

Hidden charm pentaquark states and $\Sigma_c \bar{D}^{(*)}$ interaction in ChPT

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Based on [arXiv:1905.07742](https://arxiv.org/abs/1905.07742) and work in preparation

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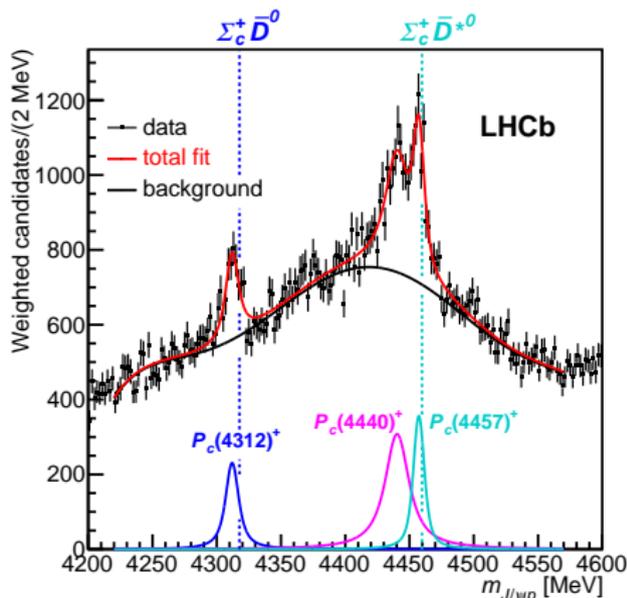
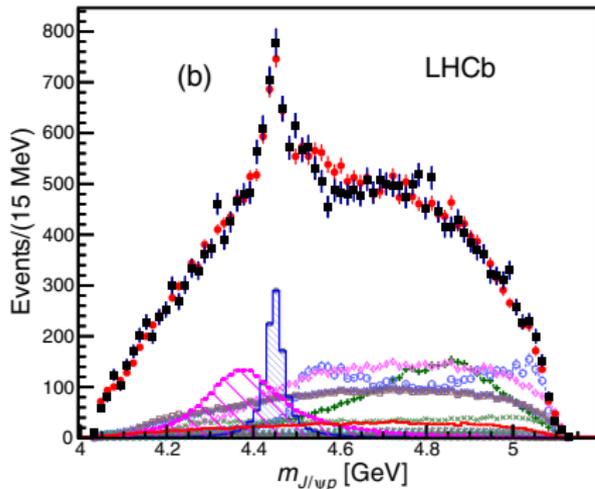
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Introduction

P_c states in LHCb

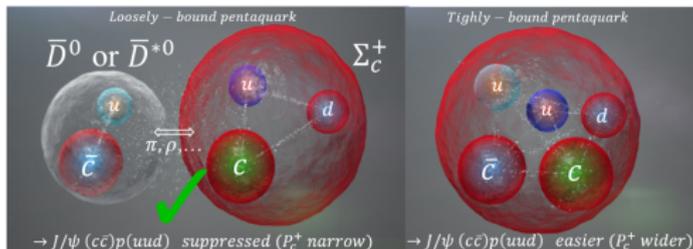
- In 2015, $\Lambda_b \rightarrow J/\psi p K$, $P_c(4380)$ and $P_c(4450)$
- Recently, $P_c(4450) \Rightarrow P_c(4440) + P_c(4457)$; A new state $P_c(4312)$ with 7.3σ ; $I = 1/2$?



Phys.Rev.Lett. 115 (2015) 072001; arXiv:1904.03947;

Compact or molecular states ?

- Compact pentaquark states: tightly bounded states
- Molecular states: loosely bound states of two color singlet hadrons
- The three P_c states under the thresholds 9 MeV, 5 MeV and 22 MeV
- Three P_c states are the good candidates of molecular states
- Our work
 - ⇒ Obtain the $\Sigma_c \bar{D}^{(*)}$ potential in ChPT
 - ⇒ Solve the Schrödinger Eq.



arXiv:1904.03947; arXiv:1903.11013

Chiral perturbation theory

- QCD Lagrangian

$$\mathcal{L}_{QCD} = \sum_f \bar{q}_f (i\not{D} - \mathcal{M}q_f) - \frac{1}{4} G_{\mu\nu}^a G^{\mu\nu,a}$$

$$f = (u, d, s, c, b, t),$$

$$\mathcal{M} = \text{diag}(m_u, m_d, m_s, m_c, m_b, m_t)$$



S.Weinberg

- two approximate symmetry: chiral symmetry and heavy quark symmetry

$$m_u, m_d, m_s \ll 1\text{GeV}, \quad m_c, m_b \gg \Lambda_{QCD} \quad (1)$$

- Chiral perturbation theory (ChPT) and heavy quark effective theory (HQET)
- $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V \Rightarrow 8$ Goldstone bosons
- Quark masses break the chiral symmetry explicitly: $m_\pi^2 \sim m_q$
- Freedom: Goldstone bosons and matter fields, e.g. N , D and Σ_c
- Expansion ϵ/Λ_χ , $\Lambda_\chi \approx 4\pi F_\pi \approx m_\rho$
 $\epsilon : m_\pi$, momentum of pion and residue momentum of matter fields

Why Chiral perturbation theory (ChPT)?

- Effective theory, model independence
- Systematically expansion, controllable and estimable error
- Loop diagrams
- Lattice QCD: chiral extrapolation
- Modern theory of nucleon force Phys. Rept. 503, 1 (2011).; Rev. Mod. Phys. 81, 1773 (2009).

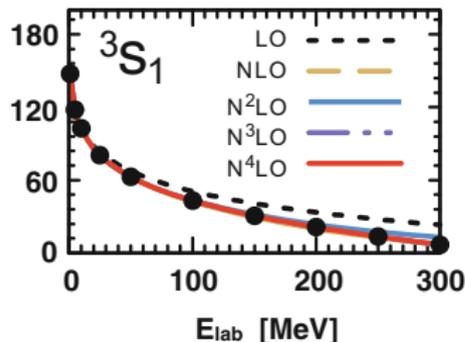
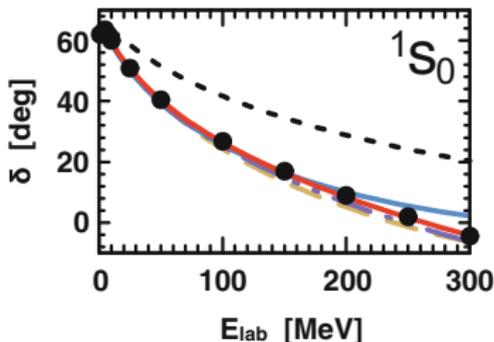
HEP

找到 1 笔记录

1. **Observation of a narrow pentaquark state**,
LHCb Collaboration (Roel Aaij (NIKHEF, Amsterdam) et al.)
Published in **Phys.Rev.Lett.** **122** (2019) no.22, 22200
LHCb-PAPER-2019-014 CERN-EP-2019-058
DOI: [10.1103/PhysRevLett.122.222001](https://doi.org/10.1103/PhysRevLett.122.222001)
e-Print: [arXiv:1904.03947](https://arxiv.org/abs/1904.03947) [hep-ex] | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [CERN Document Server](#); [ADS Abstract Service](#);
Data: [INSPIRE](#) | [HepData](#)

[详细记录](#) - Cited by 37 records

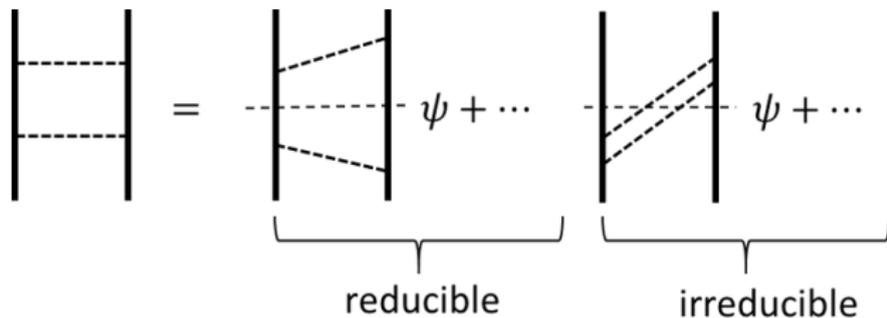


$\Sigma_c \bar{D}^{(*)}$ **interaction in ChPT**

Weinberg's formalism

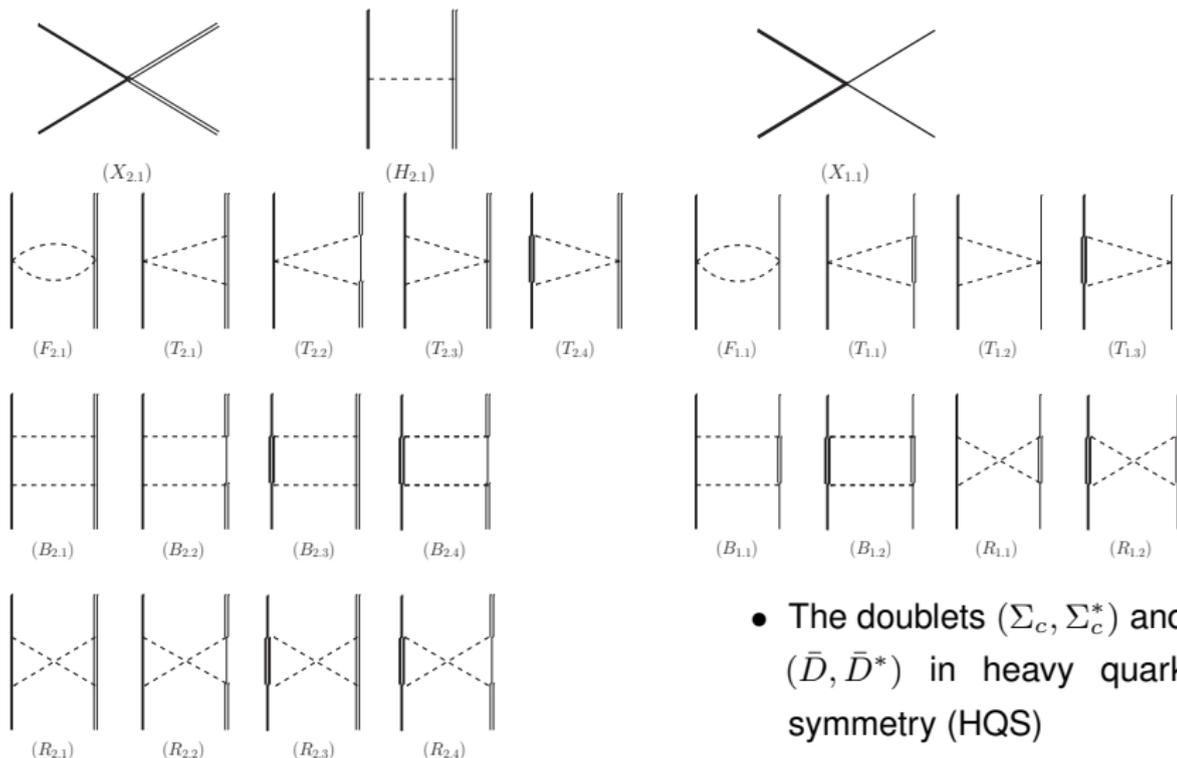
- Enhanced by pinch singularity, two nucleon on-shell, power count fails
- Time-ordered perturbation theory

$$Amp = \langle NN | H_I | NN \rangle + \sum_{\psi} \frac{\langle NN | H_I | \psi \rangle \langle H_I | NN \rangle}{E_{NN} - E_{\psi}} \quad (2)$$



- Only include the two particle irreducible (2PIR) graphs in potential
- Potential as the kernel of Lippmann-Schwinger Eq. or Schrödinger Eq.
- The tree level one-pion exchange diagrams would be iterated to generate the 2PR contributions automatically

Feynman diagrams of $\Sigma_c \bar{D}^{(*)}$ to NLO

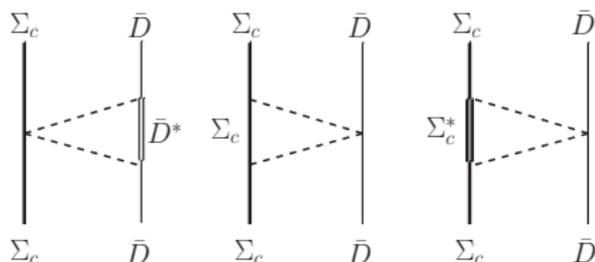
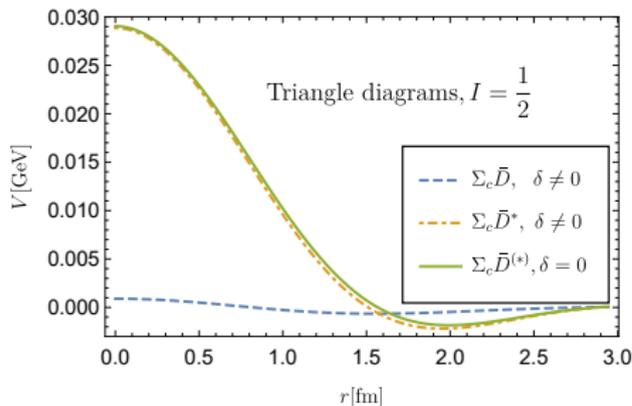


- The doublets (Σ_c, Σ_c^*) and (\bar{D}, \bar{D}^*) in heavy quark symmetry (HQS)

- All intermediate states, keep mass splitting, HQS violation
- Unknown low energy constants (LECs): contact terms

Heavy quark symmetry: violation

- $\Lambda_{QCD}/m_c \simeq 0.2$, the HQS violation is sizable
- HQS with guidance for compact systems, (Σ_c^*, Σ_c) (2518,2454) MeV
- HQS violation effect is more significant for the $\Sigma_c \bar{D}$ system than $\Sigma_c \bar{D}^*$



- Minimum of potential with the loosely bound state: -0.06-0.15 GeV.

It may be misleading to adopt the HQS to calculate the molecular states.

Heavy quark symmetry: quark model

- The heavy dof.: spectators; light dof.: interactions

$$V_{\text{quark-level}} = \left[V_a + \tilde{V}_a \mathbf{l}_1 \cdot \mathbf{l}_2 \right] + \left[\frac{V_c}{m_c} \mathbf{l}_1 \cdot \mathbf{h}_2 + \frac{V_d}{m_c} \mathbf{l}_2 \cdot \mathbf{h}_1 + \frac{V_e}{m_c^2} \mathbf{h}_1 \cdot \mathbf{h}_2 \right],$$
$$V_{\Sigma_c \bar{D}} = V_1, \quad V_{\Sigma_c \bar{D}^*} = V_2 + \tilde{V}_2 \mathbf{S}_1 \cdot \mathbf{S}_2,$$
$$V_{\Sigma_c^* \bar{D}} = V_3, \quad V_{\Sigma_c^* \bar{D}^*} = V_4 + \tilde{V}_4 \mathbf{S}_1 \cdot \mathbf{S}_2. \quad (3)$$

- Ignoring mass splittings in loops, the HQS manifests itself

M. Z. Liu, et.al arXiv:1903.11560 [hep-ph].

- In QM, the HQS violation vanishes for $\Sigma_c \bar{D}$ system

$$\langle \mathbf{l}_1 \cdot \mathbf{h}_2 \rangle = \langle \mathbf{l}_2 \cdot \mathbf{h}_1 \rangle = \langle \mathbf{h}_1 \cdot \mathbf{h}_2 \rangle = 0 \quad (4)$$

- QM: analytical terms; Loop diagrams: nonanalytical structures
- Another eg. enhancement of isospin violation in loop diagrams

F. K. Guo, H. J. Jing, U. G. Meißner and S. Sakai, Phys. Rev. D 99, no. 9, 091501 (2019).

Loops bring novel effects.

Numerical results

Contact terms

$$\mathcal{V}_{\Sigma_c \bar{D}}^{X_{1,1}} = -D_1 - \tilde{D}_1(2\mathbf{I}_1 \cdot \mathbf{I}_2), \quad (5)$$

$$\mathcal{V}_{\Sigma_c \bar{D}^*}^{X_{2,1}} = -\left(D_1 + \frac{1}{3}D_2\boldsymbol{\sigma} \cdot \mathbf{T}\right) - \left(\tilde{D}_1 + \frac{1}{3}\tilde{D}_2\boldsymbol{\sigma} \cdot \mathbf{T}\right)(2\mathbf{I}_1 \cdot \mathbf{I}_2),$$

- Package heavy mesons exchanged interaction like ρ and ω
- Renormalization
 - ⇒ absorb the divergence in the loops
 - ⇒ remove the scale dependence.
- Contact or pion-exchange? depend on regularization schemes

Phys. Rev. D91, 034002 (2015).

- Depend on chiral truncation order; types of regulator and values of cutoff

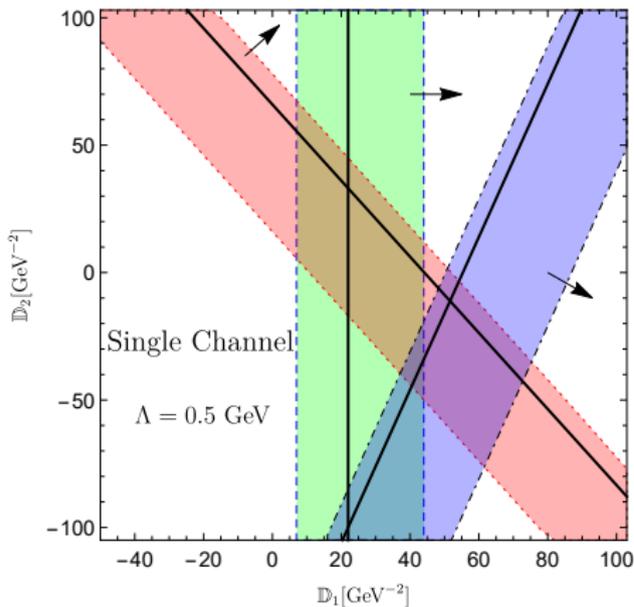
Phys. Rept. 503, 1 (2011).

- Dimensional regularization, \overline{MS} -scheme, $\Lambda_\chi = 1.0$ GeV; Gaussian regulator $\Lambda=0.5$ GeV

$$V(r) = \frac{1}{(2\pi)^3} \int d^3\mathbf{q} e^{i\mathbf{q}\cdot\mathbf{r}} \mathcal{V}(\mathbf{q}) \mathcal{F}(\mathbf{q}), \quad \mathcal{F}(\mathbf{q}) = \exp(-\mathbf{q}^{2n}/\Lambda^{2n}) \quad (6)$$

Scenario II: single channel

$$\text{For } I = 1/2, \quad \mathcal{V}_{\Sigma_c \bar{D}}^{X_{1,1}} = -\mathbb{D}_1, \quad \mathcal{V}_{\Sigma_c^* \bar{D}}^{X_{2,1}} = -(\mathbb{D}_1 + \frac{1}{3}\mathbb{D}_2 \boldsymbol{\sigma} \cdot \mathbf{T}) \quad (7)$$



- There is a very **SMALL** region where three states coexist as the molecular states
- Restricting the binding energy in exp., it is hard to reproduce three states as molecules simultaneously

$$\langle \boldsymbol{\sigma} \cdot \mathbf{T} \rangle = \begin{cases} 2 & J = 1/2 \\ -1 & J = 3/2 \end{cases}$$

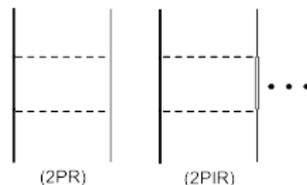
Spin-Spin interaction is an obstacle.

Scenario III: couple channel

Single Channel



one-pion exchange

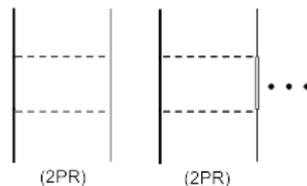


two-pion exchange

Couple Channel



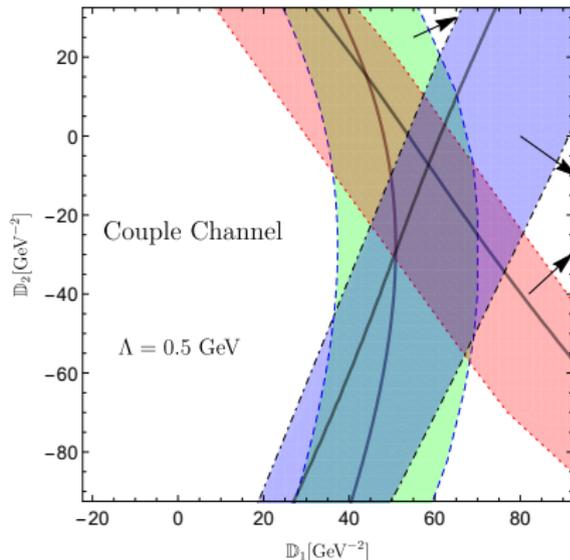
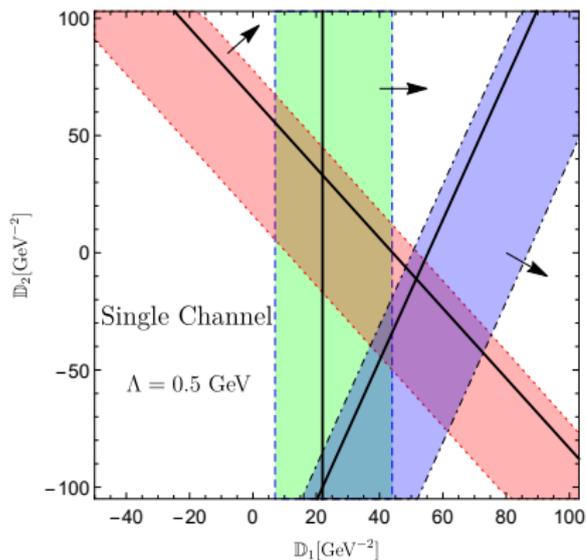
one-pion exchange



two-pion exchange

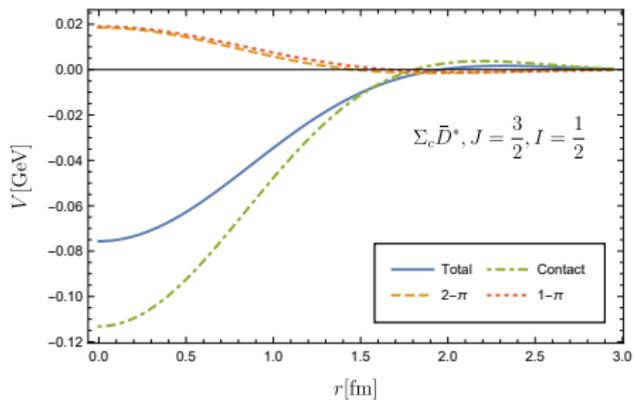
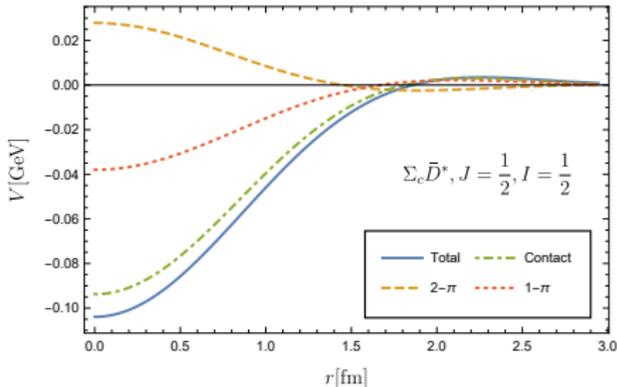
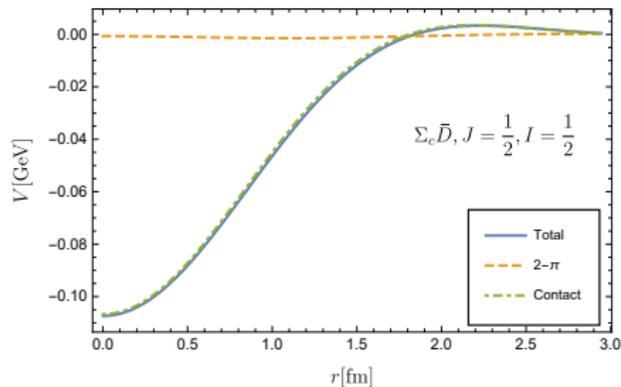
Channel	1	2	3	4
$J = \frac{1}{2}$	$\Sigma_c \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$	$\Sigma_c^* \bar{D}$
$J = \frac{3}{2}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}$	$\Sigma_c^* \bar{D}^*$	

Scenario III: couple channel



S-III	Exp.(MeV)	Mass(MeV)	RMS(fm)	P_1 (%)	P_2 (%)	P_3 (%)
$P_c(4312)$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	4305	1.21	99.4	0.5	0.1
$P_c(4440)$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	4446	1.22	1.0	98.0	0.9
$P_c(4457)$	$4457.3 \pm 1.3^{+0.6}_{-4.1}$	4458	1.28	96.8	2.5	0.7

Scenario III: couple channel



- Reproduce the three P_c states as molecular states simultaneously
- Attraction mainly stems from the contact interaction
- The couple channel effect is important
- Minimum of potential

Summary and Outlook

Summary and Outlook

- $\Sigma_c \bar{D}^{(*)}$ potential in ChPT to NLO
 - ⇒ contact, $1 - \pi$, $2 - \pi$
 - ⇒ HQS breaking effect, **IMPORTANT !**
 - ⇒ Couple channel effect
 - ⇒ Reproduce three P_c states simultaneously as molecular states

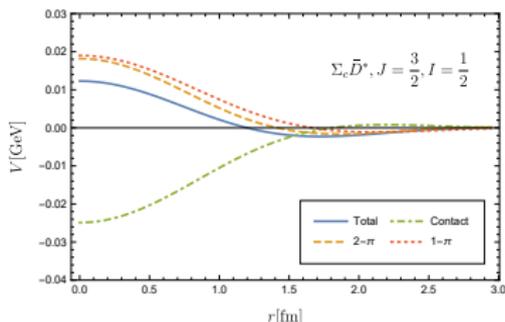
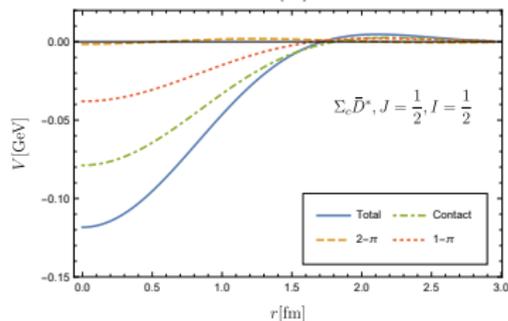
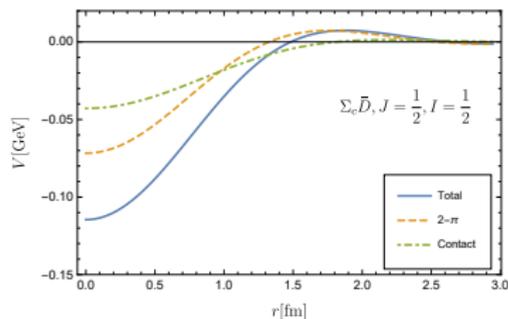
- Outlook
 - ⇒ Lattice QCD simulation on $\Sigma_c \bar{D}^{(*)}$ potential is called for
 - ⇒ Chiral extrapolation
 - ⇒ Three P_c states are HQSS partner states, more HQSS and HQFS partner states in molecular scheme? [1903.11560](#); [1904.01296...](#)
 - ⇒ HQS breaking effect? $\Sigma_c^* \bar{D}^{(*)}$ and $\Sigma_c^{(*)} D^{(*)}$ system (on-going)
 - ⇒ Test the ChPT in the charm sector
 - for chiral dynamics, $c(qq)_{s=1}^{I=1} = \Sigma_c + \Sigma_c^*$*

Thanks for your attention!

Scenario I: model

$$\mathcal{L}_{\text{quark}} = -\frac{1}{2}c_s \bar{q}q\bar{q}q - \frac{1}{2}c_t(\bar{q}\boldsymbol{\sigma}q) \cdot (\bar{q}\boldsymbol{\sigma}q), \quad (8)$$

$$\text{For } I = 1/2, \quad \mathcal{V}_{\Sigma_c \bar{D}}^{X_{1.1}} = -\mathbb{D}_1, \quad \mathcal{V}_{\Sigma_c^* \bar{D}}^{X_{2.1}} = -\left(\mathbb{D}_1 + \frac{1}{3}\mathbb{D}_2 \boldsymbol{\sigma} \cdot \mathbf{T}\right) \quad (9)$$

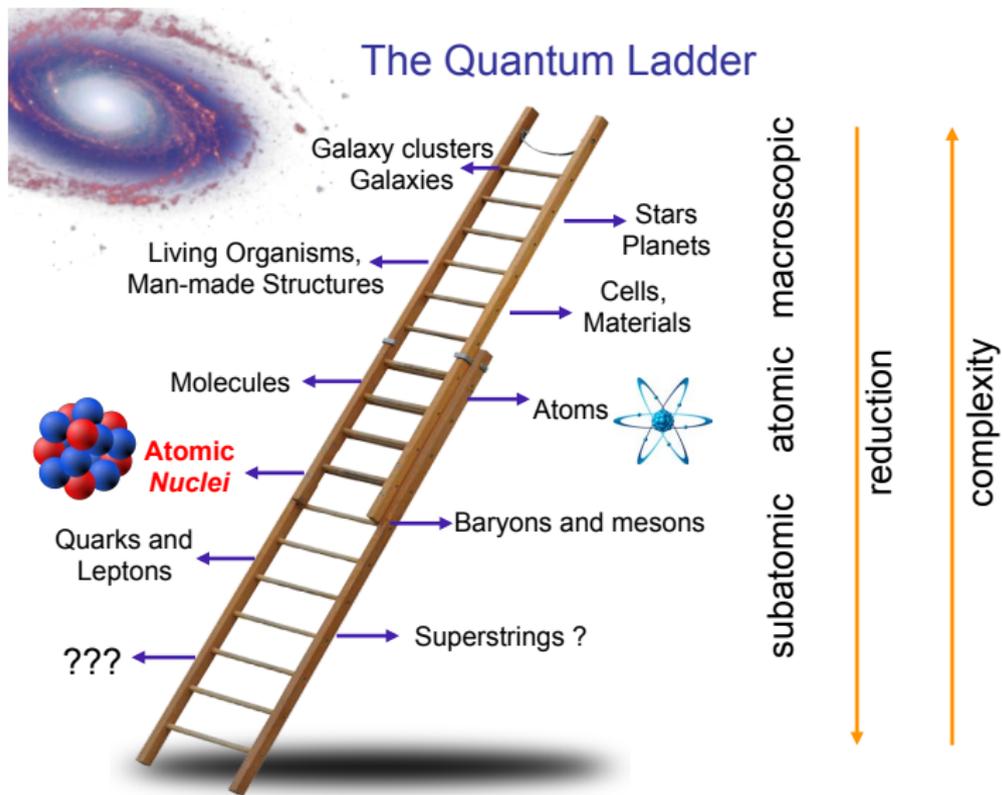


$$[\Sigma_c \bar{D}]_{J=1/2}^{I=1/2} : E = -9.21 \text{ MeV}$$

$$[\Sigma_c \bar{D}^*]_{J=1/2}^{I=1/2} : E = -18.93 \text{ MeV}$$

$$[\Sigma_c \bar{D}^*]_{J=3/2}^{I=1/2} : \text{No bound states}$$

Physics at the different scales never talk to each other



Effective field theory

- An effective field theory (EFT) is a low-energy approximation to some underlying, more fundamental theory.
⇒ Large energy scale Λ
- The EFT Lagrangian: the most general Lagrangian with **SYMMETRIES** of the underlying theory.
⇒ Low-energy constants (LECs)
- Expand the theory in powers of p/Λ
⇒ Power counting law

$$\mathcal{M} = \sum_{\nu} \left(\frac{Q}{\Lambda} \right)^{\nu} f(Q/\mu, g_i) \quad (10)$$

- Calculate and renormalize order-by-order
- Controllable and estimable error
- Prediction: experiment data as input



S. Weinberg

Go for the messes - that's where
the action is. *Physica A96 (1979) 327-340*

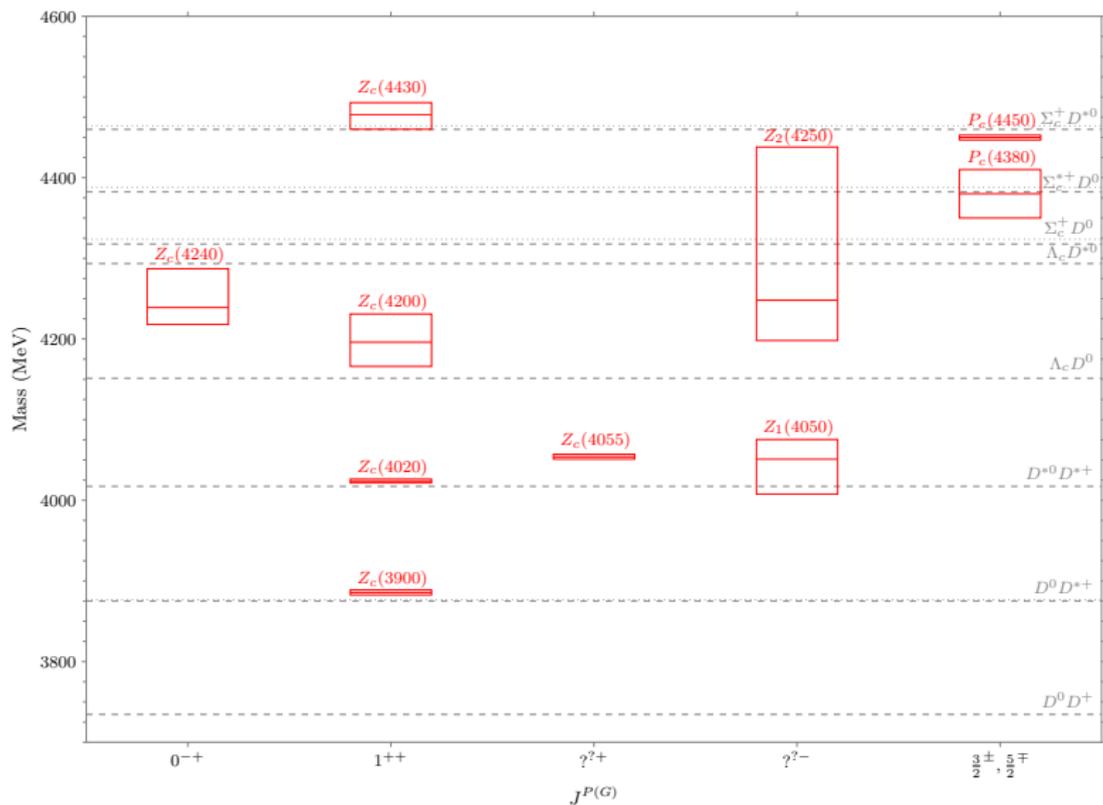
Contact terms of NN

C_S	C_T	Λ , channel	C_S	C_T	Λ , channel
Ordonez:1995rz			Epelbaum:2004fk		
112	13.5	$I = 0$	-107.57	-11.64	$\{0.45, 0.5\}, np$
-26.6	-68.9	$I = 1$	88.61	53.20	$\{0.6, 0.5\}, np$
Machleidt:2011zz			-121.08	-6.17	$\{0.45, 0.7\}, np$
-100.28	5.61	$\Lambda = 0.5, np$	33.70	25.66	$\{0.6, 0.7\}, np$
-99.55	7.07	$\Lambda = 0.6, np$			

$$\mathcal{L}_{NN}^{(0)} = -\frac{1}{2}C_S \bar{N}N \bar{N}N - \frac{1}{2}C_T \bar{N}\boldsymbol{\sigma}N \cdot \bar{N}\boldsymbol{\sigma}N, \quad (11)$$

$$\mathcal{V}_{NN} = C_S + C_T \boldsymbol{\sigma} \cdot \boldsymbol{\sigma}. \quad (12)$$

XYZ states



Spontaneous symmetry breaking

- Chiral symmetry: Conservation charge Q_A^a

$$H_{QCD}^0|i, +\rangle = E_i|i, +\rangle, \quad P|i, +\rangle = +|i, +\rangle, \quad |\phi\rangle = Q_A^a|i, +\rangle \quad (13)$$

$$H_{QCD}^0|\phi\rangle = E_i|\phi\rangle, \quad P|\phi\rangle = -|\phi\rangle \quad (14)$$

- Degenerate states with different parity? \rightarrow SSB
- Goldstone's theorem: spontaneous breaking of continuous global symmetries implies the existence of massless particles.
- NO. of Goldstone boson $= n_G - n_H$
 G : symmetry group of Lagrangian;
 H : the subgroup leaves the ground state invariant after SSB
- $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V \Rightarrow 8$ Goldstone bosons
- Quark masses break the chiral symmetry explicitly: $m_\pi^2 \sim m_q$

$$V \sim \int \frac{d^d \lambda^{4-d}}{(2\pi)^d} \frac{1}{-v \cdot l + i\epsilon} \frac{1}{v \cdot l + i\epsilon} \frac{1}{l^2 - m_1^2 + i\epsilon} \frac{1}{(l+q)^2 - m_2^2 + i\epsilon} \quad (15)$$

$$\sim \int \frac{d^d \lambda^{4-d}}{(2\pi)^d} \frac{1}{-l^0 + i\epsilon} \frac{1}{l^0 + i\epsilon} \frac{1}{l^{02} - \omega_1^2 + i\epsilon} \frac{1}{l^{02} - \omega_2^2 + i\epsilon} \quad (16)$$

$$\frac{1}{-v \cdot l + i\epsilon} \frac{1}{v \cdot l + i\epsilon} \rightarrow \frac{1}{-v \cdot l - \frac{l^2}{2M_1} + i\epsilon} \frac{1}{v \cdot l - \frac{l^2}{2M_2} + i\epsilon} \quad (17)$$

$$\int dl^0 \frac{f(l^0)}{-l^0 - \frac{l^2}{2M_1} + i\epsilon} \frac{1}{l^0 - \frac{l^2}{2M_2} + i\epsilon} \quad (18)$$

$$\sim \frac{f(\frac{l^2}{2M_2})}{-\frac{l^2}{2M_2} - \frac{l^2}{2M_1}} \sim f \frac{M}{l^2} \quad (19)$$

power counting: $\frac{1}{l}$, our calculation $\frac{M}{l^2}$

The Lagrangians

$$\Sigma_c = \begin{pmatrix} \Sigma_c^{++} & \frac{\Sigma_c^+}{\sqrt{2}} \\ \frac{\Sigma_c^+}{\sqrt{2}} & \Sigma_c^0 \end{pmatrix}, \quad \Sigma_c^{*\mu} = \begin{pmatrix} \Sigma_c^{*++} & \frac{\Sigma_c^{*+}}{\sqrt{2}} \\ \frac{\Sigma_c^{*+}}{\sqrt{2}} & \Sigma_c^{*0} \end{pmatrix}^{\mu}, \quad (20)$$

$$\tilde{P} = \begin{pmatrix} \bar{D}^0 \\ \bar{D}^- \end{pmatrix}, \quad \tilde{P}^{*\mu} = \begin{pmatrix} \bar{D}^{*0} \\ \bar{D}^{*-} \end{pmatrix}, \quad (21)$$

$$\psi^\mu = \mathcal{B}^{*\mu} - \sqrt{\frac{1}{3}}(\gamma^\mu + v^\mu)\gamma^5\mathcal{B},$$

$$\tilde{H} = (\tilde{P}_\mu^*\gamma^\mu + i\tilde{P}\gamma_5)\frac{1-\not{v}}{2} \quad (22)$$

$$\mathcal{L}_{\Sigma_c\phi}^{(0)} = -\text{Tr}[\bar{\psi}^\mu i v \cdot D\psi_\mu] + ig_a \epsilon_{\mu\nu\rho\sigma} \text{Tr}[\bar{\psi}^\mu u^\rho v^\sigma \psi^\nu] + i\frac{\delta_a}{2} \text{Tr}[\bar{\psi}^\mu \sigma_{\mu\nu} \psi^\nu].$$

$$\mathcal{L}_{\bar{D}\phi}^{(0)} = -i\langle \bar{H}v \cdot D\tilde{H} \rangle + g_b \langle \bar{H}u_\mu \gamma^\mu \gamma_5 \tilde{H} \rangle - \frac{\delta_b}{8} \langle \bar{H}\sigma^{\mu\nu} \tilde{H}\sigma_{\mu\nu} \rangle, \quad (23)$$

Building Block

- building block

	$D_\mu \psi$	ψ	$\bar{\psi}$	χ_\pm	$f_{\mu\nu}^\pm$	u_μ	Γ_μ
CH	$K D_\mu \psi$	$K \psi$	$\bar{\psi} K^\dagger$	$K \chi_\pm K^\dagger$	$K f_{\mu\nu}^\pm K^\dagger$	$K u_\mu K^\dagger$	$K \Gamma^\mu K^\dagger - \partial^\mu K K^\dagger$
P	$\gamma^0 D^\mu \psi$	$\gamma^0 \psi$	$\bar{\psi} \gamma^0$	$\pm \chi_\pm$	$\pm f^{\pm\mu\nu}$	$-u^\mu$	Γ^μ
C	$C D'_\mu \bar{\psi}^T$	$C \bar{\psi}^T$	$\psi^T C$	χ_\pm^T	$\mp (f_{\mu\nu}^\pm)$	$(u_\mu)^T$	$-(\Gamma_\mu)^T$

$$F_{\mu\nu}^\pm = u^\dagger F_{\mu\nu}^R u \pm u F_{\mu\nu}^L u^\dagger,$$

$$F_{\mu\nu}^R = \partial_\mu r_\nu - \partial_\nu r_\mu - i[r_\mu, r_\nu], \quad (24)$$

$$F_{\mu\nu}^L = \partial_\mu l_\nu - \partial_\nu l_\mu - i[l_\mu, l_\nu]. \quad (25)$$

$$\Gamma_\mu = \frac{1}{2} \left[u^\dagger (\partial_\mu - i r_\mu) u + u (\partial_\mu - i l_\mu) u^\dagger \right], \quad (26)$$

$$u_\mu \equiv \frac{1}{2} i \left[u^\dagger (\partial_\mu - i r_\mu) u - u (\partial_\mu - i l_\mu) u^\dagger \right], \quad (27)$$

$$\chi = 2B_0(s + ip), \quad \chi_\pm = u^\dagger \chi u^\dagger \pm u \chi^\dagger u \quad (28)$$

Effective field theory

- An effective field theory (EFT) is a low-energy approximation to some underlying, more fundamental theory.
⇒ Large energy scale Λ
- The EFT Lagrangian: the most general Lagrangian with the symmetries of the underlying theory.
⇒ Low-energy constants (LECs)
- Expand the theory in powers of p/Λ
⇒ Power counting law
- Calculate and renormalize order-by-order
- Prediction: experiment data as input

Chiral Symmetry

- $m_u, m_d, m_s \ll 1\text{GeV} \leq m_c, m_b, m_t$; Chiral limit: $m_u, m_d, m_s = 0$
- The QCD Lagrangian in the chiral limit can then be written as

$$\mathcal{L}_{QCD}^0 = \sum_{l=u,d,s} (\bar{q}_{R,l} i \not{D} q_{R,l} + \bar{q}_{L,l} i \not{D} q_{L,l}) - \frac{1}{4} \mathcal{G}_{\mu\nu,a} \mathcal{G}_a^{\mu\nu}. \quad (29)$$

where $P_{R,L} = \frac{1}{2}(1 \pm \gamma_5)$

- Chiral symmetry $SU(3)_L \times SU(3)_R \times U(1)_L \times U(1)_R$

$$\begin{aligned} \begin{pmatrix} u_L \\ d_L \\ s_L \end{pmatrix} &\mapsto U_L \begin{pmatrix} u_L \\ d_L \\ s_L \end{pmatrix} = \exp\left(-i \sum_{a=1}^8 \Theta_a^L \frac{\lambda_a}{2}\right) e^{-i\Theta^L} \begin{pmatrix} u_L \\ d_L \\ s_L \end{pmatrix}, \\ \begin{pmatrix} u_R \\ d_R \\ s_R \end{pmatrix} &\mapsto U_R \begin{pmatrix} u_R \\ d_R \\ s_R \end{pmatrix} = \exp\left(-i \sum_{a=1}^8 \Theta_a^R \frac{\lambda_a}{2}\right) e^{-i\Theta^R} \begin{pmatrix} u_R \\ d_R \\ s_R \end{pmatrix}, \end{aligned} \quad (30)$$

Spontaneous symmetry breaking

- Goldstone's theorem: spontaneous breaking of continuous global symmetries implies the existence of massless particles.
- NO. of Goldstone boson = $n_G - n_H$
 G : symmetry group of Lagrangian;
 H : the subgroup leaves the ground state invariant after SSB
- $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V \Rightarrow 8$ Goldstone bosons
- nonlinear realization of chiral symmetry

$$U(x) = \exp\left(i\frac{\phi(x)}{F_0}\right), \quad U \rightarrow RUL^\dagger, \quad (31)$$

$$\phi(x) = \sum_{a=1}^8 \lambda_a \phi_a(x) \equiv \begin{pmatrix} \pi^0 + \frac{1}{\sqrt{3}}\eta & \sqrt{2}\pi^+ & \sqrt{2}K^+ \\ \sqrt{2}\pi^- & -\pi^0 + \frac{1}{\sqrt{3}}\eta & \sqrt{2}K^0 \\ \sqrt{2}K^- & \sqrt{2}\bar{K}^0 & -\frac{2}{\sqrt{3}}\eta \end{pmatrix}. \quad (32)$$

- Quark masses break the chiral symmetry explicitly: $m_\pi^2 \sim m_q$

Effective Lagrangian and Power-Counting Scheme

- The Lagrangian is organized as the **NO. of derivatives** of Goldstone bosons
- The chiral dimension D of given diagrams

$$\mathcal{M}(tp_i, t^2 m_q) = t^D \mathcal{M}(p_i, m_q), \quad (33)$$

$$D = 2 + 2N_L + \sum_{n=1}^{\infty} N_{2n}(2n - 2), \quad (34)$$

- Λ_{CSB} scale: either $4\pi F_0$ or m_ρ
- The leading order Lagrangian

$$\mathcal{L}_2 = \frac{F_0^2}{4} \text{Tr}[\nabla_\mu U (\nabla^\mu U)^\dagger] + \frac{F_0^2}{4} \text{Tr}(\chi U^\dagger + U \chi^\dagger). \quad (35)$$

S. Weinberg, Physica A 96, 327 (1979).

J. Gasser and H. Leutwyler, Annals Phys. 158, 142 (1984).

J. Gasser and H. Leutwyler, Nucl. Phys. B 250, 465 (1985).

Heavy baryon formalism

- the baryon mass does not vanish in the chiral limit
⇒ mess up the power counting
- the heavy and light freedom

$$p_\mu = Mv_\mu + l_\mu \quad (36)$$

$$\Psi = e^{-iMv \cdot x}(H + h), \text{ with } \phi H = H, \quad \phi h = -h \quad (37)$$

$$\begin{aligned} \mathcal{L} &= \bar{\Psi}(i\not{\partial} - M)\Psi \\ &= \bar{H}(iv \cdot \partial)H - \bar{h}(iv \cdot \partial + 2M)h + \bar{H}i\not{\partial}^\perp h + \bar{h}i\not{\partial}^\perp H \end{aligned} \quad (38)$$

- Integrate the heavy field h ,

$$\mathcal{L} = \bar{H}(iv \cdot \partial)H + \mathcal{O}\left(\frac{1}{2M}\right) \quad (39)$$

E. E. Jenkins and A. V. Manohar, Phys. Lett. B 255, 558 (1991),

V. Bernard, N. Kaiser, J. Kambor and U. G. Meissner, Nucl. Phys. B 388, 315 (1992).

Heavy baryon formalism

- Power counting for diagrams with only one baryon line

$$D = 2L + 1 + \sum_{n=2}^{\infty} (n-2)N_n^M + \sum_{n=1}^{\infty} (n-1)N_n^B$$

- The leading order Lagrangian

$$\mathcal{L}^{(1)} = \bar{\Psi}(i\mathcal{D} - M_H)\Psi + \frac{\tilde{g}_A}{2}\bar{\Psi}\gamma^\mu\gamma_5 u_\mu\Psi \quad (40)$$

$$\mathcal{L}^{(1)} = \bar{H}(iv \cdot D)H + \tilde{g}_A \text{Tr}\bar{H}S^\mu u_\mu H, \quad (41)$$

where $S_\mu = \frac{i}{2}\gamma_5\sigma_{\mu\nu}v^\nu$ is the covariant spin-operator.

- In this work,

$$Q_B = \text{diag}(2, 1, 1) \text{ and } Q_M = \text{diag}(2/3, -1/3, -1/3)$$

$$r_\mu = l_\mu = -eQA_\mu; \quad F_{\mu\nu}^+ = -2eQF_{\mu\nu} + \dots$$

- Traceless part and trace part: \hat{A} and $\text{Tr}(A)$