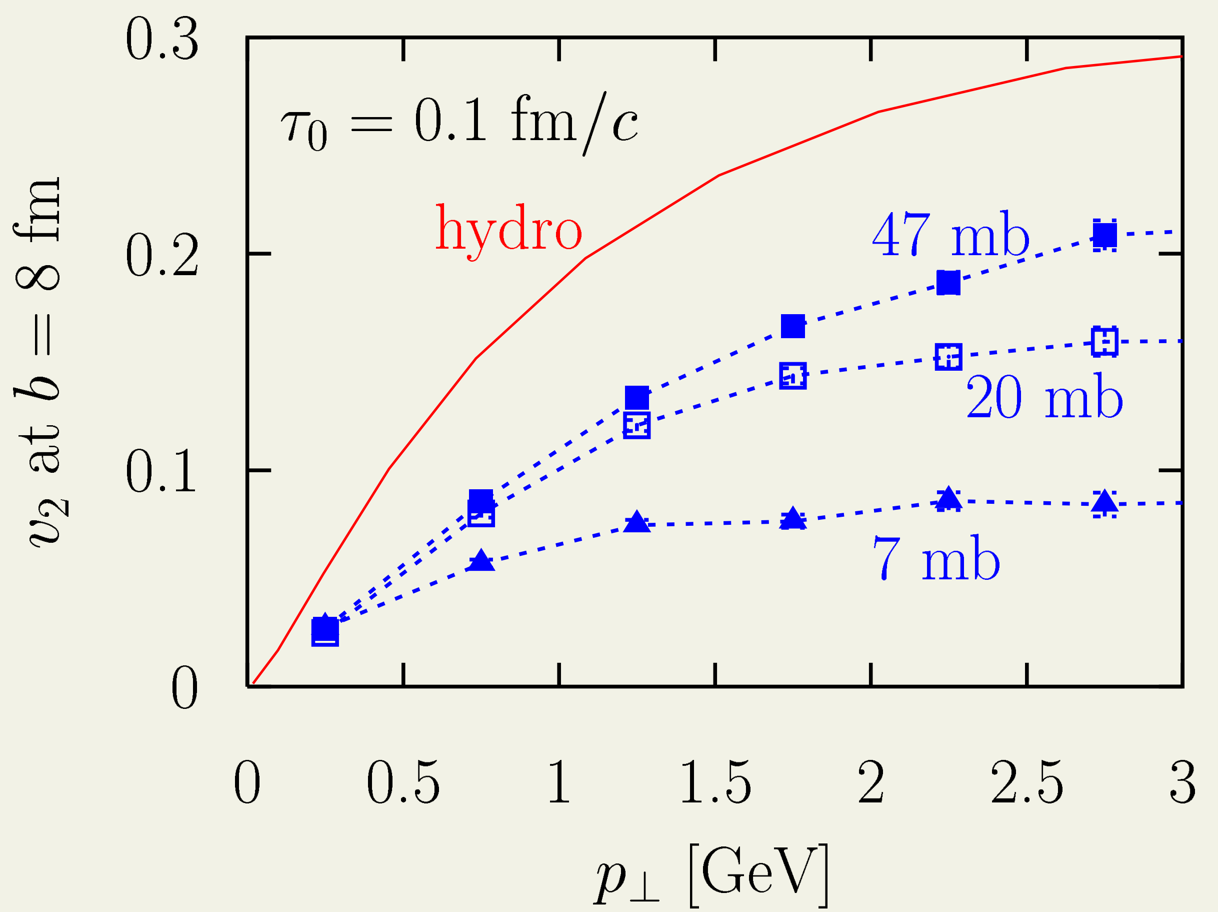
$\rightarrow 5\times$ **for pentaquark,** $6\times$ **for deuteron**



$\Rightarrow$ **AMPT can get hadron v_2 with lower opacity... in principle**

could we be in or near the hydro limit? $\rightarrow$ No.

DM & Huovinen, PRL94 ('05)

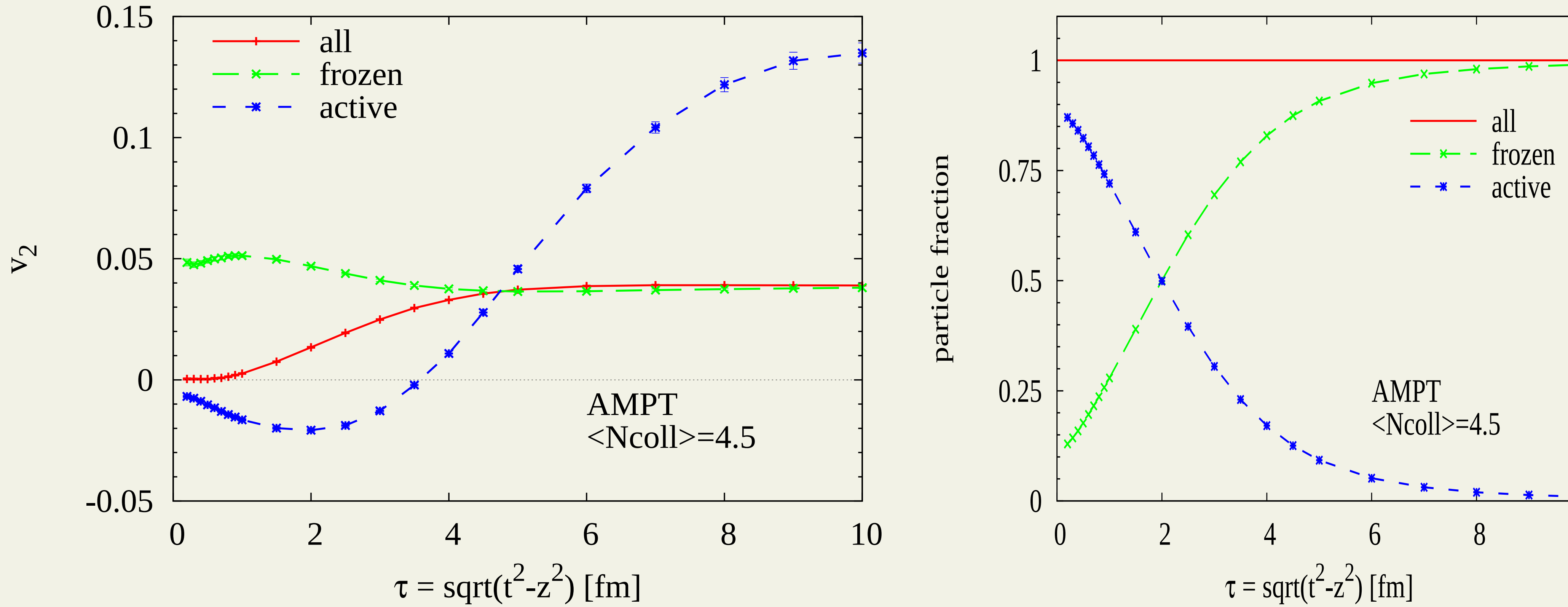


- $2 \rightarrow 2$ **parton kinetic theory is definitely not ideal hydro**
- **for large $\sigma \sim 40 - 50$ mb, viscous hydro is reachable** Huovinen & DM, JPG35 ('08)

AMPT $\neq$ Hydro

AMPT's v_2 comes from "anisotropic escape" He et al, PLB 753 ('15); Li et al, ...

DM et al ('15): **AMPT v_2 vs Bjorken τ**



- **for long time, still interacting partons carry nearly zero or even negative v_2**
- **almost all v_2 is carried by frozen-out partons**
- **the combined parton v_2 rises than saturates as expected** Ko, Zhang, Gyulassy ('99)

AMPT still gets $v_2 \sim 6$% for quarks with only 3 mb... but how?

Test: use parton transport MPC to check AMPT's partonic stage

1) dynamics - issue of parton subdivision

2) initconds - AMPT vs just minijets

focus on 200-GeV Au+Au at RHIC, fixed $b = 8$ fm impact parameter

Covariant transport

(on-shell) phase-space density $f(x,\vec{p}) \equiv \frac{dN(\vec{x},\vec{p},t)}{d^3x d^3p}$

transport equation (BTE):

$$p^\mu \partial_\mu f_i(x,p) = C^i_{2\to 2}[\{f_j\}](x,p) + C^i_{2\leftrightarrow 3}[\{f_j\}](x,p) + \cdots$$

with, e.g.,

$$C^i_{2\to 2} = \frac{1}{2}\sum_{jkl}\int_{234} (f^k_3 f^l_4 - f^i_1 f^j_2) W^{ij\to kl}_{12\to 34} \qquad \left(\int_j \equiv \int \frac{d^3p_j}{2E_j}\ , \qquad f^k_a \equiv f^k(x,p_a) \right)$$

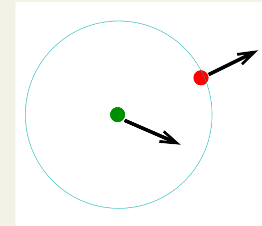
thermalizes (in box), fully causal and stable $\to$ **can derive hydro eqns**
e.g., Denicol, Rischke et al

handles both high or low opacities $\to$ **usable for fluid-to-particle conversion**
e.g., Teaney, Moore & Dusling; DM & Wolff, ...

hydro limit: transport coeffs & rel. times $(\eta \approx 1.2T/\sigma,\ \tau_\pi \approx 1.2\lambda_{tr}\ \ldots)$

$\exists$ **covariant transport codes: ZPC** (Zhang), **MPC** (Molnar), **BAMPS** (Xu), **...**

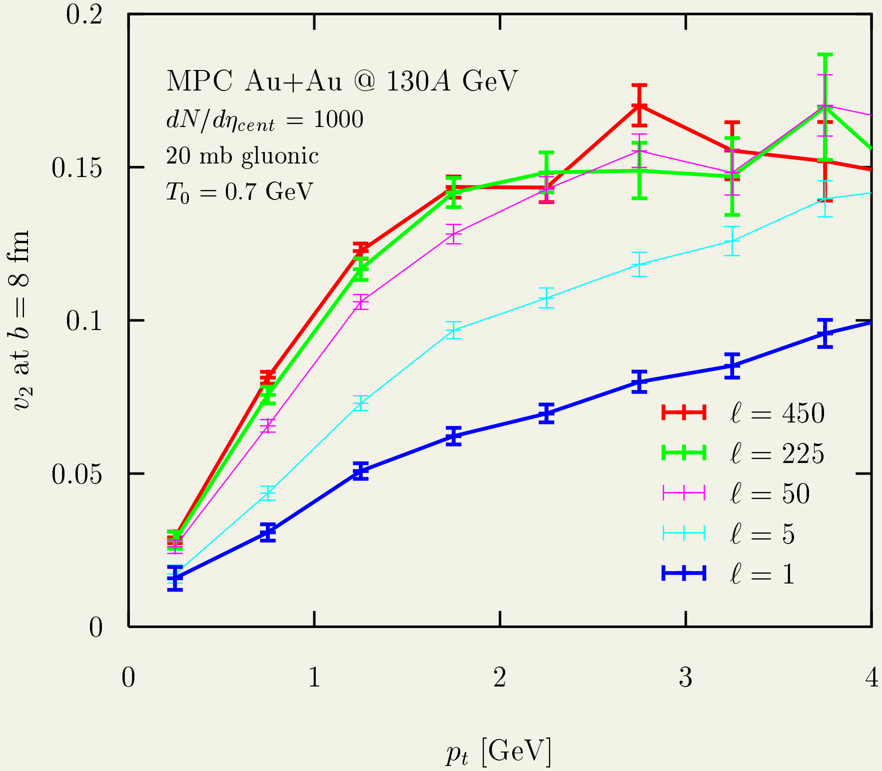
Parton subdivision



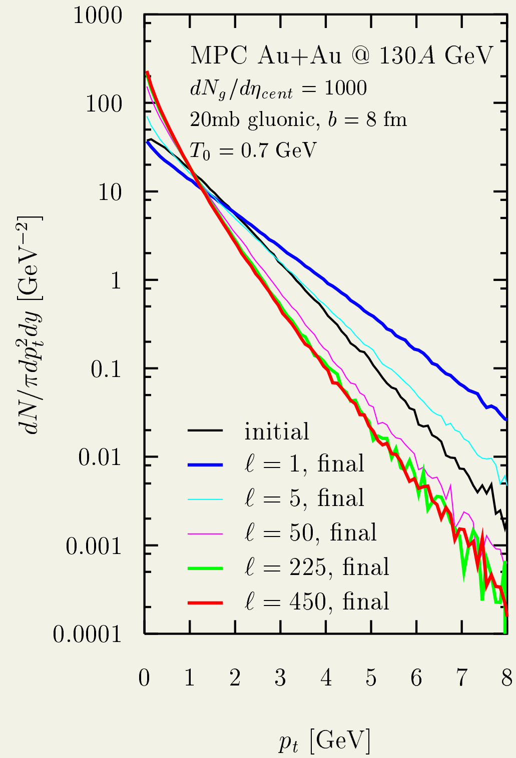
Nonlocal artifacts: due to action at distance $d < \sqrt{\frac{\sigma}{\pi}}$

subdivision: rescale $f \to f \cdot \ell$, $\sigma \to \sigma/\ell$ $\Rightarrow$ $d \propto \ell^{-1/2}$ **local as $\ell \to \infty$**

DM & Gyulassy ('02): $v_2(p_T)$



spectra



- **ZPC could do subdivision, but AMPT runs it with $\ell = 1$**
- **high RHIC opacities: need subdivision $\ell \sim \mathcal{O}(100)$ to remove artifacts in v_2**

Initial conditions (Au+Au at RHIC)

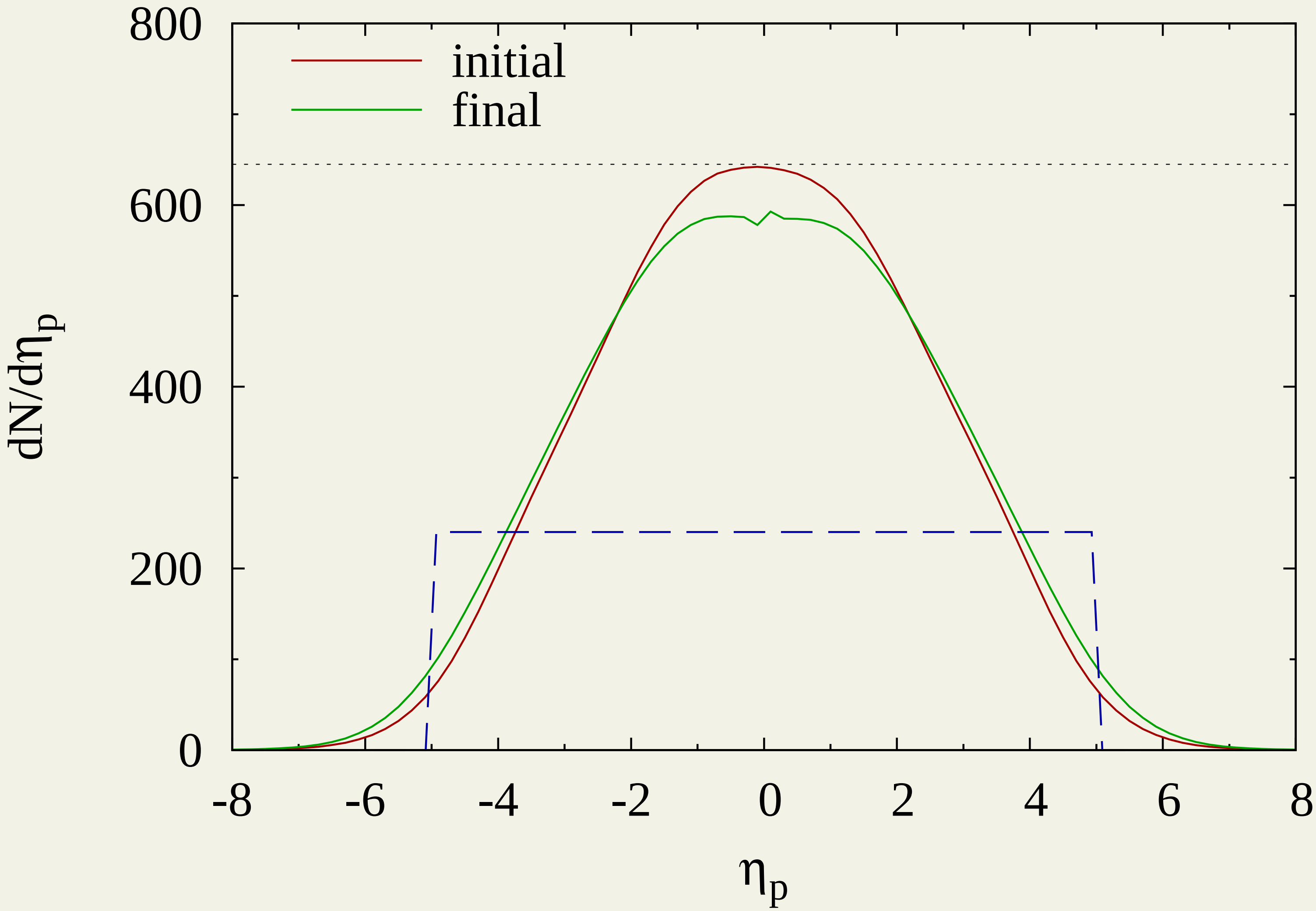
Molnar-Gyulassy study: boost-invariant fit to HIJING minijets

- massless gluons
- flat $dN_g/d\eta(b=0) = 1000 \Rightarrow dN/d\eta(b = 8\ \mathrm{fm}) \approx 240$
- locally thermal $T_0 = 0.7$ GeV, $f = N(\vec{x}_T)e^{-m_T \cosh(\eta-y)/T_0}$
- constant formation time $\tau_0 = 0.1$ fm $\sim 1/p_T$
- binary collision transverse profile for Au+Au at $b = 8$ fm
- $d\sigma/dt \propto 1/(t-\mu_D^2)^2$, $\sigma_{gg} = 9\pi\alpha_s^2/2\mu_D^2$, with $\mu_D = 0.7$ GeV

AMPT: v2.26t5d6

- almost massless u, d & massive s quarks
- enhanced $dN_q/d\eta \approx 2.5 \times dN_h/d\eta$ (string melting), nonuniform in η
- formation time distribution
- transverse profile close to wounded nucleons
- sizeable event-by-event fluctuations
- $\mu_D = 0.45$ GeV, $\alpha_s = 0.33 \ \Rightarrow\ \sigma = 3$ mb (quark Casimirs ignored)

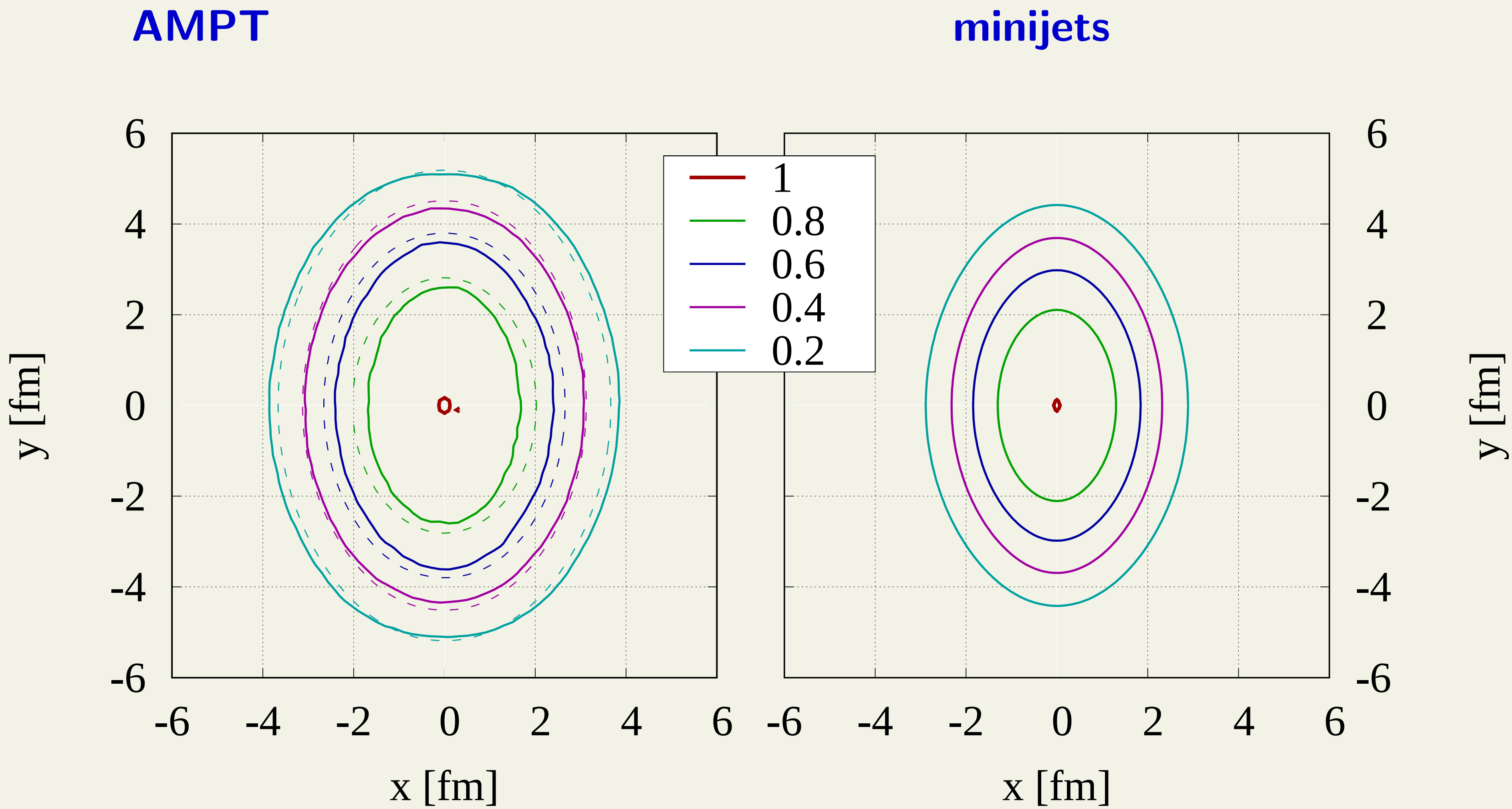
Au+Au, b=8 fm - AMPT pseudorapidity $dN/d\eta_p$



$$\eta_p \equiv \frac{1}{2} \ln \frac{|p| + p_z}{|p| - p_z}$$

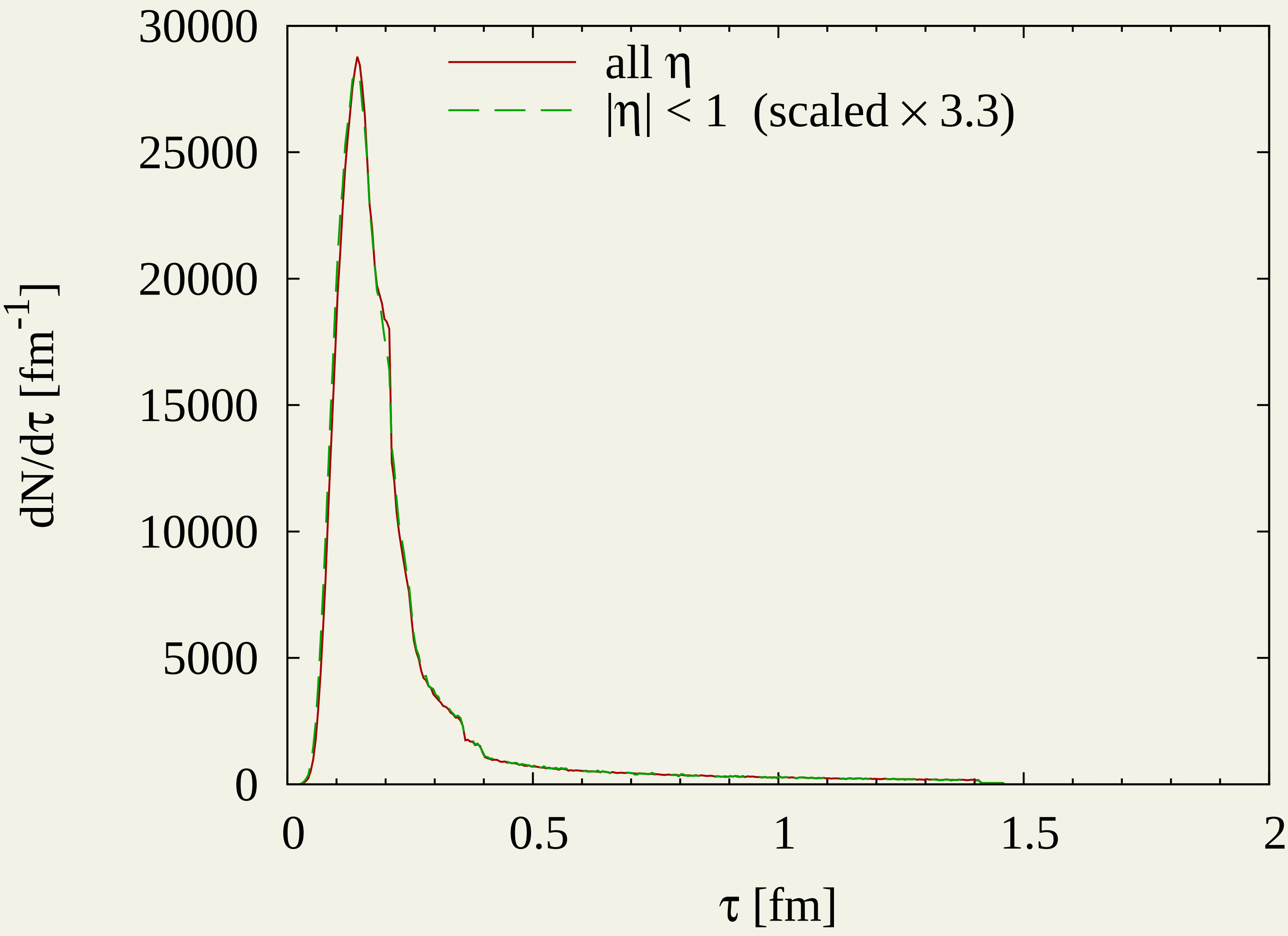
evidently not boost invariant, peak around $dN/d\eta_p \sim 650$

Au+Au, b=8 fm - transverse profile dN/d^2x_T for $|\eta_p| < 1$



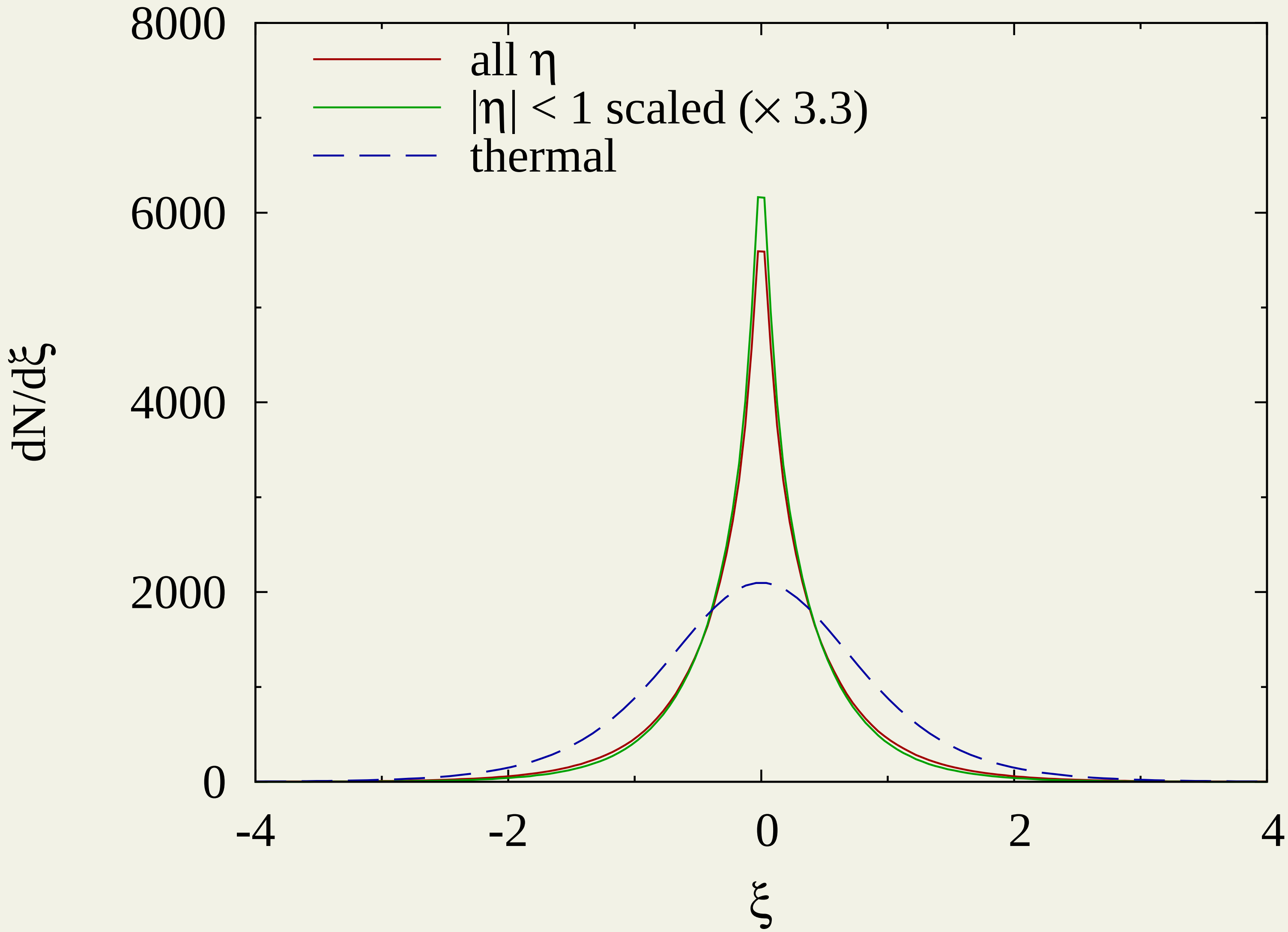
AMPT: close to wounded nucleons (dashed); minijets: binary coll profile

Au+Au, b=8 fm - AMPT formation time $\tau = \sqrt{t^2 - z^2}$



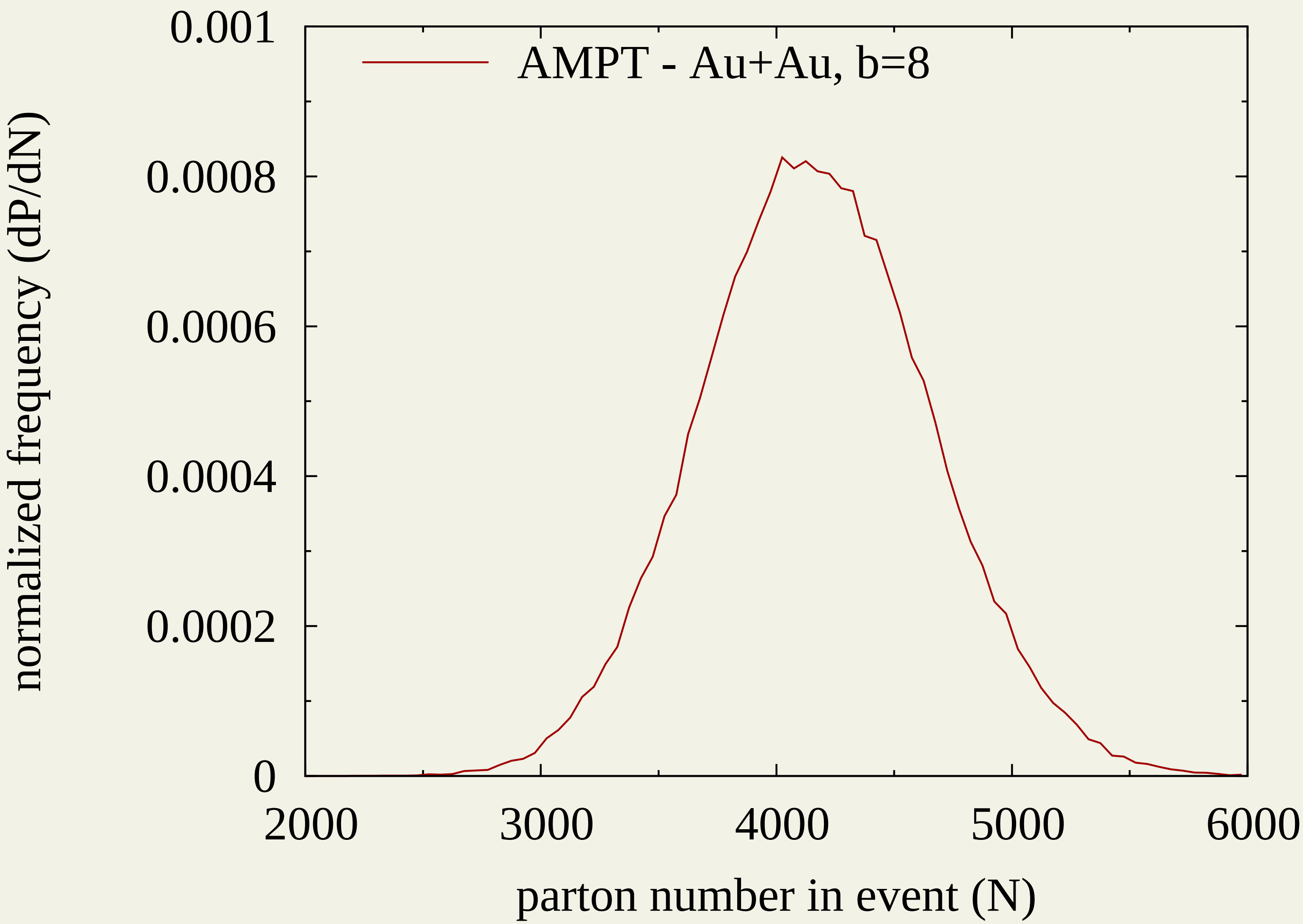
broad distribution, peaks around $\boldsymbol{\tau \sim 0.2}$ fm (average $\tau \approx 0.23$ fm)

Au+Au, b=8fm - AMPT coord rapidity - pseudorapity correlation $\xi \equiv \eta - \eta_p$



much sharper than boost-invariant thermal $\propto 1/\cosh^2 \xi$ correlation

Au+Au, b=8fm - AMPT total quark number in event



large event-by-event fluctuations, $\langle N_{quark} \rangle \approx 4200$

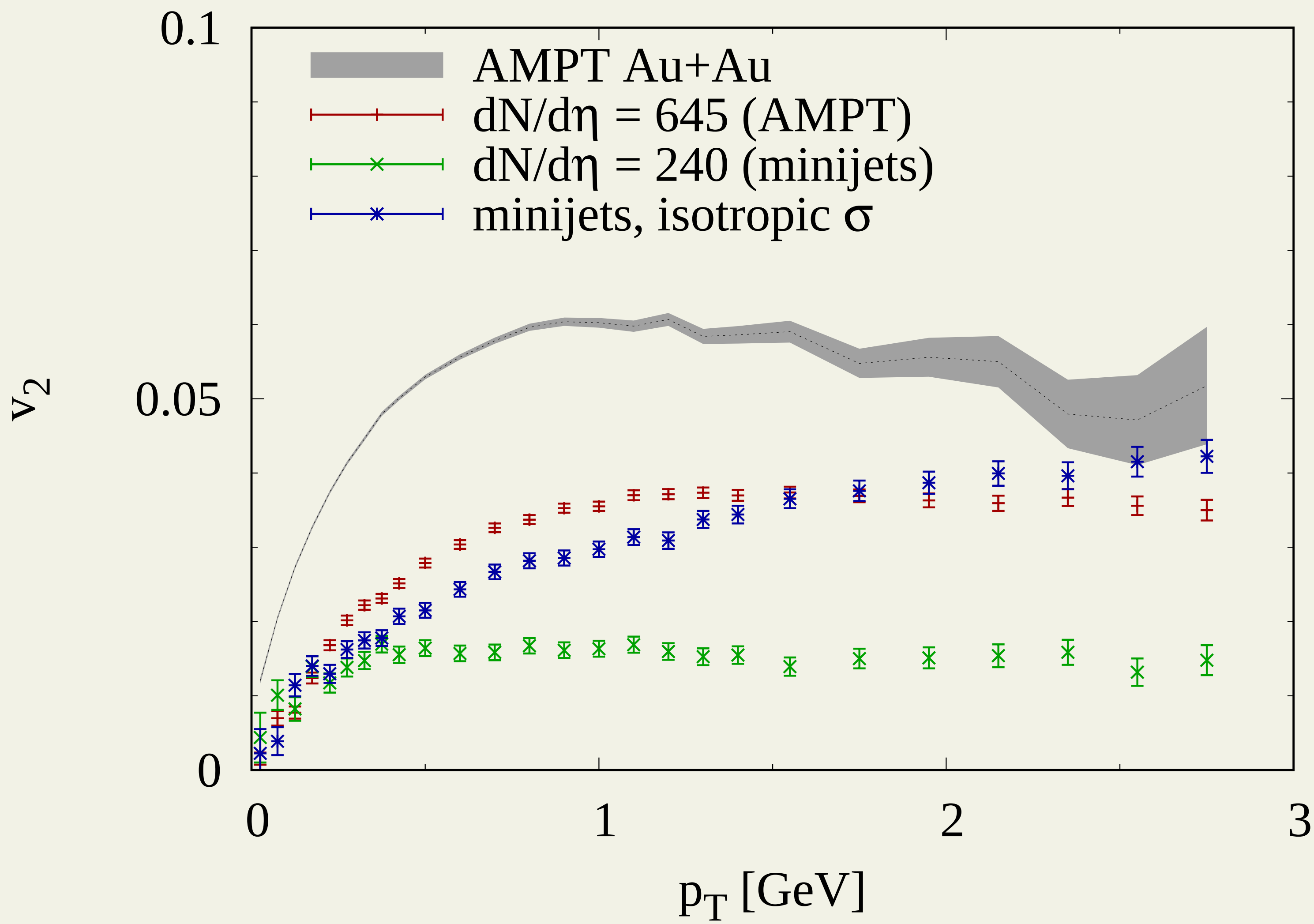
MPC v1.9 comparison strategy: go from simple to complicated

- **take boost-invariant minijet study as baseline**

- **gradually include features of AMPT initconds**

- **use wounded nucleon profile, and the same $d\sigma/dt$ as AMPT**

1) set $dN/\eta_p \approx 650$ to match AMPT (at midrapidity), use AMPT $d\sigma/dt$

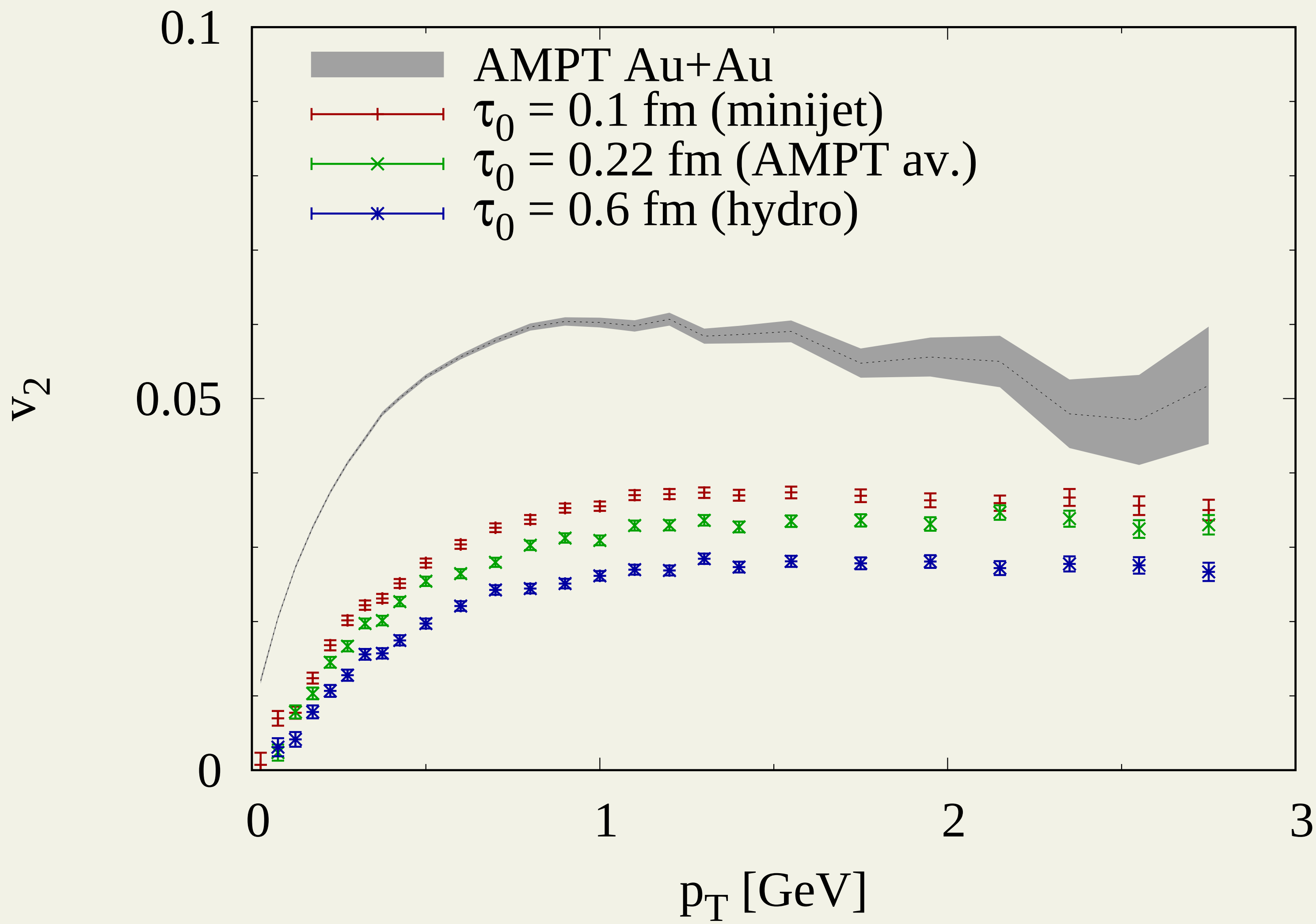


$\tau_0 = 0.1$ fm

$T_0 = 0.7$ GeV

$2.7\times$ larger density, but only gets v_2 to $\approx 3.5\%$... (need $5\times$ more opacity)

2) match formation time to AMPT average, $\langle \tau_0 \rangle = 0.22$ fm

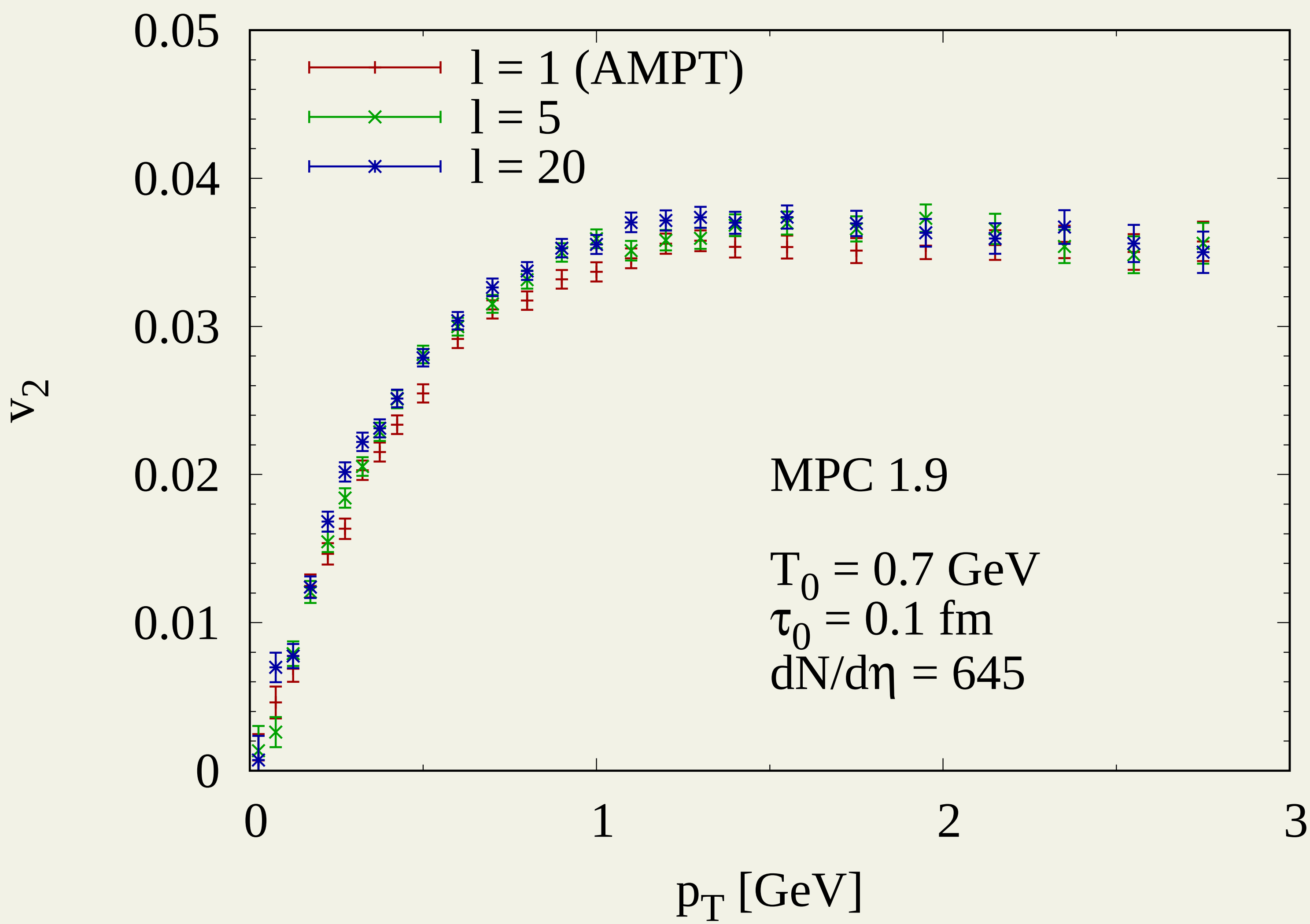


$dN/d\eta = 645$

$T_0 = 0.7$ GeV

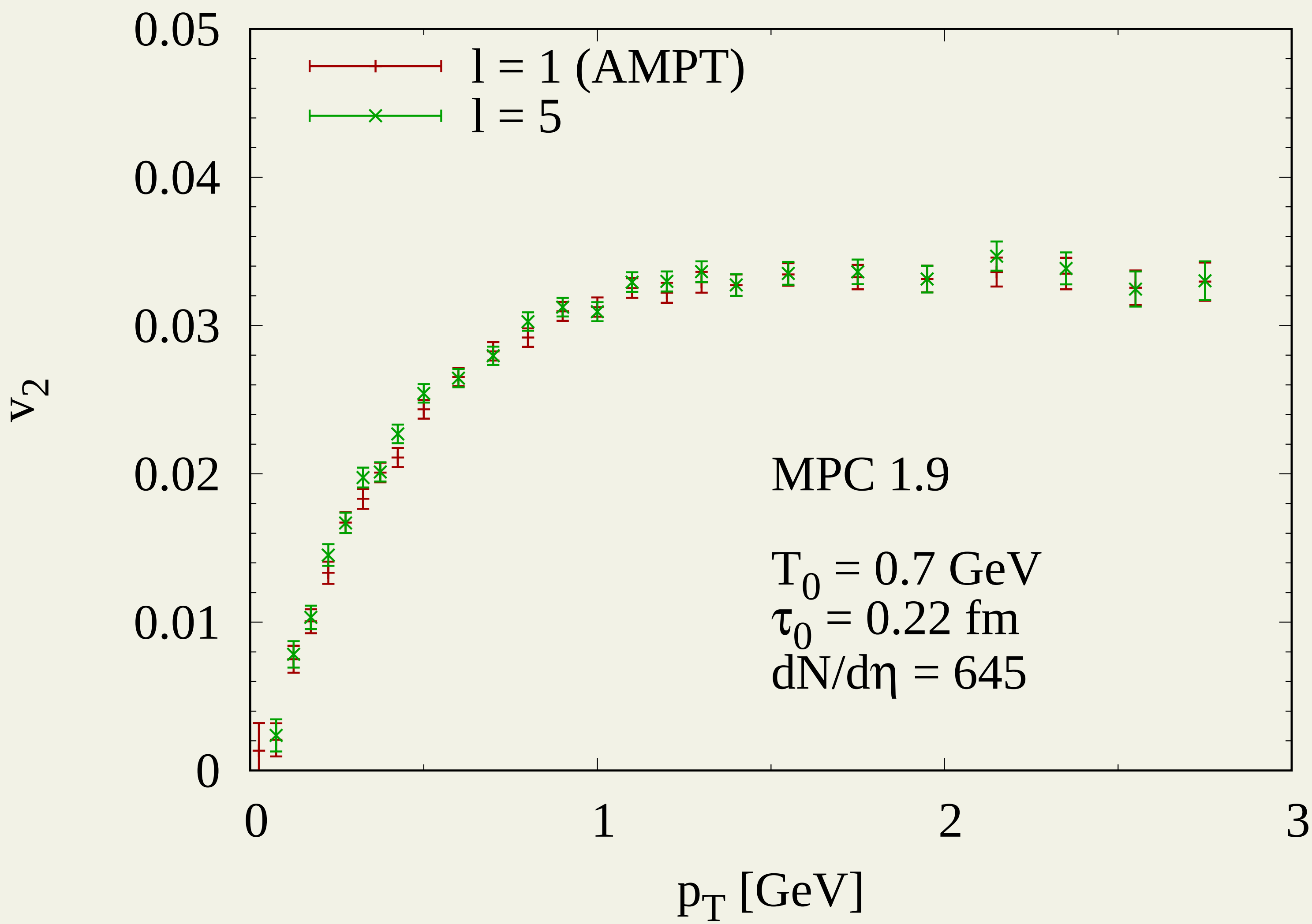
larger $\tau_0 \Rightarrow$ smaller v_2 (lower density $n \sim 1/\tau$, also shorter evolution)

3) decrease parton subdivision, down to $\ell = 1$



modest $\lesssim 10$% effect on $v_2(p_T)$, for short $\tau_0 = 0.1$ fm

same, but now match $\langle \tau_0 \rangle$ from AMPT



less than 5% distortion in $v_2(p_T)$, removable with subdivision $\ell = 5$

So far we...

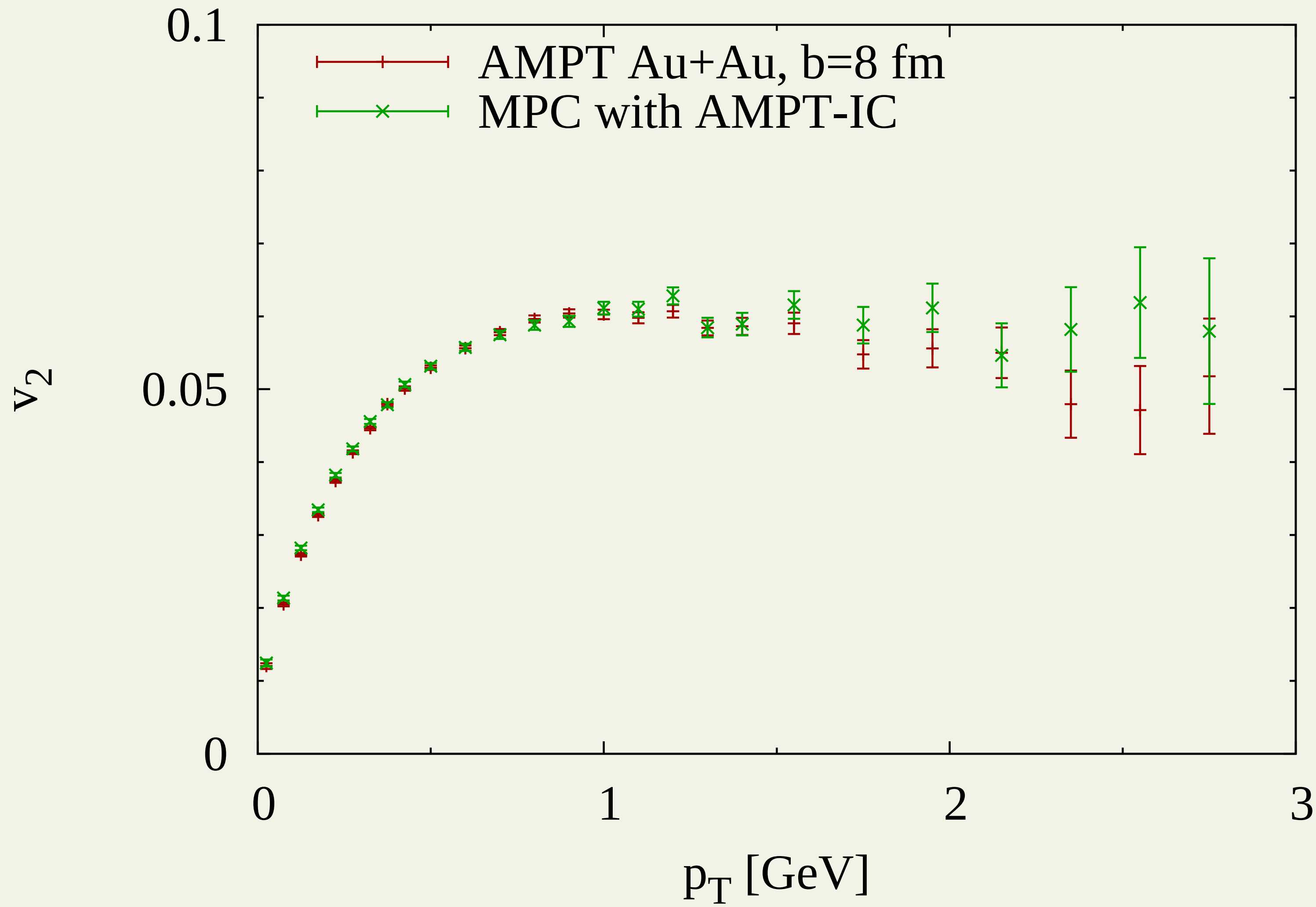
- **matched initial $dN/d\eta$, formation time, transverse profile, interactions**
- **ruled out too low parton subdivision**

  (effectively, AMPT runs at subdivision ~ 10 relative to $\sigma \sim 30$ mb, and another factor of ~ 5 would be sufficient)

still, v_2 is too small.

what if we use the exact same initial conditions?

4) MPC with full AMPT initial conditions (same $\vec{p}$, $\vec{x}$, t for each parton)



MPC with $\sigma = 3$ mb ($\ell = 1$) reproduces the elliptic flow from AMPT!

Missing link: momentum distribution

- for thermal minijets, $\langle p_T \rangle = 3\pi T/4 \approx 1.6$ **GeV for** $T_0 = 0.7$ **GeV**

$$\frac{dN}{d^2p_T dy} = E\frac{dN}{d^3p} = p_\mu d\sigma^\mu f \propto m_T\tau\ \cosh\xi\, e^{-m_T\cosh\xi/T}$$

- for AMPT quarks, $\langle p_T \rangle \approx 0.54$ **GeV** $\Rightarrow$ $T_{eff} = 0.23$ **GeV only**

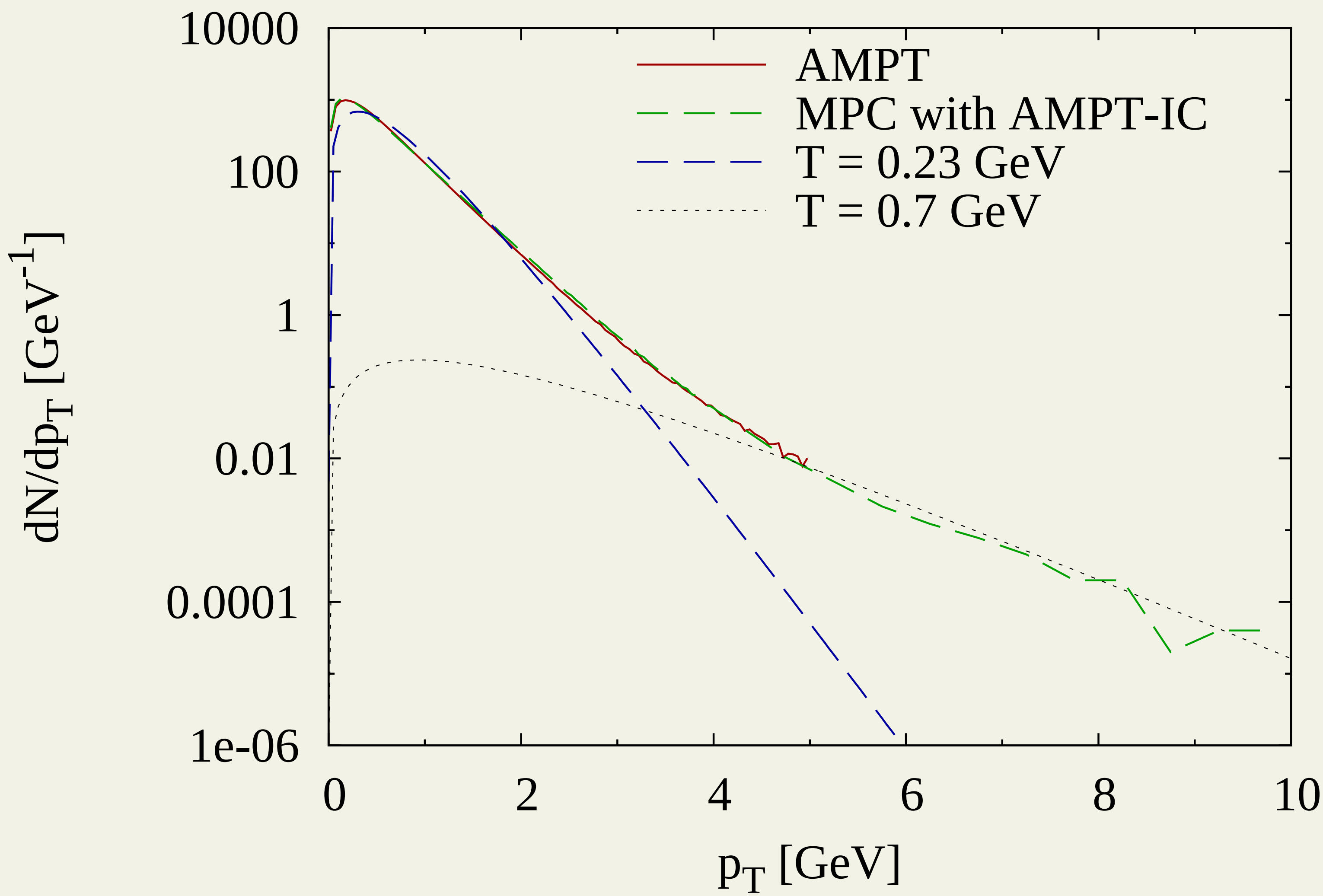
at lower temperature, the cross section is more isotropic (with μ_D fixed)

$\Rightarrow$ **more effective v_2 generation**

$$\sigma_{tr} = 4\sigma_{TOT}\, z(1+z)\left[(2z+1)\ln\left(1+\frac{1}{z}\right) - 2\right] , \qquad z \equiv \frac{\mu^2}{s} \approx \frac{\mu^2}{18T^2}$$

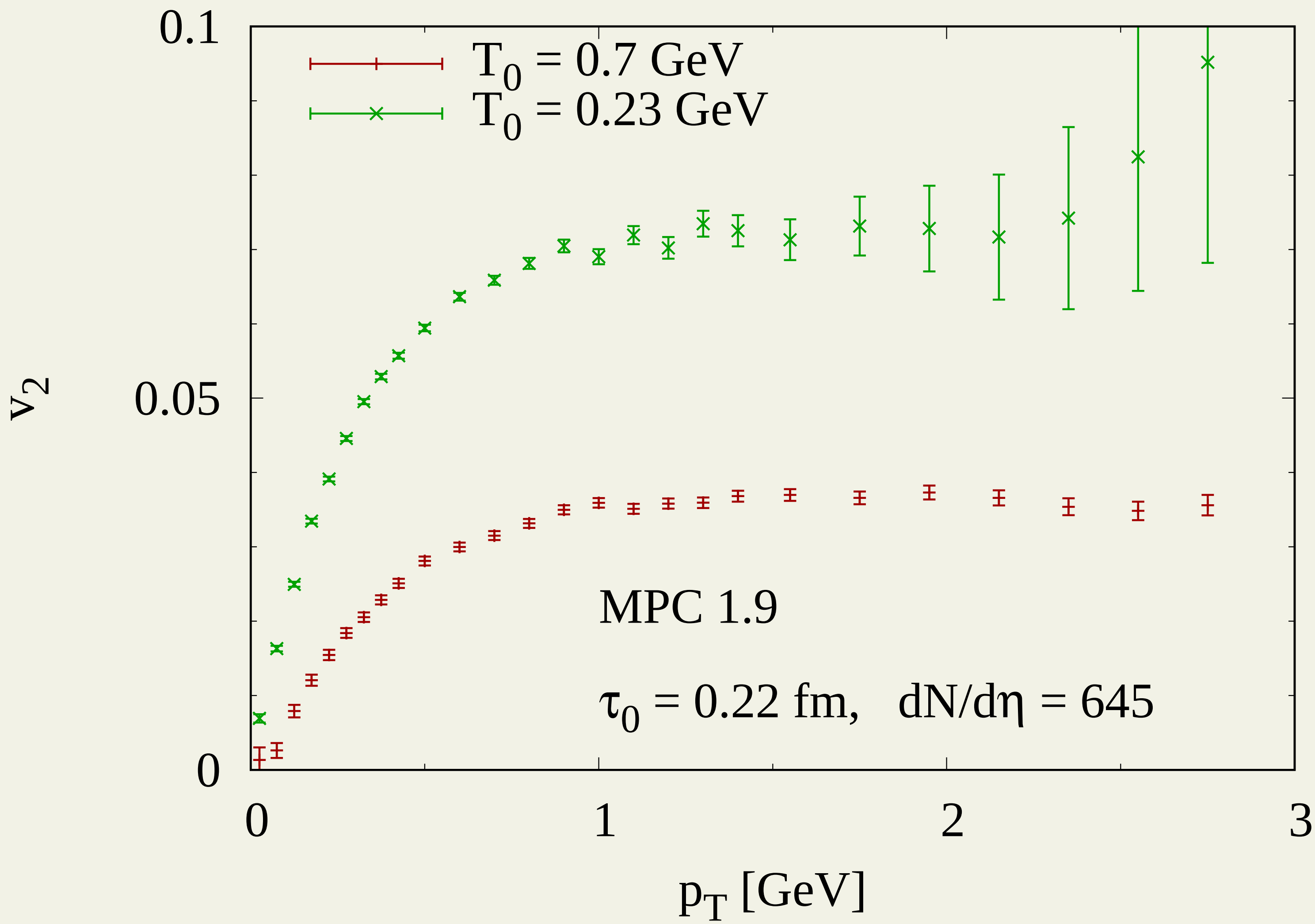
so $\dfrac{\sigma_{tr}(T = 0.23\,\mathrm{GeV})}{\sigma_{tr}(T = 0.7\,\mathrm{GeV})} \approx 2.6$ **(!)**

initial parton spectrum in Au+Au at RHIC, b=8 fm ($|\eta_p| < 1$)



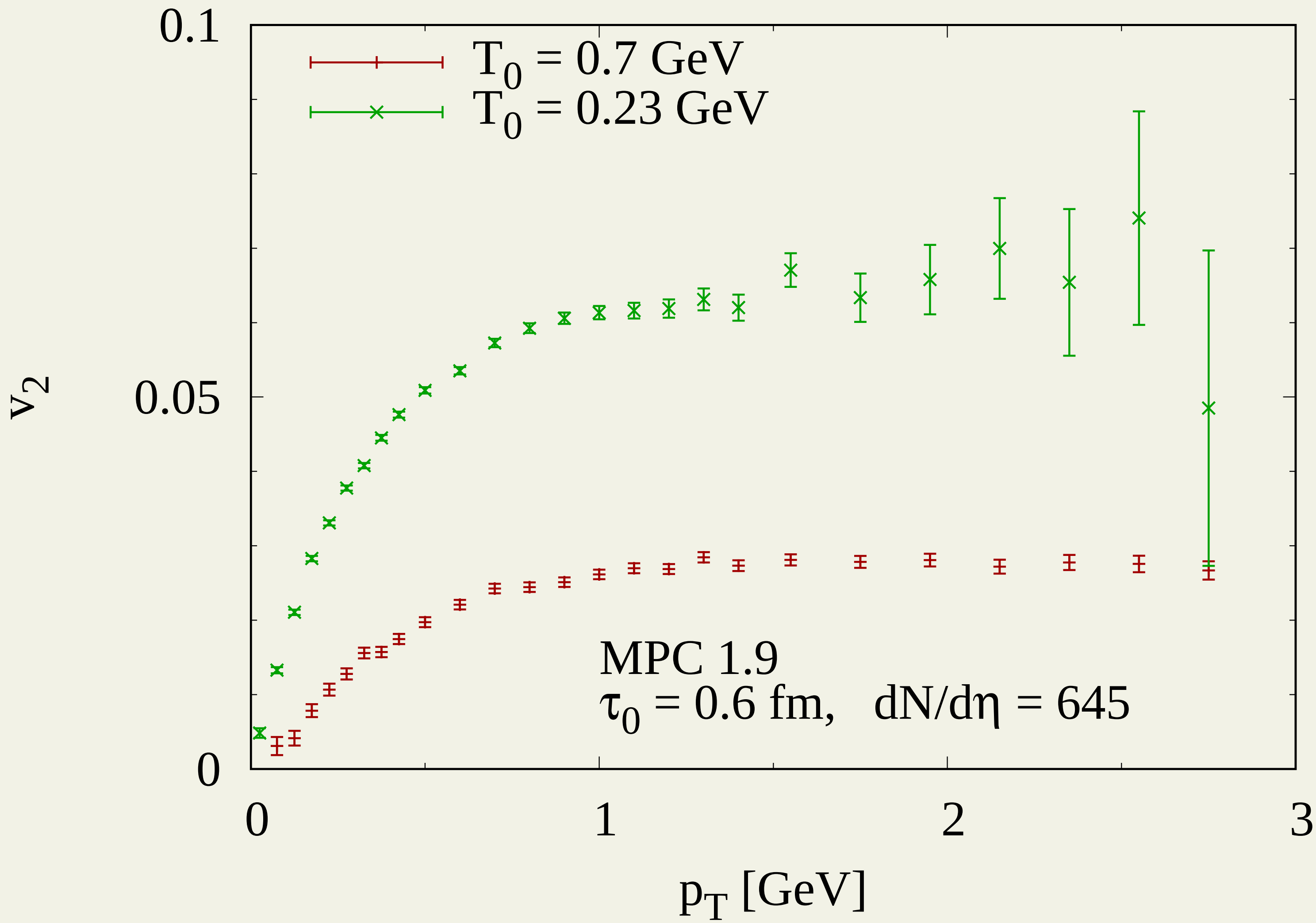
$T = 0.7$ **GeV captures minijet tail, but string melting plasma is** $3\times$ **colder**

4) now set T_{eff} to AMPT $\langle p_T \rangle$



large $6-7\%$ v_2, even slightly higher than from AMPT

same comparison but for higher $\tau_0 = 0.6$ fm



even $2.5\times$ later formation time works, v_2 practically doubles

Summary

Using the covariant transport solver MPC (Molnar's Parton Cascade), we investigated how AMPT generates enough elliptic flow (v_2) in Au+Au at RHIC with only 3-mb cross sections. Two ingredients play the most important role: i) about $2.5\times$ higher parton densities via string melting, and ii) cold initial plasma with effective temperature $T_{eff} \sim 0.2 - 0.25$ GeV, comparable to μ_D (makes forward-peaked partonic cross sections more isotropic).

The partonic stage of AMPT approximates well solutions of the covariant Boltzmann transport equation. Artifacts due to lack of parton subdivision were below 5% for $v_2(p_T)$ in Au+Au at RHIC. Compared to studies that generated high opacities with large $\sigma \sim 30$ mb, AMPT effectively incorporates a subdivision $\ell \sim 10$ already.

With 3 mb cross section, AMPT still generates $2 - 3\times$ smaller partonic v_2 than that of hadrons. But it makes up for the difference with quark coalescence - the algorithm of which needs to be tested in detail.

Next steps:

- include fluctuations in τ_0, N_{quark}, initial profile
- check v_2 distribution, not just its event average