

# Hidden-charm pentaquarks and their photo- and pion-induced productions

何军

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Eur.Phys.J. C79 (2019)393, arXiv:1903.11872; arXiv:1904.00221

Phys.Rev. D99 (2019)114007, arXiv:1904.11706; arXiv:1906.04044

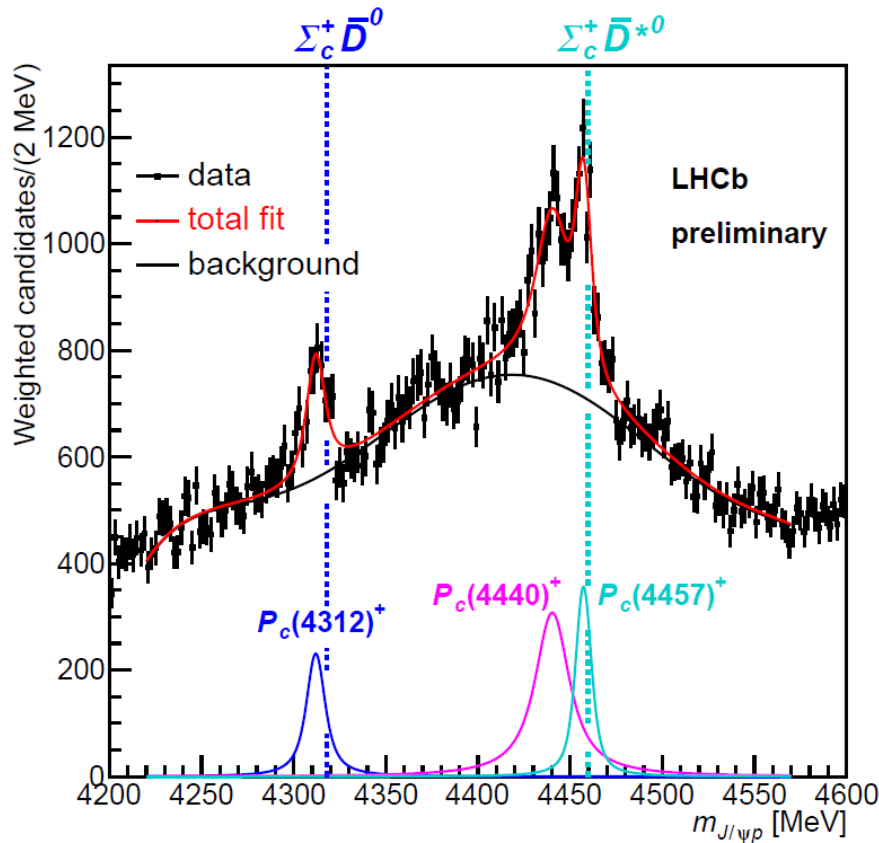
第十八届全国中高能核物理大会，长沙，2019年6月21-25日

# Outline

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- LHCb pentaquarks
- Molecular state interpretation of  $P_c$  states
- Photo- and pion induced productions
- Summary

# New results at LHCb

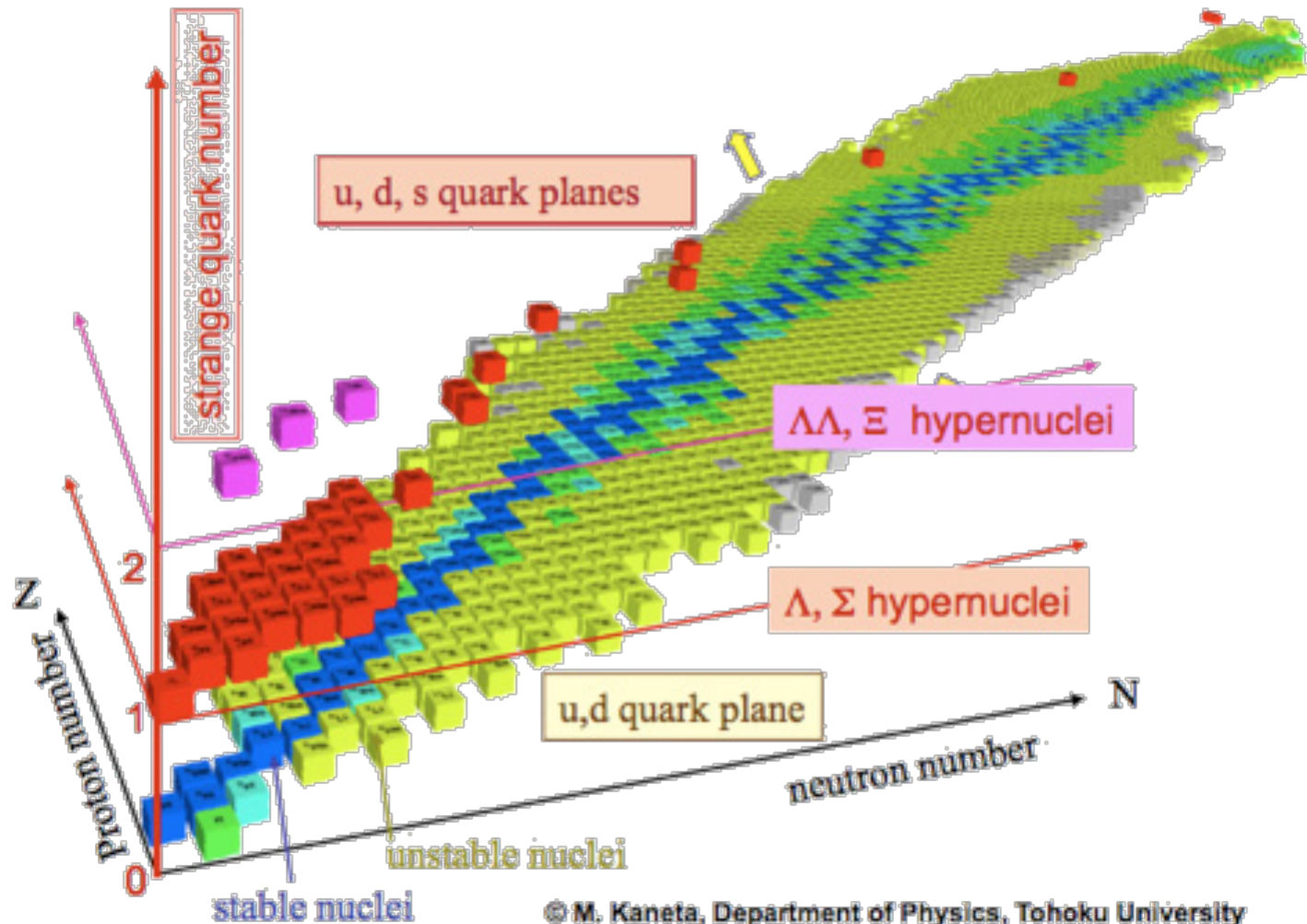


- $P_c(4450) \rightarrow P_c(4440) + P_c(4457)$
- New  $P_c(4312)$
- Confirmation of  $P_c(4380)$  awaits construction of new amplitude model

Moriond QCD, Tomasz Skwarnicki, Mar 26, 2019  
 Phys.Rev.Lett. 122 (2019) no.22, 222001

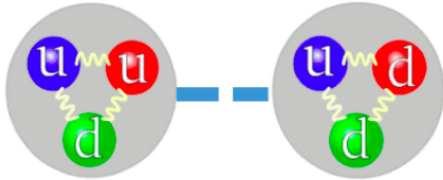
| State         | $M$ [ MeV ]                    | $\Gamma$ [ MeV ]              | (95% CL) | $\mathcal{R}$ [%]               |
|---------------|--------------------------------|-------------------------------|----------|---------------------------------|
| $P_c(4312)^+$ | $4311.9 \pm 0.7^{+6.8}_{-0.6}$ | $9.8 \pm 2.7^{+3.7}_{-4.5}$   | (< 27)   | $0.30 \pm 0.07^{+0.34}_{-0.09}$ |
| $P_c(4440)^+$ | $4440.3 \pm 1.3^{+4.1}_{-4.7}$ | $20.6 \pm 4.9^{+8.7}_{-10.1}$ | (< 49)   | $1.11 \pm 0.33^{+0.22}_{-0.10}$ |
| $P_c(4457)^+$ | $4457.3 \pm 0.6^{+4.1}_{-1.7}$ | $6.4 \pm 2.0^{+5.7}_{-1.9}$   | (< 20)   | $0.53 \pm 0.16^{+0.15}_{-0.13}$ |

# Multi-Favored Nuclear Chart



# Deuteron

Only well-established hadronic molecular state [1].

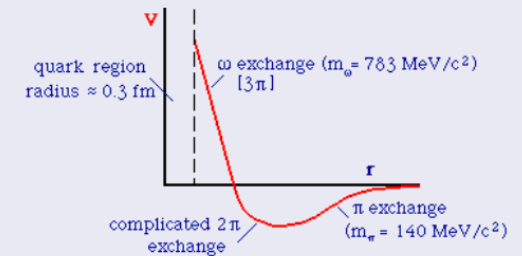
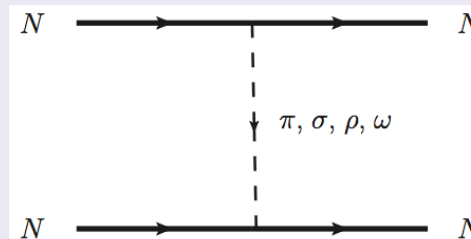


Phys. Rept., 639(2016)1

## Main properties

- bound state of  $pn$
- quantum number  $J^P = 1^+$
- binding energy: about 2.2 MeV  
nucleon mass: about 1 GeV
- charge radius: about 2 fm  
nucleon radius: about 1 fm
- stable

## Yukawa model

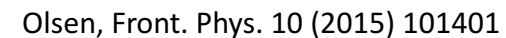


The effective  $\pi NN$  interaction Lagrangian

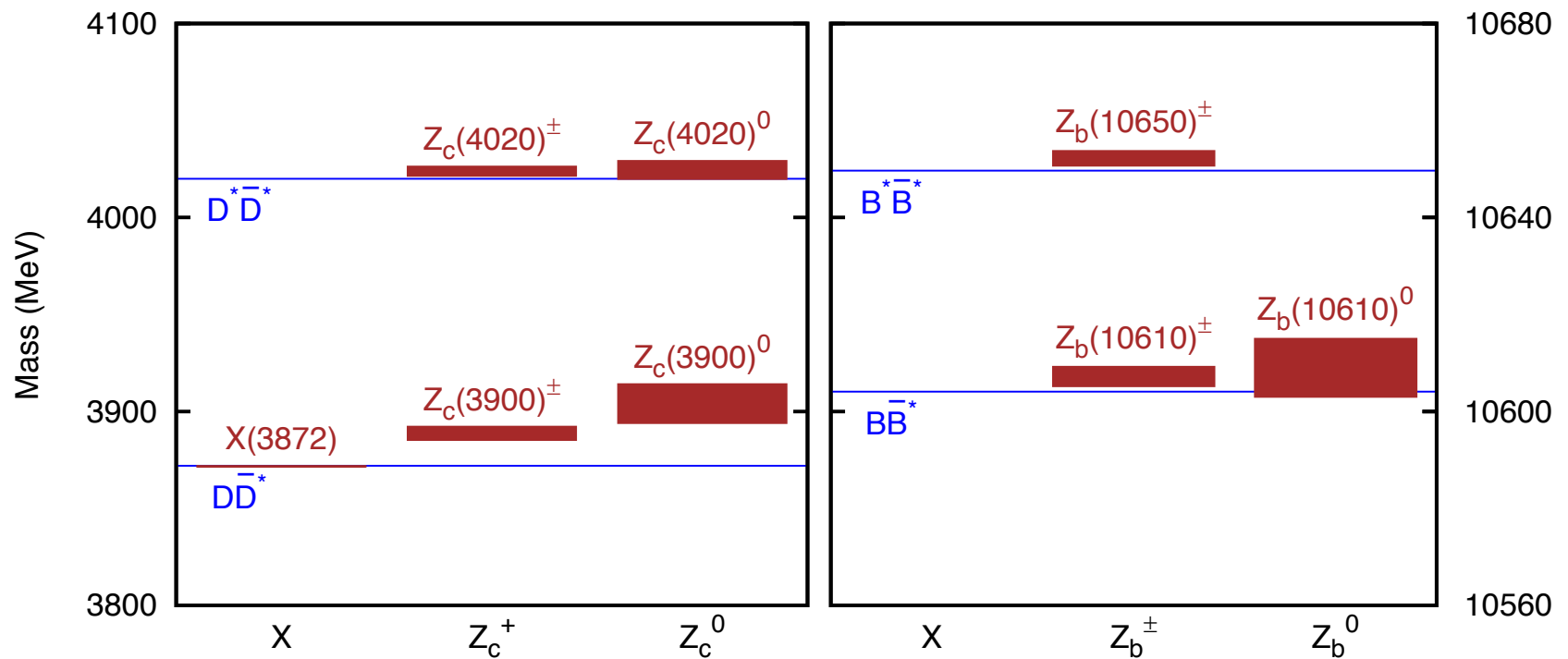
$$\mathcal{L} = g_{NN\pi} \bar{\psi} i \gamma_5 \boldsymbol{\tau} \psi \cdot \boldsymbol{\pi}.$$

The non-relativistic nucleon-nucleon potential [1]

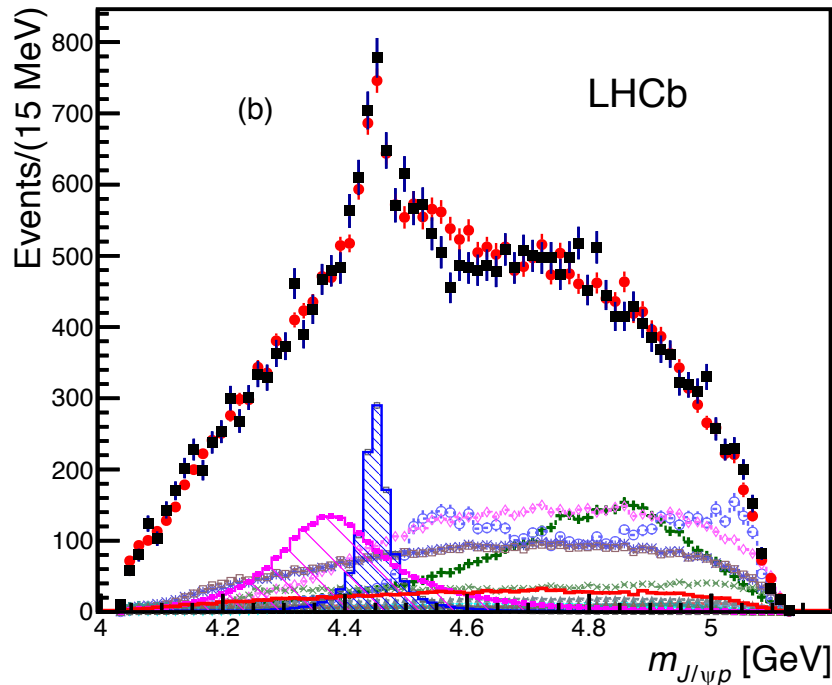
$$V_\pi = \frac{g_{NN\pi}^2}{4\pi} \frac{m_\pi^2}{12m_N^2} (\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2) \frac{e^{-m_\pi r}}{r} \left\{ \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 + \left[ \frac{3(\boldsymbol{\sigma}_1 \cdot \mathbf{r})(\boldsymbol{\sigma}_2 \cdot \mathbf{r})}{r^2} - \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 \right] \left[ 1 + \frac{3}{m_\pi r} + \frac{3}{m_\pi^2 r^2} \right] \right\}.$$



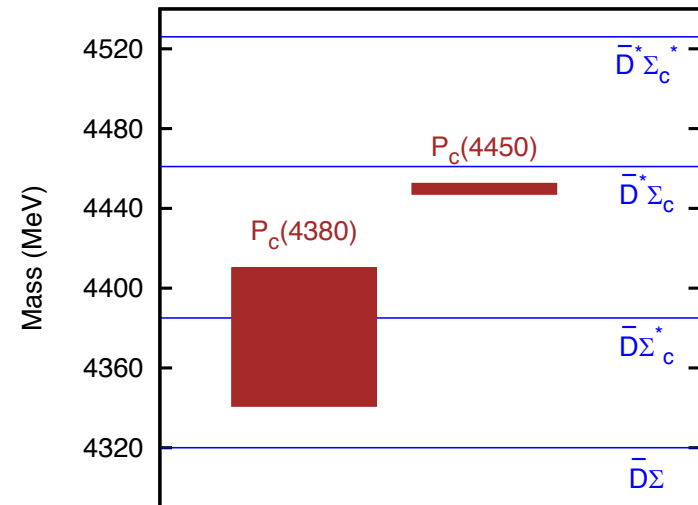
# BB\*/DD\* thresholds



# Old results at LHCb



$J=3/2$  or  $5/2$ ; opposite parities



无论是 $5/2^-$  还是 $5/2^+$ 都很难在s波分子态图像下解释  
 特别是我们坚持分子态在阈值附近 $P_c(4450): \Sigma_c \bar{D}^*$ ,  $P_c(4380): \Sigma_c^* \bar{D}$ .

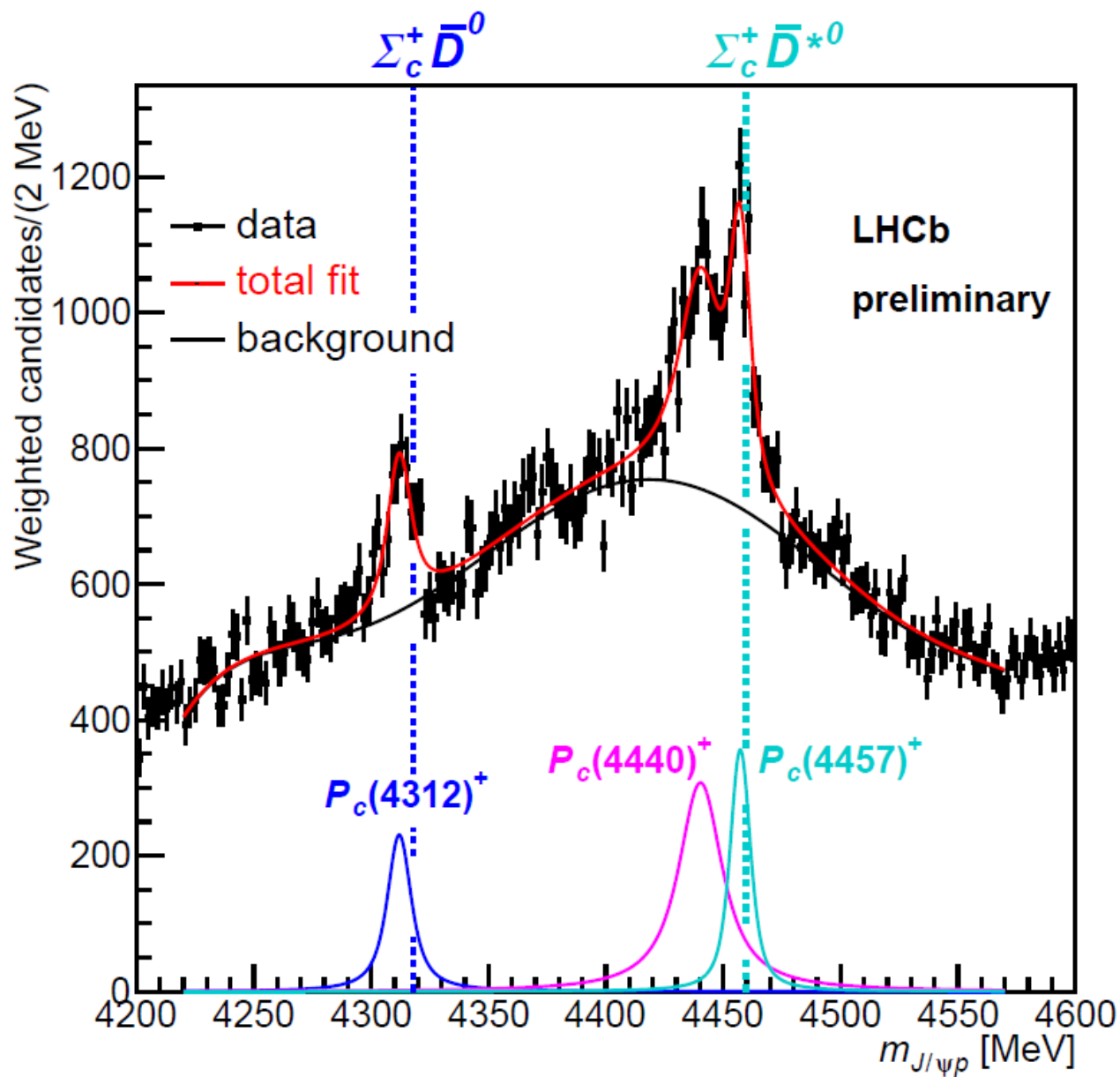
# Difficulties of molecular state interpretation

$P_c(4380), P_c(4450): \Sigma_c \left(\frac{1}{2}^+\right), \Sigma_c^* \left(\frac{3}{2}^+\right) \text{ and } \bar{D}(0^-), \bar{D}^*(1^-)$

No S-wave state with spin 5/2!

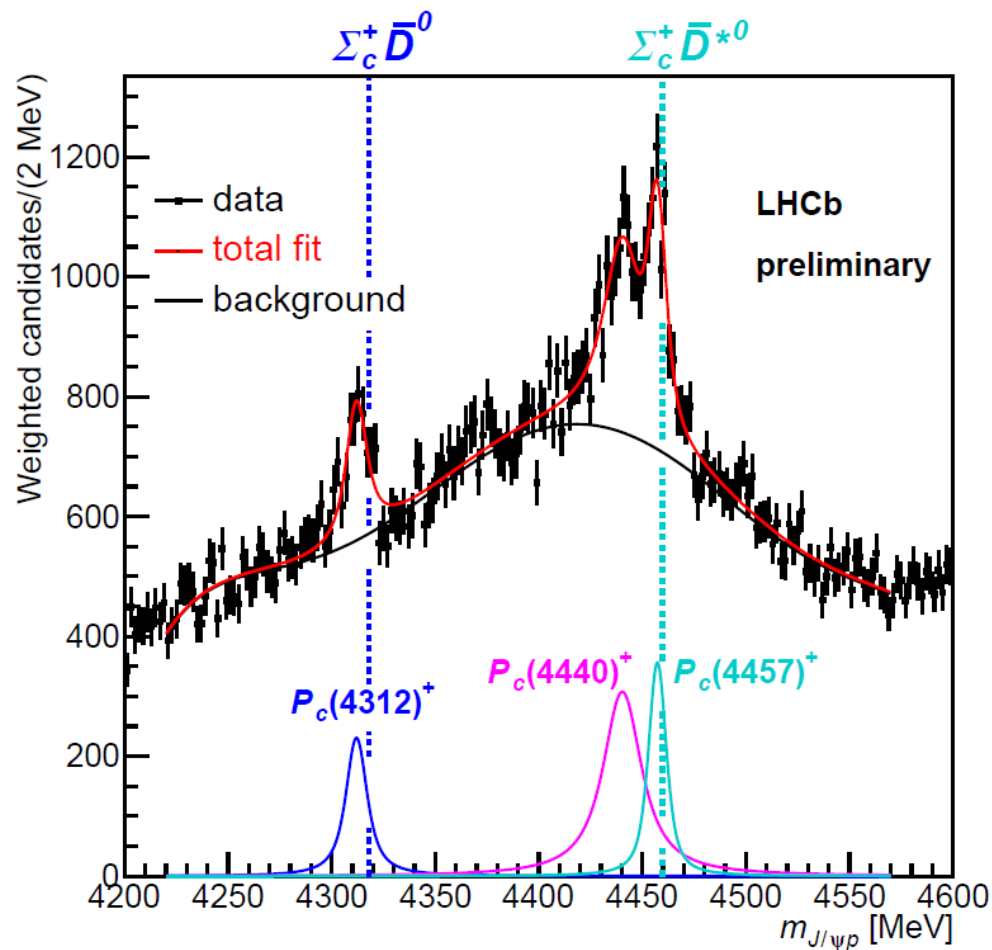
Exp:  $J=3/2$  or  $5/2$ ; opposite parities.

- L.Roca, J.Nieves, E.Oset, PRD92 (2015) 094003;  
 $P_c(4450): \Sigma_c \bar{D}^* - \Sigma_c^* \bar{D}^* (3/2^-); P_c(4380): \Sigma_c^* \bar{D}?$
- R. Chen, X.Liu, X.Q.Li, S.L.Zhu, PRL115 (2015) 132002;  
 $P_c(4450): \Sigma_c^* \bar{D}^* (5/2^-); P_c(4380): \Sigma_c \bar{D}^* (3/2^-)$
- J.He, PLB 753 (2016)547 ;  
 $P_c(4450): \Sigma_c \bar{D}^* (5/2^+); P_c(4380): \Sigma_c^* \bar{D} (3/2^-)$
- .....



新的实验没有给出 $J^P, 5/2$ 可能是来源于双峰

# 新结果更倾向于分子态解释



## 接近阈值

$\Sigma_c \bar{D}$ :  $P_c(4312)$

$\Sigma_c \bar{D}^*$ :  $P_c(4440), P_c(4457)$

$\Sigma_c^* \bar{D}$ :  $P_c(4380)?$

## 量子数 S波

$\Sigma_c \bar{D}$ :  $\frac{1}{2}^- \rightarrow P_c(4312)$

$\Sigma_c \bar{D}^*$ :  $\frac{1}{2}^-, \frac{3}{2}^- \rightarrow P_c(4440), P_c(4457)$

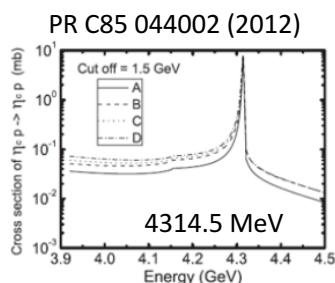
$\Sigma_c^* \bar{D}$ :  $\frac{3}{2}^- \rightarrow P_c(4380)?$

## 宽度

# Comparison to numerical predictions

- Many theoretical predictions for  $\Sigma_c^+ \bar{D}^{(*)0}$  published before 2015, **some in quantitative agreement with the LHCb data**

- Wu,Molina,Oset,Zou, PRL105, 232001 (2010),
- Wang,Huang,Zhang,Zou, PR C84, 015203 (2011),
- Yang,Sun,He,Liu,Zhu, Chin. Phys. C36, 6 (2012),
- Wu, Lee,Zou, PR C85 044002 (2012),
- Karliner,Rosner, PRL 115, 122001 (2015)



$\Delta E$  – binding energy

Example:

Nucleon resonances with hidden charm in coupled-channels models

Jia-Jun Wu, T.-S. H. Lee, and B. S. Zou

Phys. Rev. C **85**, 044002 – Published 17 April 2012

arXiv:1202.1036

TABLE III: The pole position ( $M - i\Gamma/2$ ) and “binding energy” ( $\Delta E = E_{thr} - M$ ) for different cut-off parameter  $\Lambda$  and spin-parity  $J^P$ . The threshold  $E_{thr}$  is 4320.79 MeV of  $\bar{D}\Sigma_c$  in PB system and 4462.18 MeV of  $\bar{D}^*\Sigma_c$  in VB system. The unit for the listed numbers is MeV.

| $J^P = \frac{1}{2}^-$ | PB System |                   |            | VB System         |            |
|-----------------------|-----------|-------------------|------------|-------------------|------------|
|                       | $\Lambda$ | $M - i\Gamma/2$   | $\Delta E$ | $M - i\Gamma/2$   | $\Delta E$ |
|                       | 650       | -                 | -          | -                 | -          |
|                       | 800       | -                 | -          | 4462.178 - 0.002i | 0.002      |
|                       | 1200      | 4318.964 - 0.362i | 1.826      | 4459.513 - 0.417i | 2.667      |
|                       | 1500      | 4314.531 - 1.448i | 6.259      | 4454.088 - 1.662i | 8.092      |
|                       | 2000      | 4301.115 - 5.835i | 19.68      | 4438.277 - 7.115i | 23.90      |
| $J^P = \frac{3}{2}^-$ |           |                   |            |                   |            |
|                       | 650       | -                 | -          | -                 | -          |
|                       | 800       | -                 | -          | 4462.178 - 0.002i | 0.002      |
|                       | 1200      | -                 | -          | 4459.507 - 0.420i | 2.673      |
|                       | 1500      | -                 | -          | 4454.057 - 1.681i | 8.123      |
|                       | 2000      | -                 | -          | 4438.039 - 7.268i | 23.14      |

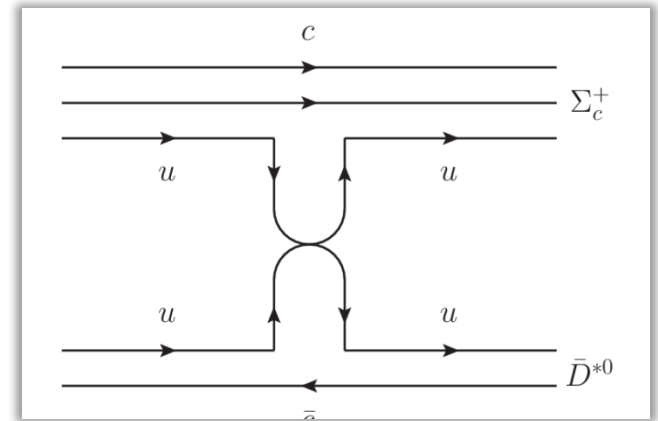
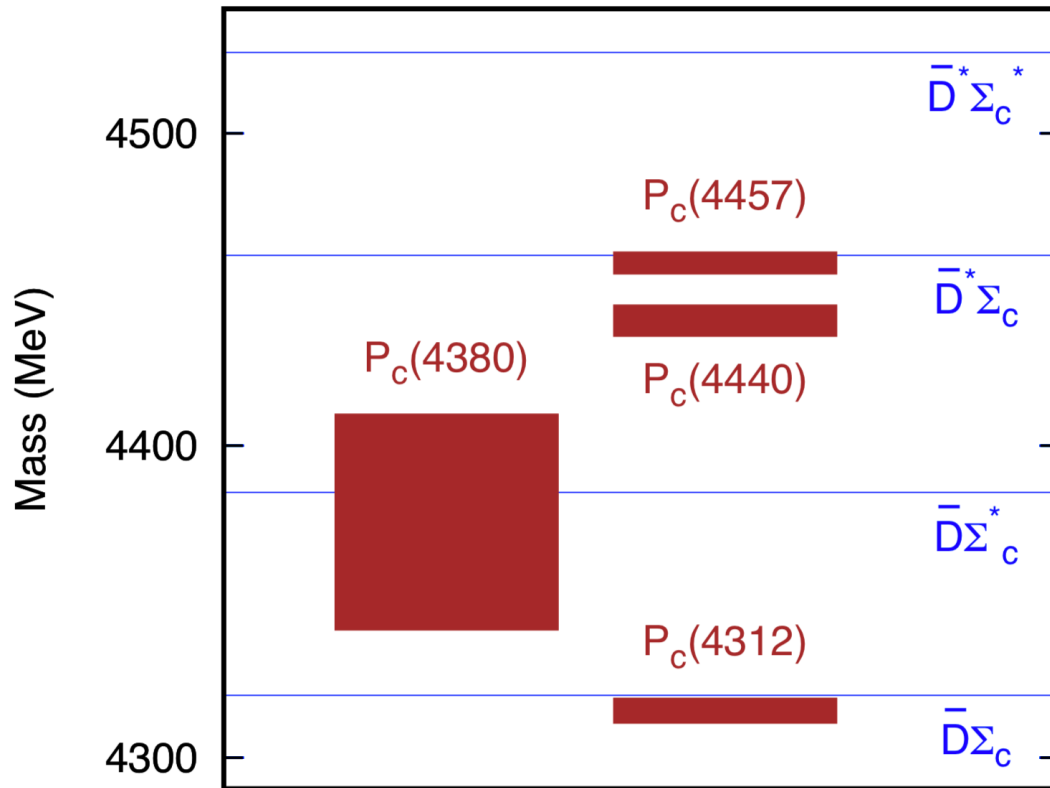
$$\Delta E(4312) = 5.8^{+1.0}_{-6.8} \text{ MeV} \quad \Delta E(4457) = 2.5^{+4.3}_{-4.1} \text{ MeV}$$

$\Lambda$  - cut off on exchanged meson mass.

$$\Delta E(4440) = 19.5^{+4.9}_{-4.3} \text{ MeV}$$

Molecular state interpretation  
of  $P_c(4312)$ ,  $P_c(4440)$ ,  $P_c(4457)$

# LHCb五夸克态的分子态解释



$$\bar{D}\Sigma_c - \bar{D}\Sigma_c^* - \bar{D}^*\Sigma_c - \bar{D}^*\Sigma_c^*$$

Exchanged mesons :  
 $\pi, \eta, \rho, \omega, \sigma$

# Heavy quark limit and chiral symmetry

Chen et al. PRD47(1993)1030; Yan et al. PRD46(1992)1148;  
Wise, PRD45(1992)2188; Casalbuoni et al. Phys. Rept. 281(1997)145

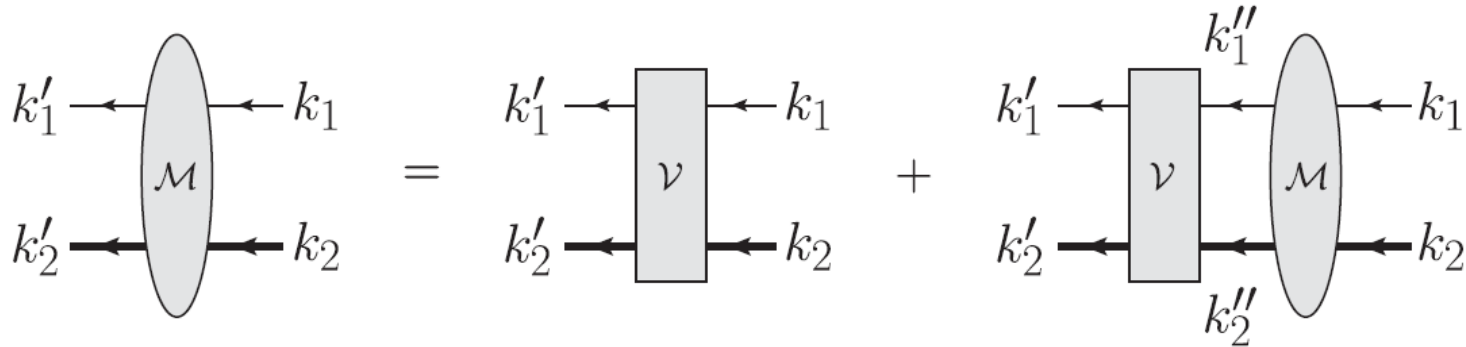
$$\begin{aligned}
 \mathcal{L}_{\tilde{\mathcal{P}}^* \tilde{\mathcal{P}} \mathbb{P}} &= i \frac{2g \sqrt{m_{\tilde{\mathcal{P}}} m_{\tilde{\mathcal{P}}^*}}}{f_\pi} (-\tilde{\mathcal{P}}_{a\lambda}^* \tilde{\mathcal{P}}_b + \tilde{\mathcal{P}}_a^* \tilde{\mathcal{P}}_{b\lambda}) \partial^\lambda \mathbb{P}_{ab}, \\
 \mathcal{L}_{\tilde{\mathcal{P}}^* \tilde{\mathcal{P}}^* \mathbb{P}} &= -\frac{g}{f_\pi} \epsilon_{\alpha\mu\nu\lambda} \tilde{\mathcal{P}}_a^{*\mu\dagger} \overleftrightarrow{\partial}^\alpha \tilde{\mathcal{P}}_b^{*\lambda} \partial^\nu \mathbb{P}_{ba}, \\
 \mathcal{L}_{\tilde{\mathcal{P}}^* \tilde{\mathcal{P}} \mathbb{V}} &= \sqrt{2} \lambda g_V \epsilon_{\lambda\alpha\beta\mu} (-\tilde{\mathcal{P}}_a^{*\mu\dagger} \overleftrightarrow{\partial}^\lambda \tilde{\mathcal{P}}_b + \tilde{\mathcal{P}}_a^* \overleftrightarrow{\partial}^\lambda \tilde{\mathcal{P}}_b^{*\mu}) (\partial^\alpha \mathbb{V}^\beta)_{ab}, \\
 \mathcal{L}_{\tilde{\mathcal{P}} \tilde{\mathcal{P}} \mathbb{V}} &= -i \frac{\beta g_V}{\sqrt{2}} \tilde{\mathcal{P}}_a^\dagger \overleftrightarrow{\partial}_\mu \tilde{\mathcal{P}}_b \mathbb{V}_{ab}^\mu, \\
 \mathcal{L}_{\tilde{\mathcal{P}}^* \tilde{\mathcal{P}}^* \mathbb{V}} &= -i \frac{\beta g_V}{\sqrt{2}} \tilde{\mathcal{P}}_a^{*\dagger} \overleftrightarrow{\partial}_\mu \tilde{\mathcal{P}}_b^{*\mu} \mathbb{V}_{ab}^\mu \\
 &\quad - i 2 \sqrt{2} \lambda g_V m_{\tilde{\mathcal{P}}} \tilde{\mathcal{P}}_a^{*\mu\dagger} \tilde{\mathcal{P}}_b^{*\nu} (\partial_\mu \mathbb{V}_\nu - \partial_\nu \mathbb{V}_\mu)_{ab}, \\
 \mathcal{L}_{\tilde{\mathcal{P}} \tilde{\mathcal{P}} \sigma} &= -2 g_s m_{\tilde{\mathcal{P}}} \tilde{\mathcal{P}}_a^\dagger \tilde{\mathcal{P}}_a \sigma, \\
 \mathcal{L}_{\tilde{\mathcal{P}}^* \tilde{\mathcal{P}}^* \sigma} &= 2 g_s m_{\tilde{\mathcal{P}}} \tilde{\mathcal{P}}_a^{*\dagger} \tilde{\mathcal{P}}_a^* \sigma,
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 \mathcal{L}_{\mathcal{B} \mathcal{B} \mathbb{P}} &= -\frac{g_1}{4 f_\pi} \epsilon^{\alpha\beta\lambda\kappa} \langle \bar{\mathcal{B}} \overleftrightarrow{\partial}_\kappa \gamma_\alpha \gamma_\lambda \partial_\beta \mathbb{P} \mathcal{B} \rangle, \\
 \mathcal{L}_{\mathcal{B} \mathcal{B} \mathbb{V}} &= -i \frac{\beta_S g_V}{2 \sqrt{2}} \langle \bar{\mathcal{B}} \overleftrightarrow{\partial} \cdot \mathbb{V} \mathcal{B} \rangle \\
 &\quad - \frac{i m_{\mathcal{B}} \lambda_S g_V}{3 \sqrt{2}} \langle \bar{\mathcal{B}} \gamma_\mu \gamma_\nu (\partial^\mu \mathbb{V}^\nu - \partial^\nu \mathbb{V}^\mu) \mathcal{B} \rangle, \\
 \mathcal{L}_{\mathcal{B} \mathcal{B} \sigma} &= -\ell_S m_{\mathcal{B}} \langle \bar{\mathcal{B}} \sigma \mathcal{B} \rangle, \\
 \mathcal{L}_{\mathcal{B}^* \mathcal{B}^* \mathbb{P}} &= \frac{-3 g_1}{4 f_\pi} \epsilon^{\alpha\beta\lambda\kappa} \langle \bar{\mathcal{B}}_\alpha^* \overleftrightarrow{\partial}_\kappa \partial_\beta \mathbb{P} \mathcal{B}_\lambda^* \rangle, \\
 \mathcal{L}_{\mathcal{B}^* \mathcal{B}^* \mathbb{V}} &= i \frac{\beta_S g_V}{2 \sqrt{2}} \langle \bar{\mathcal{B}}^{*\mu} \overleftrightarrow{\partial} \cdot \mathbb{V} \mathcal{B}_\mu^* \rangle \\
 &\quad + \frac{i m_{\mathcal{B}^*} \lambda_S g_V}{\sqrt{2}} \langle \bar{\mathcal{B}}_\mu^* (\partial^\mu \mathbb{V}^\nu - \partial^\nu \mathbb{V}^\mu) \mathcal{B}_\nu^* \rangle, \\
 \mathcal{L}_{\mathcal{B}^* \mathcal{B}^* \sigma} &= \ell_S m_{\mathcal{B}^*} \langle \bar{\mathcal{B}}^* \sigma \mathcal{B}^* \rangle, \\
 \mathcal{L}_{\mathcal{B} \mathcal{B}^* \mathbb{P}} &= \frac{\sqrt{3} g_S}{4 f_\pi} \epsilon^{\mu\nu\lambda\kappa} \langle \bar{\mathcal{B}} \partial_\nu \mathbb{P} \overleftrightarrow{\partial}_\kappa \gamma^5 \gamma_\mu \mathcal{B}_\lambda^* - \bar{\mathcal{B}}_\mu^* \partial_\nu \mathbb{P} \overleftrightarrow{\partial}_\kappa \gamma_\lambda \gamma^5 \mathcal{B} \rangle, \\
 \mathcal{L}_{\mathcal{B} \mathcal{B}^* \mathbb{V}} &= \frac{\beta_S g_V}{4 \sqrt{6 m_{\mathcal{B}} m_{\mathcal{B}^*}}} \langle \bar{\mathcal{B}} \overleftrightarrow{\partial} \cdot \mathbb{V} \overleftrightarrow{\partial}^\mu \gamma^5 \mathcal{B}_\mu^* + \bar{\mathcal{B}}_\mu^* \gamma^5 \overleftrightarrow{\partial} \cdot \mathbb{V} \overleftrightarrow{\partial}^\mu \mathcal{B} \rangle \\
 &\quad + \frac{i \lambda_S g_V \sqrt{m_{\mathcal{B}} m_{\mathcal{B}^*}}}{\sqrt{6}} \langle \bar{\mathcal{B}} \gamma^5 (\partial^\mu \mathbb{V}^\nu - \partial^\nu \mathbb{V}^\mu) (\gamma_\nu + \frac{i \overleftrightarrow{\partial}_\nu}{2 \sqrt{m_{\mathcal{B}} m_{\mathcal{B}^*}}}) \mathcal{B}_\mu^* \\
 &\quad - \bar{\mathcal{B}}_\mu^* (\partial^\mu \mathbb{V}^\nu - \partial^\nu \mathbb{V}^\mu) (\gamma_\nu + \frac{i \overleftrightarrow{\partial}_\nu}{2 \sqrt{m_{\mathcal{B}} m_{\mathcal{B}^*}}}) \gamma^5 \mathcal{B} \rangle
 \end{aligned} \tag{3}$$

**Table 1** The parameters and coupling constants adopted in our calculation. The  $\lambda$  and  $\lambda_S$  are in the unit of  $\text{GeV}^{-1}$ . Others are in the unit of 1.

| $\beta$ | $g$  | $g_V$ | $\lambda$ | $g_S$ | $\beta_S$ | $\ell_S$ | $g_1$ | $\lambda_S$ |
|---------|------|-------|-----------|-------|-----------|----------|-------|-------------|
| 0.9     | 0.59 | 5.8   | 0.56      | 0.76  | -1.74     | 6.2      | 0.94  | -3.31       |

# Quasipotential Bethe-Salpeter equation



$$i\mathcal{M}_{\lambda'\lambda}^{JP}(\mathbf{p}', \mathbf{p}) = i\mathcal{V}_{\lambda'\lambda}^{JP}(\mathbf{p}', \mathbf{p}) + \sum_{\lambda'' \geq 0} \int \frac{p''^2 dp''}{(2\pi)^3} \\ \cdot i\mathcal{V}_{\lambda'\lambda''}^{JP}(\mathbf{p}', \mathbf{p}'') G_0(\mathbf{p}'') i\mathcal{M}_{\lambda''\lambda}^{JP}(\mathbf{p}'', \mathbf{p}),$$

$$G_0 = 2\pi i \frac{\delta^+(k_1^2 - m_1^2)}{k_2^2 - m_2^2} \\ = 2\pi i \frac{\delta^+(k_1^0 - E_1(\mathbf{k}))}{2E_1(\mathbf{k})[W - E_1(\mathbf{k})^2 - E_2^2(\mathbf{k})]},$$

$$i\mathcal{V}_{\lambda'\lambda}^{JP}(\mathbf{p}', \mathbf{p}) = 2\pi \int d\cos\theta [d_{\lambda\lambda'}^J(\theta) i\mathcal{V}_{\lambda'\lambda}(\mathbf{p}', \mathbf{p}) \\ + \eta d_{-\lambda\lambda'}^J(\theta) i\mathcal{V}_{\lambda'-\lambda}(\mathbf{p}', \mathbf{p})],$$

- Form factors with cutoff  $\Lambda$  are introduced at the vertex for the offshell particles.

$$f(q^2) = (\Lambda_e^2 - m^2)/(\Lambda_e^2 - q^2), \Lambda_e = m + \alpha \, 0.22 \, \text{GeV} \quad G_0(p) \rightarrow G_0(p) \left[ e^{-(k^2 - m^2)^2 / \Lambda^4} \right]^2$$

# 1/2<sup>-</sup>

**Table 2** The position of the bound states with  $J^P = 1/2^-$  in a unit of MeV. The  $\Lambda$  in the unit of GeV is the cutoff in the exponential regularization in Eq. (9). The *CC* means coupled-channel calculation and  $\Sigma_c \bar{D}^*$  and  $\Sigma_c \bar{D}$  mean the corresponding single-channel calculation.

| $\Lambda$ | $CC(1/2^-)_1$ | $\Sigma_c \bar{D}^*(1/2^-)$ | $CC(1/2^-)_2$ | $\Sigma_c \bar{D}(1/2^-)$ |
|-----------|---------------|-----------------------------|---------------|---------------------------|
| 0.8       | 4448.0        | 4450.8                      | 4320.4        | 4320.3                    |
| 1.0       | 4439.4        | 4444.8                      | 4320.0        | 4319.5                    |
| 1.2       | 4431.7        | 4439.0                      | 4320.1        | 4318.7                    |
| 1.4       | 4425.2        | 4433.9                      | 4320.2        | 4318.0                    |
| 1.6       | 4420.1        | 4429.8                      | 4320.3        | 4317.5                    |
| 1.8       | 4416.4        | 4426.7                      | 4320.5        | 4317.1                    |

$P_c(4440): \Sigma_c \bar{D}^* \left(\frac{1}{2}^-\right)$

$P_c(4312): \Sigma_c \bar{D} \left(\frac{1}{2}^-\right)$

耦合道的影响较小与ChPT的结果一致（见孟璐报告）

# 3/2<sup>-</sup>

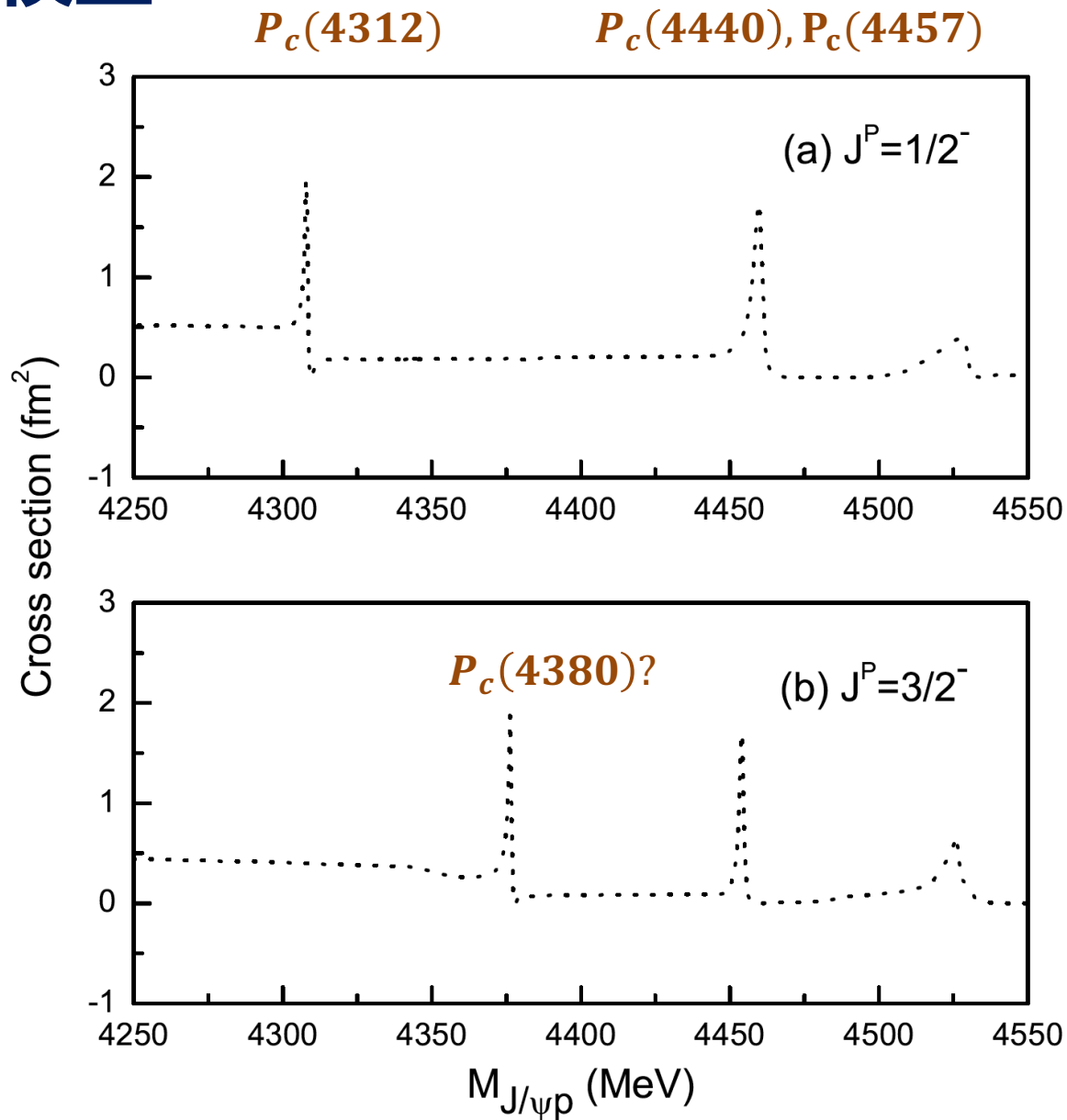
**Table 3** The position of the bound states with  $J^P = 3/2^-$  in a unit of MeV. The  $\Lambda$  in the unit of GeV is the cutoff in the exponential regularization. The *CC* means coupled-channel calculation and  $\Sigma_c \bar{D}^*$  means the single-channel calculation of  $\Sigma_c \bar{D}^*$  interaction.

| $\Lambda$ | $CC(3/2^-)$ | $\Sigma_c \bar{D}^*(3/2^-)$ |
|-----------|-------------|-----------------------------|
| 0.8       | --          | 4462.0                      |
| 1.0       | 4461.7      | 4461.9                      |
| 1.2       | 4461.5      | 4461.7                      |
| 1.4       | 4461.3      | 4461.6                      |
| 1.6       | 4461.1      | 4461.4                      |
| 1.8       | 4460.9      | 4461.3                      |

$$P_c(4457): \Sigma_c \bar{D}^* \left( \frac{3}{2}^- \right)$$

$P_c(4380): \Sigma_c^* \bar{D} \left( \frac{3}{2}^- \right)$  : 有吸引，在散射中有增强。  
如果cutoff变大，会有束缚态出现

# 夸克模型



今天下午Parallel I  
15:10 刘雪杰

Our results support **the molecular state interpretation**:

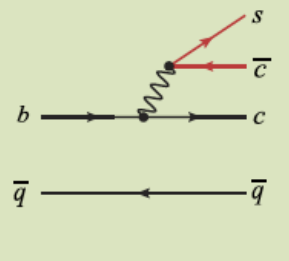
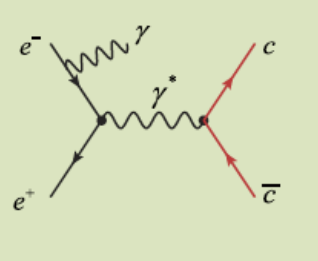
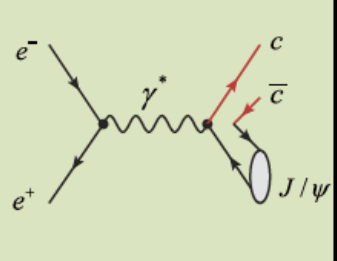
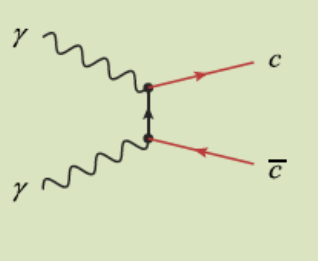
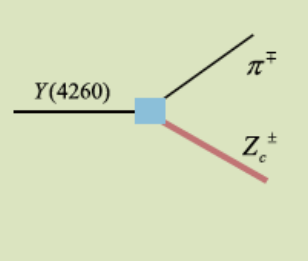
- $P_c(4450): \Sigma_c \bar{D}^* \left( \frac{5}{2}^+ \right) \rightarrow P_c(4440): \Sigma_c \bar{D}^* \left( \frac{1}{2}^- \right), P_c(4457): \Sigma_c \bar{D}^* \left( \frac{3}{2}^- \right),$
- $P_c(4380): \Sigma_c^* \bar{D} \left( \frac{3}{2}^- \right) \rightarrow ? P_c(4380): \Sigma_c^* \bar{D} \left( \frac{3}{2}^- \right),$  attractive, no bound state
- $P_c(4312): \Sigma_c \bar{D} \left( \frac{1}{2}^- \right).$

Other assignments are still not excluded.

Need determination of the spin parities of these  $P_c$  states.

Photo- and pion induced productions  
of  $P_c(4312)$ ,  $P_c(4440)$ ,  $P_c(4457)$

# Observations of the Pc's and XYZ particles

|                                                                                                                                            |                                                                                   |                                                                                    |                                                                                     |                                                                                     |
|--------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|
|                                                           |  |  |  |  |
| $X(3872)$<br>$Y(3940)$<br>$Z^+(4430)$<br>$Z^+(4051)$<br>$Z^+(4248)$<br>$Y(4140)$<br>$Y(4274)$<br>$Z_c^+(4200)$<br>$Z^+(4240)$<br>$X(3823)$ | $Y(4260)$<br>$Y(4008)$<br>$Y(4360)$<br>$Y(4630)$<br>$Y(4660)$                     | $X(3940)$<br>$X(4160)$                                                             | $X(3915)$<br>$X(4350)$<br>$Z(3930)$                                                 | $Z_c(3900)$<br>$Z_c(4025)$<br>$Z_c(4020)$<br>$Z_c(3885)$                            |

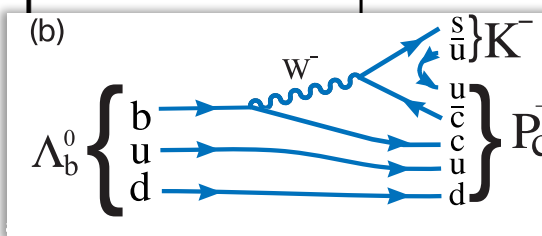
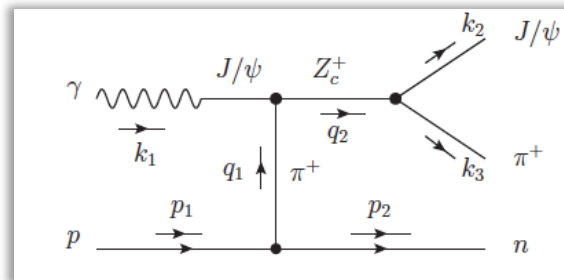
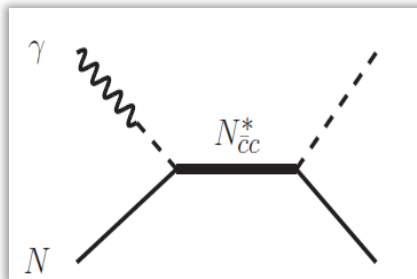
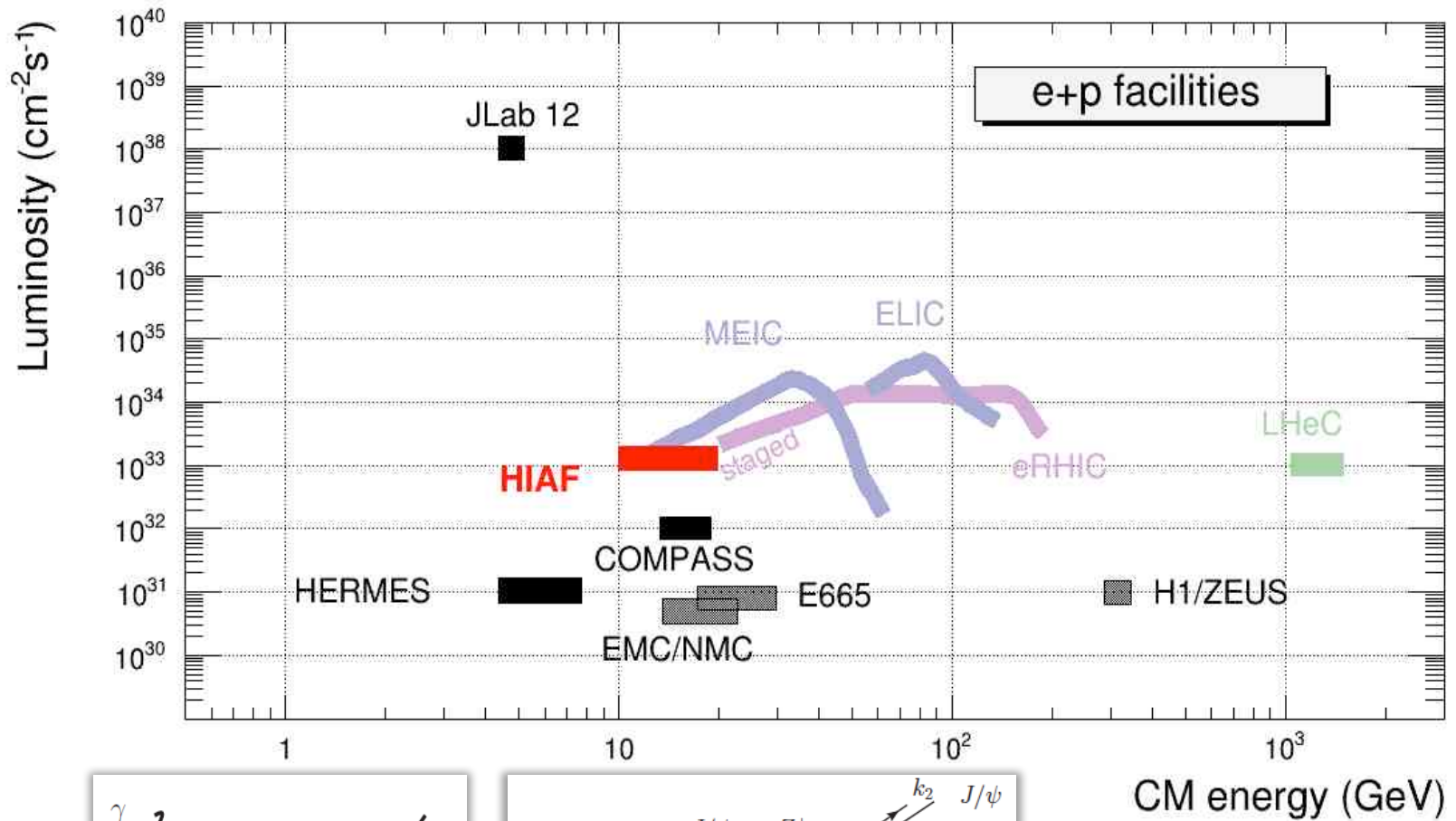


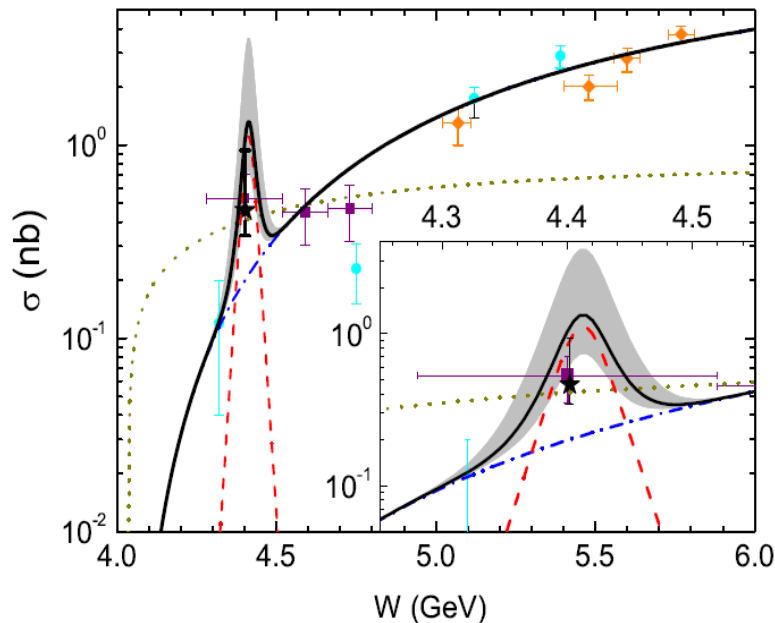
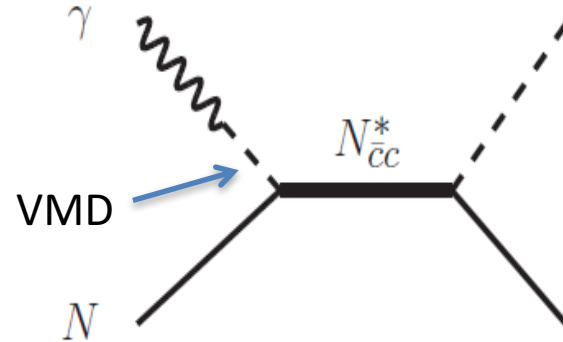
Fig. 2. (Color online) Five groups of the charmonium-like states corresponding to five production mechanisms.

# Photoproduction



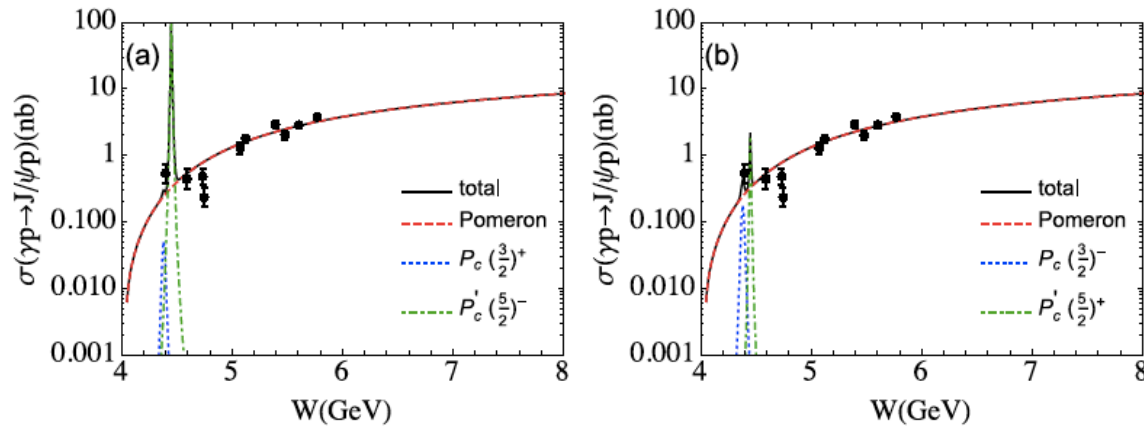
# Prediction before LHCb observation of the hidden-charmed pentaquark

|            | $PB \rightarrow PB$ |      |                        |      |      | $VB \rightarrow VB$ |      |                        |      |      |
|------------|---------------------|------|------------------------|------|------|---------------------|------|------------------------|------|------|
|            | $N_{c\bar{c}}^*$    |      | $\Lambda_{c\bar{c}}^*$ |      |      | $N_{c\bar{c}}^*$    |      | $\Lambda_{c\bar{c}}^*$ |      |      |
| $M$        | 4261                |      | 4209                   | 4394 |      | 4412                |      | 4368                   | 4544 |      |
| $\Gamma$   | 56.9                |      | 32.4                   | 43.3 |      | 47.3                |      | 28.0                   | 36.6 |      |
| $\Gamma_i$ | $\pi N$             | 3.8  | $KN$                   | 15.8 | 0.0  | $\rho N$            | 3.2  | $K^* N$                | 13.9 | 0.0  |
|            | $\eta N$            | 8.1  | $\pi \Sigma$           | 2.9  | 10.6 | $\omega N$          | 10.4 | $\rho \Sigma$          | 3.1  | 8.8  |
|            | $\eta' N$           | 3.9  | $\eta \Lambda$         | 3.2  | 7.1  | $K^* \Sigma$        | 13.7 | $\omega \Lambda$       | 0.3  | 9.1  |
|            | $K \Sigma$          | 17.0 | $\eta' \Lambda$        | 1.7  | 3.3  |                     |      | $\phi \Lambda$         | 4.0  | 0.0  |
|            |                     |      | $K \Xi$                | 2.4  | 5.8  |                     |      | $K^* \Xi$              | 1.8  | 5.0  |
|            | $\eta_c N$          | 23.4 | $\eta_c \Lambda$       | 5.8  | 16.3 | $J/\psi N$          | 19.2 | $J/\psi \Lambda$       | 5.4  | 13.8 |

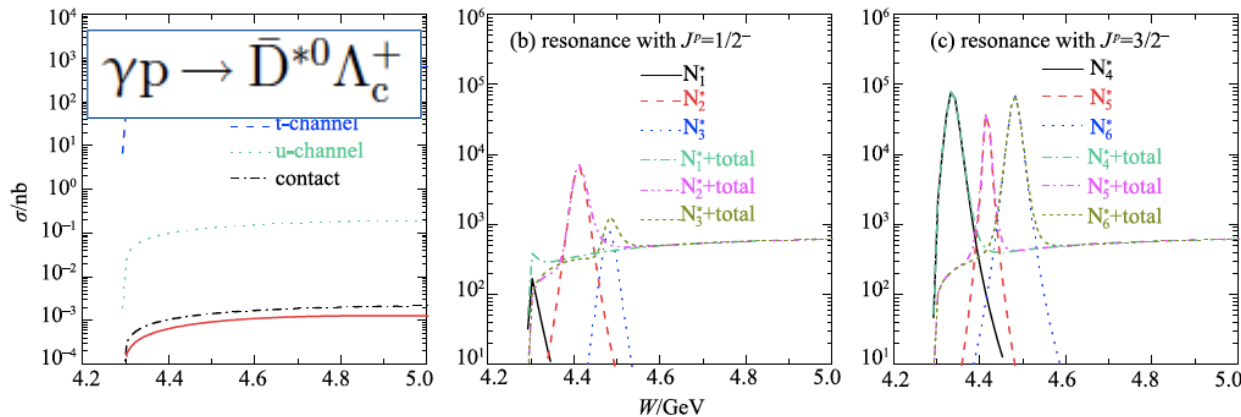


- The cross section of the hidden-charmed  $N^*$  is at order of 0.1 nb
  - The **off-shellness of the  $J/\psi$**  will suppress the cross section heavily because of its large mass
- also adopted in [Wu, Lee, Zou, arXiv:1906.05375]

# Predictions of $P_c(4450)$ and $P_c(4380)$ photoproduction



Wang, Liu, Zhao. Phys. Rev. D92(2015)034022



Huang, Xie, JH, Chen, Zhang, Chinese Physics C, 2016, 40, 124104

Many other works...

**New LHCb results → New predictions**

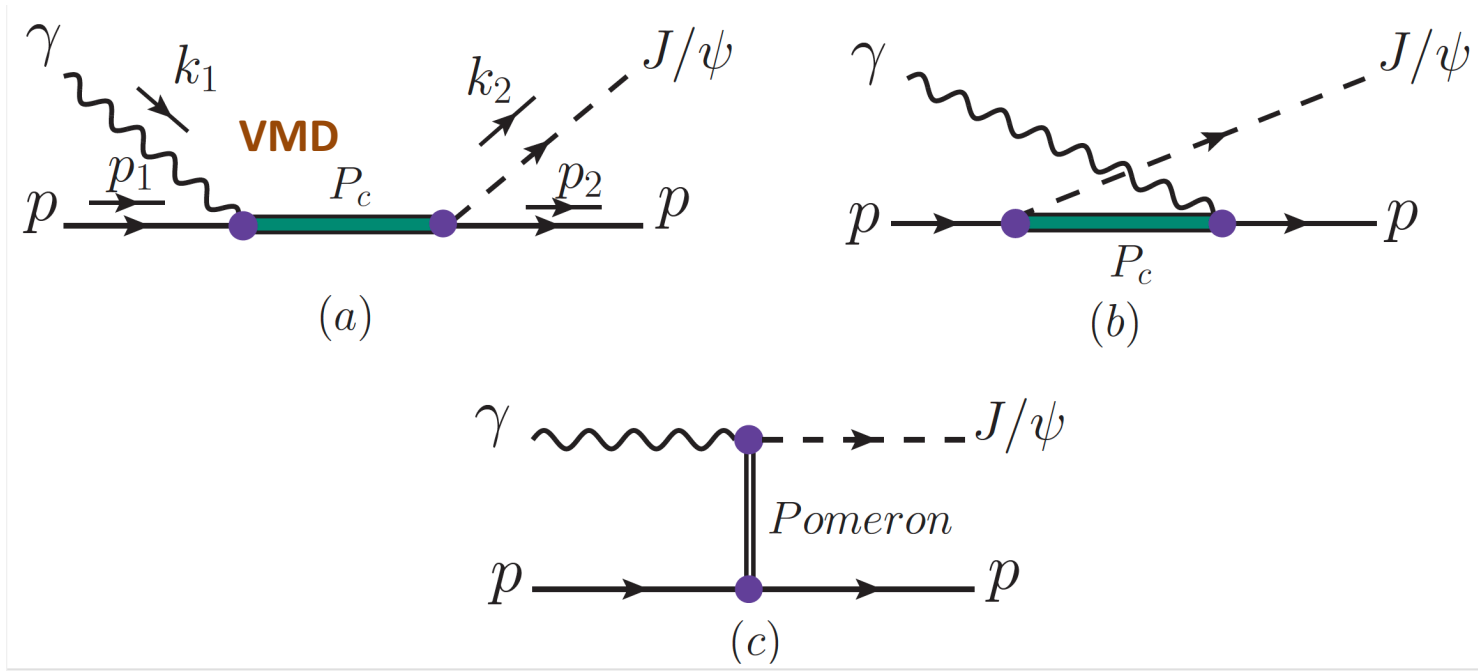
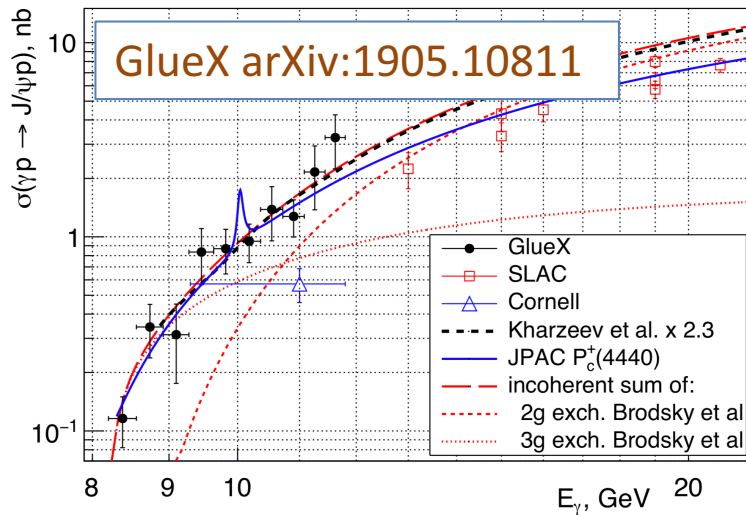
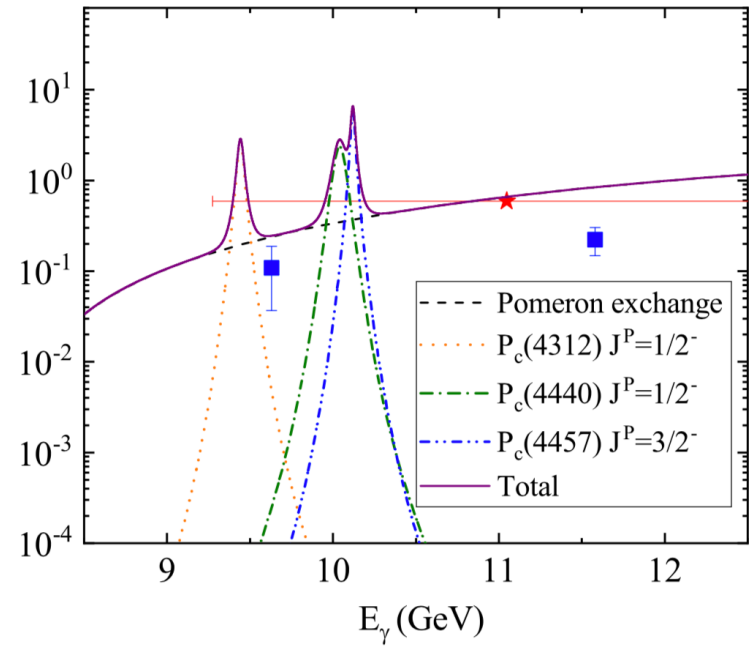
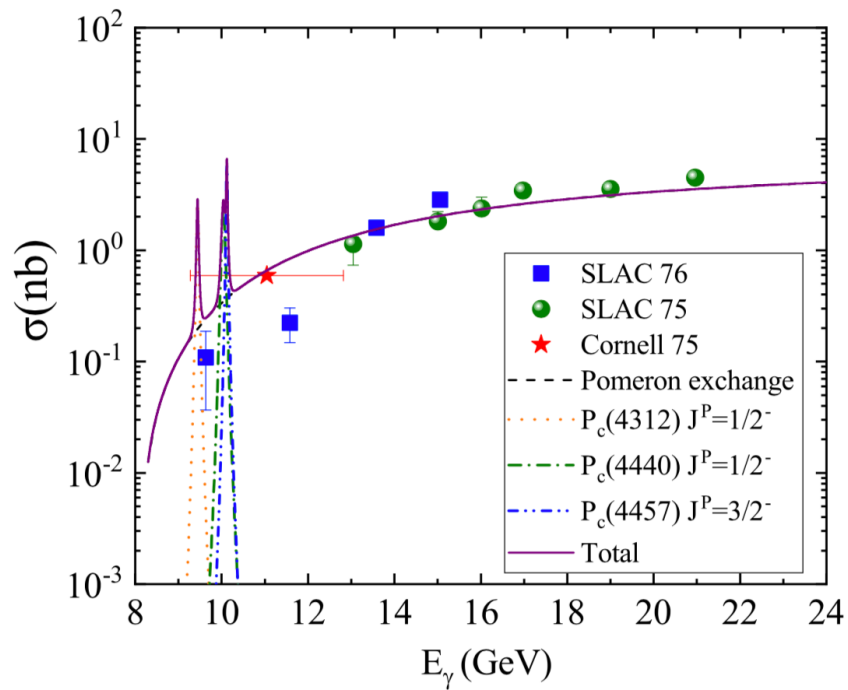


TABLE I. The values of coupling constants by assuming the  $J/\psi p$  channel accounts for 3% of total widths of the  $P_c$  states.

| States                            | $g_{P_c\psi N}$ | $eh$ or $eh_1$ |
|-----------------------------------|-----------------|----------------|
| $P_c(4312) (J^P = \frac{1}{2}^-)$ | 0.06            | 0.0014         |
| $P_c(4440) (J^P = \frac{1}{2}^-)$ | 0.08            | 0.0018         |
| $P_c(4457) (J^P = \frac{3}{2}^-)$ | 0.036           | 0.0008         |

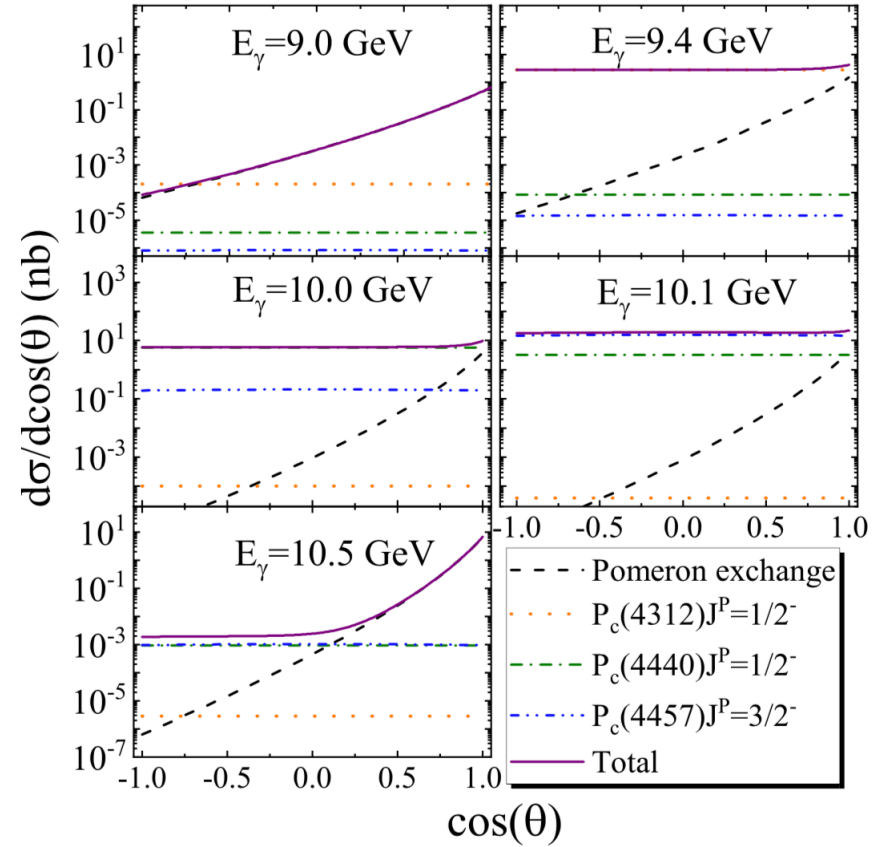
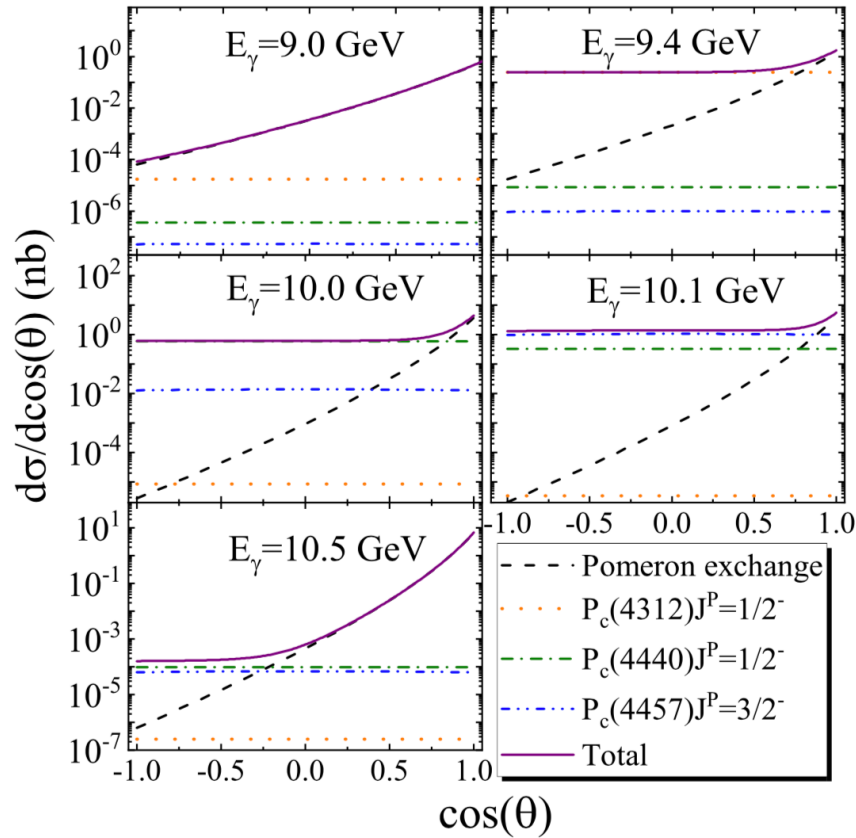


$$Br[P_c \rightarrow J/\psi p] \cong 3\%.$$

Two peaks: 0.1 nb within a bin of 100 MeV

Three peaks: 0.1nb/10 MeV

# Differential cross section



The differential cross sections from the  $P_c$  states are flat due to the spin parities

# Pion-induced production

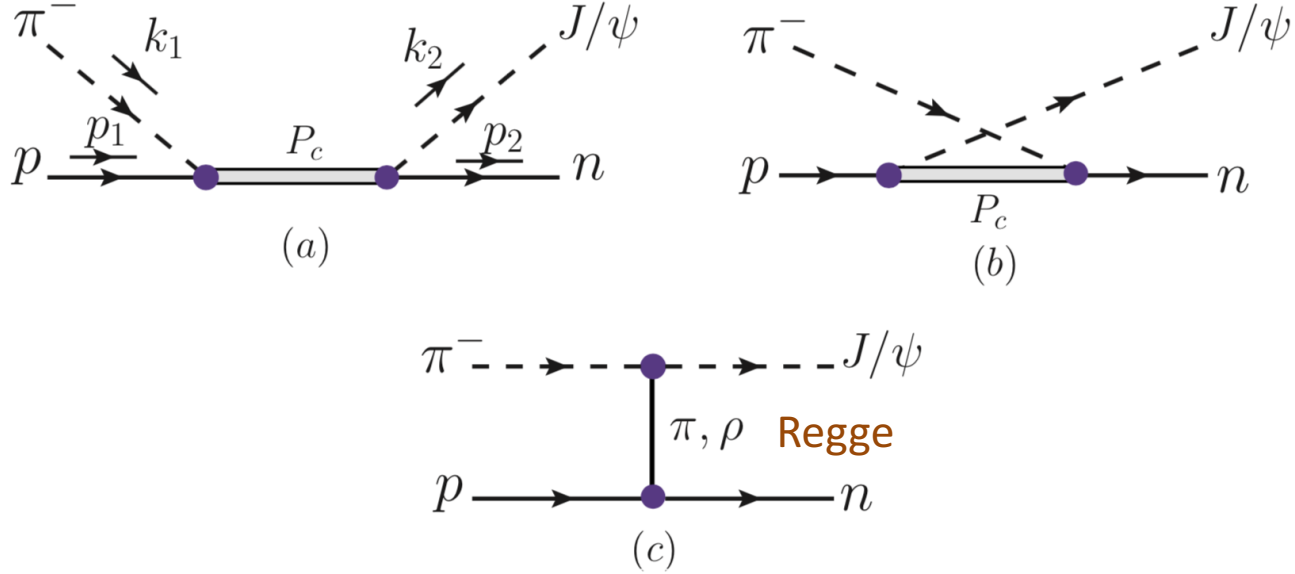
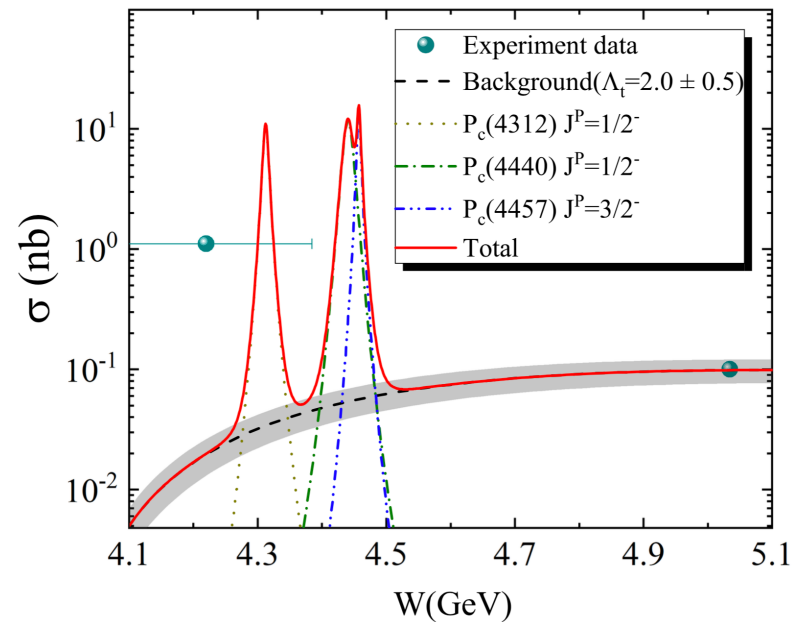
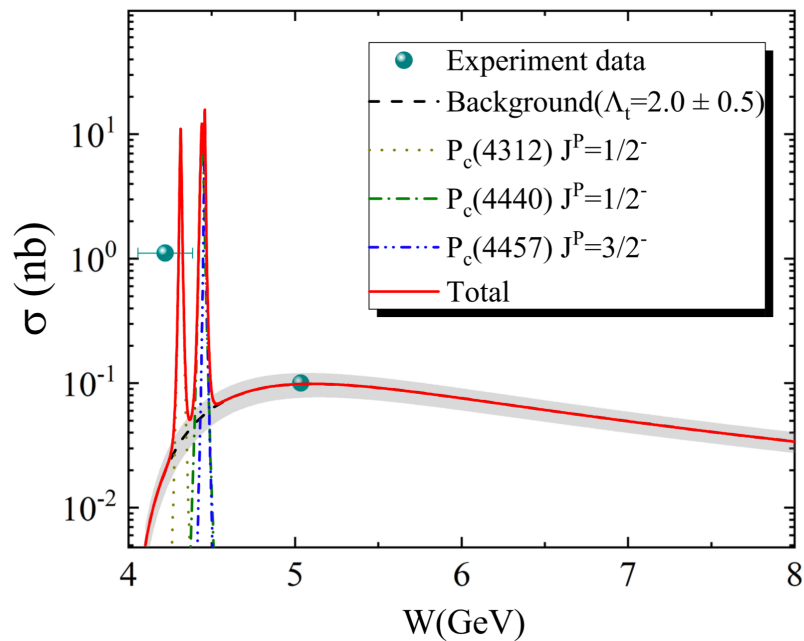


TABLE I. The values of coupling constants by assuming that the  $J/\psi N$  and  $\pi N$  channels account for 3% and 0.05% of total widths of the  $P_c$  states, respectively.

|                 | $P_c(4312)$ | $P_c(4440)$ | $P_c(4457)$ |
|-----------------|-------------|-------------|-------------|
| $g_{P_c\psi N}$ | 0.06        | 0.08        | 0.036       |
| $g_{\pi N P_c}$ | 0.0036      | 0.0053      | 0.0005      |



$Br[P_c \rightarrow J/\psi p] \cong 3\%$  and  $Br[P_c \rightarrow \pi p] \cong 0.05\%$ .

Higher precision is required to distinguish  $P_c(4440)$  and  $P_c(4457)$

# Summary

**LHCb update their results about the hidden-charm pentaquarks.**

Our results support **the molecular state interpretation**:

- $P_c(4450): \Sigma_c \bar{D}^* \left( \frac{5}{2}^+ \right) \rightarrow P_c(4440): \Sigma_c \bar{D}^* \left( \frac{1}{2}^- \right), P_c(4457): \Sigma_c \bar{D}^* \left( \frac{3}{2}^- \right),$
- $P_c(4380): \Sigma_c^* \bar{D} \left( \frac{3}{2}^- \right) \rightarrow P_c(4380)? : \Sigma_c^* \bar{D} \left( \frac{3}{2}^- \right),$  attractive, no bound state
- $P_c(4312): \Sigma_c \bar{D} \left( \frac{1}{2}^- \right).$

Other assignments are still not excluded.

Need determination of the spin parities of these  $P_c$  states.

**The photoproduction and pion-induced productions of the  $P_c$  :**

- Two peaks: 0.1 nb within a bin of 100 MeV
- Three peaks: 0.1nb/10 MeV

谢谢！