

# **Theoretical Review on Pentaquarks**

**Bing-Song Zou**

**Institute of Theoretical Physics, CAS, Beijing**

**University of Chinese Academy of Sciences, Beijing, China**

## **Outline :**

- 1. Pentaquarks before LHCb  $P_c$  states**
- 2. LHCb pentaquarks vs predictions**
- 3. Progress on  $P_c$  states after LHCb observation**
- 4. Strange & beauty partners of  $P_c$  states**
- 5. Prospects**

# 1. Pentaquarks before LHCb $P_c$ states

## **Fate of the first pentaquark predicted and observed:**

1959:  $\bar{K}N$  molecule predicted by Dalitz-Tuan, PRL2, 425

1961:  $\Lambda(1405) \rightarrow \Sigma\pi$  observed by Alston et al., PRL6, 698

1964: Quark model (uds) for  $\Lambda(1405)$

1995:  $\bar{K}N$  dynamically generated -- Kaiser et al., NPA954, 325

2001: 2 pole structure by  $\bar{K}N$ - $\Sigma\pi$  -- Oller et al., PLB500, 263

PDG2010: “The clean  $\Lambda_c$  spectrum has in fact been taken to settle the decades-long discussion about the nature of the  $\Lambda(1405)$  —true 3-quark state or mere  $\bar{K}N$  threshold effect— unambiguously in favor of the first interpretation.”

## **Fate of the last famous fake pentaquark $\theta^+(1540)$ :**

1997:  $Z^+(1530)$  predicted by Diakonov et al., ZPA359, 305

2003:  $\theta^+(1540) \rightarrow K^+n$  claimed by LEPS, PRL91, 012002

2003:  $\bar{s}(ud)(ud)$  for  $\theta(1540)$  by Jaffe&Wilczek, PRL91, 232003

2003:  $\bar{s}ud(ud)$  for  $\theta(1540)$  by Karliner&Lipkin, PLB575, 249

2004: supported by 10 expts  $\rightarrow \theta(1540)$  well-established by PDG

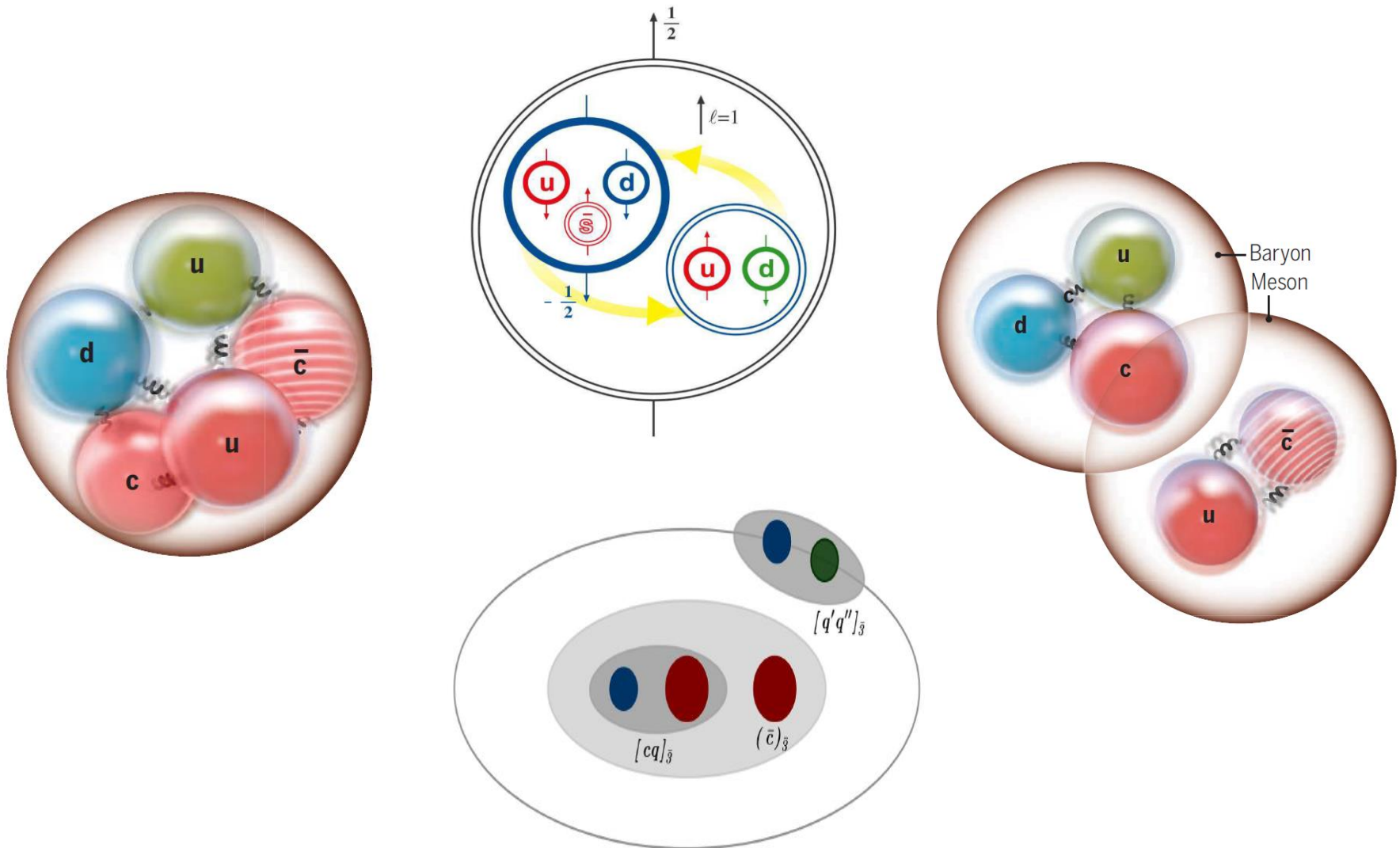
2004: not supported by BESII, PRD70, 012004

2005: not supported by many high stats experiments

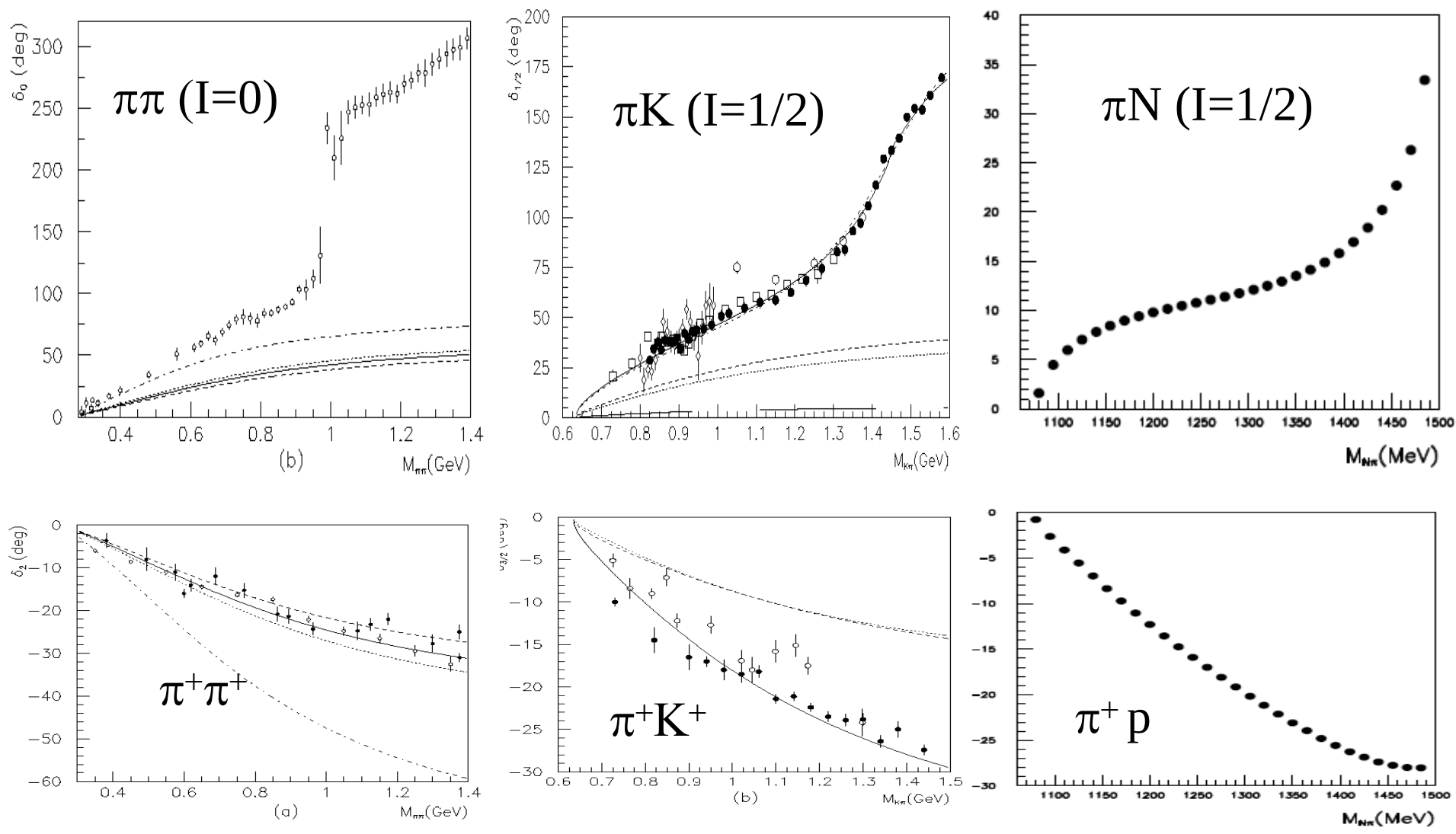
2006: removed from PDG

**Note:**  $\theta^+(1540)$  is not supported by hadronic molecule model & chiral quark model by Huang, Zhang, Yu, Zou, PLB586(2004)69

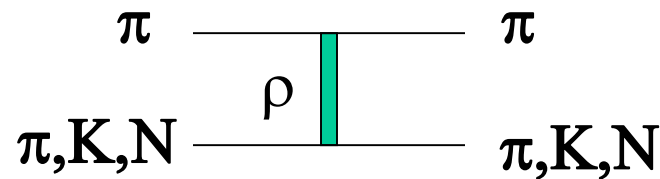
While lacking expt constraints on models of compact pentaquarks, models for hadronic molecules are much better constrained.



# Similarity for $\pi\pi$ , $\pi K$ and $\pi N$ s-wave scattering phase shifts



Important role by t-channel  $\rho$  exchange for all these processes



$\pi\pi$

$\pi K$  &  $\pi N$

$$K_{\rho}^{I=0} = -2 K_{\rho}^{I=2}, \quad K_{\rho}^{I=1/2} = -2 K_{\rho}^{I=3/2}$$

D. Lohse, J.W. Durso, K. Holinde, J. Speth, Nucl.Phys.A516, 513 (1990)

B.S.Zou, D.V.Bugg, Phys. Rev. D50, 591 (1994)

An interesting paper by T.Hyodo, D.Jido, A.Hosaka, PRL 97 (2006) 192002  
 “Exotic hadrons in s-wave chiral dynamics”

|               |                       |                      |                     |                      |
|---------------|-----------------------|----------------------|---------------------|----------------------|
|               | $\bar{K}N(I=0)$       | $\bar{K}N(I=1)$      | $KN(I=0)$           | $KN(I=1)$            |
| Phase shifts: | strong +              | weaker +             | weaker -            | strong -             |
| VMD :         | $-V_\omega - 3V_\rho$ | $-V_\omega + V_\rho$ | $V_\omega - V_\rho$ | $V_\omega + 3V_\rho$ |

Similarity between  $\pi\Sigma - \bar{K}N(I=0)$  and  $\pi\pi - \bar{K}K(I=0)$

dipole structure for  $\Lambda(1405) \leftarrow \sigma - f_0(980)$

VMD – ChPT unitarized  $\rightarrow N^*(1535)$  as  $K\Sigma$  bound state

**Kaiser et al., PLB362(1995)23**

Many hadrons are proposed to be hadronic molecules

**Problem:**

None of them can be clearly distinguished from  $qqq$  or  $\bar{q}q$  due to tunable ingredients and possible large mixing of various configurations

**Solution:** Extension to hidden charm and beauty for baryons

$N^*(1535)$   $\bar{s}suud$

$N^*(4260)$   $\bar{c}cuud$  J.J.Wu, R.Molina, E.Oset, B.S.Zou.  
Phys.Rev.Lett. 105 (2010) 232001

$N^*(11050)$   $\bar{b}buud$  J.J.Wu, L.Zhao, B.S.Zou. PLB709(2012)70

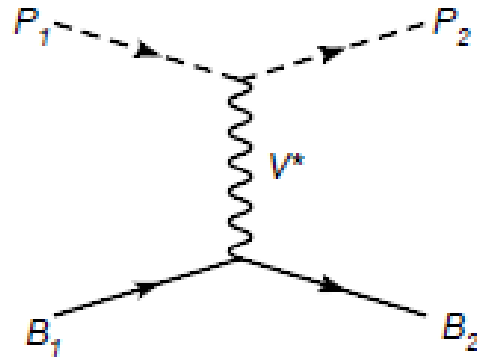
$\Lambda^*(1405)$   $\bar{q}quds$

$\Lambda^*(4210)$   $\bar{c}cuds$  J.J.Wu, R.Molina, E.Oset, B.S.Zou.  
Phys.Rev.Lett. 105 (2010) 232001

$\Lambda^*(11020)$   $\bar{b}buds$  J.J.Wu, L.Zhao, B.S.Zou. PLB709(2012)70

From  $K\Sigma$ ,  $\bar{K}N \rightarrow \bar{D}\Sigma_c$ ,  $\bar{D}_s\Lambda_c \rightarrow B\Sigma_b$ ,  $B_s\Lambda_b$  bound states

“Prediction of narrow  $N^*$  and  $\Lambda^*$  resonances with hidden charm above 4 GeV”,  
Wu, Molina, Oset, Zou, PRL105 (2010) 232001



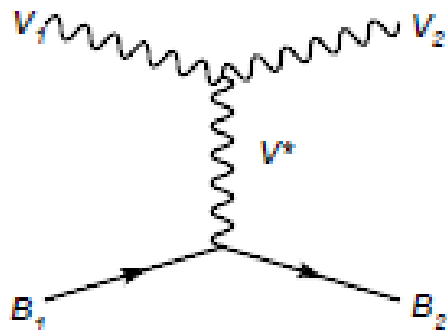
$$\mathcal{L}_{VVV} = ig\langle V^\mu [V^\nu, \partial_\mu V_\nu] \rangle$$

$$\mathcal{L}_{PPV} = -ig\langle V^\mu [P, \partial_\mu P] \rangle$$

$$\mathcal{L}_{BBV} = g(\langle \bar{B}\gamma_\mu [V^\mu, B] \rangle + \langle \bar{B}\gamma_\mu B \rangle \langle V^\mu \rangle)$$

$$V_{ab}(P_1 B_1 \rightarrow P_2 B_2) = \frac{C_{ab}}{4f^2}(E_{P_1} + E_{P_2}),$$

$$V_{ab}(V_1 B_1 \rightarrow V_2 B_2) = \frac{C_{ab}}{4f^2}(E_{V_1} + E_{V_2})\vec{\epsilon}_1 \cdot \vec{\epsilon}_2,$$



$$T = [1 - VG]^{-1}V$$

$$T_{ab} = \frac{g_a g_b}{\sqrt{s} - z_R}$$

|                         |            | $(I, S)$ | $M$  | $\Gamma$ | $\Gamma_i$ |             |               |                |            | $J^P$           |
|-------------------------|------------|----------|------|----------|------------|-------------|---------------|----------------|------------|-----------------|
| $N^* - \bar{D}\Sigma_c$ | $(1/2, 0)$ |          |      |          | $\pi N$    | $\eta N$    | $\eta' N$     | $K\Sigma$      | $\eta_c N$ | $1/2^-$         |
|                         |            | 4261     | 56.9 |          | 3.8        | 8.1         | 3.9           | 17.0           | 23.4       |                 |
| $\Lambda^*$             | $(0, -1)$  |          |      |          | $\bar{K}N$ | $\pi\Sigma$ | $\eta\Lambda$ | $\eta'\Lambda$ | $K\Xi$     | $\eta_c\Lambda$ |
|                         |            | 4209     | 32.4 |          | 15.8       | 2.9         | 3.2           | 1.7            | 2.4        | 5.8             |
|                         |            | 4394     | 43.3 |          | 0          | 10.6        | 7.1           | 3.3            | 5.8        | 16.3            |

TABLE V: Mass ( $M$ ), total width ( $\Gamma$ ), and the partial decay width ( $\Gamma_i$ ) for the states from  $PB \rightarrow PB$ , with units in MeV.

| $N^* - \bar{D}^*\Sigma_c$<br><br>$\Lambda^*$ | $(I, S)$   | $M$  | $\Gamma$ | $\Gamma_i$ |              |                 |               |          | $J/\psi N$<br><br>$1/2^-, 3/2^-$ |                 |
|----------------------------------------------|------------|------|----------|------------|--------------|-----------------|---------------|----------|----------------------------------|-----------------|
|                                              | $(1/2, 0)$ |      |          | $\rho N$   | $\omega N$   | $K^*\Sigma$     |               |          |                                  |                 |
|                                              |            | 4412 | 47.3     | 3.2        | 10.4         | 13.7            | 19.2          |          |                                  |                 |
|                                              | $(0, -1)$  |      |          | $K^*N$     | $\rho\Sigma$ | $\omega\Lambda$ | $\phi\Lambda$ | $K^*\Xi$ |                                  | $J/\psi\Lambda$ |
|                                              |            | 4368 | 28.0     | 13.9       | 3.1          | 0.3             | 4.0           | 1.8      | 5.4                              |                 |
|                                              |            | 4544 | 36.6     | 0          | 8.8          | 9.1             | 0             | 5.0      | 13.8                             |                 |

TABLE VI: Mass ( $M$ ), total width ( $\Gamma$ ), and the partial decay width ( $\Gamma_i$ ) for the states from  $VB \rightarrow VB$  with units in MeV.

# Further studies support such hidden charm $N^*$

W.L.Wang, F.Huang, Z.Y.Zhang, B.S.Zou, PRC84(2011)015203:

**Chiral quark model  $\rightarrow \bar{D}\Sigma_c$  state  $\sim 4.3$  GeV**

J.J.Wu, T.S.H.Lee, B.S.Zou, PRC85(2012)044002:

**EBAC-DCC model  $\rightarrow \bar{D}\Sigma_c(1/2^-) \sim 4.3$  GeV,  
 $\bar{D}^*\Sigma_c(1/2^-, 3/2^-) \sim 4.4 - 4.5$  GeV -**

C.W.Xiao, J.Nieves, E.Oset, PRD 88 (2013) 056012:

**Heavy quark spin symmetry  $\rightarrow 7$  such  $N^*$  molecules**  
 $\bar{D}\Sigma_c(1/2^-) \sim 4.26$  GeV,  $\bar{D}\Sigma_c^*(3/2^-) \sim 4.33$  GeV,  
 $\bar{D}^*\Sigma_c(1/2^-, 3/2^-) \sim 4.41, 4.42$  GeV,  
 $\bar{D}^*\Sigma_c^*(1/2^-, 3/2^-, 5/2^-) \sim 4.48 - 4.49$  GeV

M.Karliner, J.L.Rosner, PRL115(2015)122001:

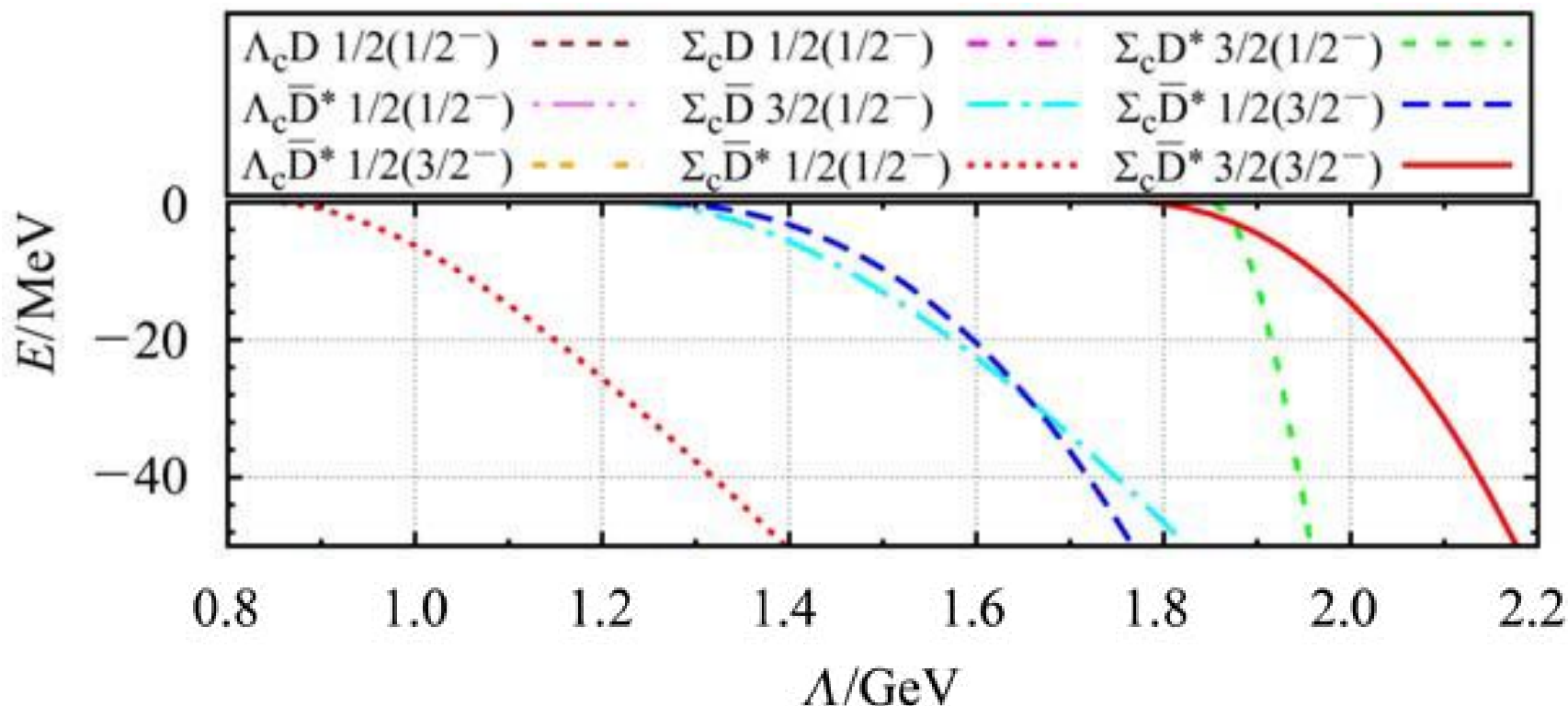
**Pion exchange  $\rightarrow \bar{D}^*\Sigma_c(1/2^-, 3/2^-) \sim 4.5$  GeV**

Z.C.Yang, Z.F.Sun, J.He, X.Liu, S.L.Zhu, Chin. Phys. C36 (2012) 6

Schoedinger Equation method with  $\pi$ ,  $\eta$ ,  $\rho$ ,  $\omega$ ,  $\sigma$  exchanges:

$\bar{D}^*\Sigma_c$  (**1/2<sup>-</sup>,3/2<sup>-</sup>**)  $N^*$  state -- 4360 ~ 4460 MeV

$\bar{D}\Sigma_c$  (**I=3/2**)  $N^*$  state -- ~ 4300 MeV



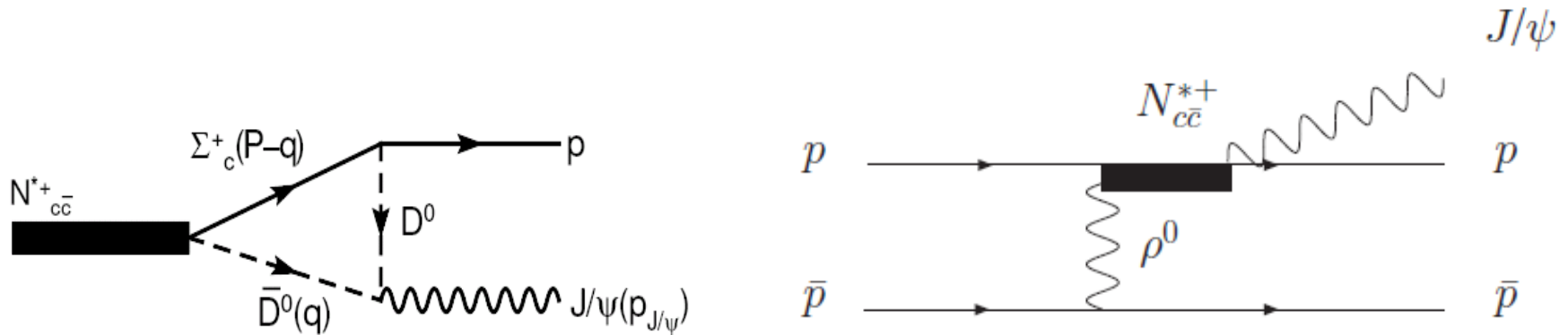
**S.G.Yuan, K.W.Wei, J.He, H.S.Xu, B.S.Zou, “Study of  $\bar{c}cqqq$  five quark system with three kinds of quark-quark hyperfine interaction,”  
Eur. Phys. J. A48 (2012) 61**

|                 | <i>CM</i>     |               | <i>FS</i>     |               | <i>Inst.</i>  |               |
|-----------------|---------------|---------------|---------------|---------------|---------------|---------------|
| $J^P$           | $udsc\bar{c}$ | $uudc\bar{c}$ | $udsc\bar{c}$ | $uudc\bar{c}$ | $udsc\bar{c}$ | $uudc\bar{c}$ |
| $\frac{1}{2}^-$ | 4273          | 4267          | 4084          | 3933          | 4209          | 4114          |
| $\frac{1}{2}^-$ | 4377          | 4363          | 4154          | 4013          | 4216          | 4131          |
| $\frac{1}{2}^-$ | 4453          | 4377          | 4160          | 4119          | 4277          | 4204          |
| $\frac{1}{2}^-$ | 4469          | 4471          | 4171          | 4136          | 4295          | 4207          |
| $\frac{1}{2}^-$ | 4494          | 4541          | 4253          | 4156          | 4360          | 4272          |
| $\frac{1}{2}^-$ | 4576          |               | 4263          |               | 4362          |               |
| $\frac{1}{2}^-$ | 4649          |               | 4278          |               | 4416          |               |
| $\frac{3}{2}^-$ | 4431          | <u>4389</u>   | 4154          | 4013          | 4216          | 4131          |
| $\frac{3}{2}^-$ | 4503          | <u>4445</u>   | 4171          | 4119          | 4295          | 4204          |
| $\frac{3}{2}^-$ | 4549          | 4476          | 4263          | 4136          | 4362          | 4272          |
| $\frac{3}{2}^-$ | 4577          | 4526          | 4278          | 4236          | 4416          | <u>4322</u>   |
| $\frac{3}{2}^-$ | 4629          |               | 4362          |               | 4461          |               |
| $\frac{5}{2}^-$ | 4719          | 4616          | 4362          | 4236          | 4461          | 4322          |

|                 | <i>CM</i>     |               | <i>FS</i>     |               | <i>Inst.</i>  |               |
|-----------------|---------------|---------------|---------------|---------------|---------------|---------------|
| $J^P$           | $udsc\bar{c}$ | $uudc\bar{c}$ | $udsc\bar{c}$ | $uudc\bar{c}$ | $udsc\bar{c}$ | $uudc\bar{c}$ |
| $\frac{1}{2}^+$ | 4622          | 4456          | 4291          | 4138          | 4487          | 4396          |
| $\frac{1}{2}^+$ | 4636          | 4480          | 4297          | 4140          | 4501          | 4426          |
| $\frac{1}{2}^+$ | 4645          | 4557          | 4363          | 4238          | 4520          | 4426          |
| $\frac{1}{2}^+$ | 4658          | 4581          | 4439          | 4320          | 4540          | 4470          |
| $\frac{1}{2}^+$ | 4690          | 4593          | 4439          | 4367          | 4557          | 4482          |
| $\frac{1}{2}^+$ | 4696          | 4632          | 4467          | 4377          | 4587          | 4490          |
| $\frac{1}{2}^+$ | 4714          | 4654          | 4469          | 4404          | 4590          | 4517          |
| $\frac{1}{2}^+$ | 4728          | 4676          | 4486          | 4489          | 4614          | 4518          |
| $\frac{1}{2}^+$ | 4737          | 4714          | 4492          | 4508          | 4616          | 4549          |
| $\frac{1}{2}^+$ | 4766          | 4720          | 4510          | 4515          | 4626          | 4566          |
| $\frac{3}{2}^+$ | 4623          | <u>4457</u>   | 4291          | 4138          | 4487          | 4396          |
| $\frac{3}{2}^+$ | 4638          | 4515          | 4297          | 4140          | 4501          | 4426          |
| $\frac{3}{2}^+$ | 4680          | 4561          | 4363          | 4238          | 4520          | 4426          |
| $\frac{3}{2}^+$ | 4692          | 4582          | 4439          | 4320          | 4540          | 4470          |
| $\frac{3}{2}^+$ | 4695          | 4625          | 4439          | 4367          | 4557          | 4482          |
| $\frac{5}{2}^+$ | 4705          | 4539          | 4297          | 4140          | 4501          | <u>4426</u>   |
| $\frac{5}{2}^+$ | 4719          | 4649          | 4439          | 4320          | 4540          | 4470          |
| $\frac{5}{2}^+$ | 4773          | 4689          | 4467          | 4367          | 4587          | 4482          |
| $\frac{5}{2}^+$ | 4793          | 4696          | 4486          | 4404          | 4615          | 4490          |
| $\frac{5}{2}^+$ | 4821          | 4710          | 4492          | 4515          | 4632          | 4517          |
| $\frac{7}{2}^+$ | 4945          | 4841          | 4638          | 4508          | 4698          | 4566          |
| $\frac{7}{2}^+$ | 4955          | 4862          | 4671          | 4551          | 4712          | 4634          |
| $\frac{7}{2}^+$ | 4974          | 4919          | 4705          | 4587          | 4765          | 4669          |
| $\frac{7}{2}^+$ | 5010          |               | 4759          |               | 4797          |               |

**M(5/2<sup>+</sup>) – M(3/2<sup>-</sup>) : 130 ~300 MeV**

# Prediction for PANDA



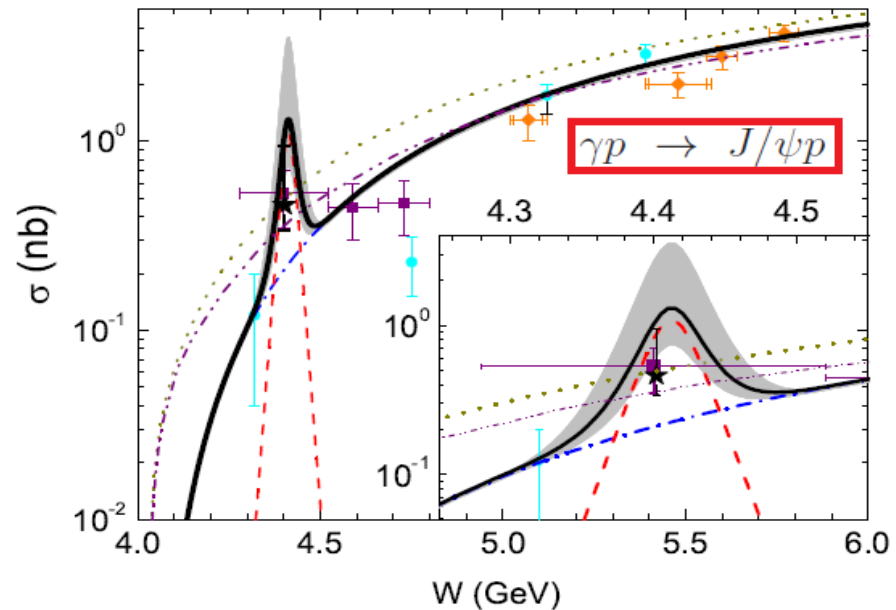
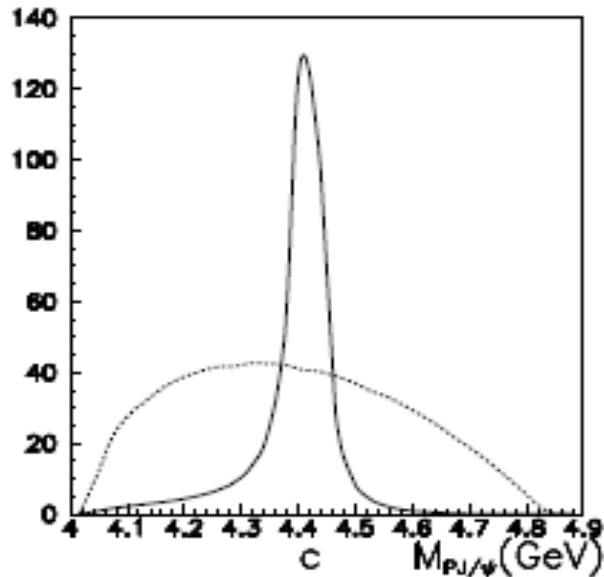
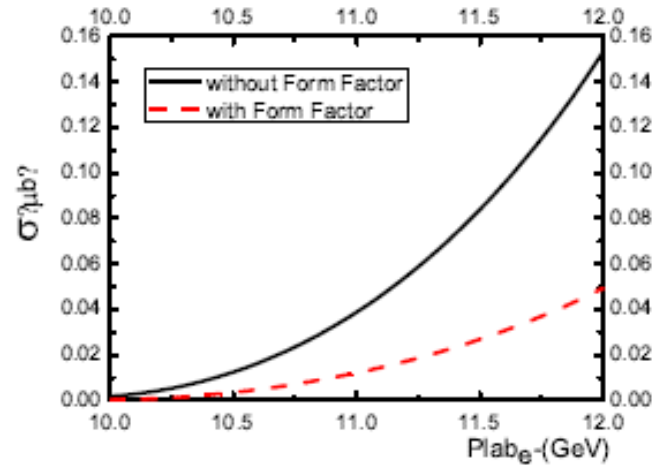
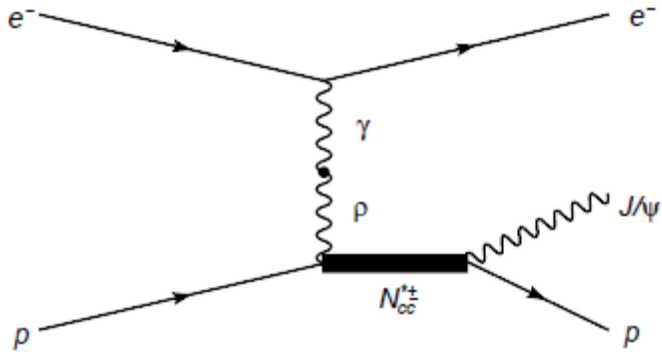
$$\bar{p}p \rightarrow \bar{p}pJ/\psi > 0.1 \text{ nb}$$

> 100 events per day at PANDA/FAIR by  $L=10^{31} \text{ cm}^{-2}\text{s}^{-1}$

**These Super-heavy narrow  $N^*$  and  $\Lambda^*$  can be found at PANDA !**

Albrecht Gillitzer@Juelich had a plan to find them at PANDA

# Prediction for 12GeV@JLab



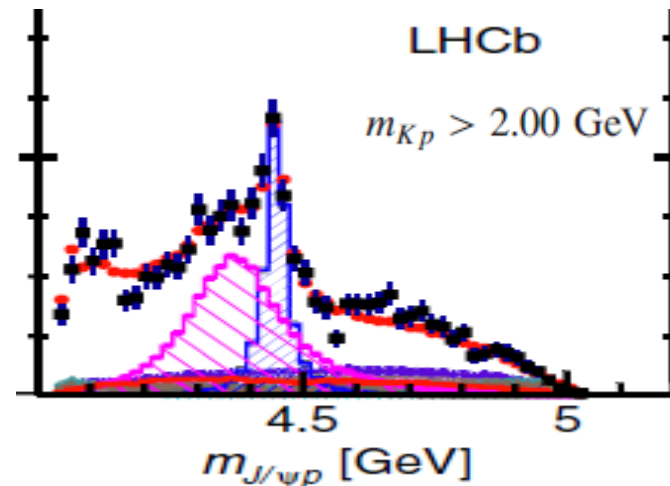
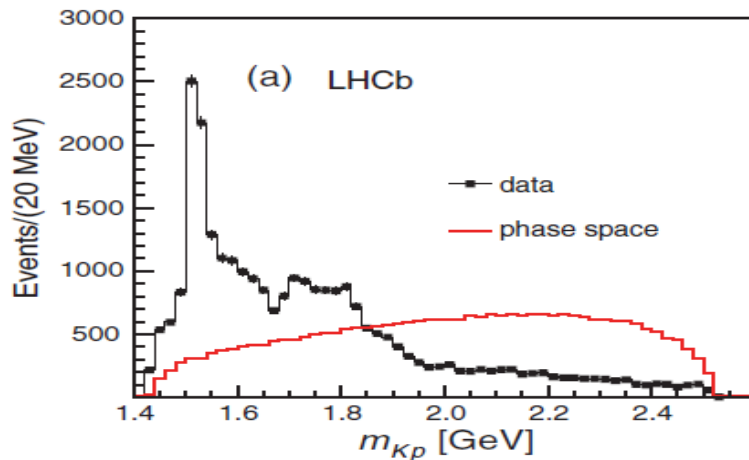
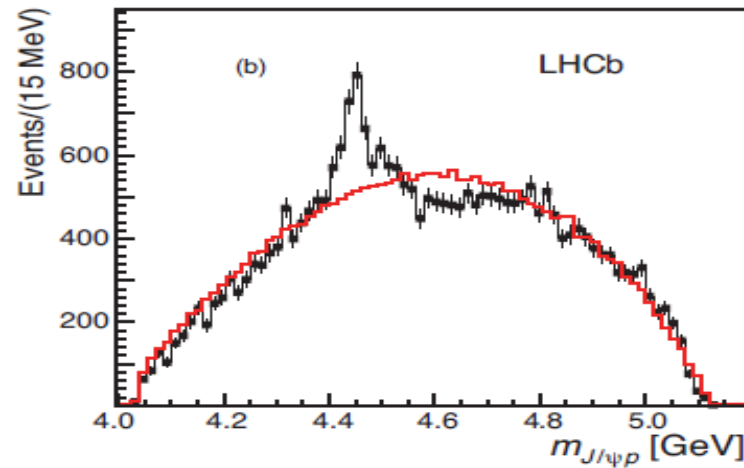
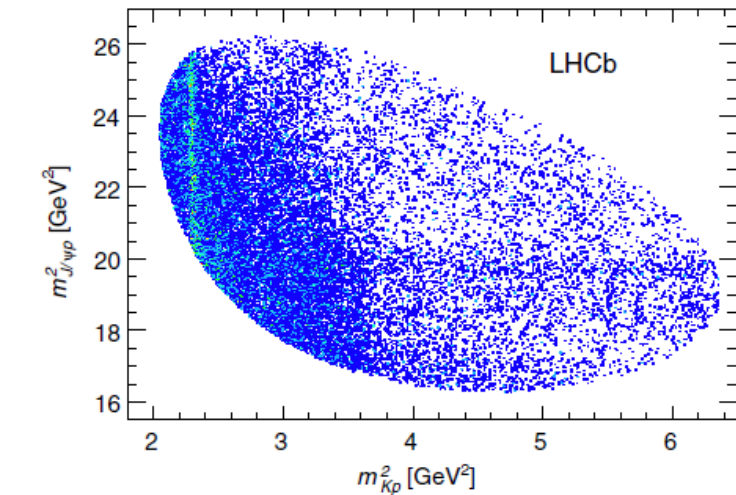
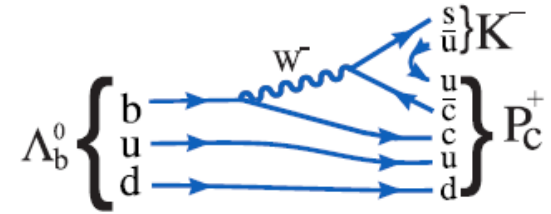
Y. Huang, J.He, H.F.Zhang and X.R.Chen, JPG41, 115004 (2014)

## Proposals for looking for $N_{cc}^-$ & $\Lambda_{cc}^-$ with $\pi^-$ , K beams at JPARC

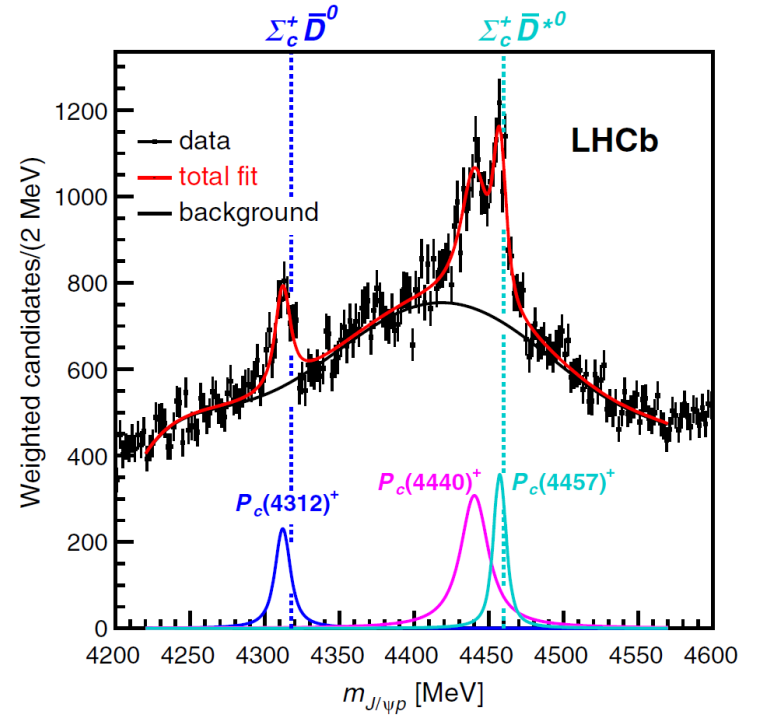
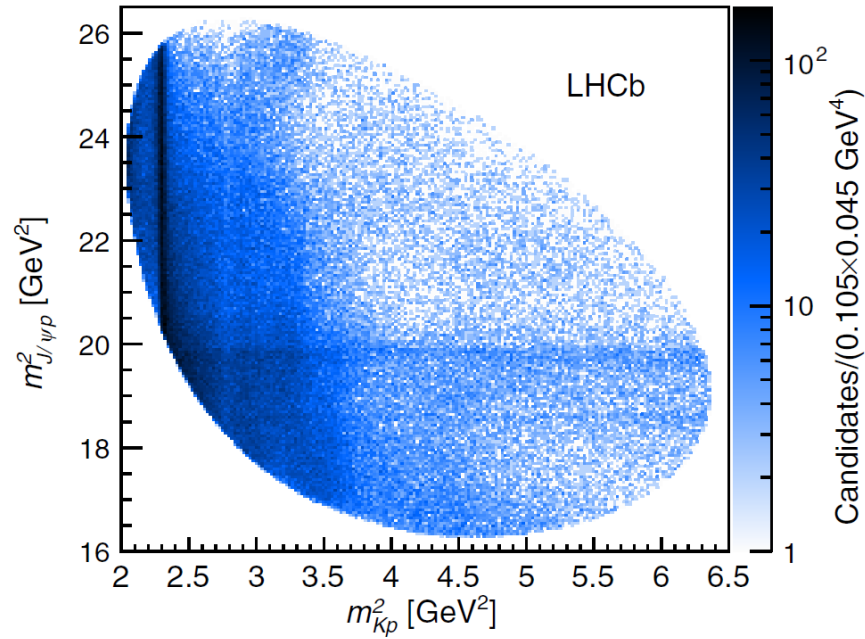
- a) **X.Y.Wang, X.R.Chen, “The production of hidden charm baryon  $N^*(4261)$  from  $\pi^-p \rightarrow \eta_c n$  reaction”, EPL109 (2015) 41001.**
- b) **E.J.Garzon, J.J.Xie, “Effects of a  $N_{cc}^-$  resonance with hidden charm in the  $\pi^-p \rightarrow D^- \Sigma_c^+$  reaction near threshold”, PRC 92 (2015) 035201**
- c) **X.Y.Wang, X.R.Chen, “Production of the superheavy baryon  $\Lambda^*(4209)$  in kaon-induced reaction”, EPJA51 (2015) 85**

## 2. LHCb pentaquarks vs predictions

LHCb, Phys.Rev.Lett. 115 (2015) 072001 :  
**Observation of two  $N^*$  from  $\Lambda_b^0 \rightarrow J/\psi K^- p$**



# LHCb, Phys.Rev.Lett. 122 (2019) 222001

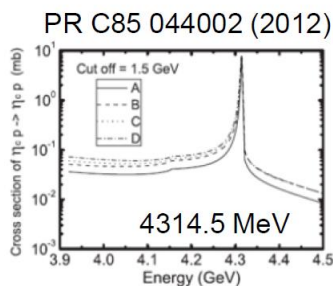


| State         | $M$ [MeV]                      | $\Gamma$ [MeV]                | (95% C.L.) | $\mathcal{R}$ [%]               |
|---------------|--------------------------------|-------------------------------|------------|---------------------------------|
| $P_c(4312)^+$ | $4311.9 \pm 0.7^{+6.8}_{-0.6}$ | $9.8 \pm 2.7^{+3.7}_{-4.5}$   | (<27)      | $0.30 \pm 0.07^{+0.34}_{-0.09}$ |
| $P_c(4440)^+$ | $4440.3 \pm 1.3^{+4.1}_{-4.7}$ | $20.6 \pm 4.9^{+8.7}_{-10.1}$ | (<49)      | $1.11 \pm 0.33^{+0.22}_{-0.10}$ |
| $P_c(4457)^+$ | $4457.3 \pm 0.6^{+4.1}_{-1.7}$ | $6.4 \pm 2.0^{+5.7}_{-1.9}$   | (<20)      | $0.53 \pm 0.16^{+0.15}_{-0.13}$ |

## Comparison to numerical predictions

- Many theoretical predictions for  $\Sigma_c^+ \bar{D}^{(*)0}$  published before 2015, **some in quantitative agreement with the LHCb data**

- Wu, Molina, Oset, Zou, PRL 105, 232001 (2010),
- Wang, Huang, Zhang, Zou, PR C 84, 015203 (2011),**
- Yang, Sun, He, Liu, Zhu, Chin. Phys. C 36, 6 (2012),**
- Wu, Lee, Zou, PR C 85 044002 (2012),**
- Karliner, Rosner, PRL 115, 122001 (2015)



$\Delta E$  – binding energy

Example:

Nucleon resonances with hidden charm in coupled-channels models

Jia-Jun Wu, T.-S. H. Lee, and B. S. Zou

Phys. Rev. C **85**, 044002 – Published 17 April 2012

arXiv:1202.1036

TABLE III: The pole position ( $M - i\Gamma/2$ ) and “binding energy” ( $\Delta E = E_{thr} - M$ ) for different cut-off parameter  $\Lambda$  and spin-parity  $J^P$ . The threshold  $E_{thr}$  is 4320.79 MeV of  $\bar{D}\Sigma_c$  in PB system and 4462.18 MeV of  $\bar{D}^*\Sigma_c$  in VB system. The unit for the listed numbers is MeV.

| $J^P = \frac{1}{2}^-$ | PB System |                   |            | VB System         |            |
|-----------------------|-----------|-------------------|------------|-------------------|------------|
|                       | $\Lambda$ | $M - i\Gamma/2$   | $\Delta E$ | $M - i\Gamma/2$   | $\Delta E$ |
| 650                   | 800       |                   |            |                   |            |
|                       | 1200      | 4318.964 - 0.362i | 1.826      | 4459.513 - 0.417i | 2.667      |
|                       | 1500      | 4314.531 - 1.448i | 6.259      | 4454.088 - 1.662i | 8.092      |
|                       | 2000      | 4301.115 - 5.835i | 19.68      | 4438.277 - 7.115i | 23.90      |
|                       |           |                   |            |                   |            |
| $J^P = \frac{3}{2}^-$ | 650       | -                 | -          | -                 | -          |
|                       | 800       | -                 | -          | 4462.178 - 0.002i | 0.002      |
|                       | 1200      | -                 | -          | 4459.507 - 0.420i | 2.673      |
|                       | 1500      | -                 | -          | 4454.057 - 1.681i | 8.123      |
|                       | 2000      | -                 | -          | 4438.039 - 7.268i | 23.14      |

$$\Delta E(4312) = 5.8^{+1.0}_{-6.8} \text{ MeV} \quad \Delta E(4457) = 2.5^{+4.3}_{-4.1} \text{ MeV}$$

$\Lambda$  - cut off on exchanged meson mass.

$$\Delta E(4440) = 19.5^{+4.9}_{-4.3} \text{ MeV}$$

## LHCb pentaquark states vs Predictions

Consistence :  $P_c(4312) \rightarrow \bar{D}\Sigma_c(1/2^-)$   
 $P_c(4380) \rightarrow \bar{D}\Sigma_c^*(3/2^-)$   
 $P_c(4440) \text{ \& } P_c(4457) \rightarrow \bar{D}^*\Sigma_c(1/2^-, 3/2^-)$

### Problems:

- 1)  $P_c(4380)$  -- much larger decay width than prediction
- 2) Other  $P_c$  states have narrower width than prediction
- 3) All  $P_c$  states have negative parity ?

### 3. Progress on $P_c$ states after LHCb observation

Thresholds  $\bar{D}\Sigma_c^*$  (4383MeV),  $\bar{D}^*\Sigma_c$  (4460MeV),  $p\chi_{c1}$  (4449MeV)

#### 1) $\bar{D}\Sigma_c^*$ , $\bar{D}^*\Sigma_c$ , $\bar{D}^*\Sigma_c^*$ molecular states

R.Chen, X.Liu, X.Q.Li, S.L.Zhu, PRL115 (2015) 132002;

L.Roca, J.Nieves, E.Oset, PRD92 (2015) 094003;

J.He, PLB 753 (2016)547 ;

#### 2) diquark $cu$ & triquark $\bar{c}(ud)$ states

L.Maiani, A.D.Polosa, V. Riquer, PLB749 (2015) 289;

R.Lebed, PLB749 (2015) 454;

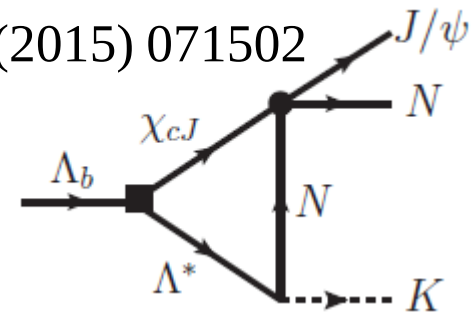
G.N.Li, M.He, X.G.He, JHEP 1512 (2015) 128;

R.Zhu, C.F.Qiao, PLB756 (2016) 259;

#### 3) Kinematic triangle-singularity

F.K.Guo, Ulf-G.Meißner, W.Wang, Z.Yang, PRD92 (2015) 071502

X.H.Liu, Q.Wang, Q.Zhao, PLB757 (2016) 231



**For comprehensive reviews, cf.:**

**H.X.Chen, W.Chen, X.Liu, S.L.Zhu, Phys.Rept. 639 (2016) 1**

**F.K.Guo, C.Hanhart, U.Meissner, Q.Wang, Q.Zhao, B.S.Zou, RMP 90 (2018)015004**

**Y.R.Liu, H.X.Chen, W.Chen, X.Liu, S.L.Zhu, Prog.Part.Nucl.Phys. 107 (2019) 237**

# Different predictions from various models :

Diquark model by  
A.Ali et al., PLB793 (2019) 365

| $J^P$               | This work     | Refs. [22, 23] |
|---------------------|---------------|----------------|
| $S_{ld} = 0, L = 0$ |               |                |
| $1/2^-$             | $3830 \pm 34$ | $4086 \pm 42$  |
|                     | $4150 \pm 29$ | $4162 \pm 38$  |
| $3/2^-$             | $4240 \pm 29$ | $4133 \pm 55$  |
| $S_{ld} = 0, L = 1$ |               |                |
| $1/2^+$             | $4030 \pm 39$ | $4030 \pm 62$  |
|                     | $4351 \pm 35$ | $4141 \pm 44$  |
|                     | $4430 \pm 35$ | $4217 \pm 40$  |
| $3/2^+$             | $4040 \pm 39$ |                |
|                     | $4361 \pm 35$ |                |
|                     | $4440 \pm 35$ |                |
| $5/2^+$             | $4457 \pm 35$ | $4510 \pm 57$  |

Hadrocharmonium states by  
M.Eides et al., arXiv:1904.11616

| Constituents     | Binding energy [MeV] | Mass [MeV] | Spin-parity    |
|------------------|----------------------|------------|----------------|
| $\eta_c(2S)N$    | 176.1                | 4401       | $1/2^-$        |
| $\chi_{c1}(1P)N$ | 44.2                 | 4406       | $3/2^+, 1/2^+$ |
| $h_c(1P)N$       | 43.9                 | 4421       | $1/2^+, 3/2^+$ |
| $\chi_{c2}(1P)N$ | 43.7                 | 4452       | $5/2^+, 3/2^+$ |

## $\bar{D}\Sigma_c^*$ , $\bar{D}^*\Sigma_c$ , $\bar{D}^*\Sigma_c^*$ bound states

[1] R.Chen, X.Liu, X.Q.Li, S.L.Zhu, PRL115 (2015) 132002;

$$P_c^+(4380) \text{ -- } \bar{D}^*\Sigma_c \quad 3/2^- \quad ; \quad P_c^+(4450) \text{ -- } \bar{D}^*\Sigma_c^* \quad 5/2^-$$

[2] Y.Yamaguchi, E. Santopinto, PRD96 (2017) 014018

$$P_c^+(4380) \text{ -- } \bar{D}^{(*)}\Sigma_c^{(*)} - \bar{D}^{(*)}\Lambda_c \quad 3/2^+ \quad ; \quad P_c^+(4450) \text{ -- } \bar{D}^{(*)}\Sigma_c^{(*)} - \bar{D}^{(*)}\Lambda_c \quad 5/2^-$$

[3] J.He, PLB 753 (2016)547 ; PRD95 (2017)074004

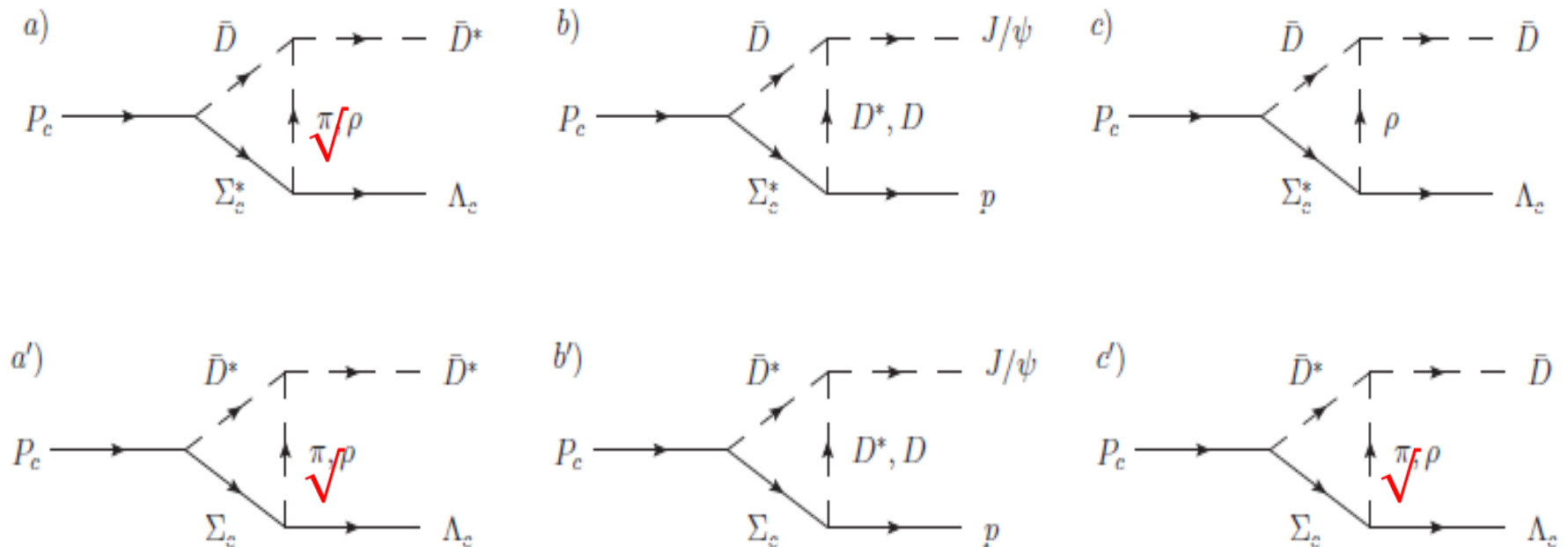
Y.H.Lin, C.W.Shen, F.K.Guo, B.S.Zou, PRD95(2017)114017

$$P_c^+(4380) \text{ -- } \bar{D}\Sigma_c^*/ \bar{D}^*\Sigma_c \quad 3/2^- \quad ; \quad P_c^+(4450) \text{ -- } \bar{D}^*\Sigma_c \quad 5/2^+$$

**→ Different predictions to be checked !**

# Disentangling $\bar{D}\Sigma_c^*$ / $\bar{D}^*\Sigma_c$ nature of $P_c^+$ states from their decays

Y.H.Lin, C.W.Shen, F.K.Guo, B.S.Zou, PRD95(2017)114017



**One pion exchange is very important !**

$\bar{D}\Sigma_c^*$  &  $\bar{D}^*\Sigma_c^*$  are much broader than  $\bar{D}\Sigma_c$  &  $\bar{D}^*\Sigma_c$  states

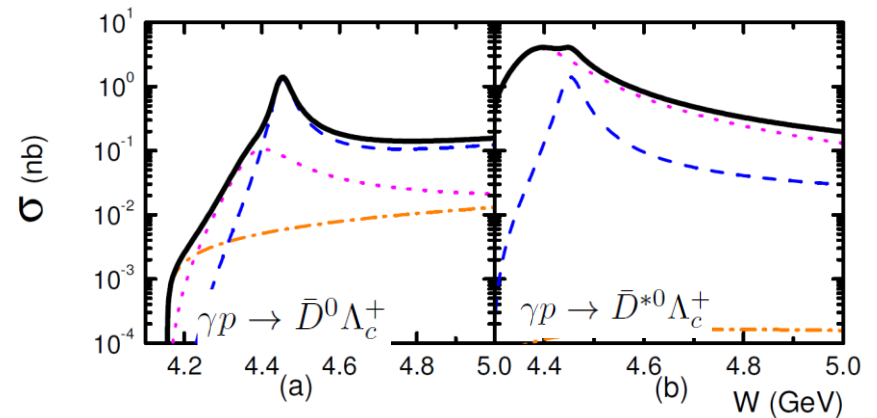
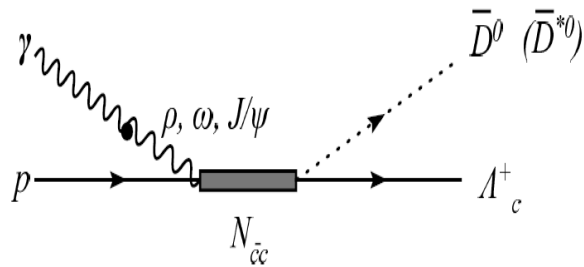
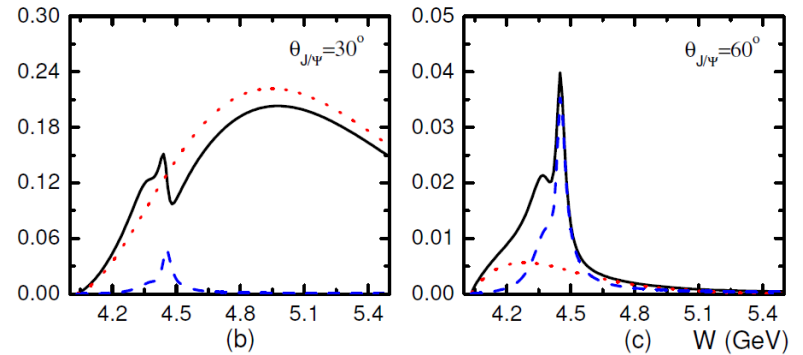
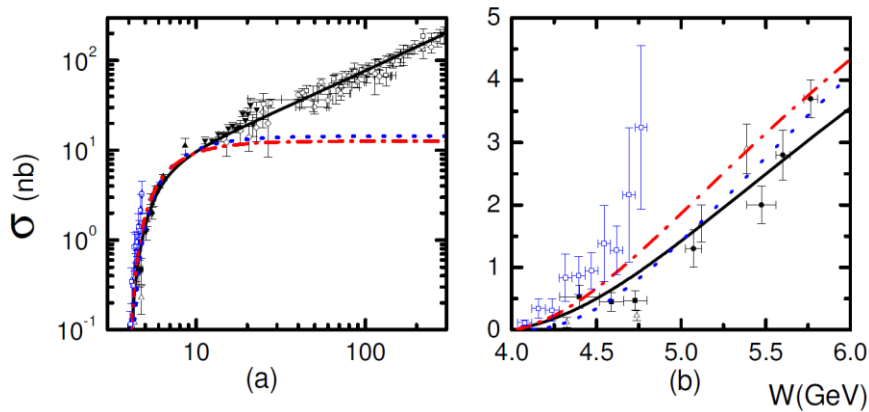
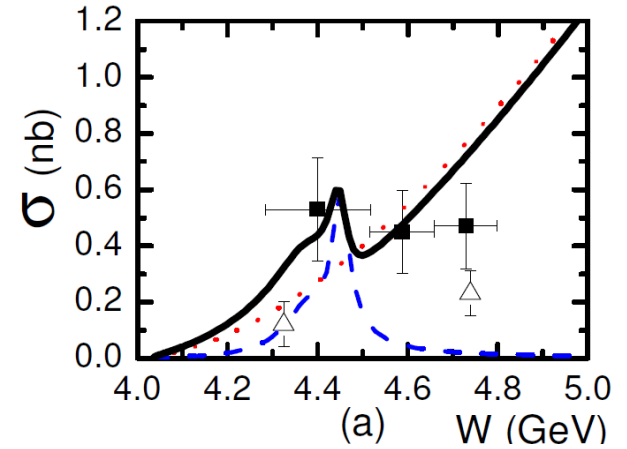
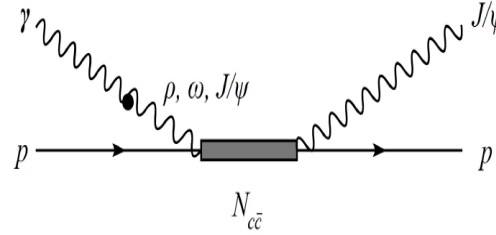
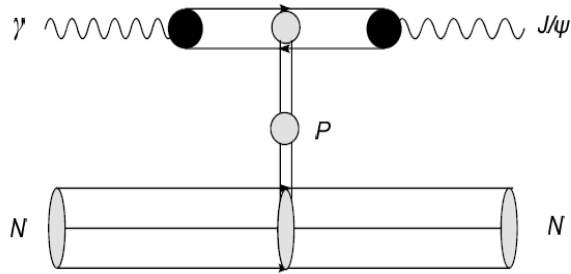
## Partial decay widths of $P_c^+(4380)$ & $P_c^+(4450)$

| Mode                  | Widths (MeV)                       |                                    |                                    |                                    |
|-----------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
|                       | $P_c(4380)$                        |                                    | $P_c(4450)$                        |                                    |
|                       | $\bar{D}\Sigma_c^*(\frac{3}{2}^-)$ | $\bar{D}^*\Sigma_c(\frac{3}{2}^-)$ | $\bar{D}^*\Sigma_c(\frac{3}{2}^-)$ | $\bar{D}^*\Sigma_c(\frac{5}{2}^+)$ |
| $\bar{D}^*\Lambda_c$  | 131.3 ✓                            | 35.3 ✓                             | 72.3 ✓                             | 20.5 ✓                             |
| $J/\psi p$            | 3.8                                | 16.6                               | 16.3                               | 4.0                                |
| $\bar{D}\Lambda_c$    | 1.2                                | 17.0 ✓                             | 41.4 ✓                             | 18.8 ✓                             |
| $\pi N$               | 0.06                               | 0.07                               | 0.07                               | 0.2                                |
| $\chi_{c0} p$         | 0.9                                | 0.004                              | 0.02                               | 0.002                              |
| $\eta_c p$            | 0.2                                | 0.09                               | 0.1                                | 0.04                               |
| $\rho N$              | 1.4                                | 0.15                               | 0.14                               | 0.3                                |
| $\omega p$            | 5.3                                | 0.6                                | 0.5                                | 0.3                                |
| $\bar{D}\Sigma_c$     | 0.01                               | 0.1                                | 1.2                                | 0.8                                |
| $\bar{D}\Sigma_c^*$   | ...                                | ...                                | 7.7                                | 1.4                                |
| $\bar{D}\Lambda_c\pi$ | 11.6                               | ...                                | ...                                | ...                                |
| Total                 | 144.3                              | 69.9                               | 139.8                              | 46.4                               |

It is very important to study  $P_c \rightarrow \bar{D}^*\Lambda_c$  &  $\bar{D}\Lambda_c$  !

# Pin down $P_c^+$ states from their photo-production

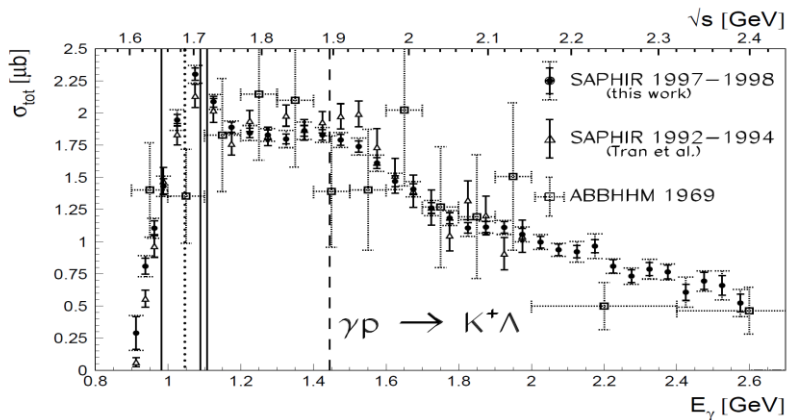
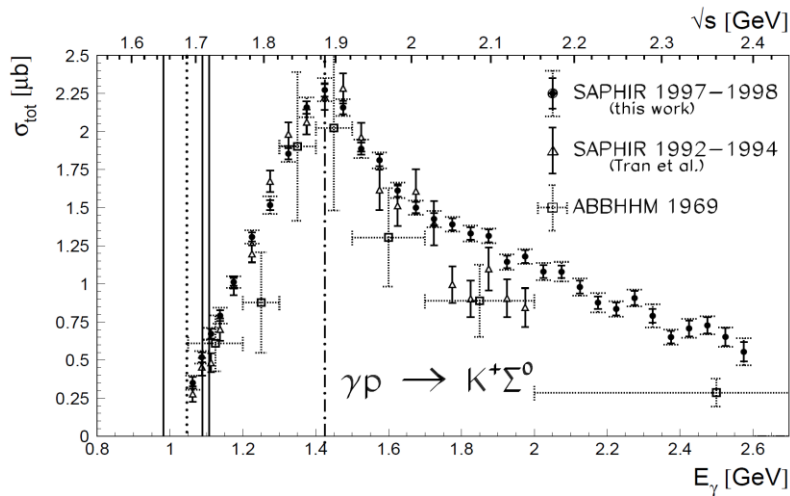
J.J.Wu, T.S.H.Lee, B.S.Zou, arXiv:1906.05375



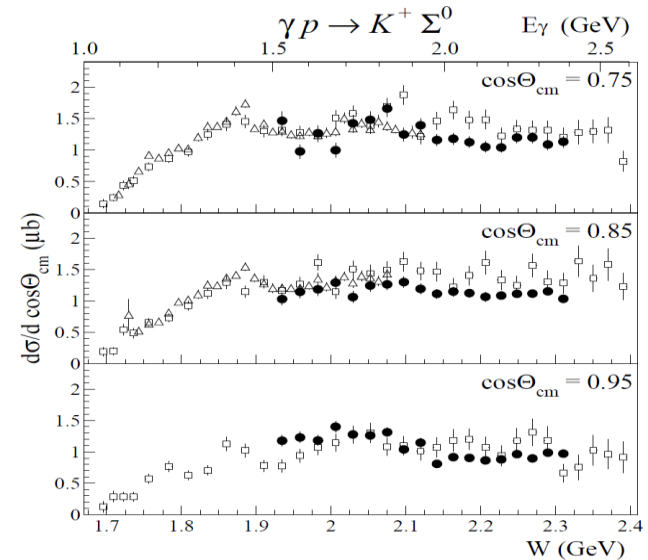
# 4. Strange & beauty partners of $P_c$ states

Strangeness partners of  $P_c$  states:  $N^*(1875)$  &  $N^*(2080)$

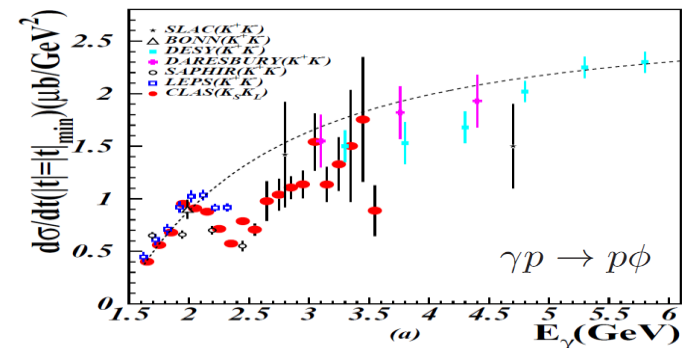
$K\Sigma^* \sim 1880$        $K^*\Sigma \sim 2086$



Glander, K.H. *et al.* EPJA19 (2004) 251-273

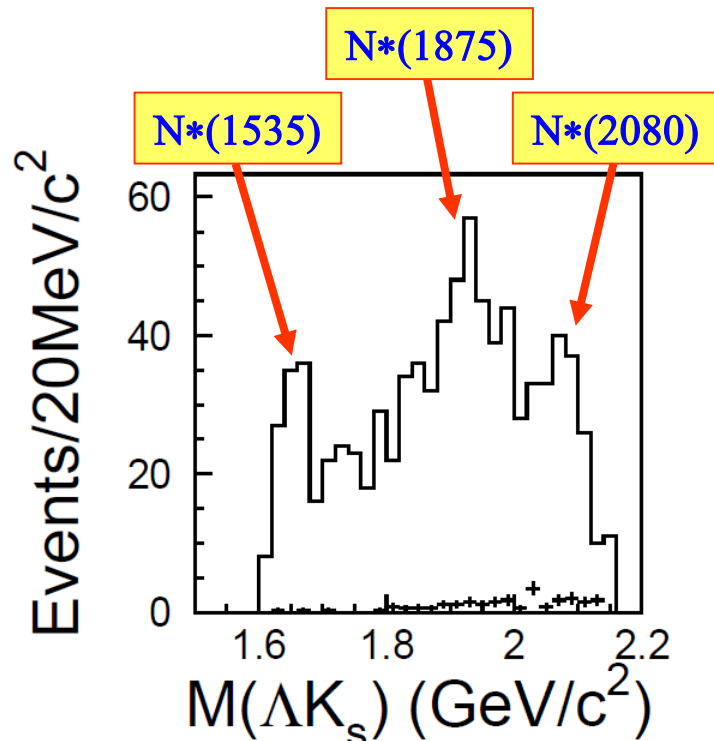


LEPS, PRC73 (2006) 035214

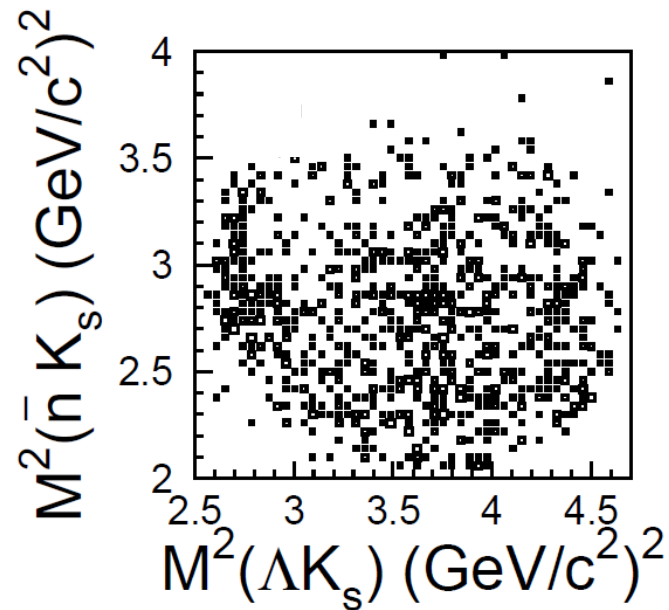


CLAS, PRC89 (2014) 055206

# $N_{ss}^-$ penta-quarks at BES ?!



$$J/\psi \rightarrow nK_s^0\bar{\Lambda}$$



BESII, Phys. Lett. B659 (2008) 789



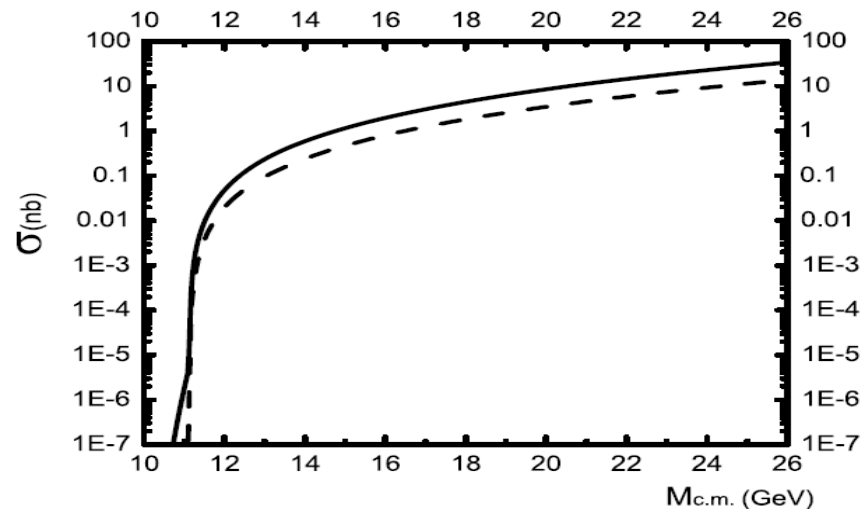
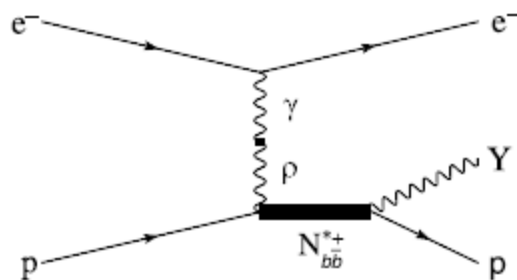
# Prediction of super-heavy $N^*$ and $\Lambda^*$ resonances with hidden beauty

Jia-Jun Wu<sup>a,\*</sup>, Lu Zhao<sup>a</sup>, B.S. Zou<sup>a,b</sup>

| $M$ (MeV) | $\Gamma$ (MeV) | $\Gamma_i$ (MeV) |            |              |              |            |
|-----------|----------------|------------------|------------|--------------|--------------|------------|
|           |                | $\pi N$          | $\eta N$   | $\eta' N$    | $K \Sigma$   | $\eta_b N$ |
| 11 052    | 1.38           | 0.10             | 0.21       | 0.11         | 0.42         | 0.52       |
|           |                | $\rho N$         | $\omega N$ | $K^* \Sigma$ | $\Upsilon N$ |            |
| 11 100    | 1.33           | 0.09             | 0.30       | 0.39         | 0.51         |            |

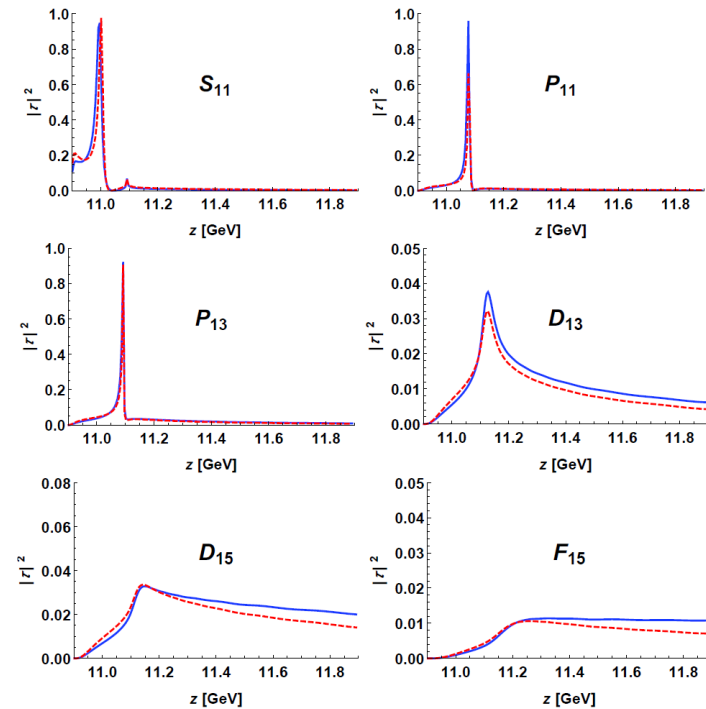
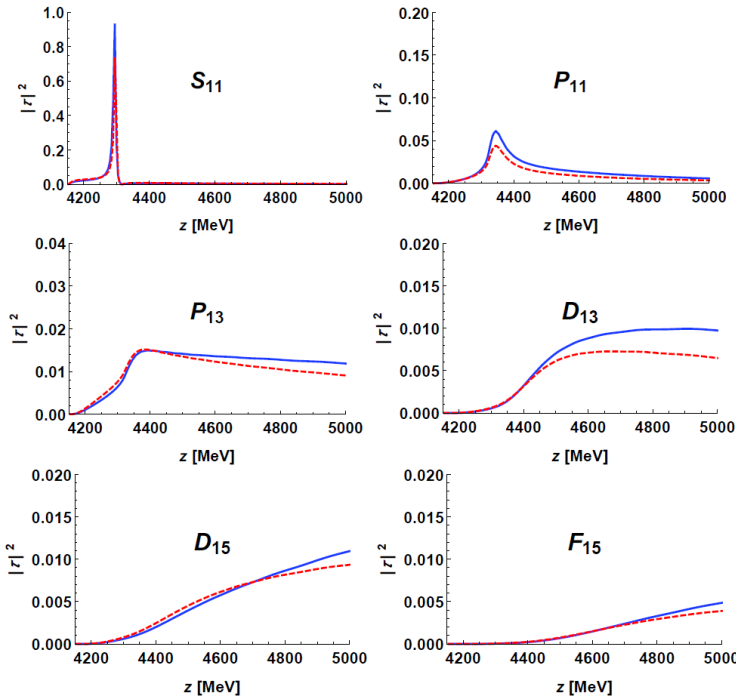
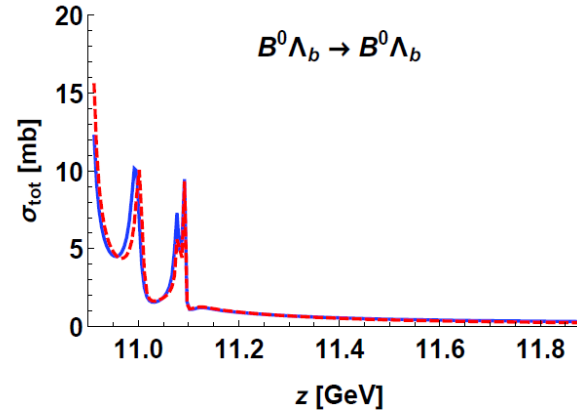
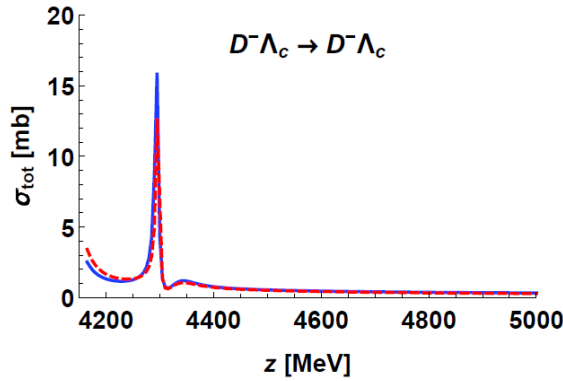
$1/2^-$

$1/2^-, 3/2^-$



# $\bar{D}\Lambda_c - \bar{D}\Sigma_c$ and $B\Lambda_b - B\Sigma_b$ dynamical coupled channel study

C.W.Shen, Roehen, Meissner, Zou, CPC42(2018) 023106



More pentaquarks with hidden beauty than with hidden charm

# Decay behavior of $P_s$ & $P_b$ pentaquark states

Y.H.Lin, C.W.Shen, B.S.Zou, NPA980(2018)21

| Mode             | Widths (MeV)        |                     |                     |
|------------------|---------------------|---------------------|---------------------|
|                  | $J^P = 3/2^-$       |                     | $J^P = 1/2^-$       |
|                  | $N(1875) K\Sigma^*$ | $N(2080) K^*\Sigma$ | $N(2080) K^*\Sigma$ |
| $N\sigma(500)$   | 2.6                 | 0.05                | 0.3                 |
| $\pi N$          | 3.8                 | 0.2                 | 22.7                |
| $\rho N$         | 2.3                 | 3.8                 | 6.1                 |
| $\omega p$       | 6.6                 | 11.3                | 18.2                |
| $K\Sigma$        | 0.03                | 1.4                 | 9.1                 |
| $K\Lambda$       | 0.7                 | 3.7                 | 19.3                |
| $\eta p$         | 0.6                 | 0.4                 | 1.8                 |
| $\pi\Delta$      | 201.4               | 82.6                | 46.9                |
| $K^*\Lambda$     | -                   | 2.4                 | 7.9                 |
| $\phi p$         | -                   | 19.2                | 27.0                |
| $K\Sigma^*$      | -                   | 7.3                 | 1.3                 |
| $K\Lambda(1520)$ | -                   | 0.1                 | 1.3                 |
| $K\Lambda(1405)$ | -                   | 8.0                 | 8.8                 |
| $K\pi\Lambda$    | 10.1                | -                   | -                   |
| $K\pi\Sigma$     | -                   | 41.3                | 46.1                |
| Total            | 228.2               | 181.7               | 216.8               |

| Mode           | Widths (MeV)  |               |               |
|----------------|---------------|---------------|---------------|
|                | $J^P = 3/2^-$ |               | $J^P = 1/2^-$ |
|                | $B\Sigma_b^*$ | $B^*\Sigma_b$ | $B^*\Sigma_b$ |
| $B^*\Lambda_b$ | 271.1         | 19.9          | 167.0         |
| $\Upsilon p$   | 0.3           | 0.04          | 0.1           |
| $\rho N$       | 5.5           | 0.02          | 0.1           |
| $\omega p$     | 20.9          | 0.07          | 0.4           |
| $B\Lambda_b$   | -             | 7.3           | 135.9         |
| $B\Sigma_b$    | -             | -             | -             |
| $\eta_b p$     | 0.02          | 0.0001        | 0.0009        |
| $\chi_{b0} p$  | 1.4           | 0.0008        | 0.2           |
| $\pi N$        | 0.7           | 0.005         | 0.003         |
| $B\Sigma_b^*$  | -             | -             | -             |
| Total          | 299.9         | 27.4          | 303.8         |

## Guidance for $P_s$ & $P_b$ search

Decay behaviors of possible  $\Lambda_{c\bar{c}}$  states in hadronic molecule pictures

C.W.Shen, J.J.Wu, B.S.Zou (2019), ArXiv:1906.03896

## Guidance for $P_{sc}$ search

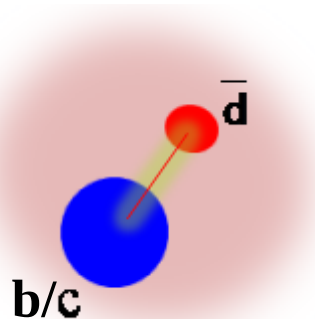
## 5. Prospects

### ◆ my favorite strategy for hadron spectroscopy:

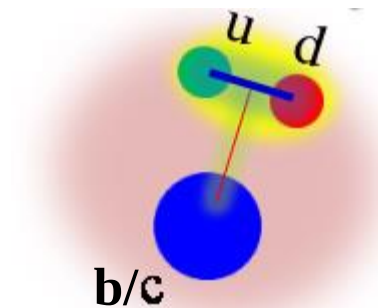
$\bar{c}c u u d$  &  $\bar{c}c u d s \rightarrow s s s - \bar{q} q s s s \rightarrow c q q - \bar{q} q c q q$   
 $\rightarrow$  hyperons  $\rightarrow$  light baryons

$\bar{c}c \bar{u} d$  &  $\bar{c} s \bar{u} d \rightarrow \bar{c}c - \bar{q} q \bar{c}c \rightarrow \bar{c}q - \bar{c}q \bar{q} q$   
 $\rightarrow$  K mesons  $\rightarrow$  light mesons

$s \rightarrow c \rightarrow b$



charm & beauty meson



charm & beauty baryon

- New penta-quark spectroscopy provides a new ideal platform for understanding multiquark dynamics
- Further experimental confirmation and extension for whole penta-quark spectroscopy from  $\gamma N$ ,  $\pi N$ ,  $KN$ ,  $e^+e^- \rightarrow \bar{\Lambda}_b \Lambda_b$ , etc.

$ep/\gamma p$ @JLab,  $\pi 10/K 10$ @JPARC, BelleII, BESIII, Eic/EicC, PANDA@FAIR, STCF etc. may play important role here!

Thank you for  
your attention!