

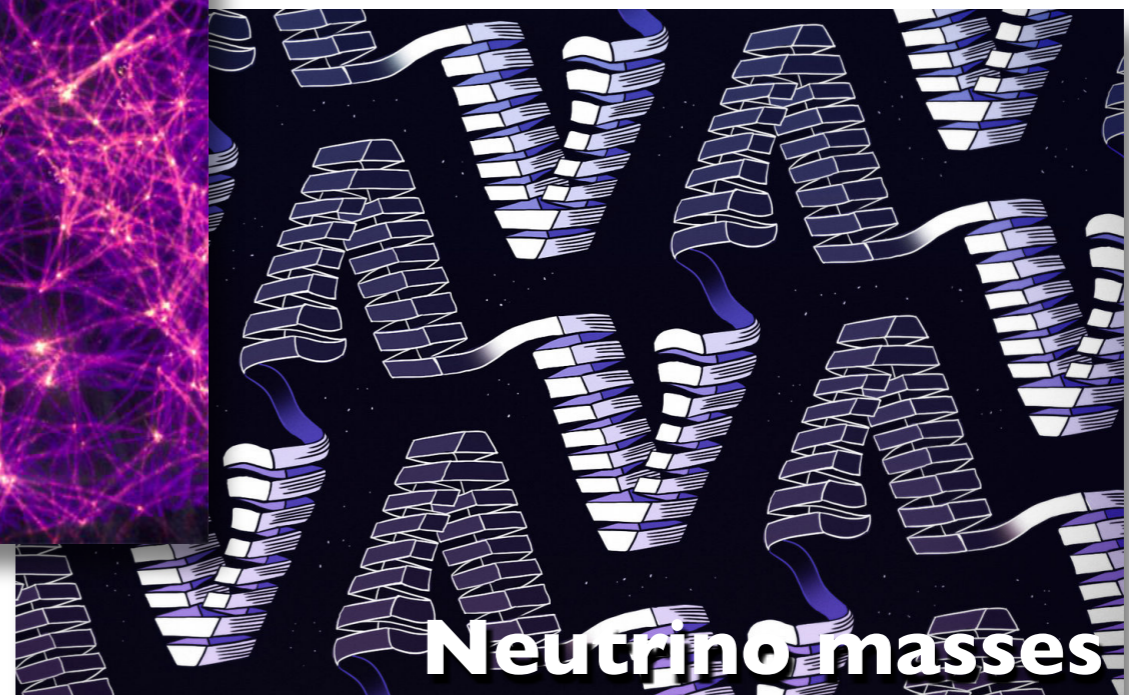
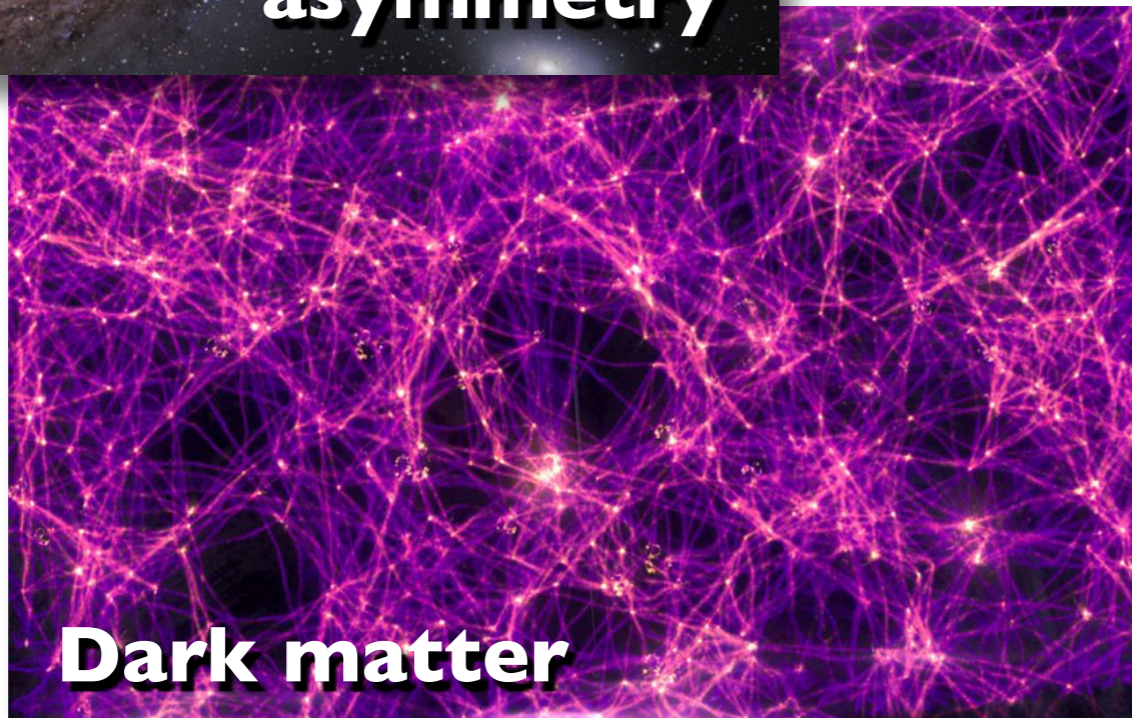
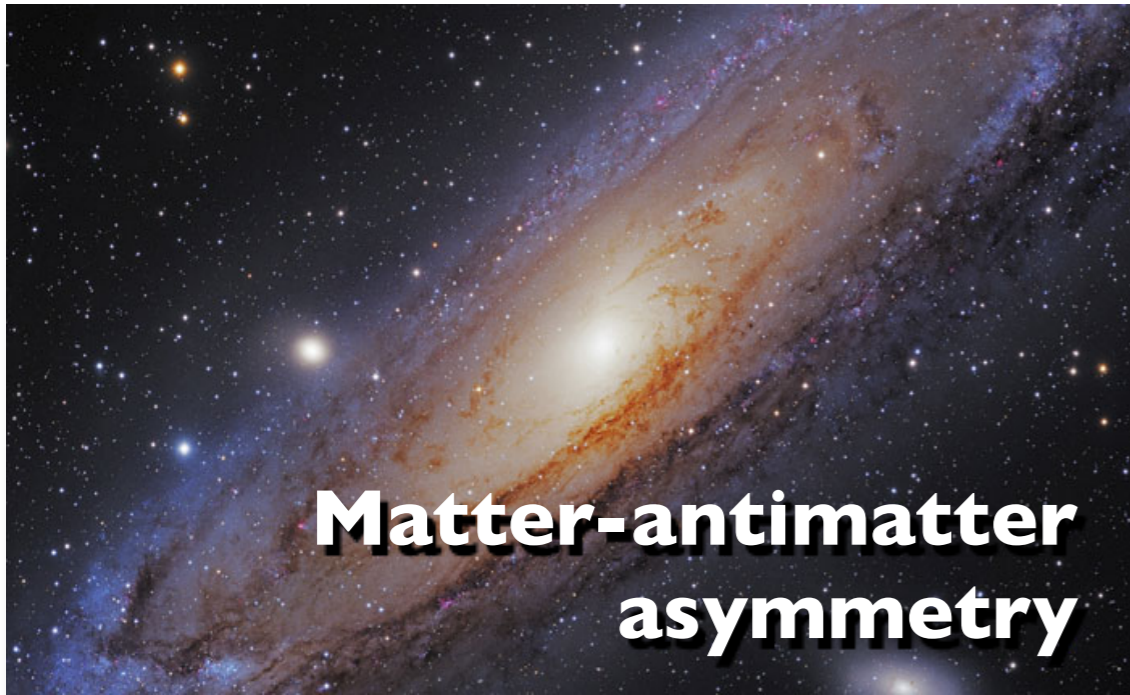
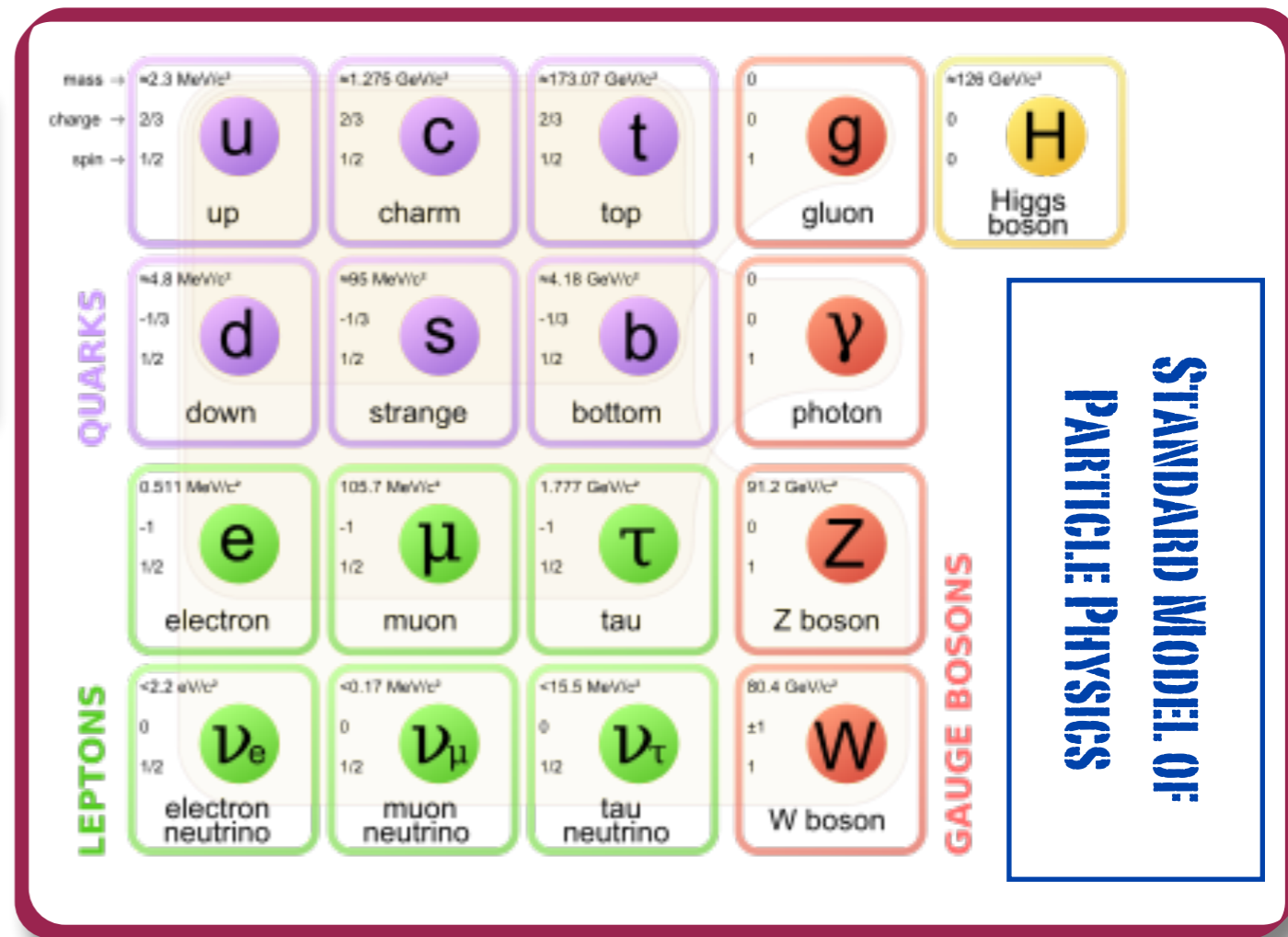
Neutrinoless double beta decay: what can lattice QCD teach us beyond the Standard Model

Amy Nicholson
UNC, Chapel Hill

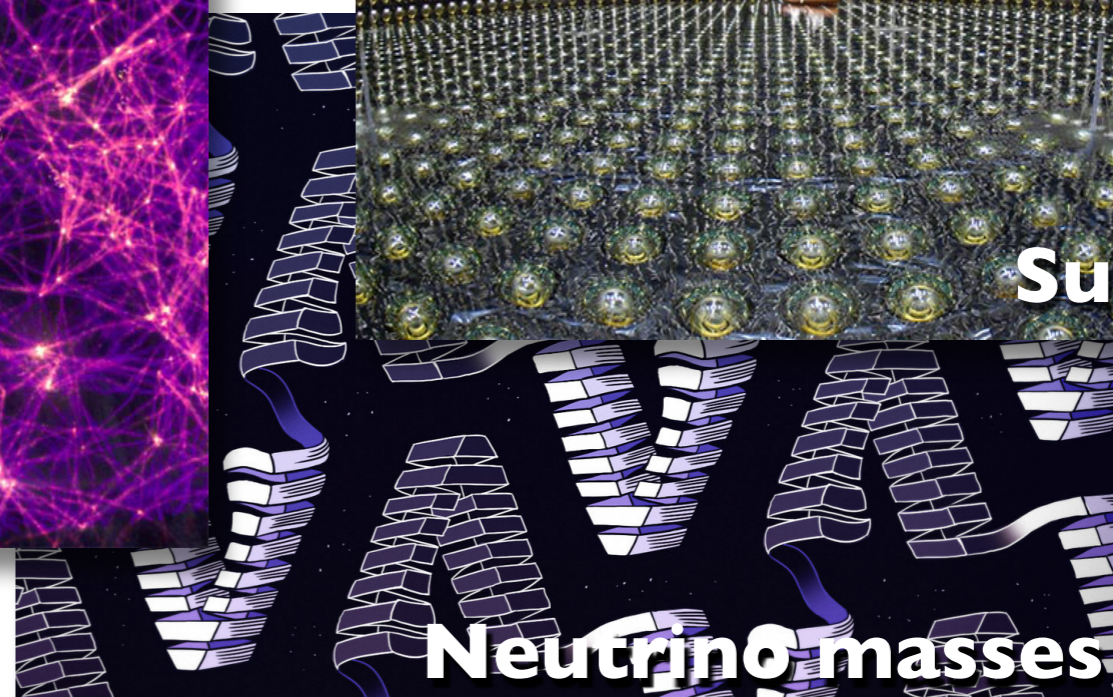
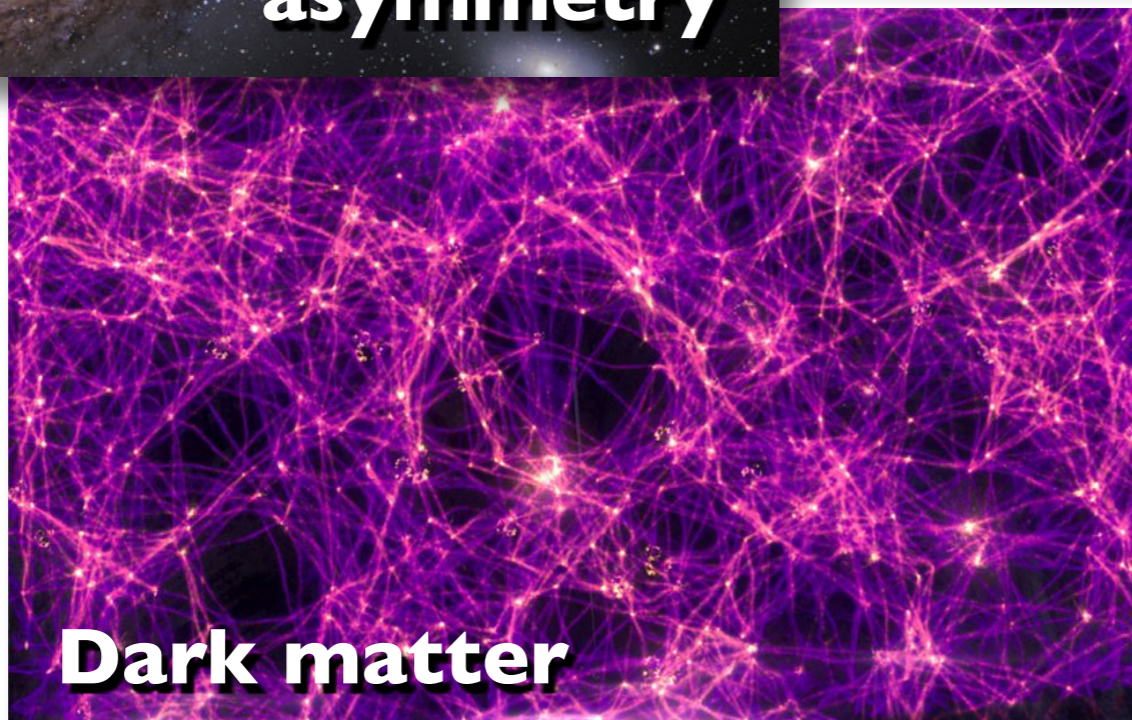
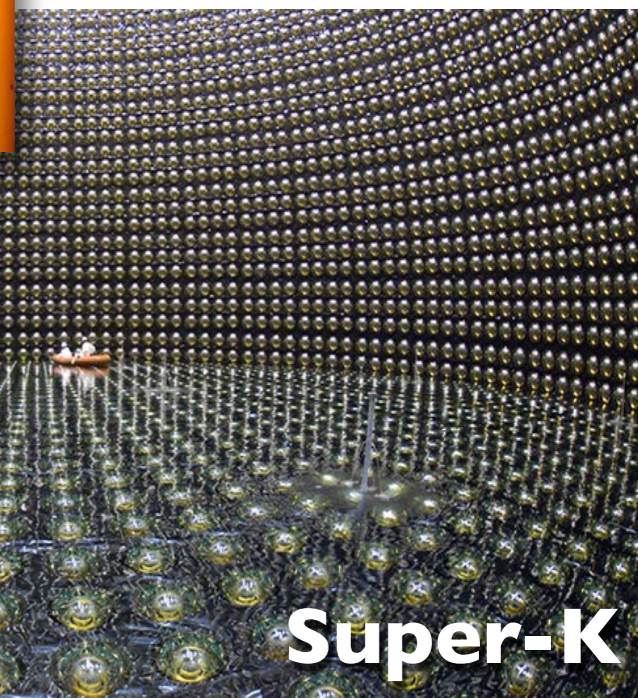
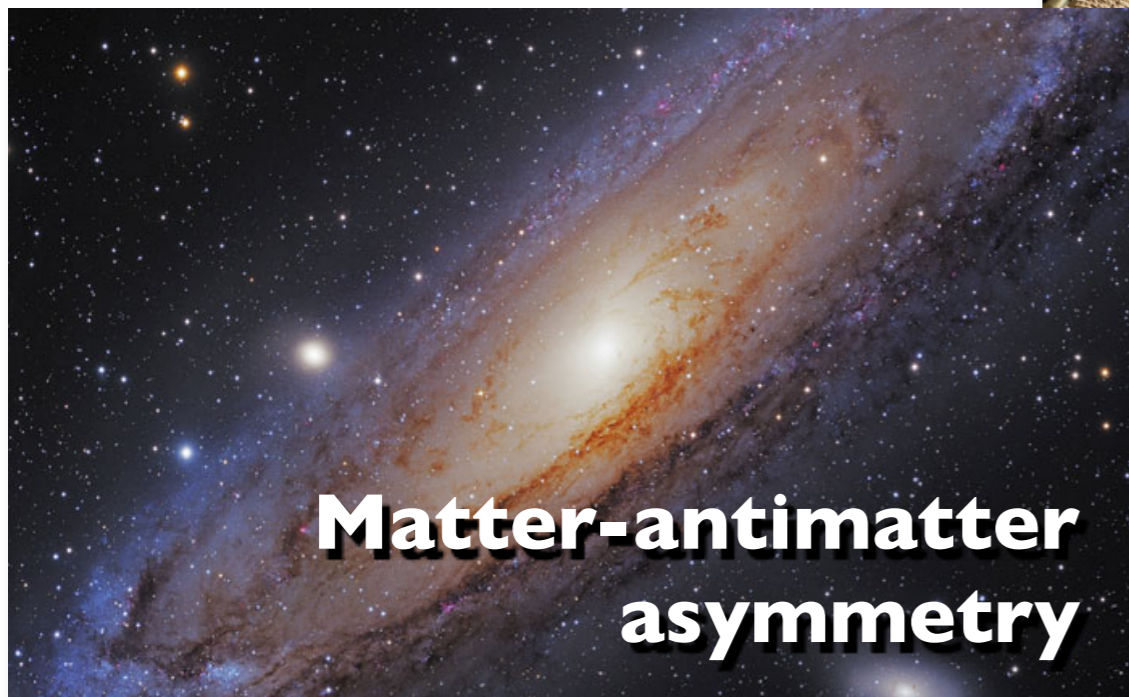
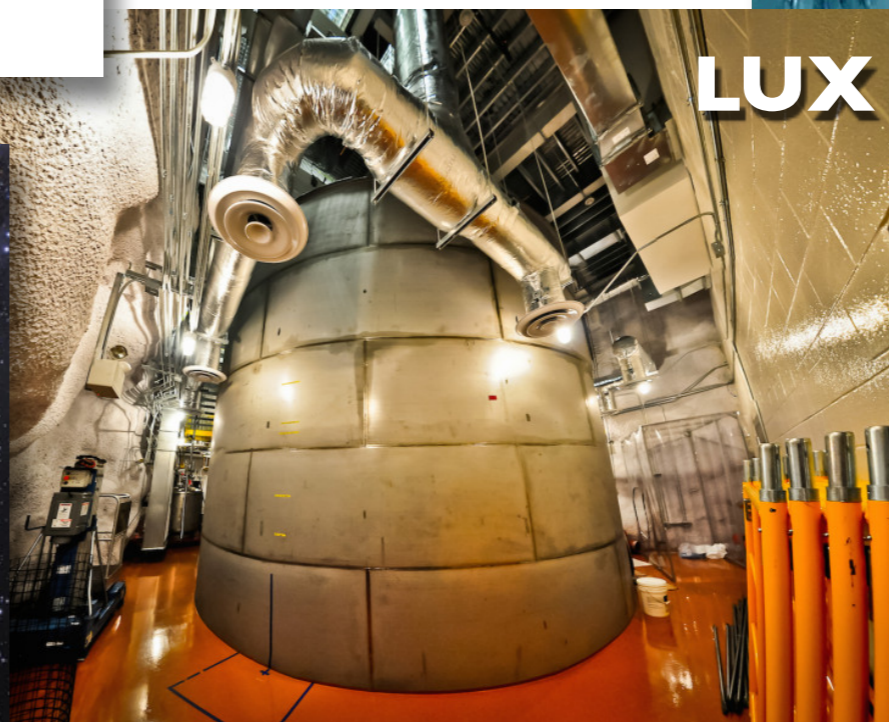
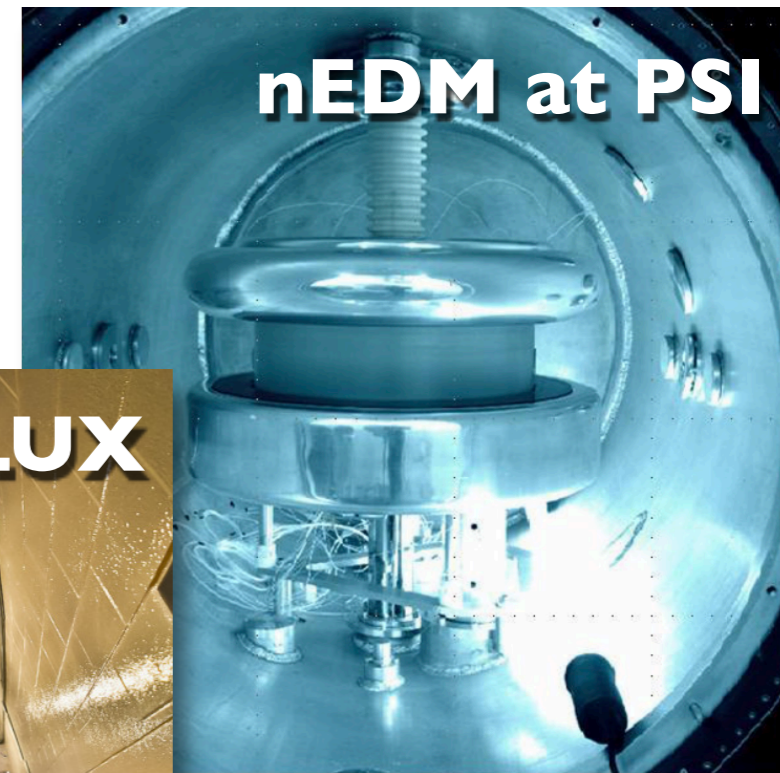
Summer School on
“Frontiers in Lattice QCD”
Peking University, July 8, 2019



The Standard Model and Beyond



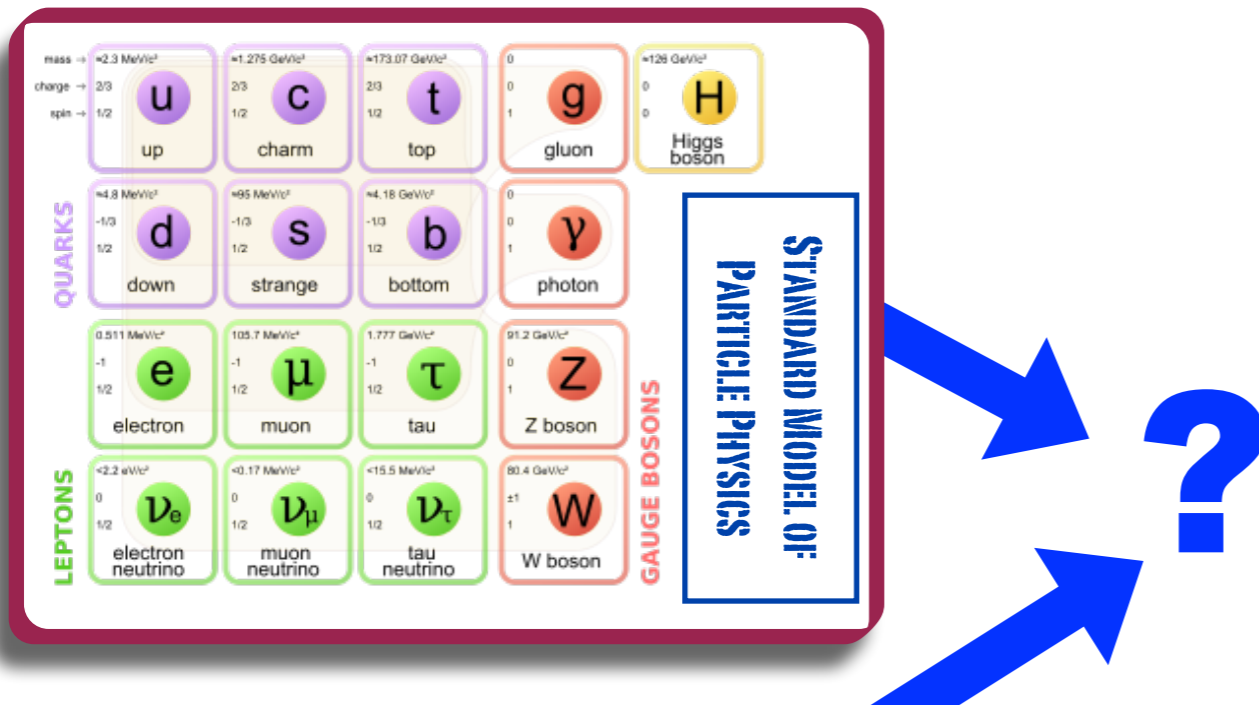
The Standard Model and Beyond



How can a solution of QCD teach us about new physics?

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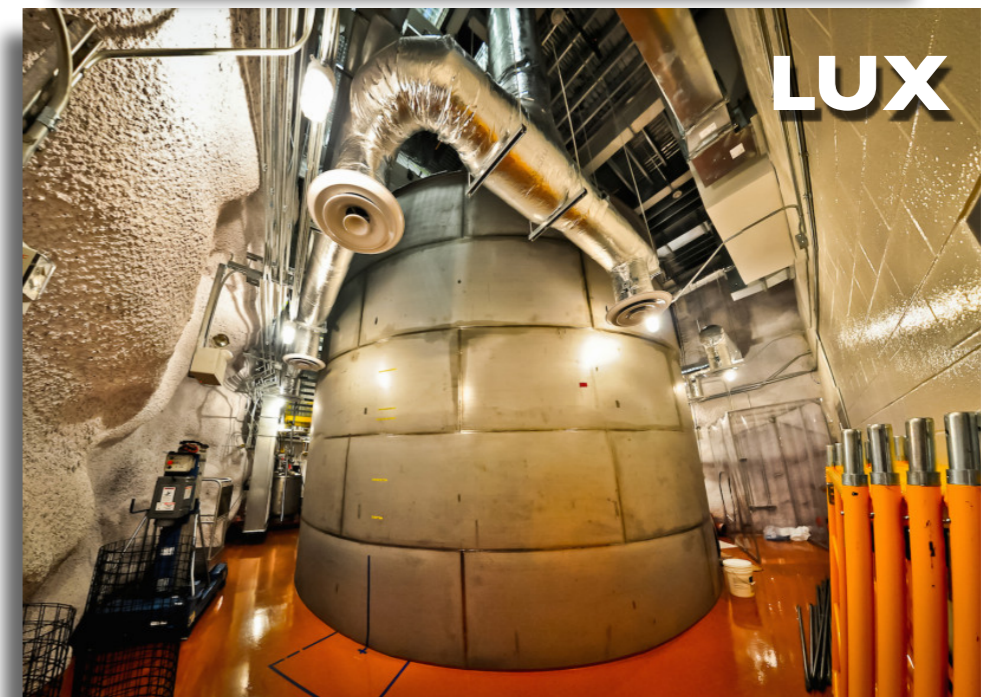
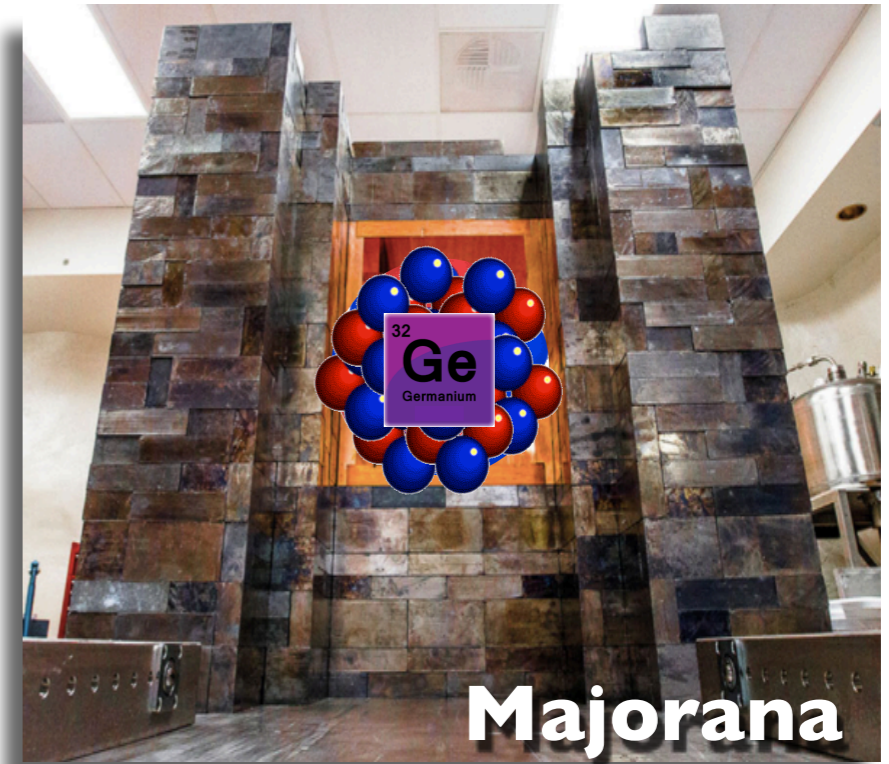
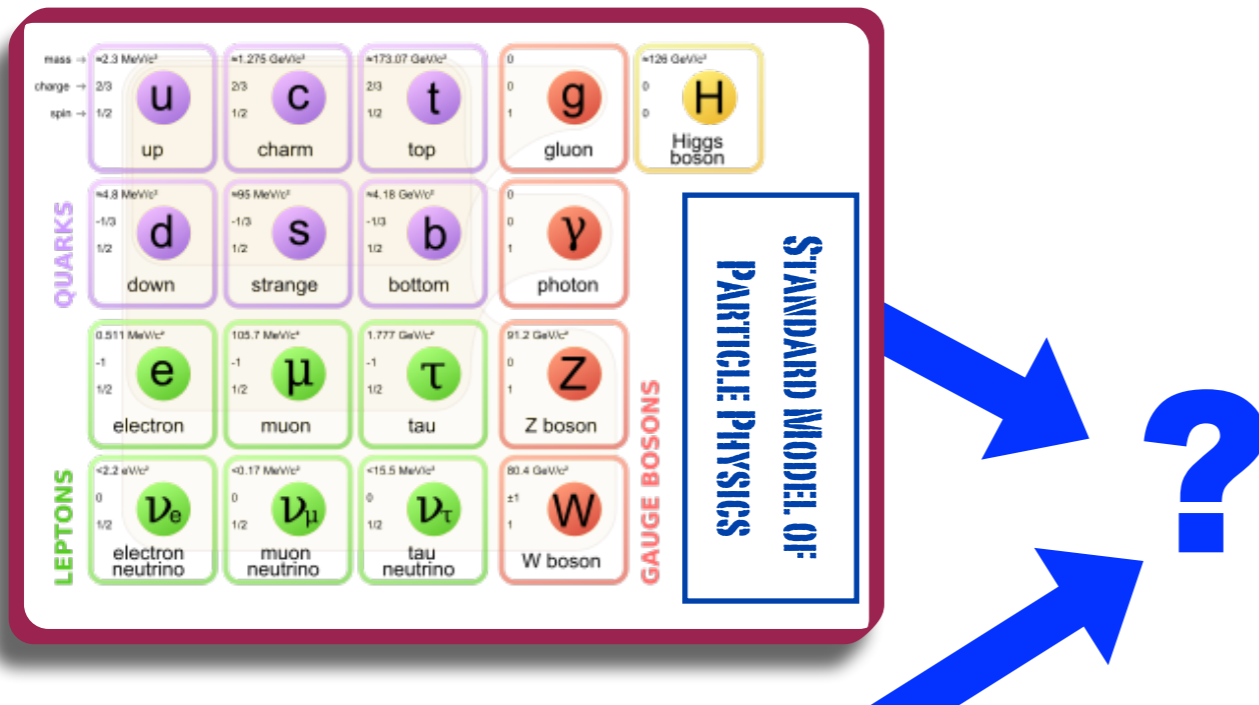
I. Look for discrepancies between the SM and experiment: g_A , proton radius, muon $g-2$



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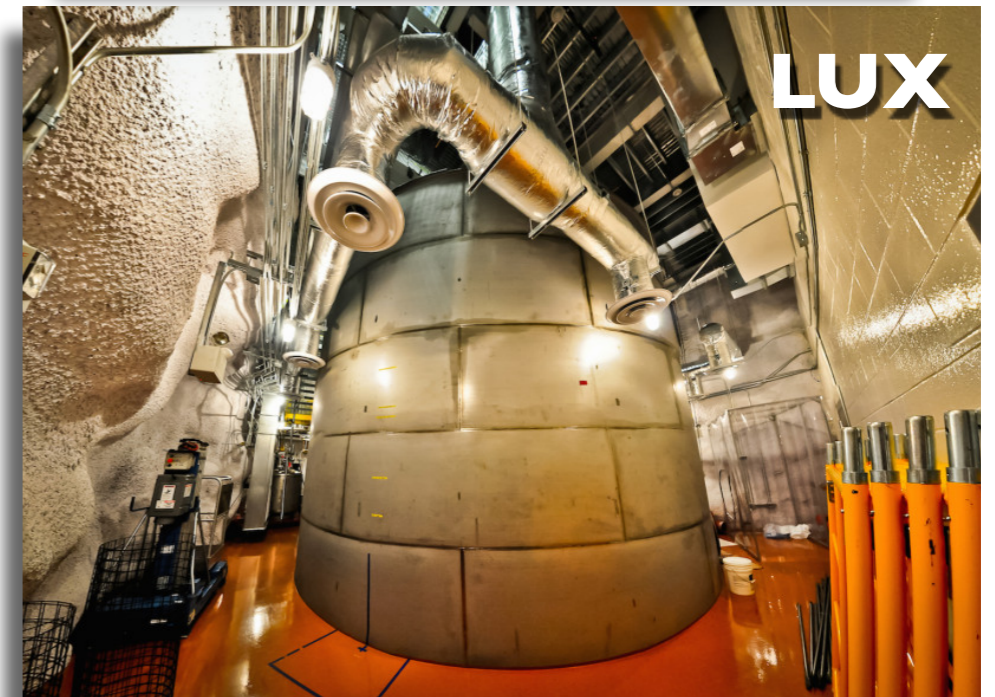
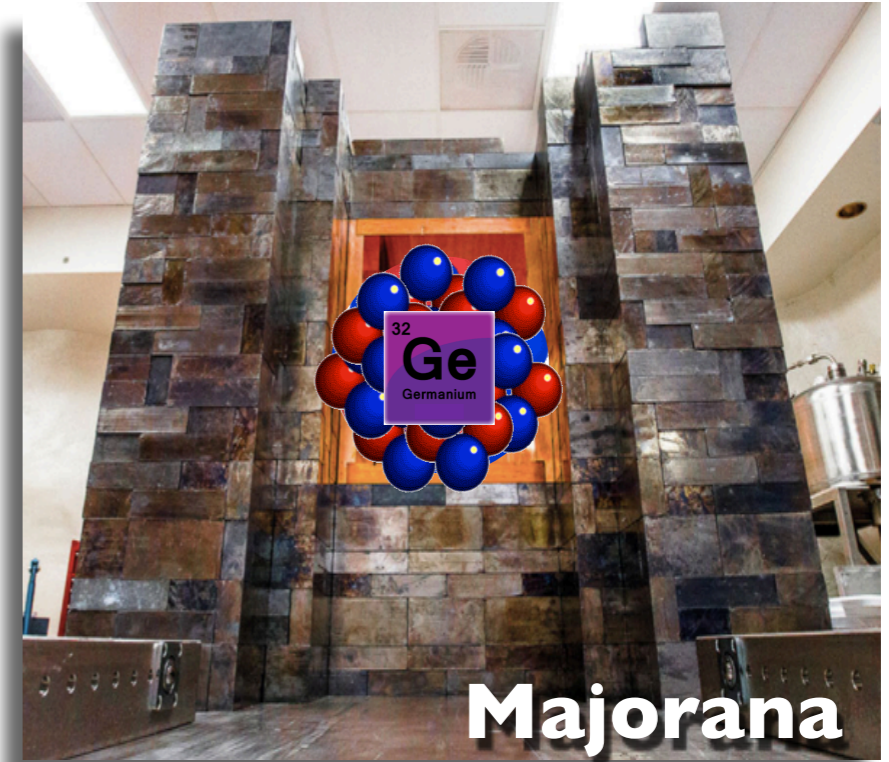
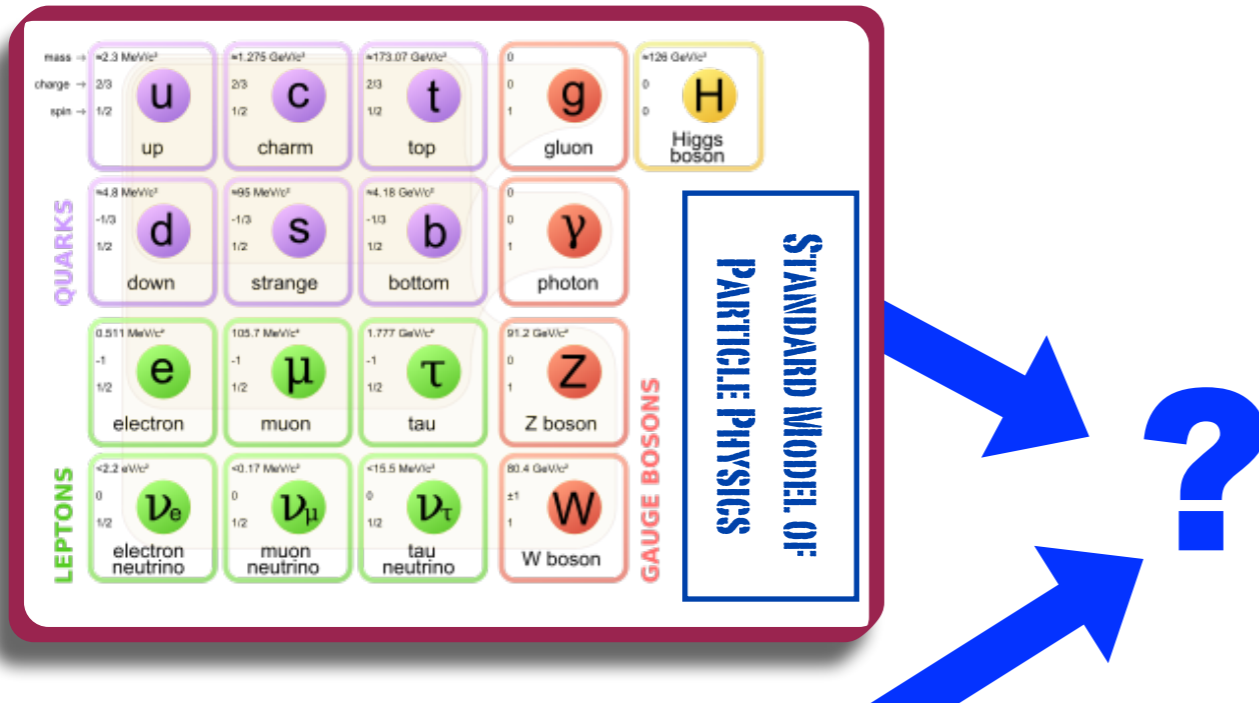
2. Match new physics model at high energies to low-energy nuclear experiments: $0\nu\beta\beta$, nucleon/nuclear EDM, DM searches



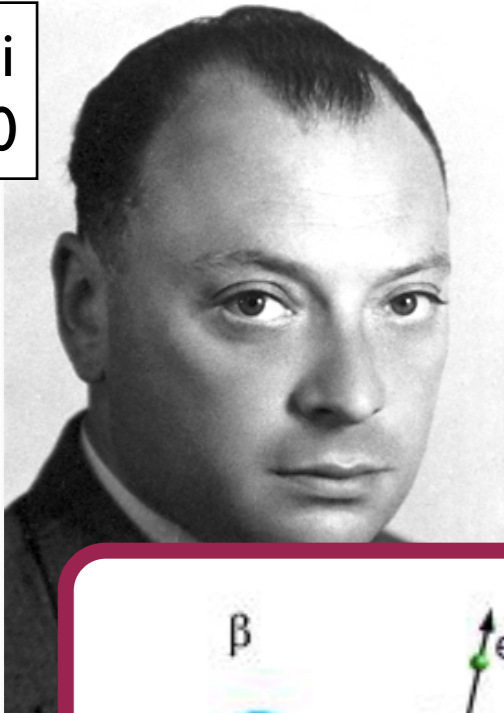
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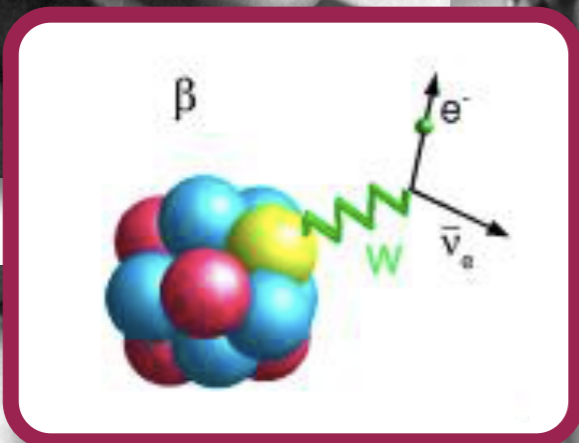
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Pauli
1930



Neutrinoless Double Beta Decay

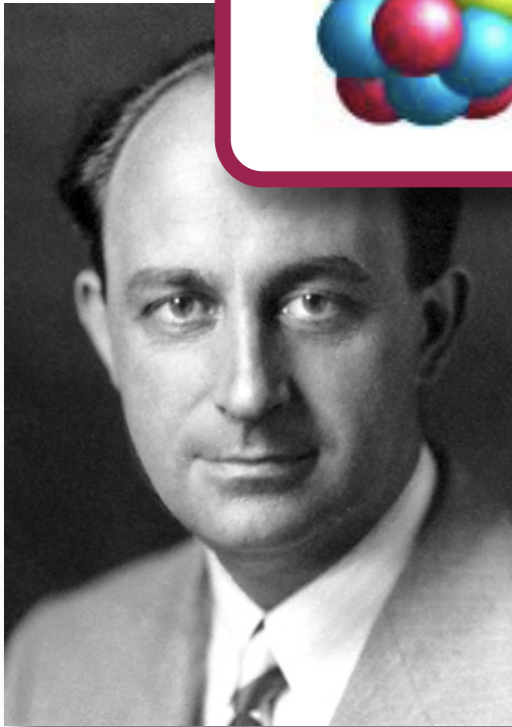


Chadwick
1932



Majorana
1937

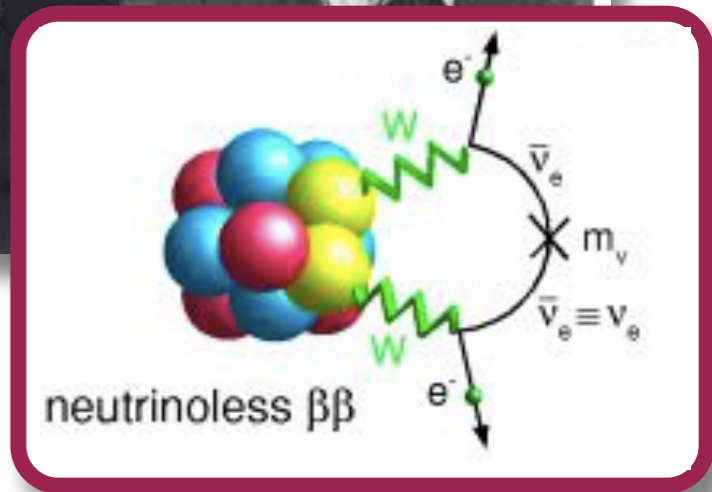
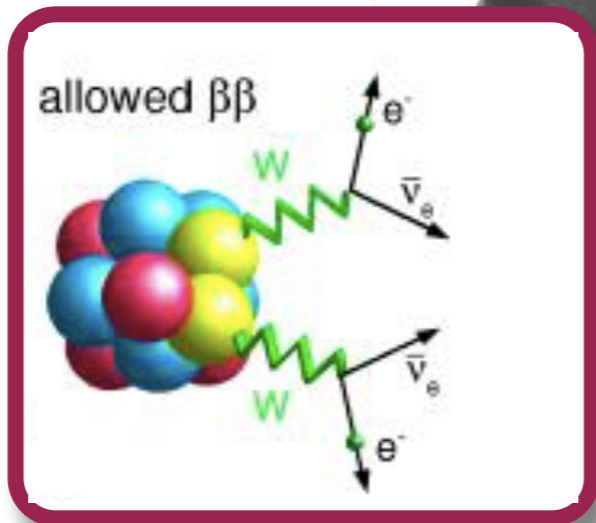
Racah
1937



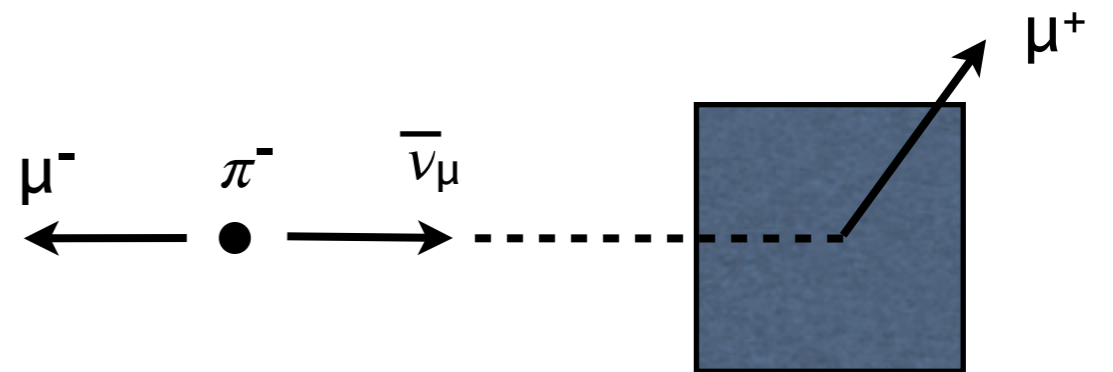
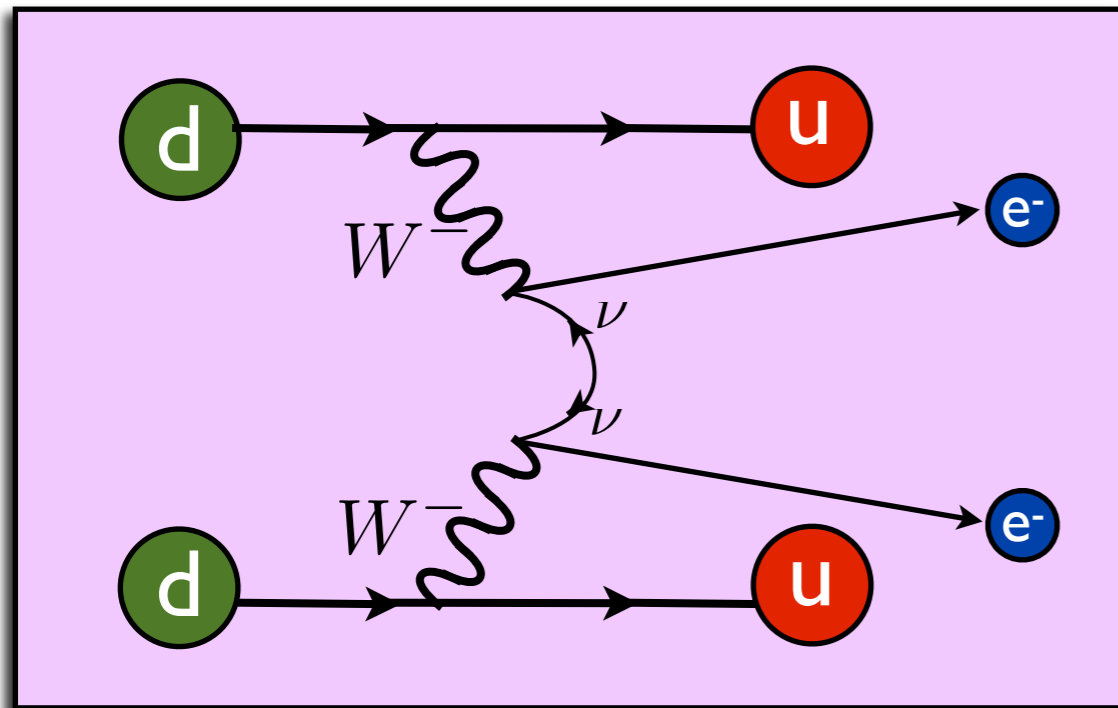
Fermi
1934



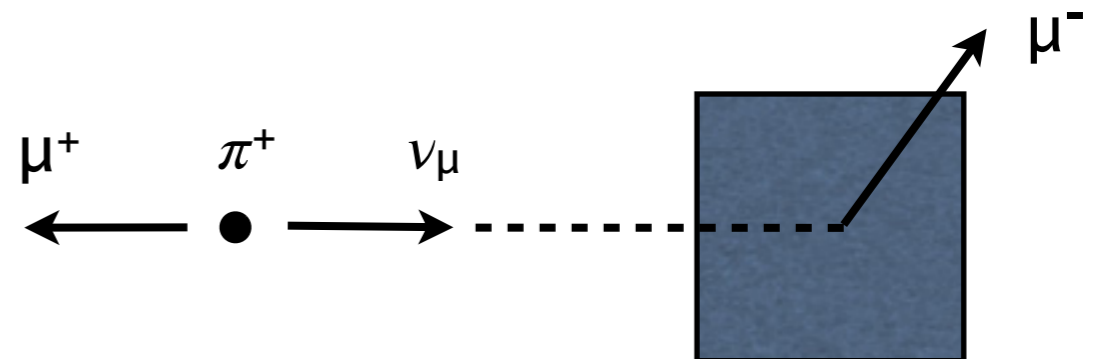
Goppert-Mayer
1935



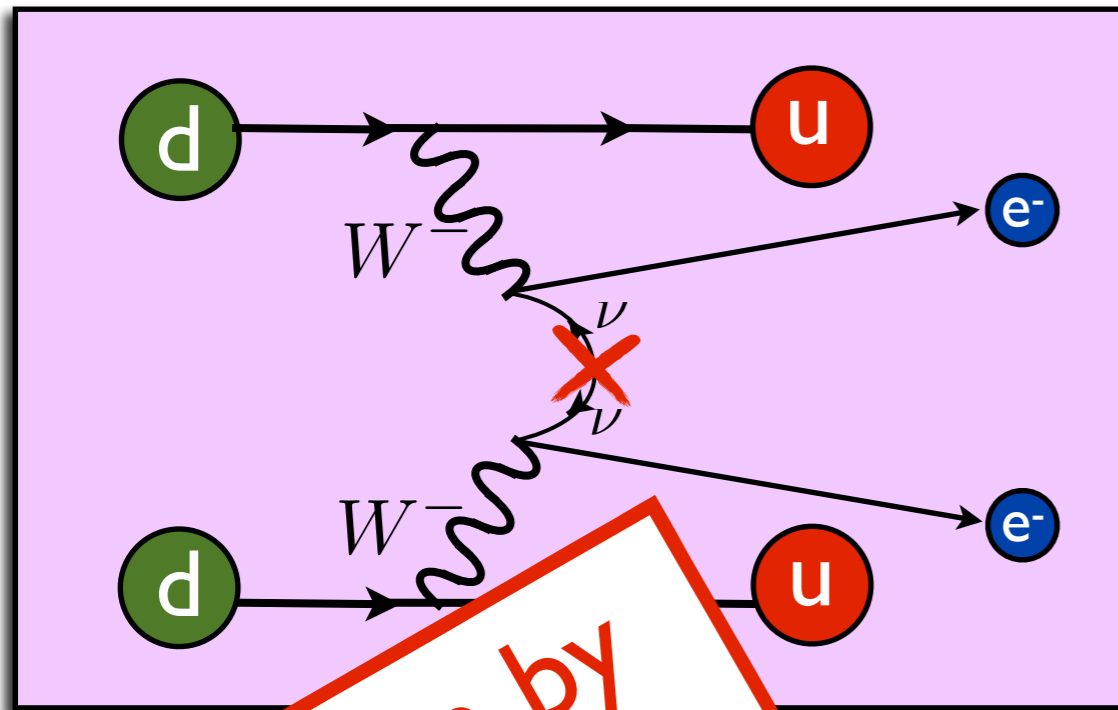
Neutrinos & Symmetries



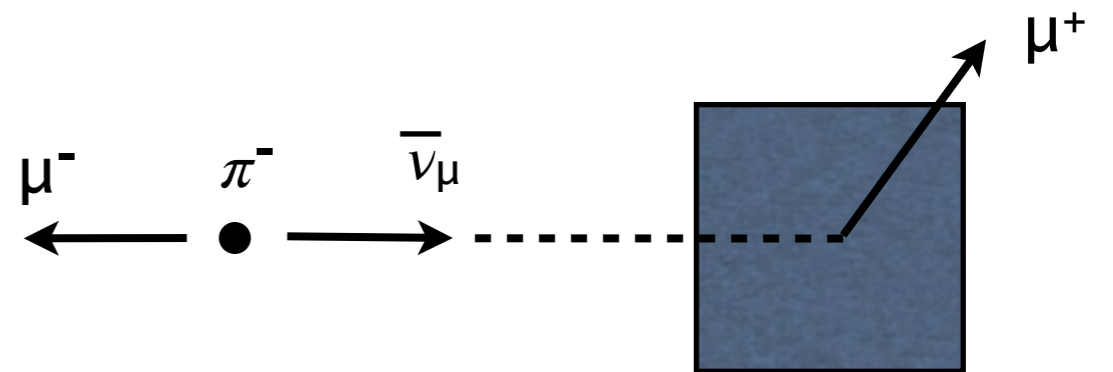
Neutrinos produced in π^- decays always produce μ^+



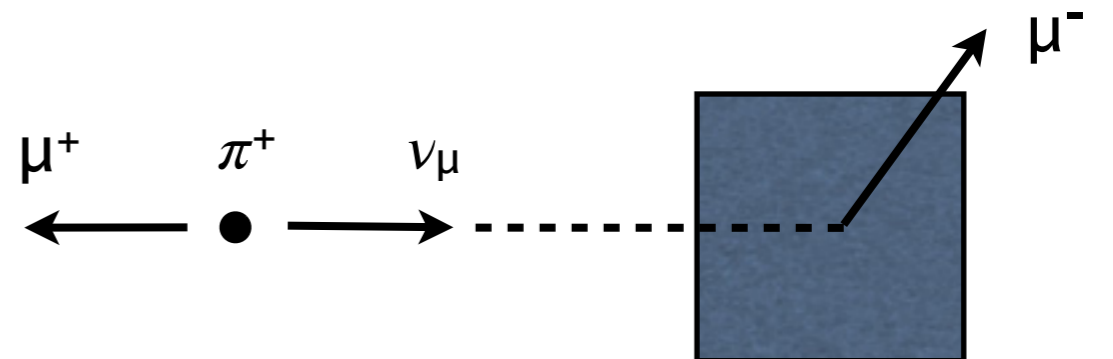
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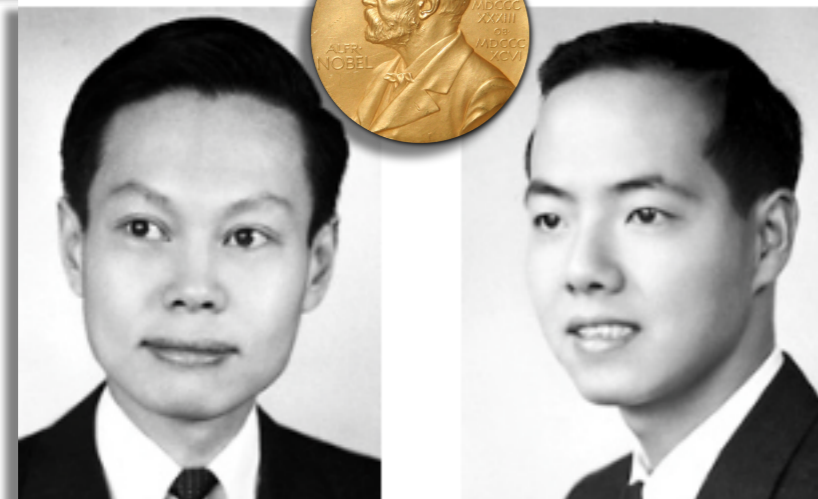
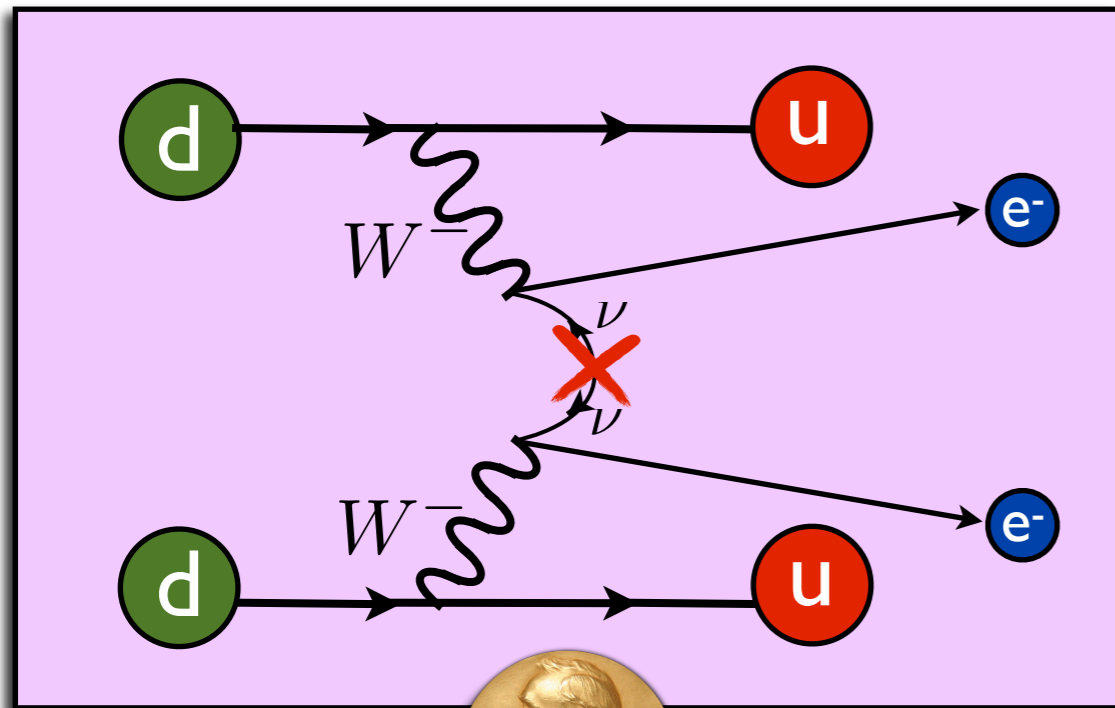
Forbidden by
lepton number



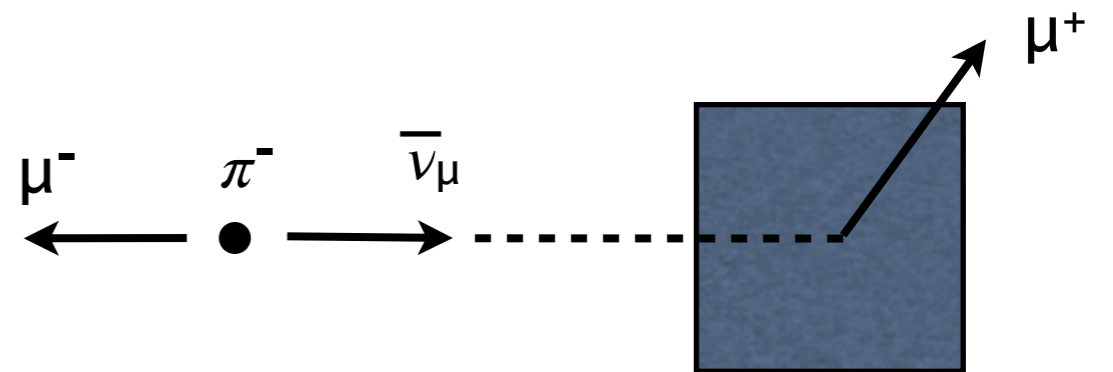
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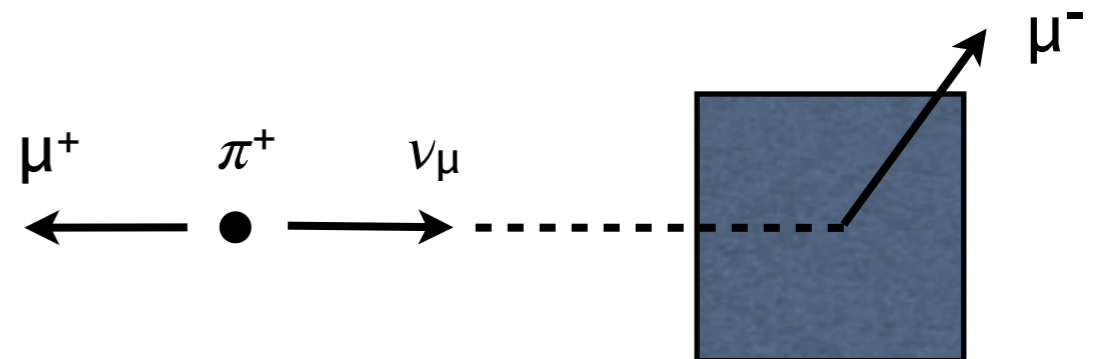
Neutrinos & Symmetries



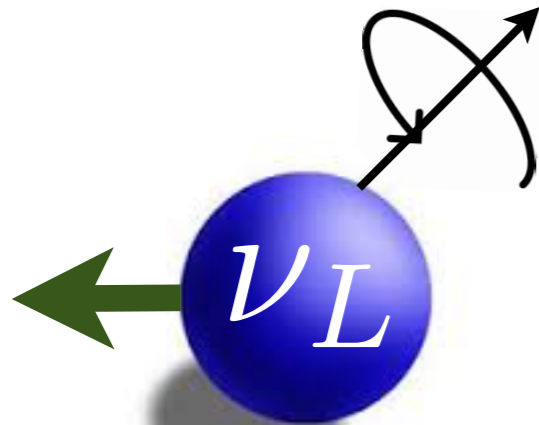
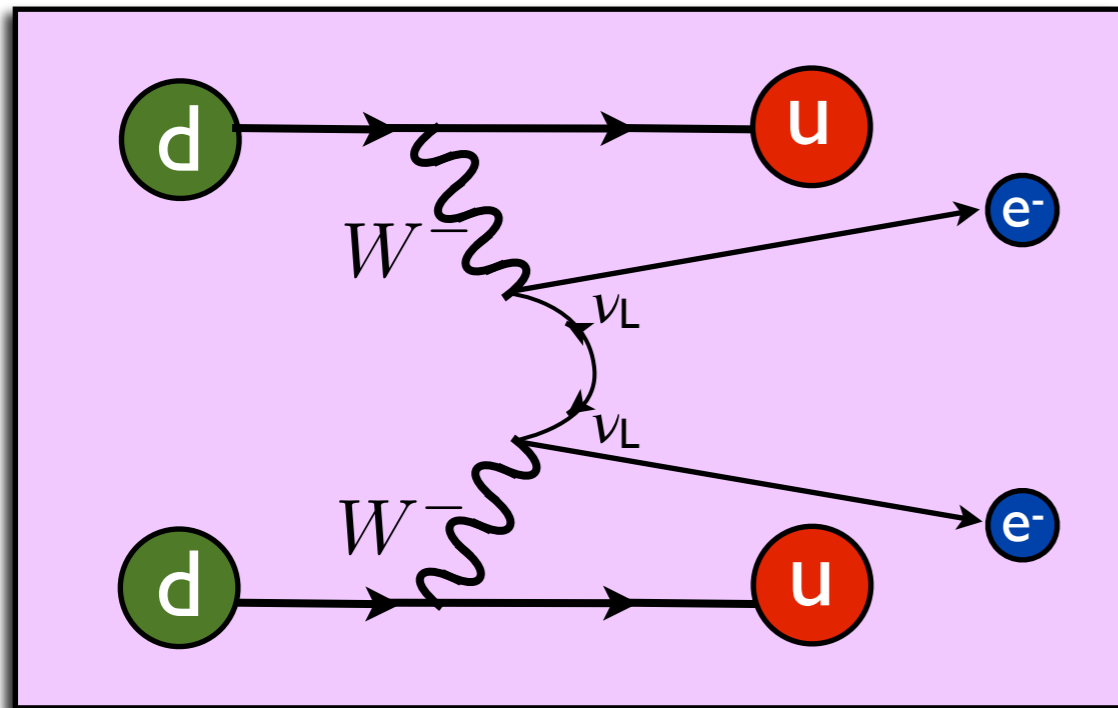
1950's: Neutrinos are produced with a specific helicity (parity violating)



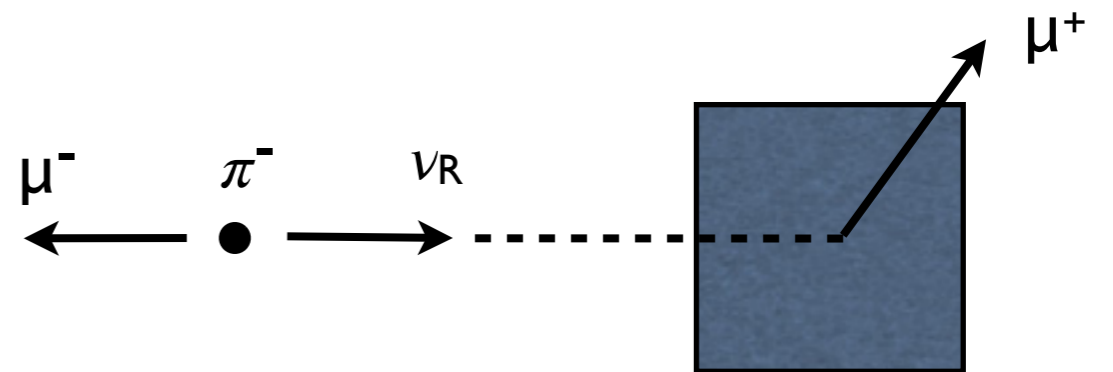
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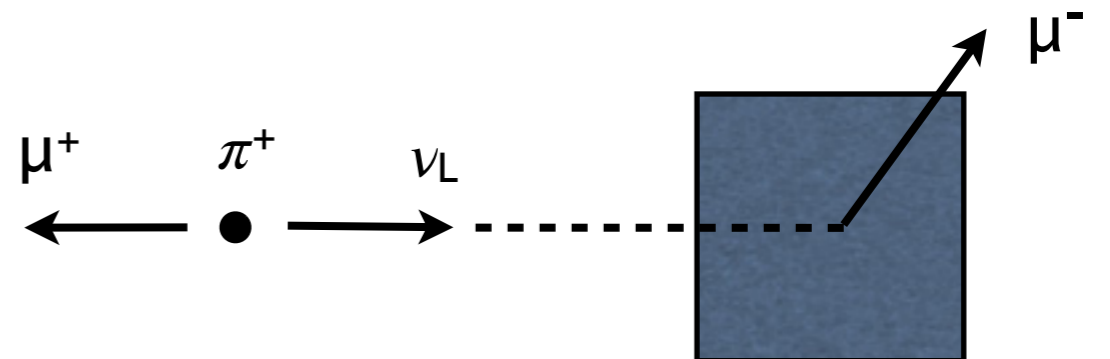
Neutrinos & Symmetries



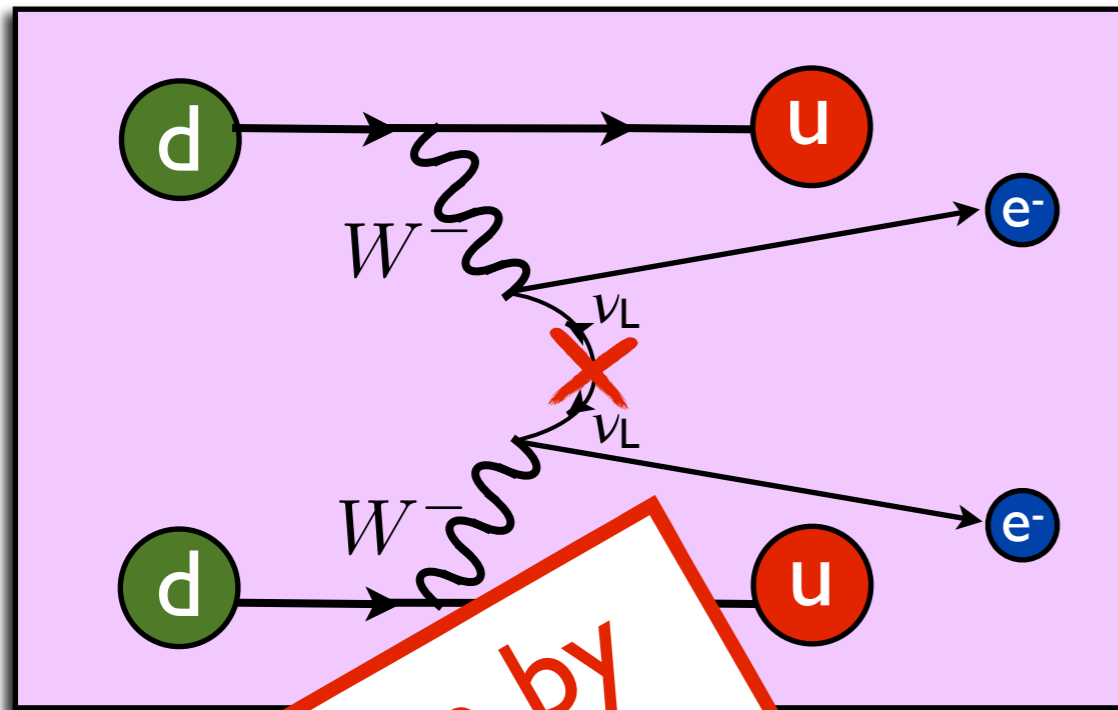
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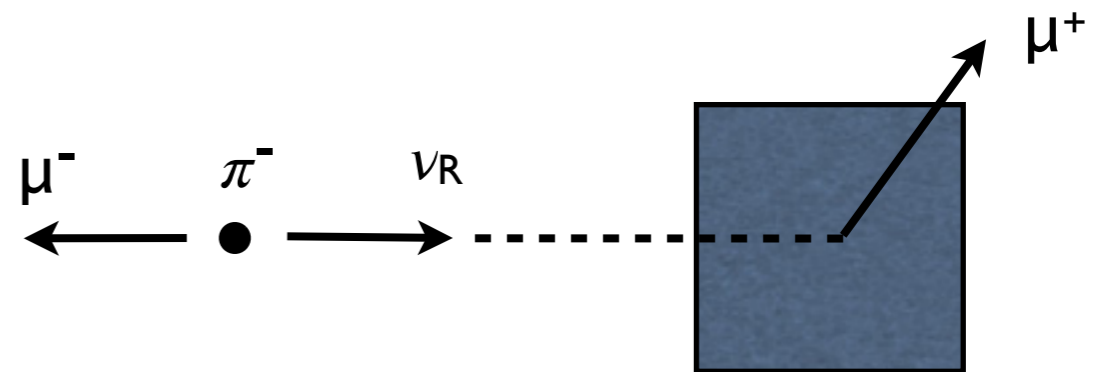
Neutrinos & Symmetries



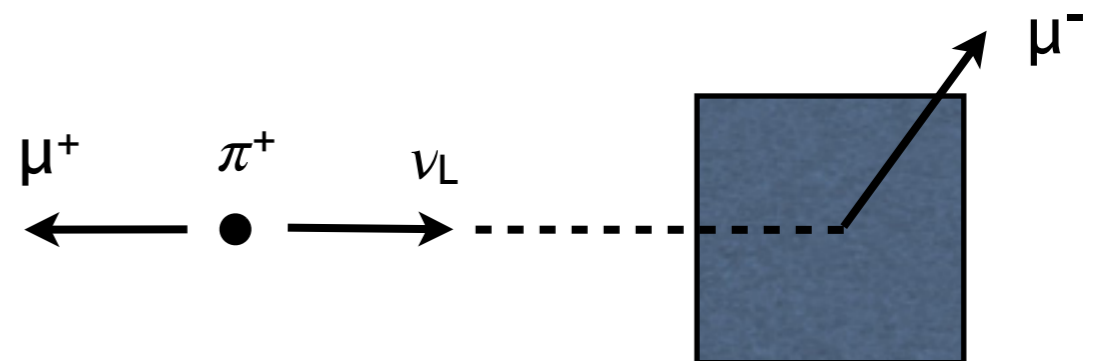
Forbidden by helicity



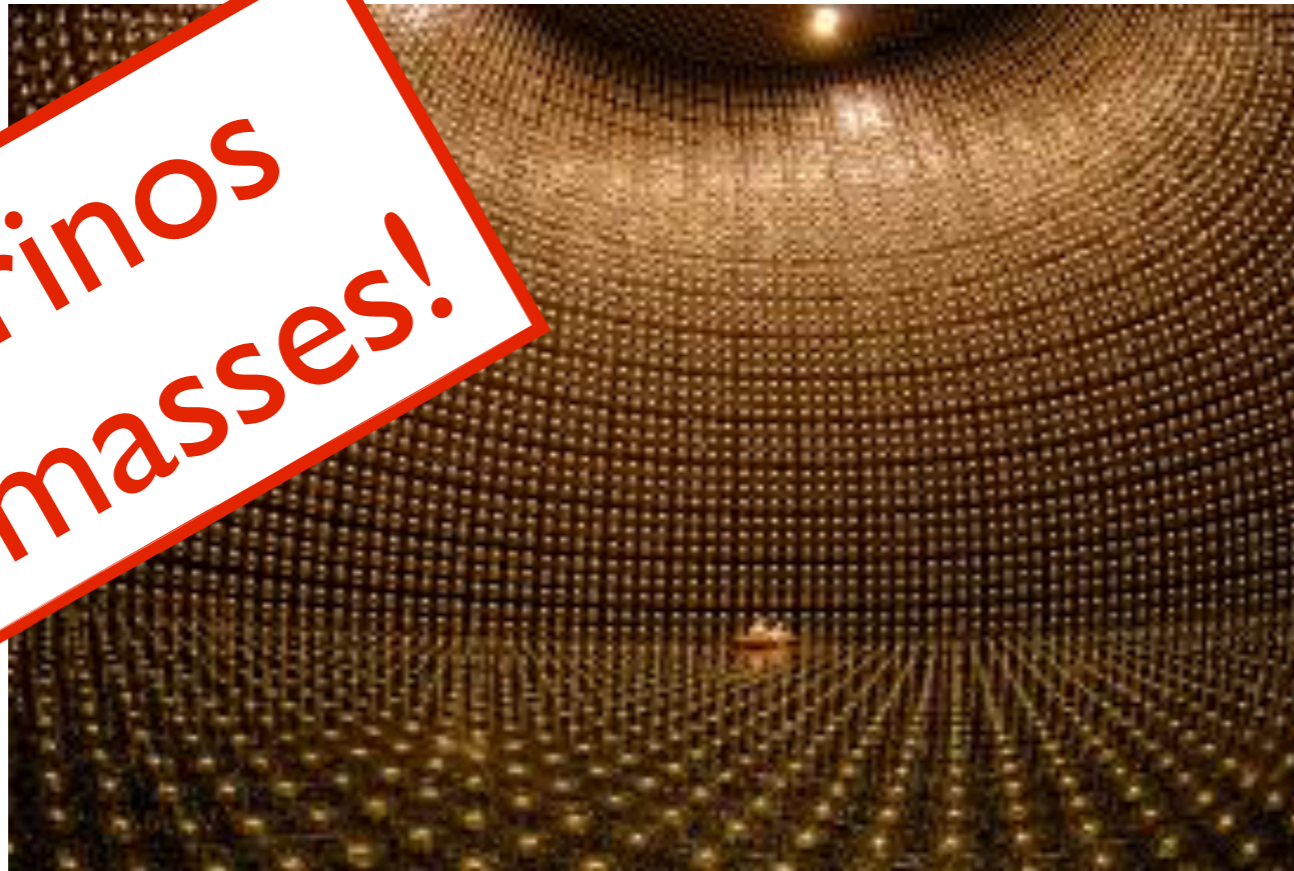
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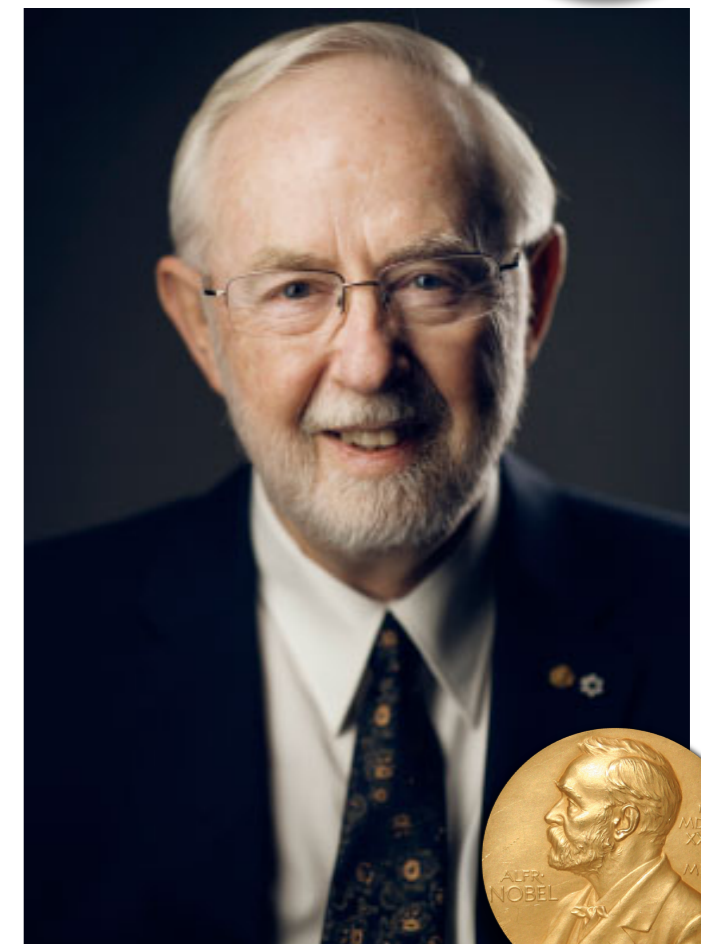
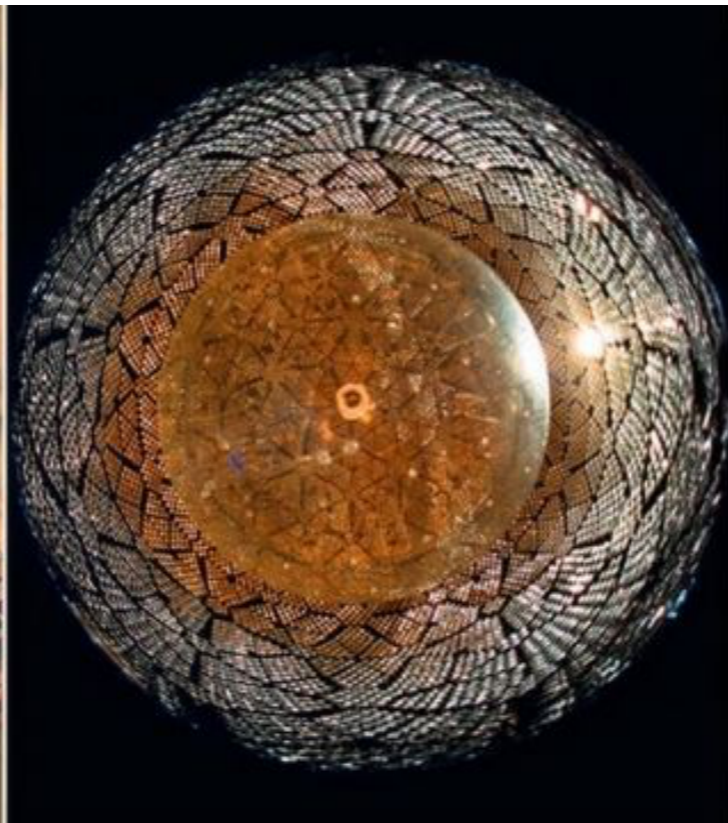
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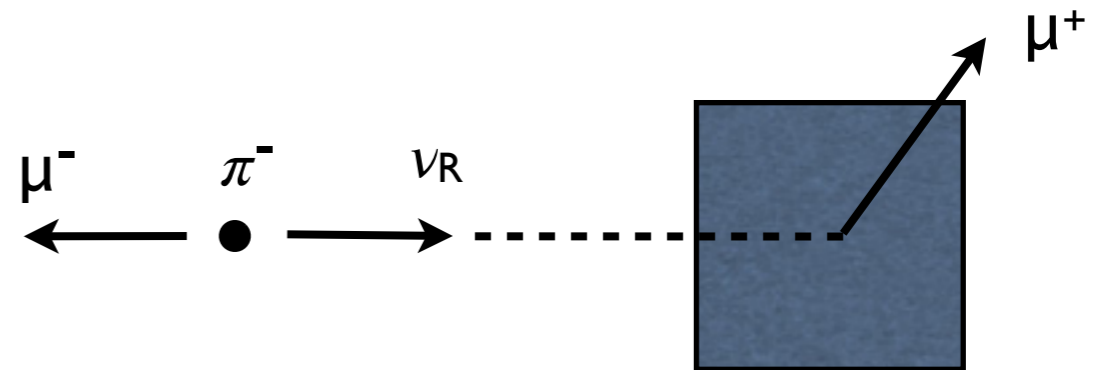
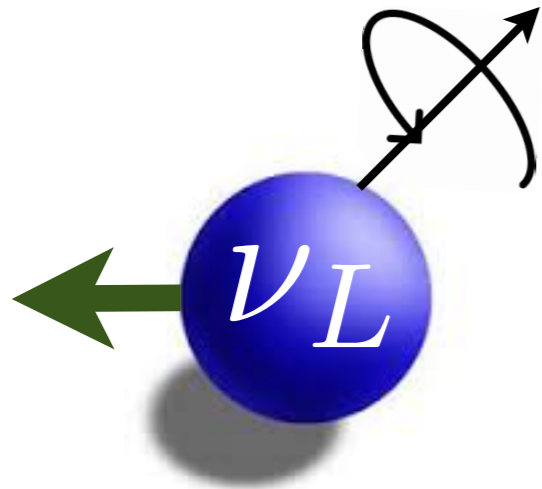
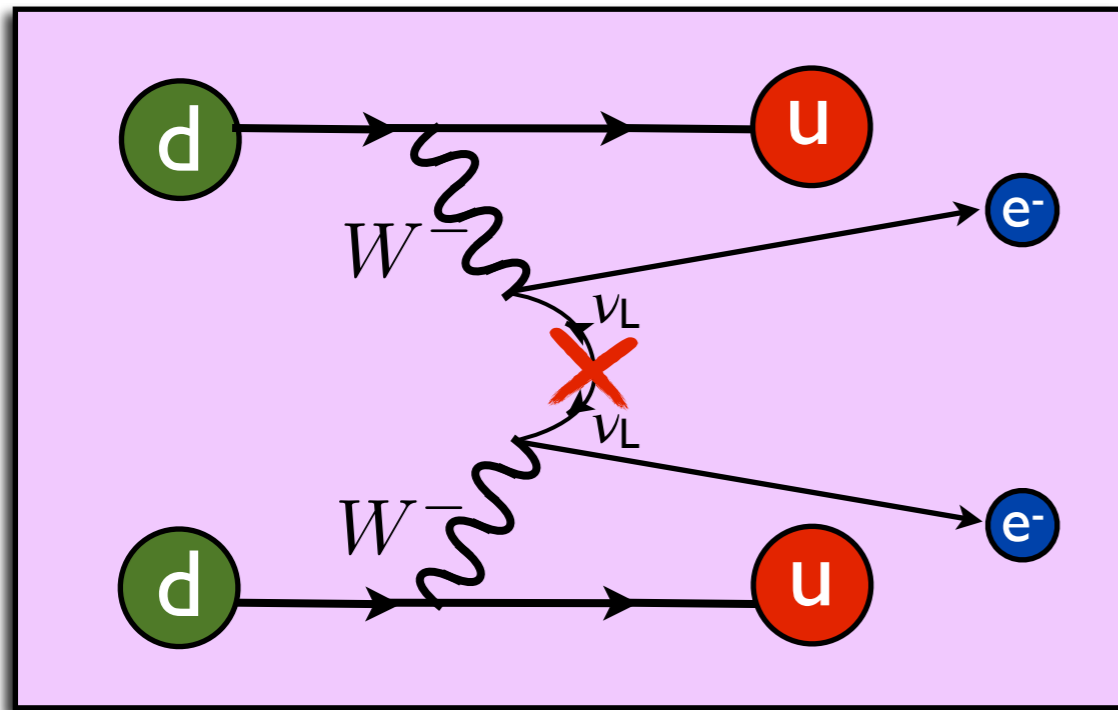
Neutrinos
have masses!



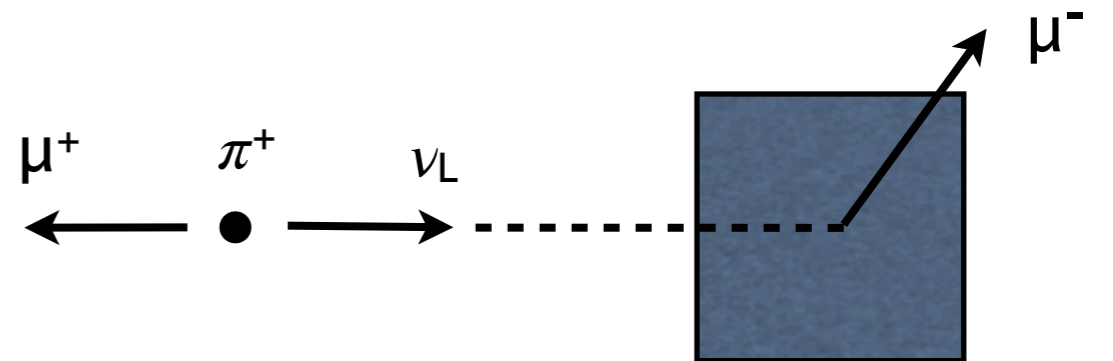
Takaaki Kajita
(Super-K)
Arthur B.
McDonald
(SNO)
Nobel Prize,
2015



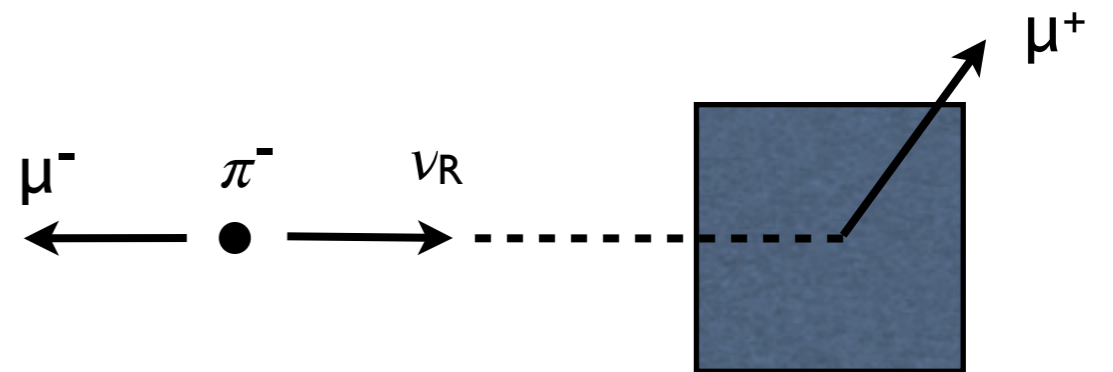
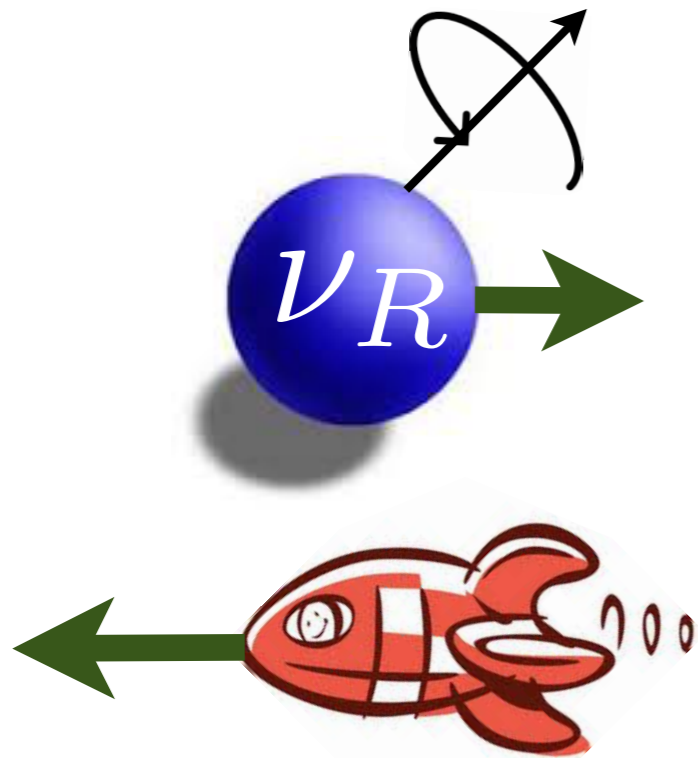
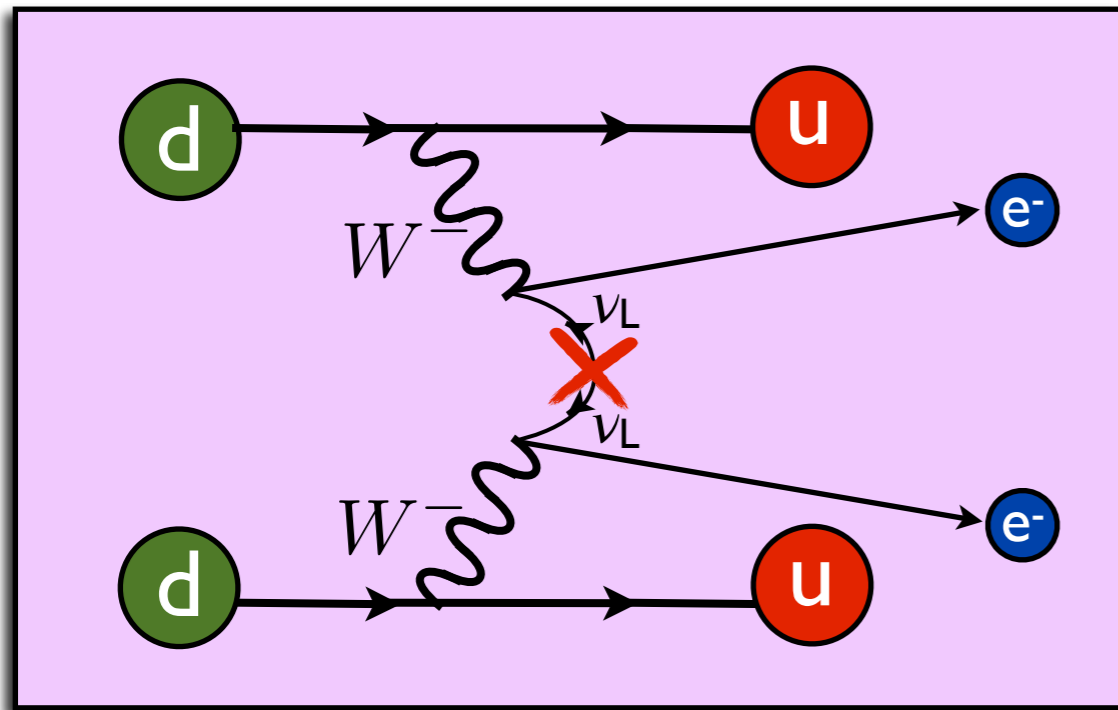
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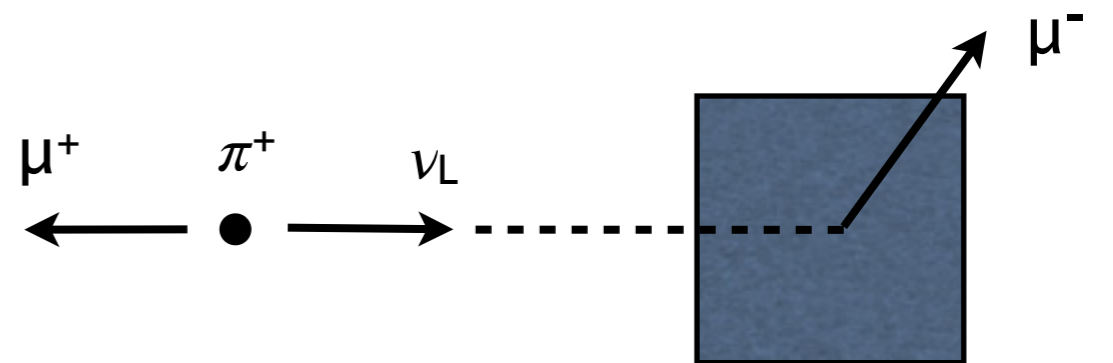
Neutrinos produced in π^- decays always produce μ^-



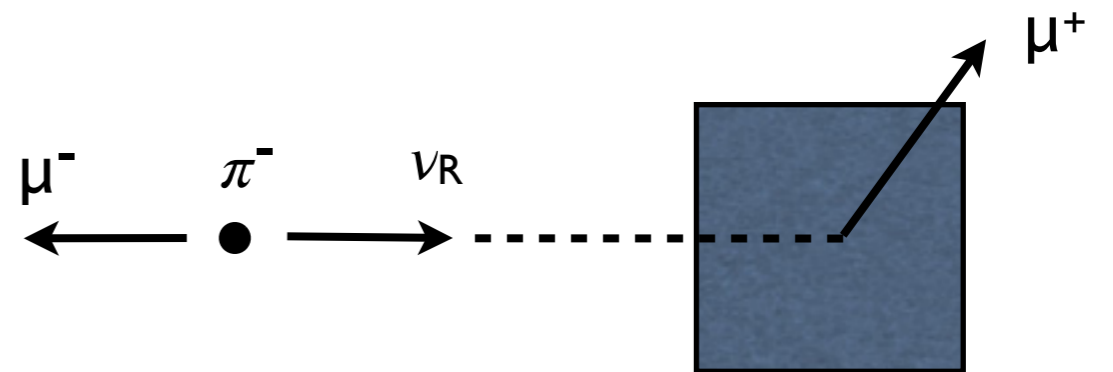
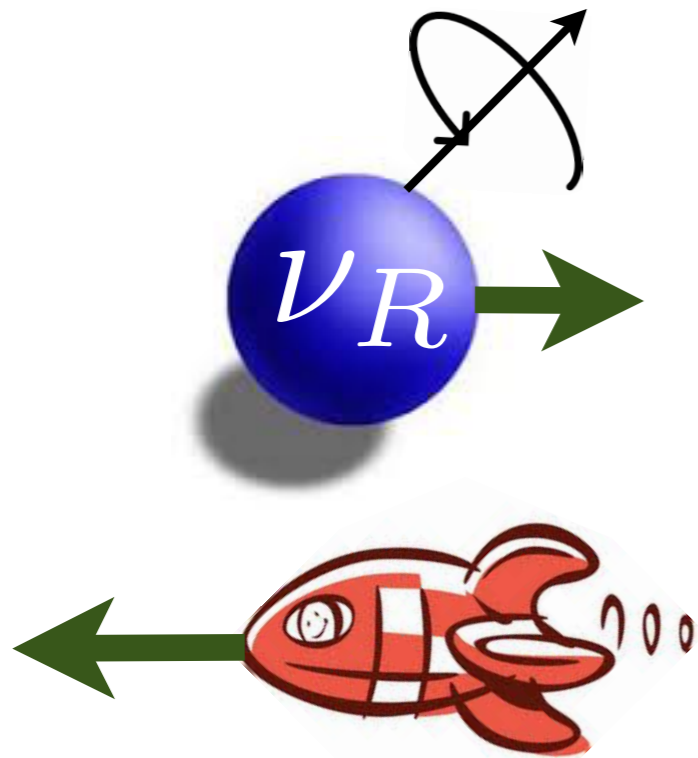
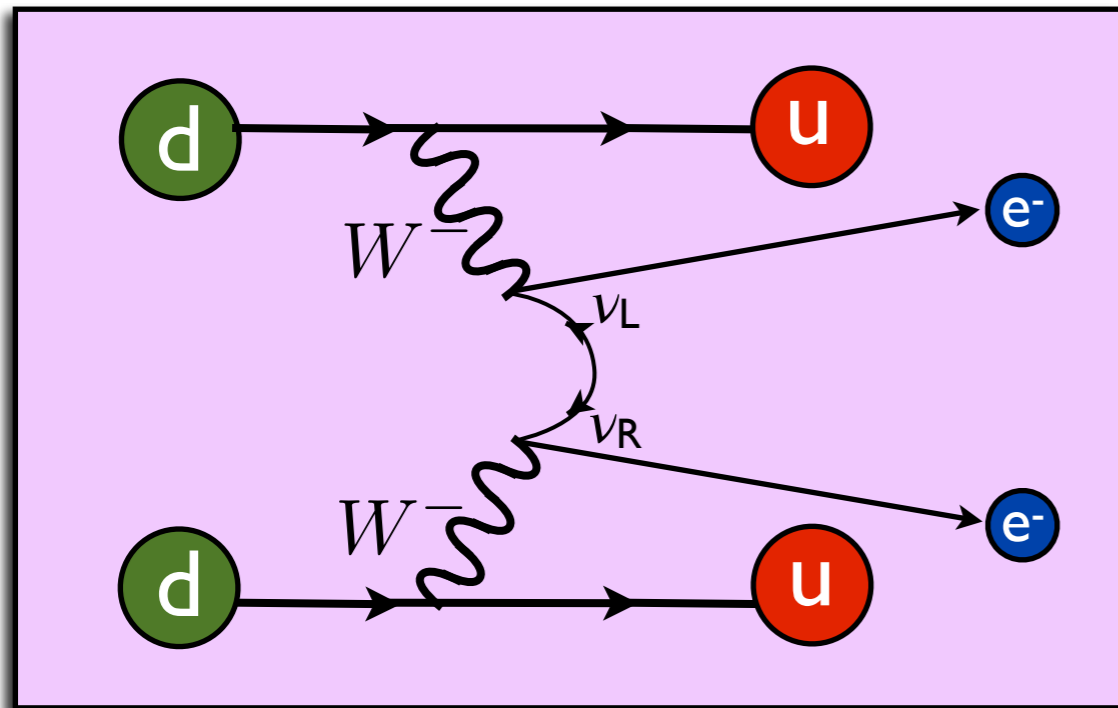
Neutrinos & Symmetries



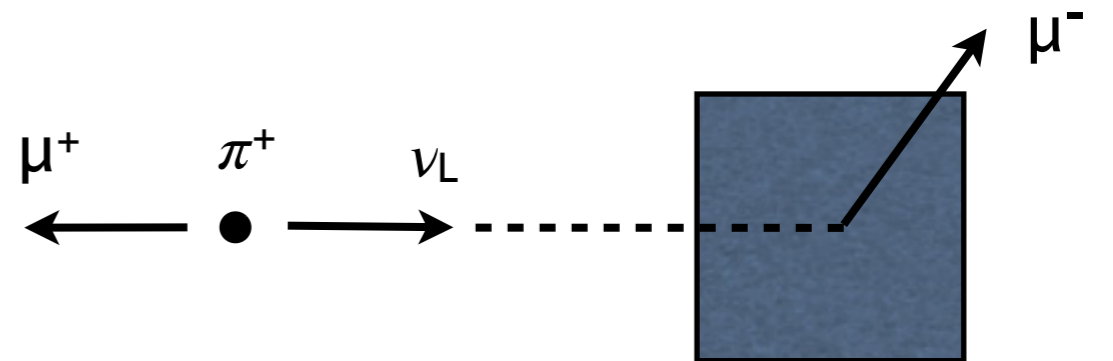
Neutrinos produced in π^- decays always produce μ^+



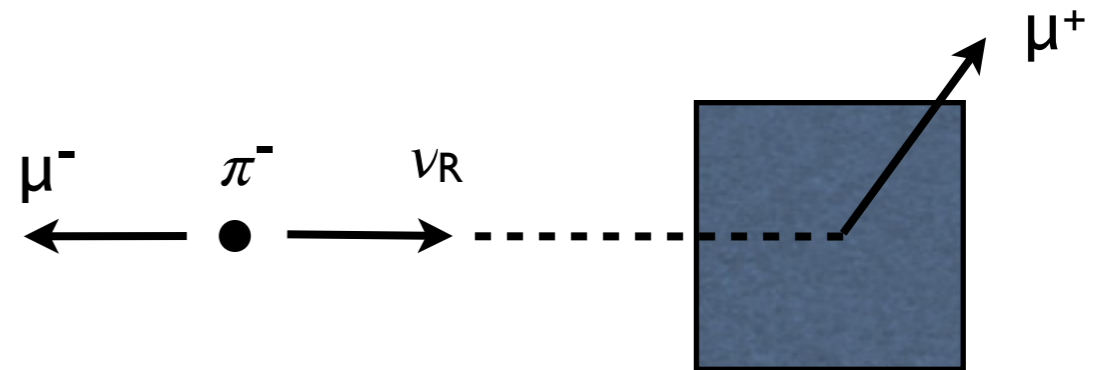
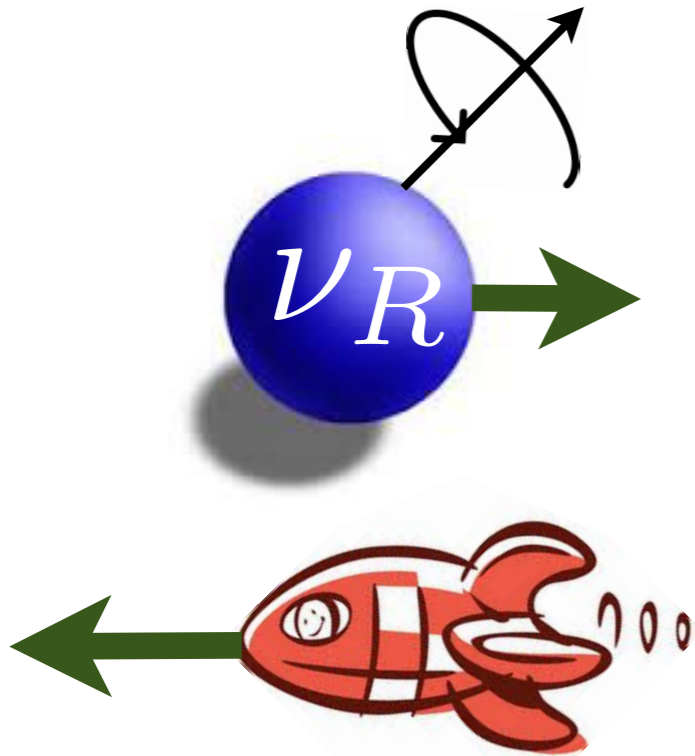
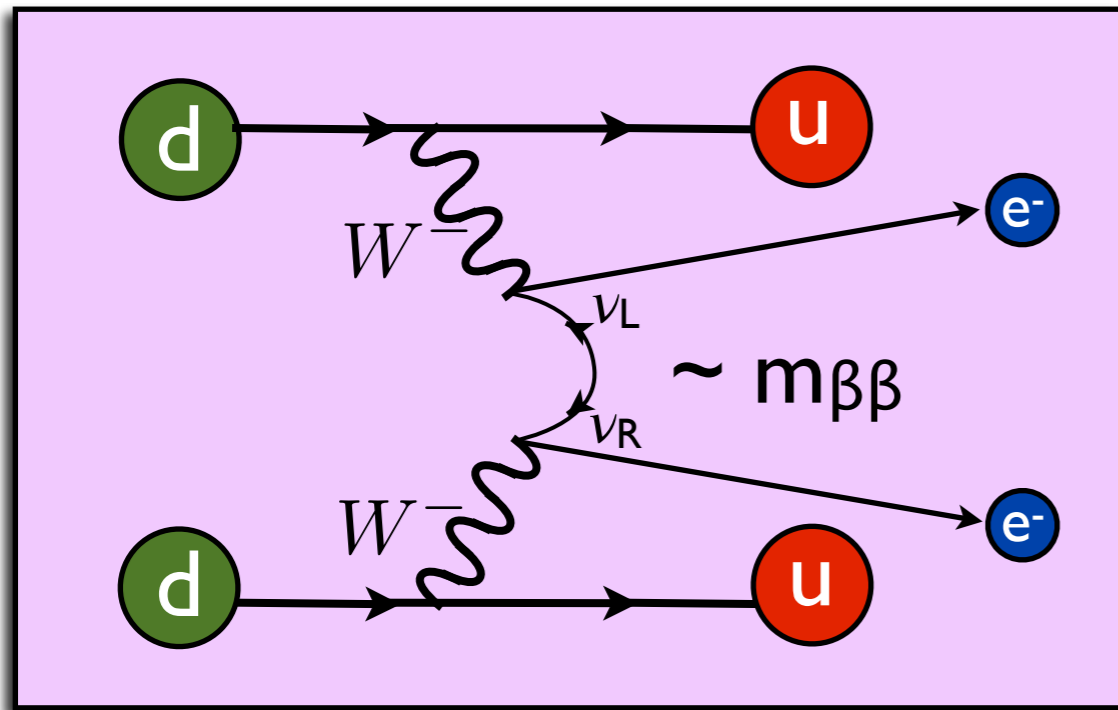
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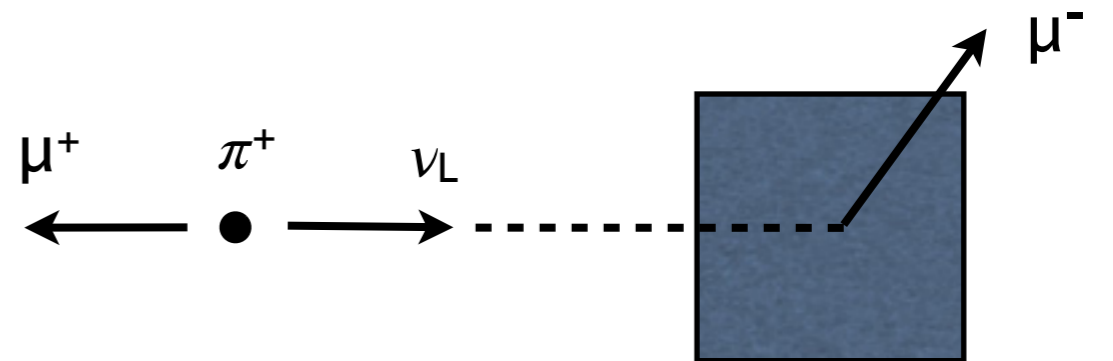
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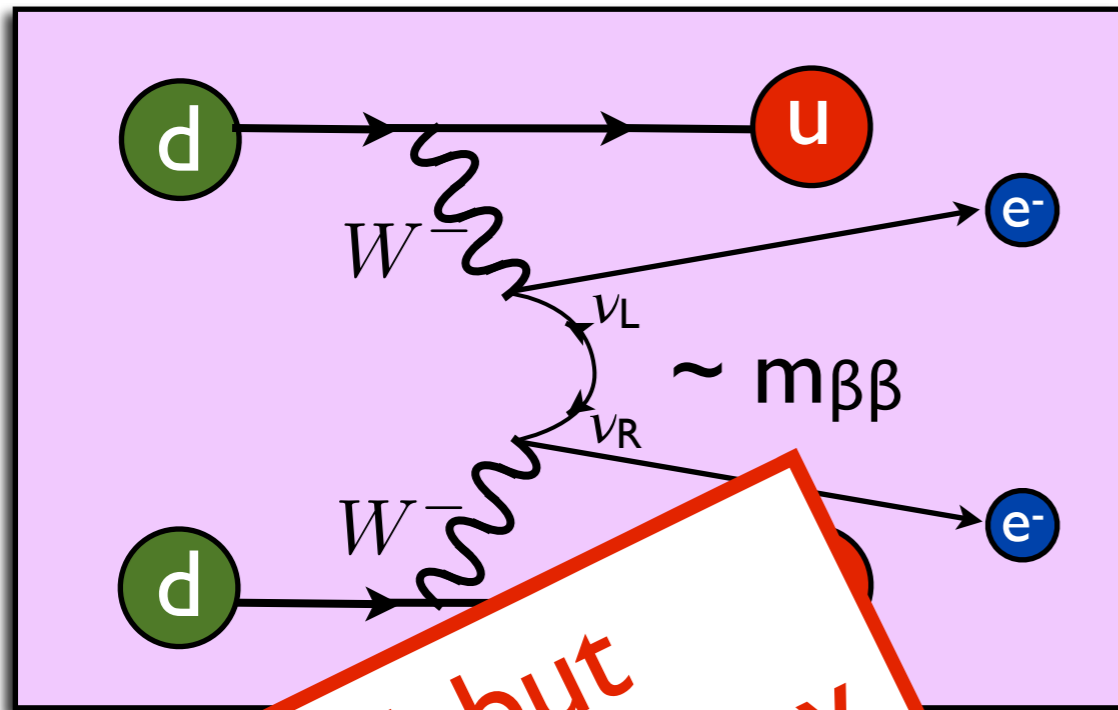
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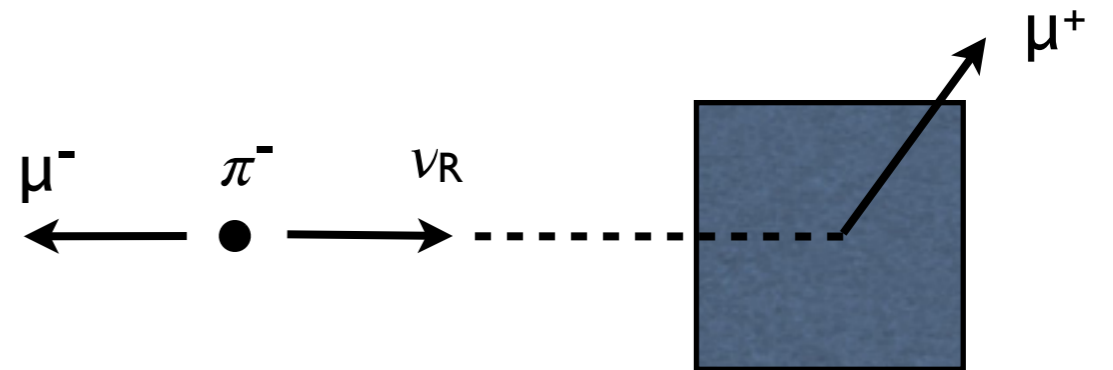
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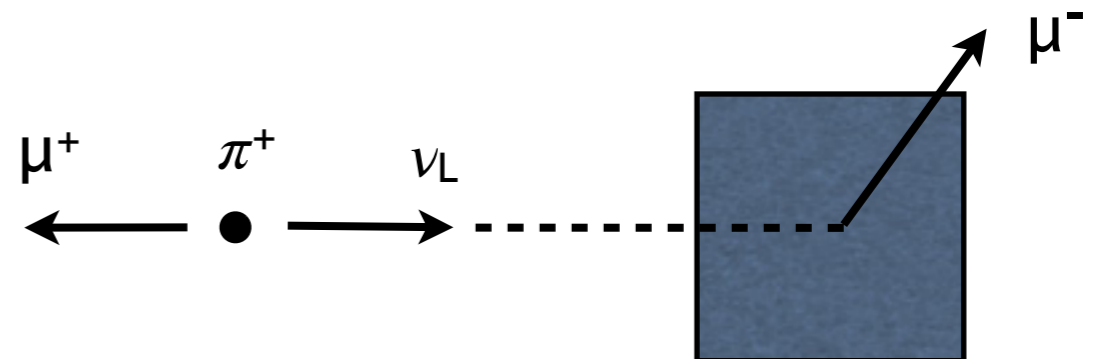
Neutrinos & Symmetries



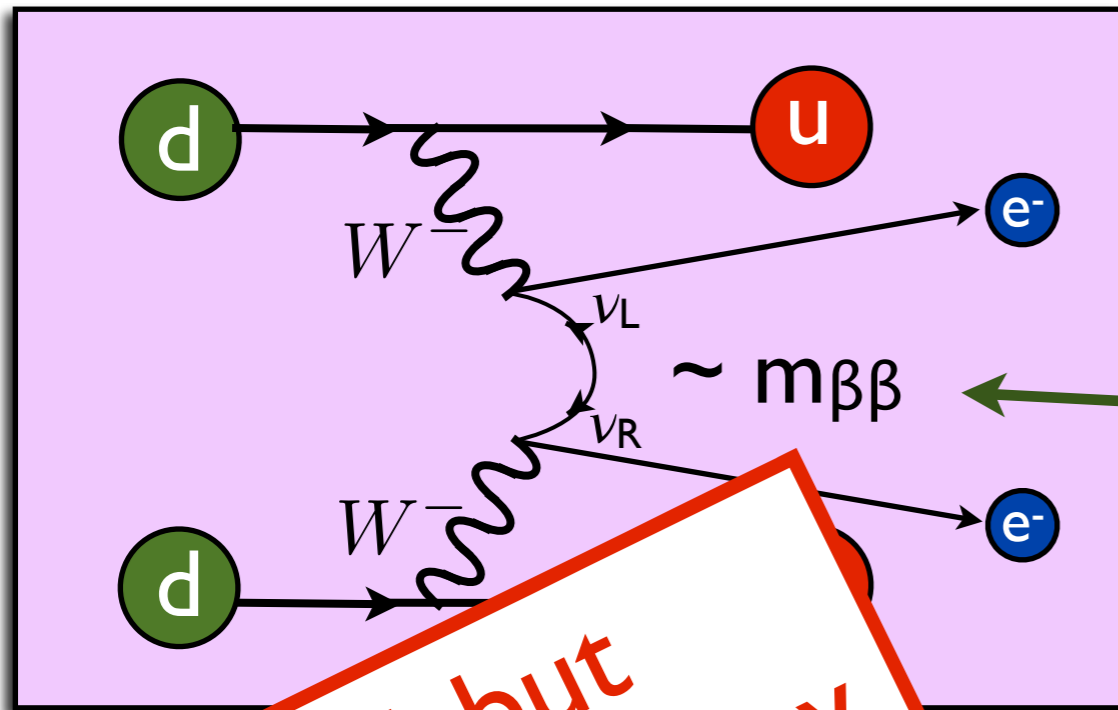
Allowed, but proportional to tiny (Majorana) mass!



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Neutrinos & Symmetries

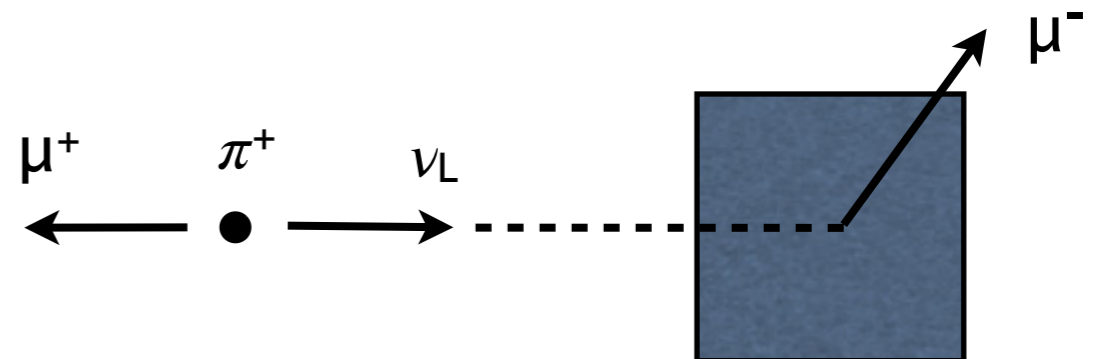


oscillation experiments
don't tell us absolute
mass scale -
 $0\nu\beta\beta$ will!

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proportional to tiny
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produce μ^+

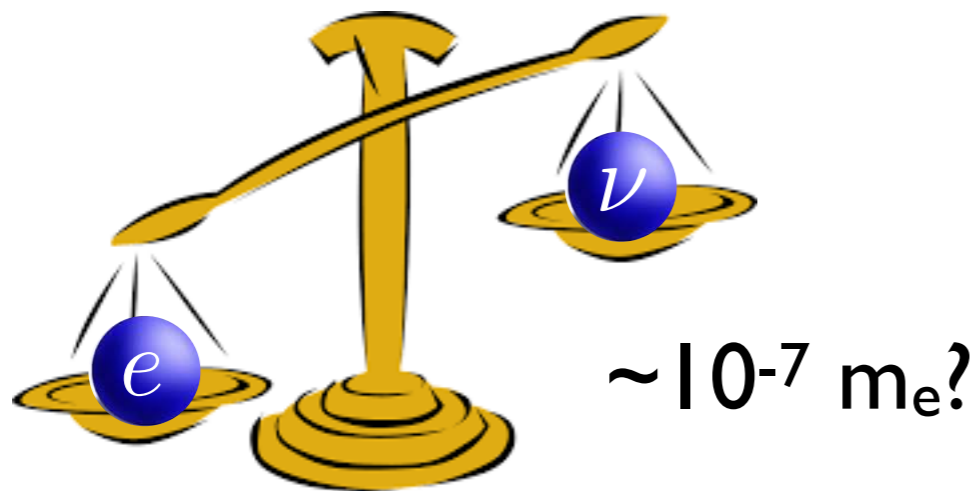


Why Majorana?

- Anything not forbidden by symmetry should occur in nature

$$\mathcal{L}_5 = \frac{c}{\Lambda} \left(\bar{L} \tilde{H} \right) \left(\tilde{H} L \right)^\dagger$$

- Why are neutrinos so light?

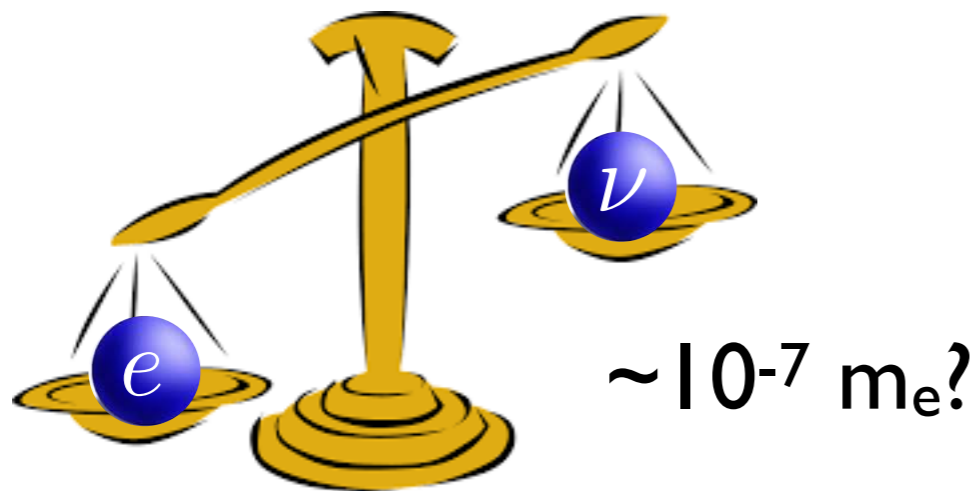


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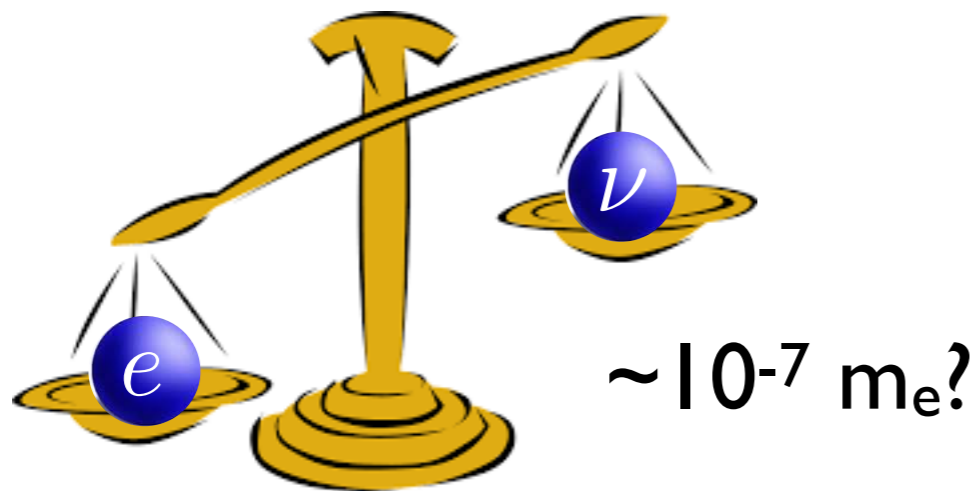
Seesaw Mechanism

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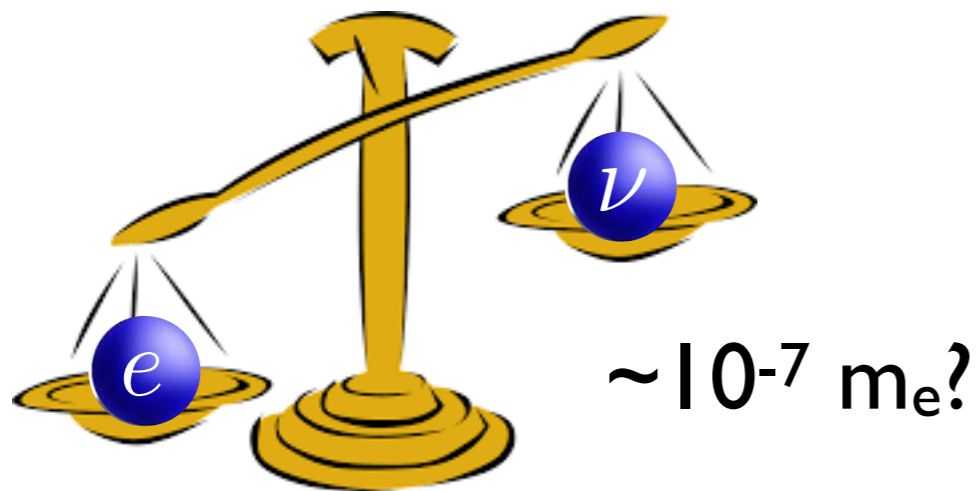
$$\begin{pmatrix} M_L & M_D \\ M_D & M_R \end{pmatrix}$$

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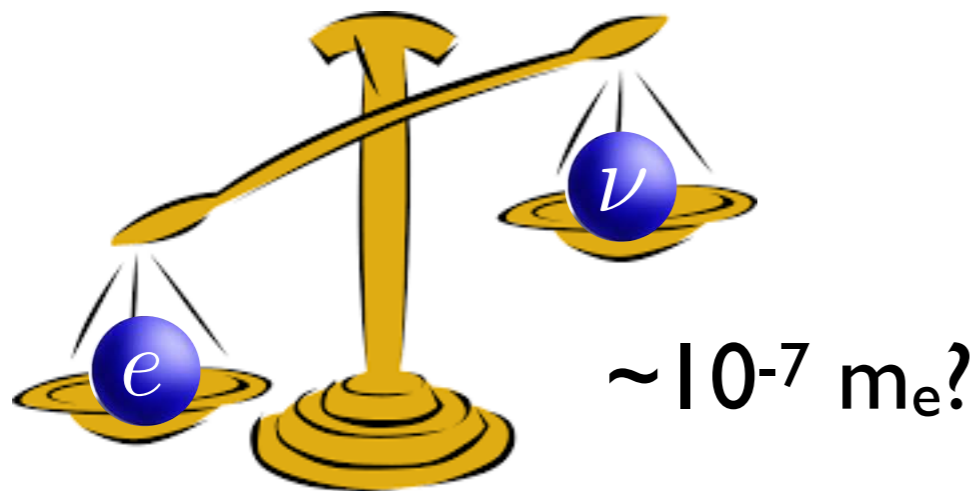
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Seesaw Mechanism

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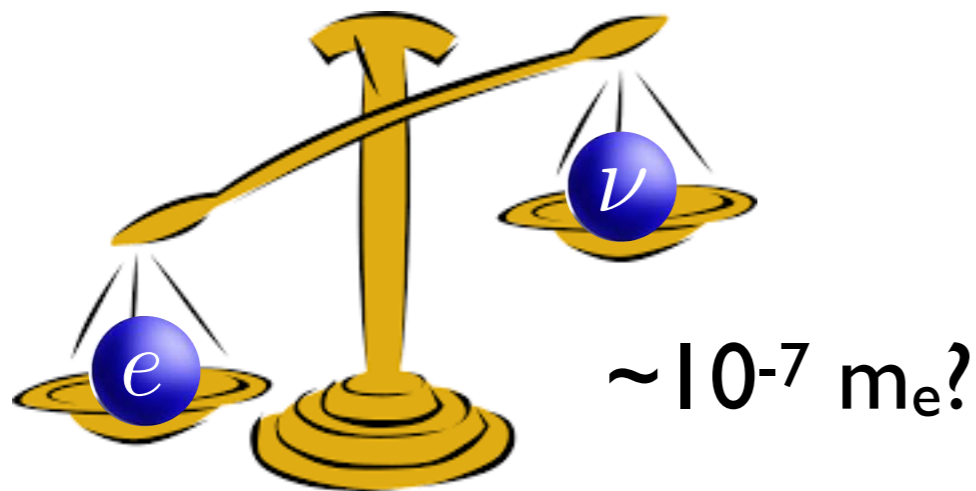
$$m_l \sim M_D^2 / M_R$$

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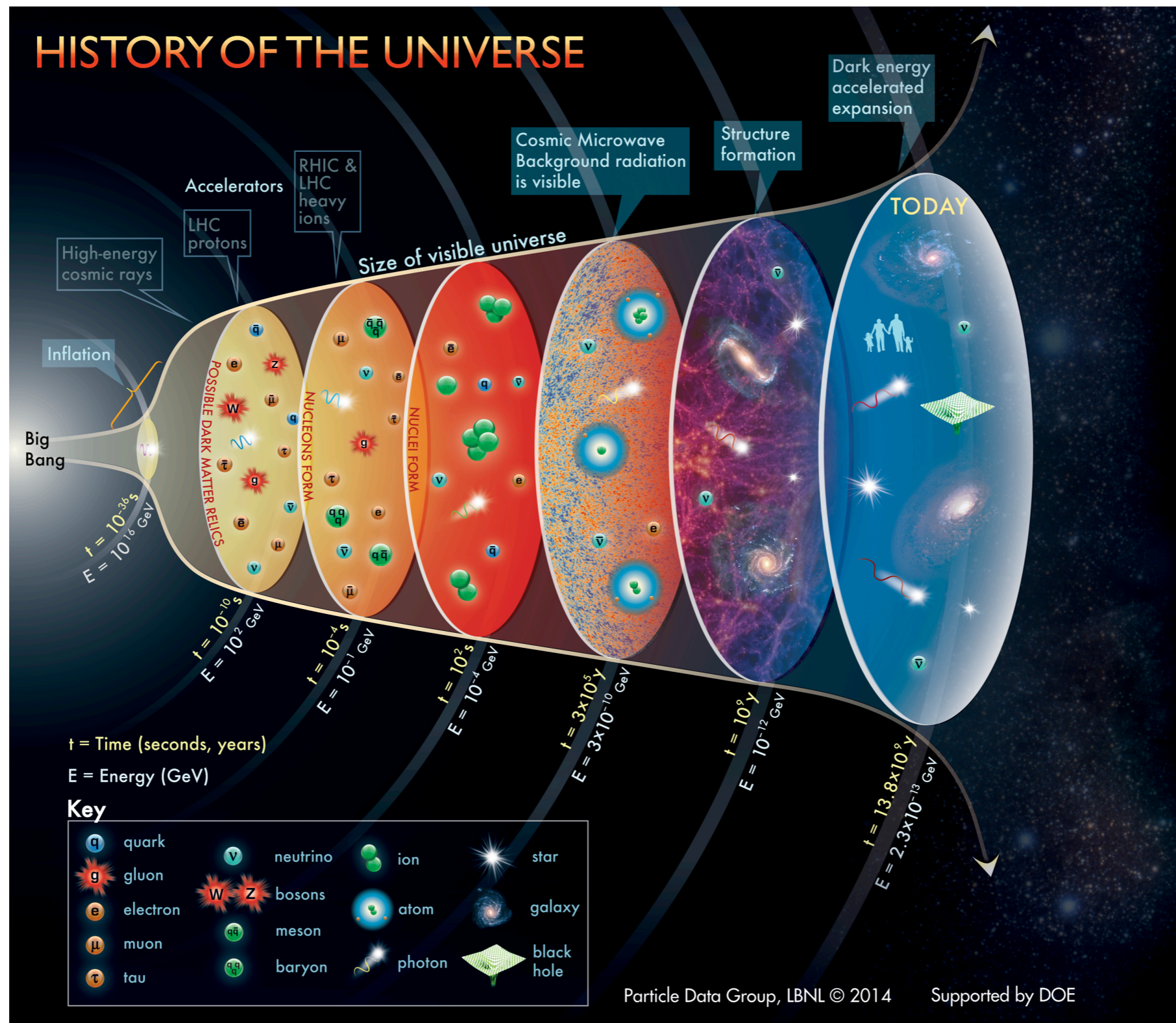
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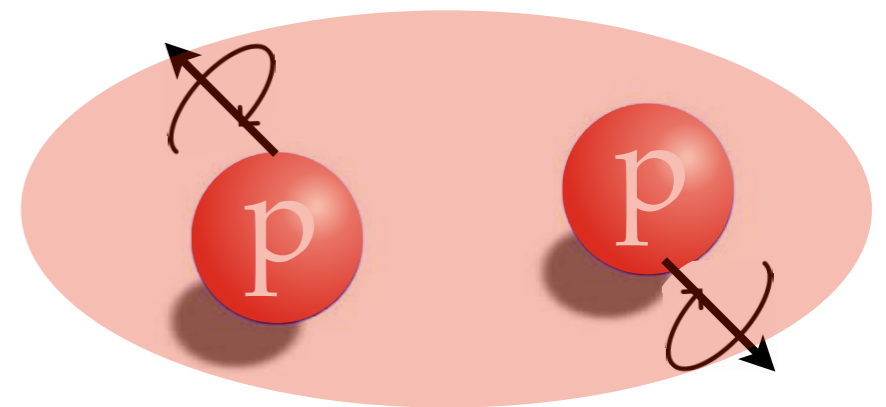
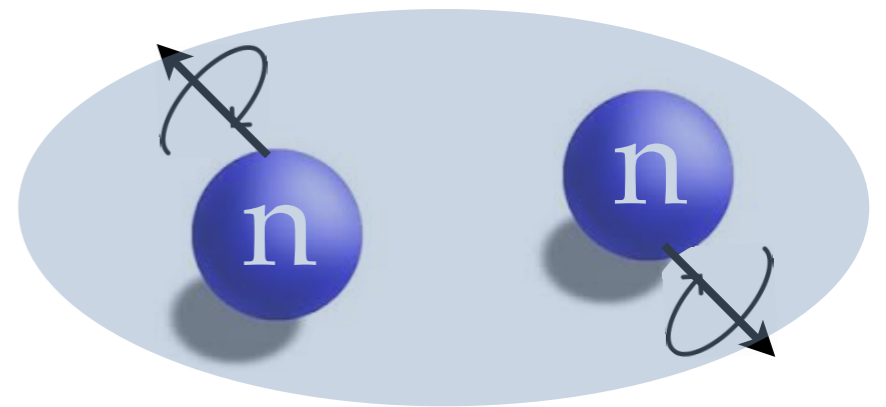
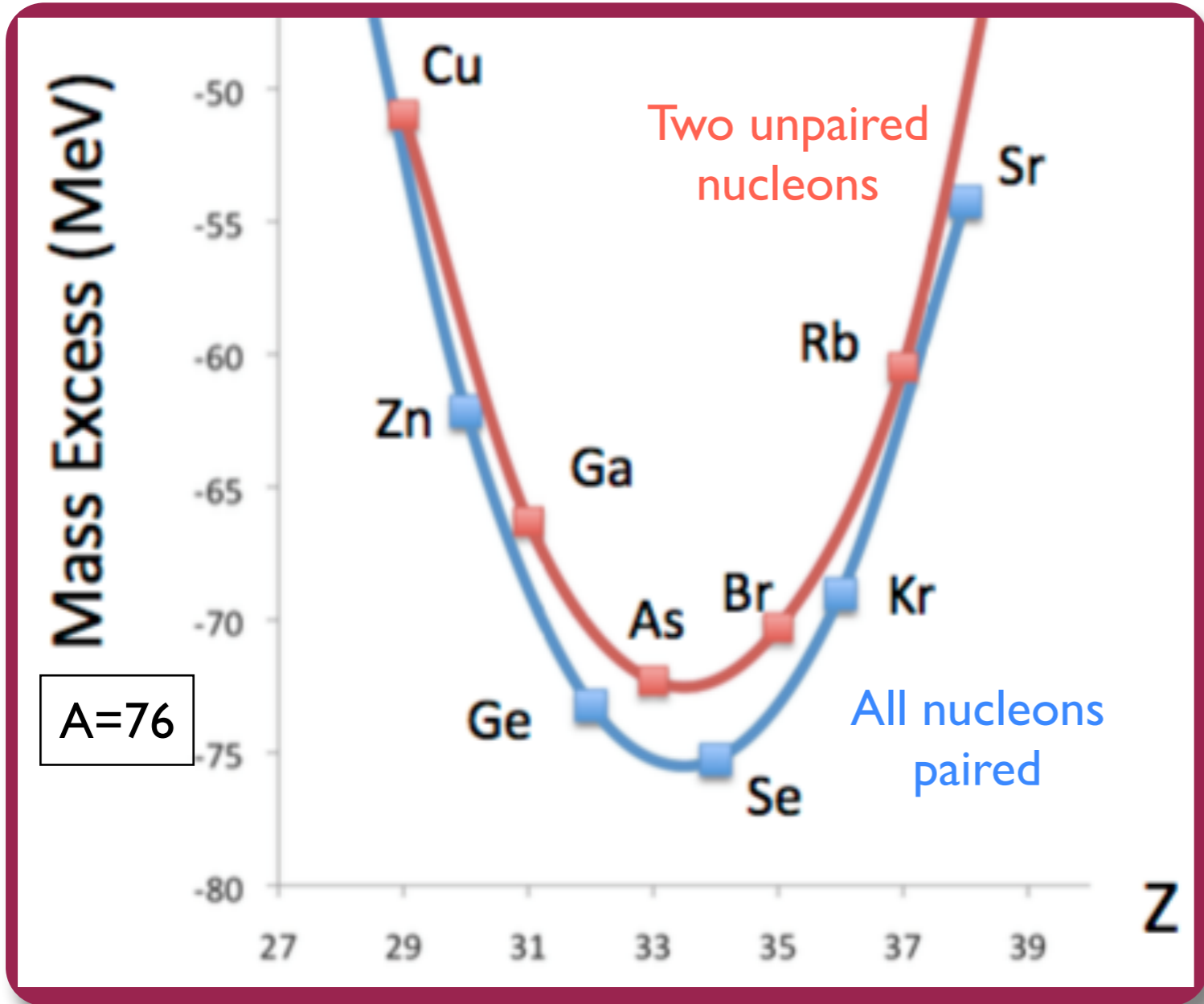
$$m_h \sim M_R$$

If observed, could help explain matter/anti-matter asymmetry in the universe!



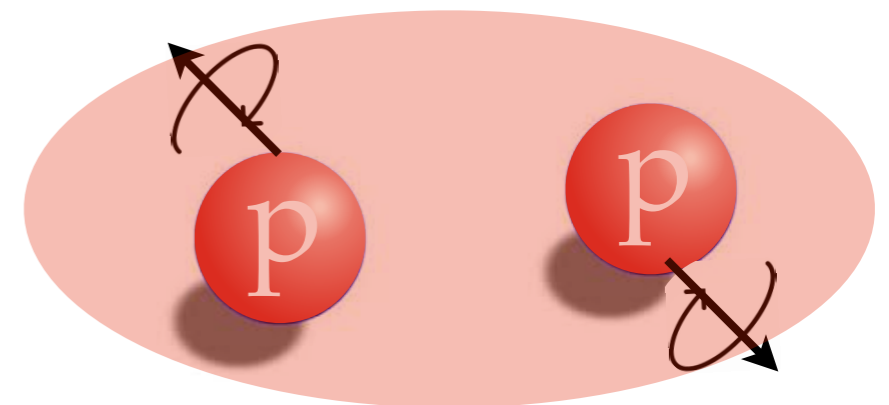
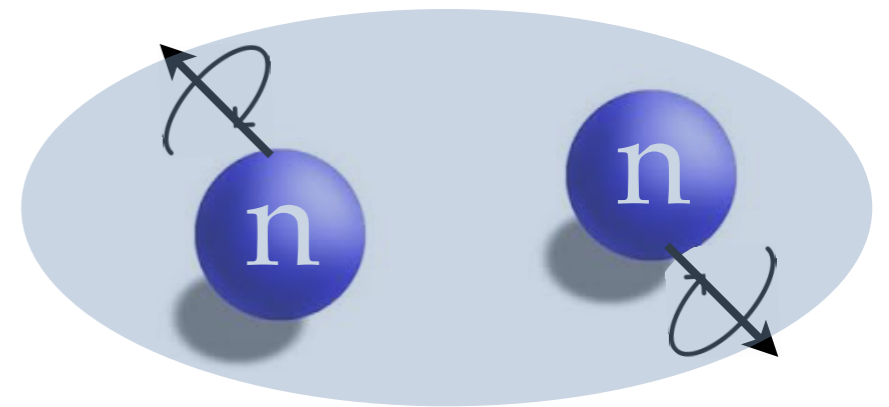
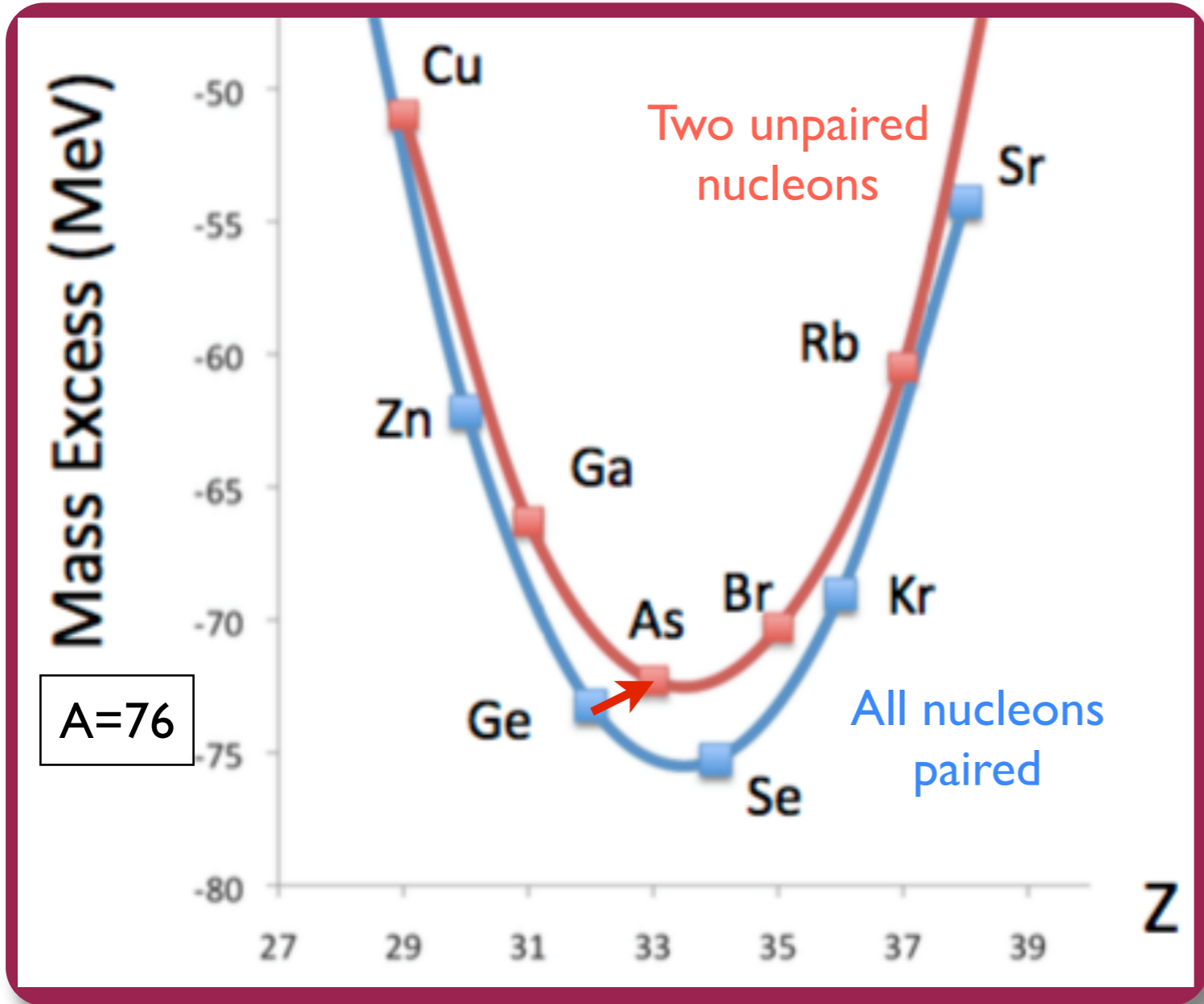
Experiment

Nuclear physics gives us a natural filter for the process



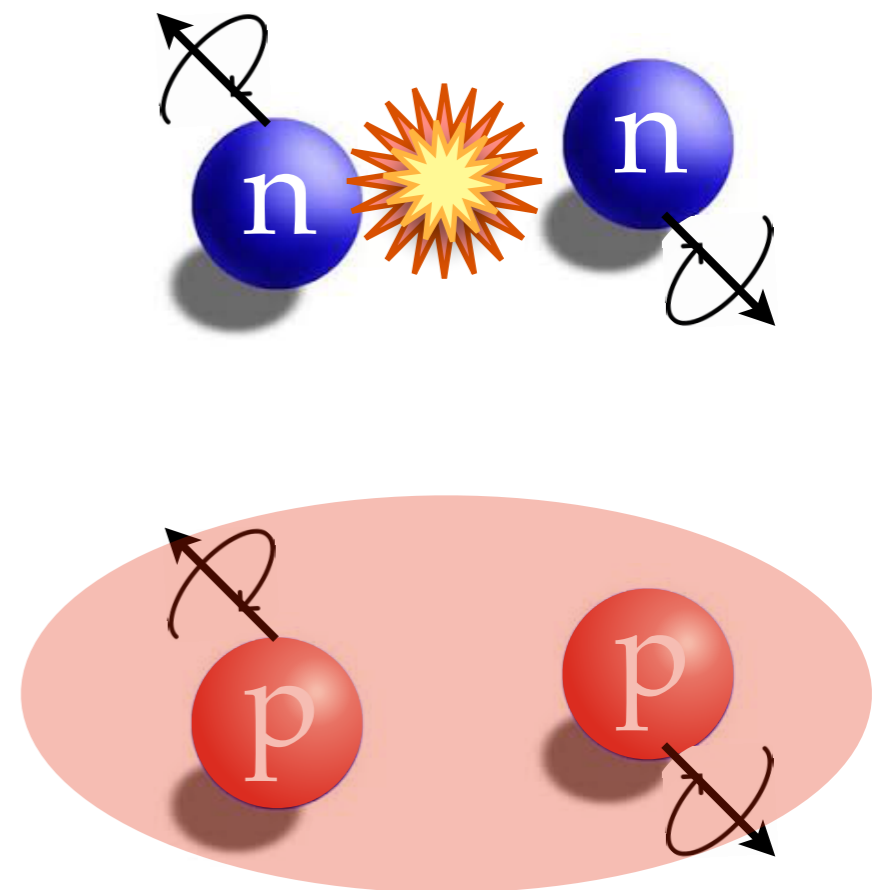
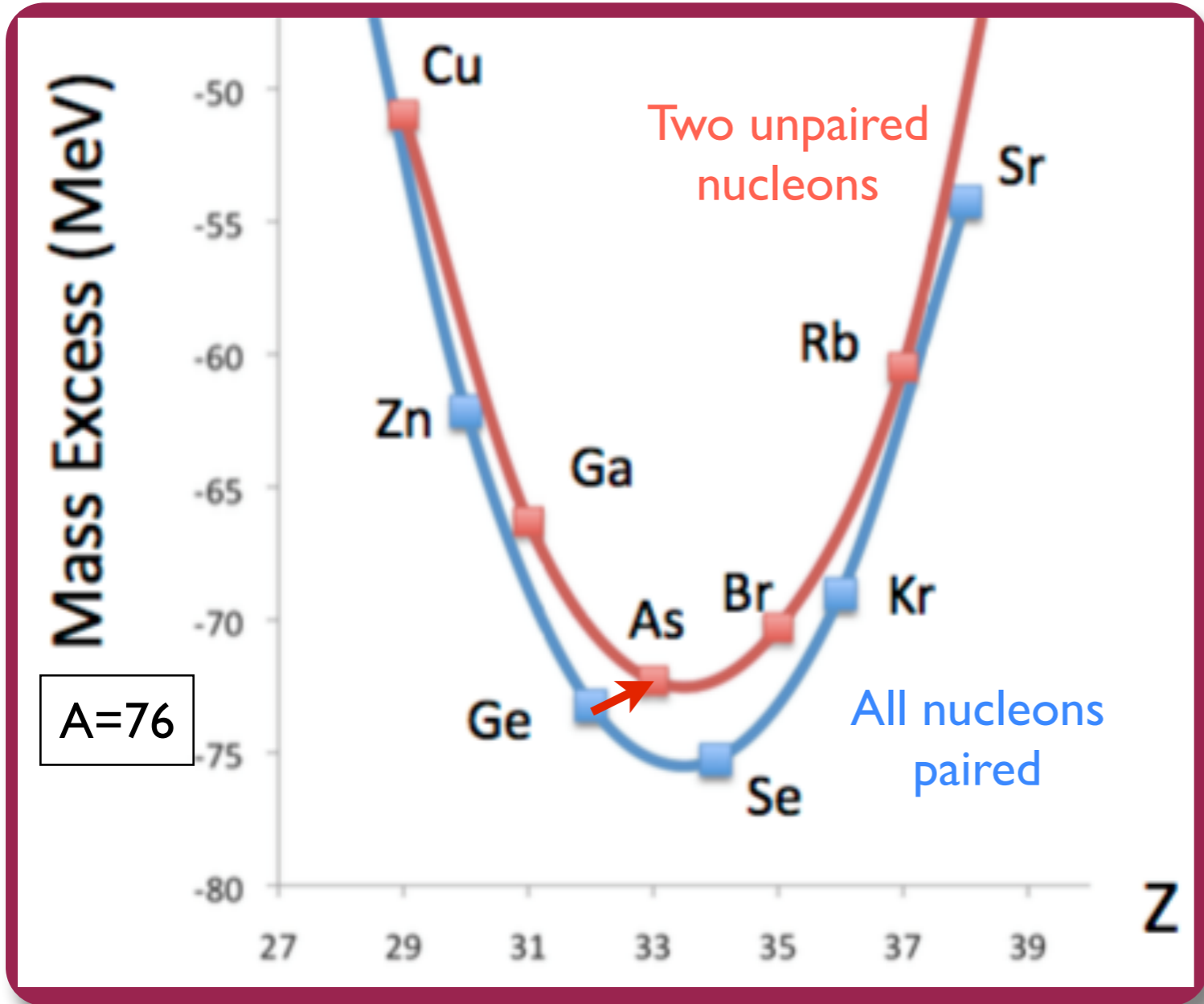
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Nuclear physics gives us a natural filter for the process



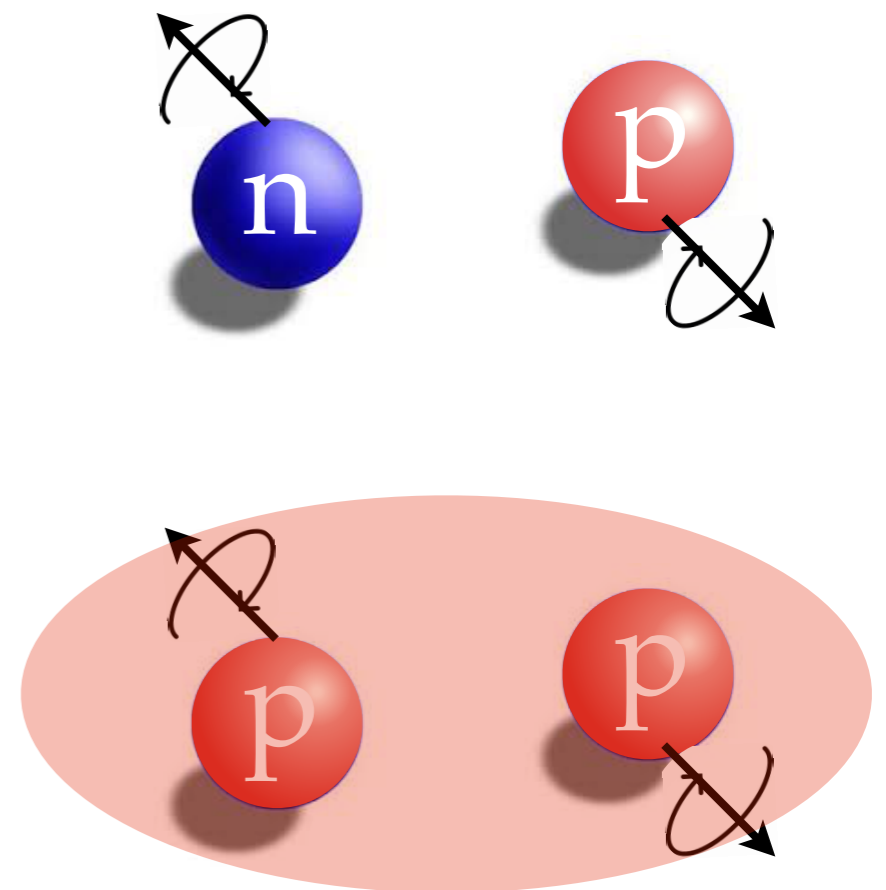
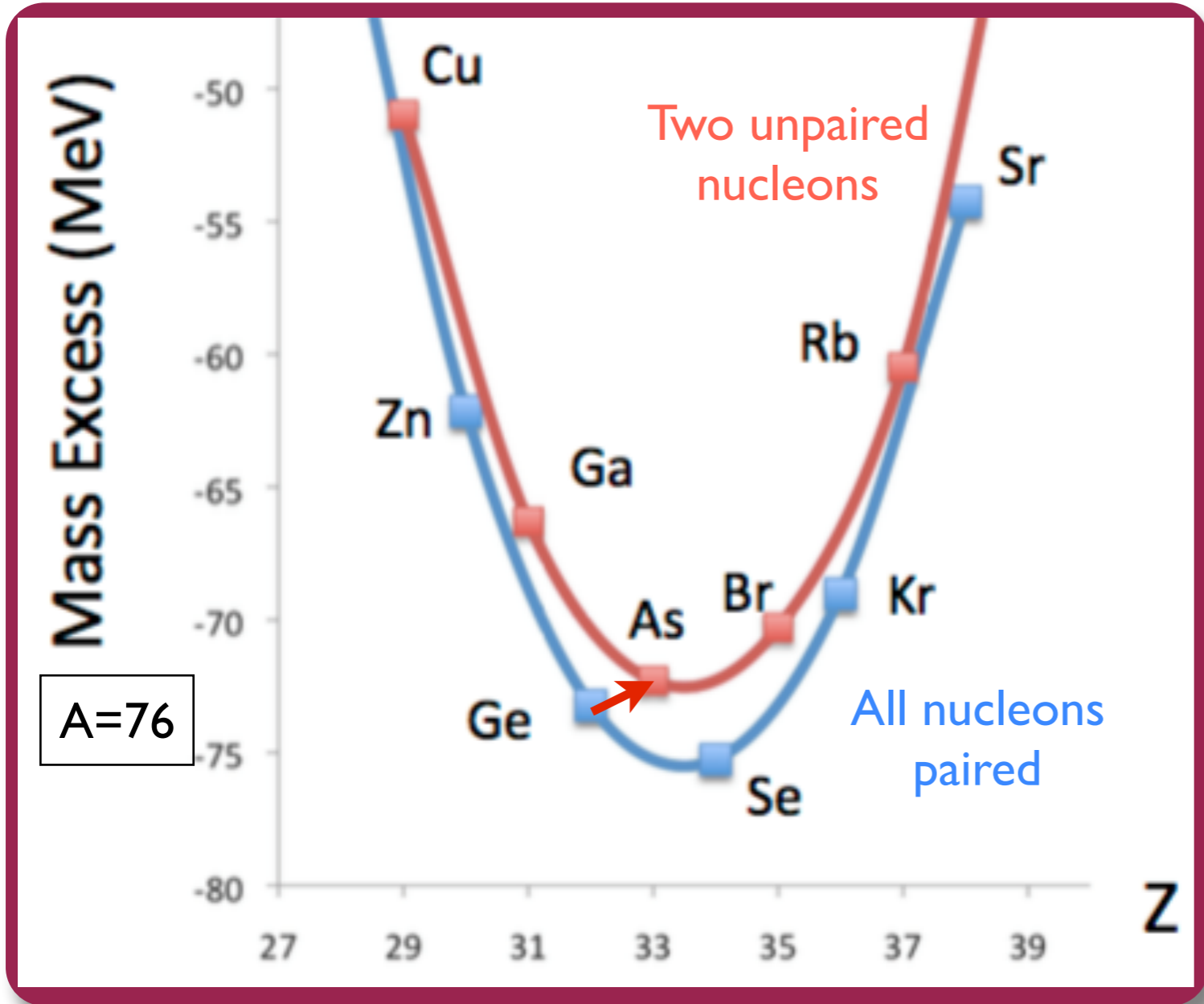
Experiment

Nuclear physics gives us a natural filter for the process



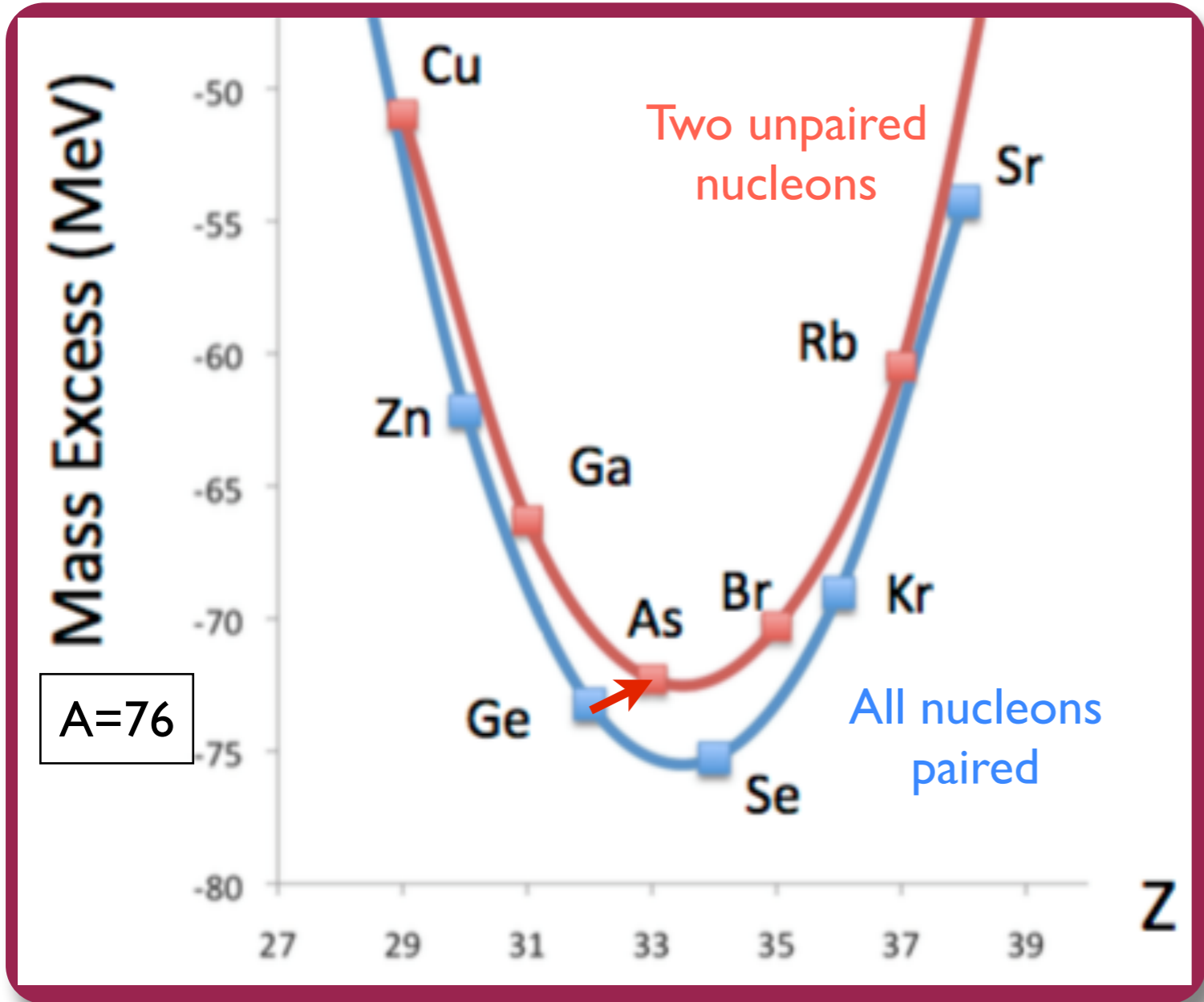
Experiment

Nuclear physics gives us a natural filter for the process

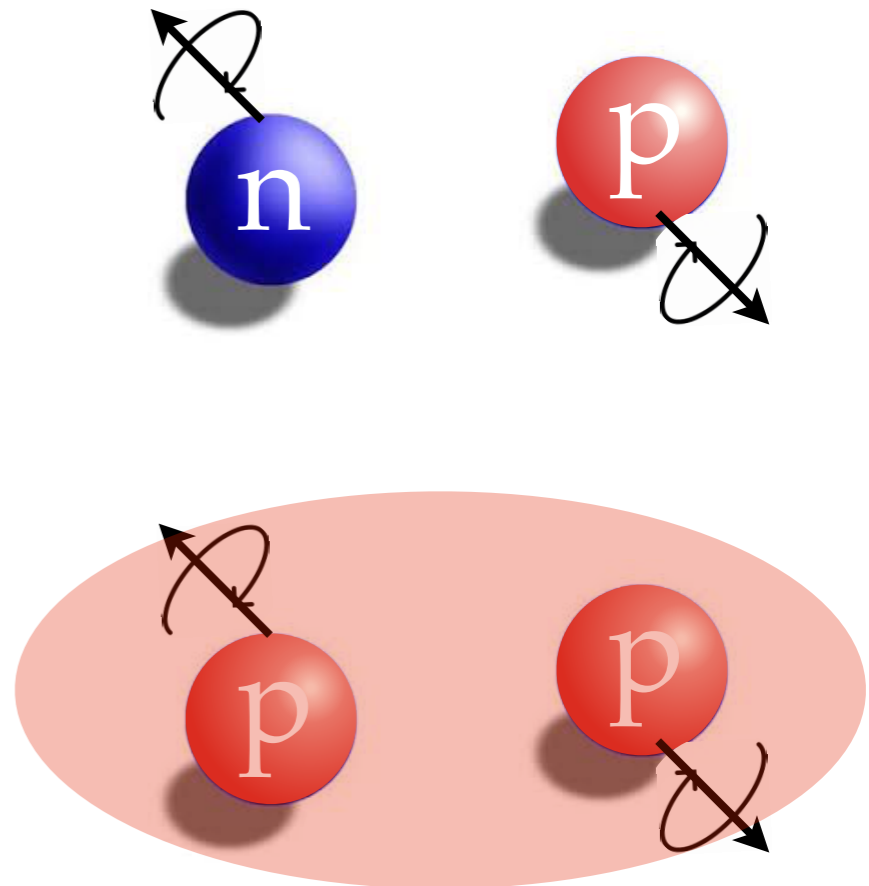


Experiment

Nuclear physics gives us a natural filter for the process

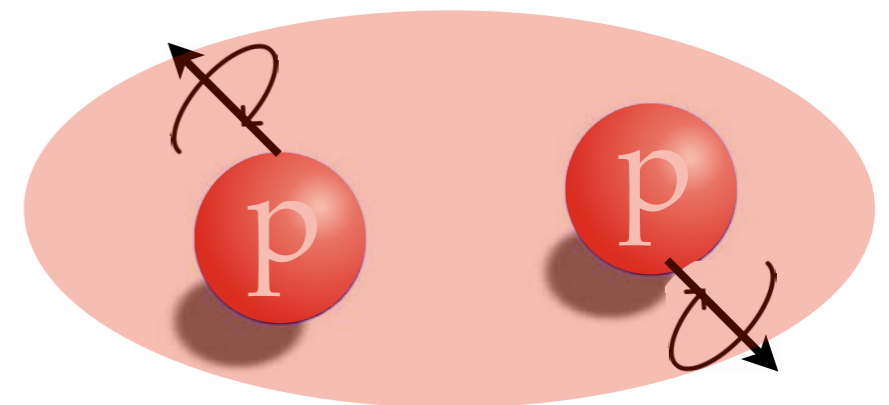
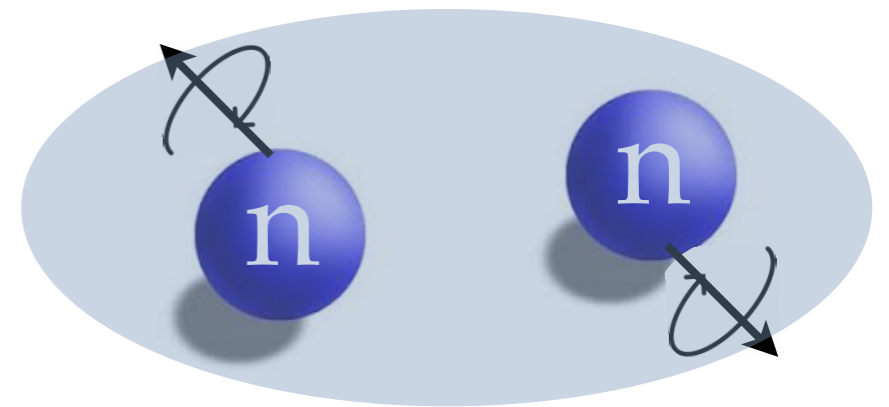
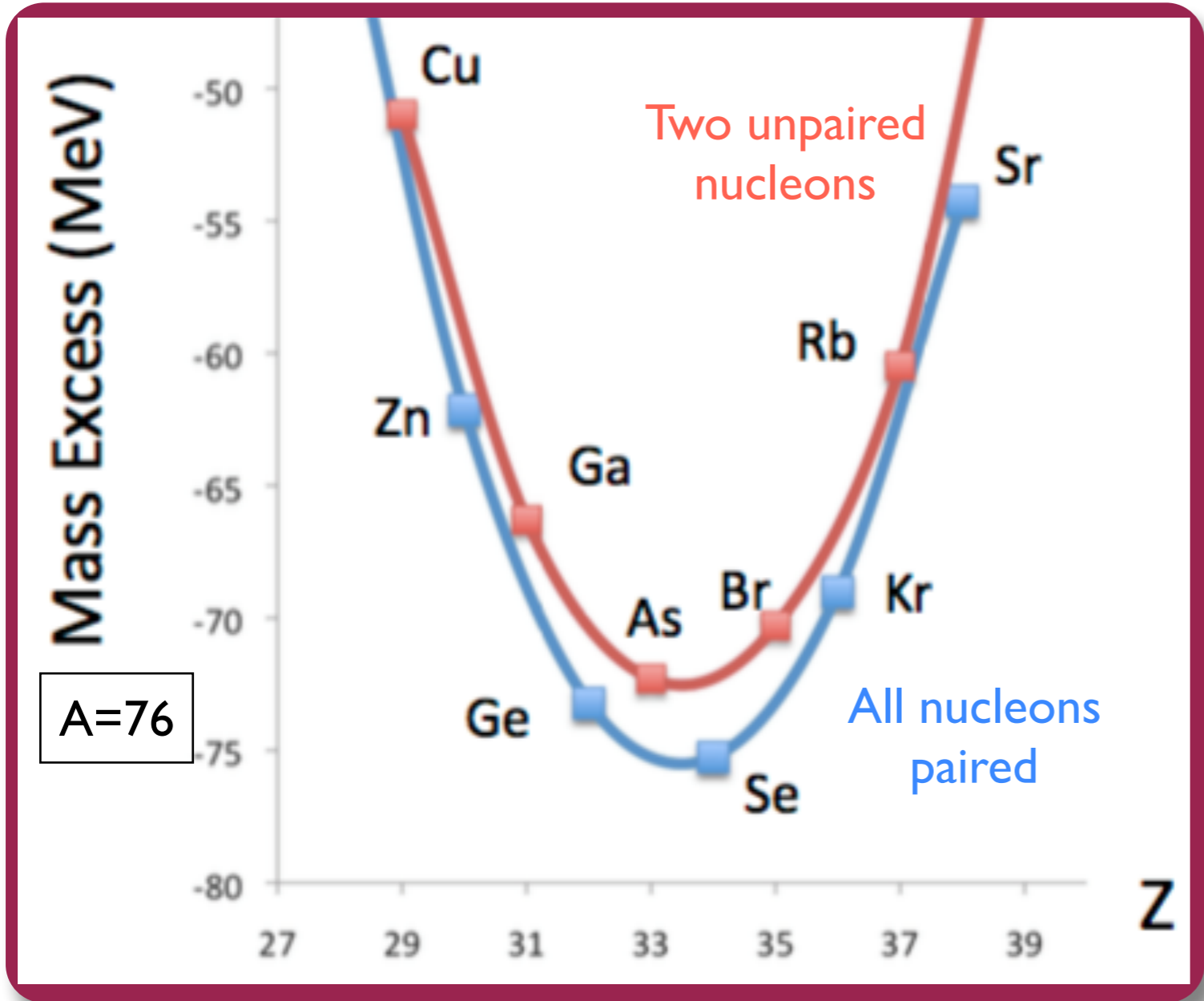


Energetically forbidden



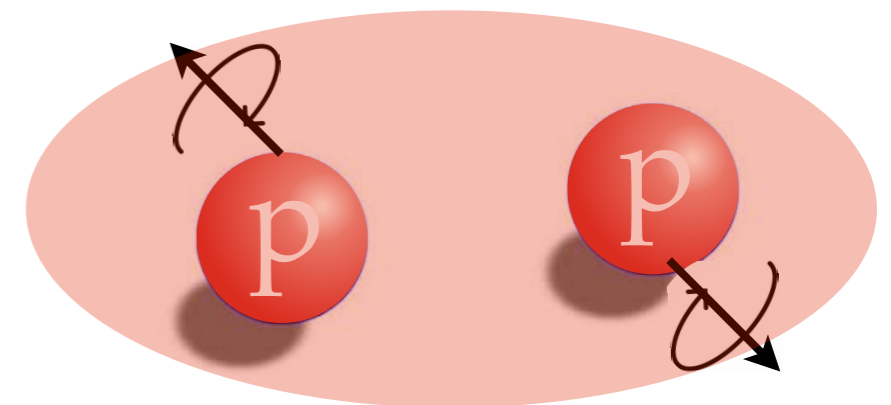
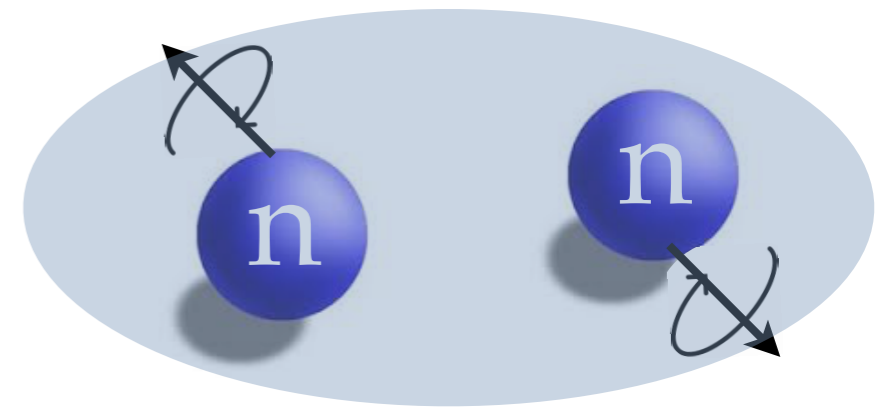
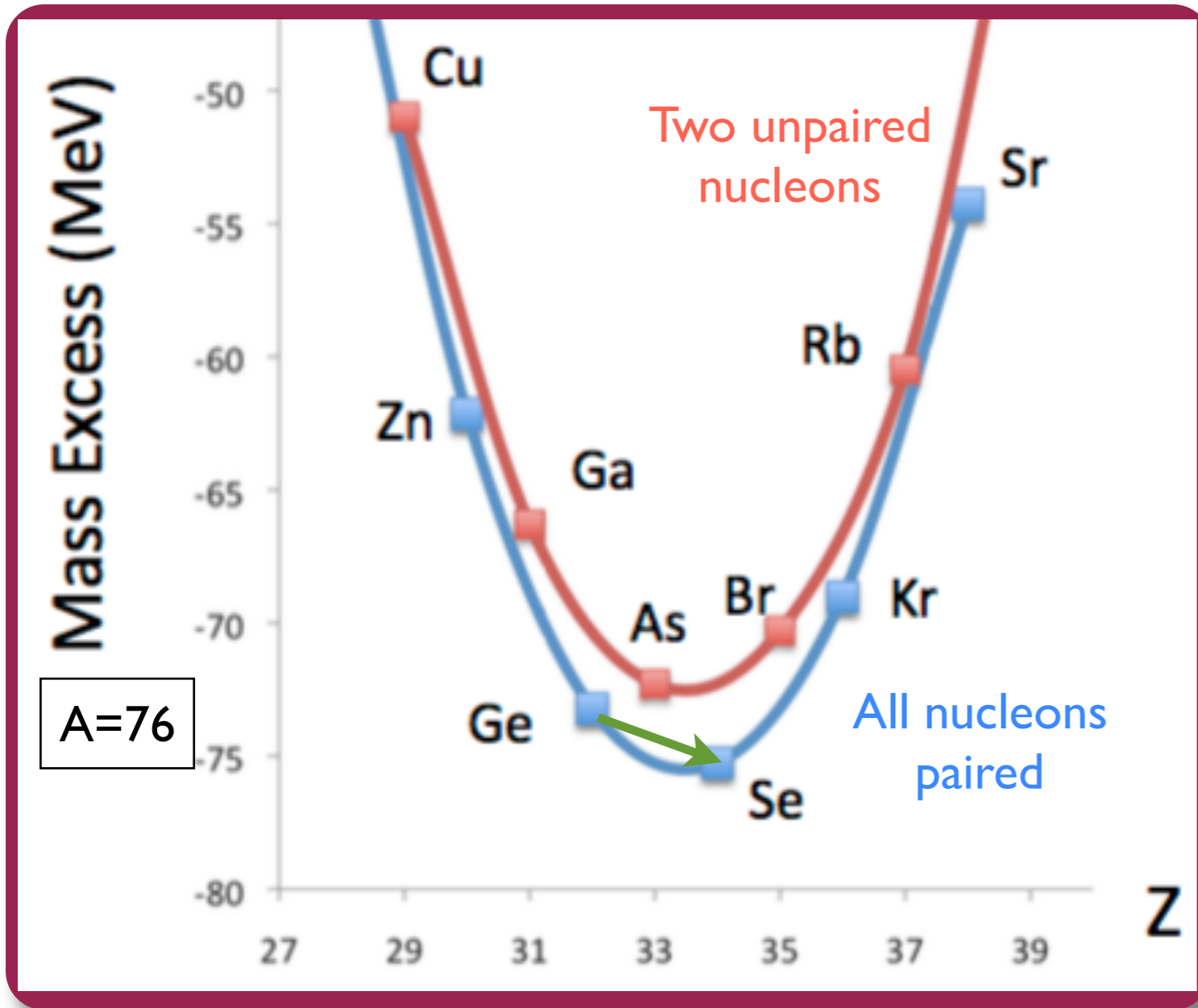
Experiment

Nuclear physics gives us a natural filter for the process



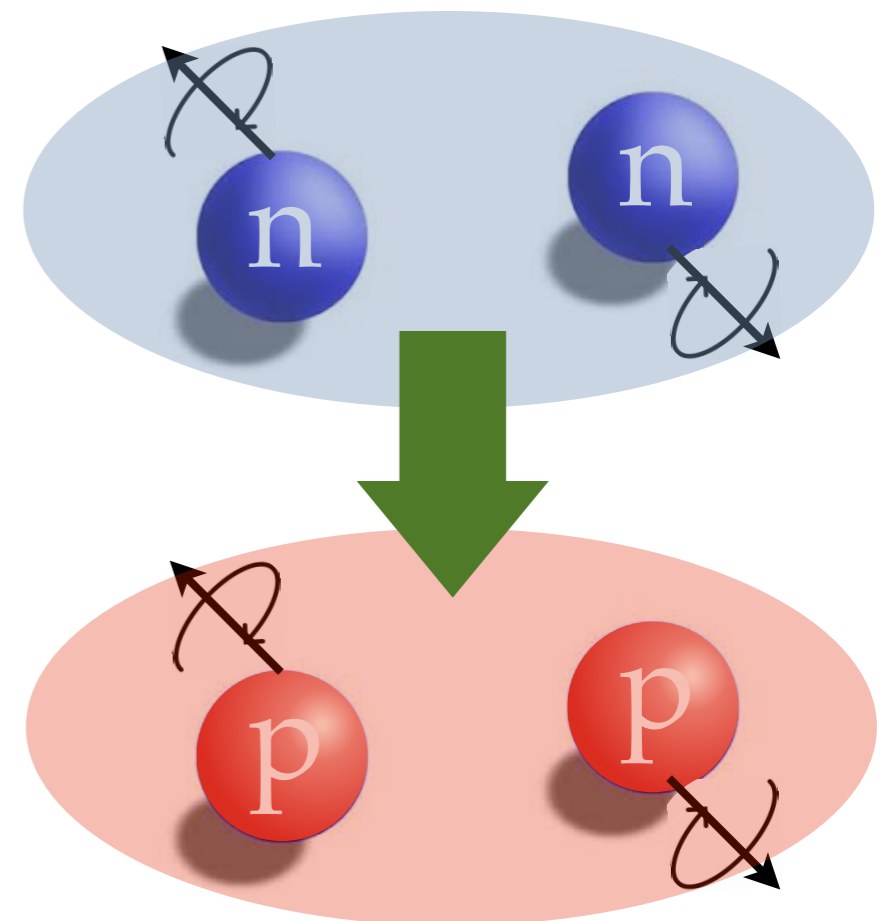
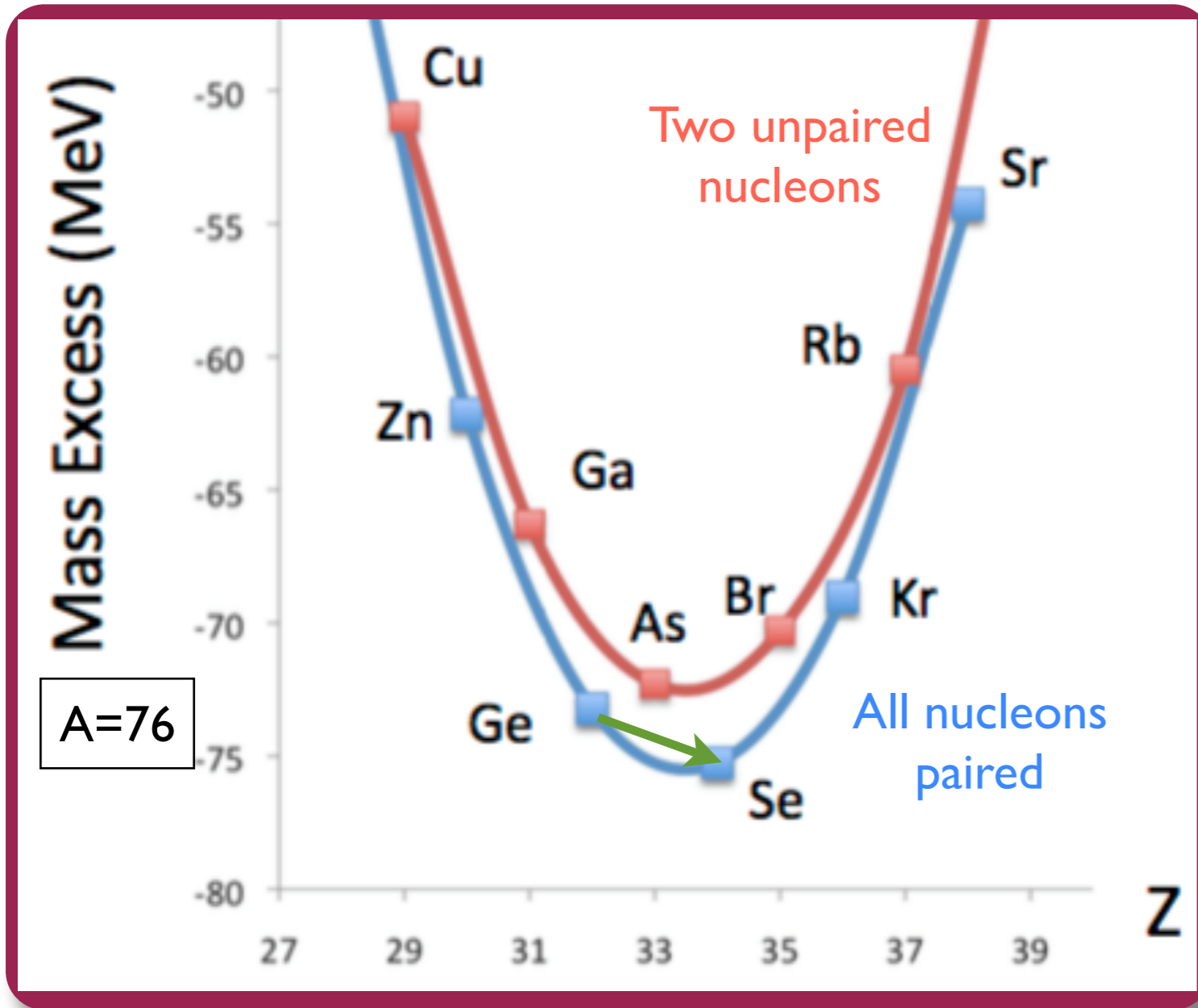
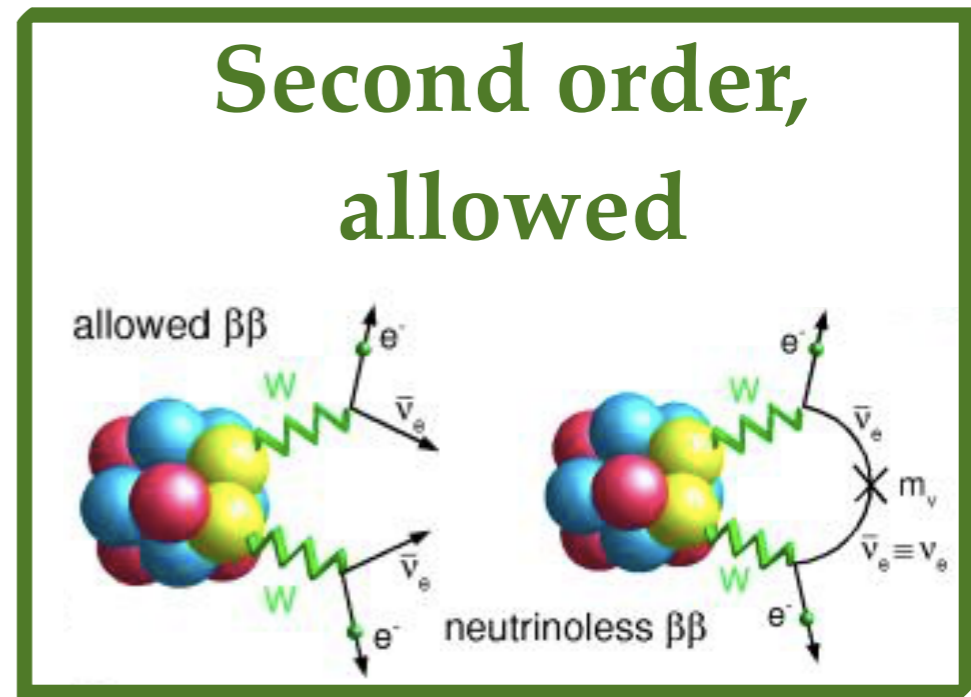
Experiment

Nuclear physics gives us a natural filter for the process



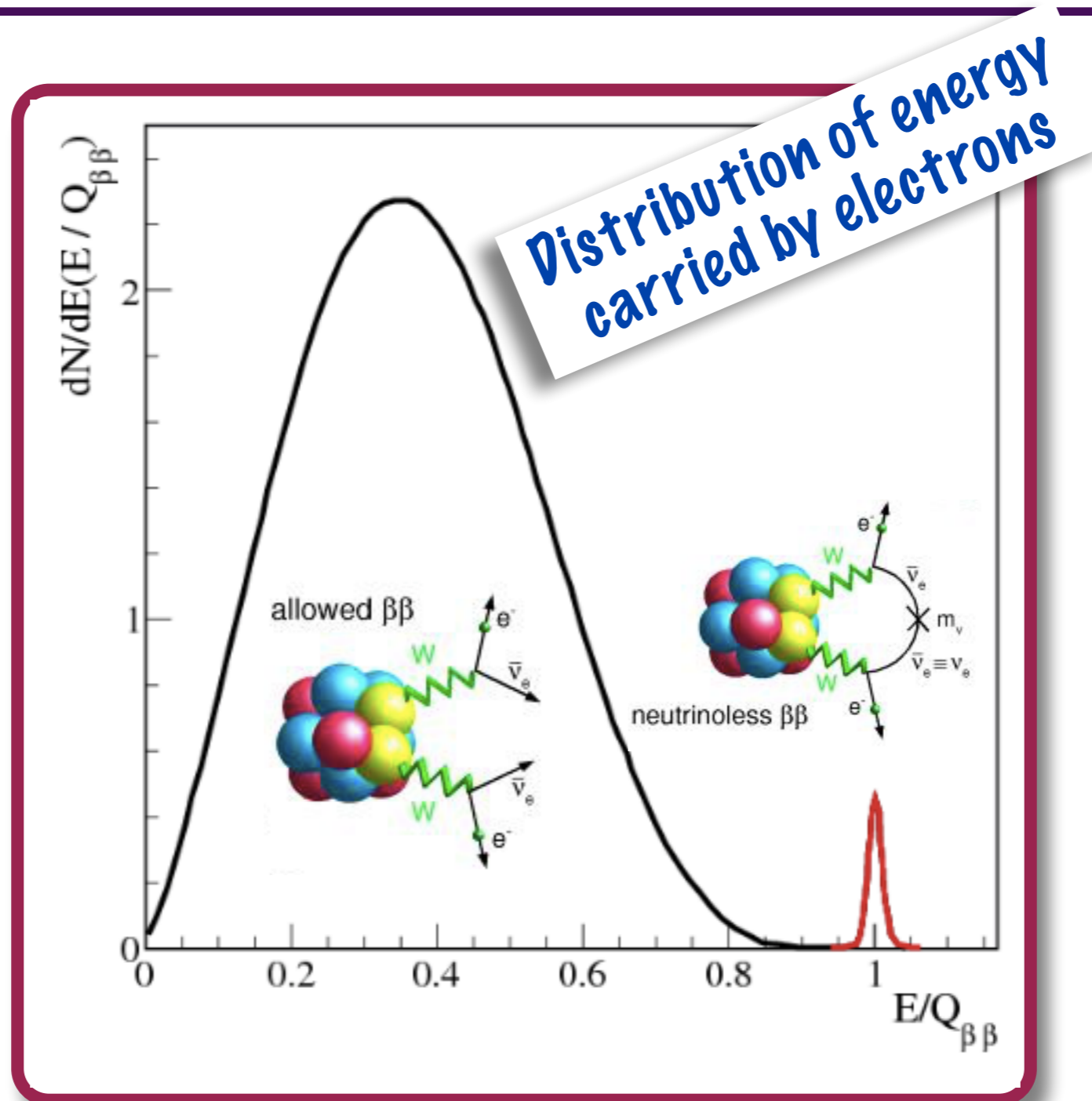
Experiment

Nuclear physics gives us a natural filter for the process



Experiment

Neutrinoless mode can be isolated using spectroscopic methods





Cuore
 ^{130}Te

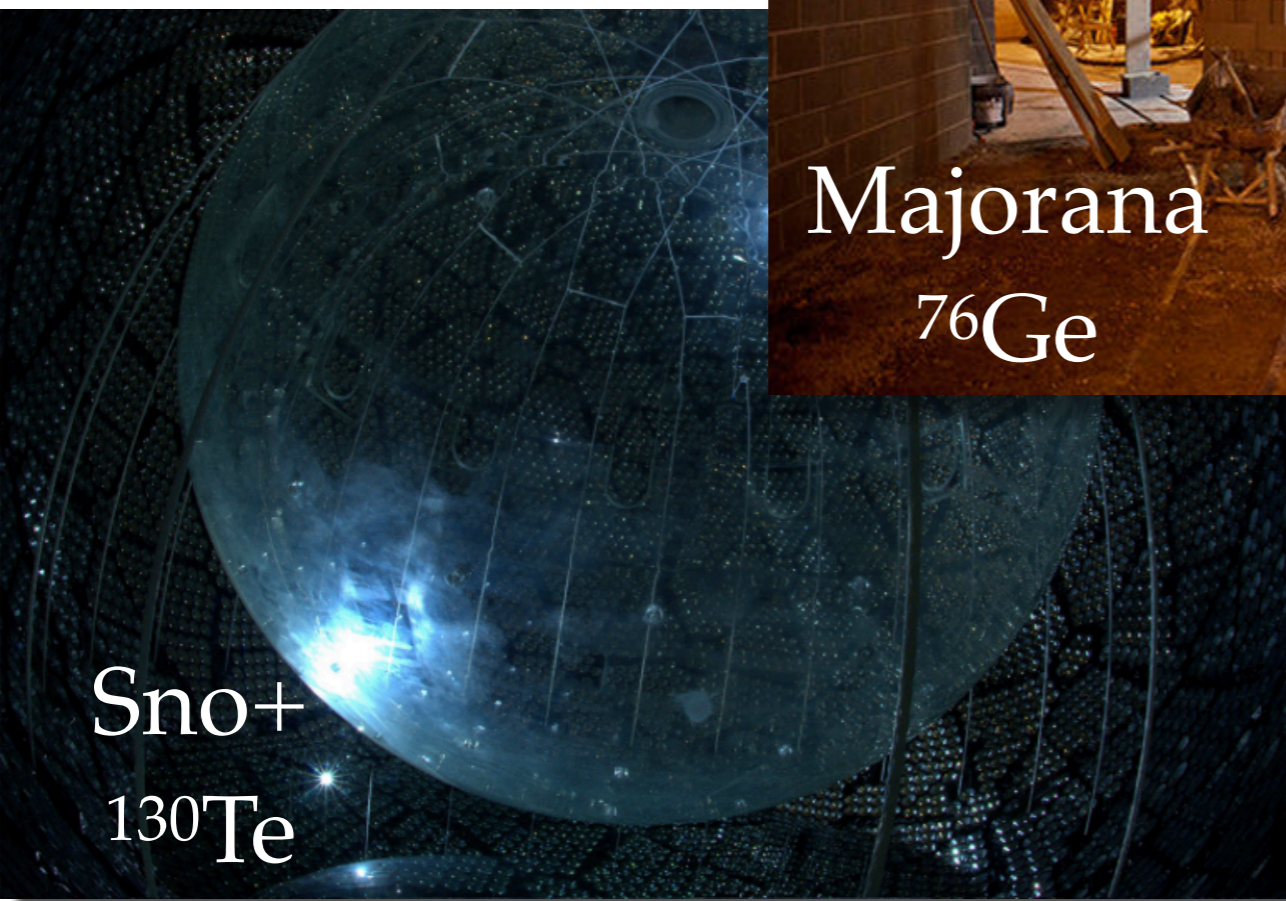


Gerda
 ^{76}Ge

Experiment



Majorana
 ^{76}Ge

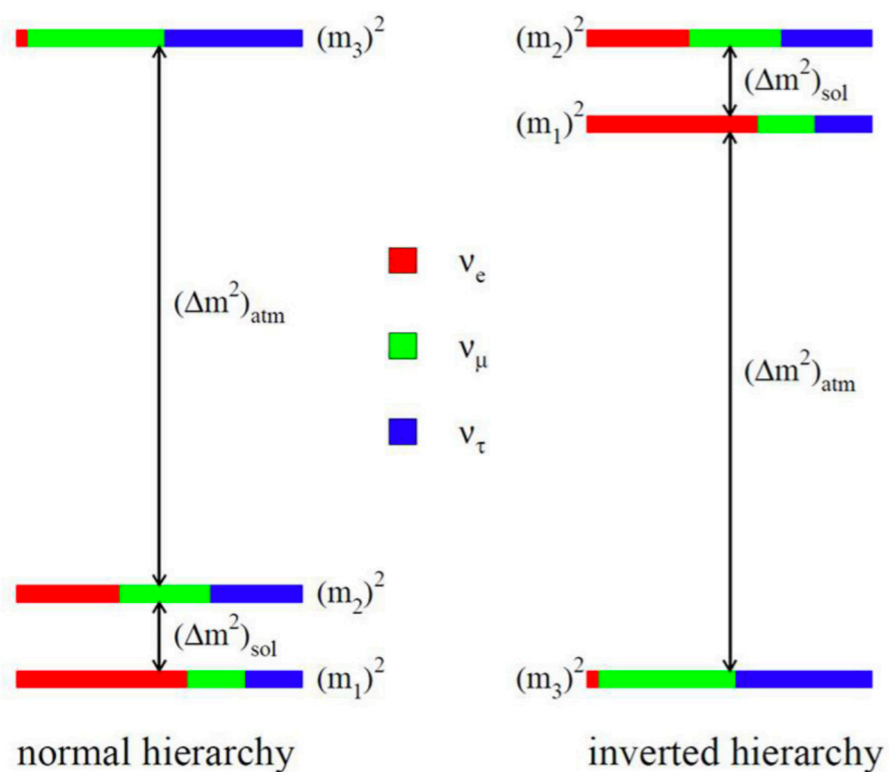
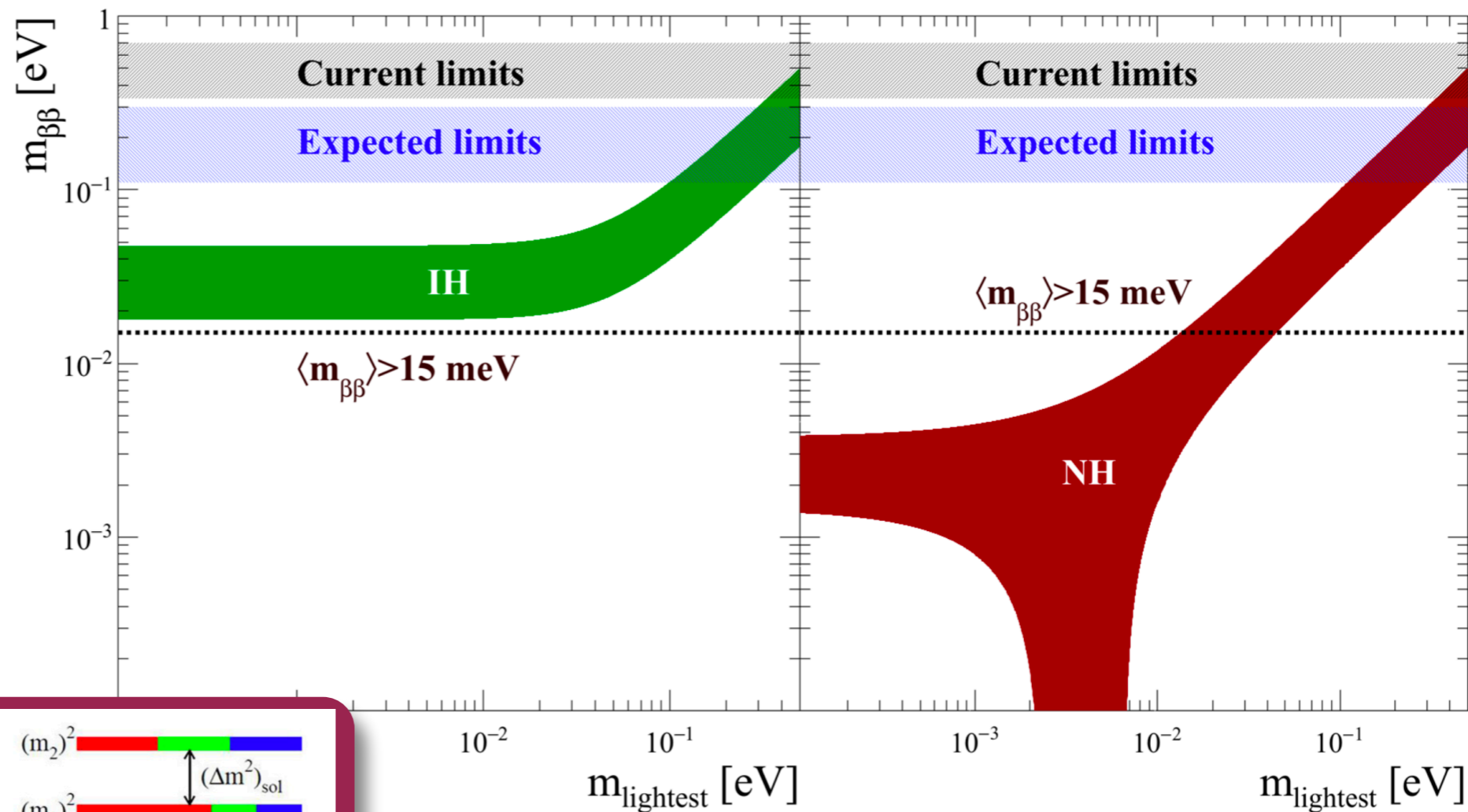


Sno+
 ^{130}Te

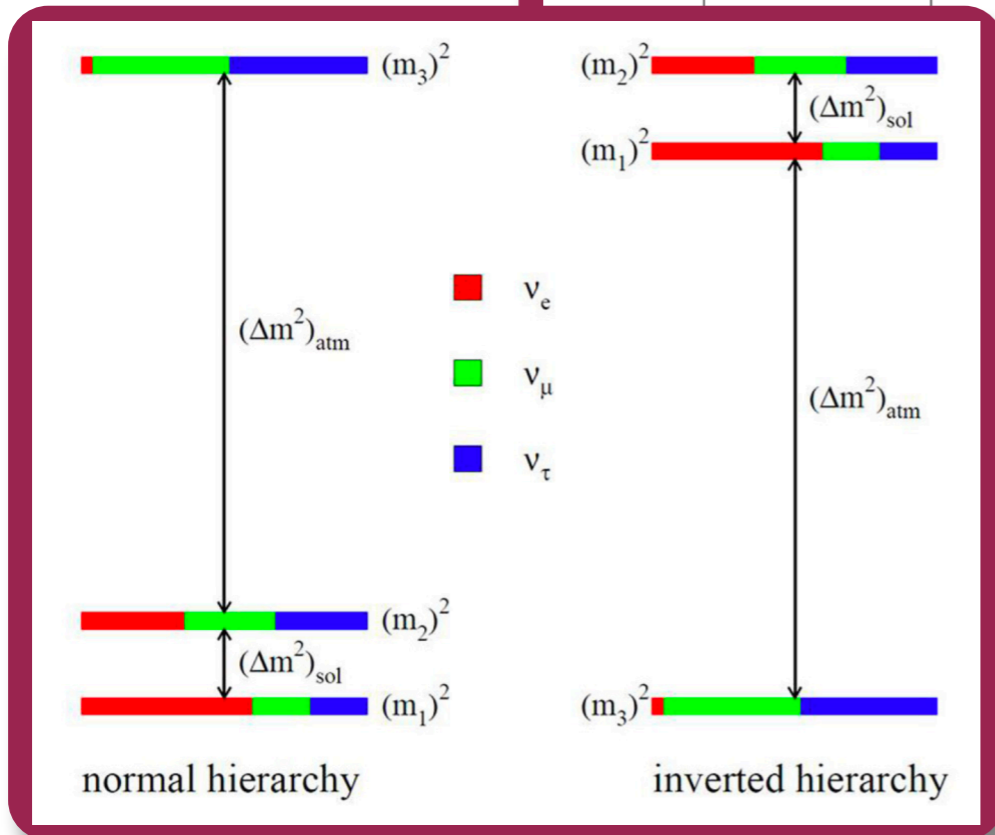
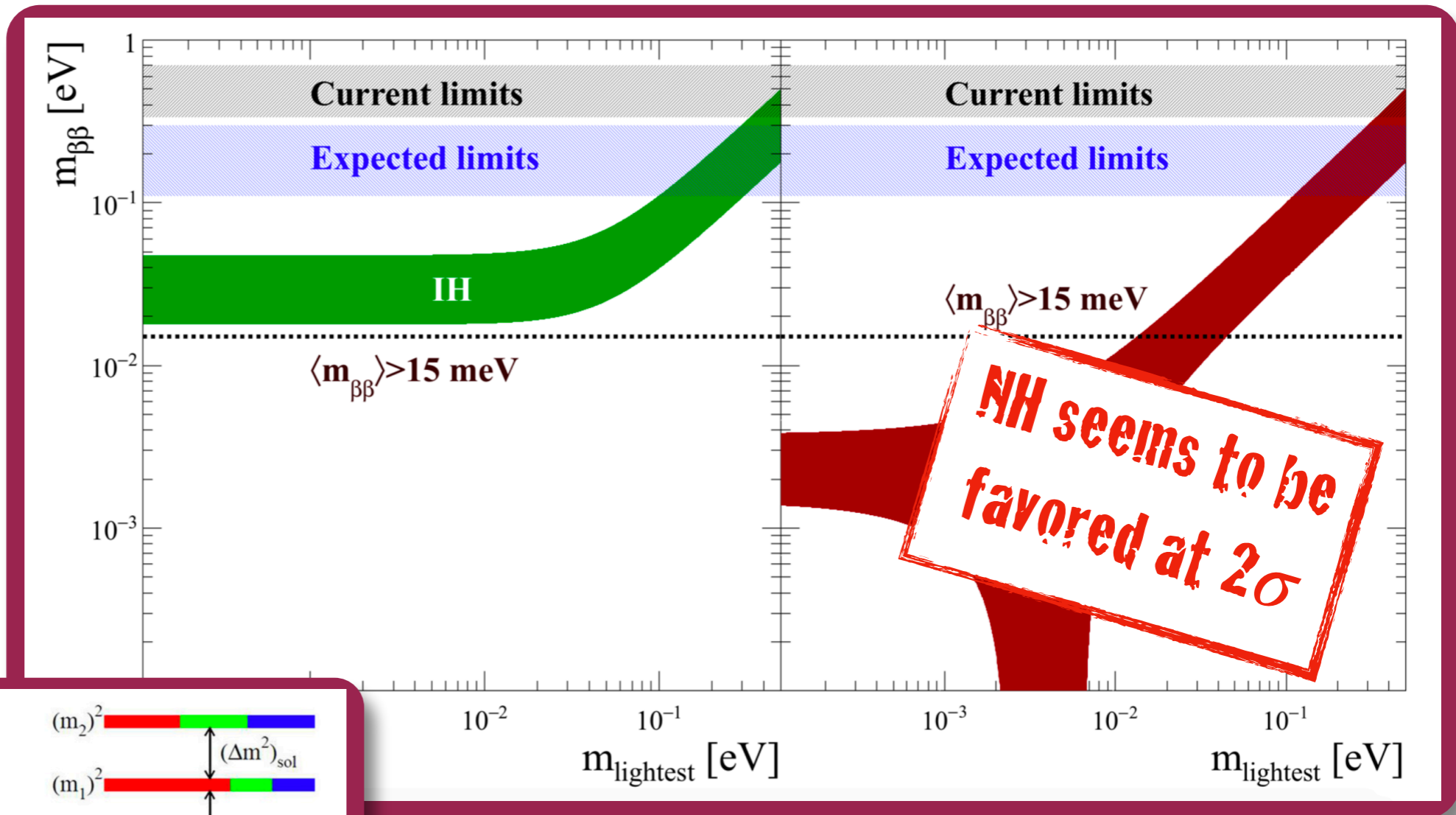


nEXO
 ^{136}Xe

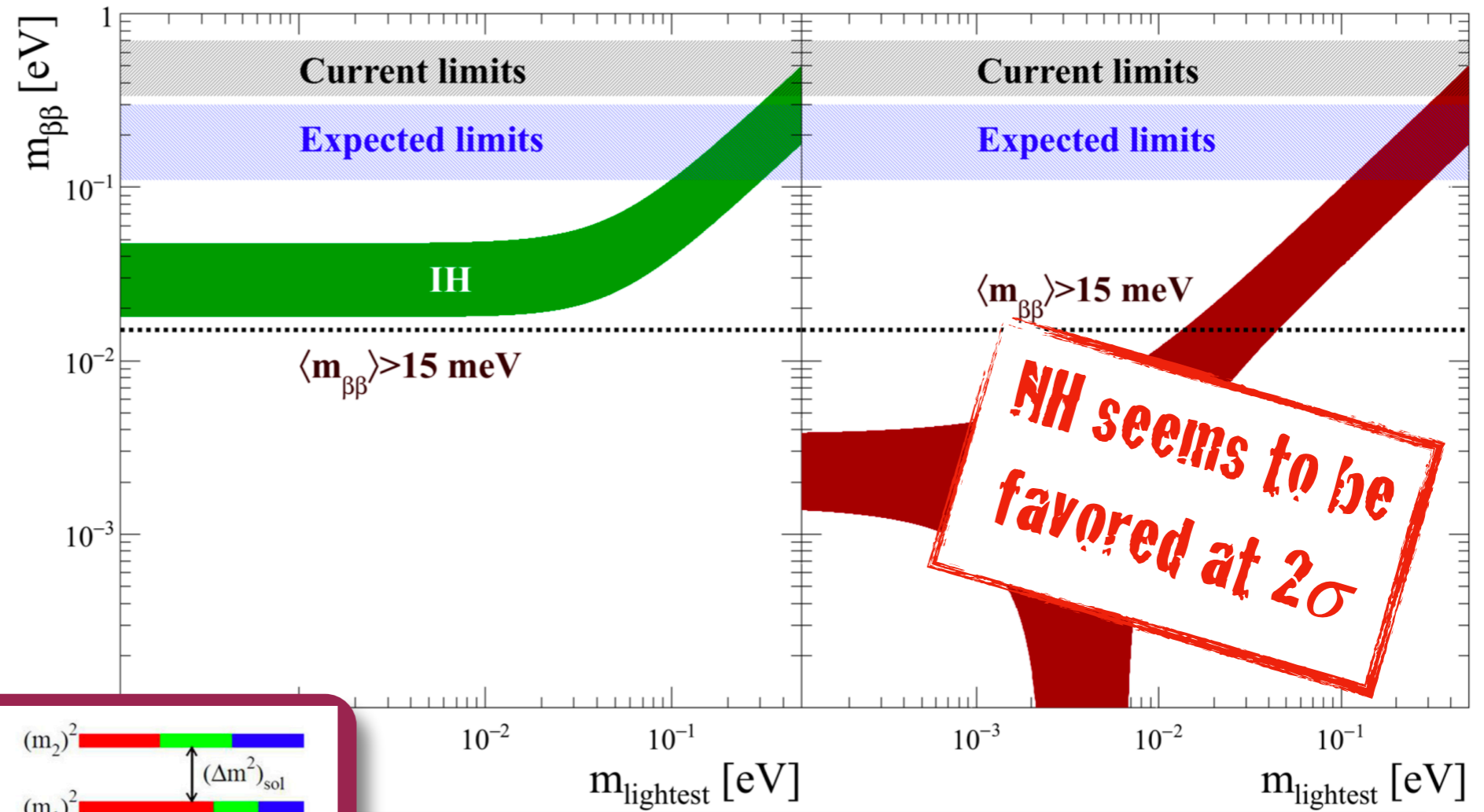
From NSAC Long Range Plan 2015



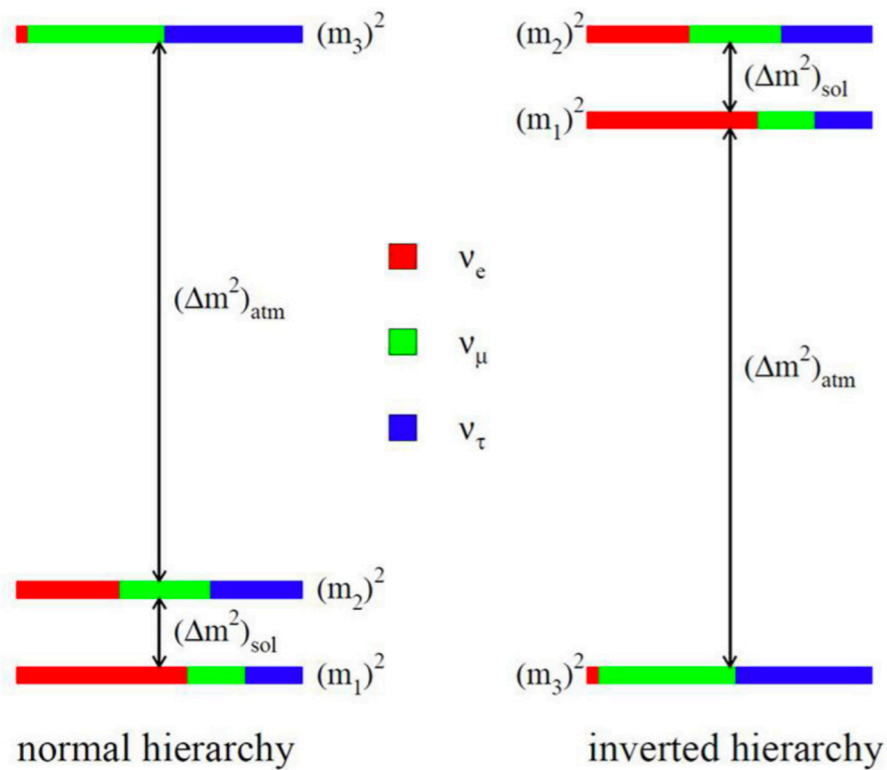
From NSAC
Long Range
Plan 2015



From NSAC
Long Range
Plan 2015

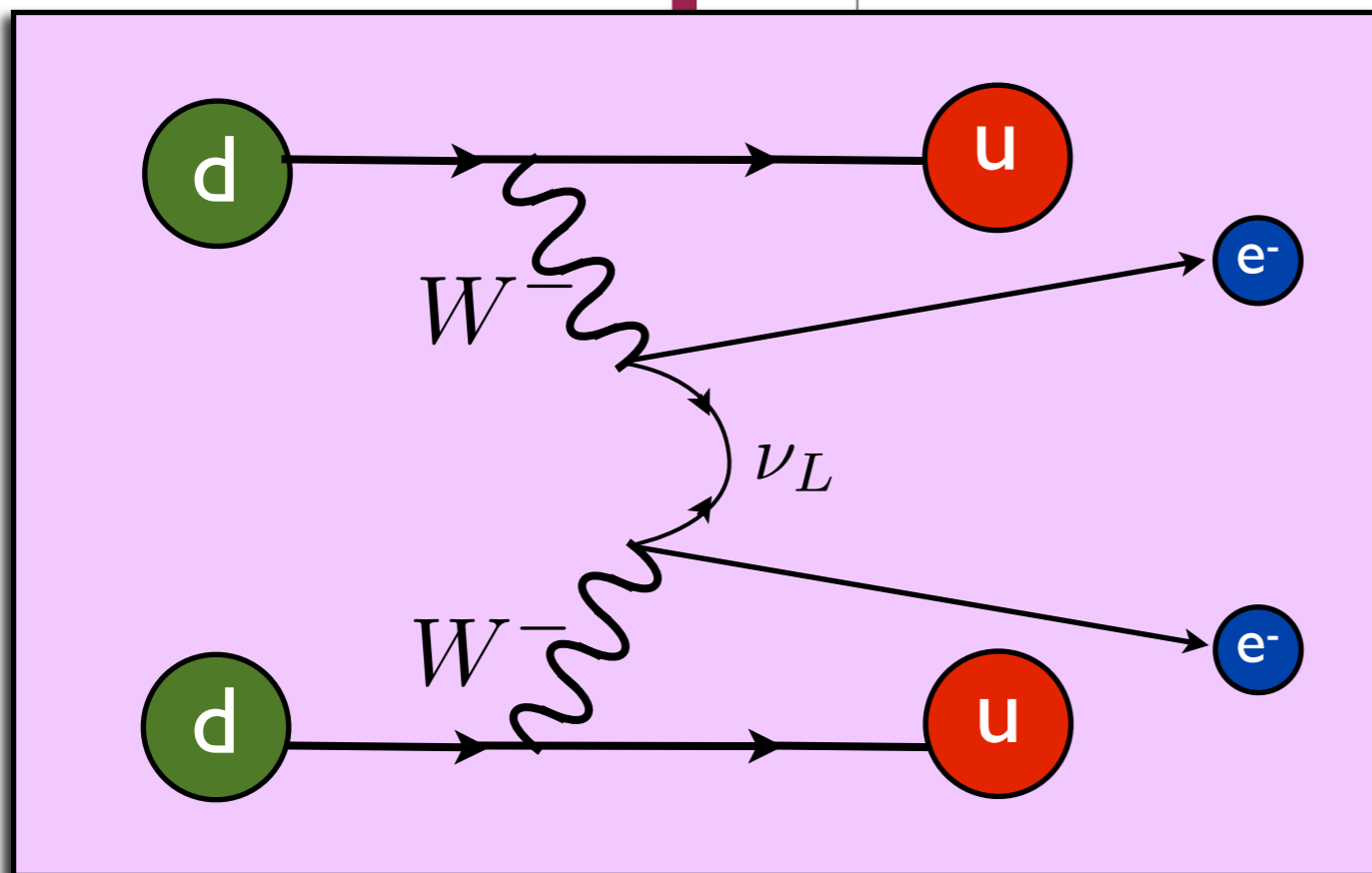
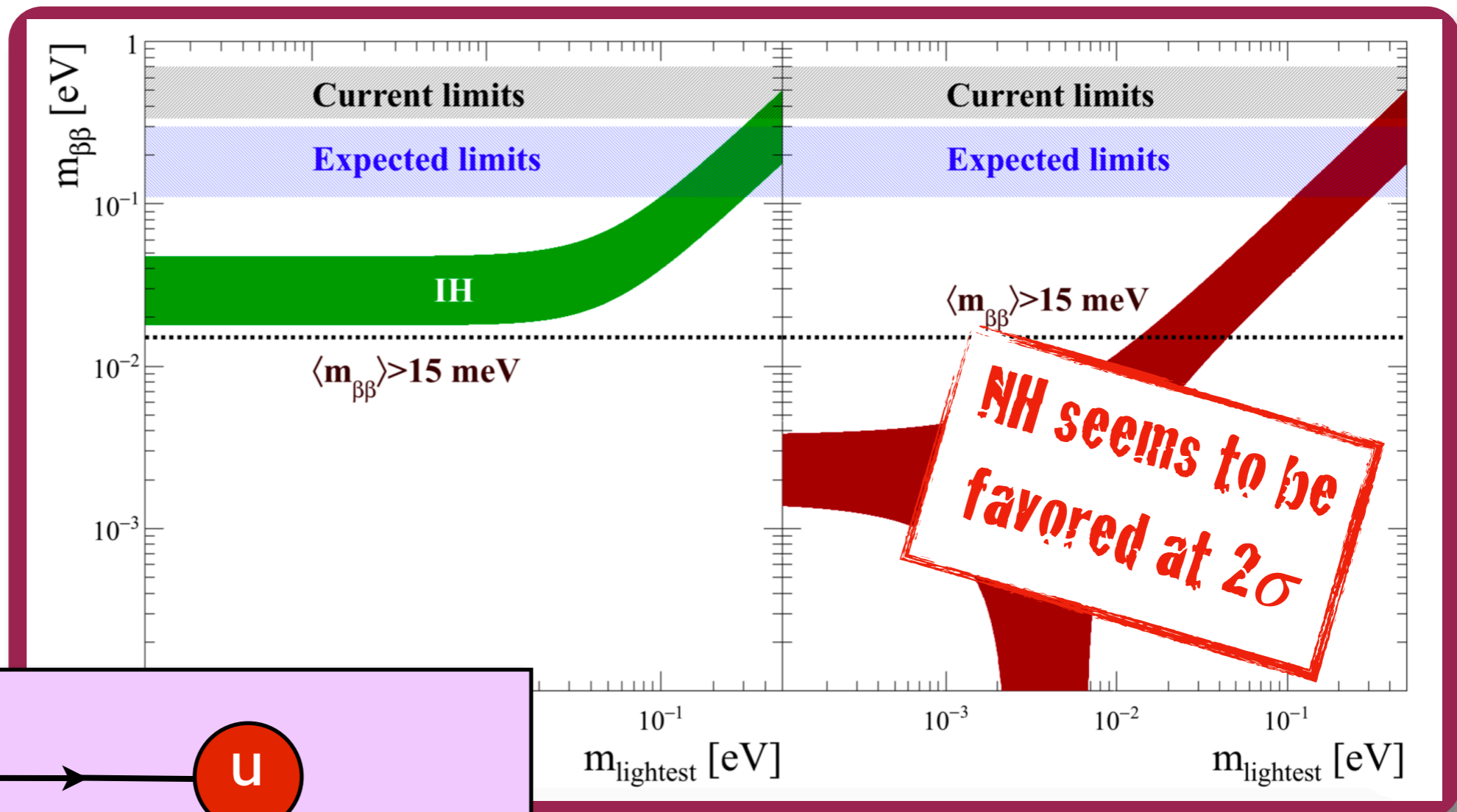


NH seems to be favored at 2σ



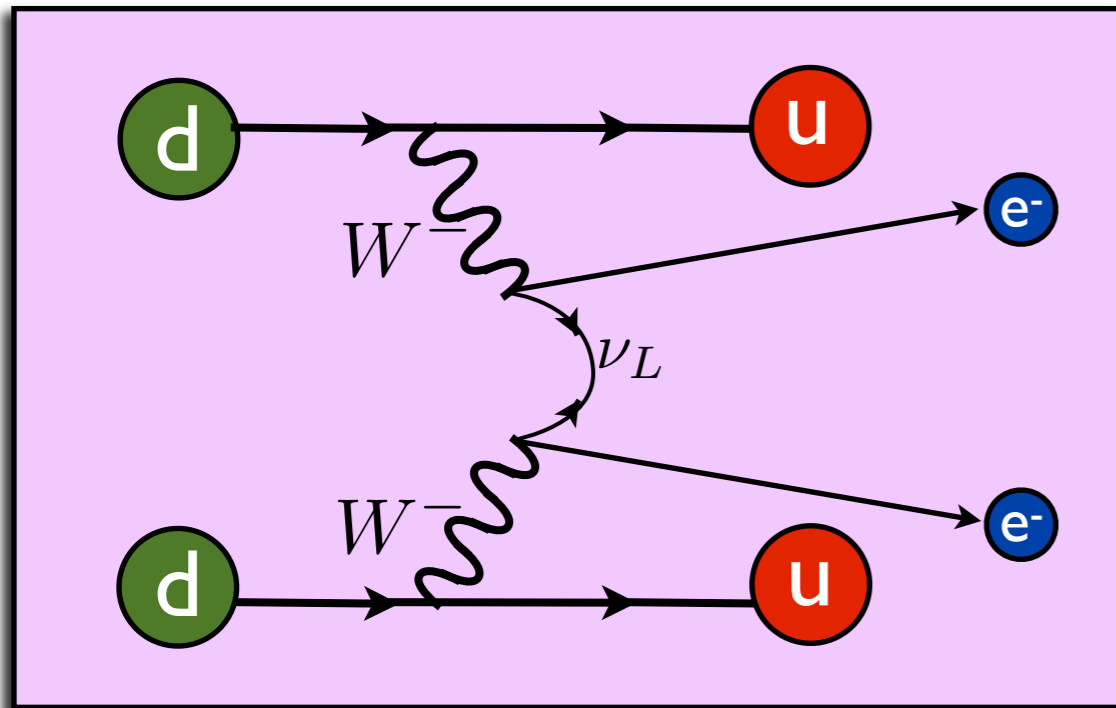
I. NME's currently have large, uncontrolled theoretical uncertainties - can we improve this?

From NSAC
Long Range
Plan 2015

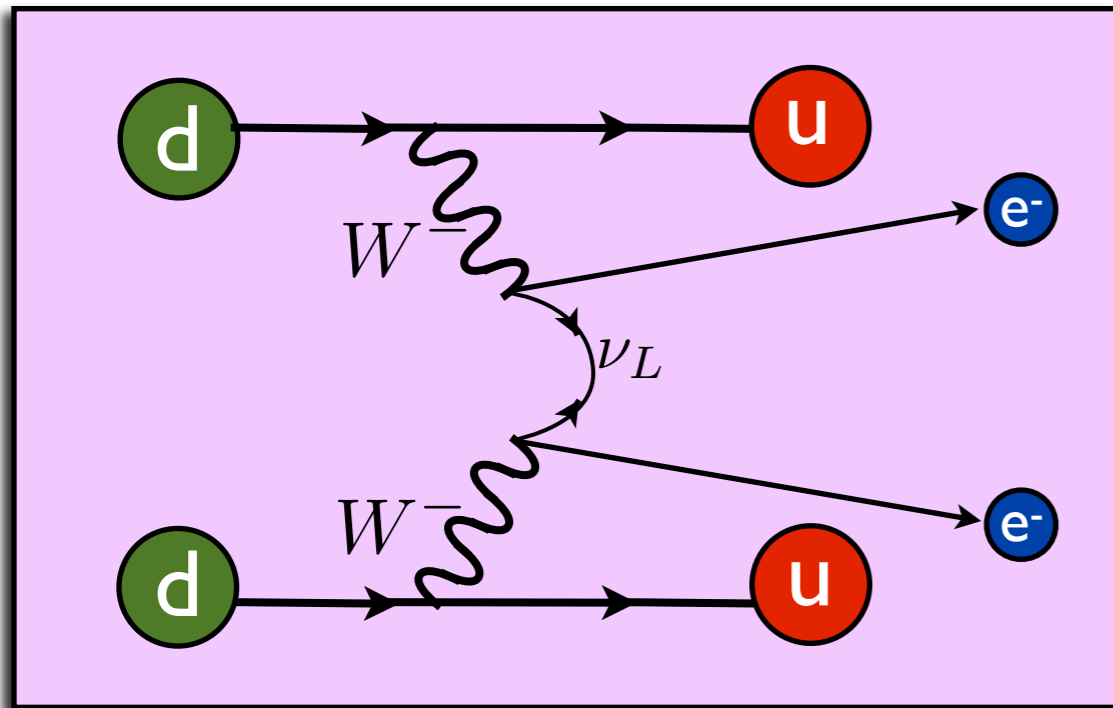


1. NME's currently have large, uncontrolled theoretical uncertainties - can we improve this?
2. This picture assumes only (perturbative) long-range neutrino exchange. There's more to the story - maybe we're missing something important!

Short-range contributions



Short-range contributions



Seesaw Mechanism

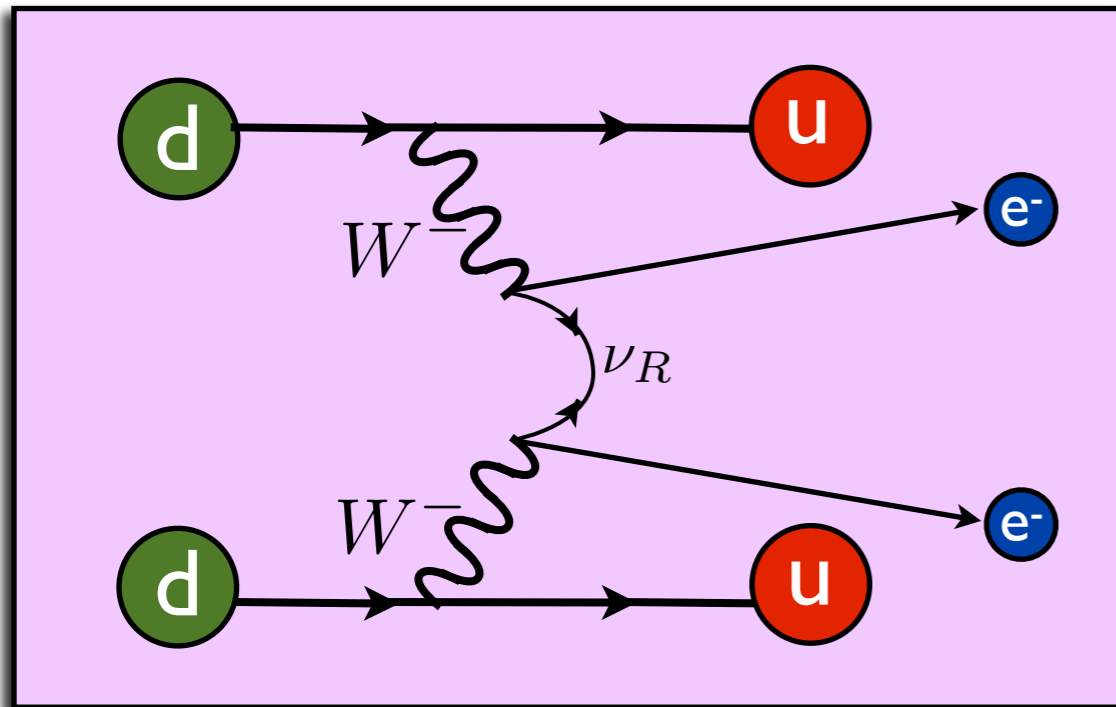
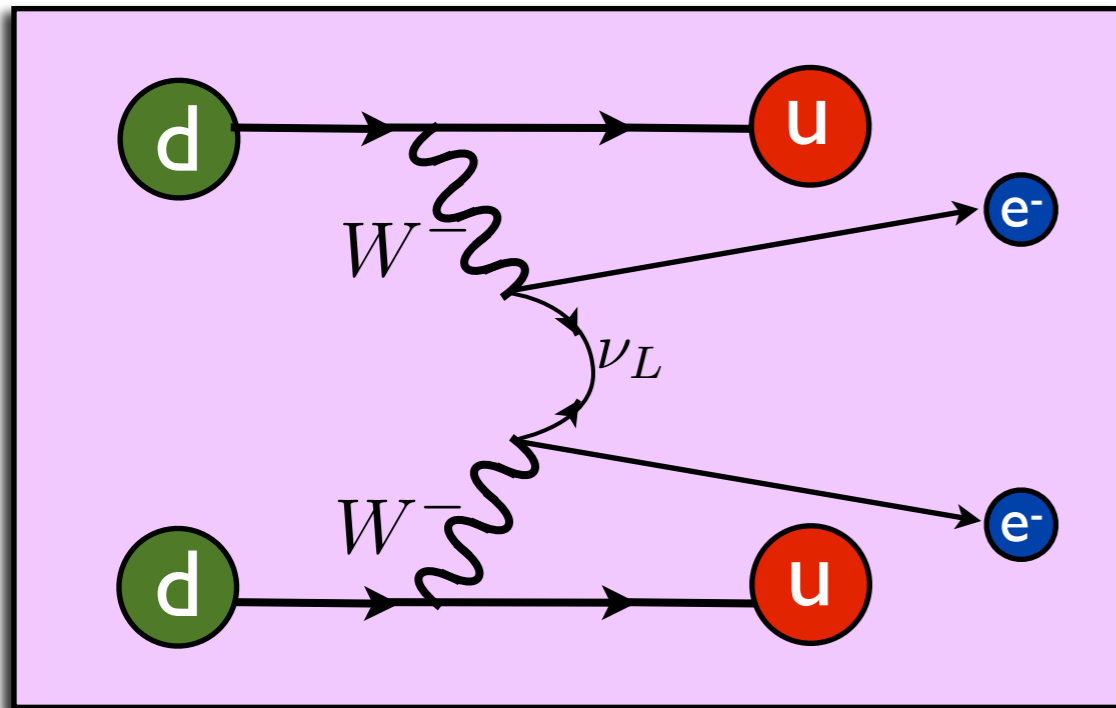


$$\begin{pmatrix} 0 & M_D \\ M_D & M_R \end{pmatrix}$$

$$m_l \sim M_D^2 / M_R$$

$$m_h \sim M_R$$

Short-range contributions



Seesaw Mechanism

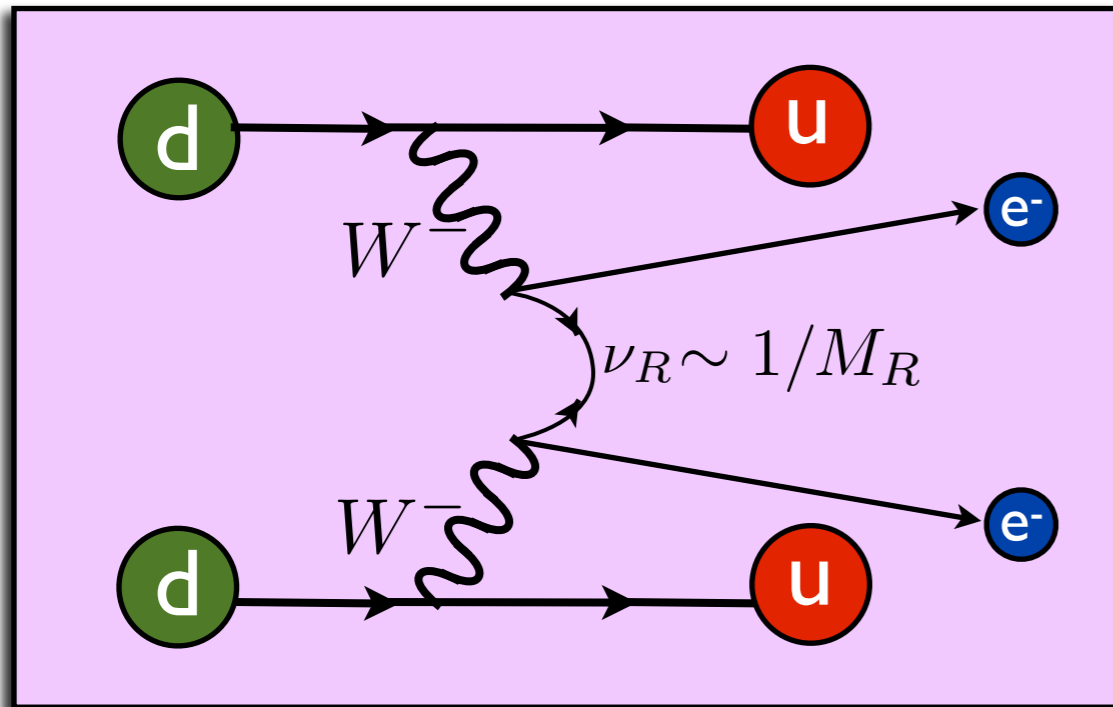
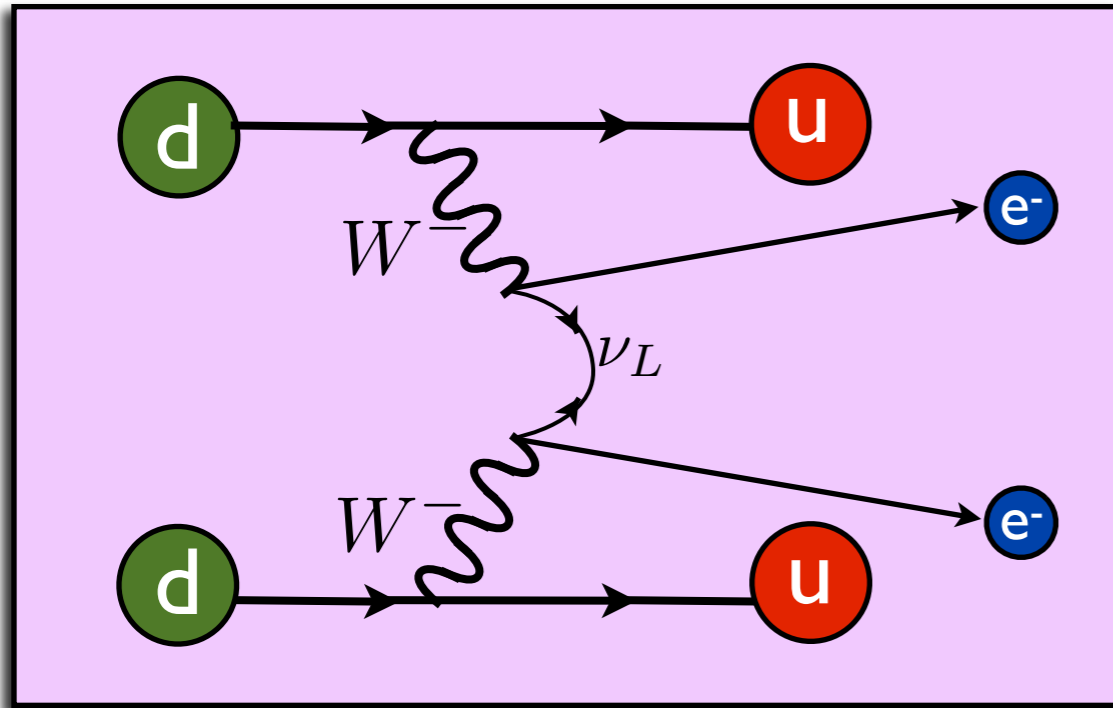


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Seesaw Mechanism

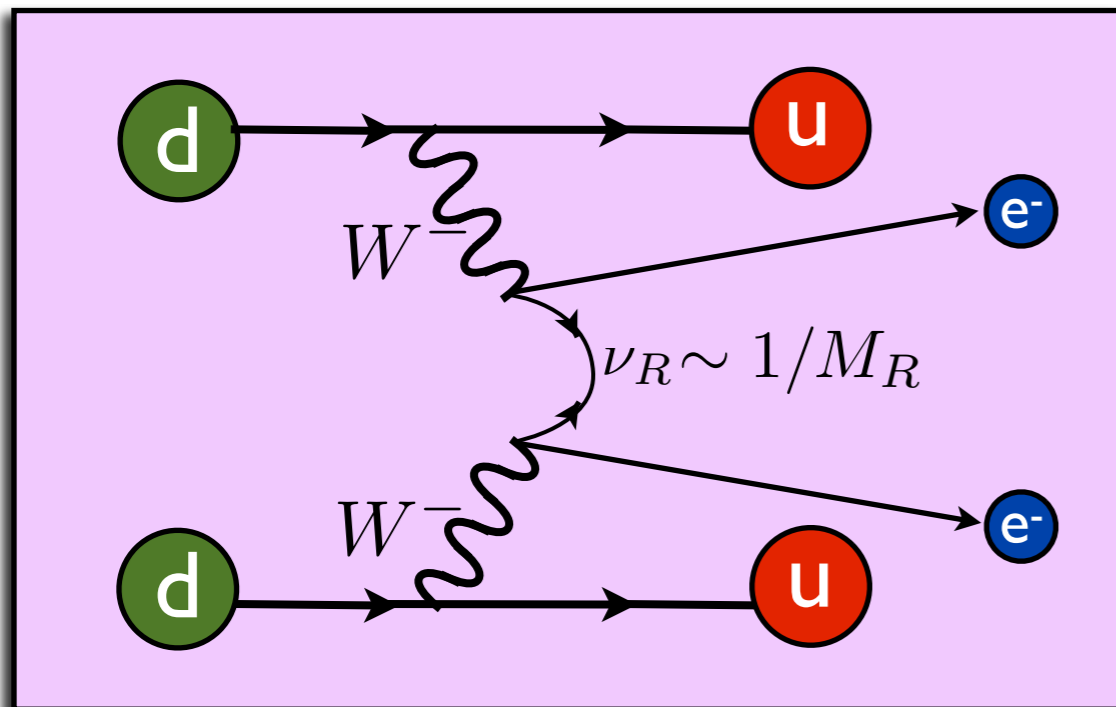
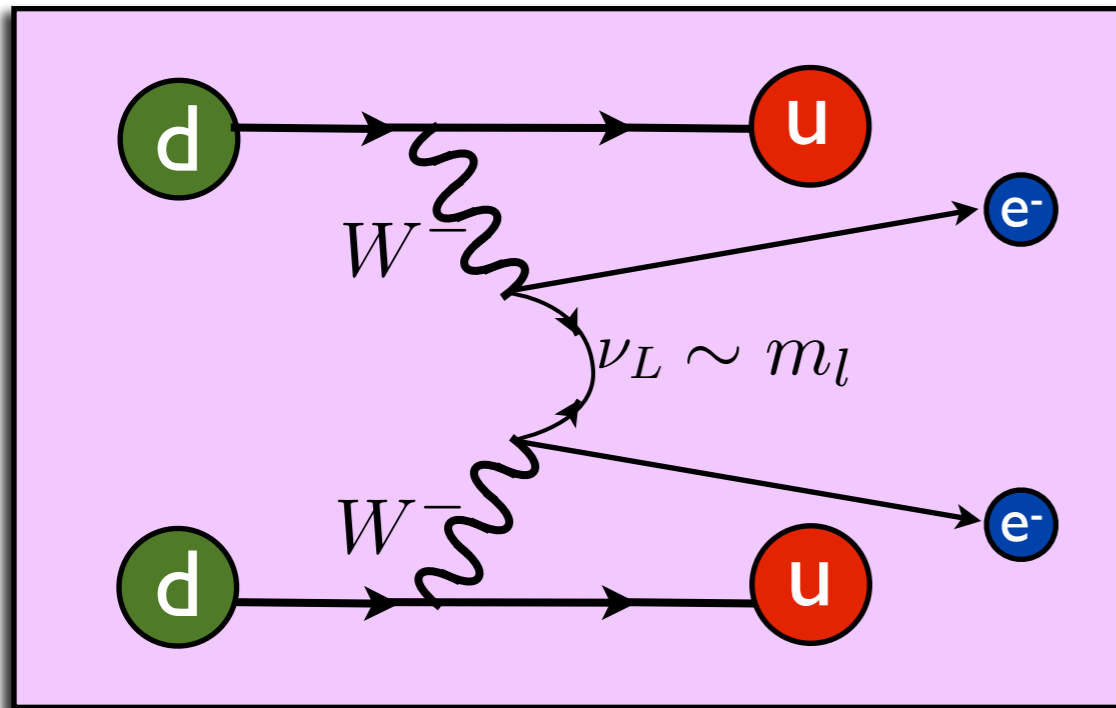


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Short-range contributions



Seesaw Mechanism

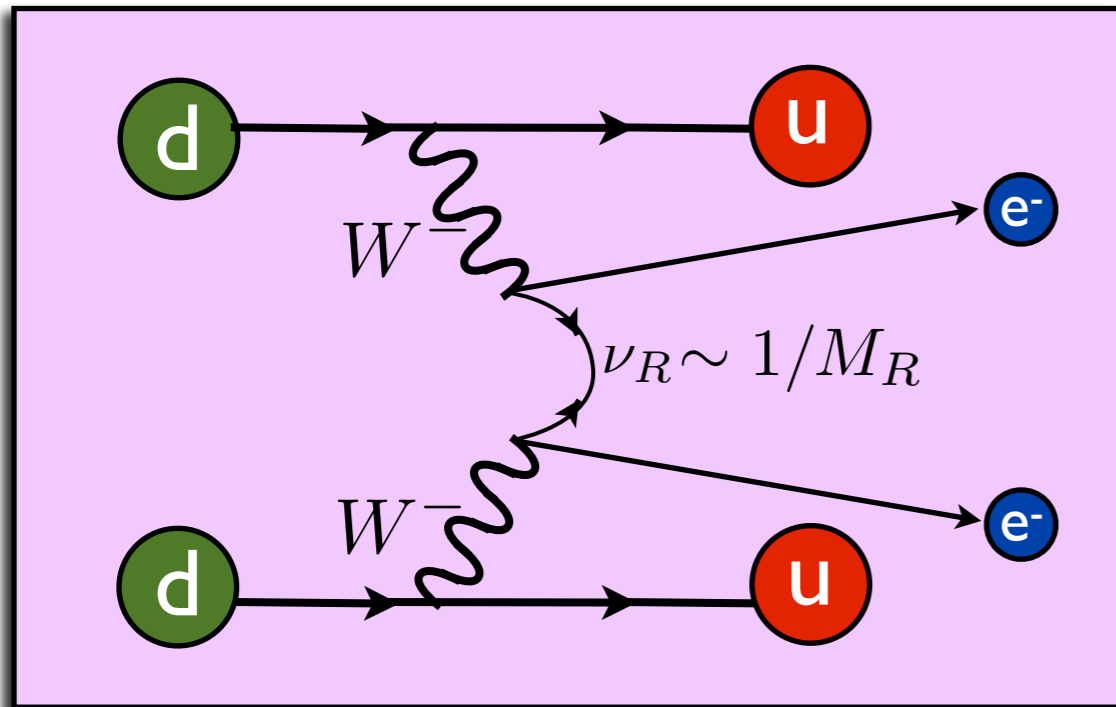
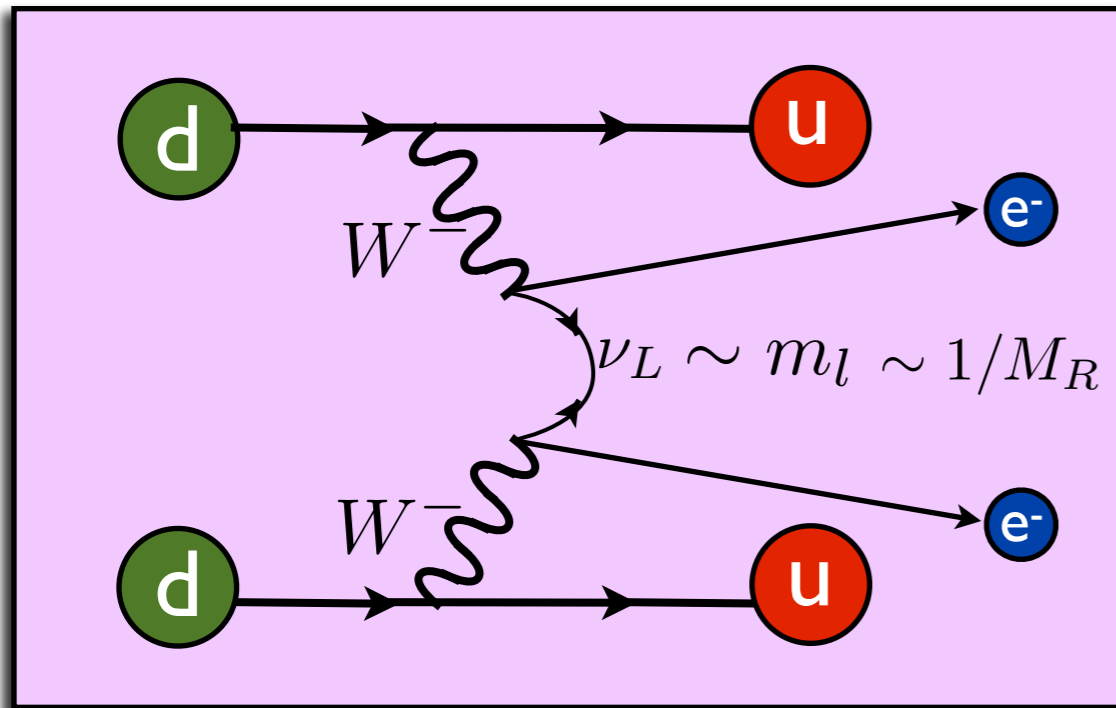


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Short-range contributions



Seesaw Mechanism

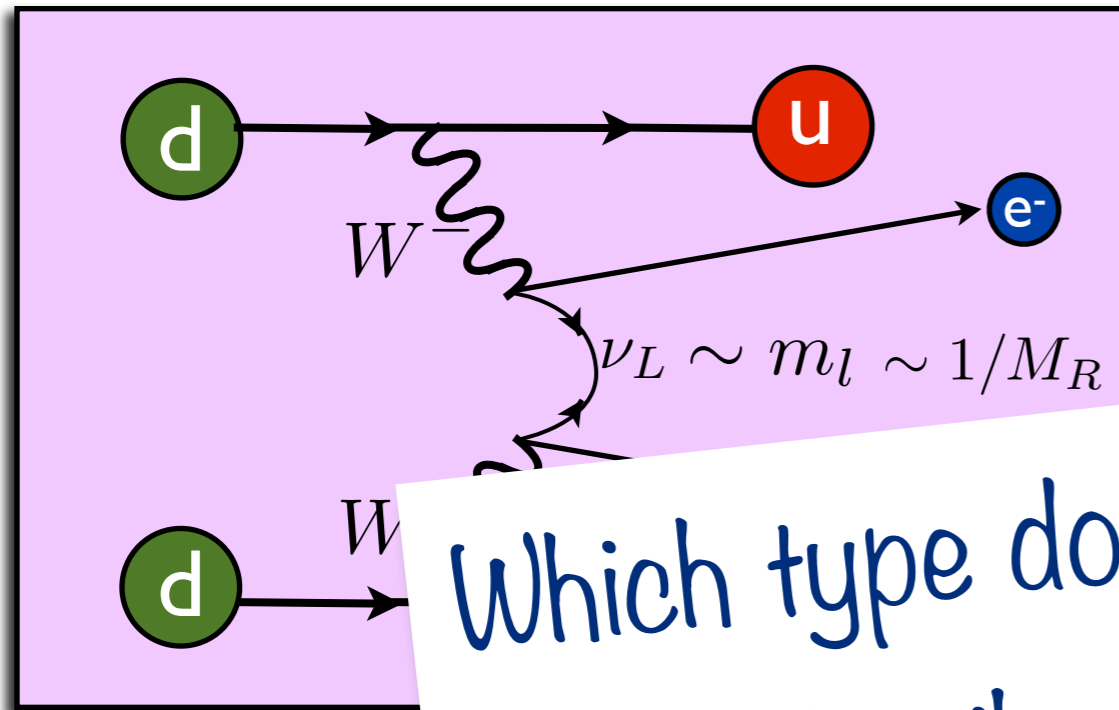


$$\begin{pmatrix} 0 & M_D \\ M_D & M_R \end{pmatrix}$$

$$m_l \sim M_D^2 / M_R$$

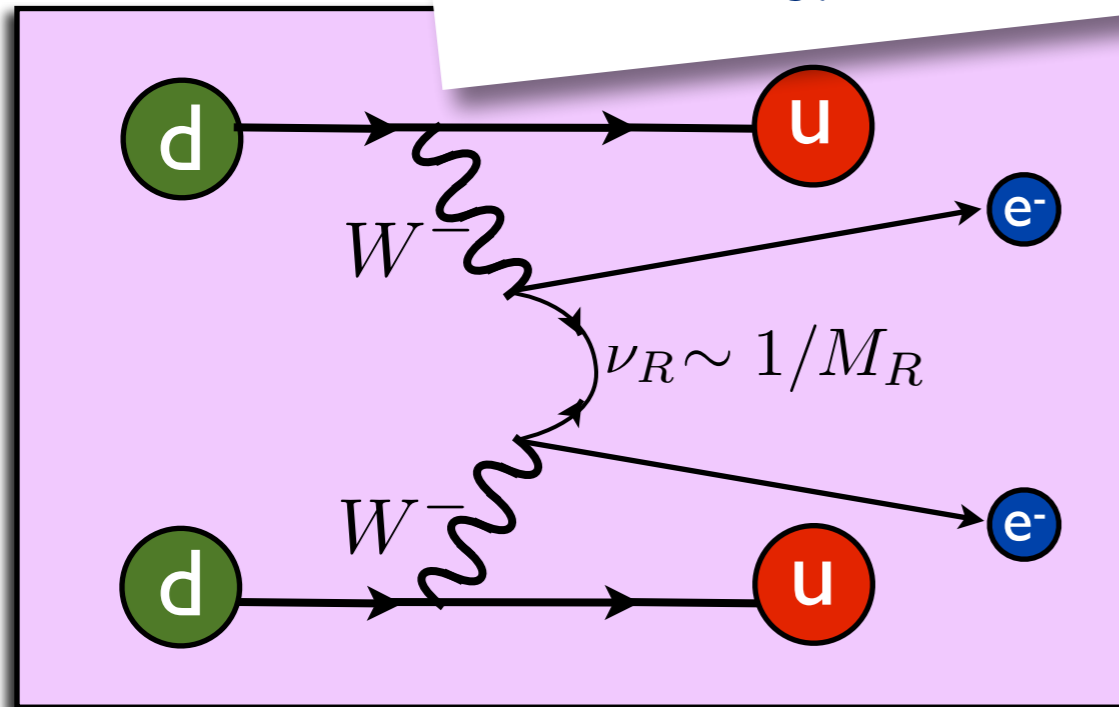
$$m_h \sim M_R$$

Short-range contributions



Seesaw Mechanism

Which type dominates depends on details of BSM model



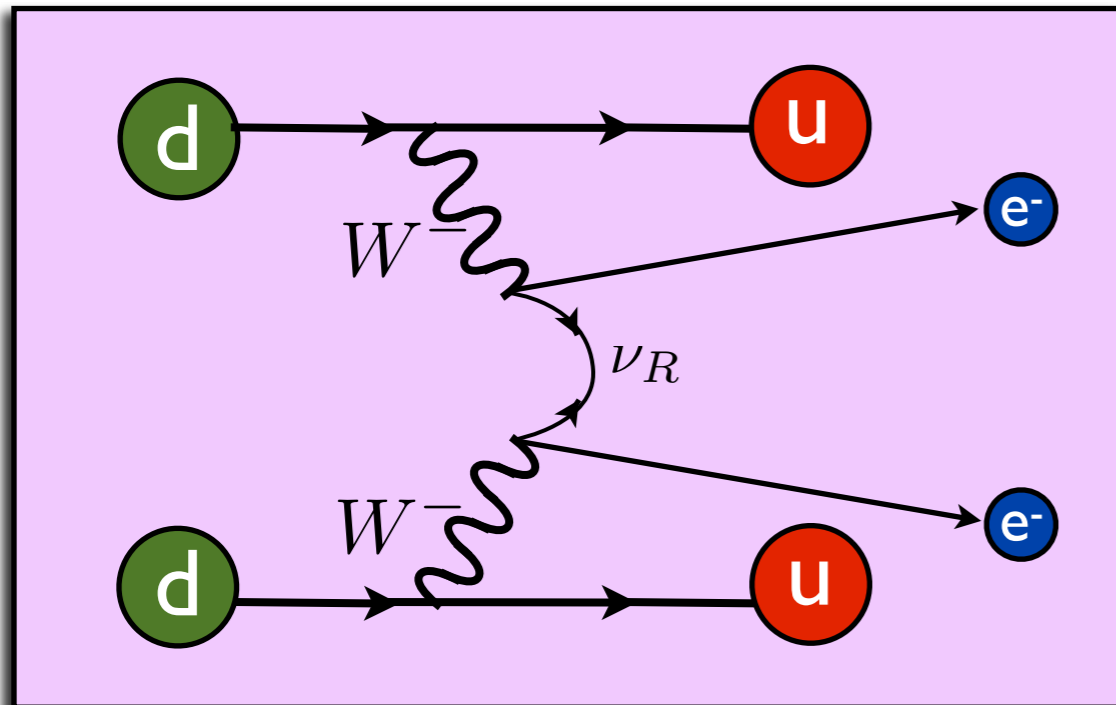
$$\begin{pmatrix} 0 & M_D \\ M_D & M_R \end{pmatrix}$$

$$m_l \sim M_D^2 / M_R$$

$$m_h \sim M_R$$

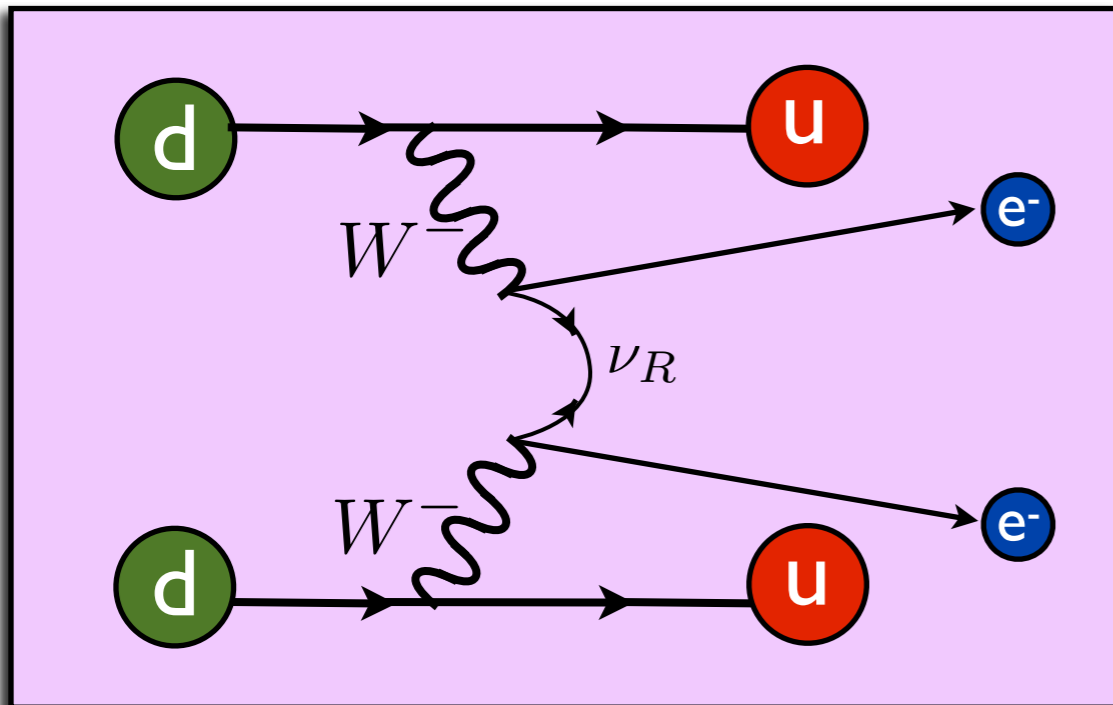
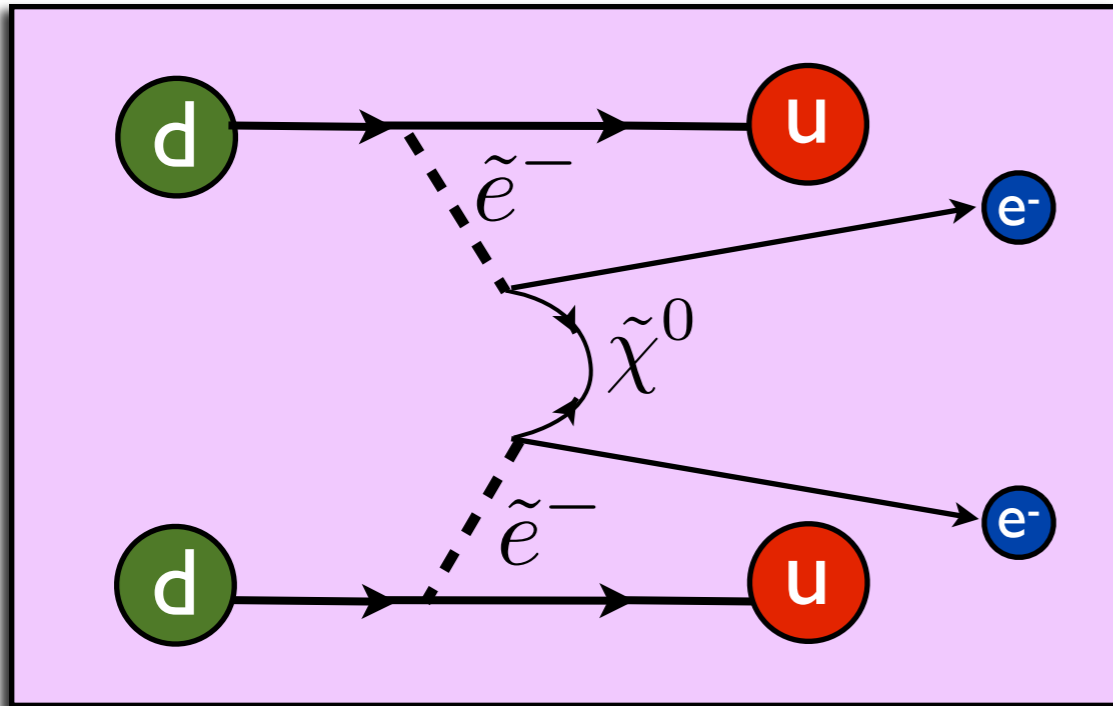
Short-range contributions

$$\mathcal{L}_5 = \frac{c}{\Lambda} (\bar{L} \tilde{H}) (\tilde{H} L)^\dagger$$



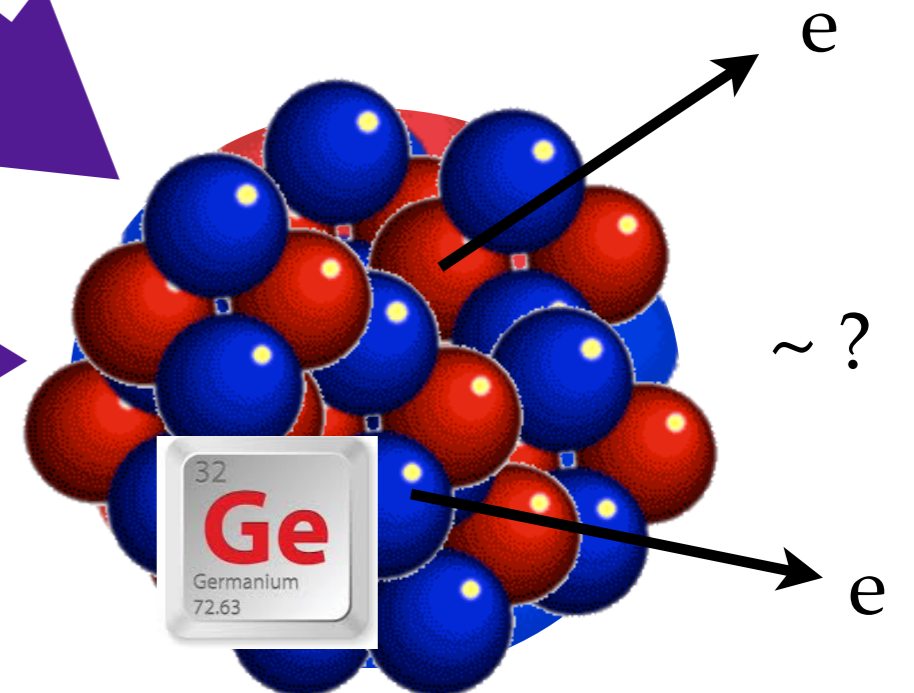
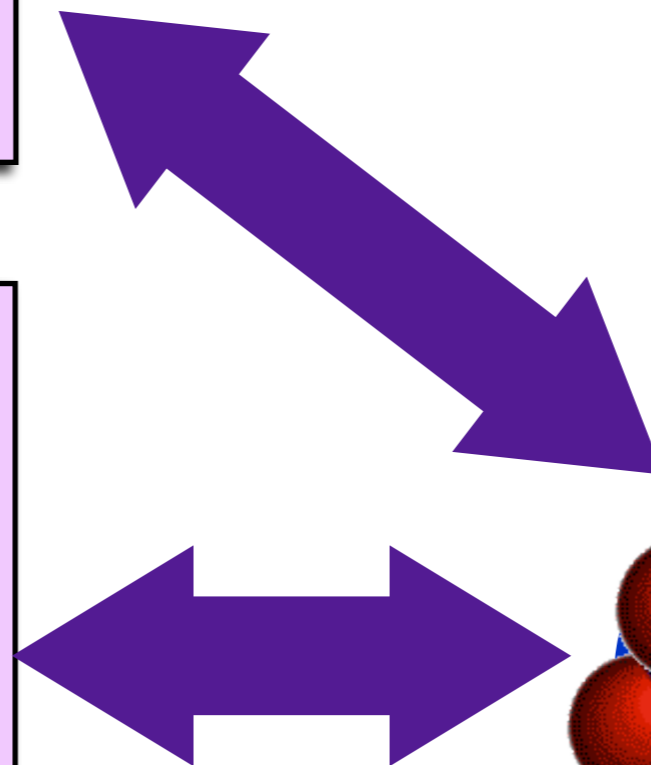
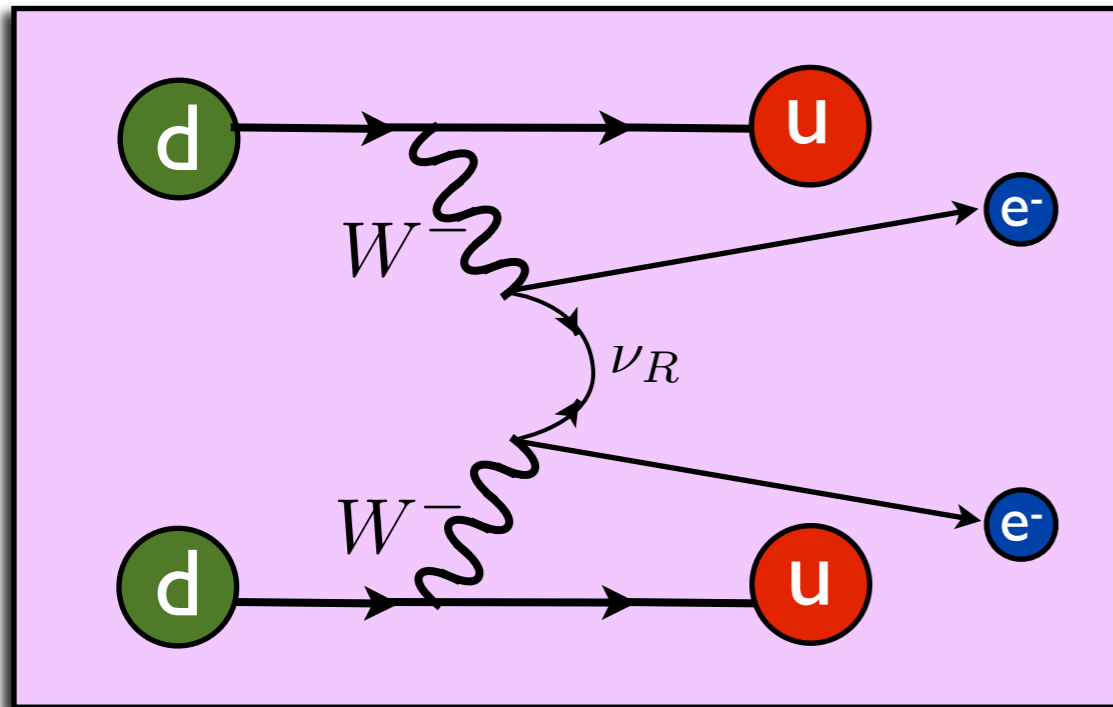
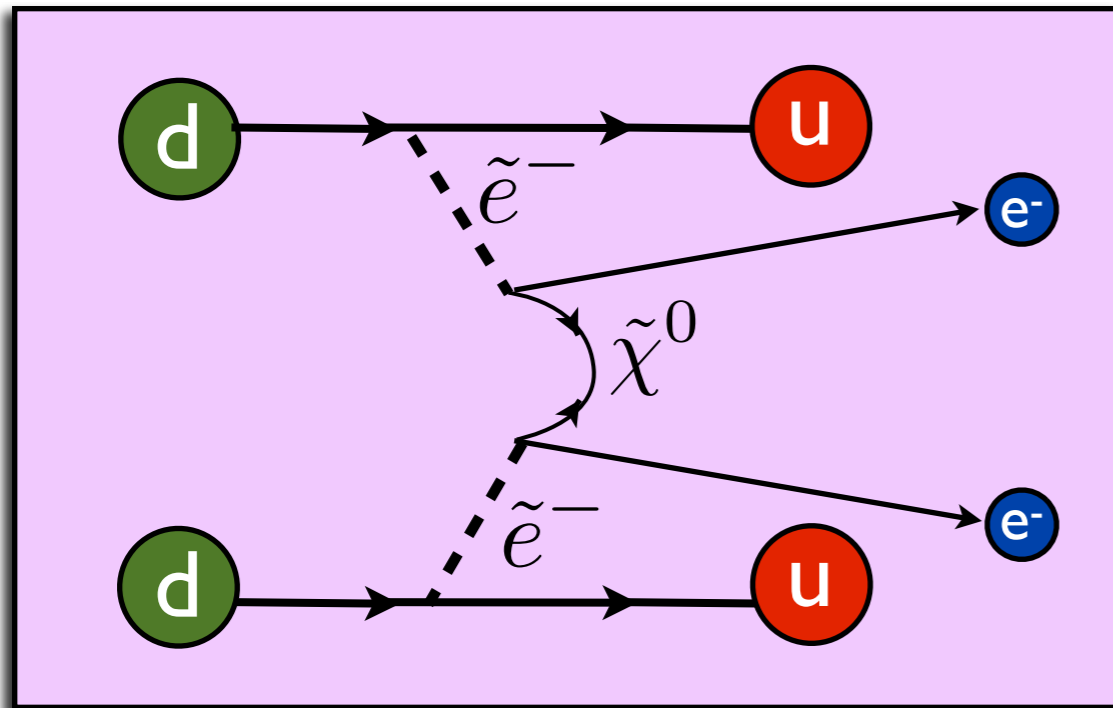
Short-range contributions

$$\mathcal{L}_5 = \frac{c}{\Lambda} (\bar{L}\tilde{H}) (\tilde{H}L)^\dagger$$

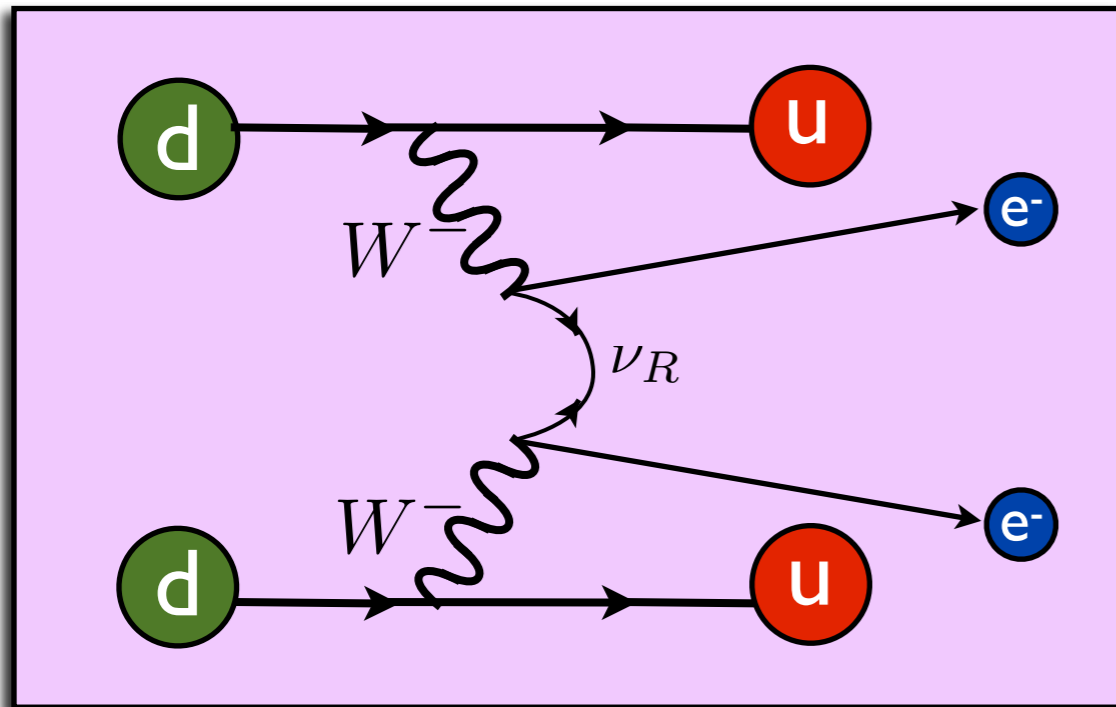
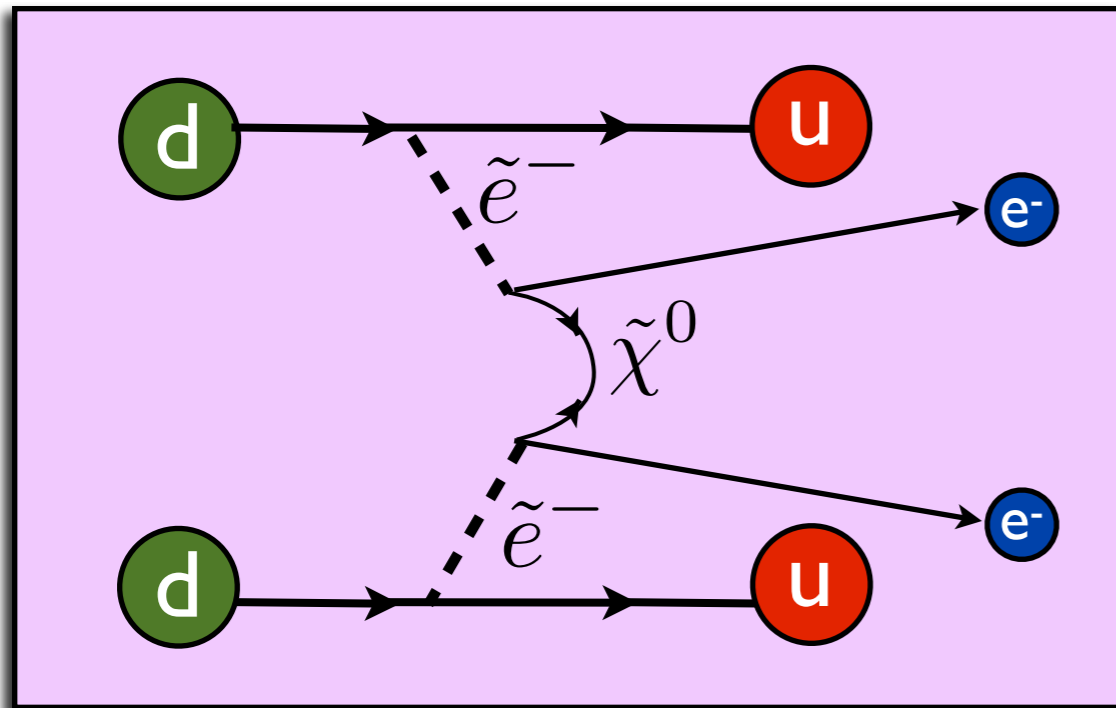


Short-range contributions

$$\mathcal{L}_5 = \frac{c}{\Lambda} (\bar{L}\tilde{H}) (\tilde{H}L)^\dagger$$

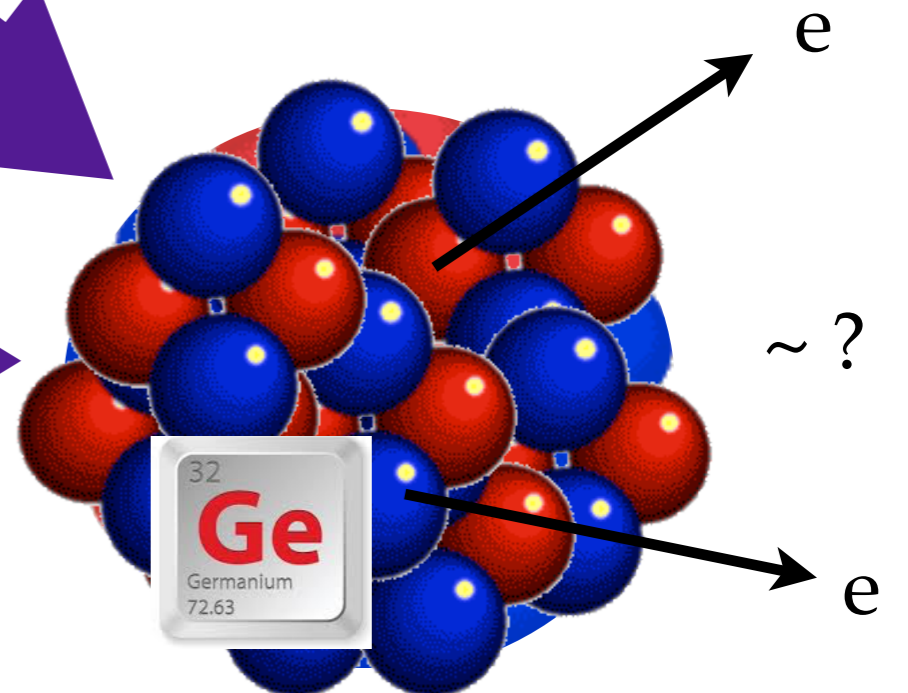
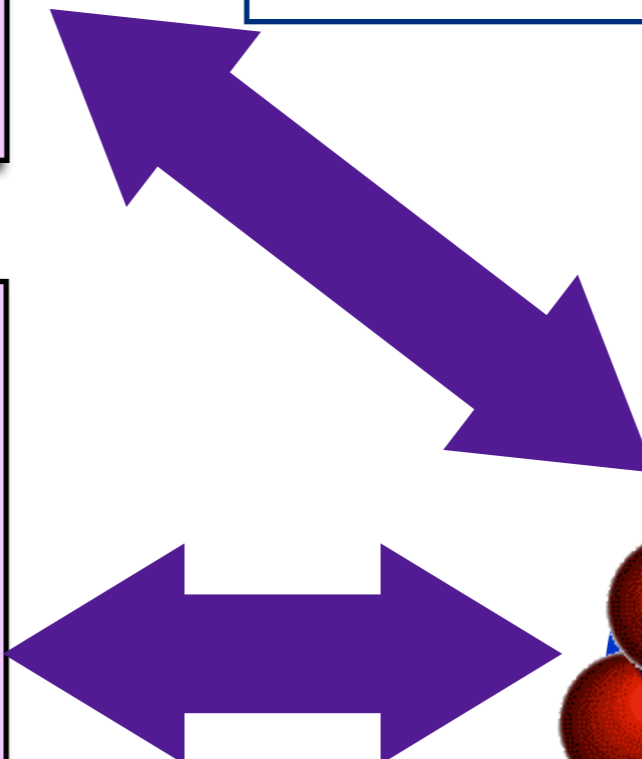


Short-range contributions

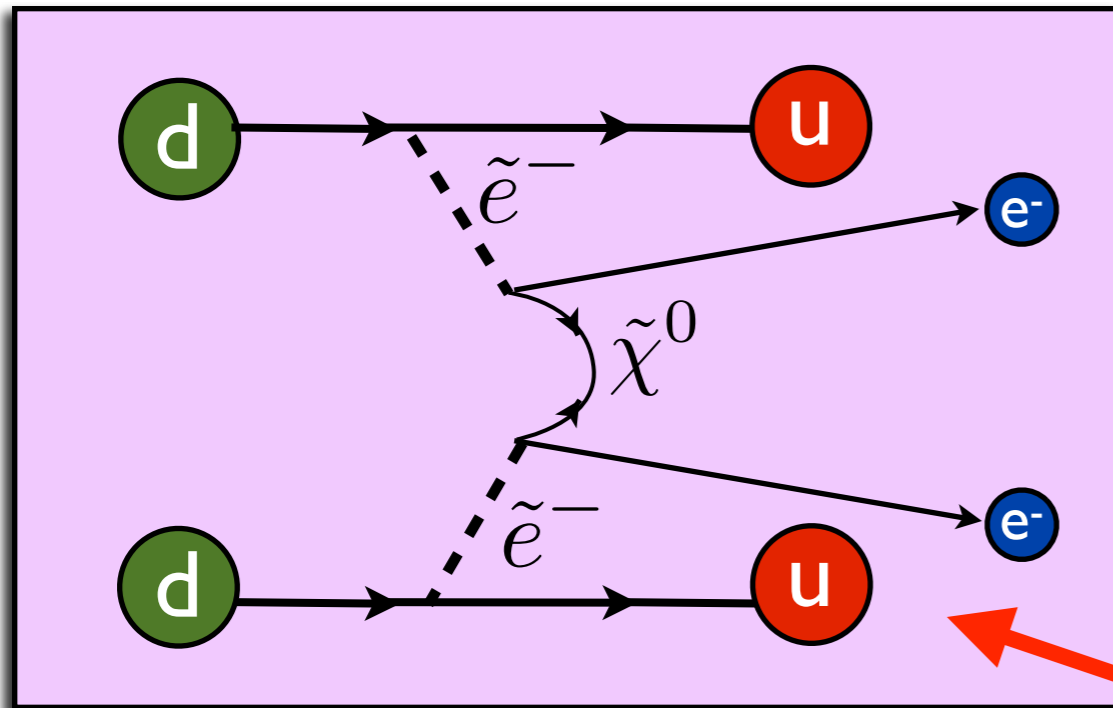


$$\mathcal{L}_5 = \frac{c}{\Lambda} (\bar{L}\tilde{H}) (\tilde{H}L)^\dagger$$

$0\nu\beta\beta$ bounds
could help
constrain R-parity
violating
coefficients

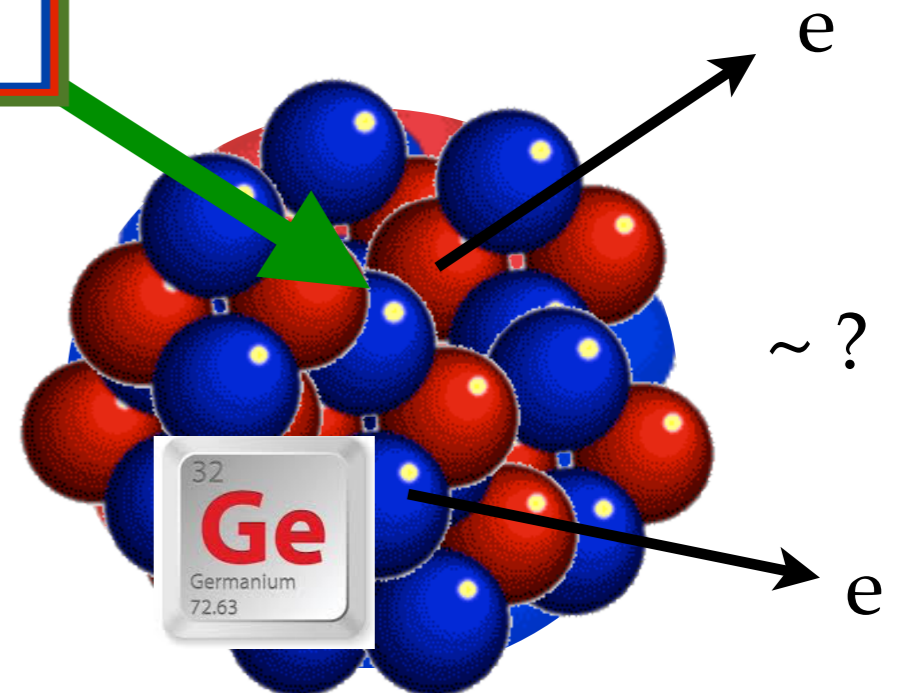
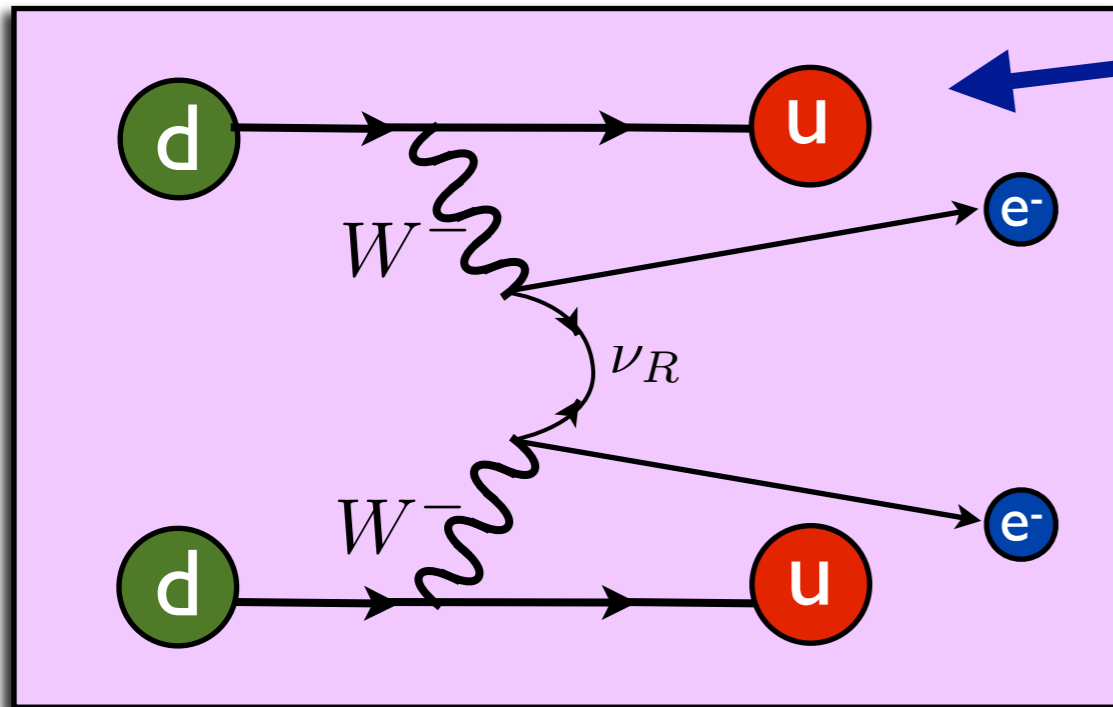


Relating Theory to Experiment

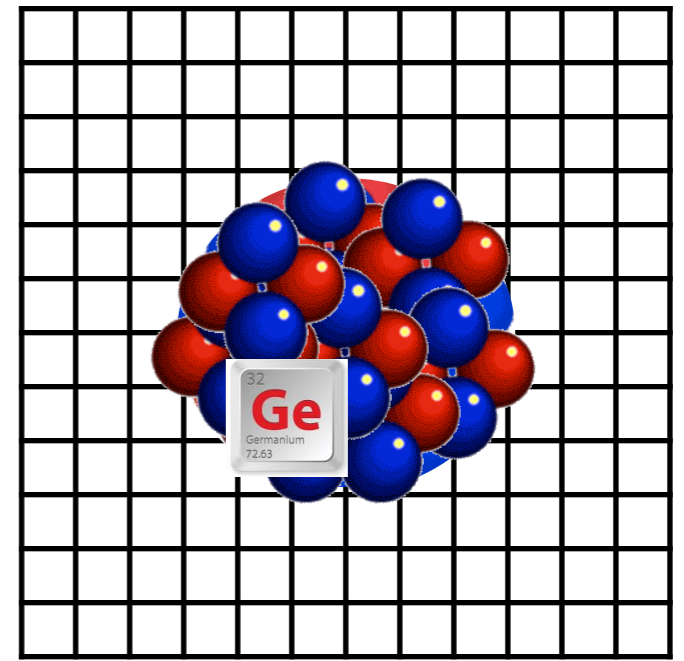


LQCD will never calculate your favorite $0\nu\beta\beta$ isotope

QCD



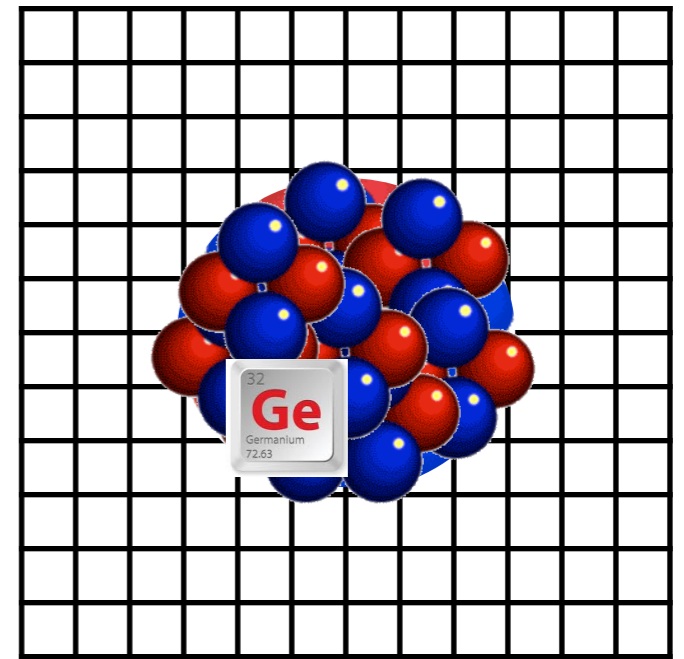
LQCD will never directly calculate
your favorite experimental isotope



Why?

LQCD will never directly calculate
your favorite experimental isotope

- Need extremely large lattices
- Large range of scales
- Tiny energy splittings

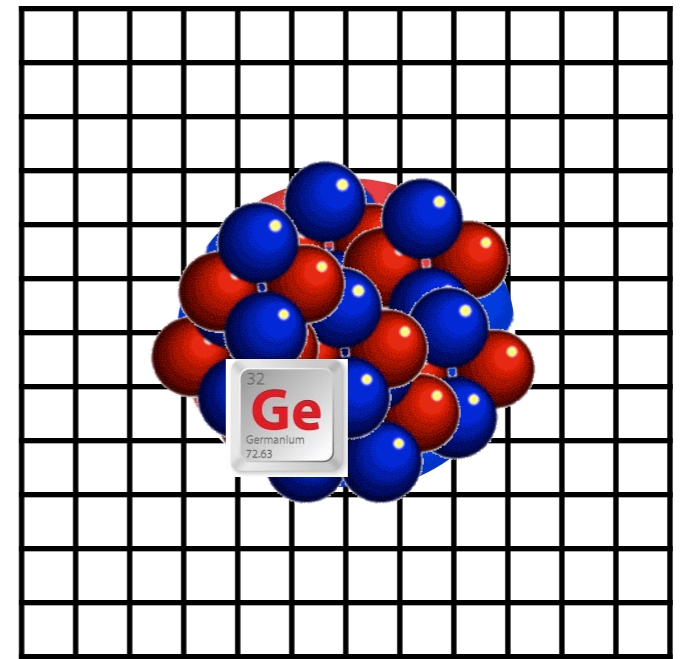


Why?

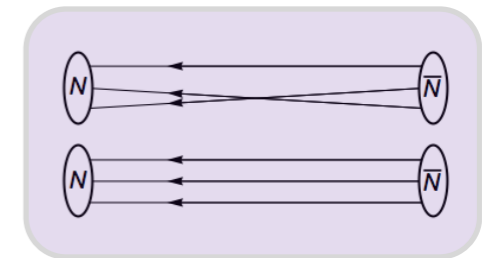
LQCD will never directly calculate your favorite experimental isotope

- Need extremely large lattices
- Large range of scales
- Tiny energy splittings
- Wick contractions:
 $(A+Z)! \times (2A-Z)!$

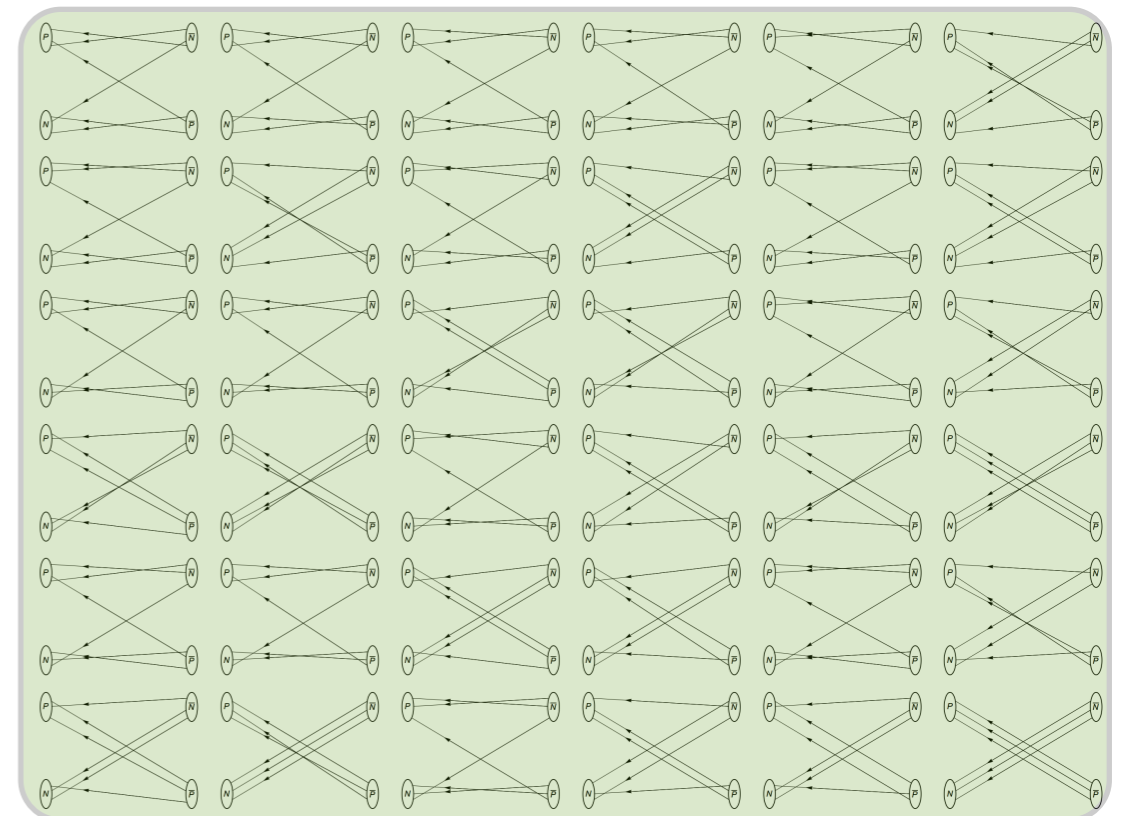
He⁴ : 518400



Nucleon:



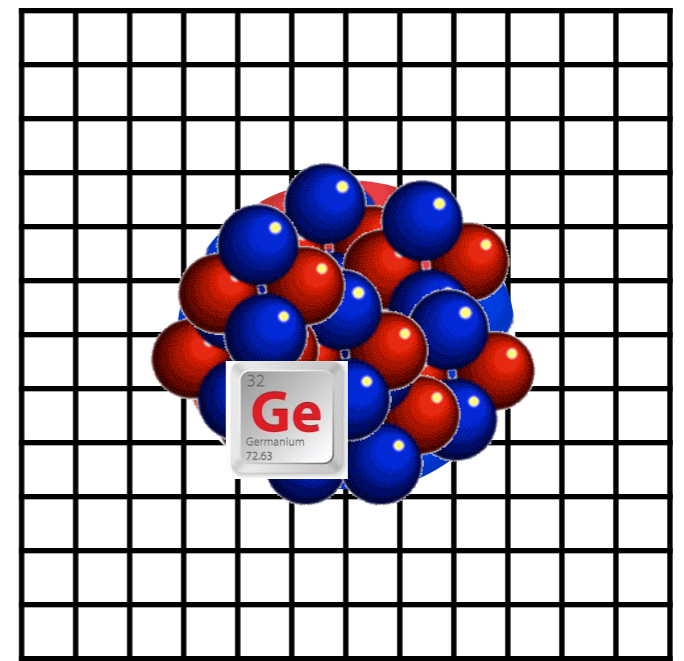
Deuteron:



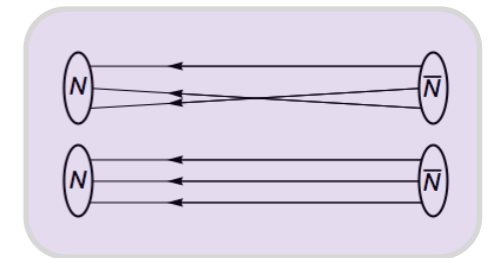
Why?

LQCD will never directly calculate your favorite experimental isotope

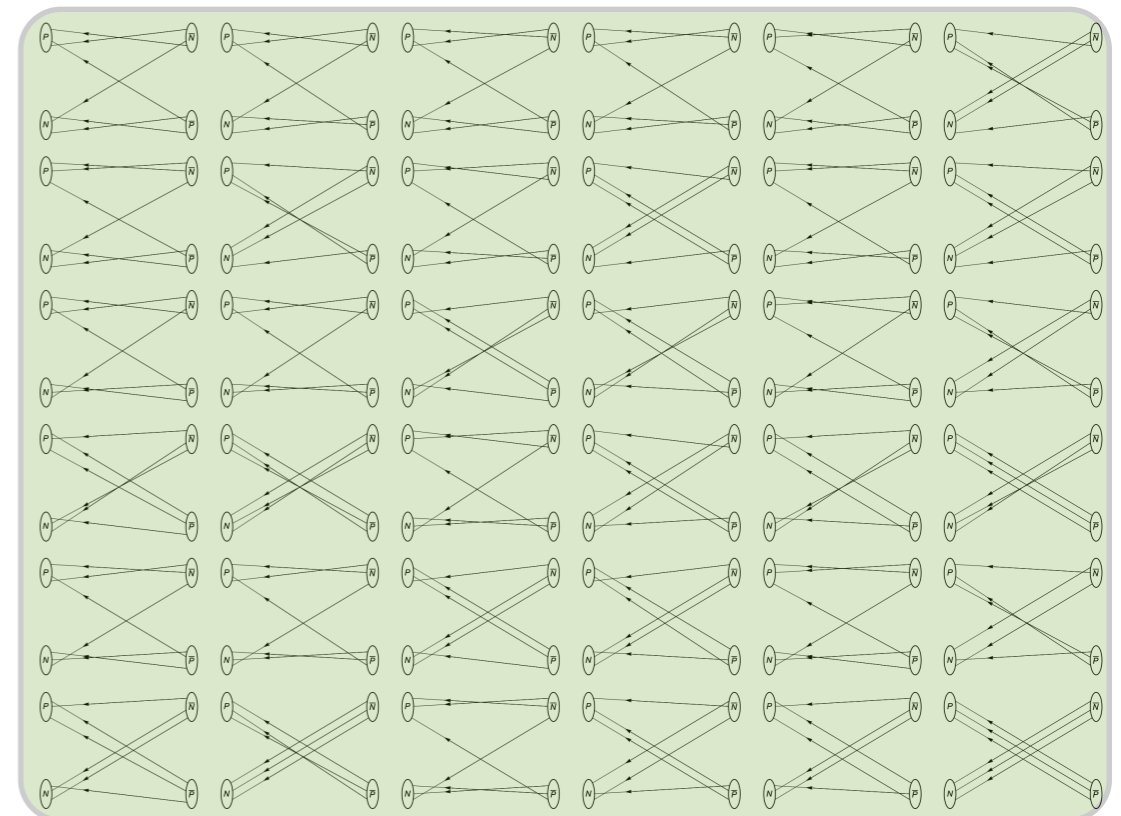
- Need extremely large lattices
- Large range of scales
- Tiny energy splittings
- Wick contractions:
 $(A+Z)! \times (2A-Z)!$ **He⁴ : 518400**
- **Nucleon noise/sign problem**
signal/noise
 $\sim e^{-A(M_n - 3/2m_\pi)t}$



Nucleon:



Deuteron:

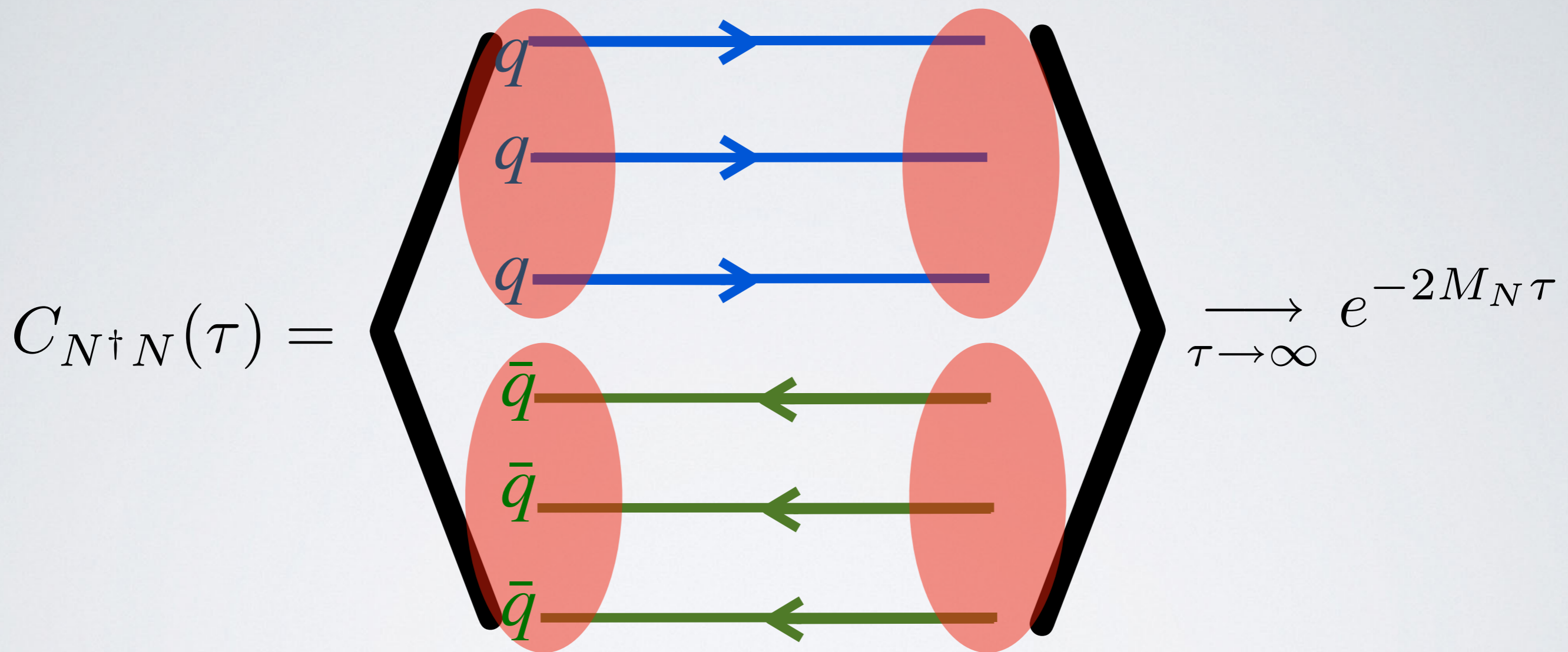


BARYON SNR

$$C_N(\tau) = \left\langle \left(\begin{array}{c} q \\ q \\ q \end{array} \right) \longrightarrow \left(\begin{array}{c} \\ \\ \end{array} \right) \right\rangle \xrightarrow[\tau \rightarrow \infty]{} e^{-M_N \tau}$$

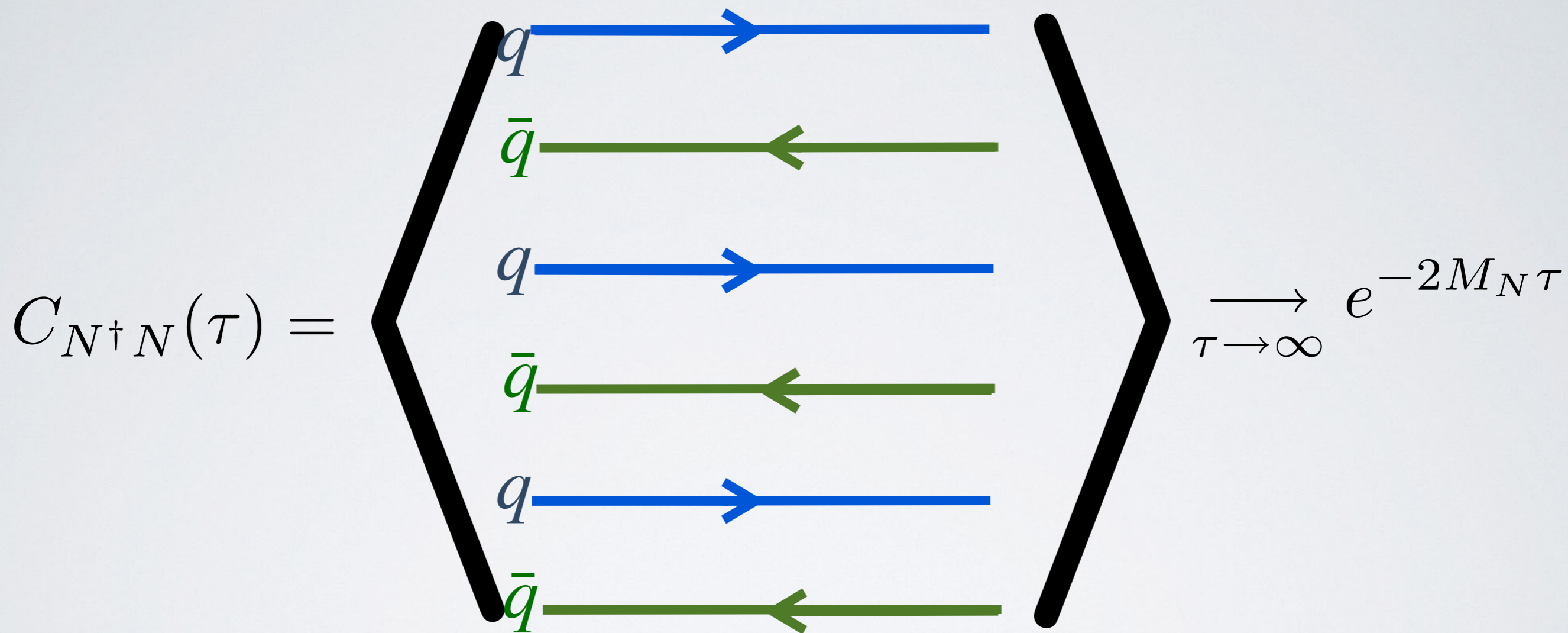
Lepage (1989)

BARYON SNR



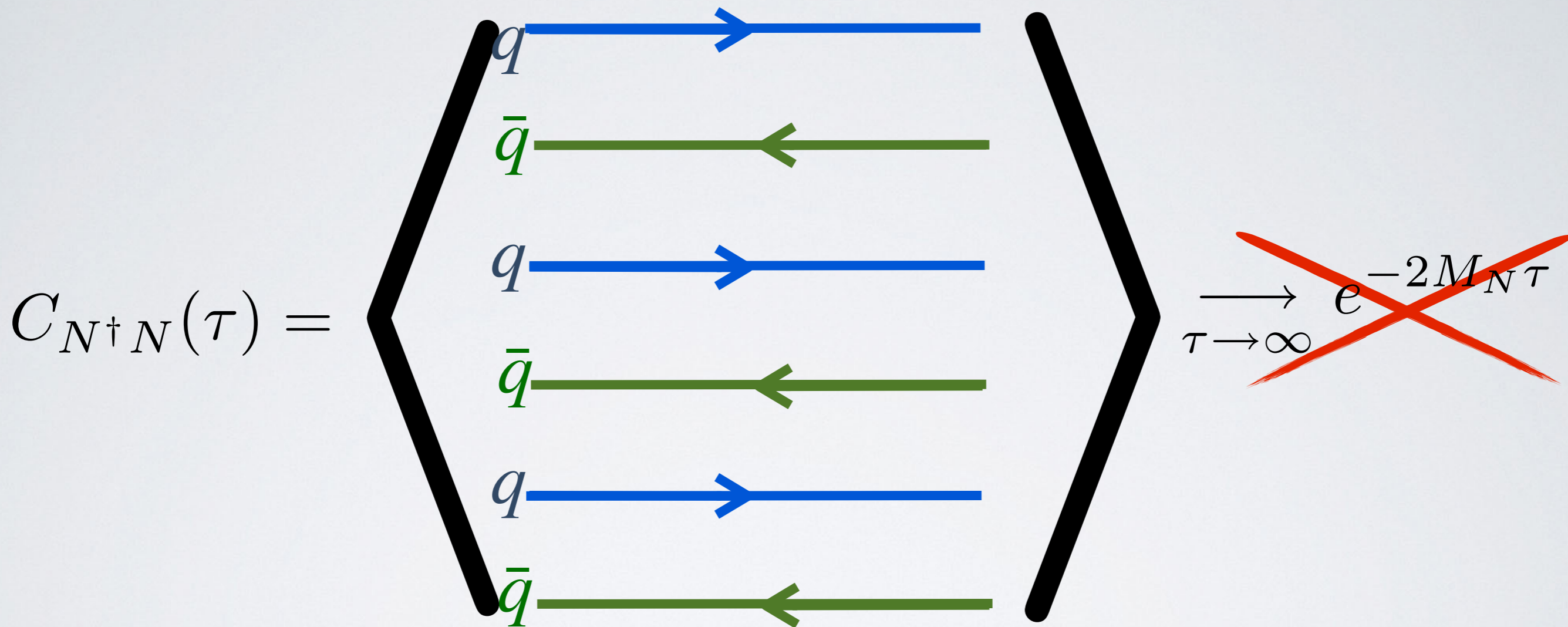
Lepage (1989)

BARYON SNR



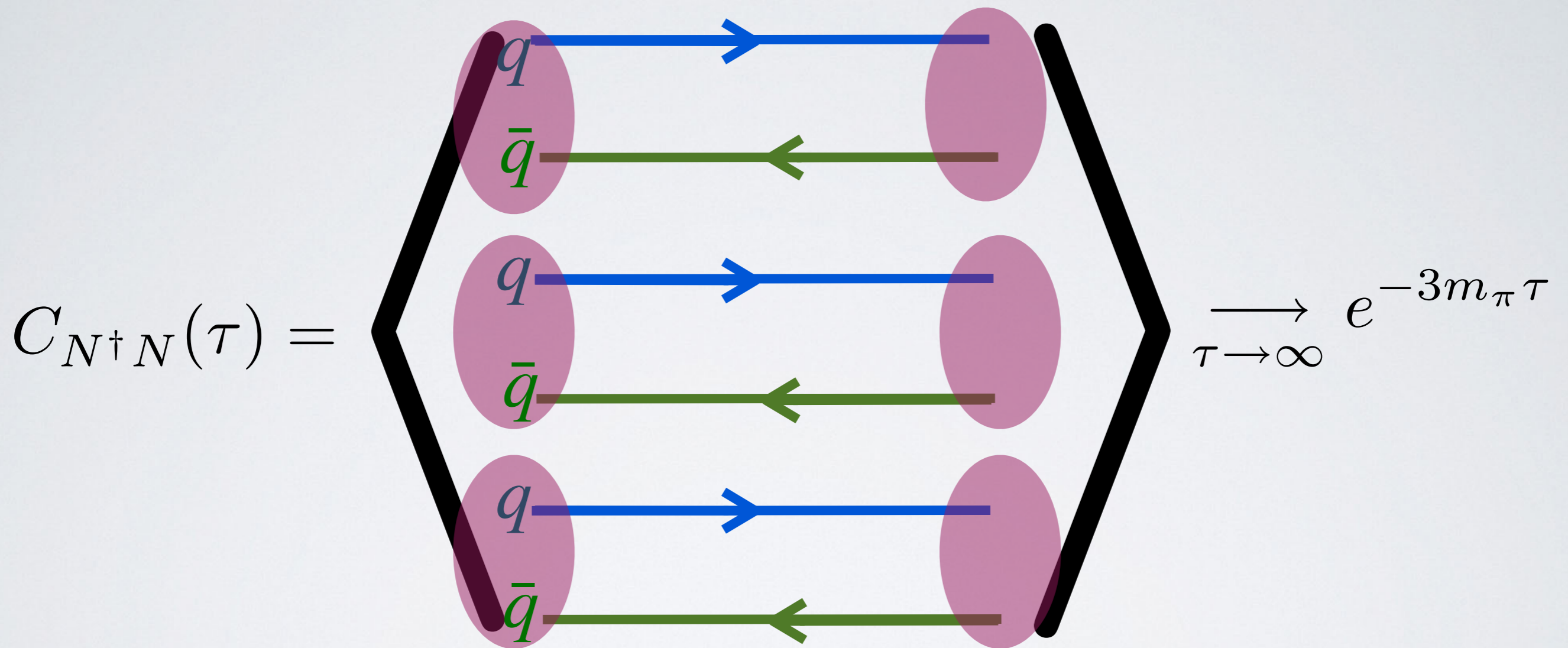
Lepage (1989)

BARYON SNR



Lepage (1989)

BARYON SNR



Lepage (1989)

BARYON SNR

Signal-to-noise ratio:

$$\frac{C_N(\tau)}{\sigma(\tau)} \xrightarrow{\tau \rightarrow \infty} \sqrt{N_{c f g}} e^{-(M_N - 3/2 m_\pi)\tau}$$

Need an exponential number
of measurements to see a signal

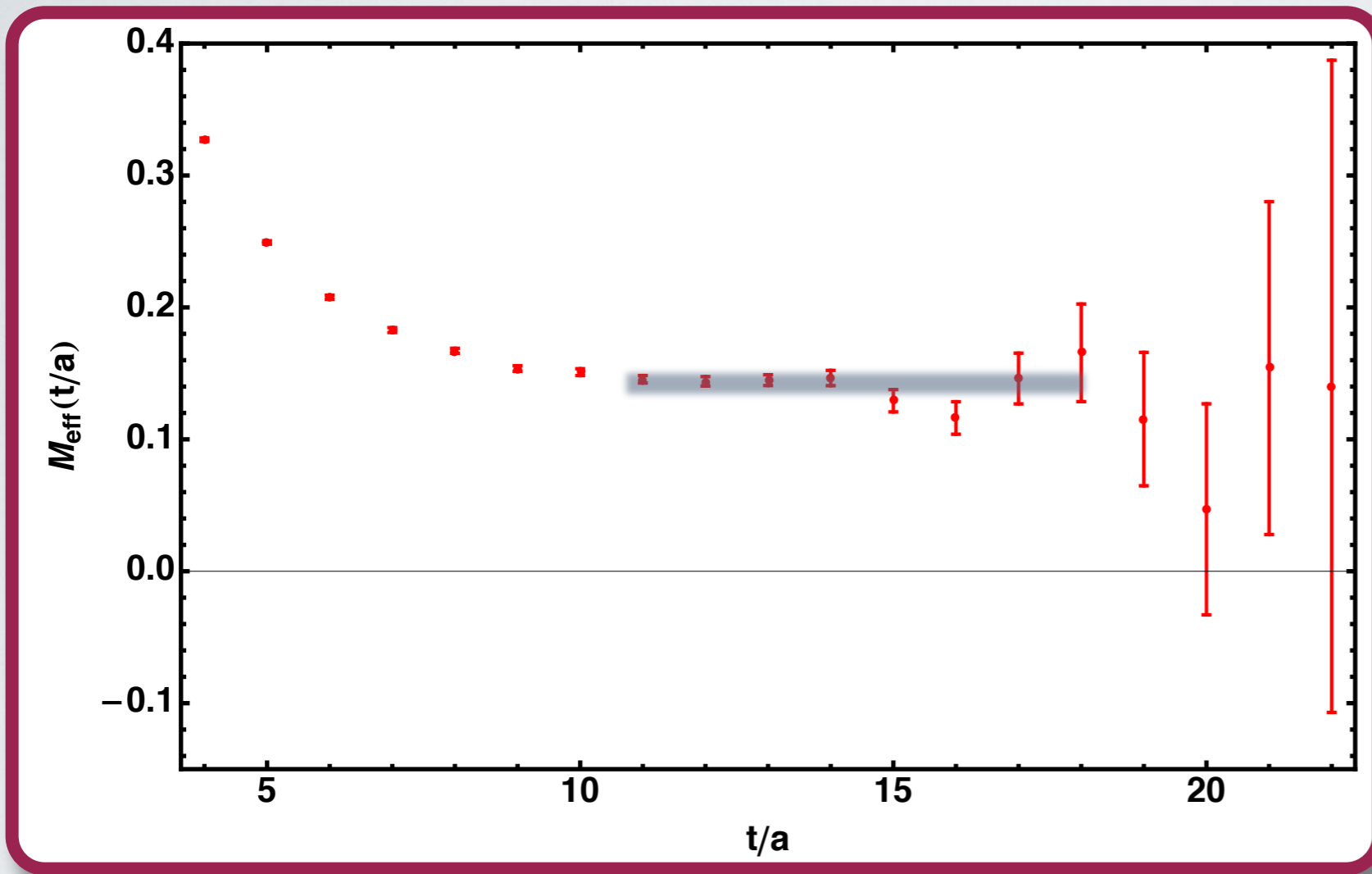
BARYON SNR

Signal-to-noise ratio:

$$\frac{C_{NA}(\tau)}{\sigma(\tau)} \xrightarrow{\tau \rightarrow \infty} \sqrt{N_{c f g}} e^{-A(M_N - 3/2 m_\pi)\tau}$$

Need an exponential number
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BARYON SNR

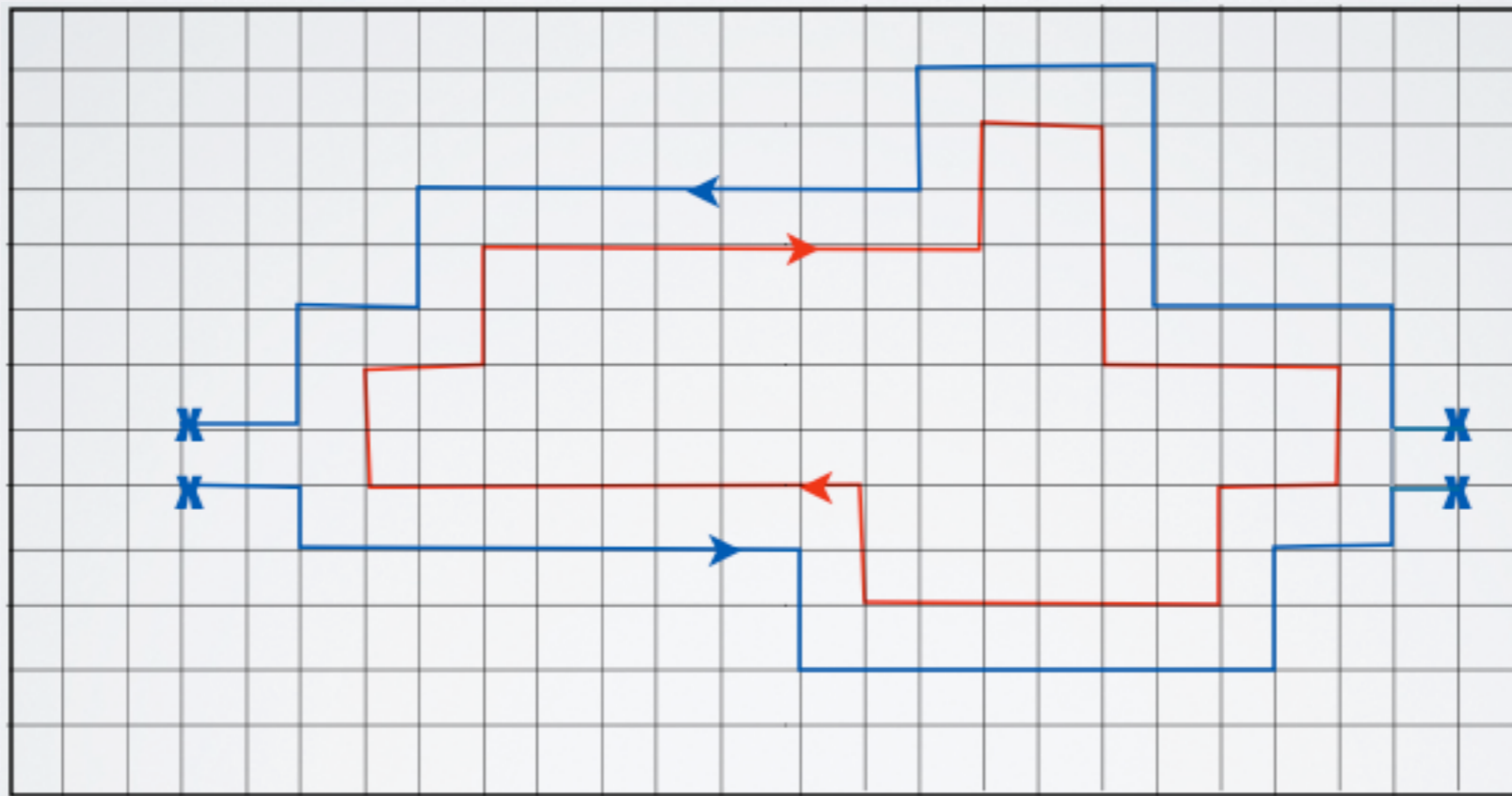


} $\sim e^{A(M_n - 3/2m_\pi)t}$

OVERLAP PROBLEM

Kaplan (sometime back
when I was a student)

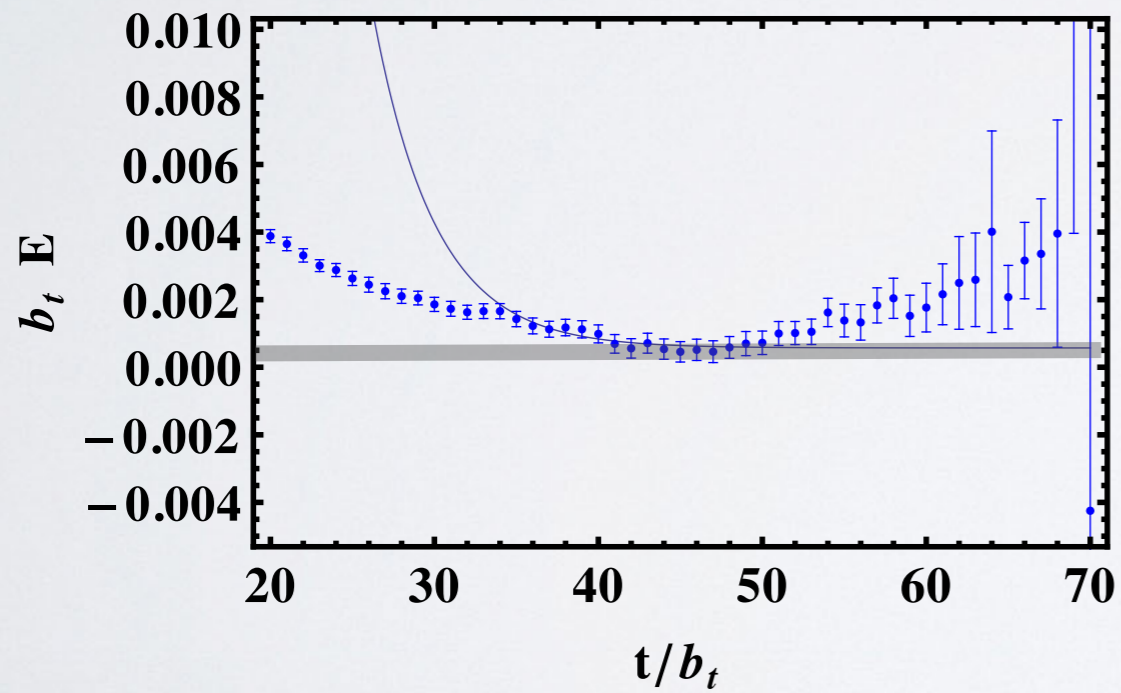
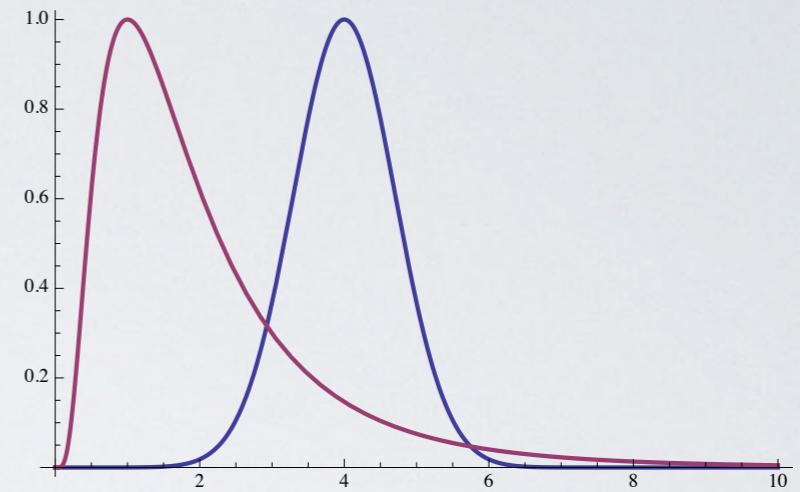
$$Z_A = \int \mathcal{D}A \det M_F(A) e^{-S_{YM}}$$



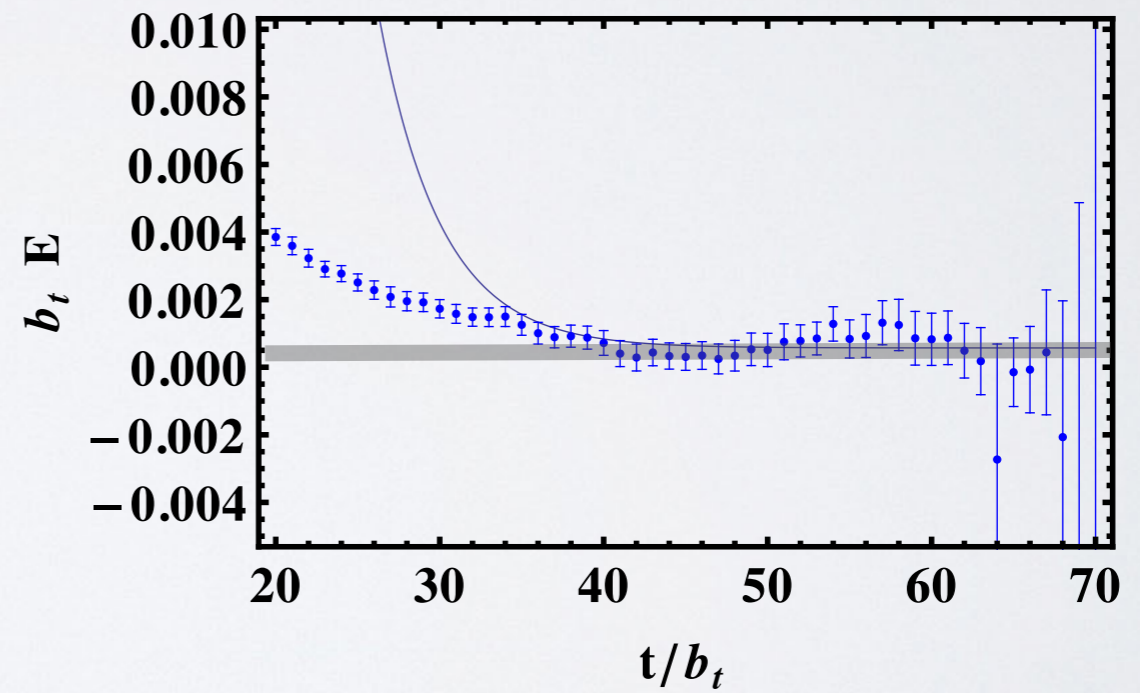
OVERLAP PROBLEM

Kaplan, Endres, Lee, A.N. (2011)

Correlator distributions

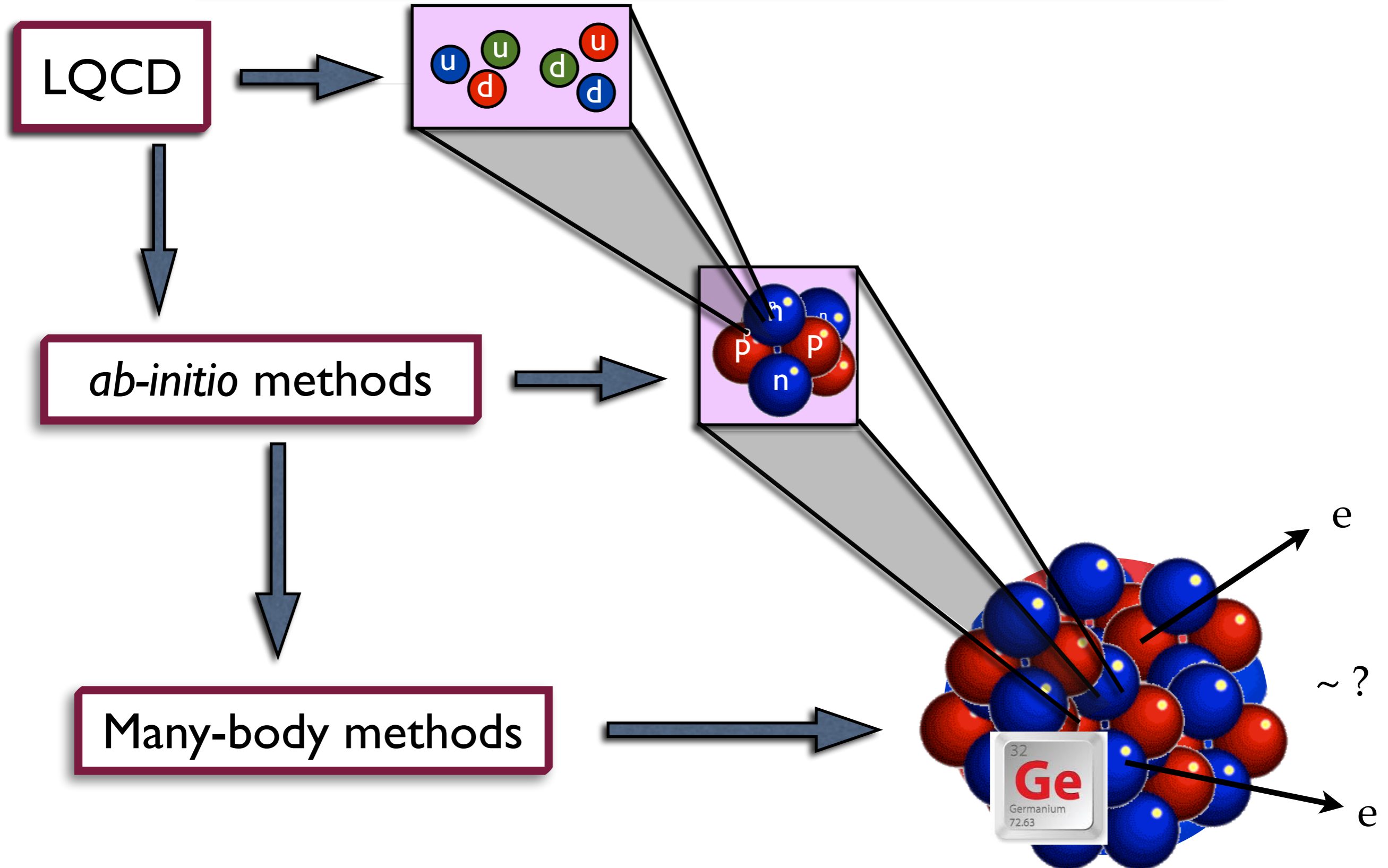


Standard

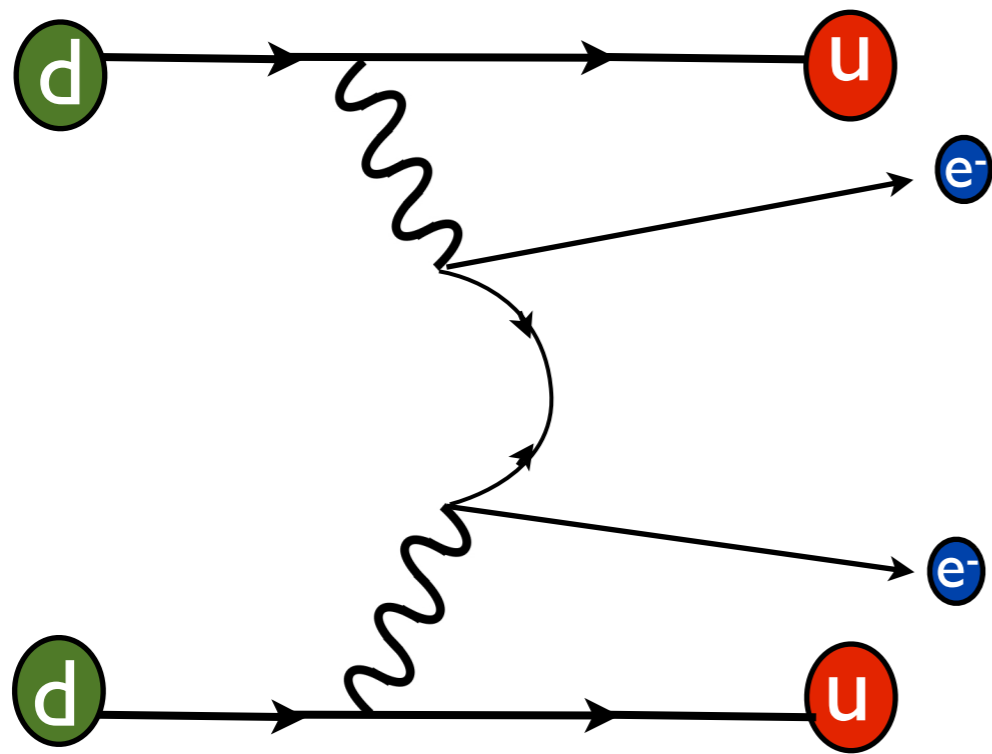


Cumulant Expansion

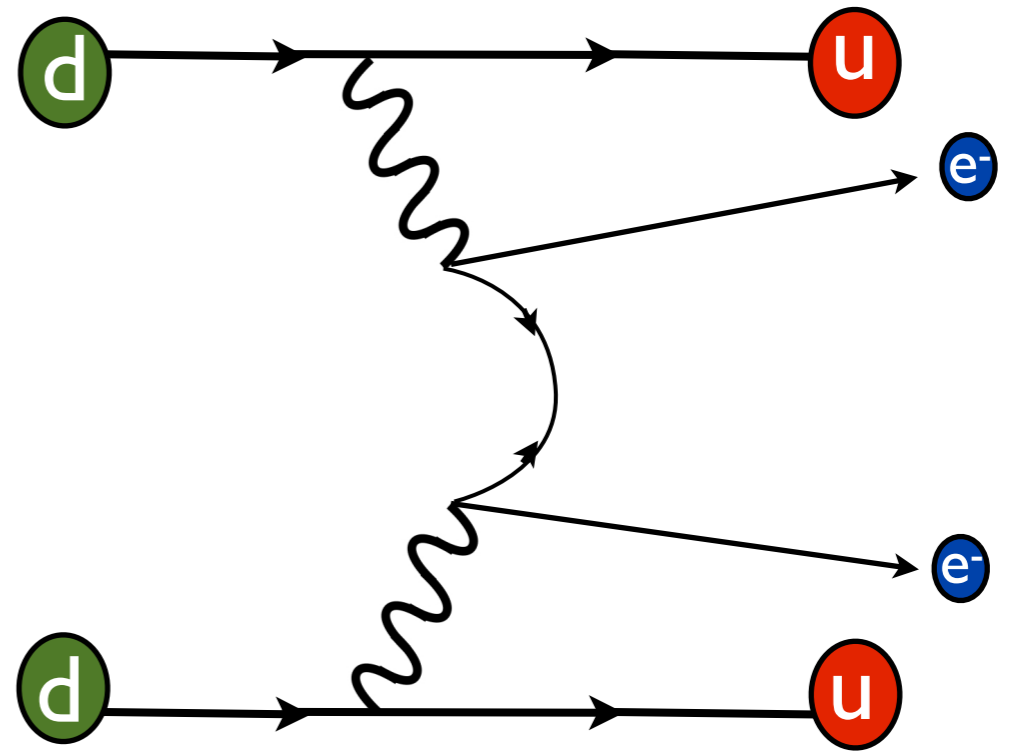
Relating Theory to Experiment



From quark to hadronic scales

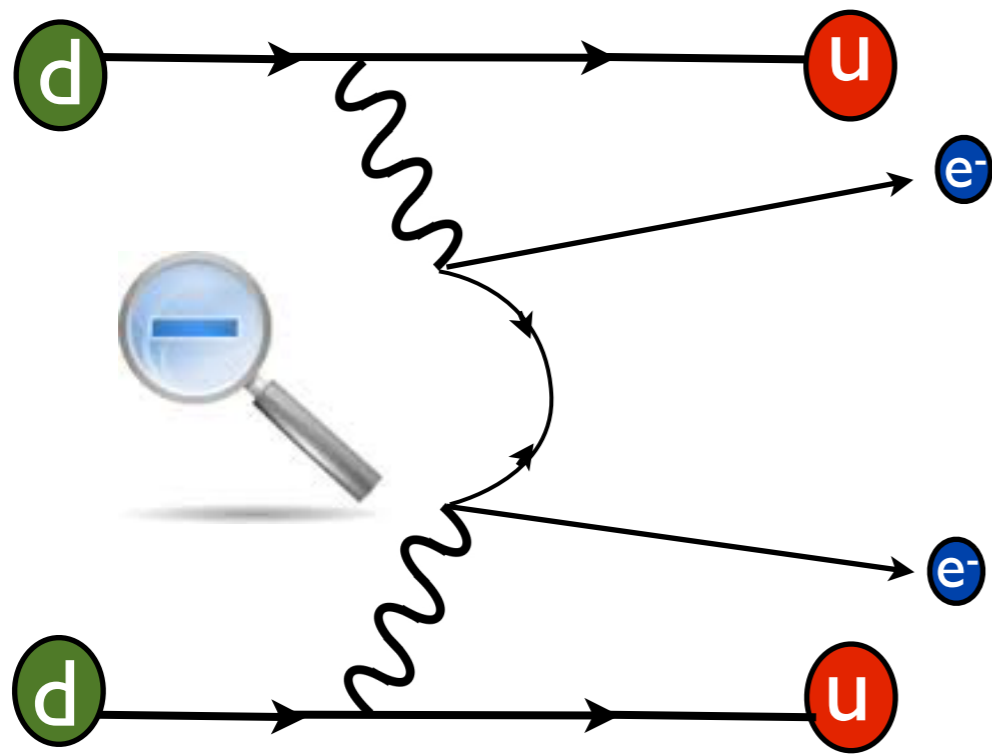


Long-range

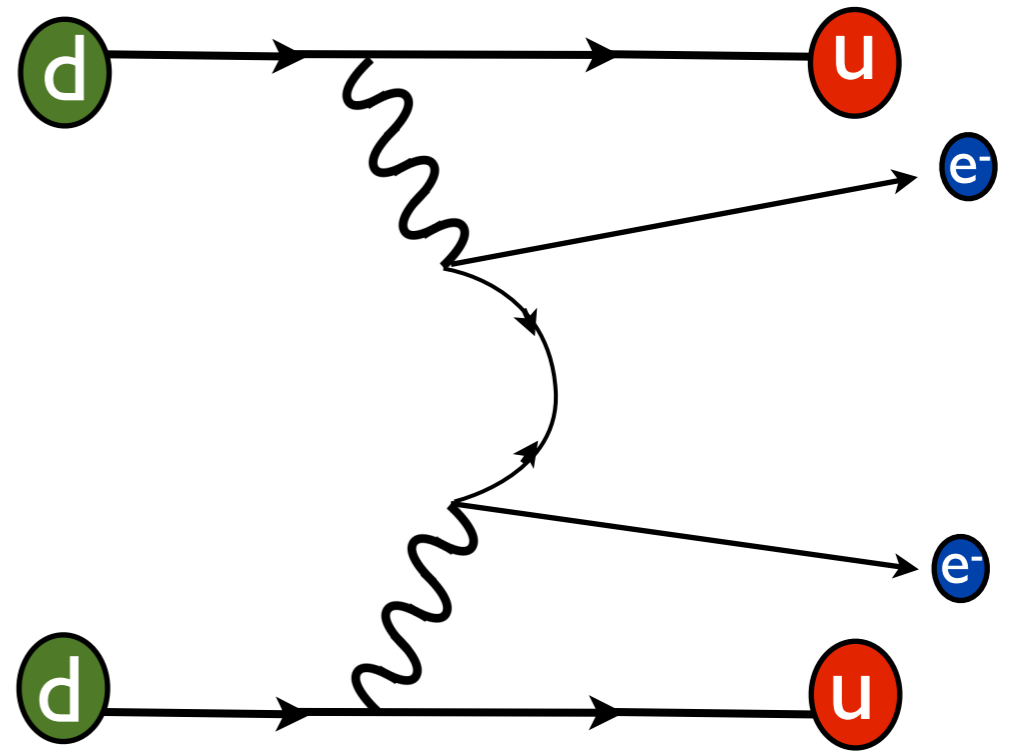


Short-range

From quark to hadronic scales



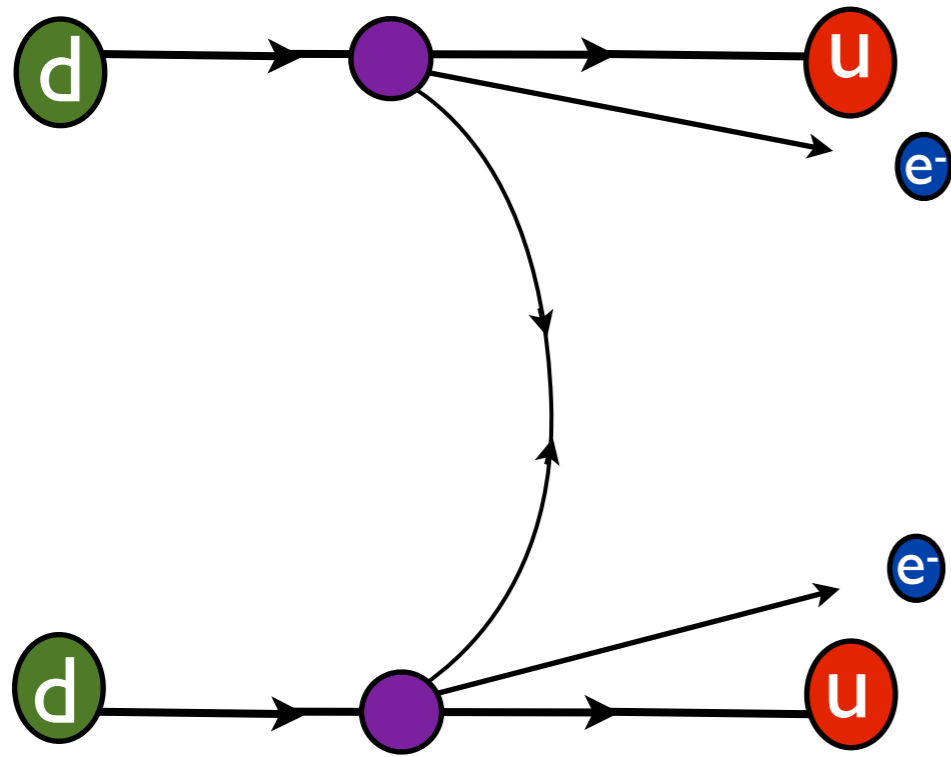
Long-range



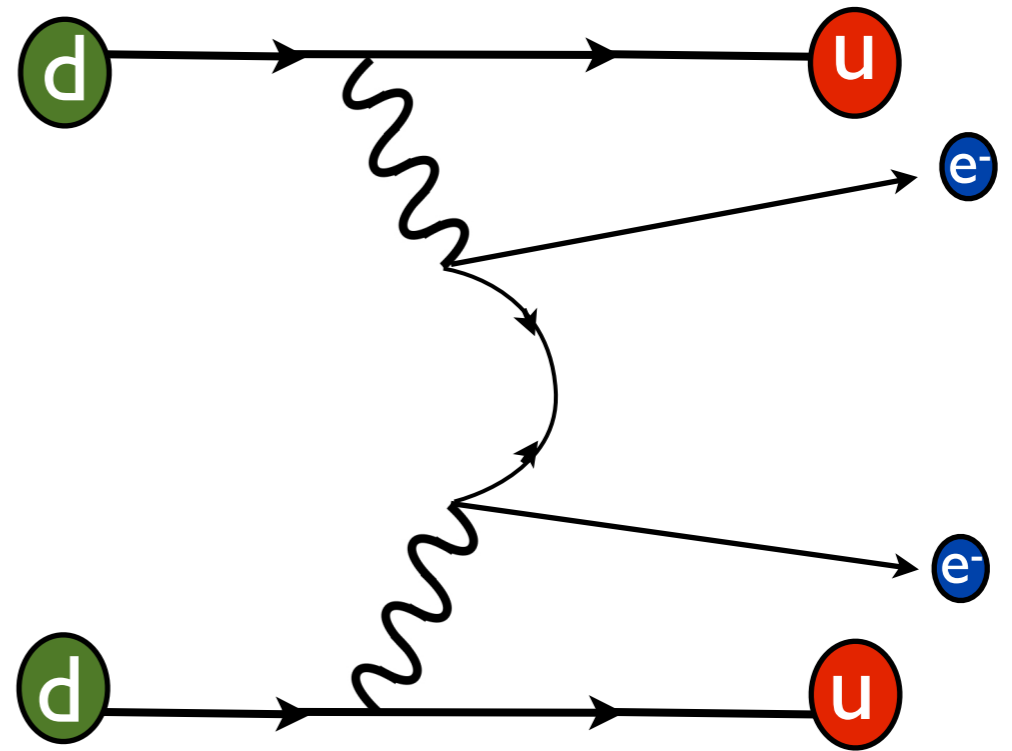
Short-range

$$\Lambda \ll M_W$$

From quark to hadronic scales

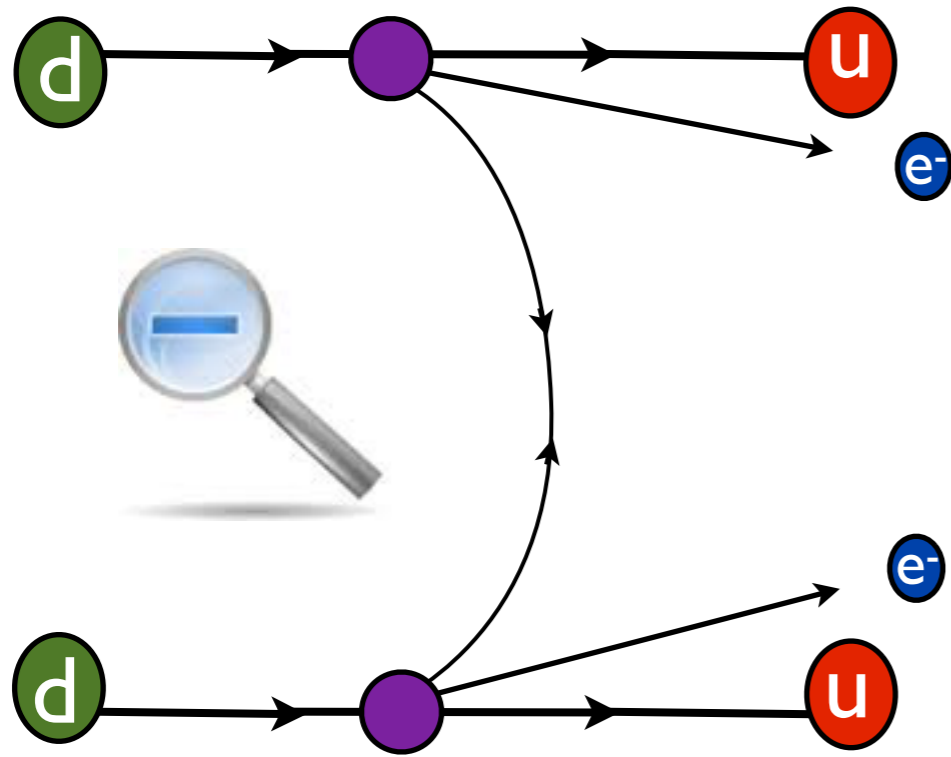


Long-range



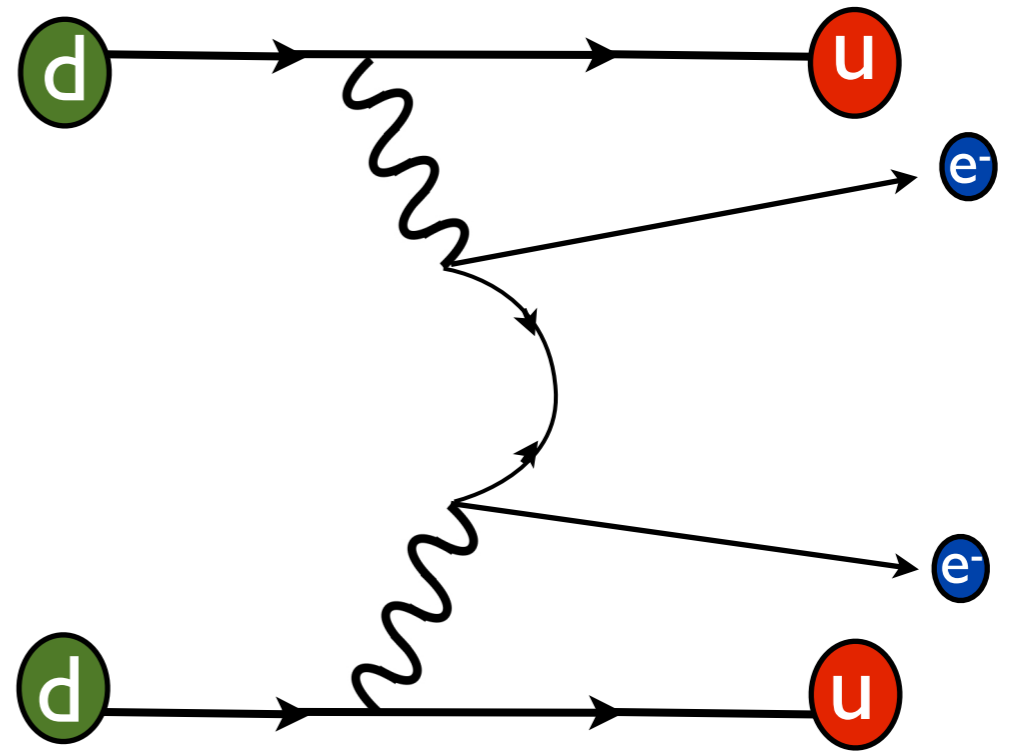
Short-range

From quark to hadronic scales



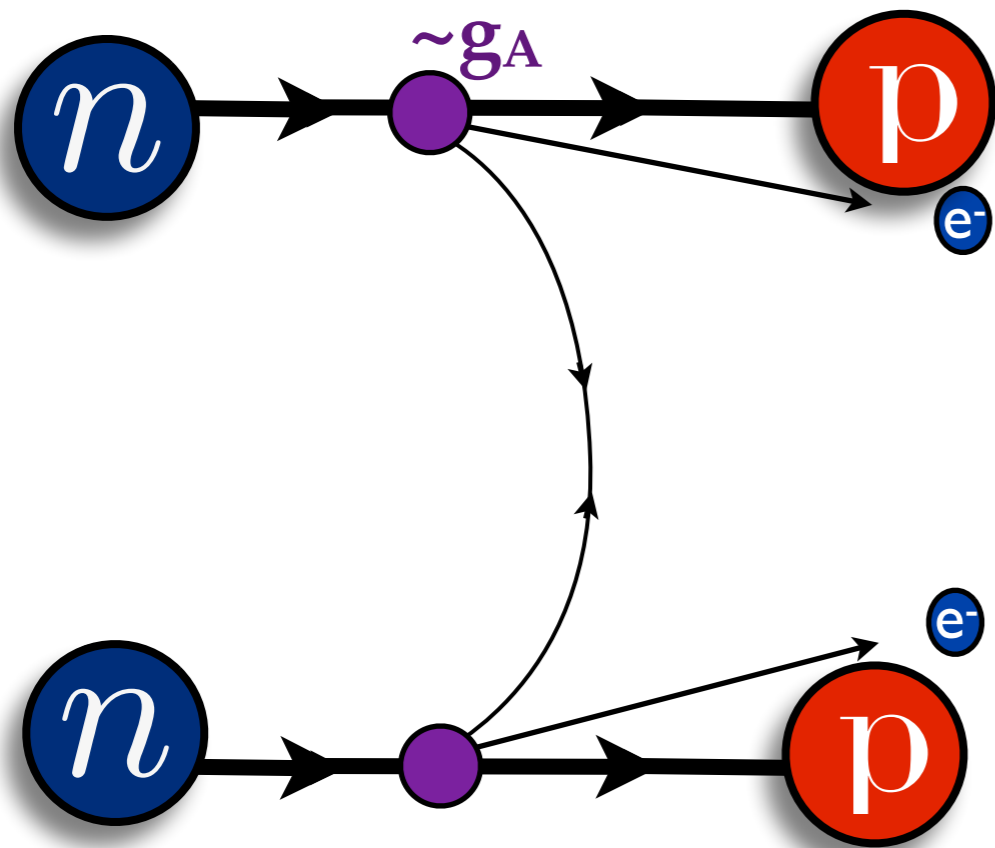
Long-range

$$\Lambda \ll \Lambda_{\text{QCD}}$$

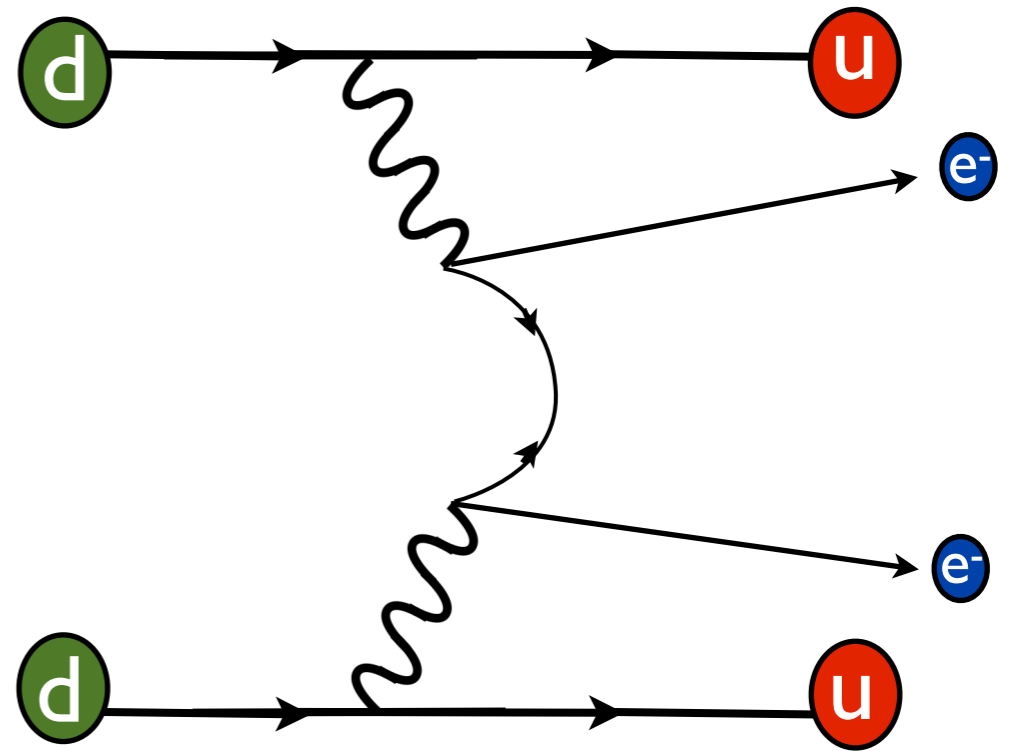


Short-range

From quark to hadronic scales

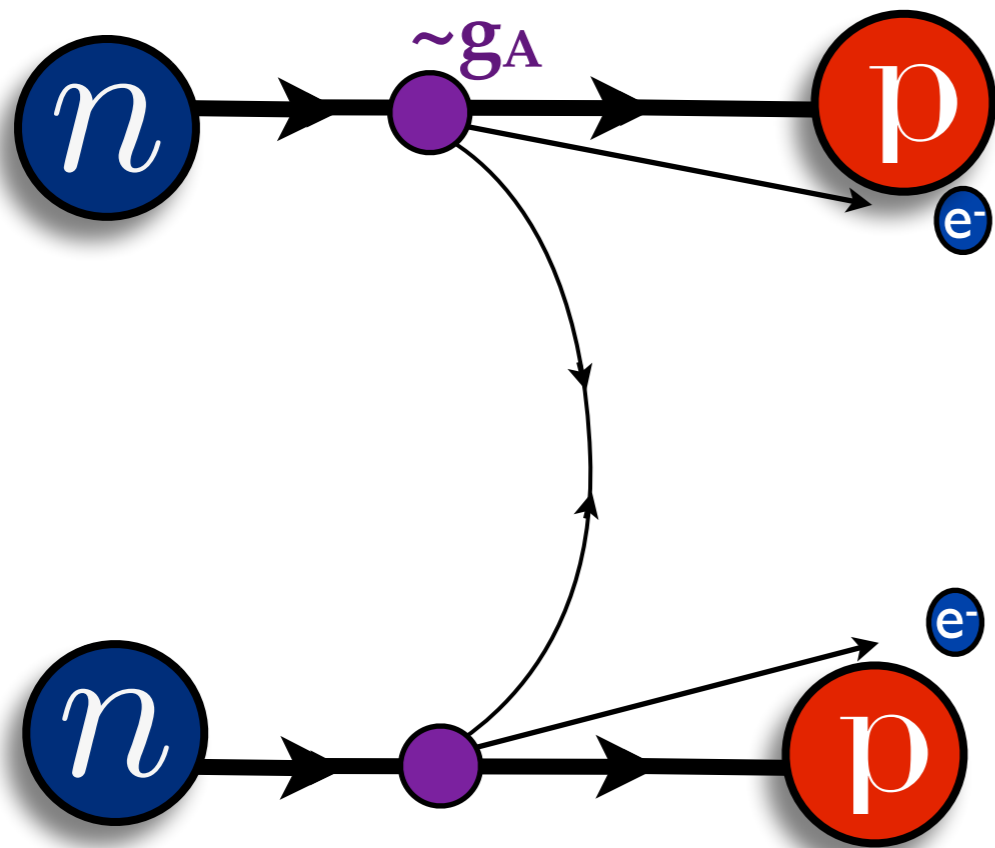


Long-range

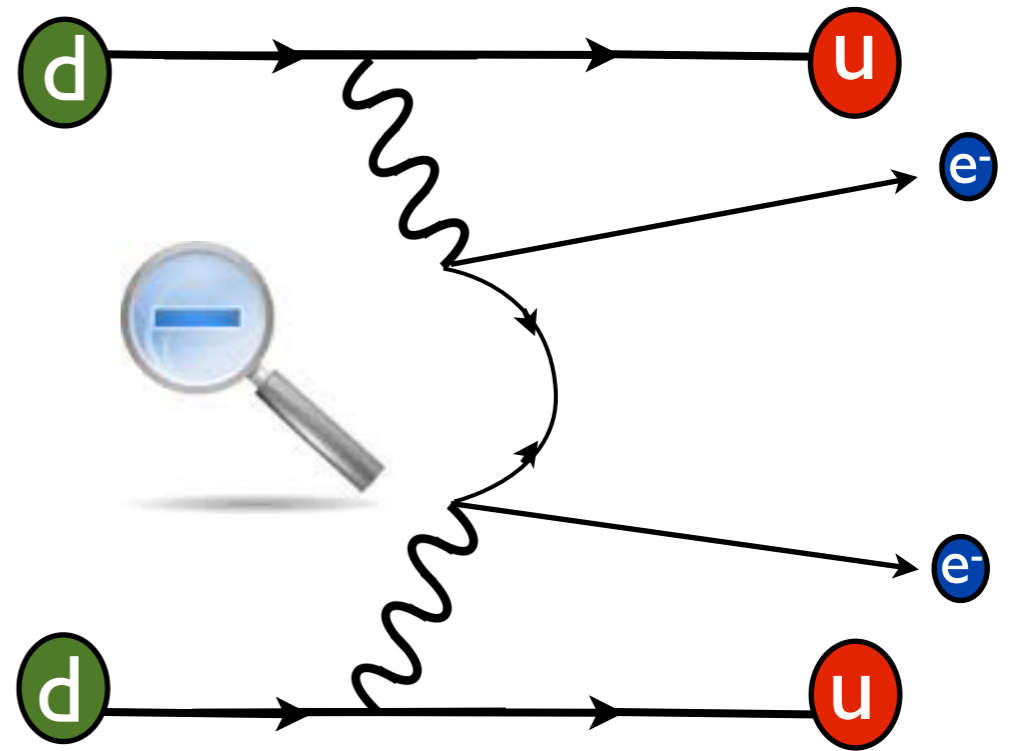


Short-range

From quark to hadronic scales



Long-range

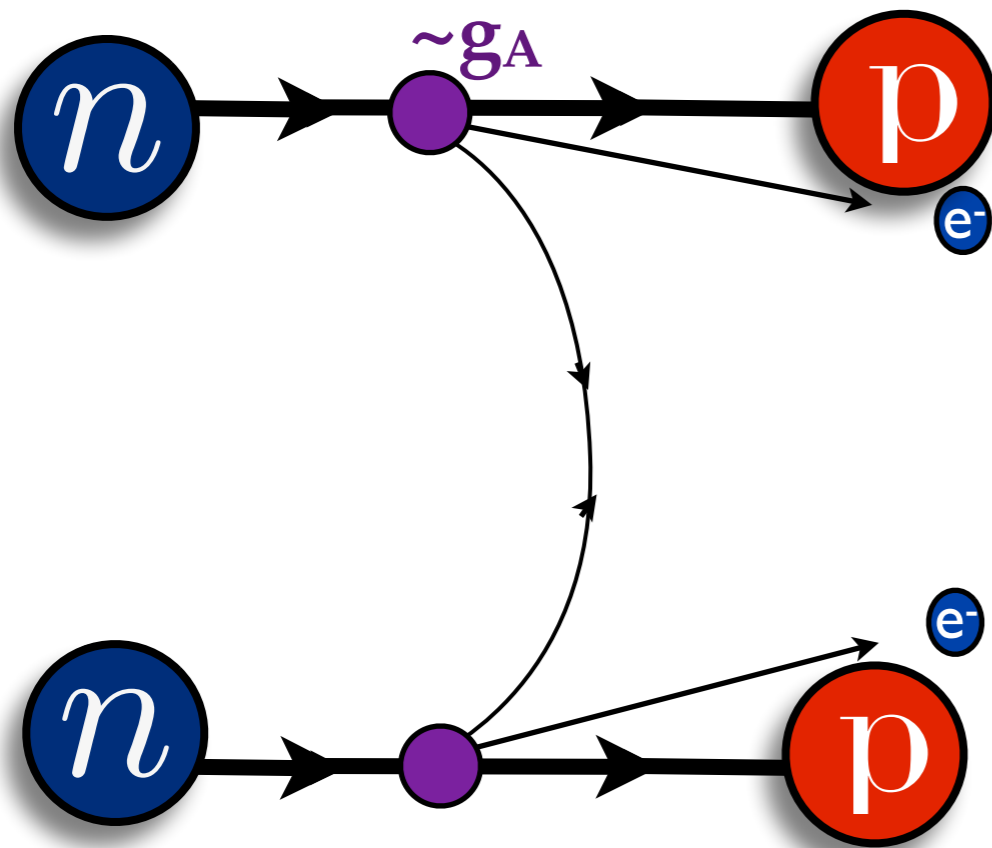


Short-range

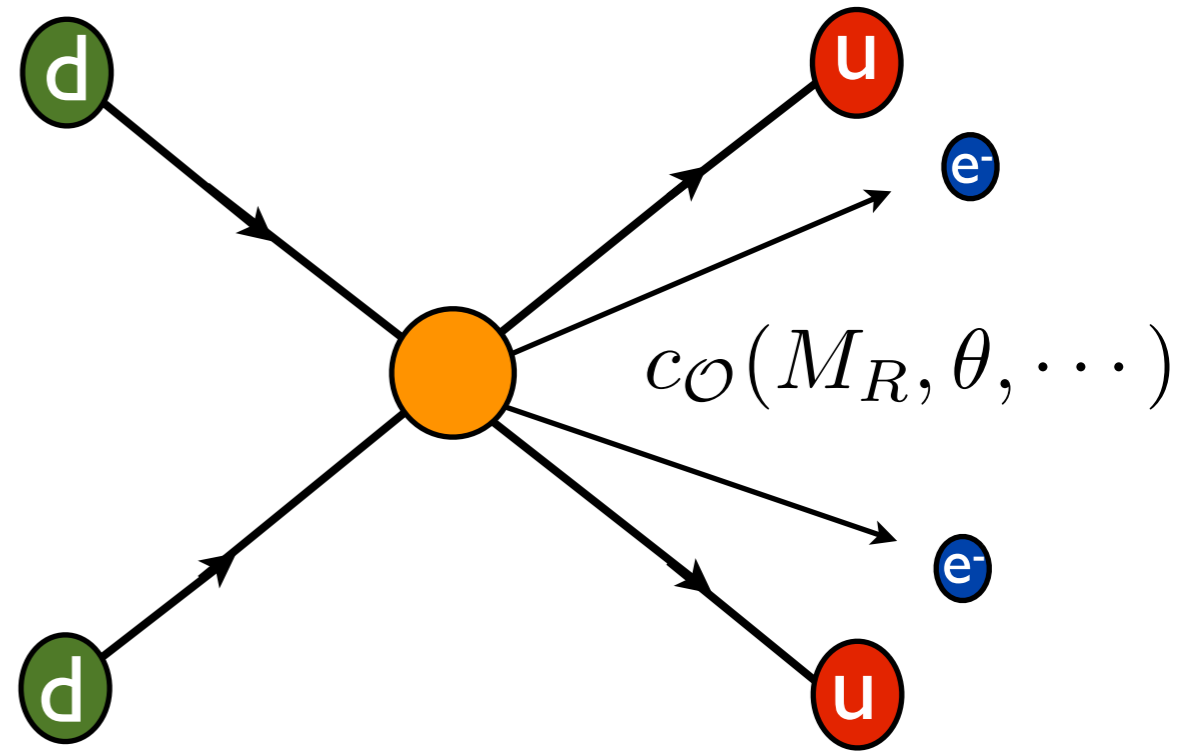
$$\Lambda \ll M_W$$

From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



Long-range



Short-range

$$\mathcal{O}_{1+}^{ab} = (\bar{q}_L \tau^a \gamma^\mu q_L) (\bar{q}_R \tau^b \gamma_\mu q_R),$$

$$\mathcal{O}_{2\pm}^{ab} = (\bar{q}_R \tau^a q_L) (\bar{q}_R \tau^b q_L) \pm (\bar{q}_L \tau^a q_R) (\bar{q}_L \tau^b q_R),$$

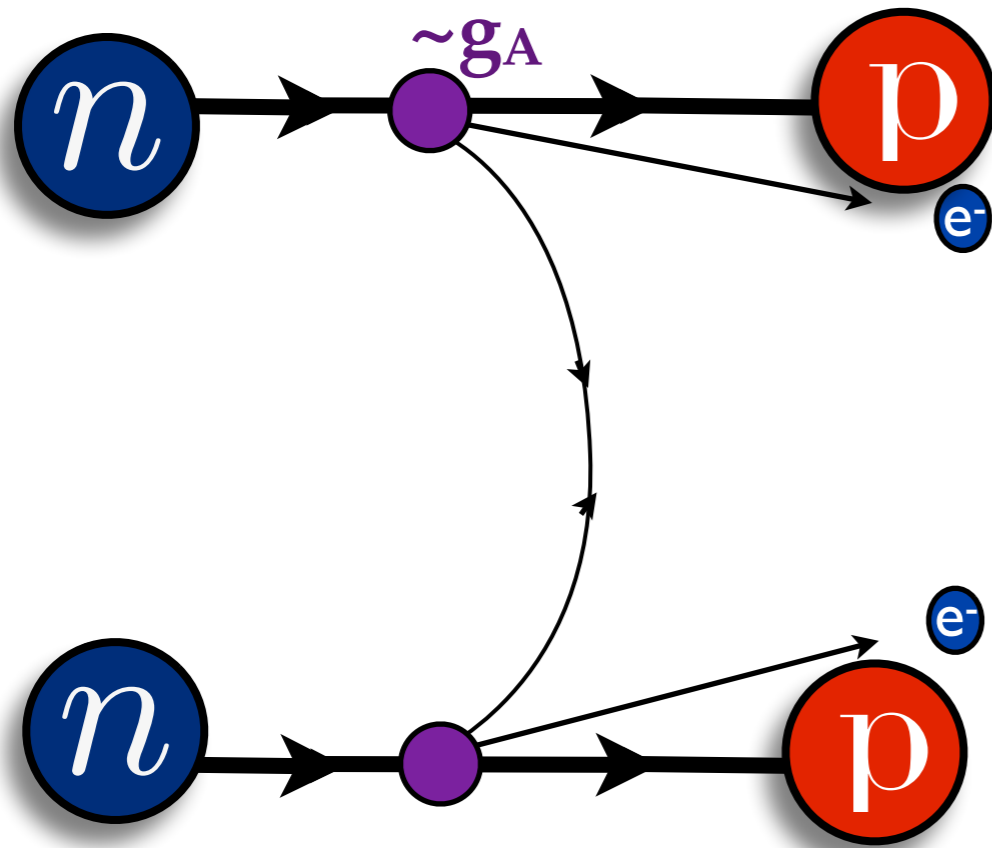
$$\mathcal{O}_{3\pm}^{ab} = (\bar{q}_L \tau^a \gamma^\mu q_L) (\bar{q}_L \tau^b \gamma_\mu q_L) \pm (\bar{q}_R \tau^a \gamma^\mu q_R) (\bar{q}_R \tau^b \gamma_\mu q_R),$$

$$\mathcal{O}_{4\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \mp \bar{q}_R \tau^a \gamma^\mu q_R) (\bar{q}_L \tau^b q_R - \bar{q}_R \tau^b q_L),$$

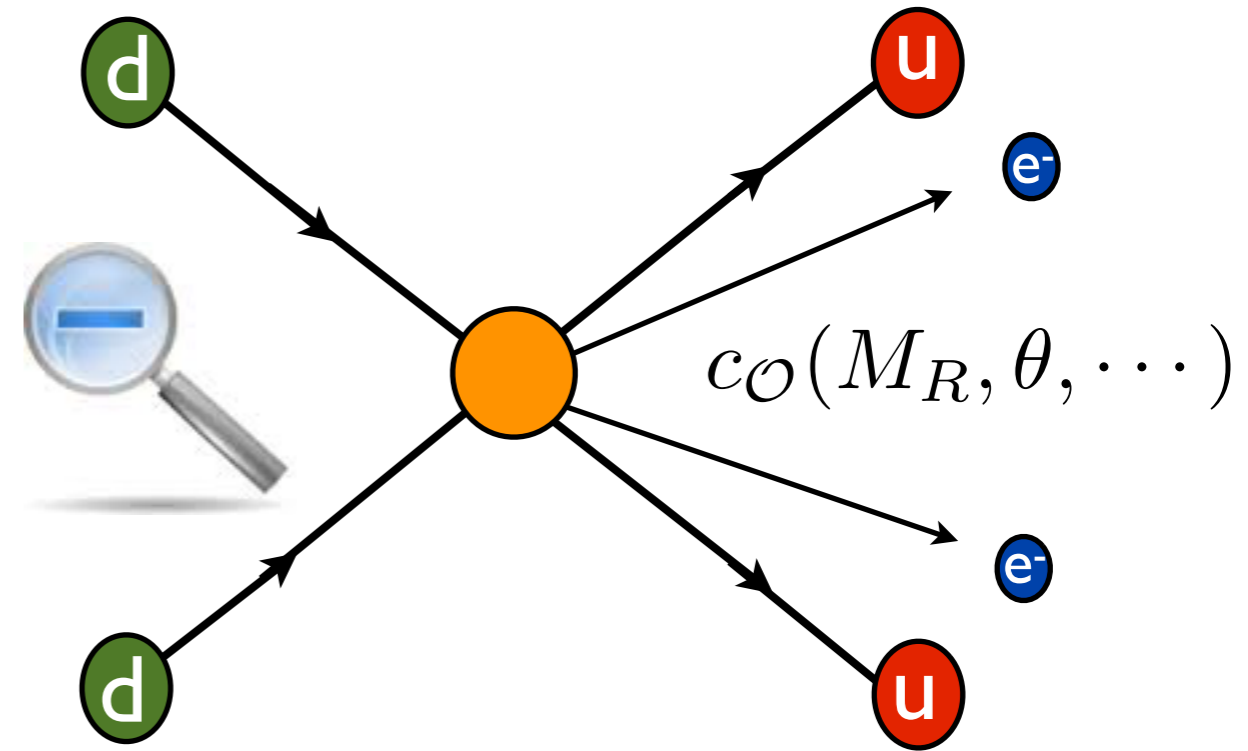
$$\mathcal{O}_{5\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \pm \bar{q}_R \tau^a \gamma^\mu q_R) (\bar{q}_L \tau^b q_R + \bar{q}_R \tau^b q_L).$$

From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



Long-range

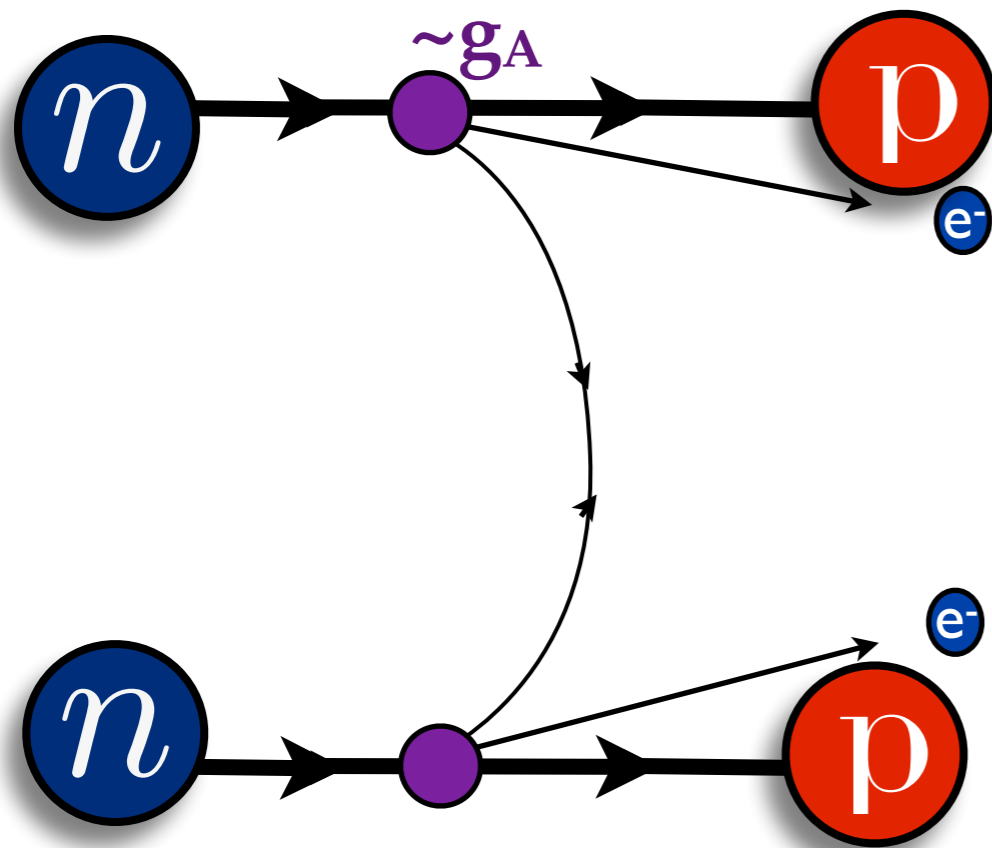


Short-range

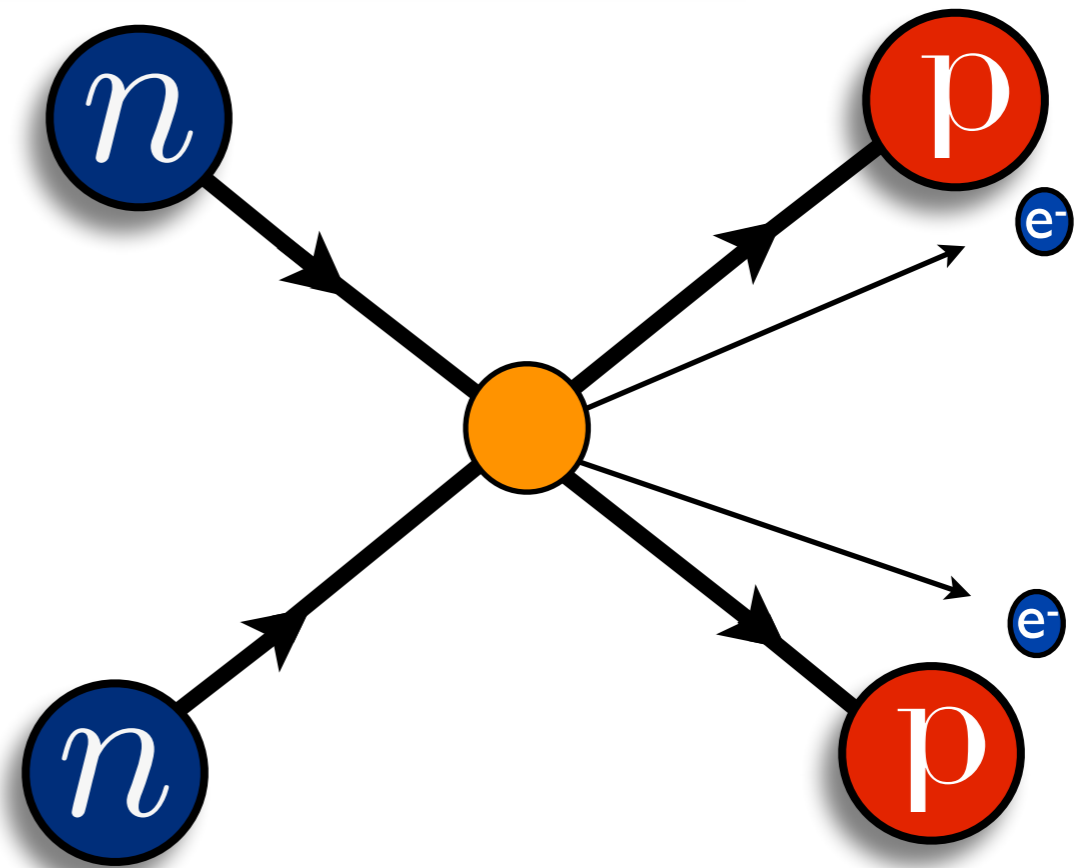
$\Lambda \ll \Lambda_{\text{QCD}}$

From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



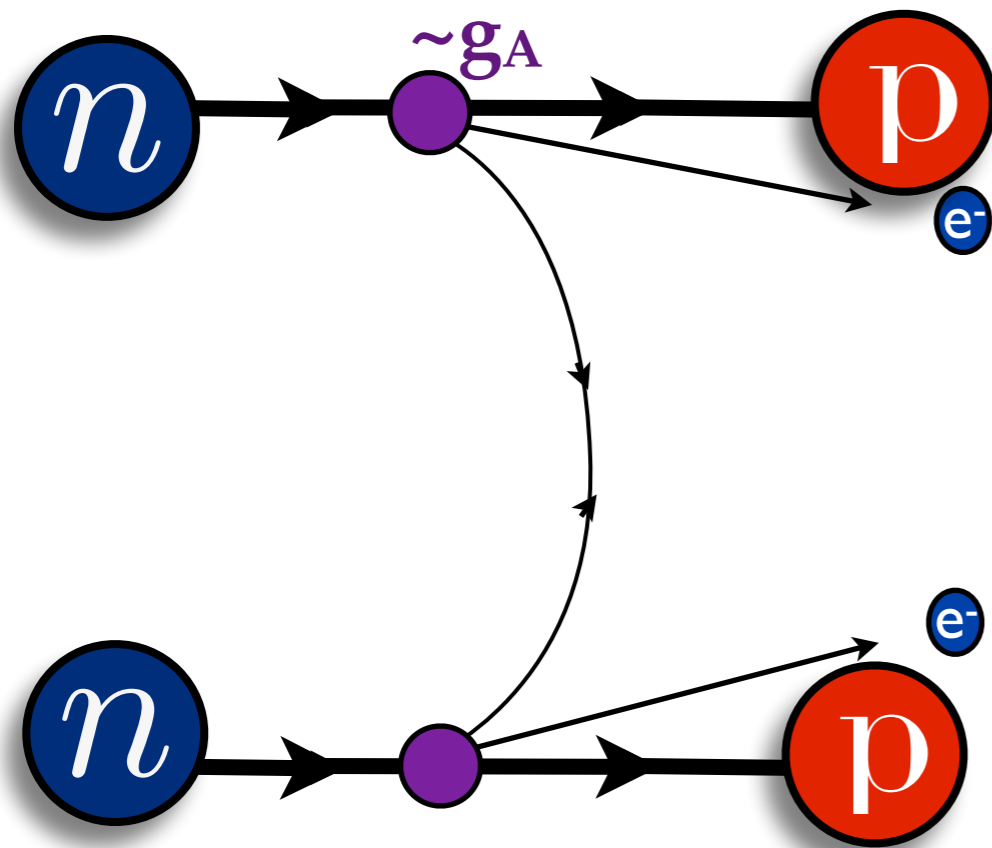
Long-range



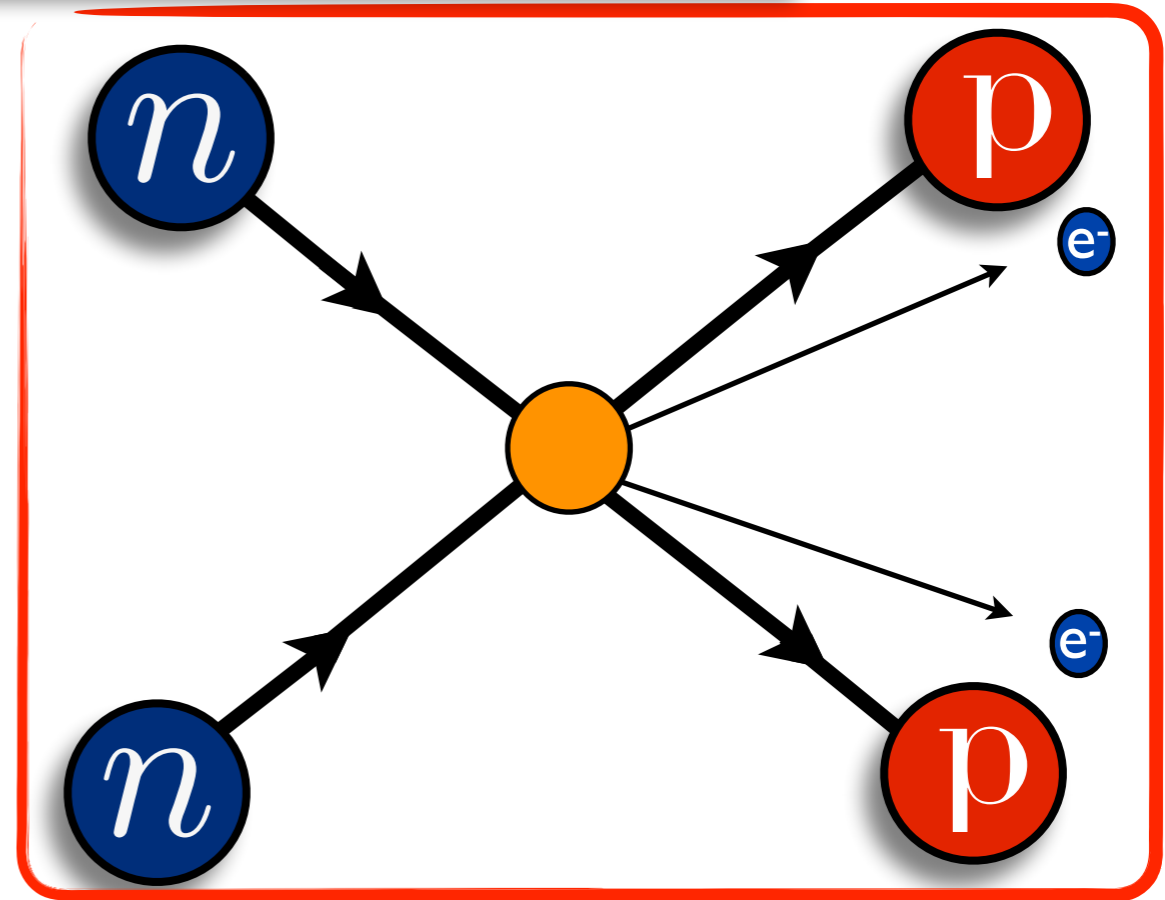
Short-range

From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



Long-range

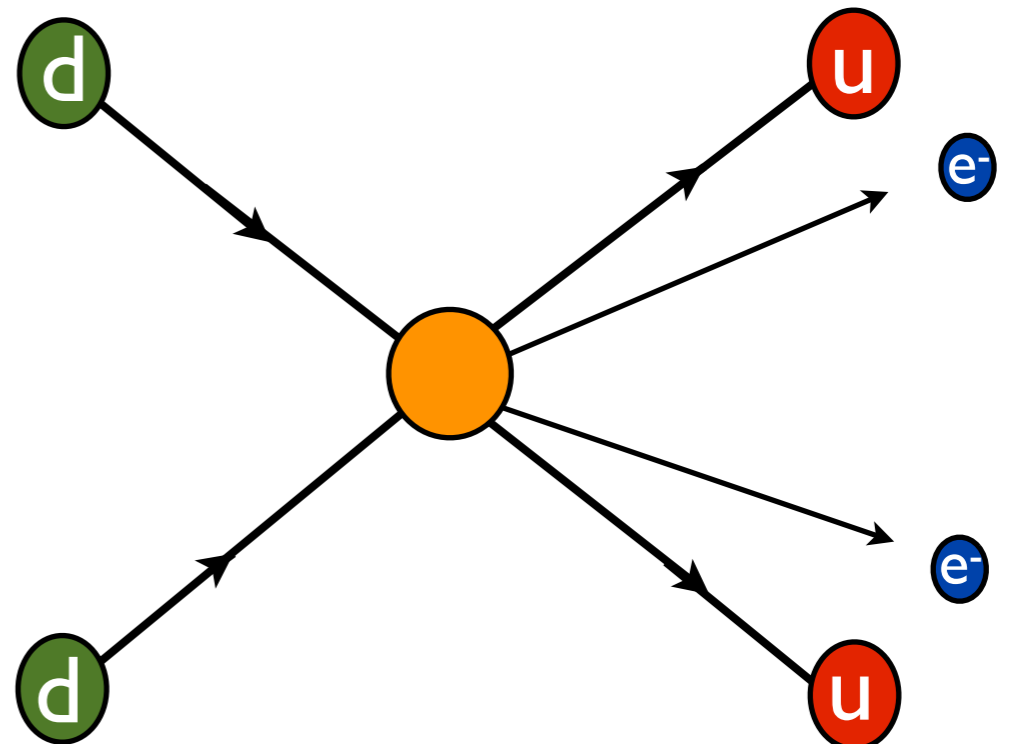
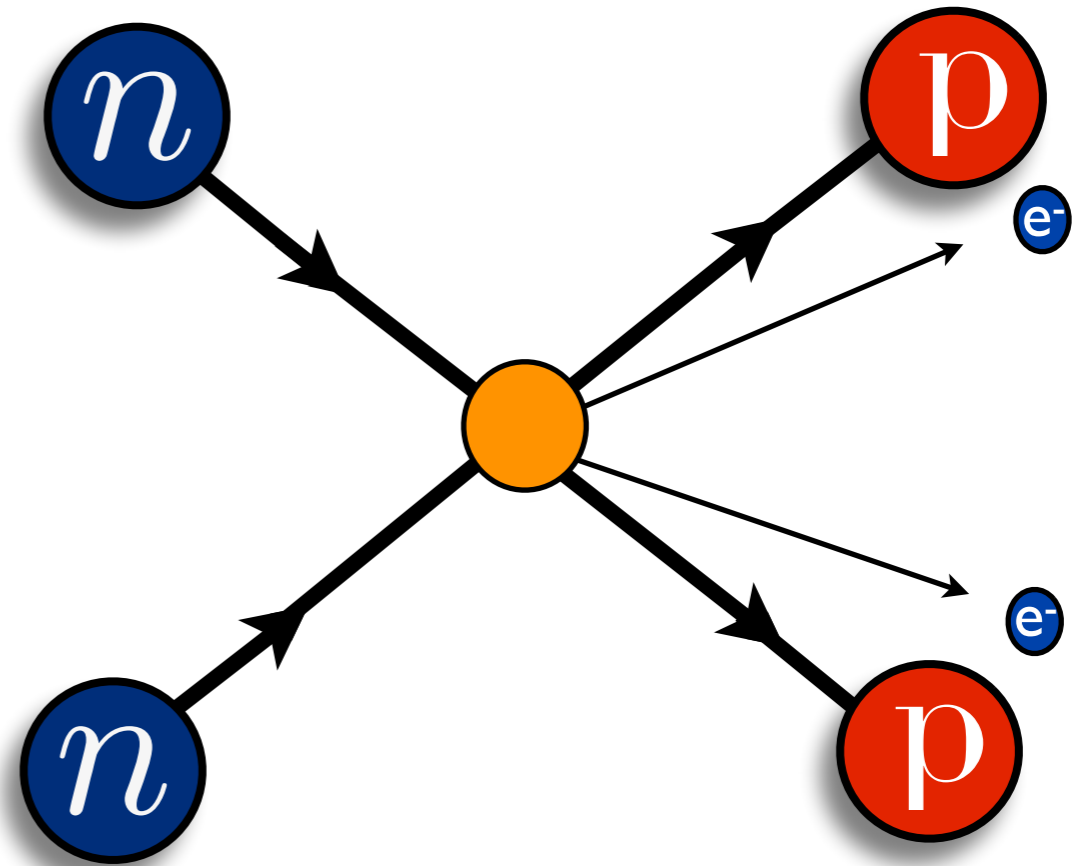
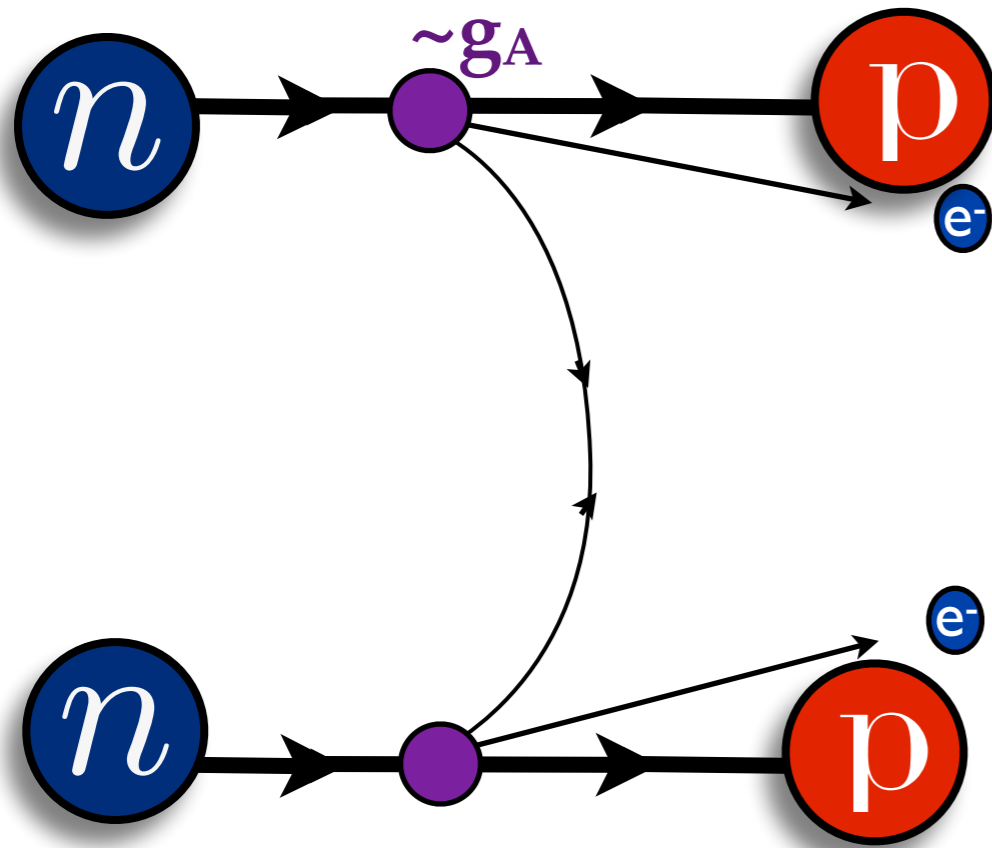


Short-range

Unknown from experiment

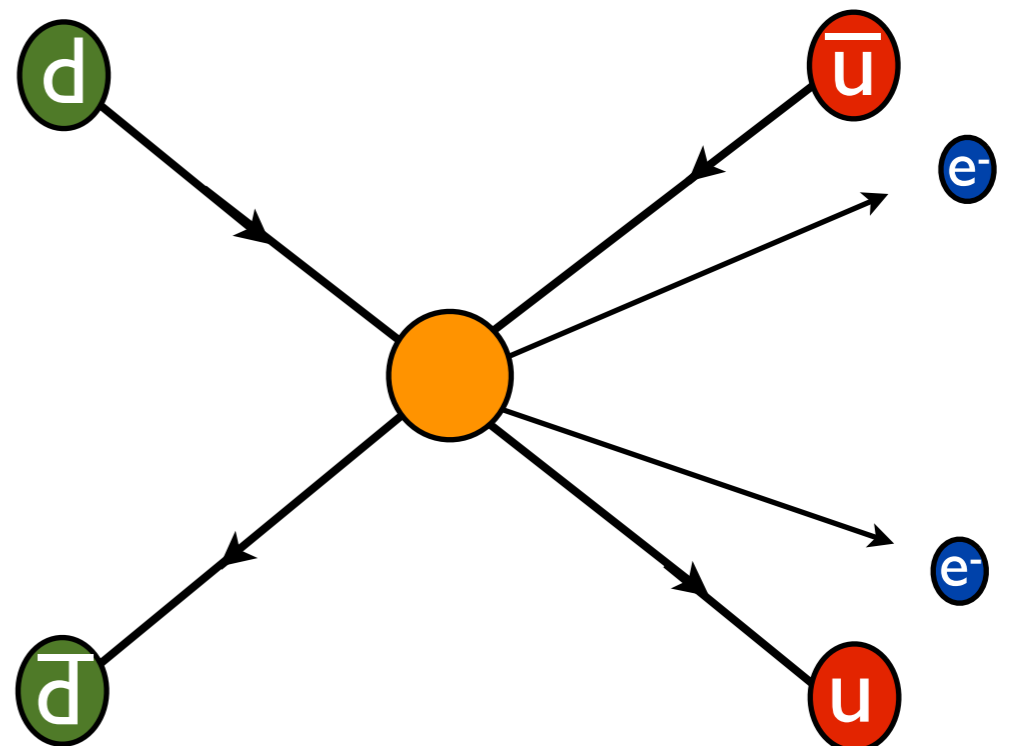
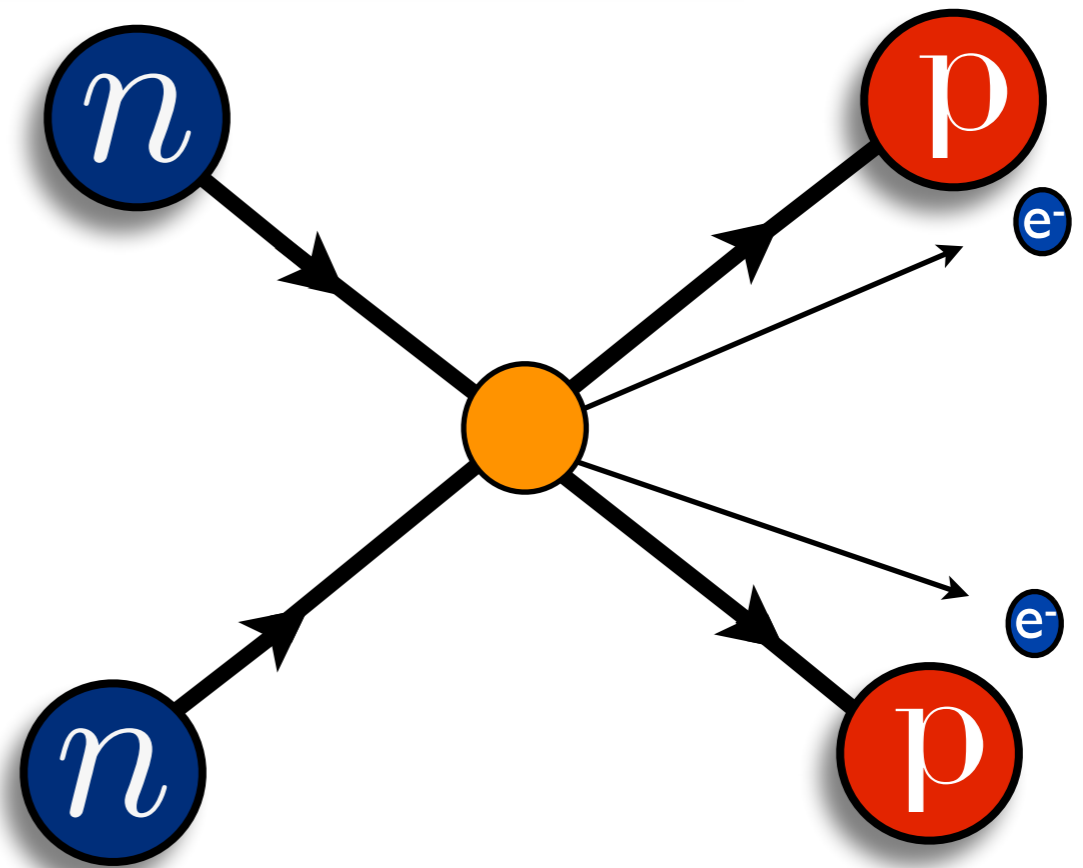
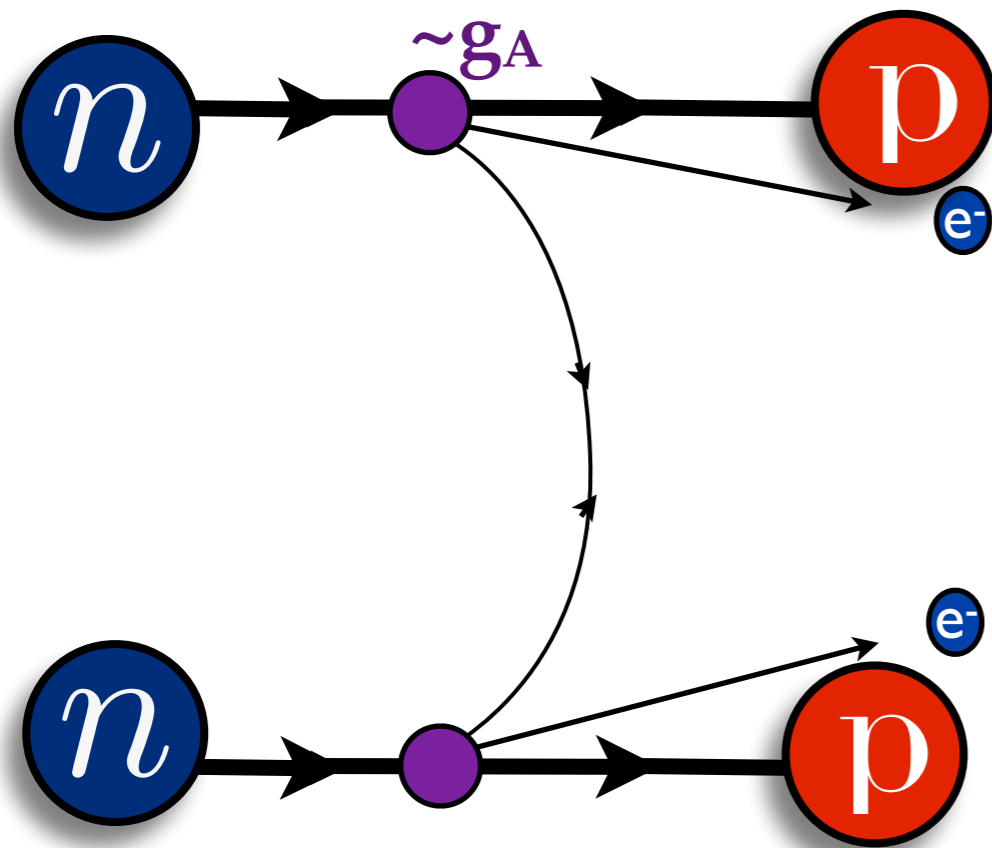
From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



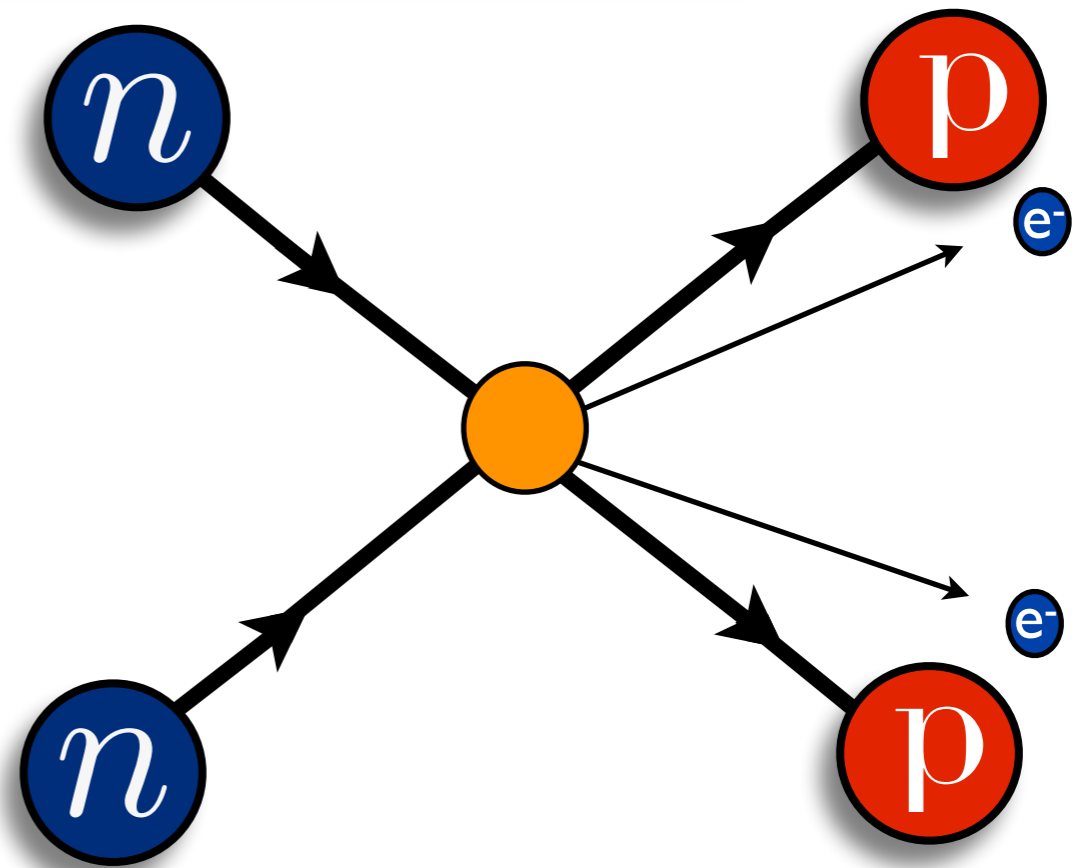
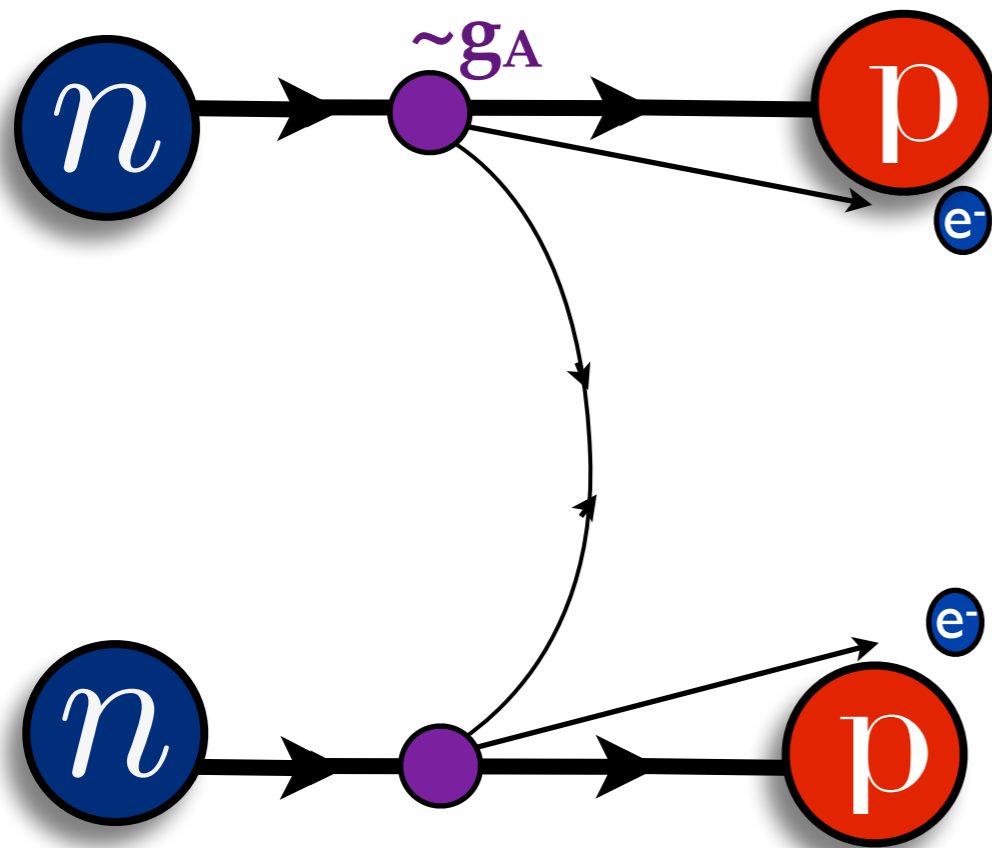
From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)

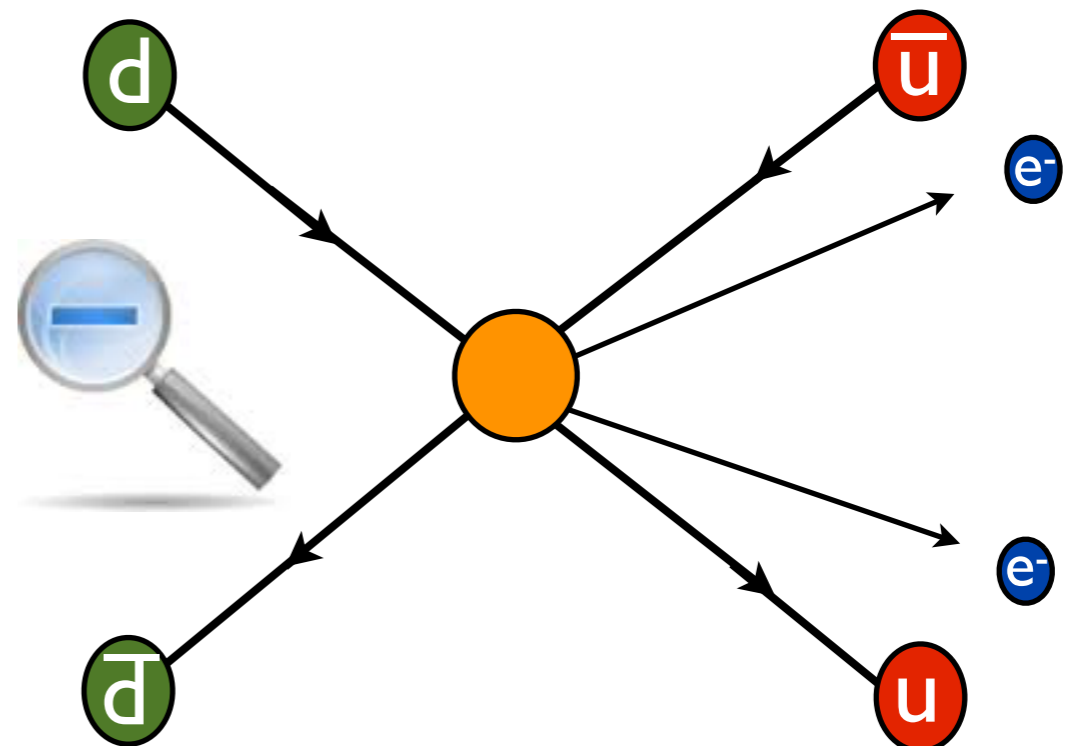


From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)

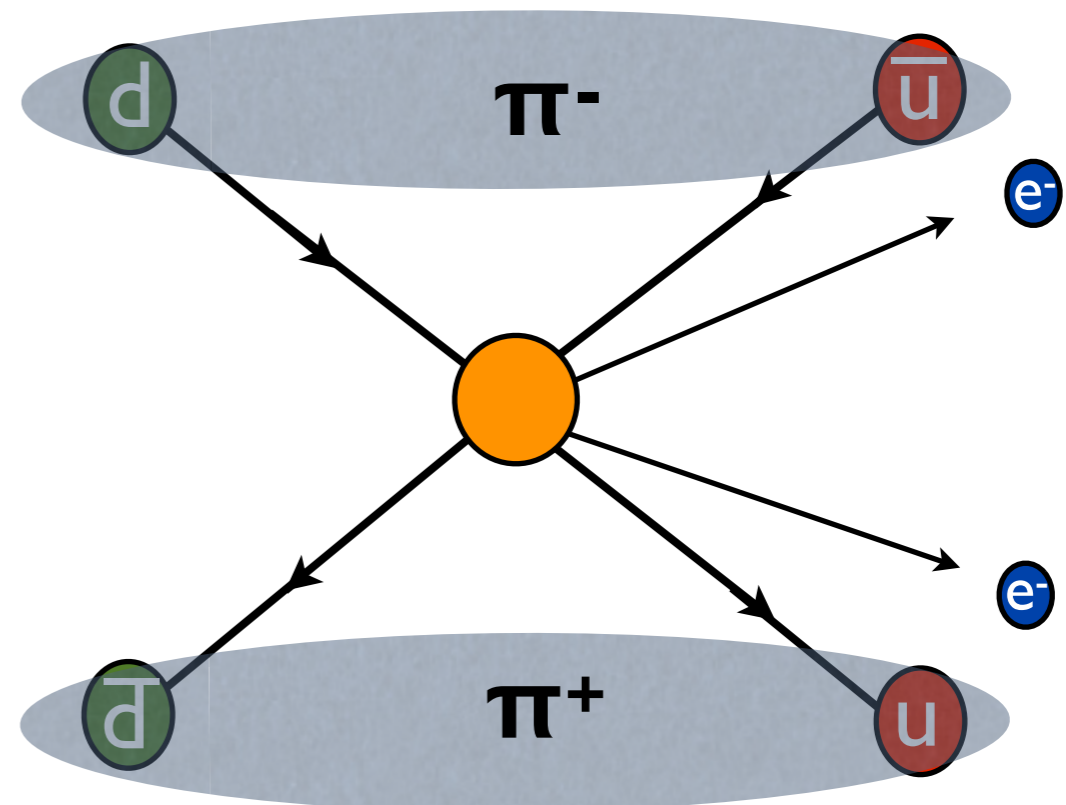
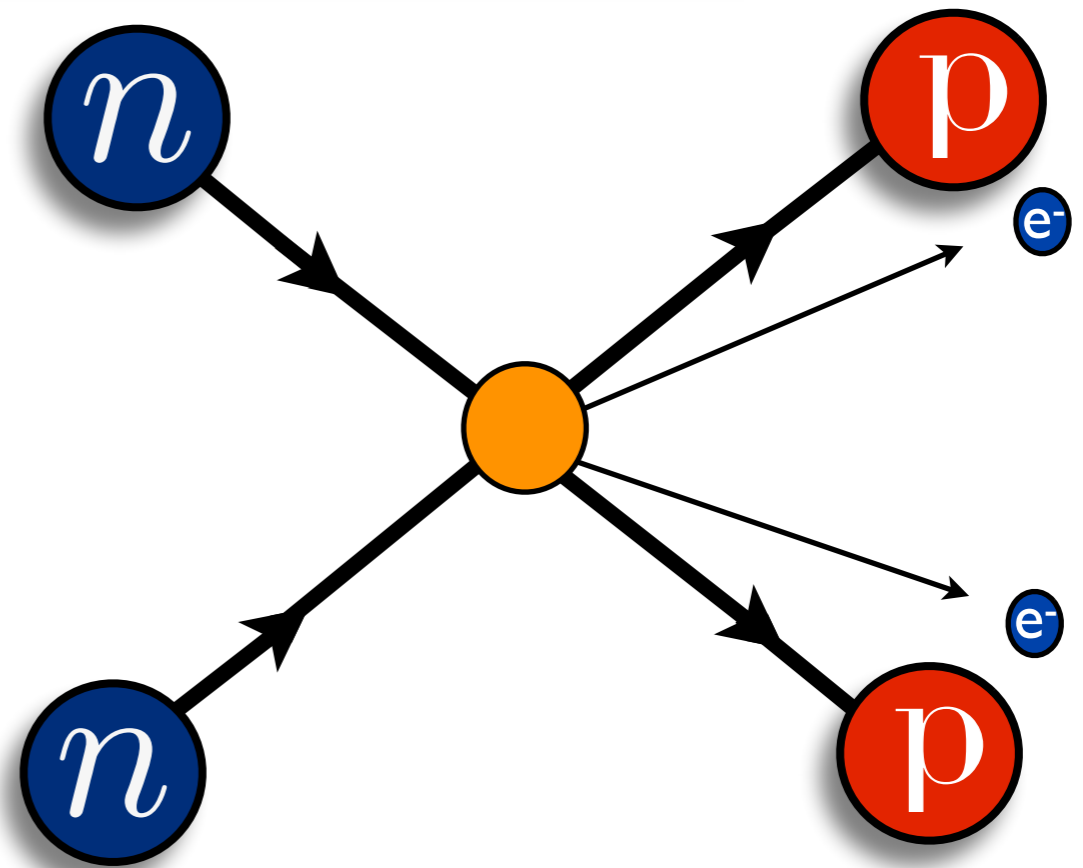
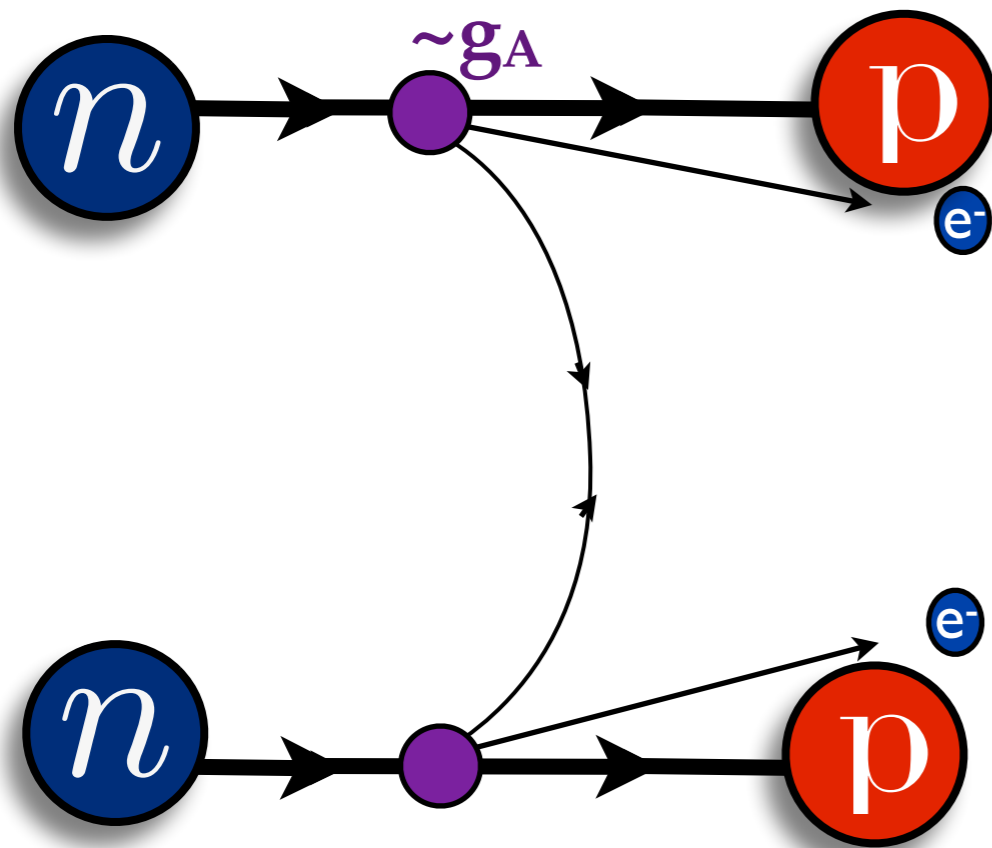


$\Lambda \ll \Lambda_{\text{QCD}}$



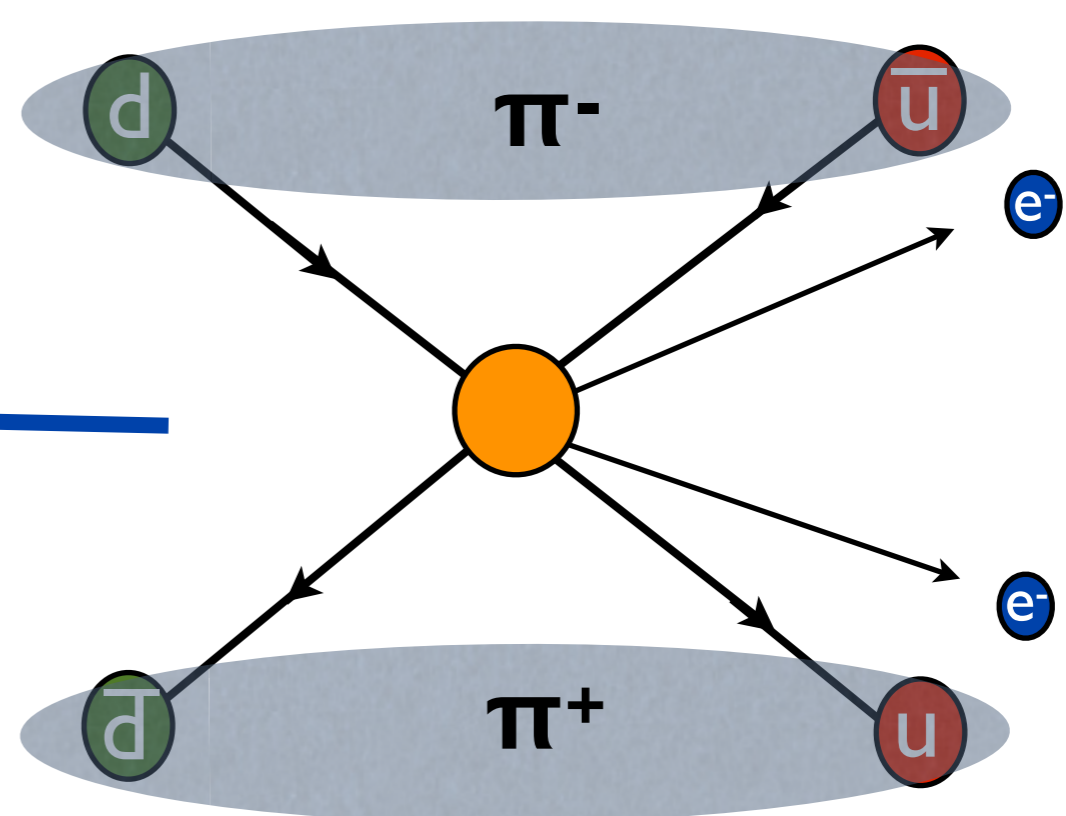
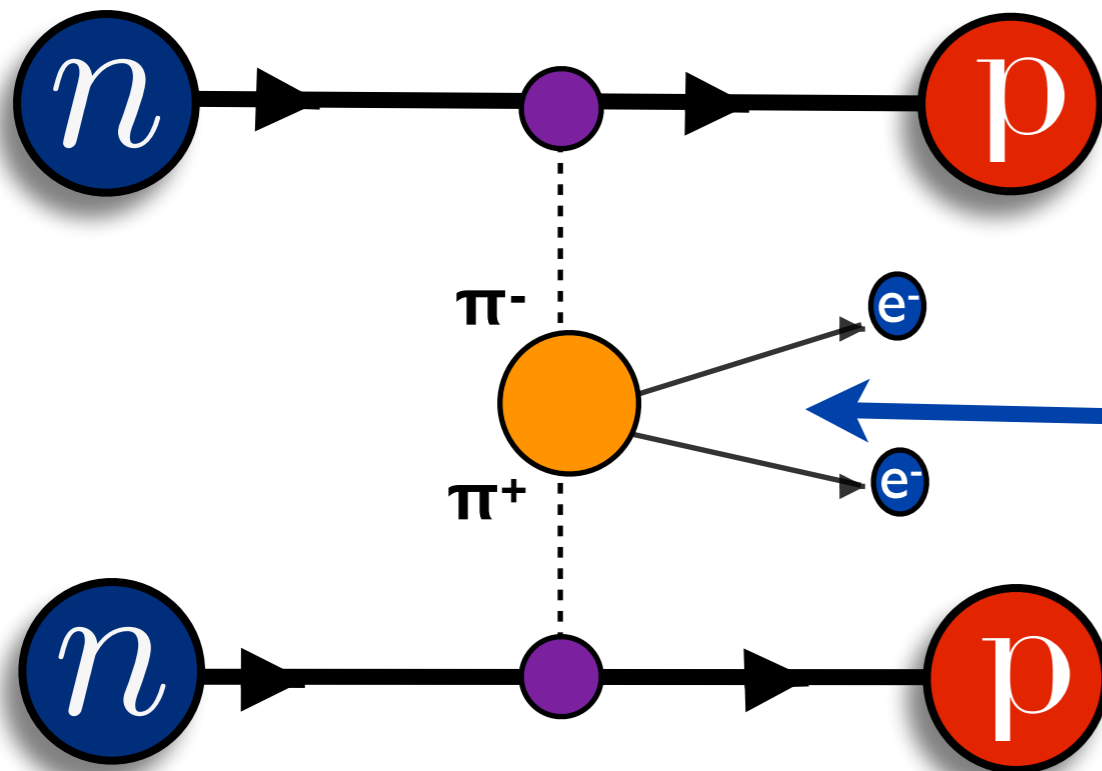
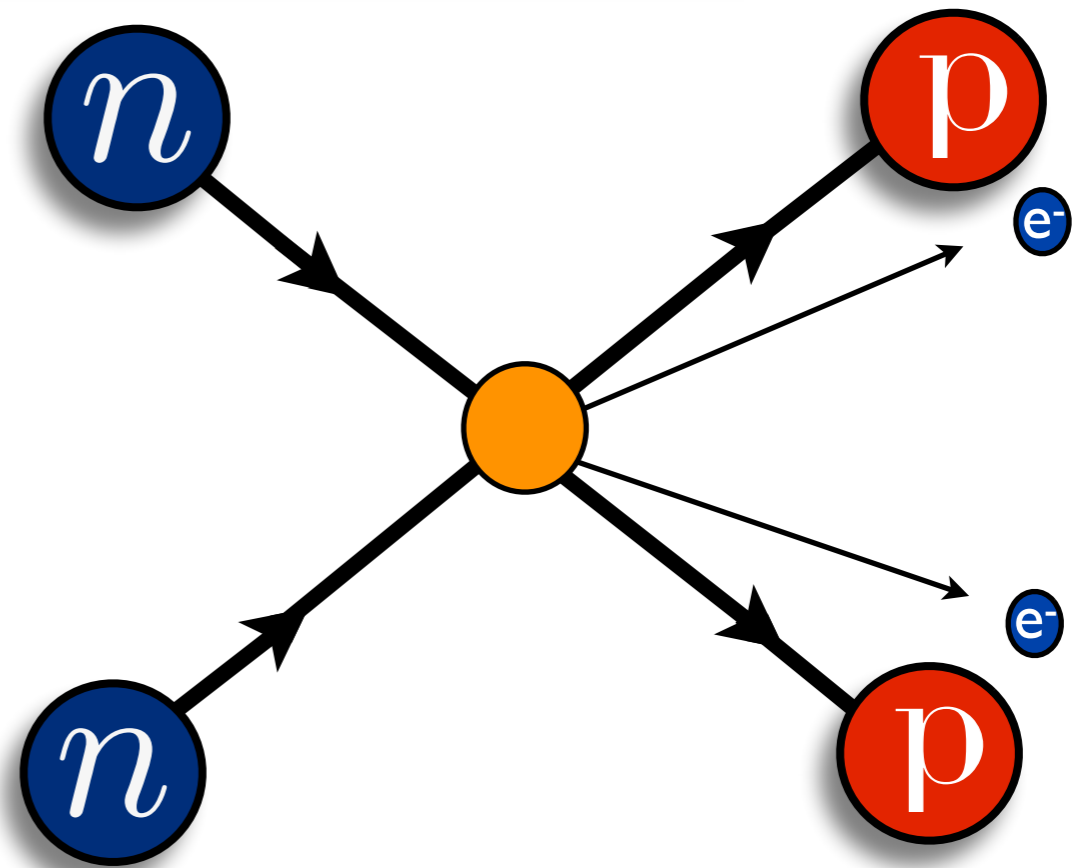
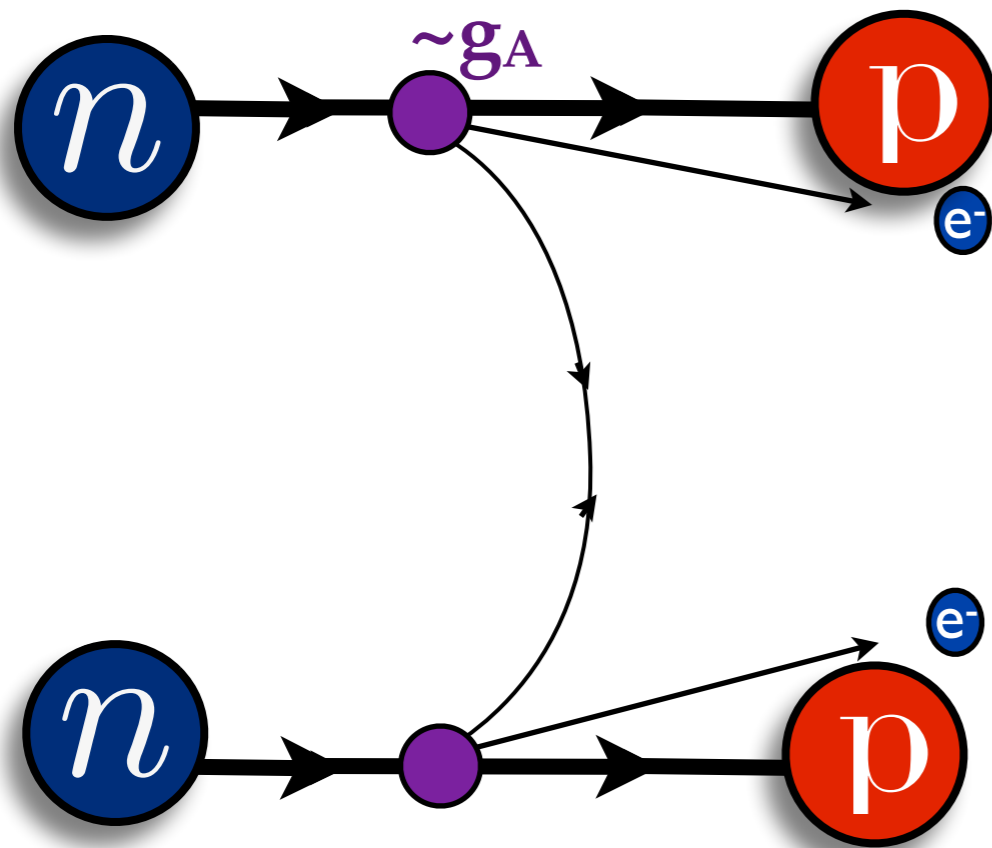
From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



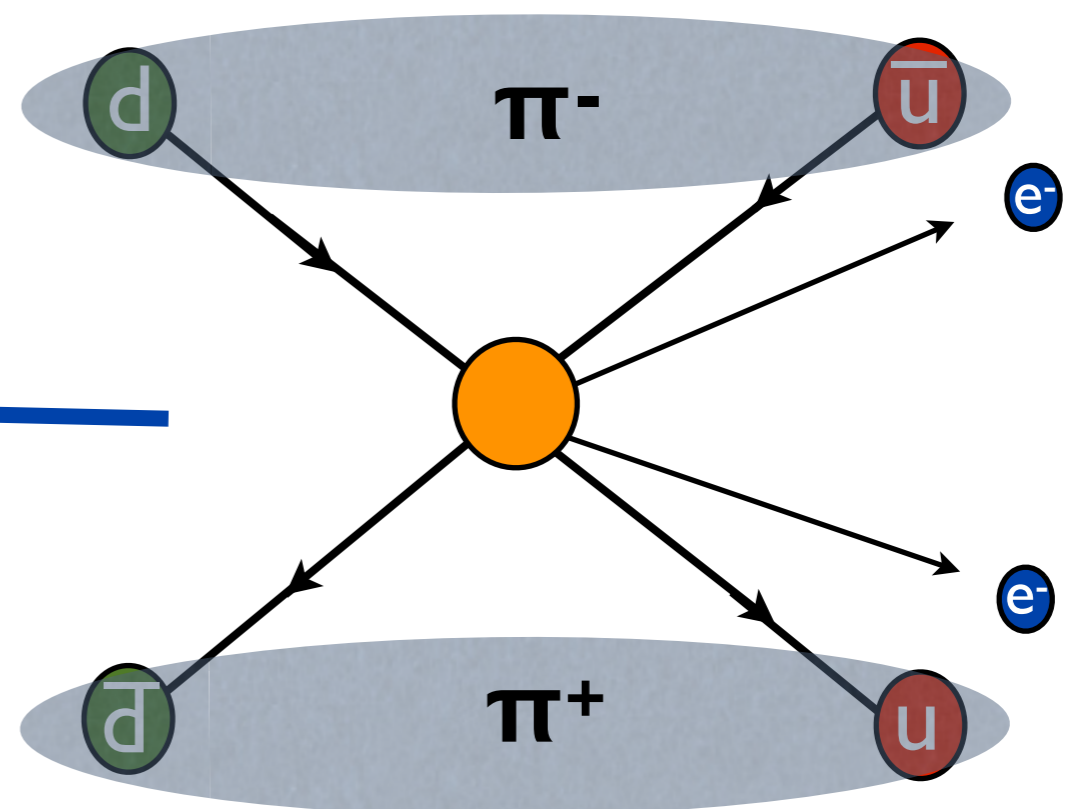
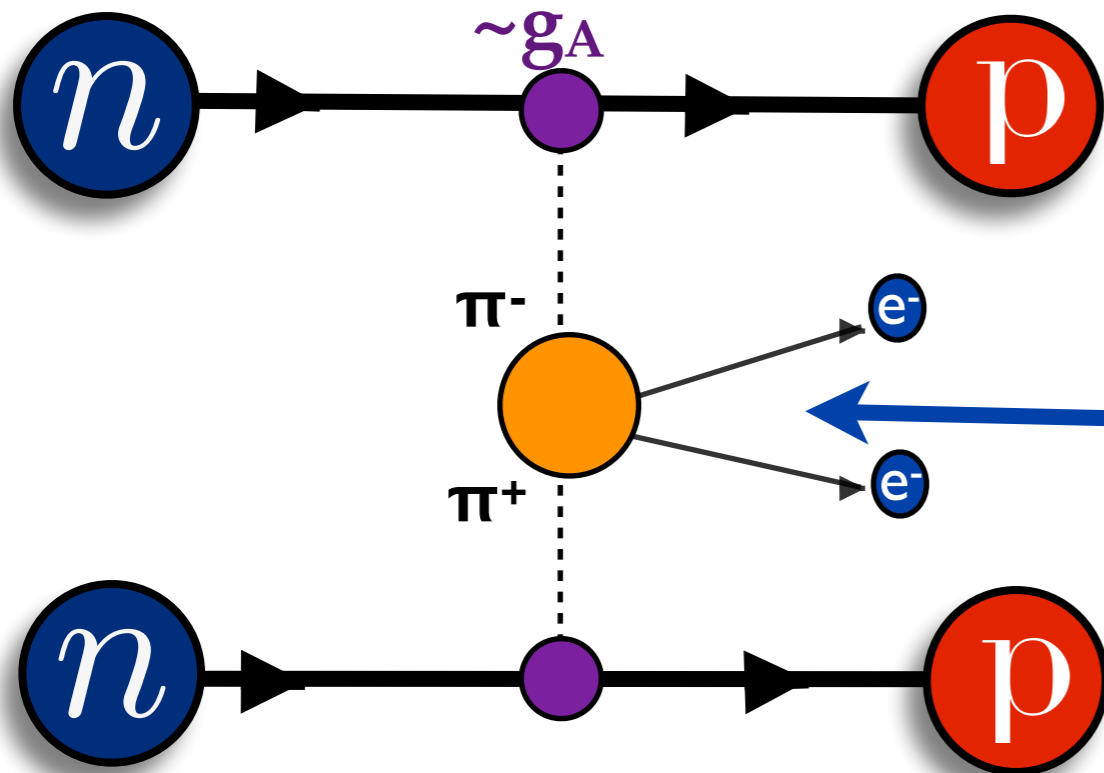
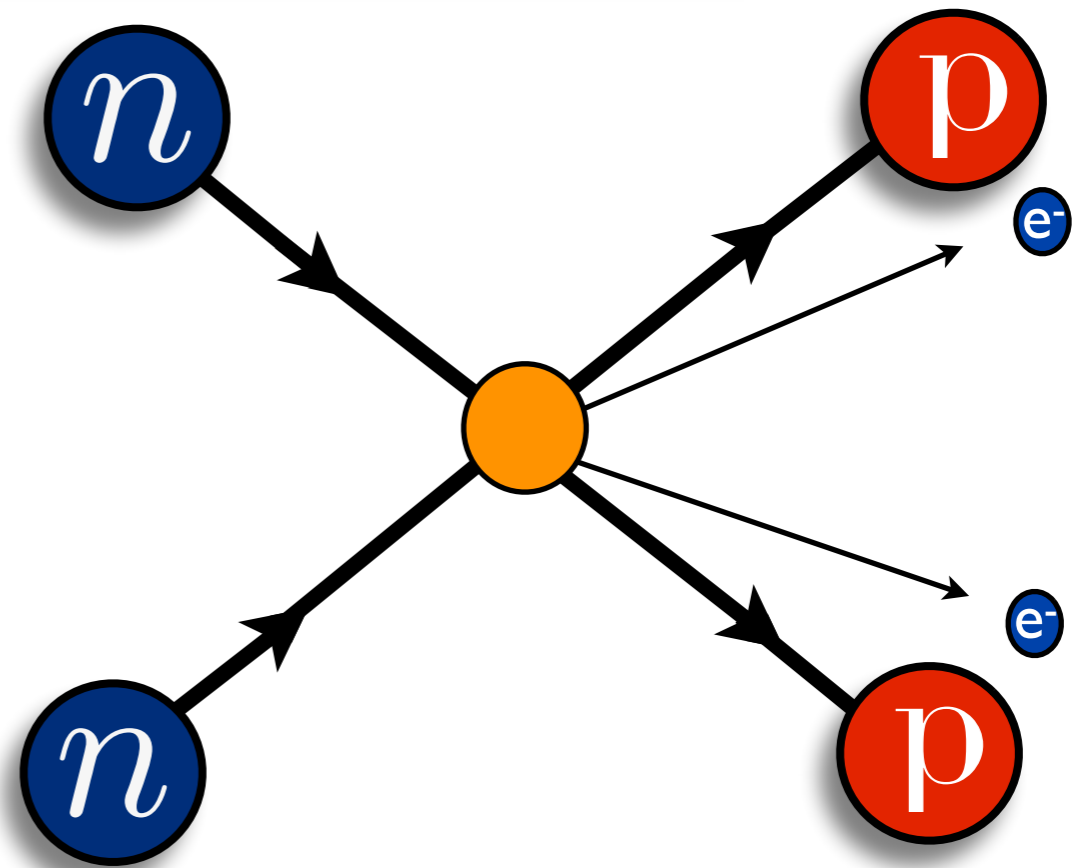
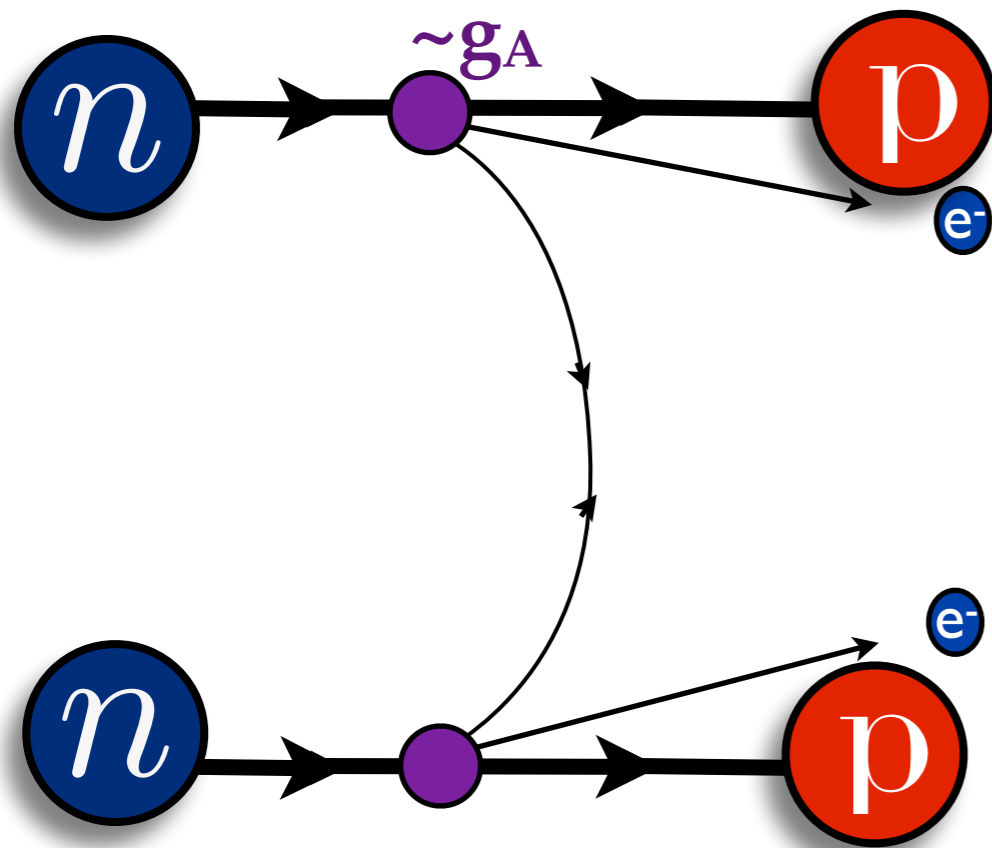
From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



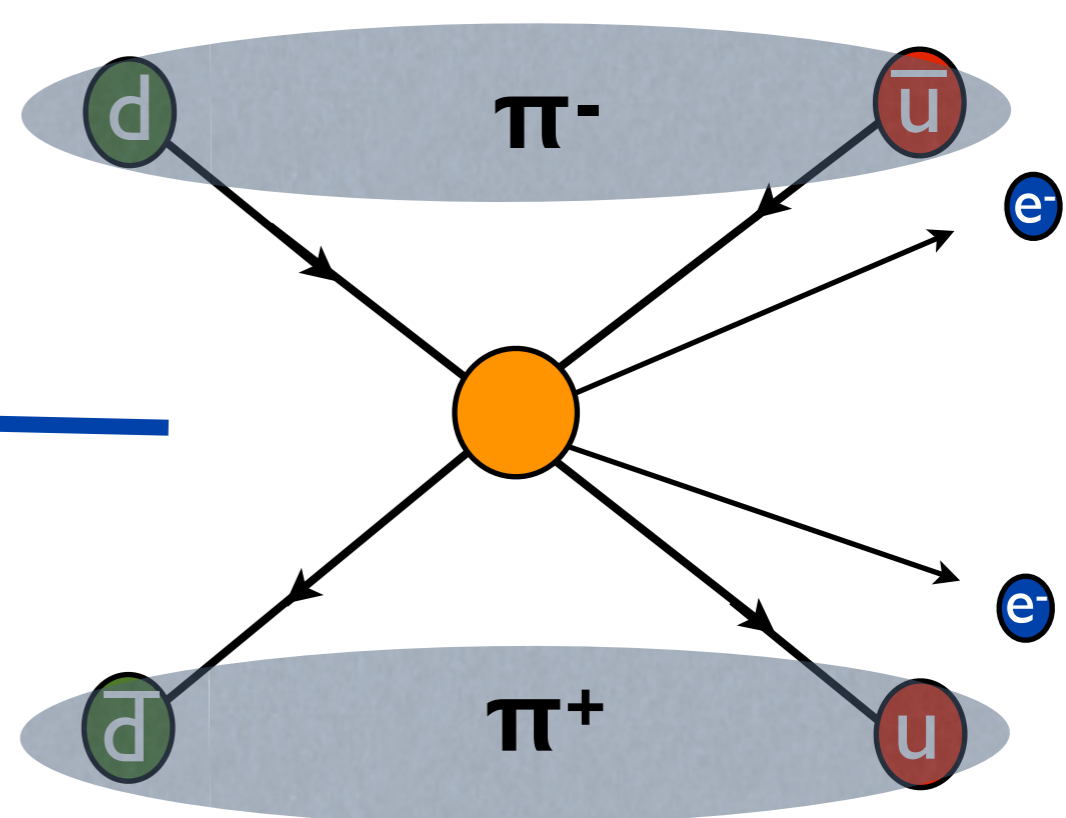
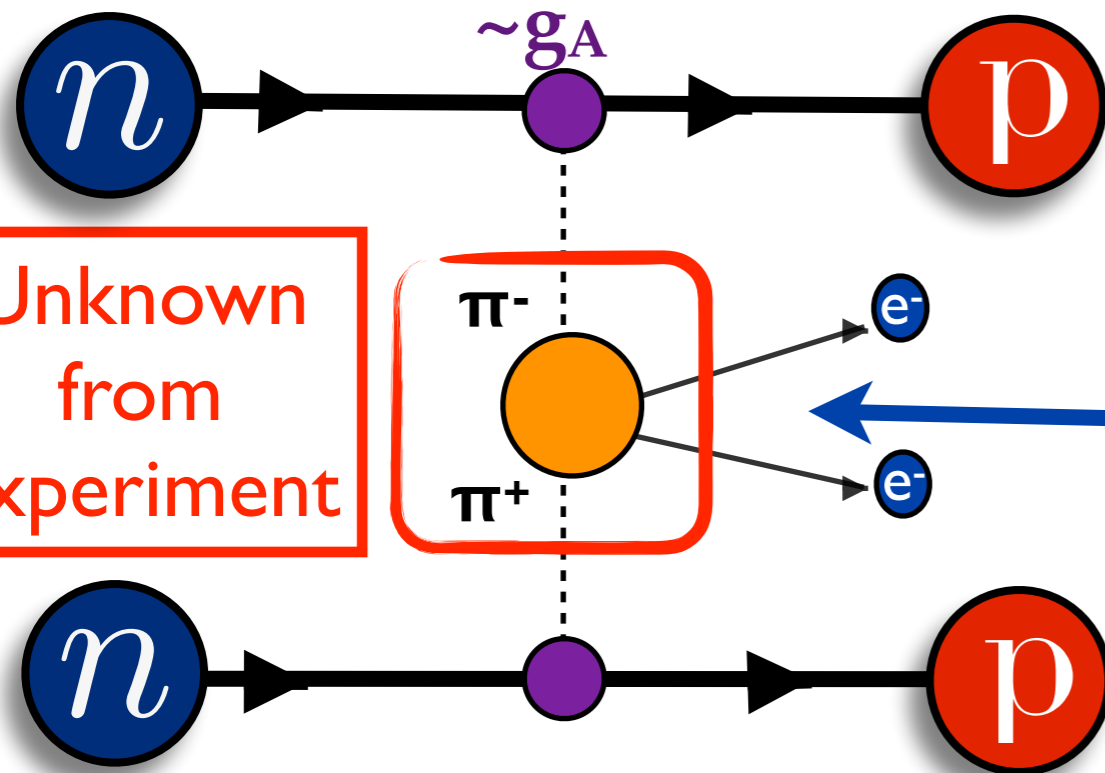
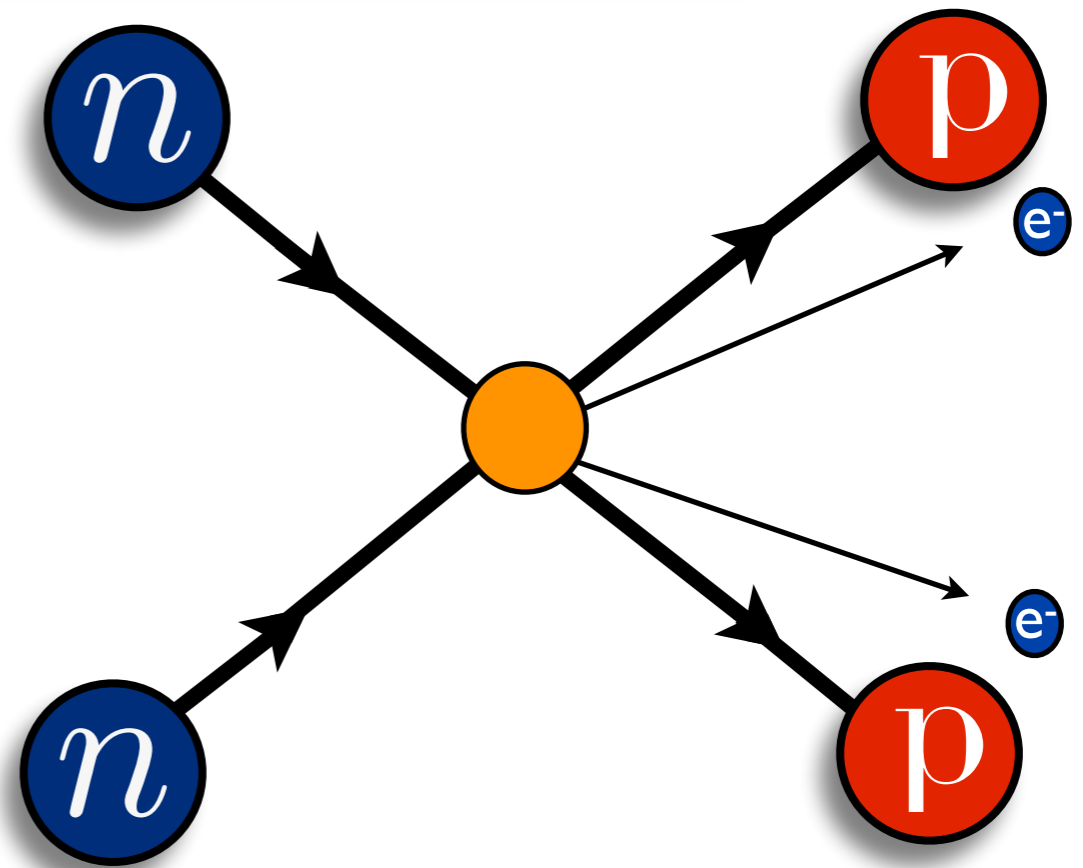
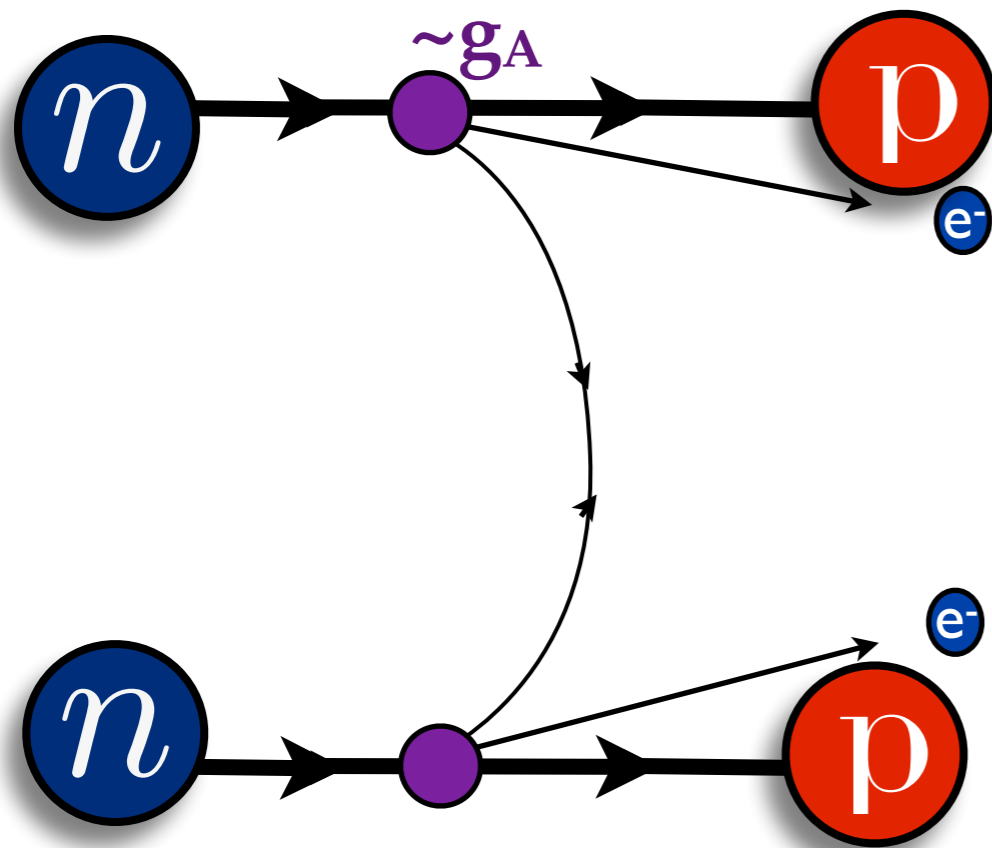
From quark to hadronic scales

Prezeau, Ramsey-Musolf, Vogel (2003)



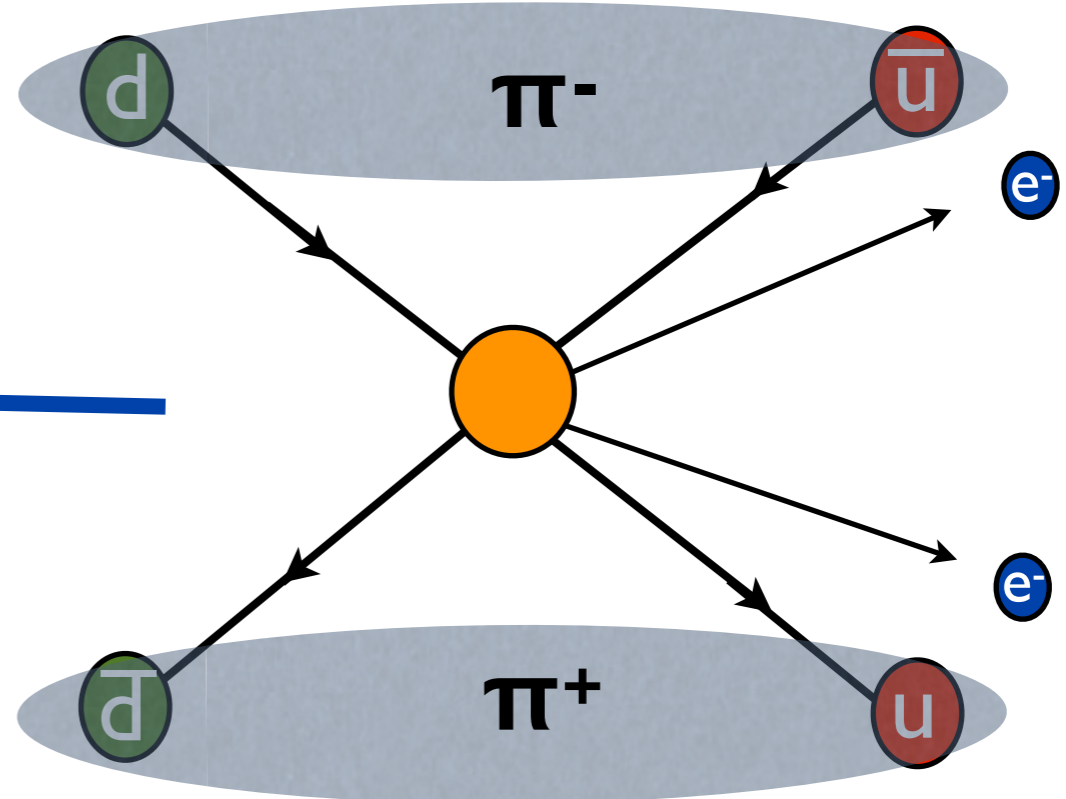
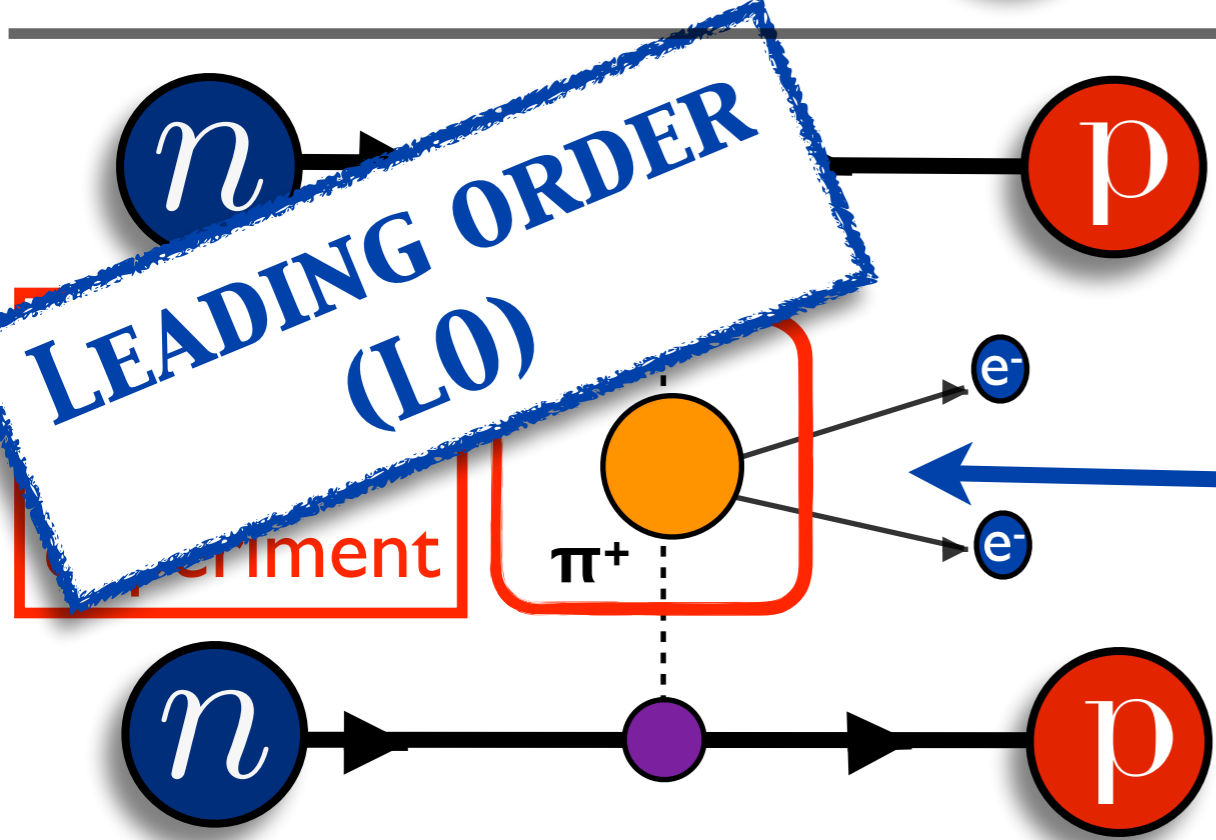
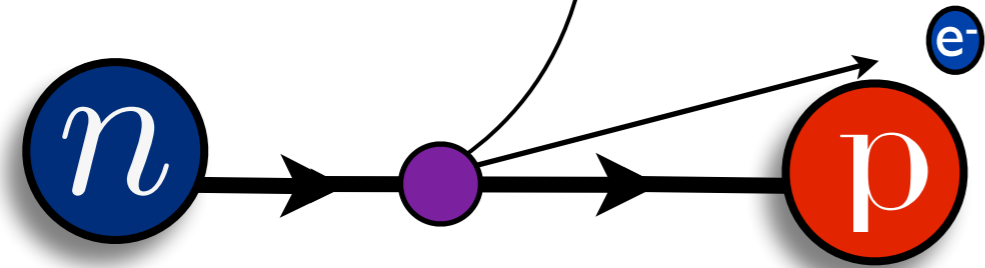
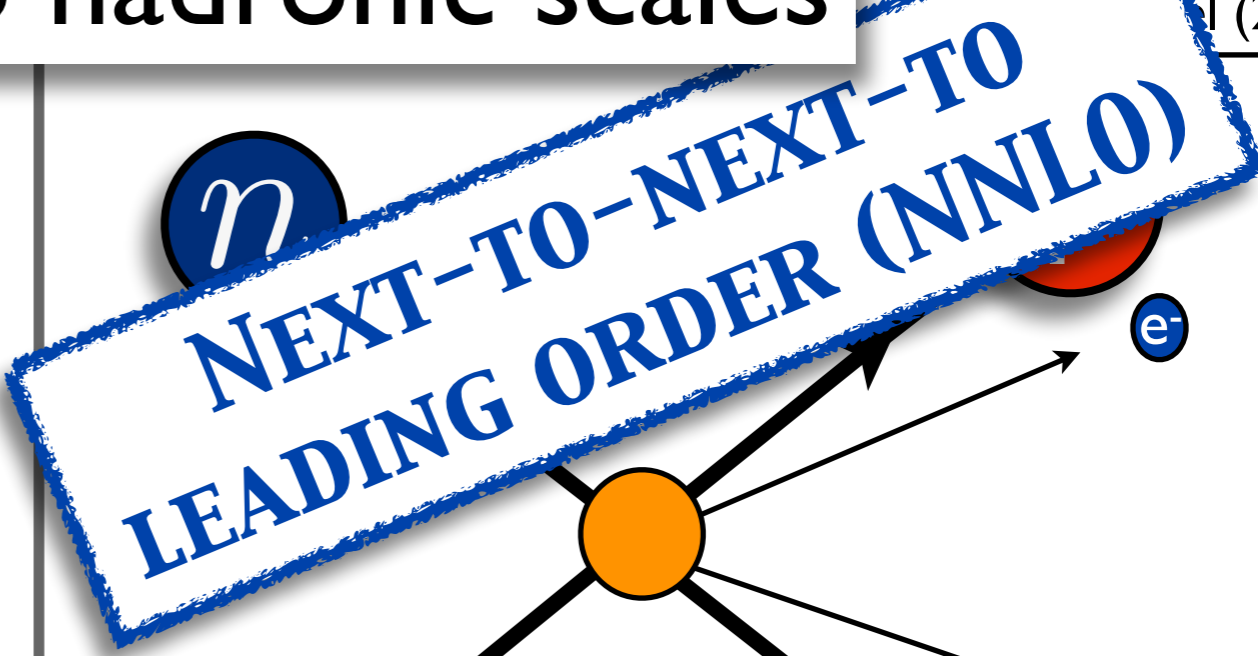
From quark to hadronic scales

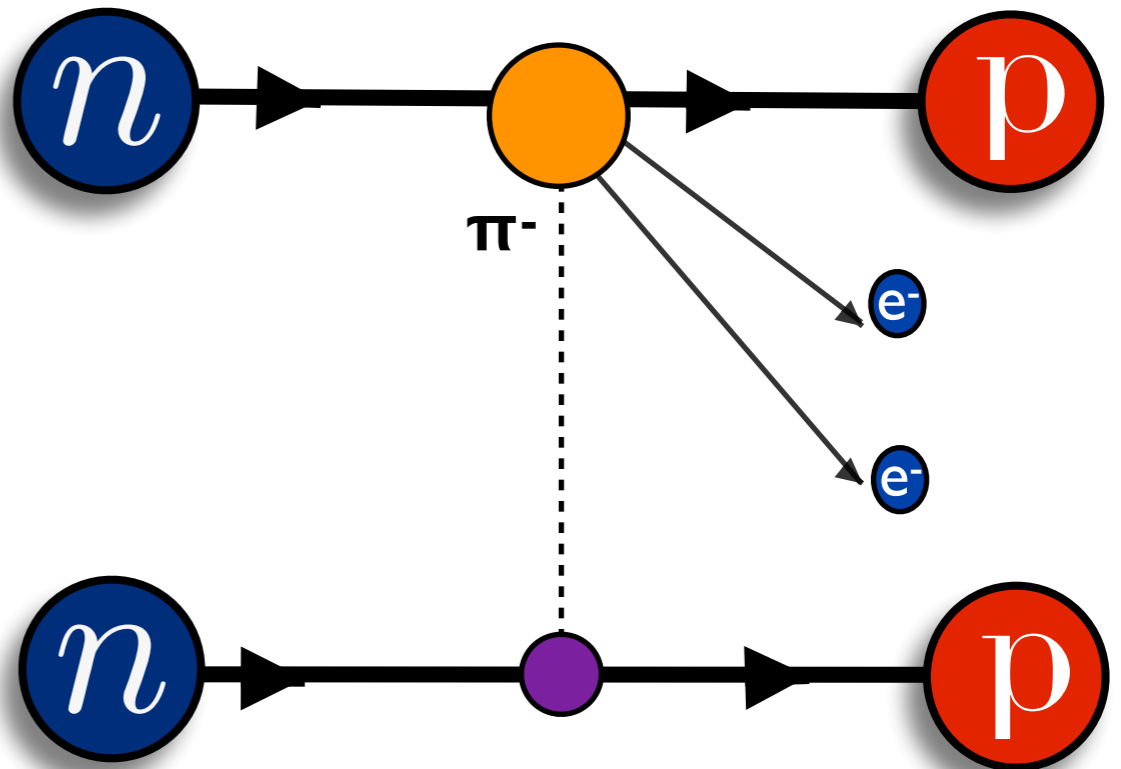
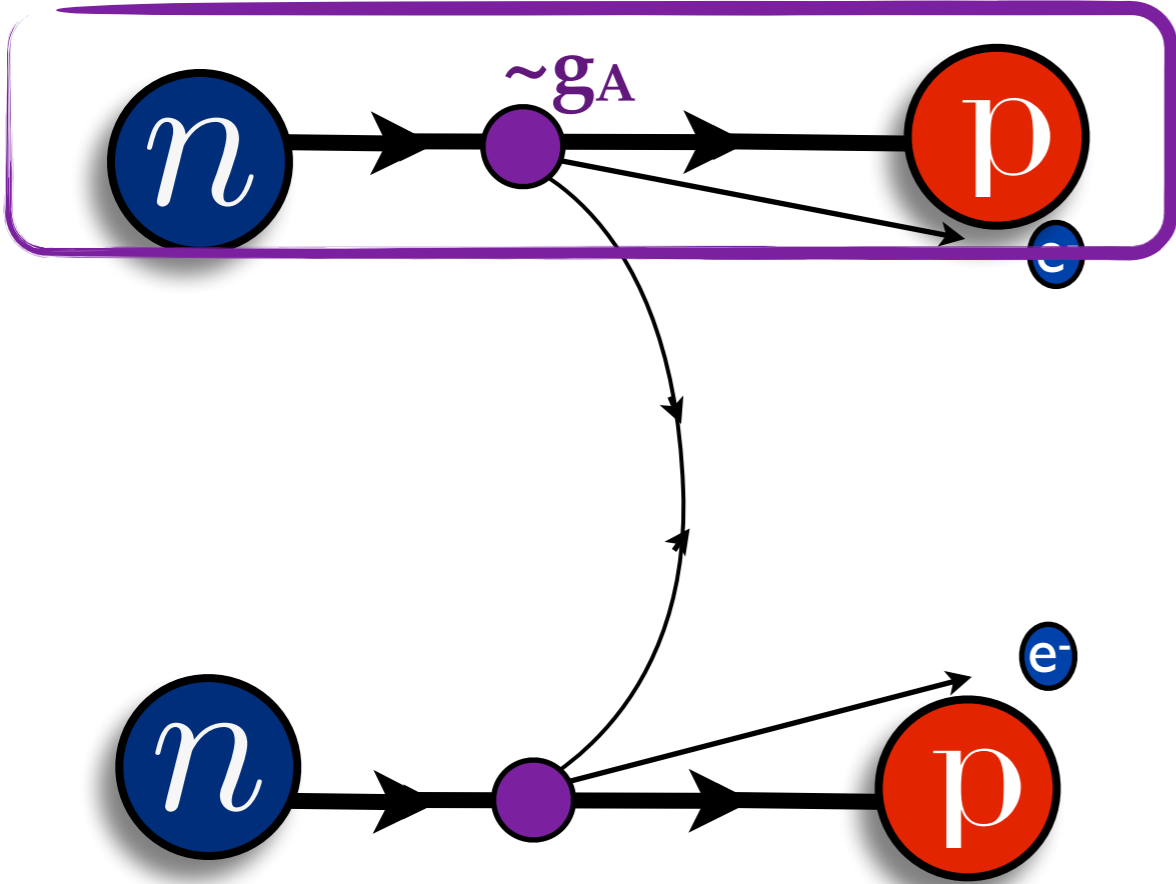
Prezeau, Ramsey-Musolf, Vogel (2003)

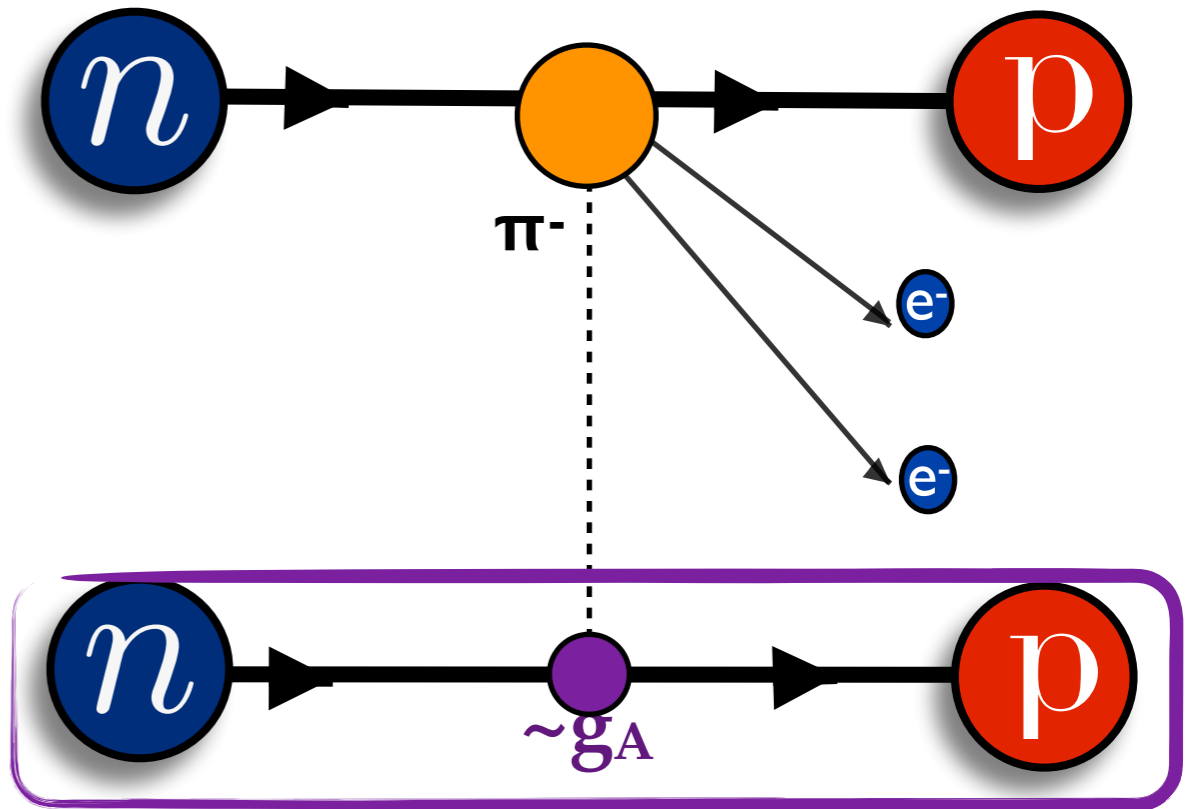
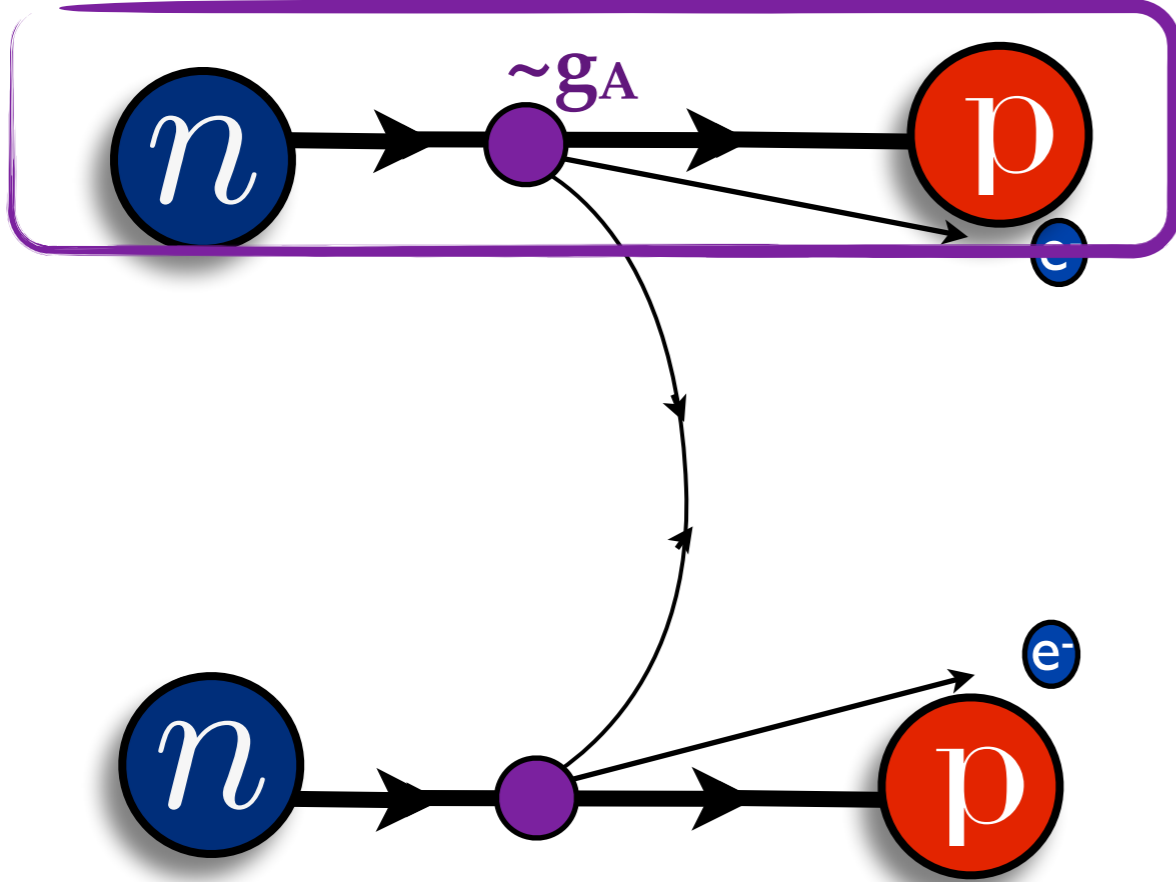


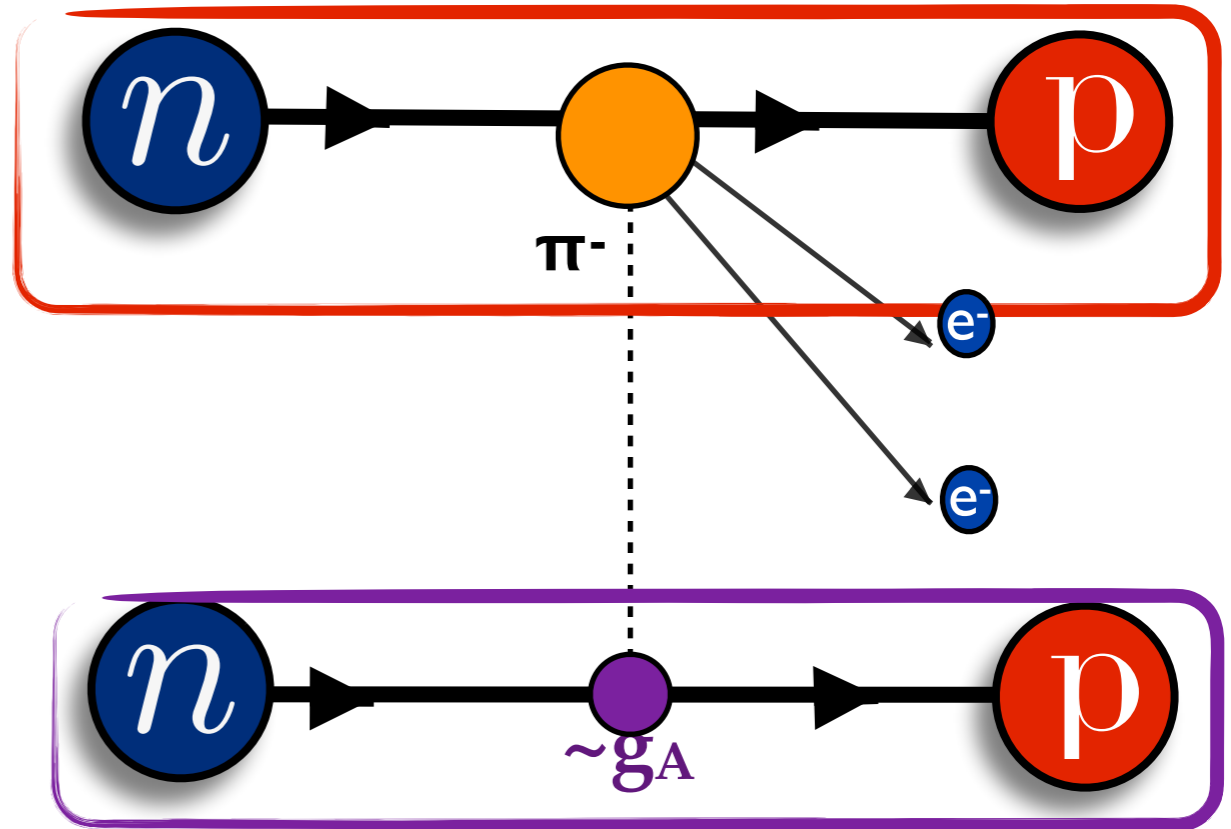
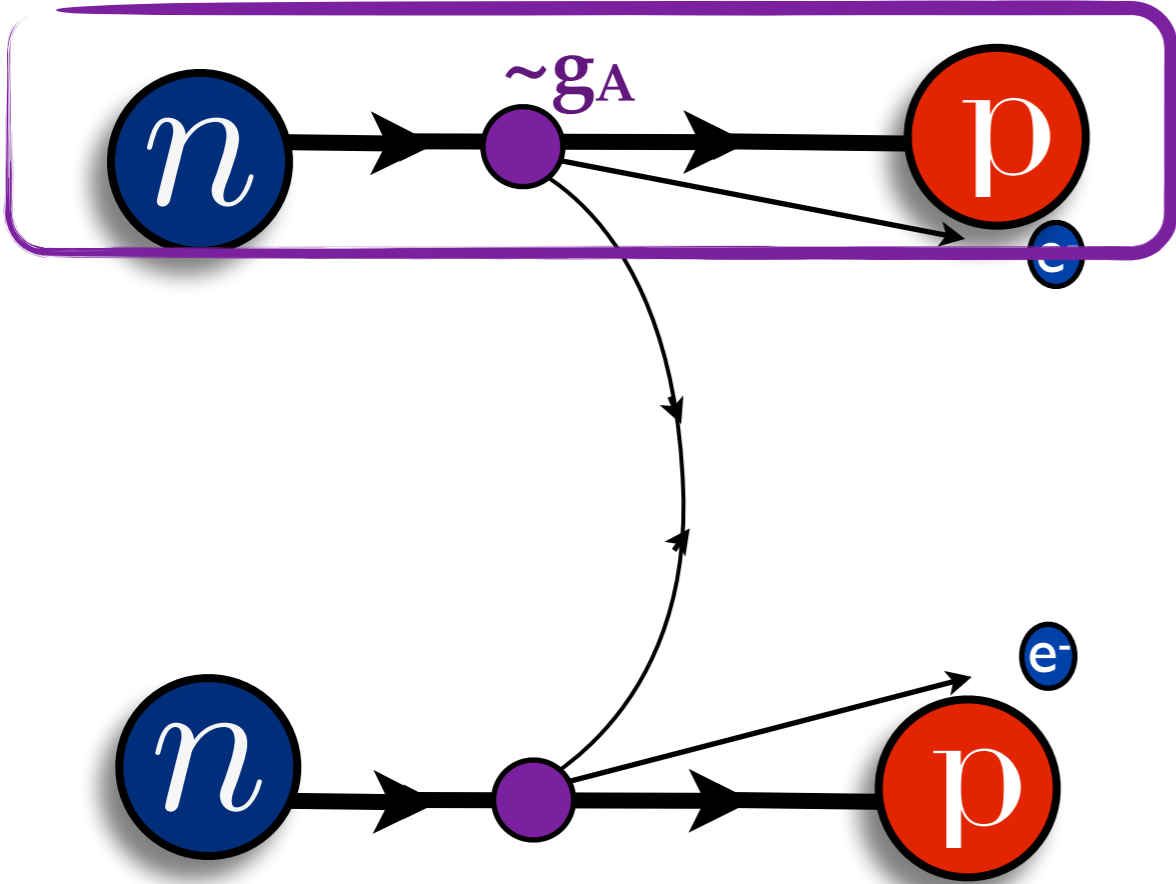
From quark to hadronic scales

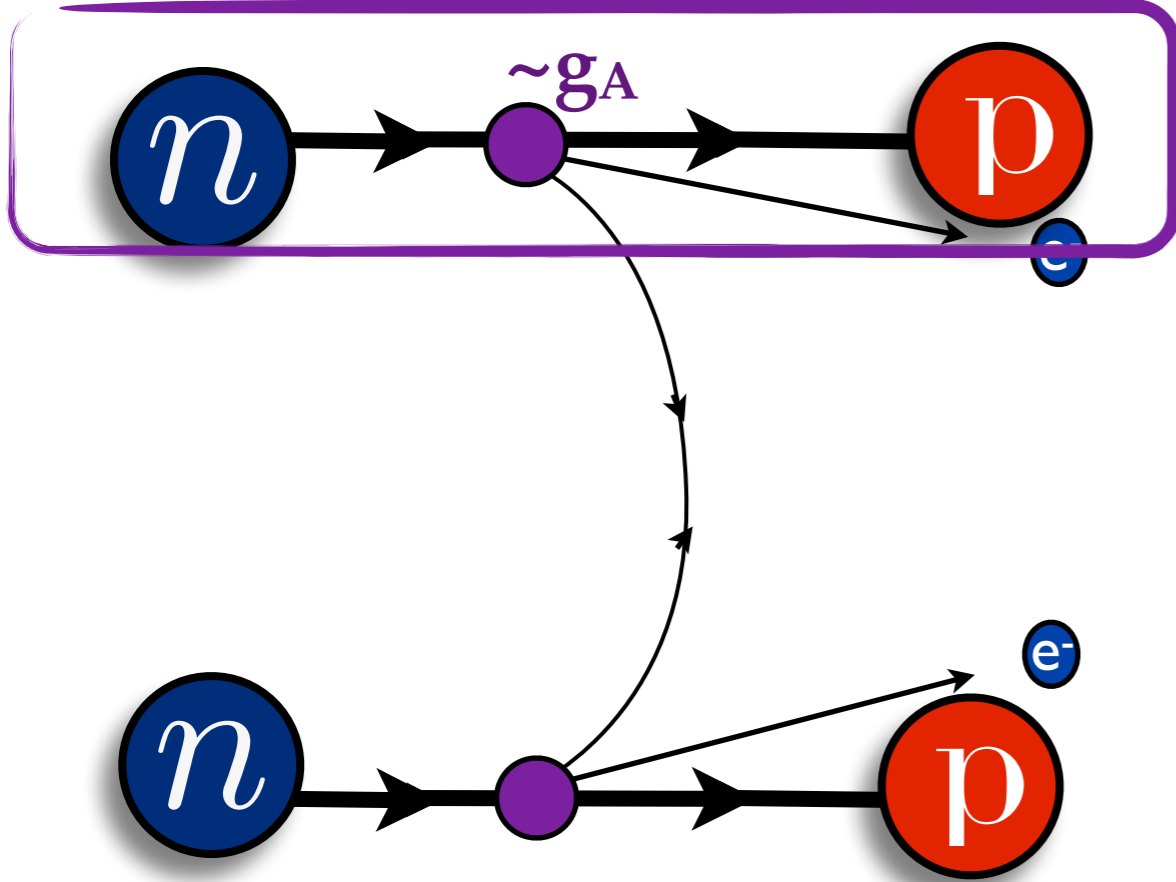
Pratt, Ramsey-
Musclow (2003)

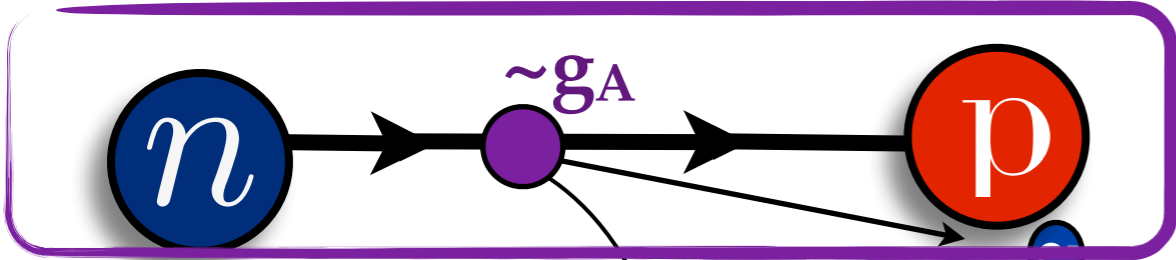




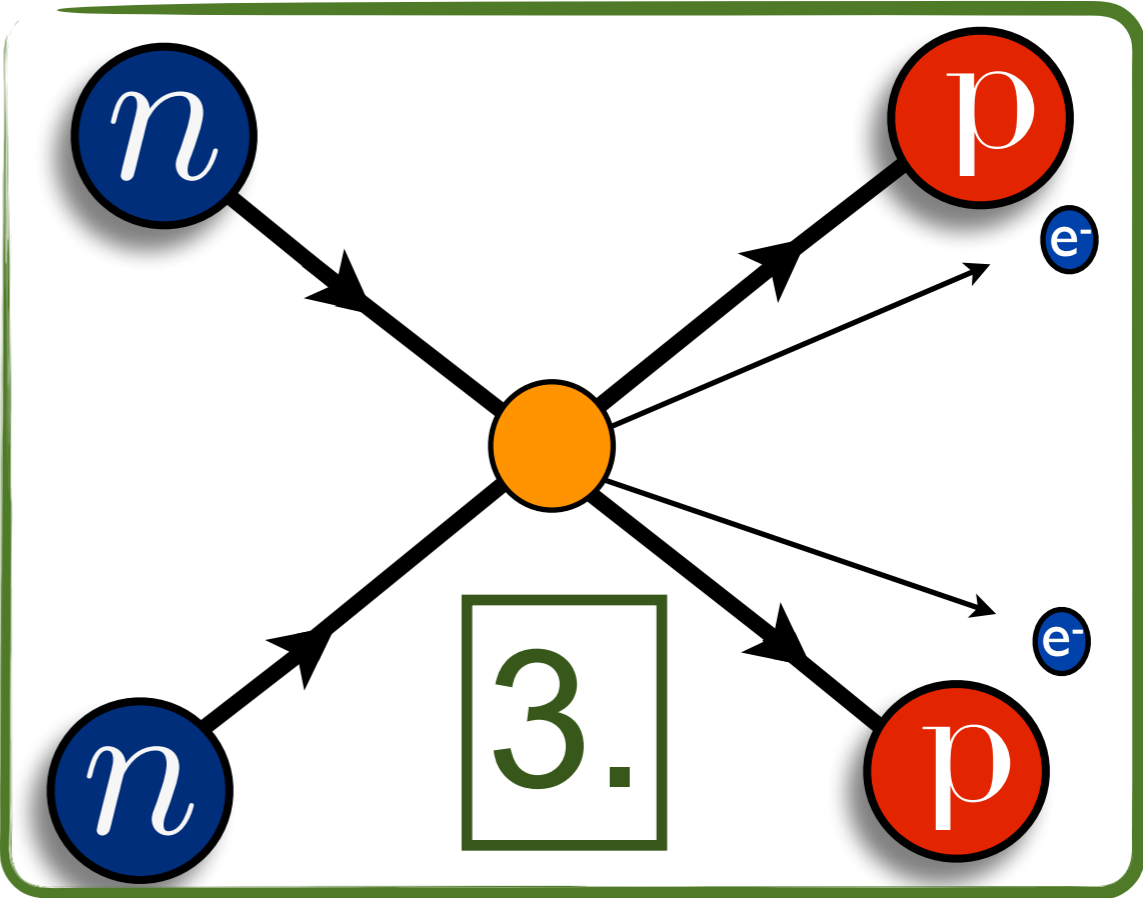
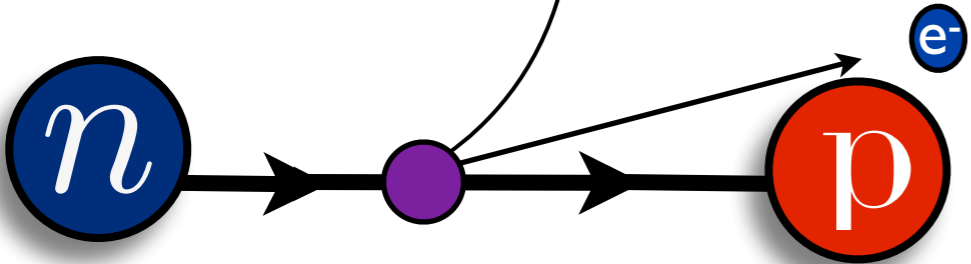




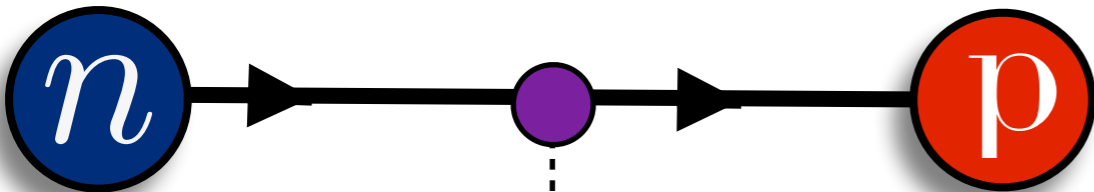




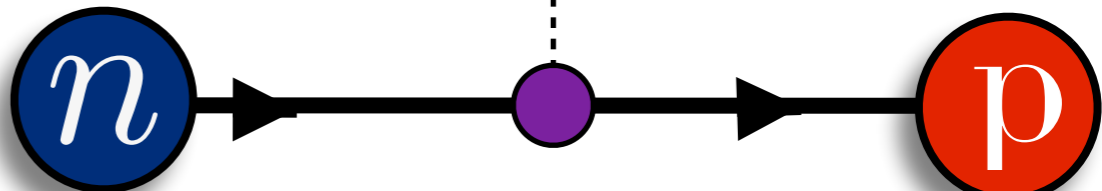
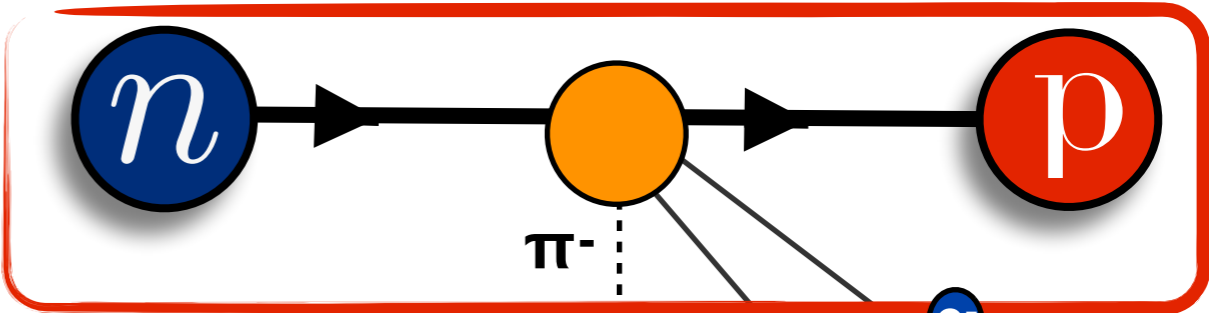
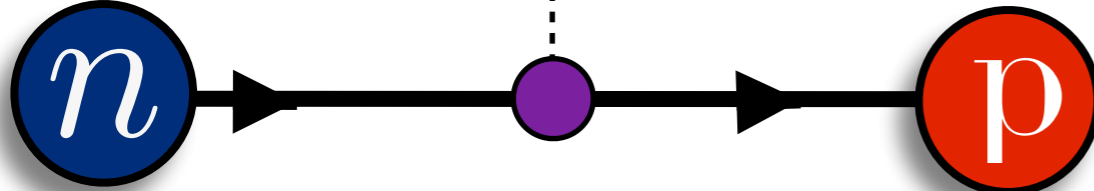
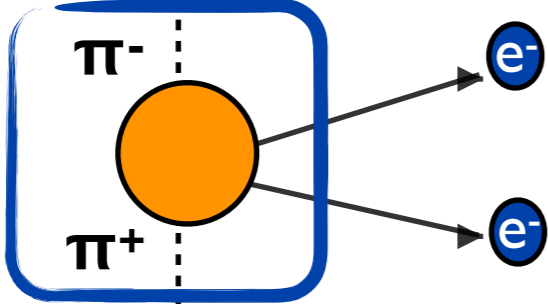
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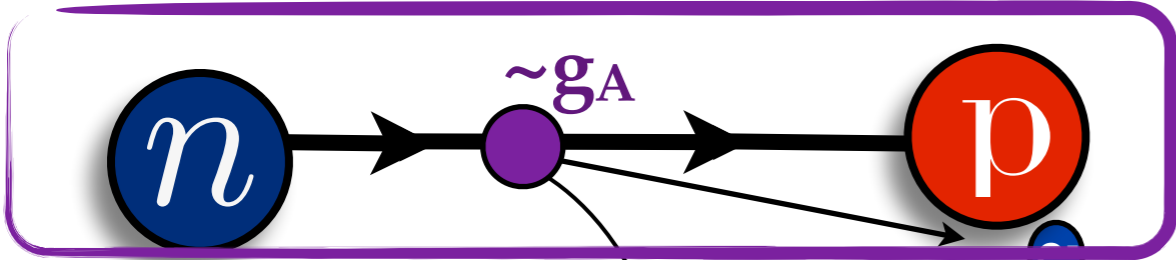


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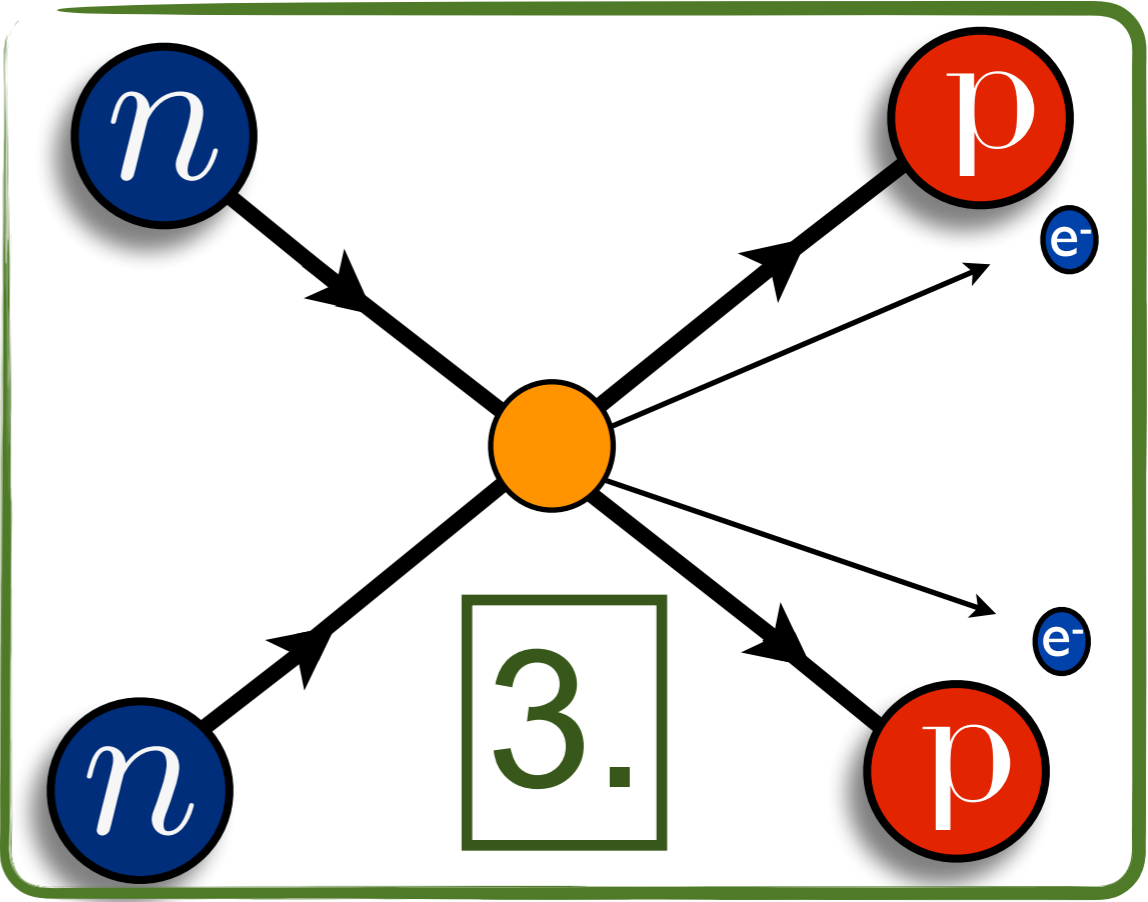
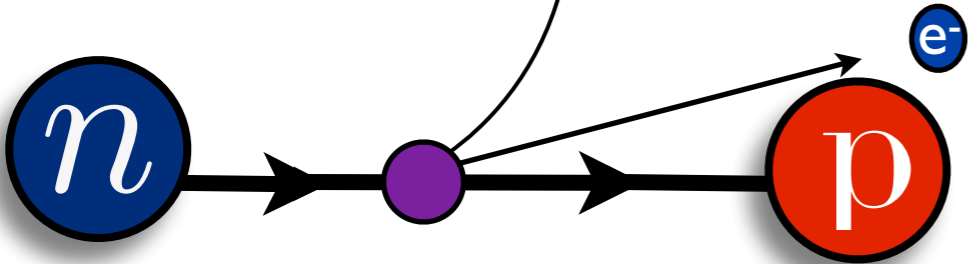


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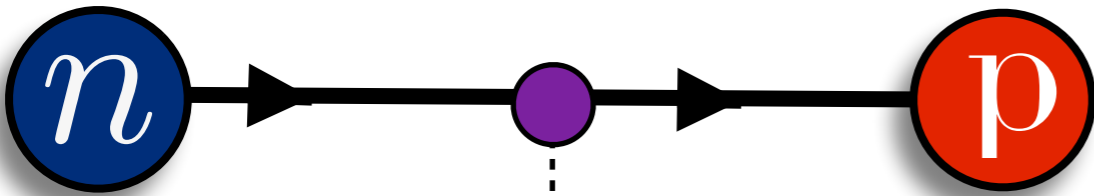




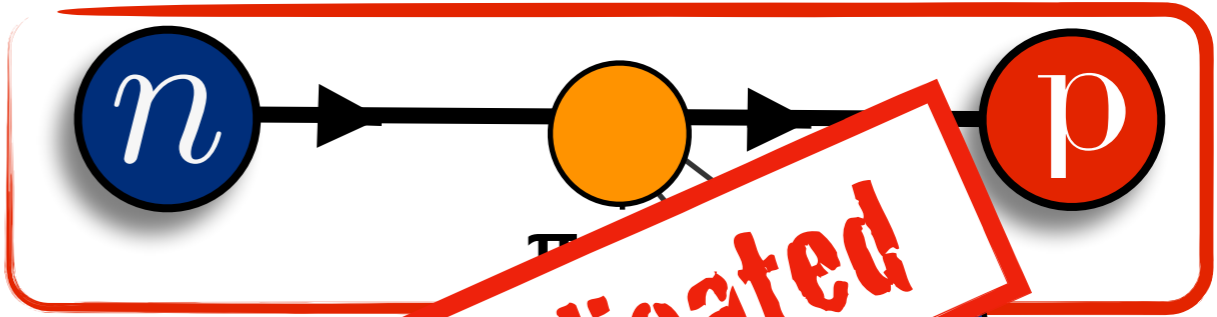
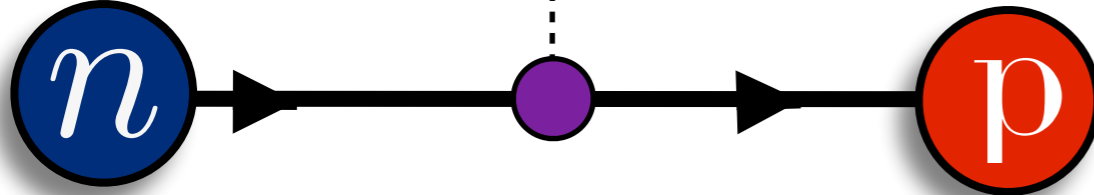
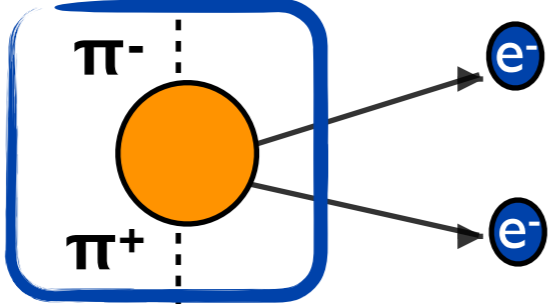
1.



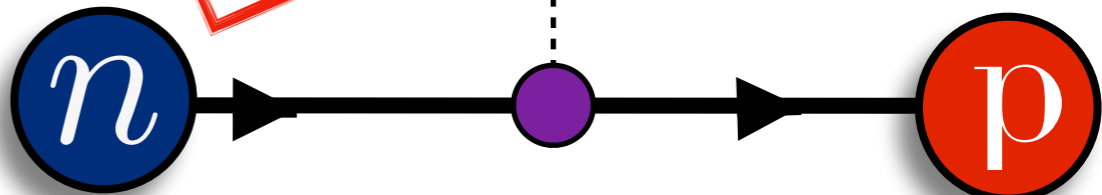
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2.



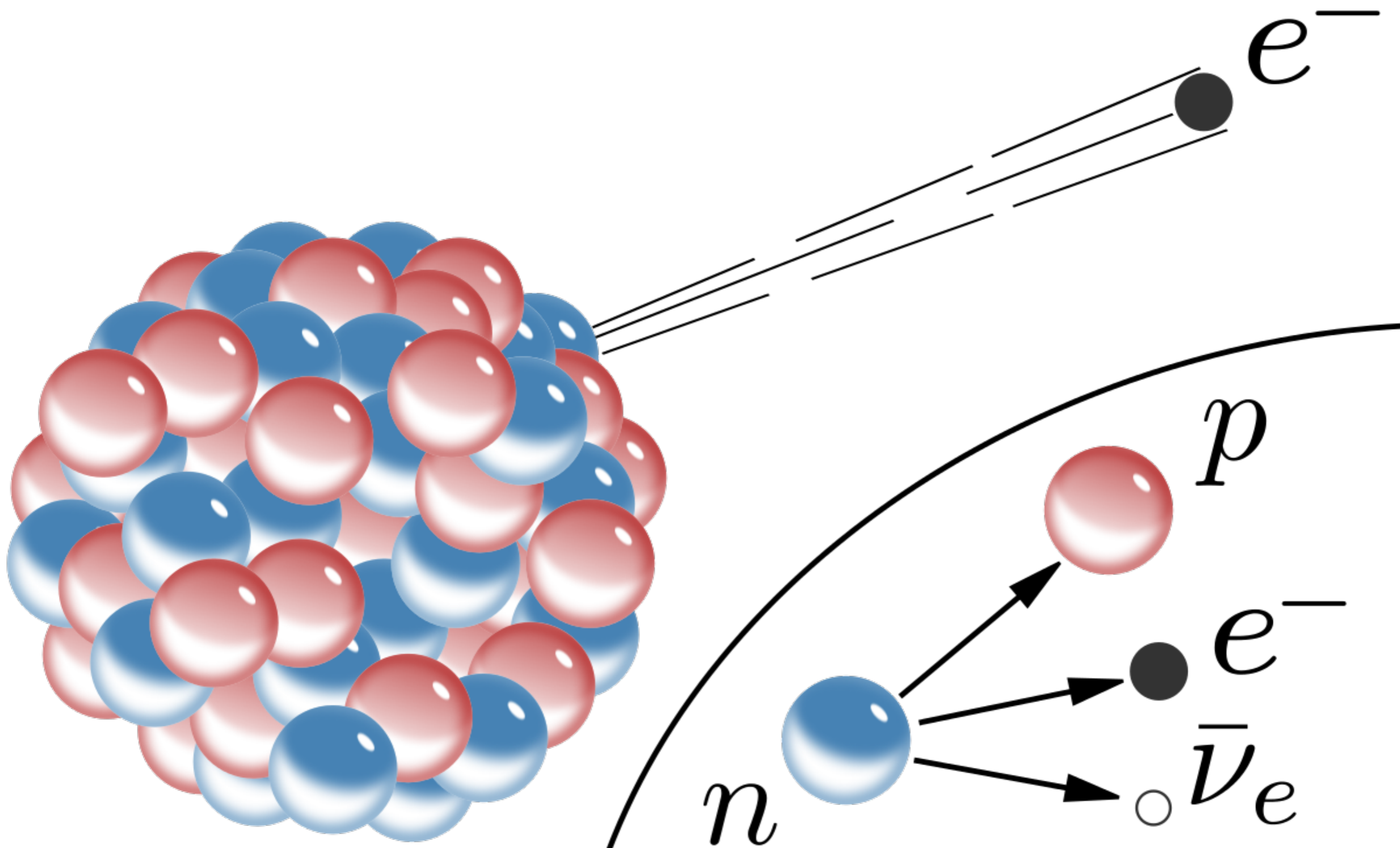
Complicated



1.

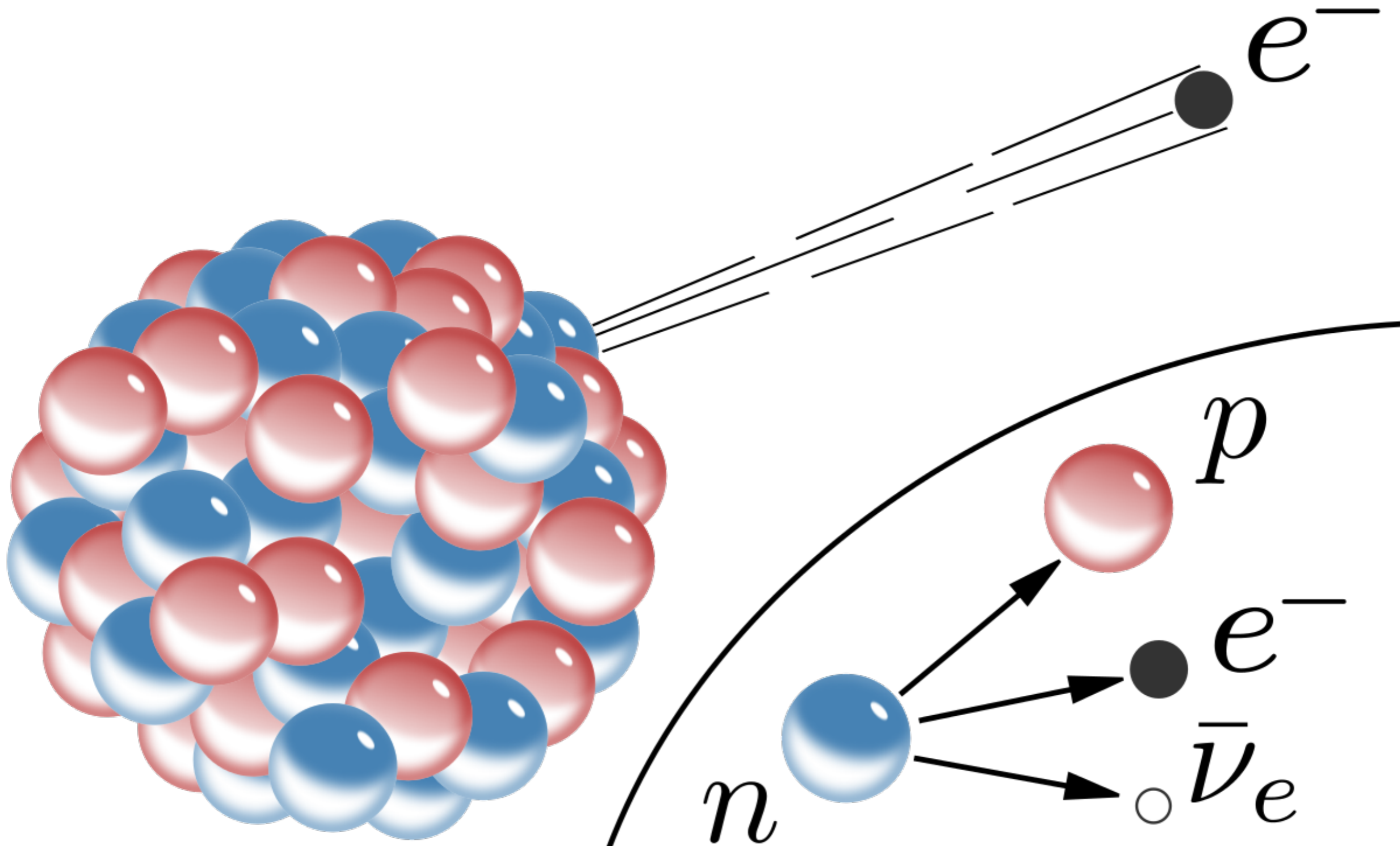
Nucleon axial charge, g_A

What depends on g_A ?



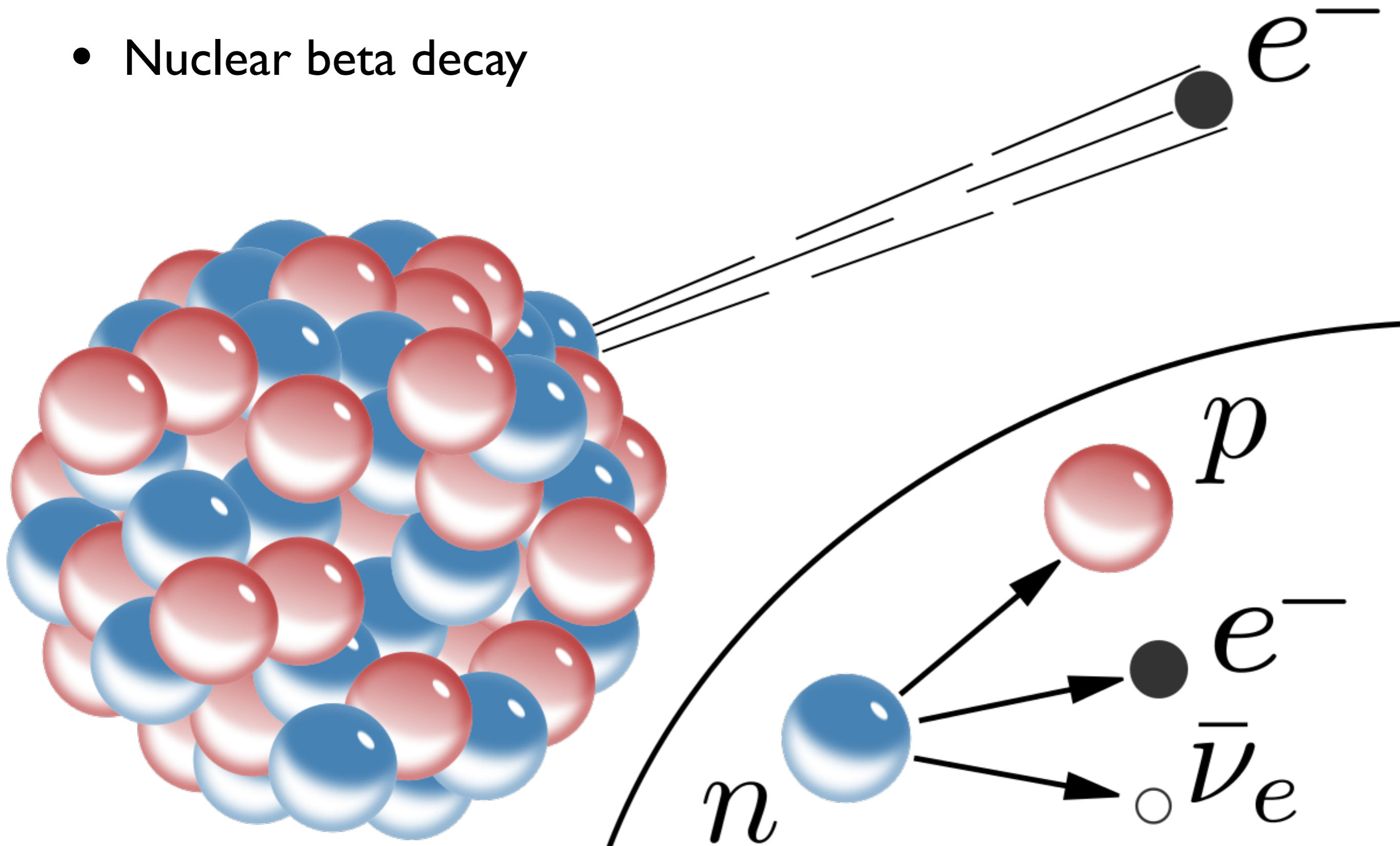
What depends on g_A ?

- Free neutron lifetime



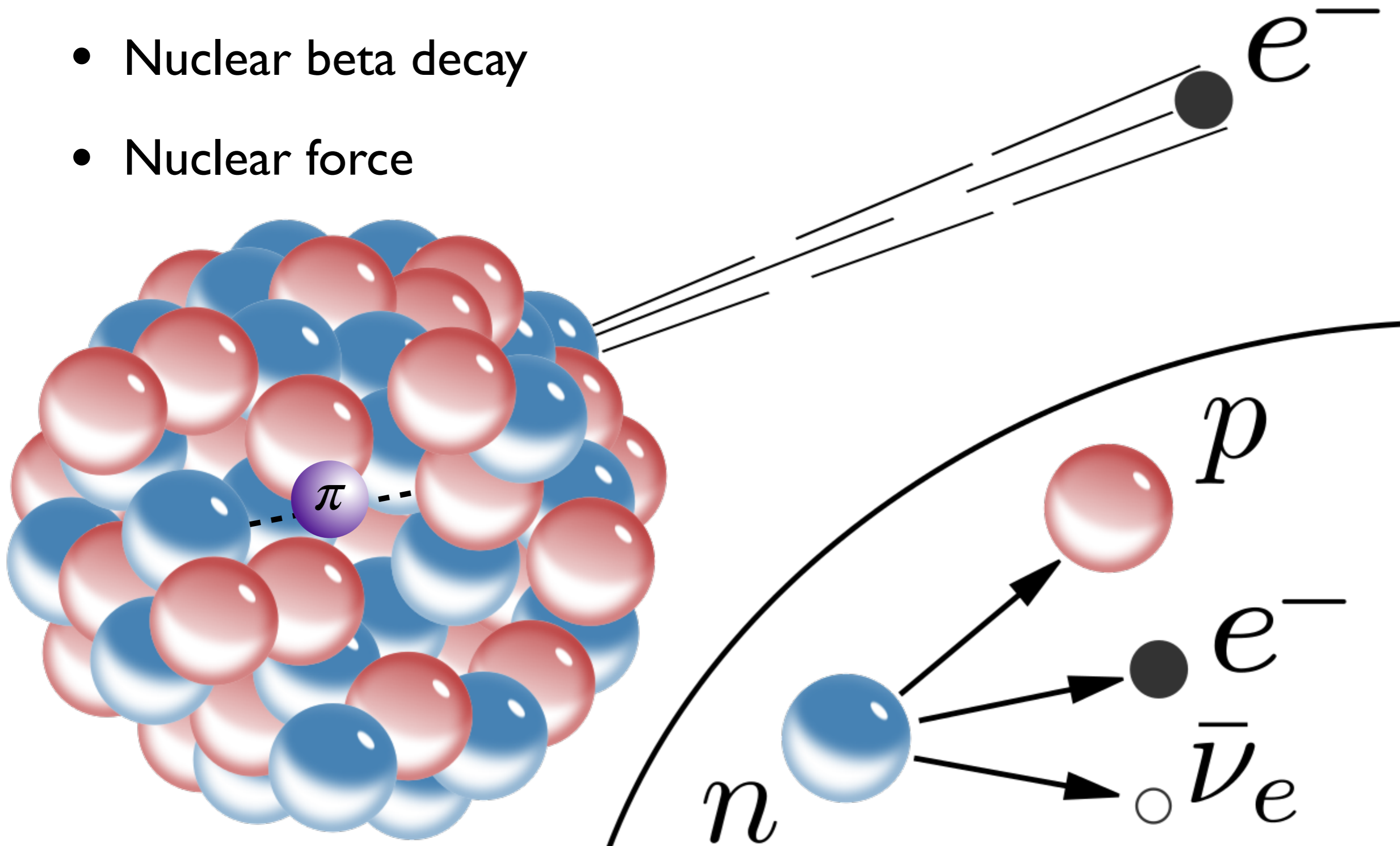
What depends on g_A ?

- Free neutron lifetime
- Nuclear beta decay



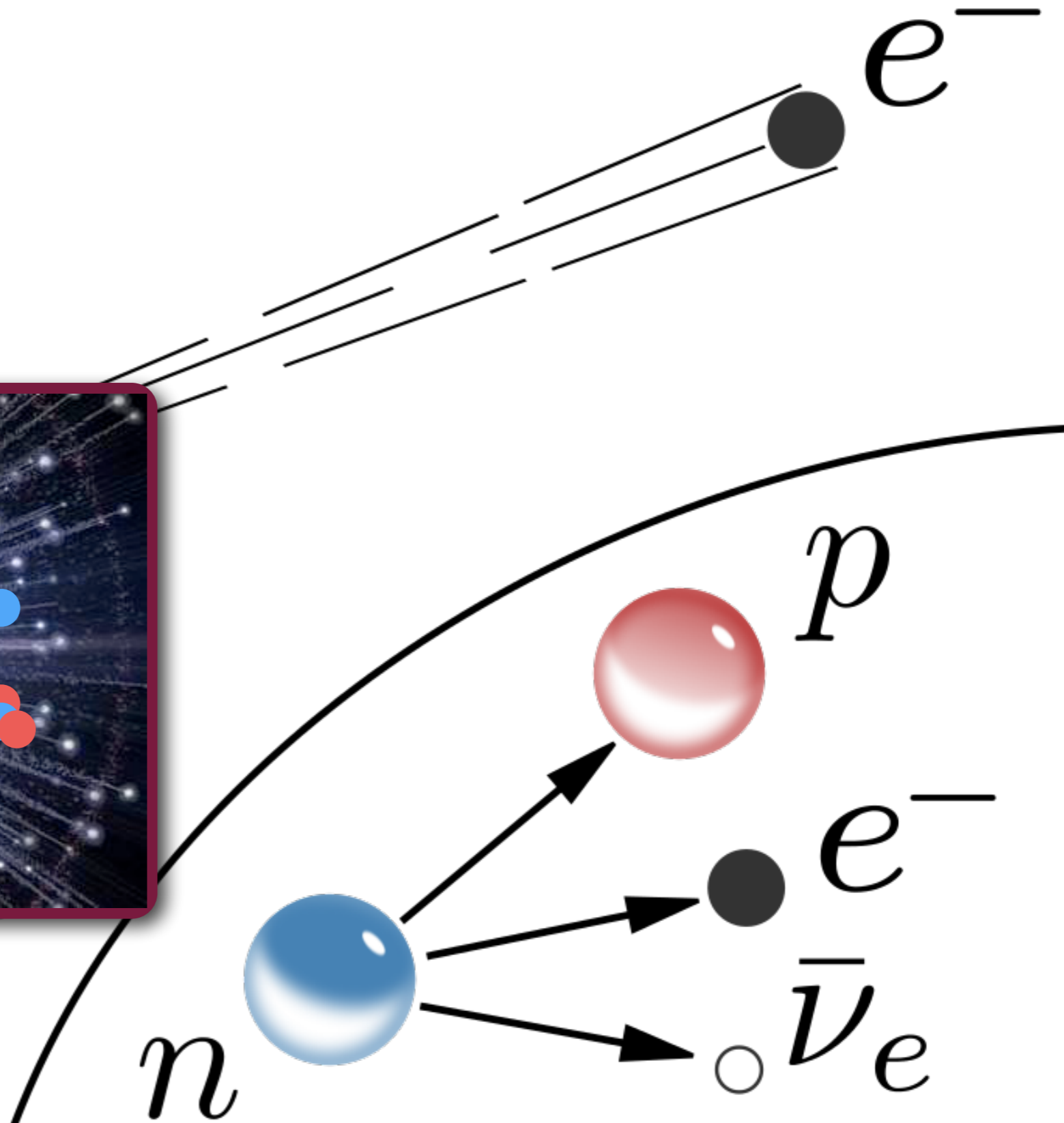
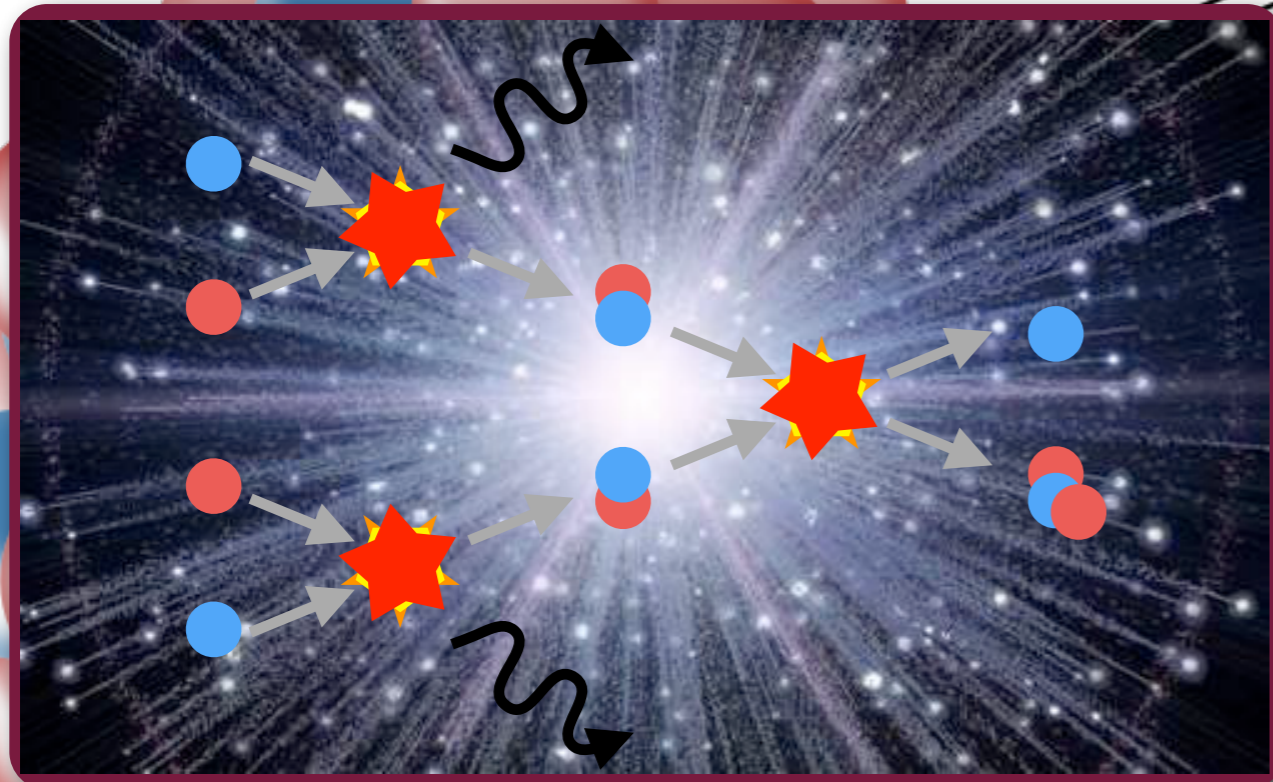
What depends on g_A ?

- Free neutron lifetime
- Nuclear beta decay
- Nuclear force



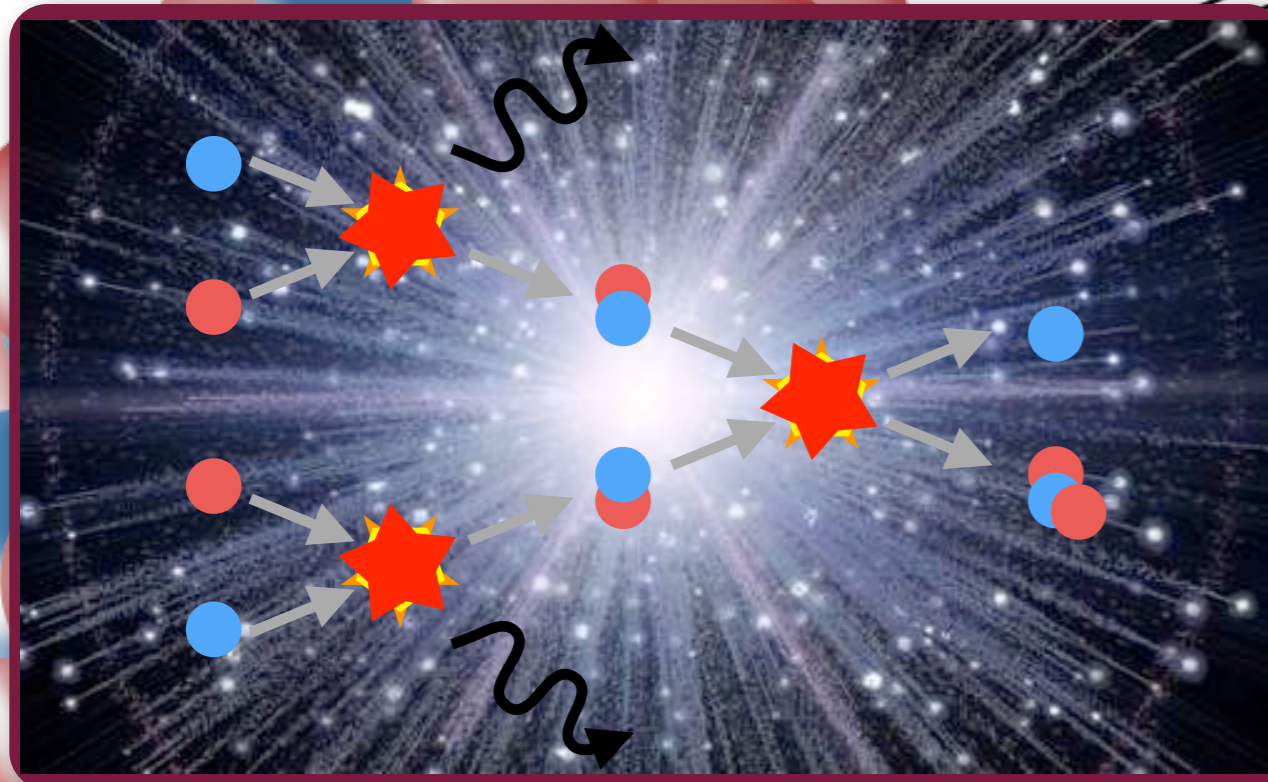
What depends on g_A ?

- Free neutron lifetime
- Nuclear beta decay
- Nuclear force
- Big Bang nucleosynthesis



What depends on g_A ?

- Free neutron lifetime
- Nuclear beta decay
- Nuclear force
- Big Bang nucleosynthesis
- Stellar processes



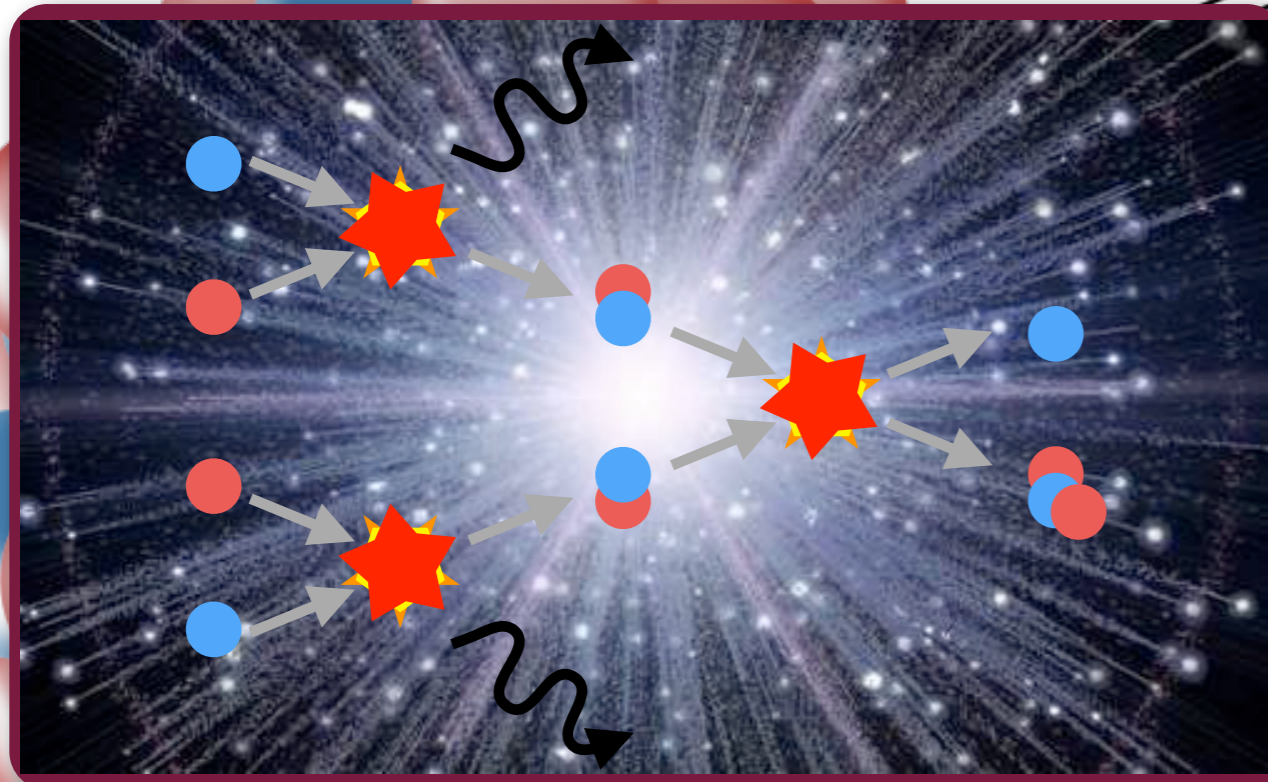
e^-

n

$\bar{\nu}_e$

What depends on g_A ?

- Free neutron lifetime
- Nuclear beta decay
- Nuclear force
- Big Bang nucleosynthesis
- Stellar processes
-



e^-

n

$\bar{\nu}_e$

- Free neutrino
- Nuclear
- Nuclear

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Nucleon Axial Charge in Full Lattice QCD

R. G. Edwards, G. T. Fleming, Ph. Hägler, J. W. Negele, K. Orginos, A. V. Pochinsky, D. B. Renner, D. G. Richards, and W. Schroers (LHPC Collaboration)
Phys. Rev. Lett. **96**, 052001 – Published 7 February 2006

The axial charge is the ideal starting point in the quest for precision lattice calculation of hadron structure for several reasons. It is accurately measured experimentally and the isovector combination $\langle 1 \rangle_{\Delta u} - \langle 1 \rangle_{\Delta d}$ has no contributions from disconnected diagrams, which are much more computationally demanding than the connected diagrams considered in this work. The functional dependence on both m_π^2 and volume is known at small masses from chiral perturbation theory (χ PT) [5,6] and renormalization of the lattice axial vector current can be performed accurately nonperturbatively using the five-dimensional conserved current for domain wall fermions. Thus, conceptually, it is a “gold plated” test of our ability to calculate hadron observables from first principles on the lattice. In addition, since it is known to be particularly sensitive to finite lattice volume effects that reduce the contributions of the pion cloud [7,8], it is also a stringent test of our control of finite volume artifacts.



synthesis

e^-

$\bar{\nu}_e$

- Free neutrino
- Nuclear
- Nuclear

PHYSICAL REVIEW LETTERS

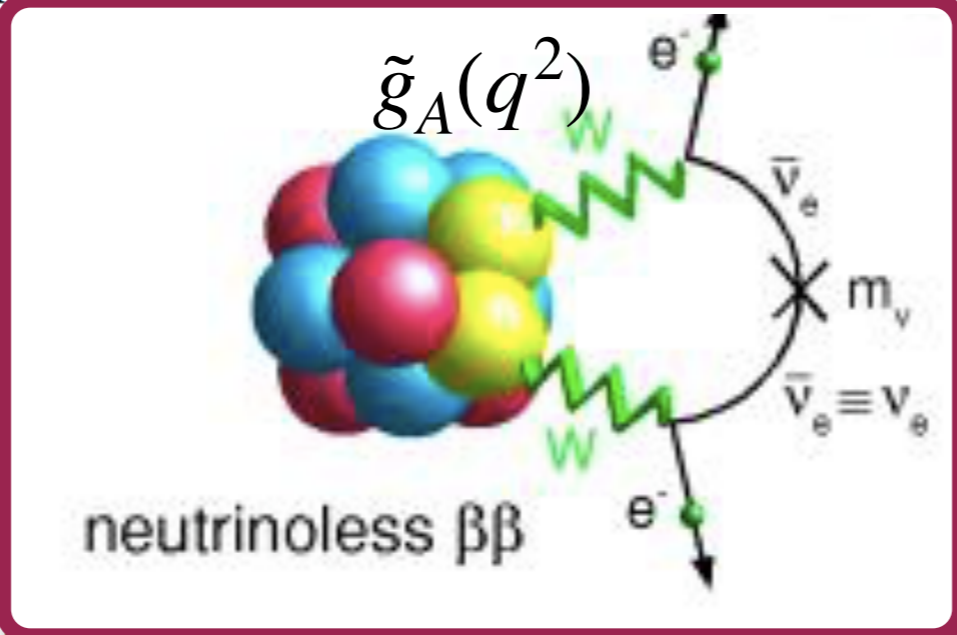
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Nucleon Axial Charge in Full Lattice QCD

R. G. Edwards, G. T. Fleming, Ph. Hägler, J. W. Negele, K. Orginos, A. V. Pochinsky, D. B. Renner, D. G. Richards, and W. Schroers (LHPC Collaboration)
 Phys. Rev. Lett. **96**, 052001 – Published 7 February 2006

The axial charge is the ideal starting point in the quest for precision structure for several reasons. Experimentally, it is the only observable with no contributions from disconnected diagrams. It is much more computationally tractable than other observables. It is independent of the lattice spacing, which allows for a direct comparison with experimental data. It is also particularly sensitive to finite lattice volume effects that reduce the contributions of the pion cloud [7,8], it is also a stringent test of our control of finite volume artifacts.



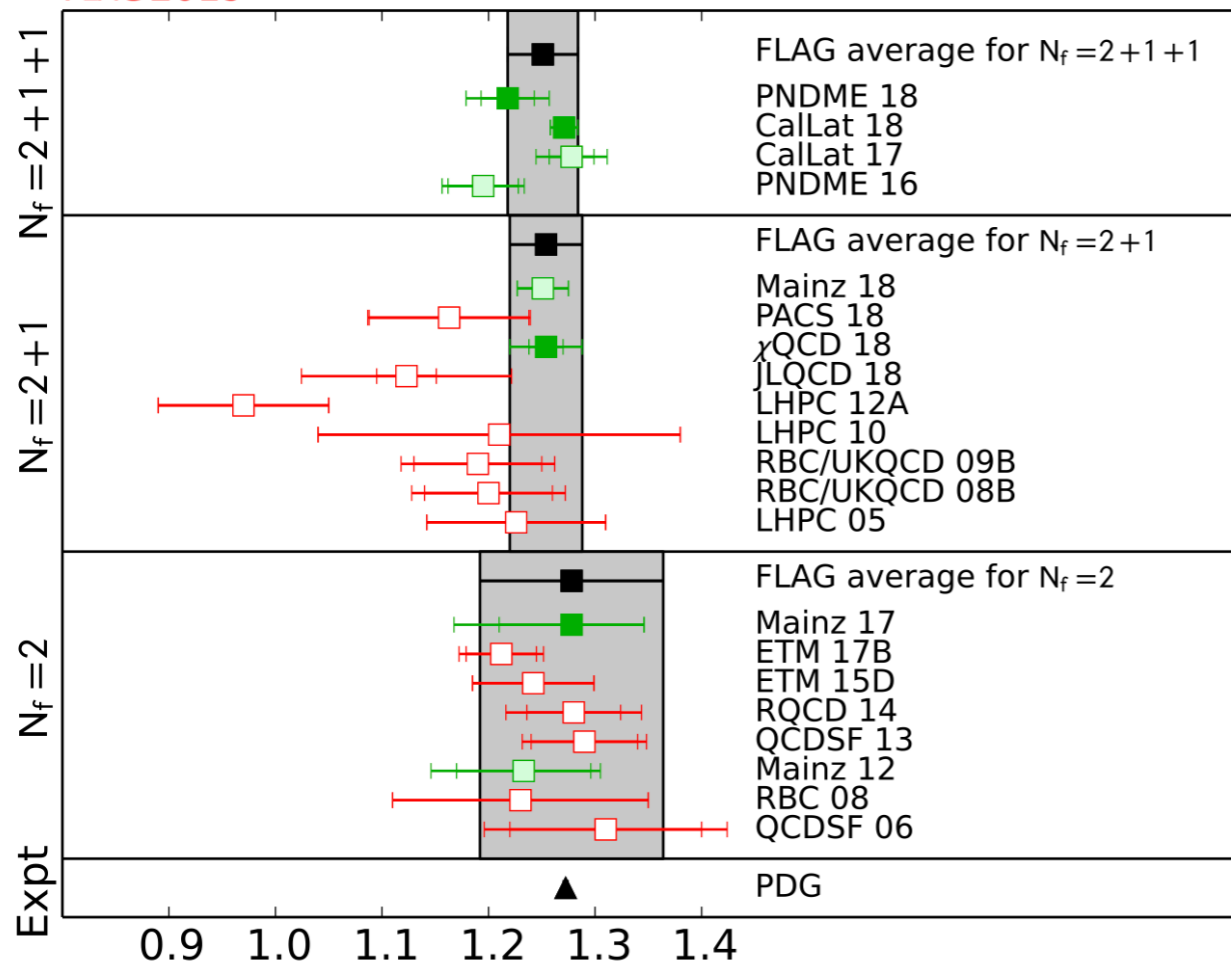
synthesis

e^-

$\bar{\nu}_e$

FLAG2019

g_A^{u-d}



nature

International journal of science

Letter | Published: 30 May 2018

A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics

C. C. Chang, A. N. Nicholson, E. Rinaldi, E. Berkowitz, N. Garron, D. A. Brantley, H. Monge-Camacho, C. J. Monahan, C. Bouchard, M. A. Clark, B. Joó, T. Kurth, K. Orginos, P. Vranas & A. Walker-Loud

Simulating the *weak* death of the neutron in a femtoscale universe with near-Exascale computing

Evan Berkowitz*, M.A. Clark†, Arjun Gambhir‡§¶, Ken McElvain¶§, Amy Nicholson||, Enrico Rinaldi**§, Pavlos Vranas ‡§ André Walker-Loud §¶¶, and Chia Cheng Chang§, Bálint Joó††, Thorsten Kurth‡‡§, Kostas Orginos^{xxi},

* Institut für Kernphysik and Institute for Advanced Simulation, Forschungszentrum Jülich, 52425 Jülich Germany

† NVIDIA Corporation, Santa Clara, California, 95051, USA

‡ Physical Sciences Directorate, Lawrence Livermore National Laboratory, Livermore, California 94550, USA

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¶ Department of Physics, University of California, Berkeley, CA 94720, USA

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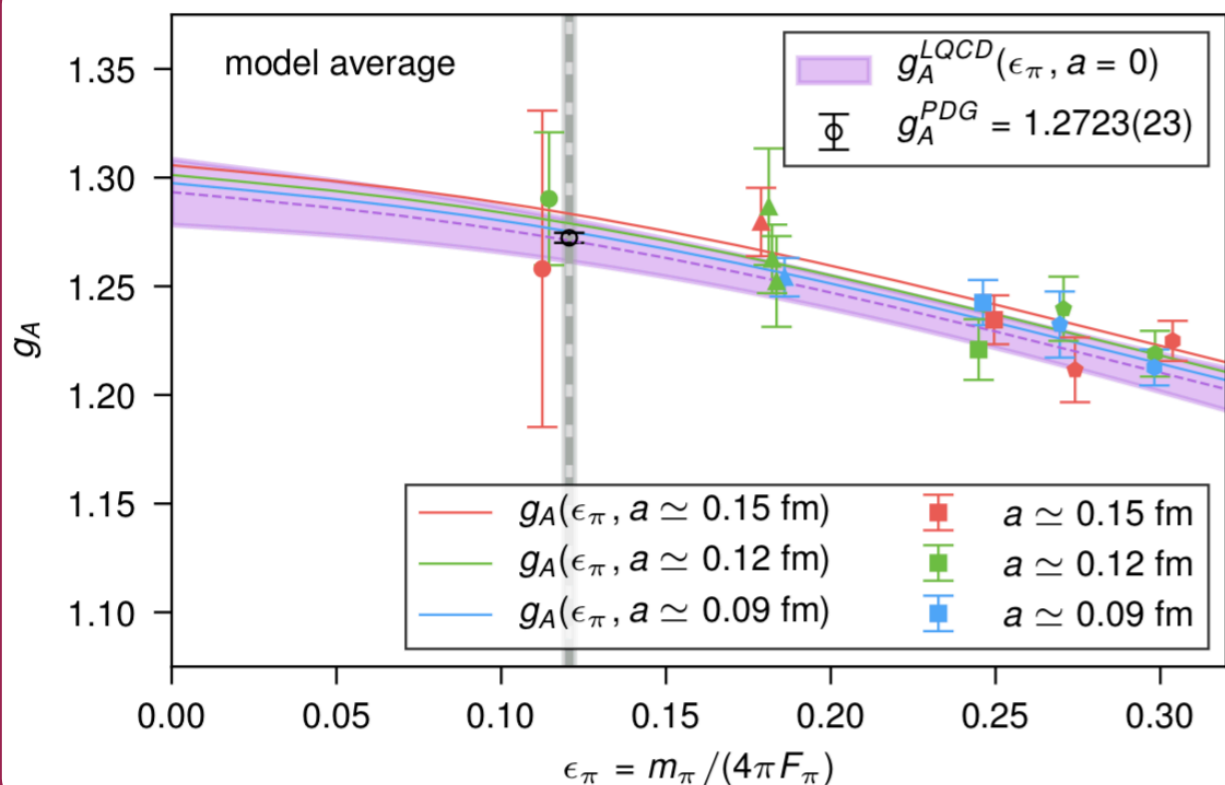
** RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973, USA

†† Scientific Computing Group, Thomas Jefferson National Accelerator Facility, Newport News, VA 23606, USA

‡‡ NERSC, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

^x Department of Physics, The College of William & Mary, Williamsburg, VA 23187, USA

^{xxi} Theory Center, Thomas Jefferson National Accelerator Facility, Newport News, VA 23606, USA



acm AWARDS

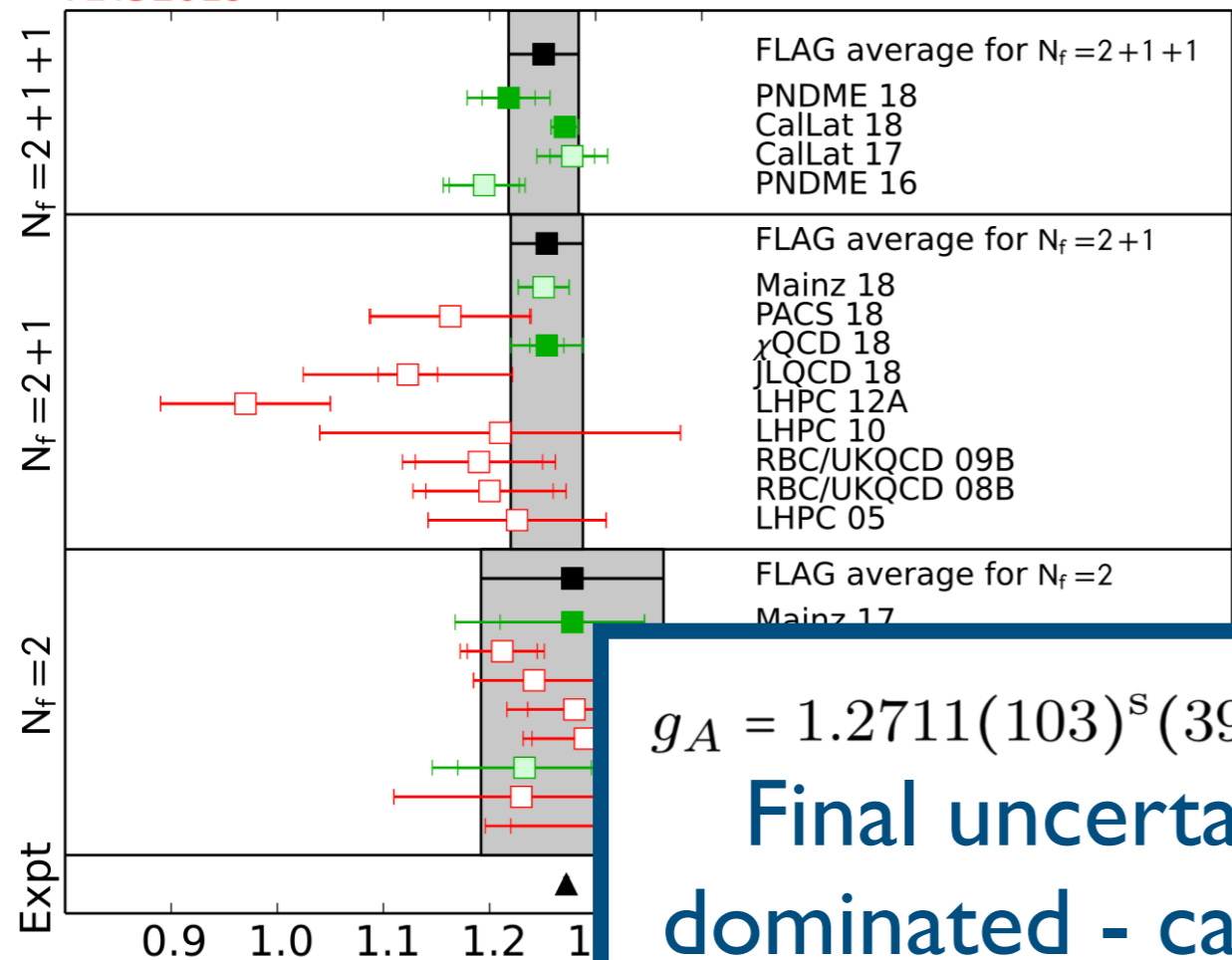
Gordon Bell Prize

Finalist

SC18
 Dallas, TX | hpc
 inspires.

FLAG2019

g_A^{u-d}



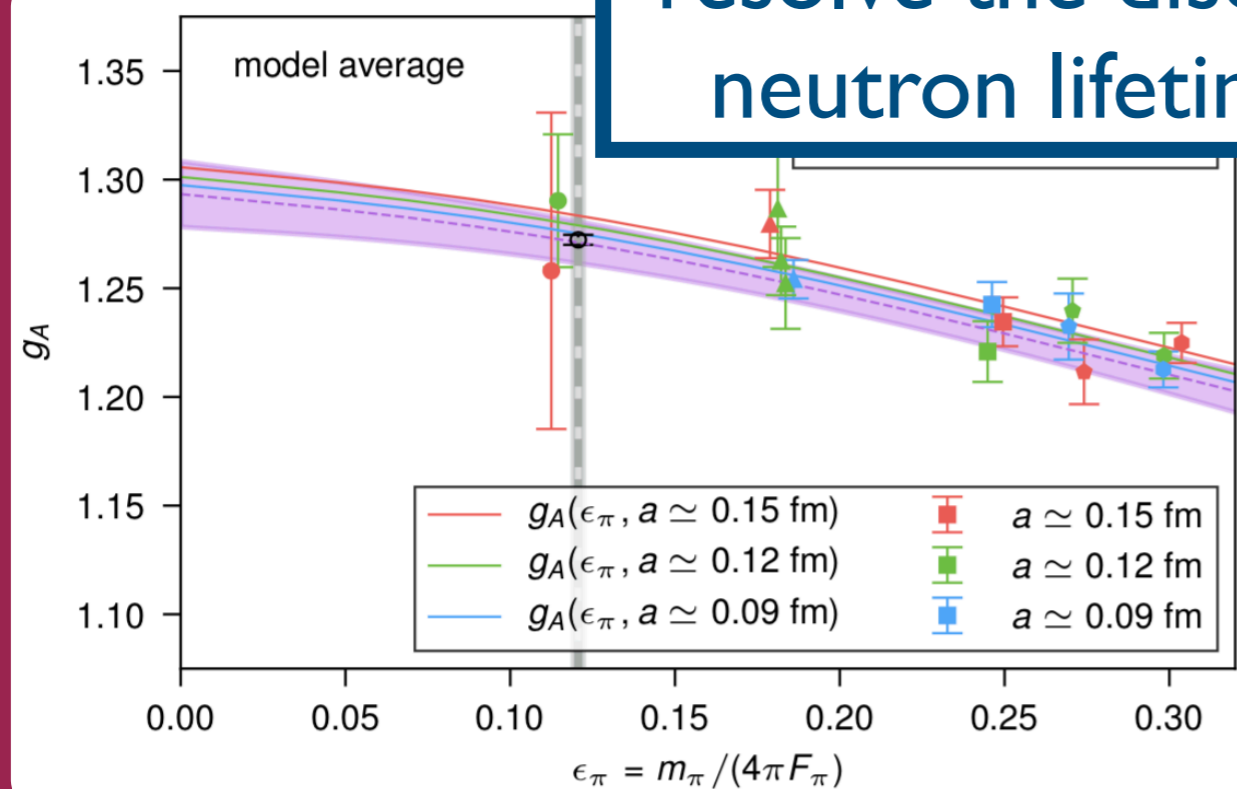
nature
International journal of science

Letter | Published: 30 May 2018

A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics

C. C. Chang, A. N. Nicholson, E. Rinaldi, E. Berkowitz, N. Garron, D. A. Brantley, H. Monge-Camacho, C. J. Monahan, C. Bouchard, M. A. Clark, B. Joó, T. Kurth, K. Orginos, P. Vranas & A. Walker-Loud

$g_A = 1.2711(103)^s(39)^x(15)^a(19)^v(04)^I(55)^M$
Final uncertainty is statistics dominated - can we push this to resolve the discrepancy between neutron lifetime experiments?



path of the neutron in a near-Exascale computing

Chir^{†††}, Ken McElvain[§], Amy Nicholson^{||},
 s^{†§} André Walker-Loud^{§†¶},
 Thorsten Kurth^{††§}, Kostas Orginos^{xxi},
 ation, Forschungszentrum Jülich, 54245 Jülich Germany
 lara, California, 95051, USA

§ Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA
 ¶ Department of Physics, University of California, Berkeley, CA 94720, USA
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 ** RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973, USA
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acm AWARDS
Gordon Bell Prize
Finalist

SC18
Dallas, TX hpc inspires.

New physics? Neutron lifetime puzzle

New physics? Neutron lifetime puzzle

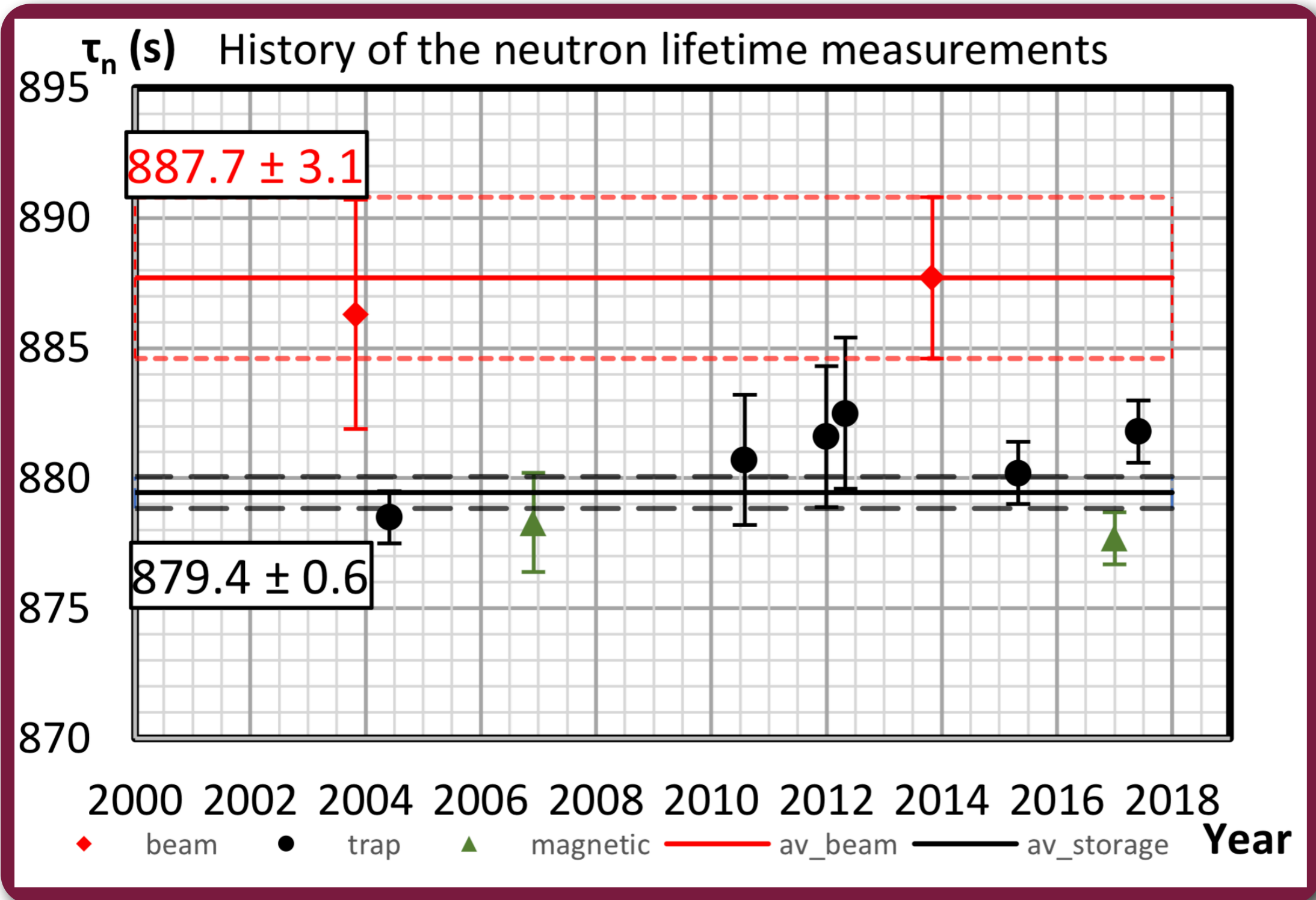


Figure: A. P. Serebrov, E. A. Kolomensky, A. K. Fomin, I. A. Krasnoschekova, A. V. Vassiljev, D. M. Prudnikov, I. V. Shoka, A. V. Chechkin, M. E. Chaikovskiy, V. E. Varlamov, S. N. Ivanov, A. N. Pirozhkov, P. Geltenbort, O. Zimmer, T. Jenke, M. Van der Grinten, M. Tucker, arXiv:1712.05663

New physics? Neutron lifetime puzzle

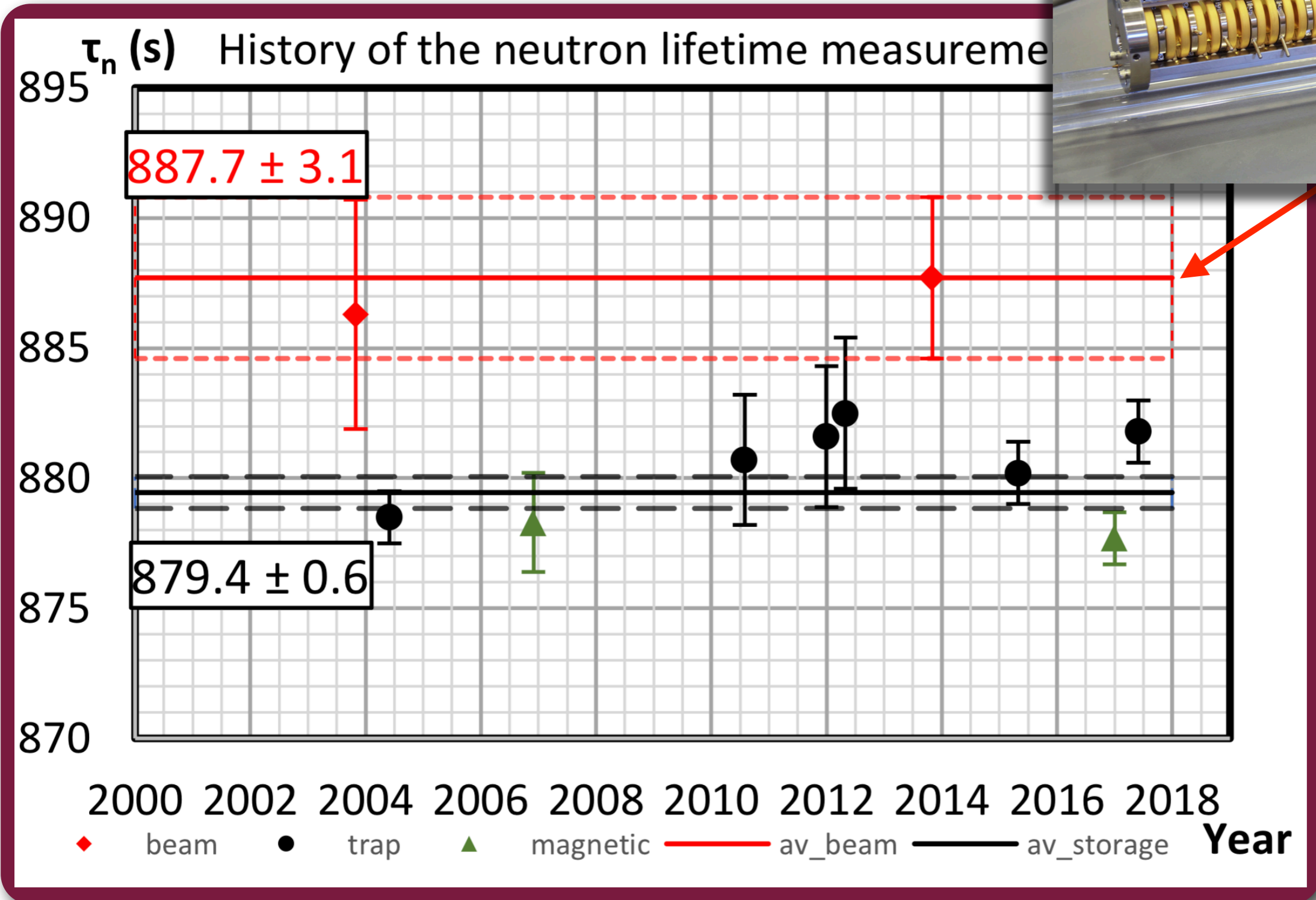
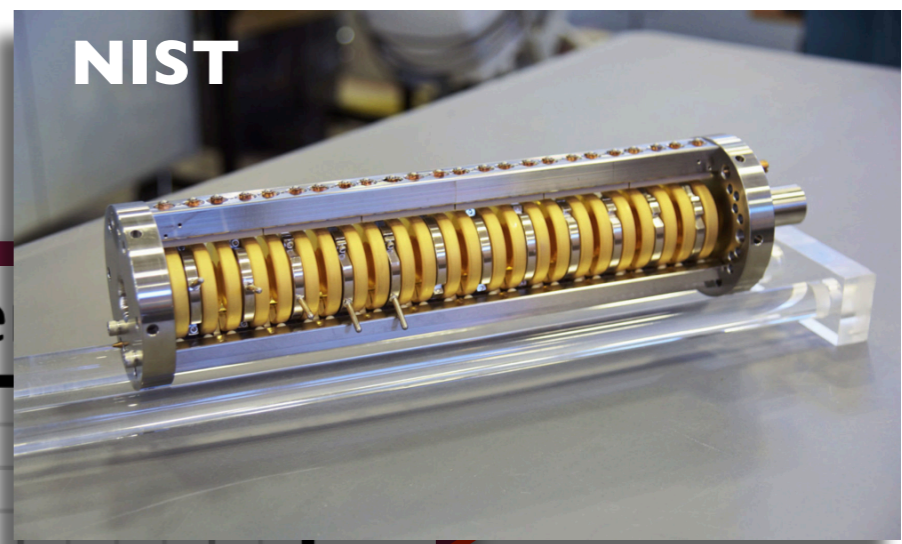


Figure: A. P. Serebrov, E. A. Kolomensky, A. K. Fomin, I. A. Krasnoschekova, A. V. Vassiljev, D. M. Prudnikov, I. V. Shoka, A. V. Chechkin, M. E. Chaikovskiy, V. E. Varlamov, S. N. Ivanov, A. N. Pirozhkov, P. Geltenbort, O. Zimmer, T. Jenke, M. Van der Grinten, M. Tucker, arXiv:1712.05663

New physics? Neutron lifetime puzzle

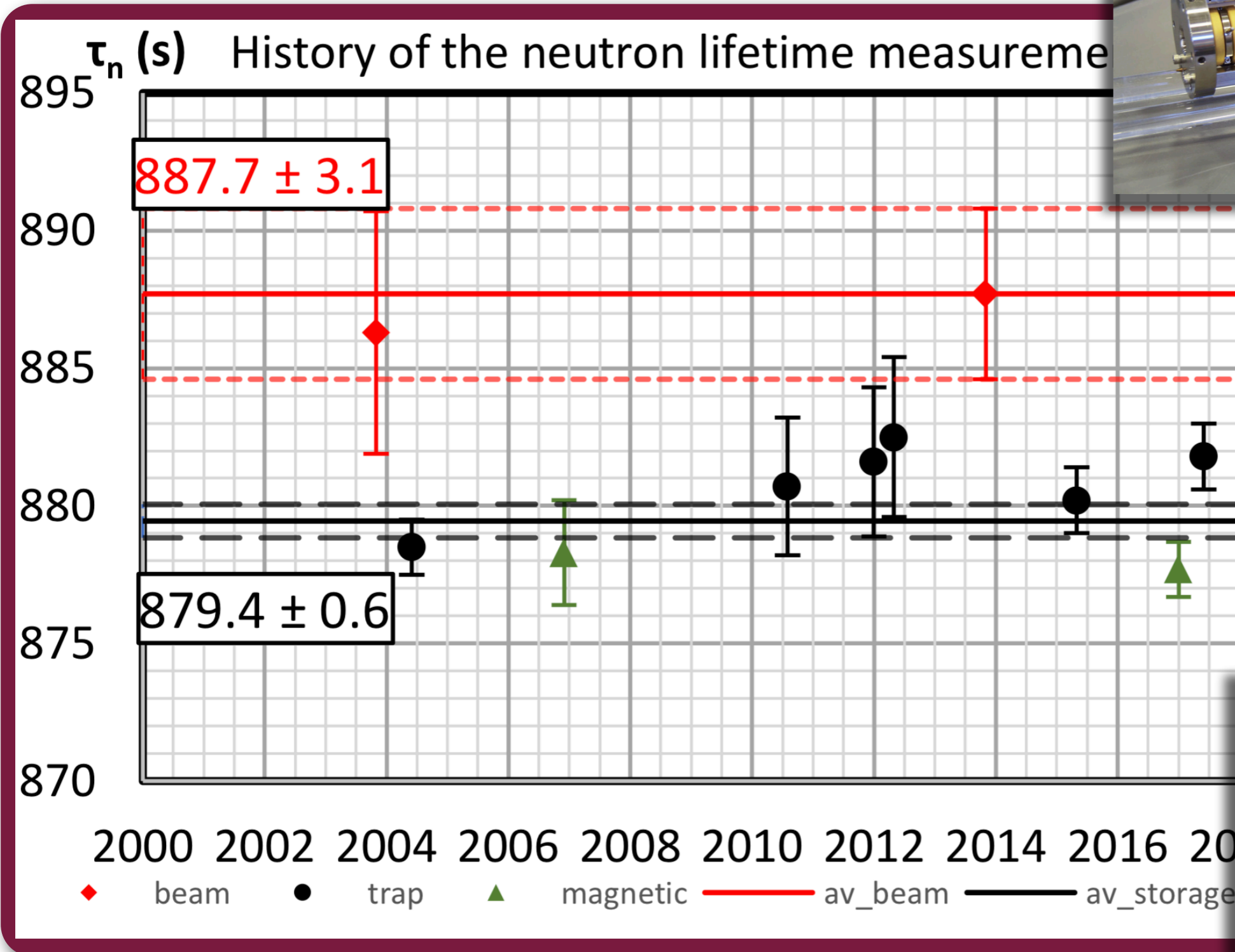
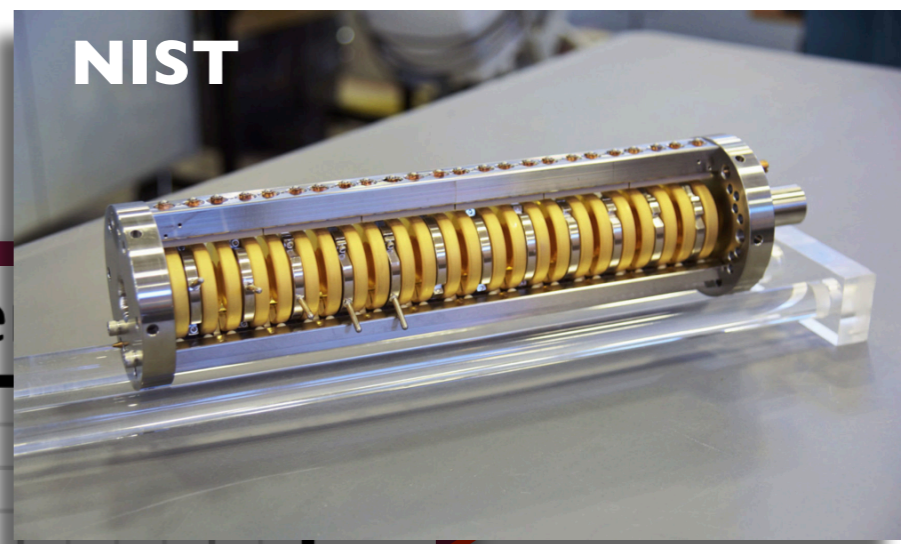


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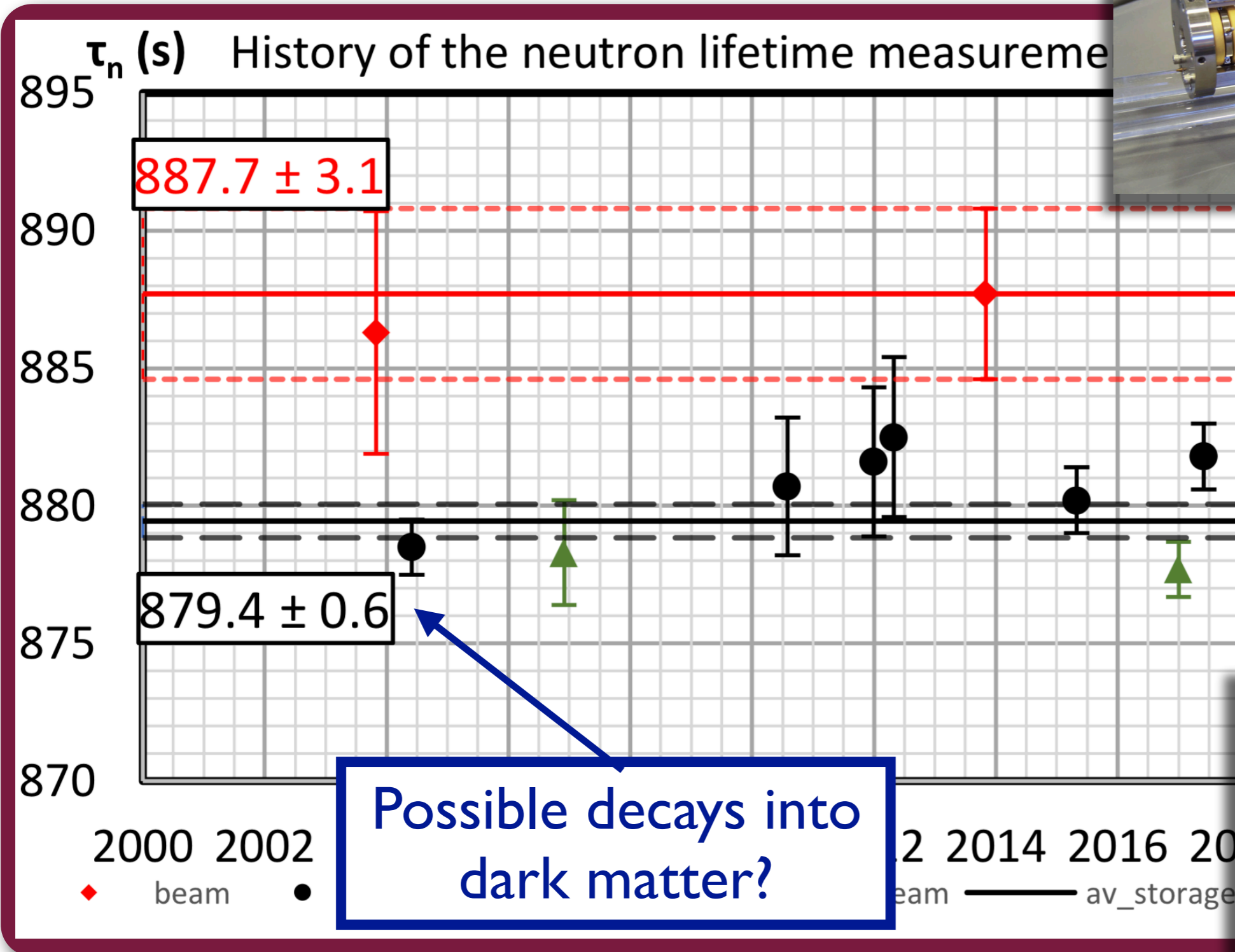
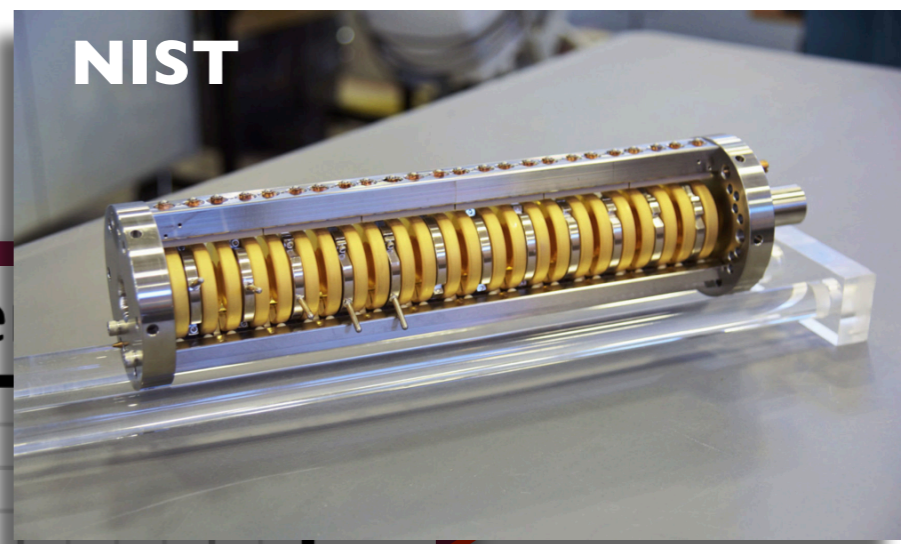


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New physics? Neutron lifetime puzzle

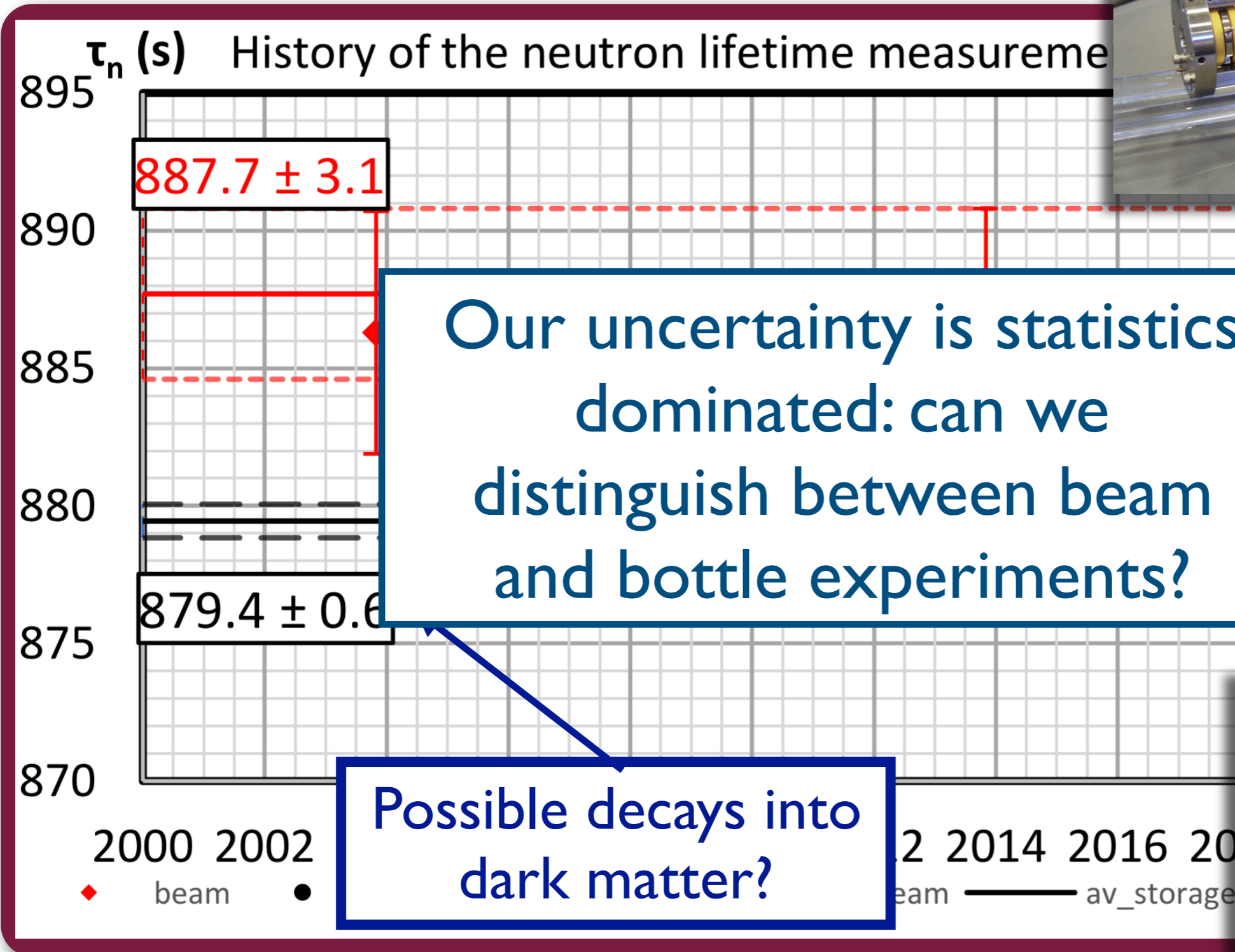
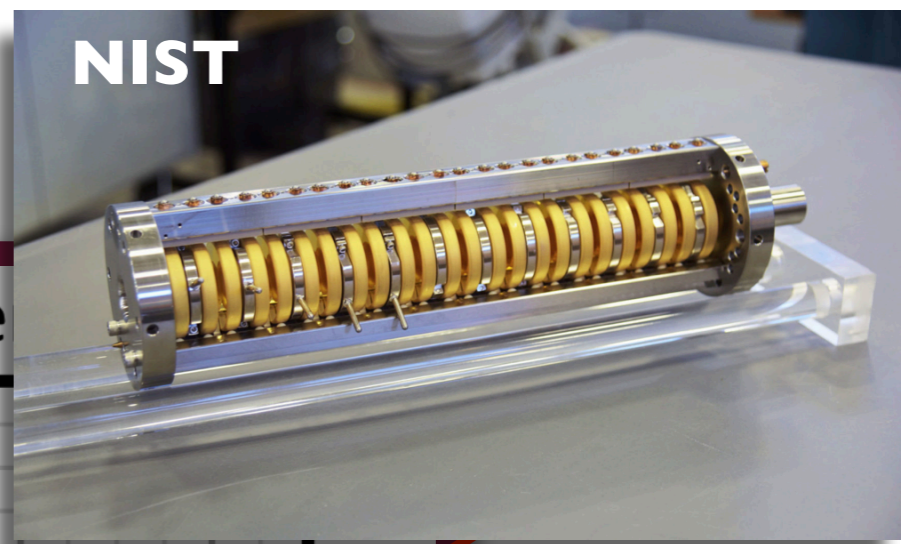
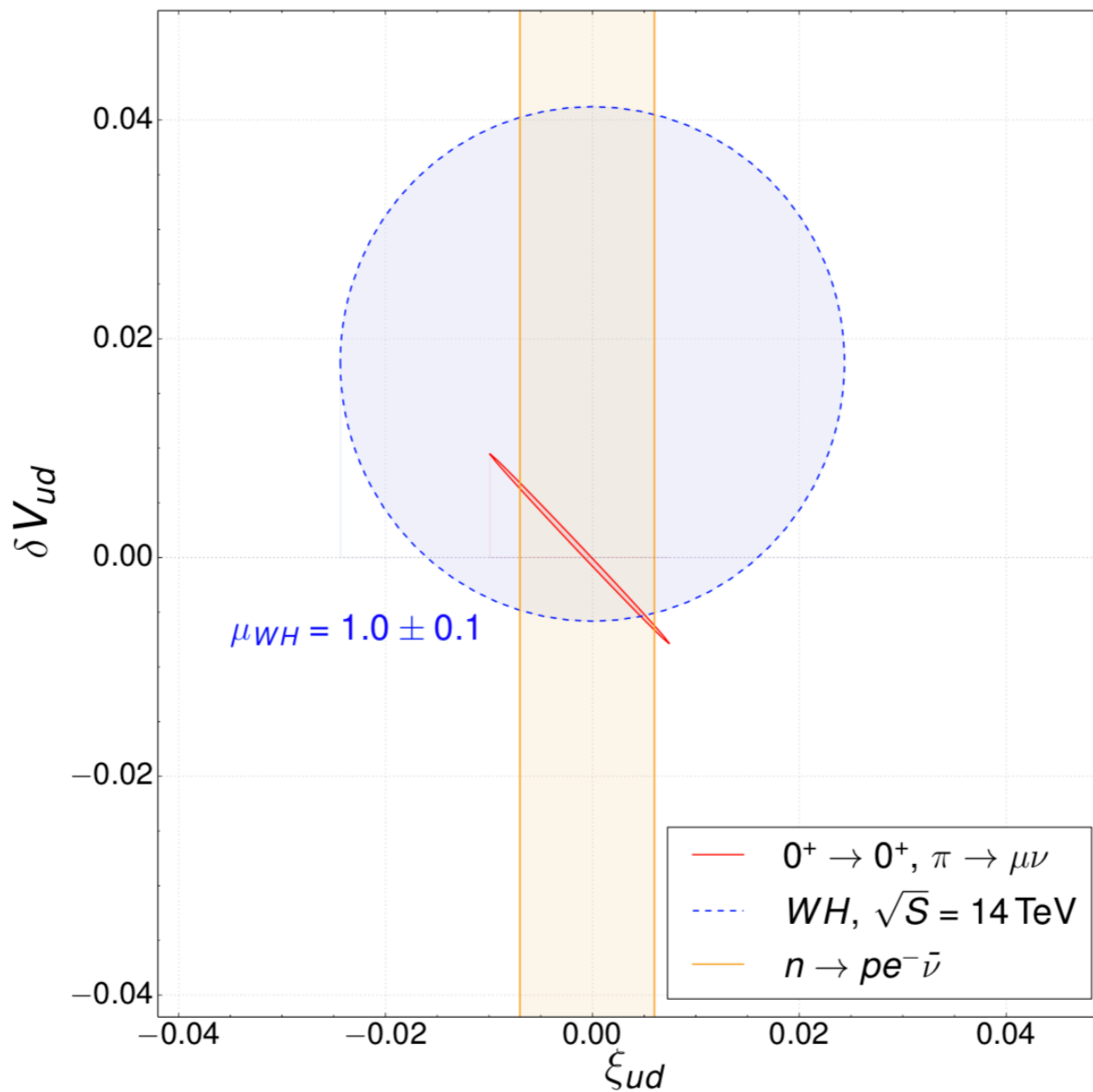


Figure: A. P. Serebrov, E. A. Kolomensky, A. K. Fomin, I. A. Krasnoschekova, A. V. Vassiljev, D. M. Prudnikov, I. V. Shoka, A. V. Chechkin, M. E. Chaikovskiy, V. E. Varlamov, S. N. Ivanov, A. N. Pirozhkov, P. Geltenbort, O. Zimmer, T. Jenke, M. Van der Grinten, M. Tucker, arXiv:1712.05663



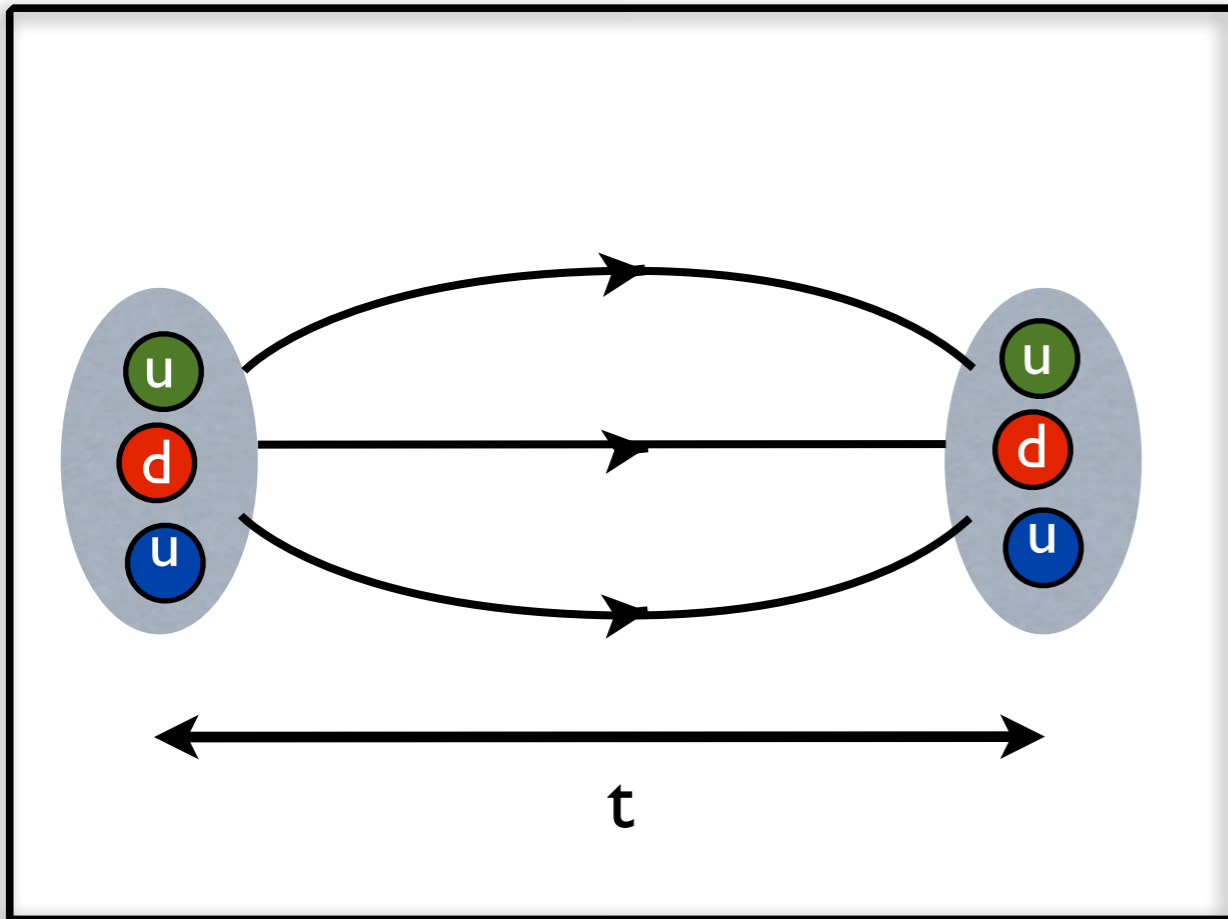
Can already place stronger constraints on right-handed BSM currents than collider experiments

Alioli, S., Cirigliano, V.,
 Dekens, W.,
 de Vries, J., and
 Mereghetti, E.
 JHEP 05, 086 (2017)

Matrix Elements



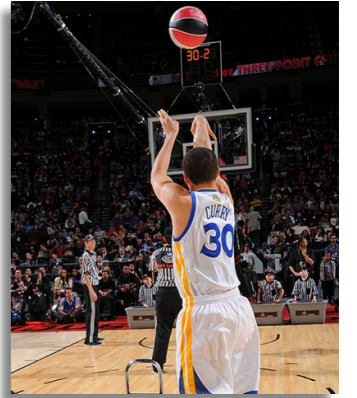
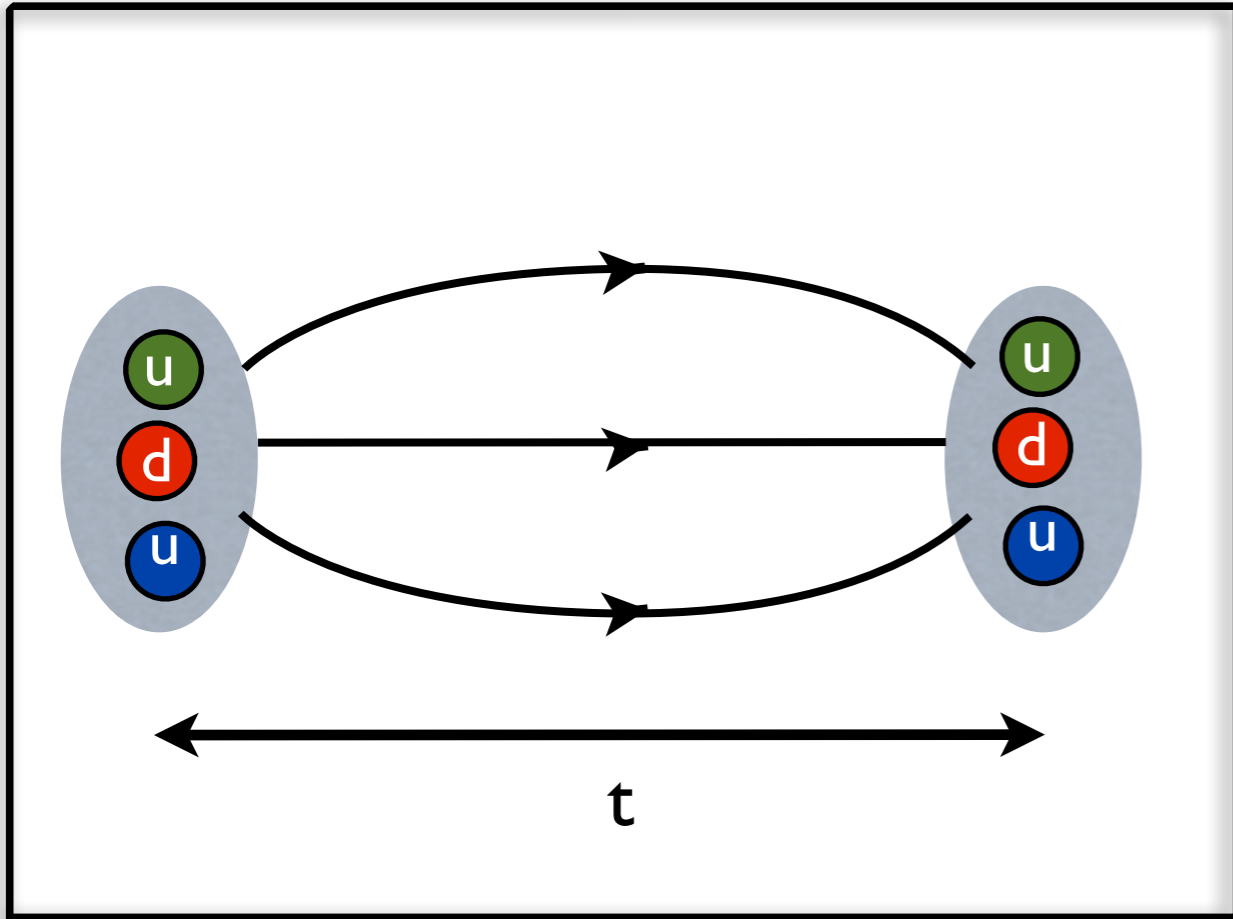
2-point function



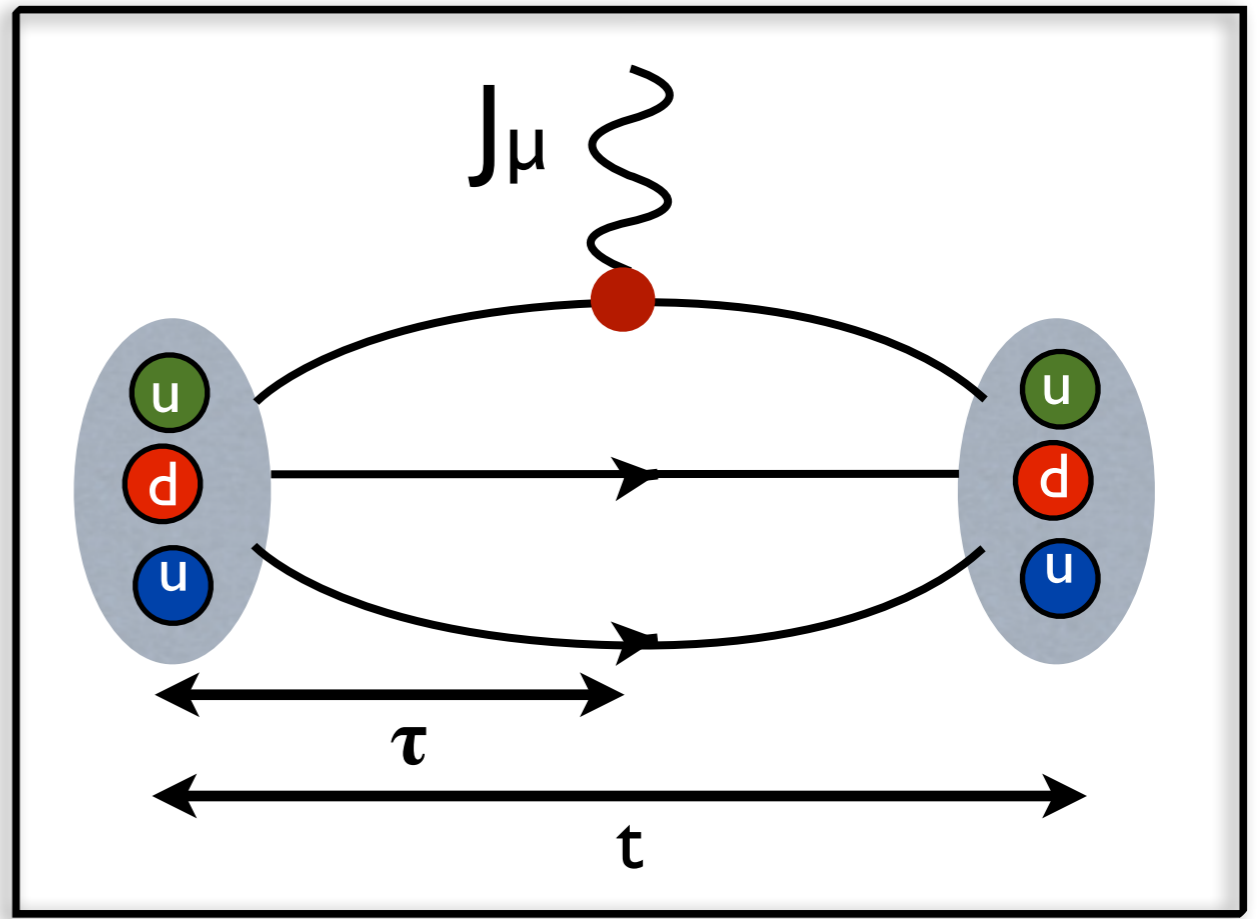
Matrix Elements



2-point function



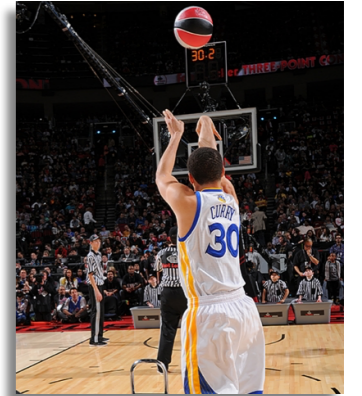
3-point function



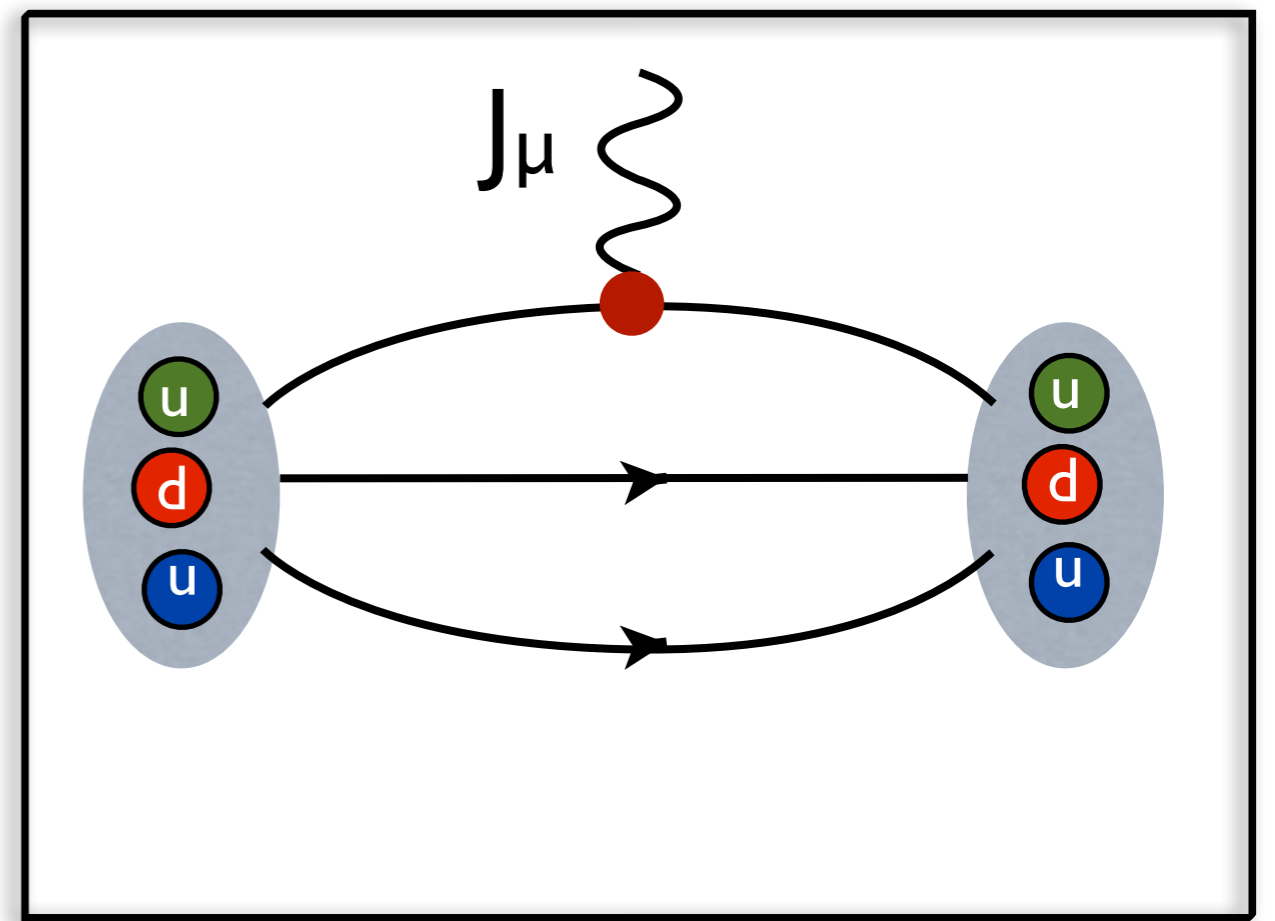
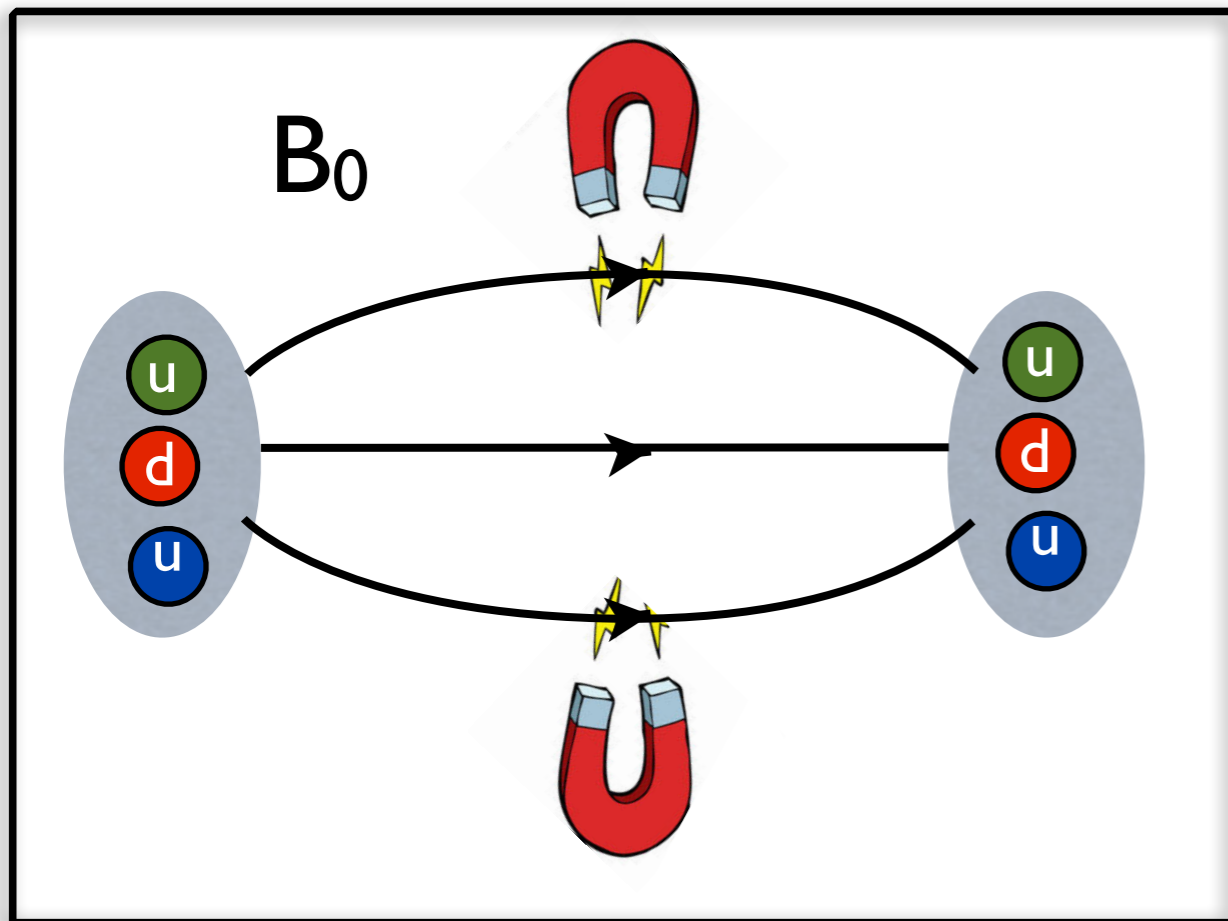
Matrix Elements



Background field



3-point function



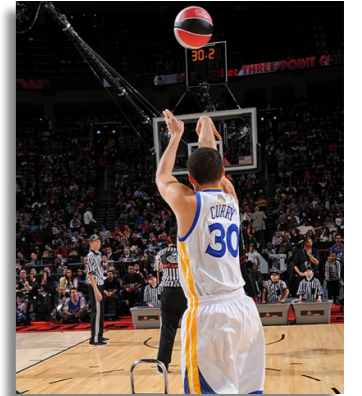
FH Theorem: $H = H_0 + \lambda J$
 $\frac{dE}{d\lambda} = \langle \psi | J | \psi \rangle$

FH turns a 3-pt calc into a 2-pt calc

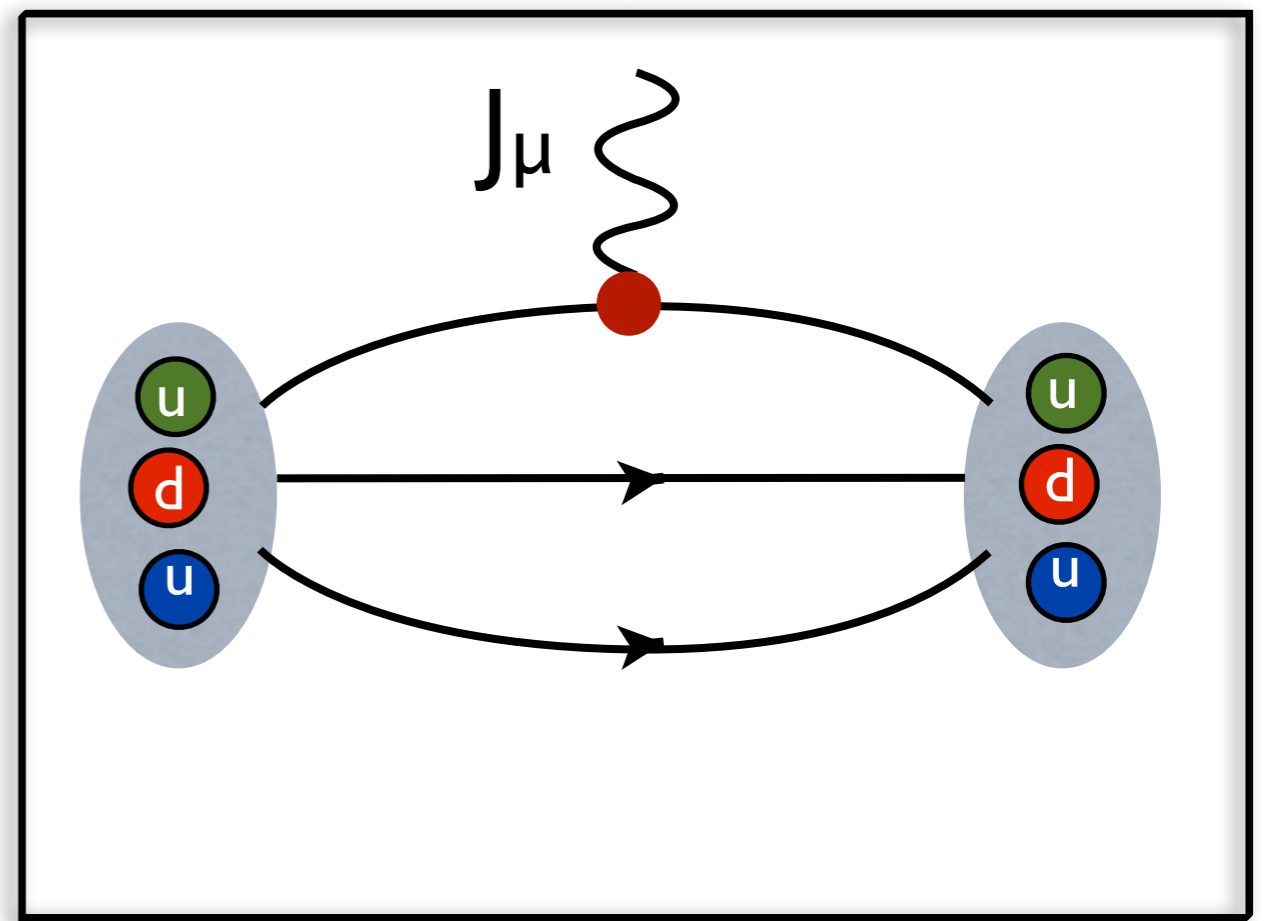
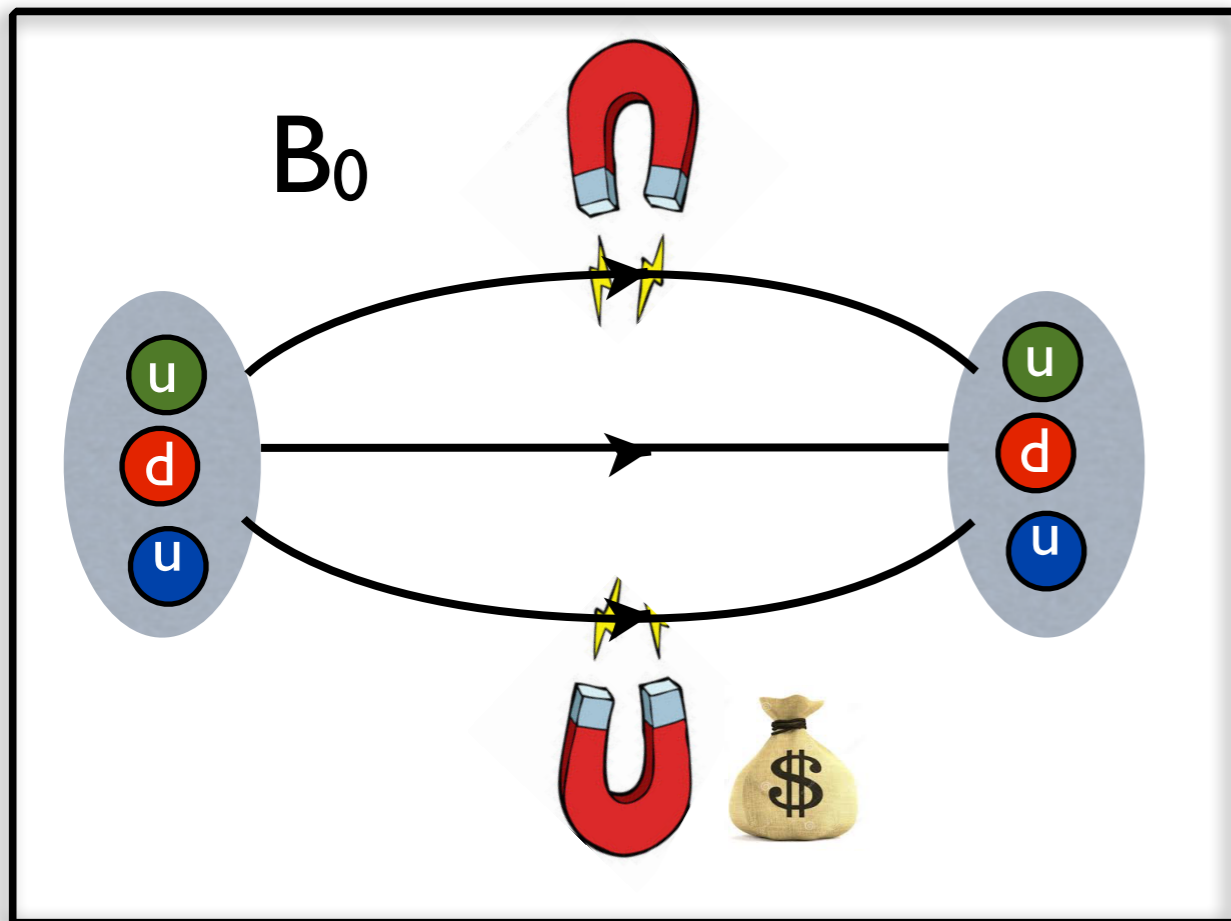
Matrix Elements



Background field



3-point function



FH Theorem: $H = H_0 + \lambda J$

$$\frac{dE}{d\lambda} = \langle \psi | J | \psi \rangle$$

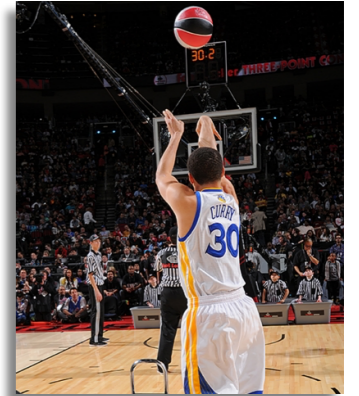
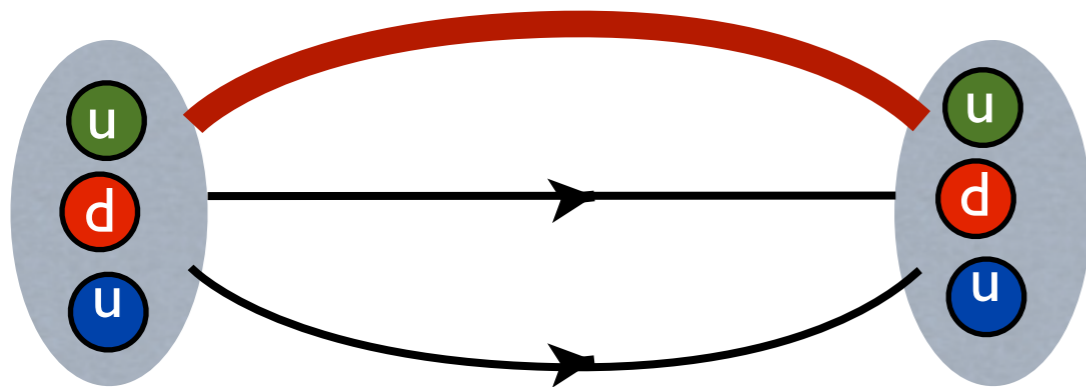
Must calculate field configurations at several λ to extract linear response

Matrix Elements

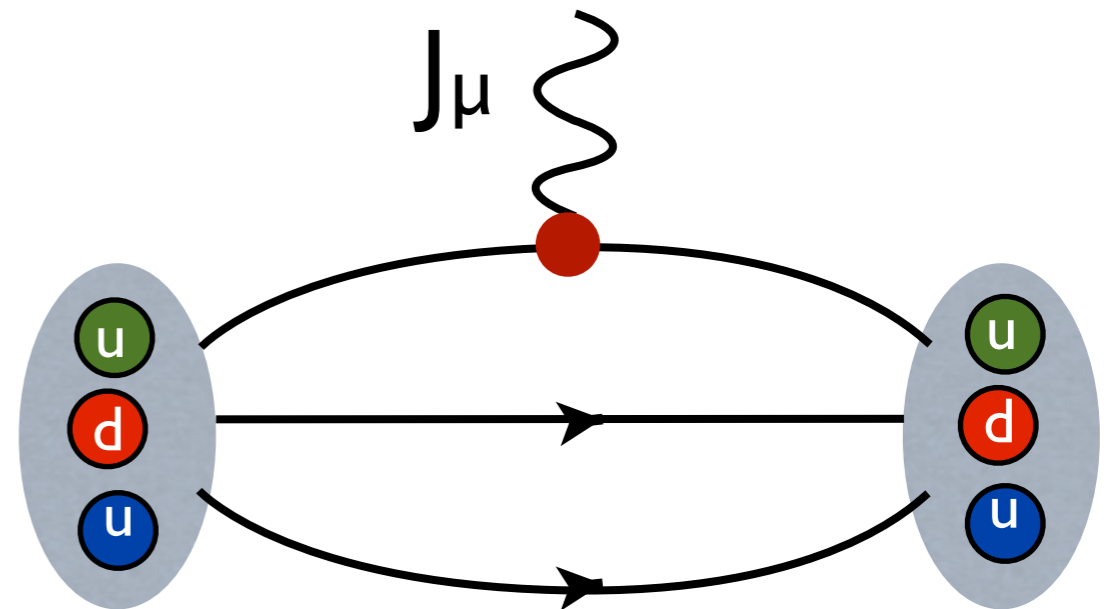


Feynman-Hellmann

Chris Bouchard, Chia Cheng Chang, Thorsten Kurth,
Kostas Orginos, Andre Walker-Loud arXiv:1612.06963
similar techniques used in:
A.J. Chambers et al. (2014,2015), M.J. Savage et al. (2016)



3-point function



FH Theorem: $H = H_0 + \lambda J$

$$\frac{dE}{d\lambda} = \langle \psi | J | \psi \rangle$$

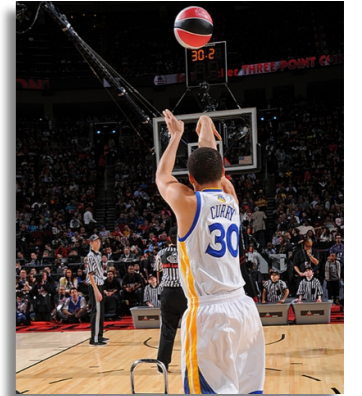
Get all time separations with a single calculation - found benefit in using earlier times where signal is more precise

Matrix Elements



Feynman-Hellmann

3-point function



Good for studying
in-medium effects

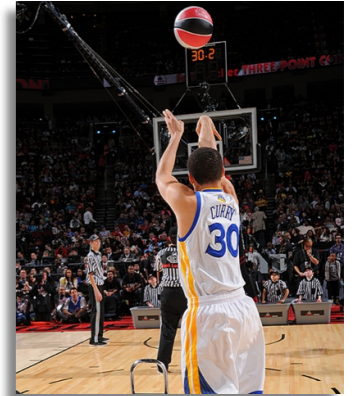
Good for studying
form factors

FH Theorem: $H = H_0 + \lambda J$

$$\frac{dE}{d\lambda} = \langle \psi | J | \psi \rangle$$

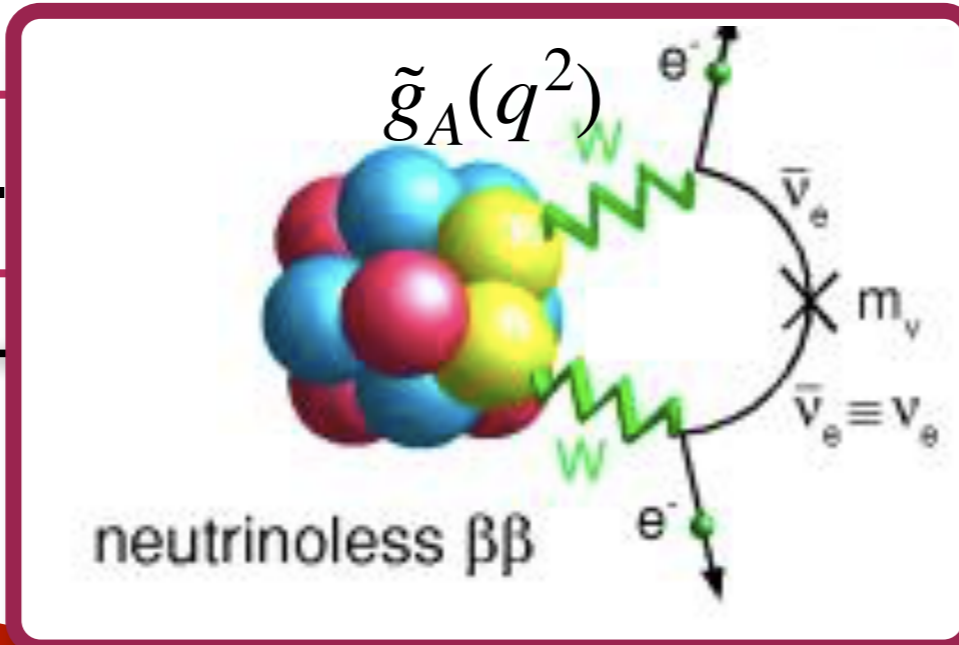
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Matrix Elements



Feynman-

function



Good for studying
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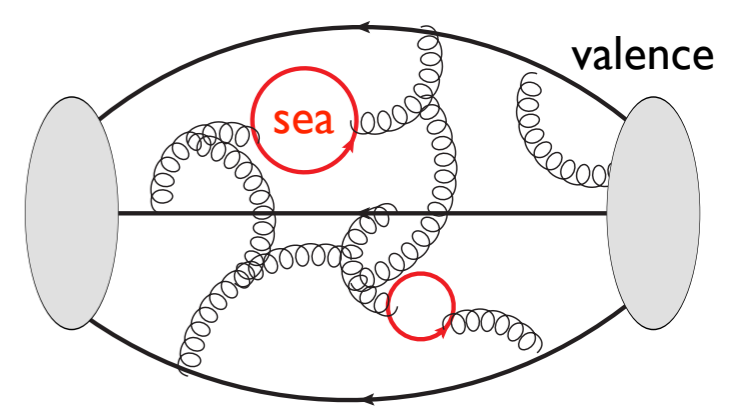
FH Theorem: $H = H_0 + \lambda J$

$$\frac{dE}{d\lambda} = \langle \psi | J | \psi \rangle$$

Get all time separations with a single calculation - found benefit in using earlier times where signal is more precise

Precision requires action with a well-behaved
approach to the physical limit

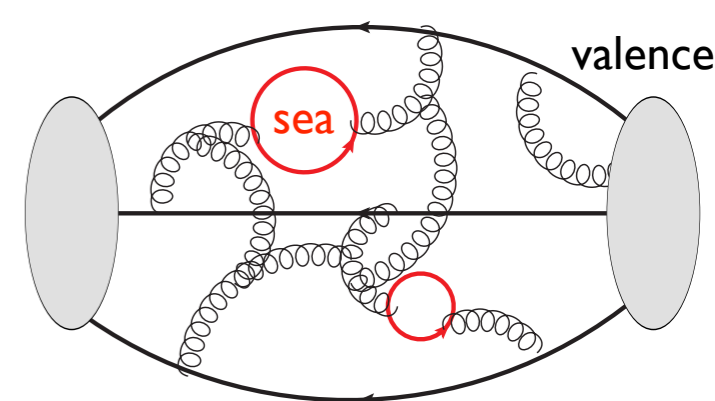
Precision requires action with a well-behaved approach to the physical limit



$a[\text{fm}] : m_\pi [\text{MeV}]$	400	350	310	220	130
0.15	$m_\pi L \sim 4.8$	$m_\pi L \sim 4.2$	$m_\pi L \sim 3.78$	$m_\pi L \sim 3.99$	$m_\pi L \sim 3.25$
				$m_\pi L \sim 3.22$	
0.12	$m_\pi L \sim 5.8$	$m_\pi L \sim 5.1$	$m_\pi L \sim 4.54$	$m_\pi L \sim 4.29$	$m_\pi L \sim 3.91$
				$m_\pi L \sim 5.36$	
0.09	$m_\pi L \sim 5.8$	$m_\pi L \sim 5.1$	$m_\pi L \sim 4.50$	$m_\pi L \sim 4.73$	

MILC Collaboration
 Phys. Rev. D87 (2013)
 054505

Precision requires action with a well-behaved approach to the physical limit



$a[\text{fm}] : m_\pi [\text{MeV}]$	400	350	310	220	130
0.15	$m_\pi L \sim 4.8$	$m_\pi L \sim 4.2$	$m_\pi L \sim 3.78$	$m_\pi L \sim 3.99$	$m_\pi L \sim 3.25$
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MILC Collaboration
Phys. Rev. D87 (2013)
054505

- DWF:
- Chiral symmetry breaking exponentially suppressed
 - g_A/g_V is a quantitative measure of chiral symmetry breaking

• Discretization effects come in at $O(a^2)$

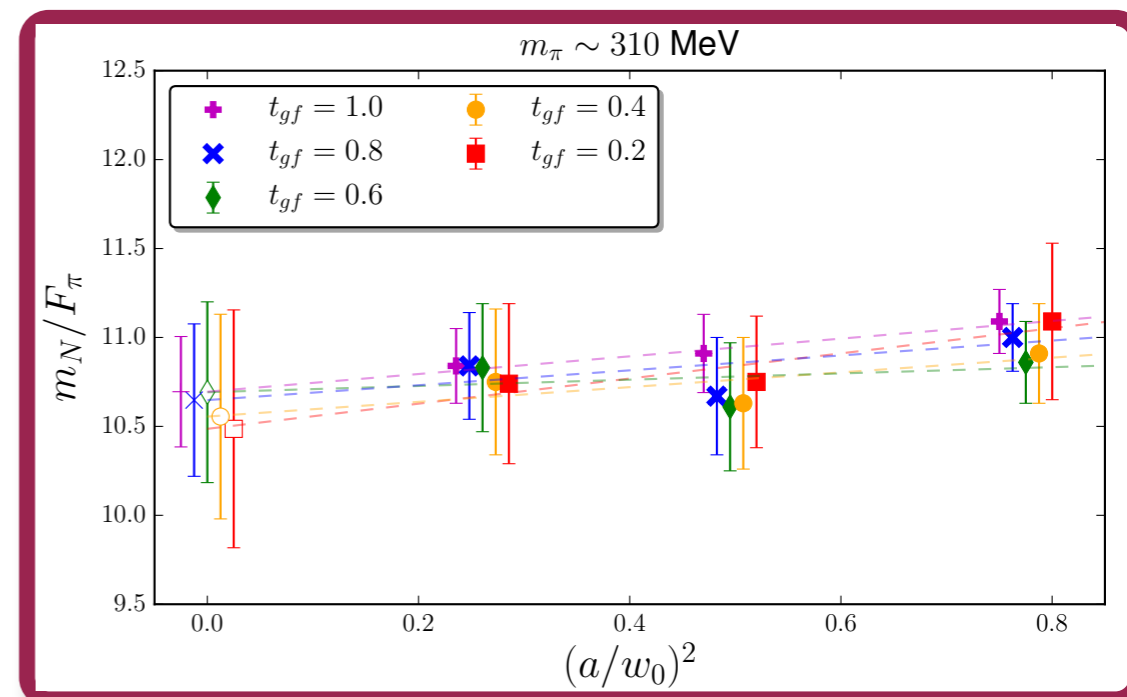
- Gradient flow method for smearing configs

• $m_{\text{res}} < 0.1 m_\ell$ for moderate L_5

Narayanan, Neuberger (2006), Luscher (2010)

• improved statistics

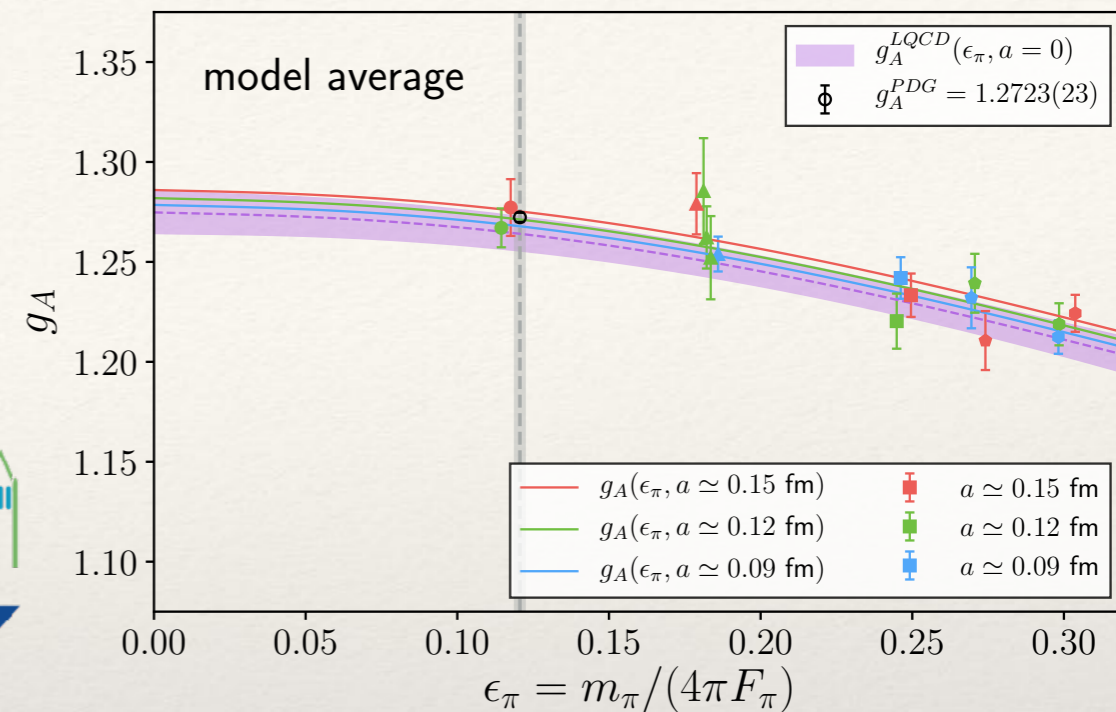
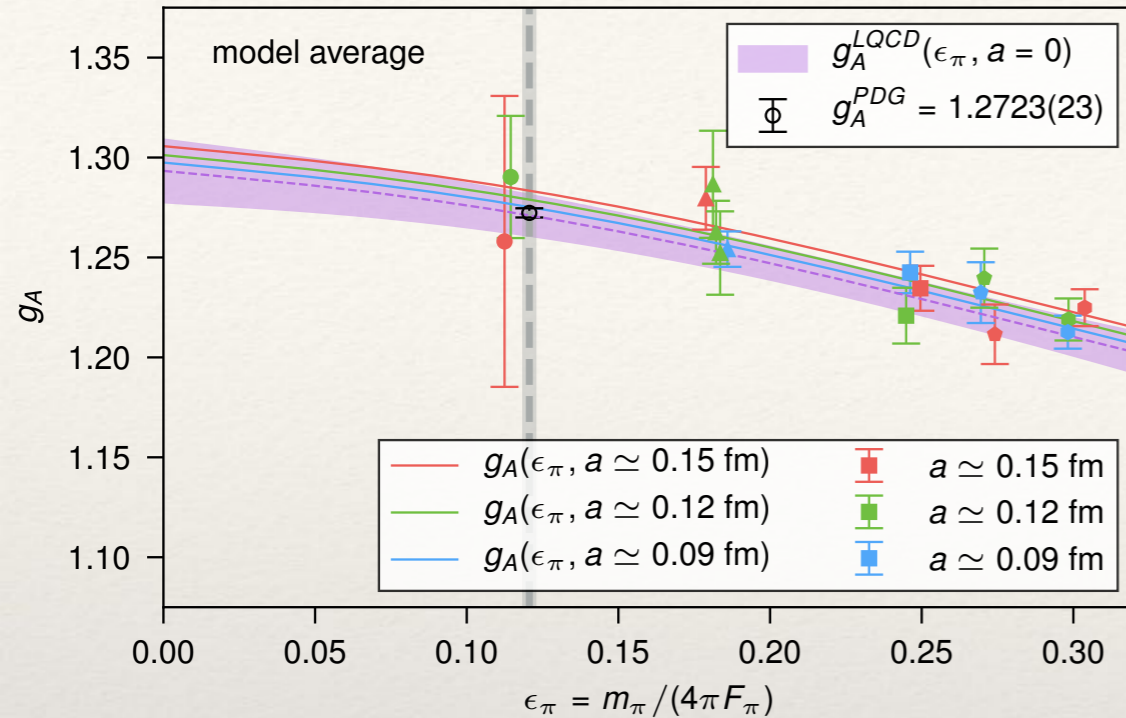
CalLat, Phys.Rev. D96 (2017) no.5, 054513



Nature 558 (2018) no. 7708, 91-94
Chang et al. [arXiv:1805.12130]

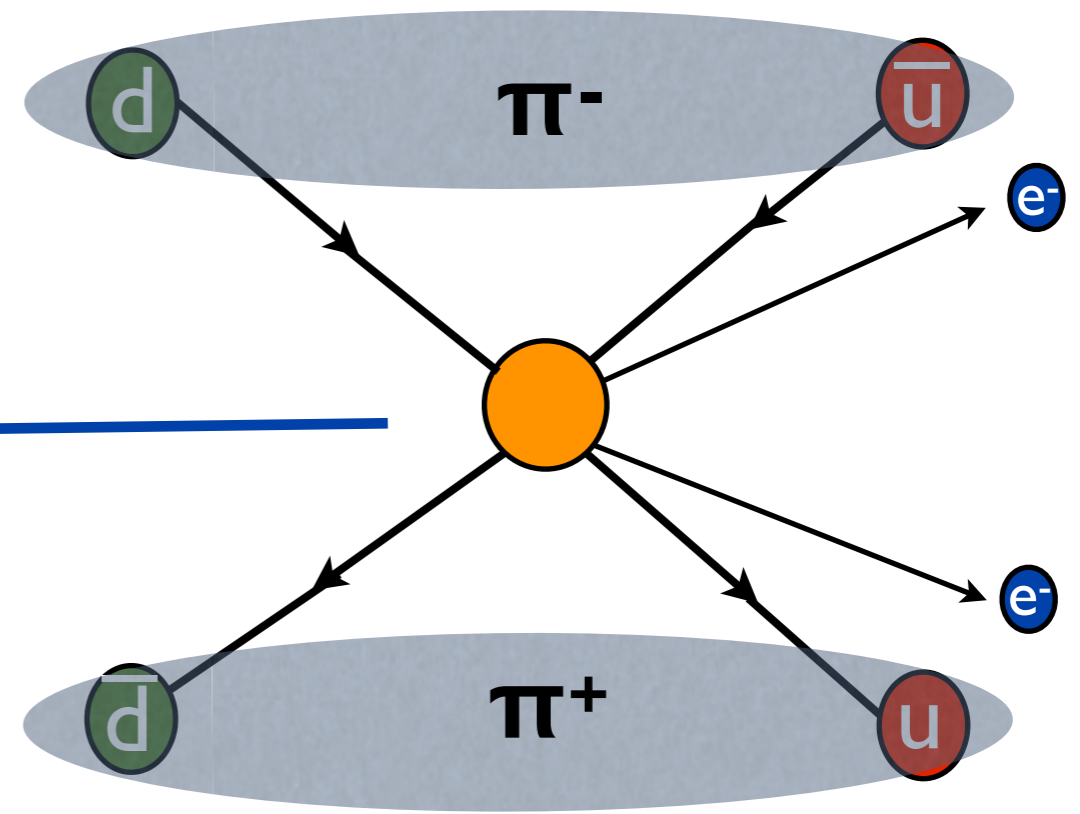
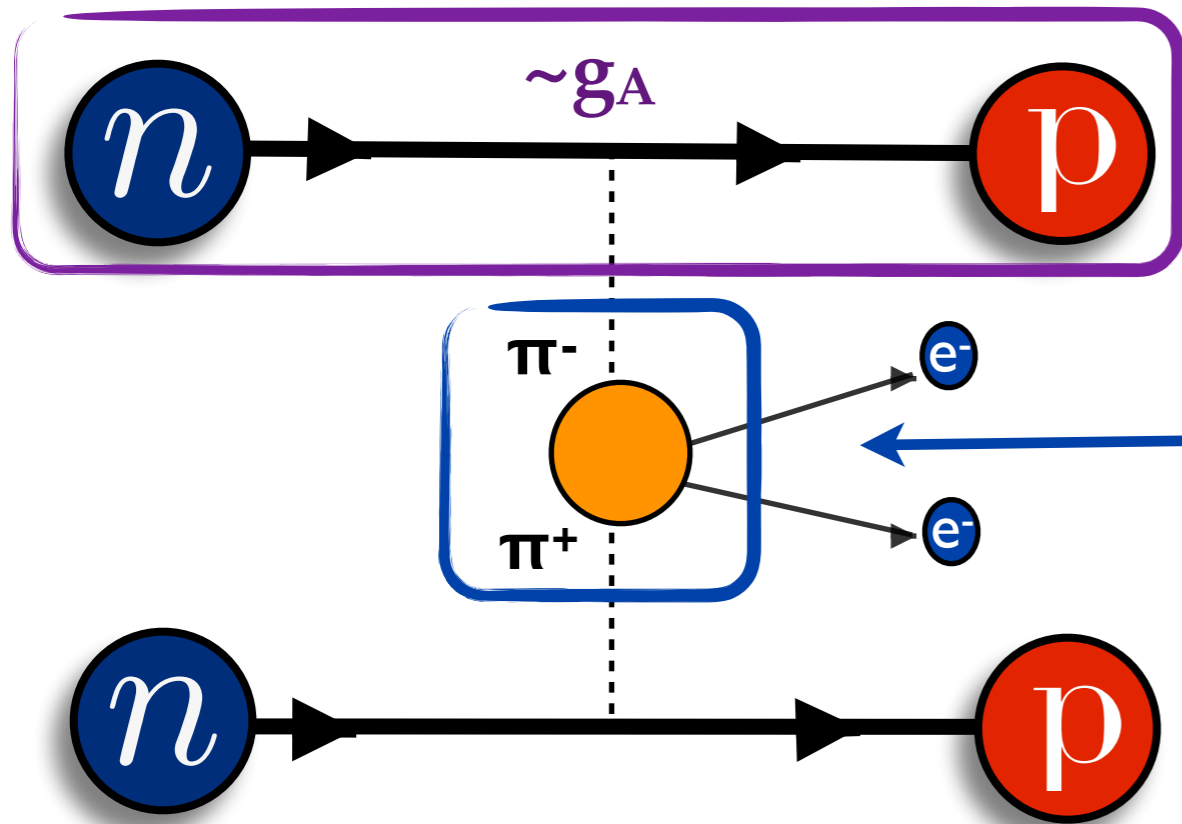
1 year on Titan (ORNL) + 2 years
on GPU machines at LLNL

PRELIMINARY



- The **a12m130** ($48^3 \times 64 \times 20$) with 3 sources cost as much as all other ensembles combined
 - 2.5 weekends on Sierra → 16 srcs
 - Now, 32 srcs (un-constrained, 3-state fit)
- We generated a new **a15m135XL** ($48^3 \times 64$) ensemble (old **a15m130** is $32^3 \times 48$)
 - $M\pi L = 4.93$ (old $M\pi L = 3.2$)
 - $L_5 = 24$, $N_{\text{src}} = 16$
- We are running $g_A(Q^2)$ on Summit this year (DOE INCITE)
 - We anticipate improving g_A to $\sim 0.5\%$

$$g_A = 1.2711(125) \rightarrow 1.2641(93) \quad [0.74\%]$$

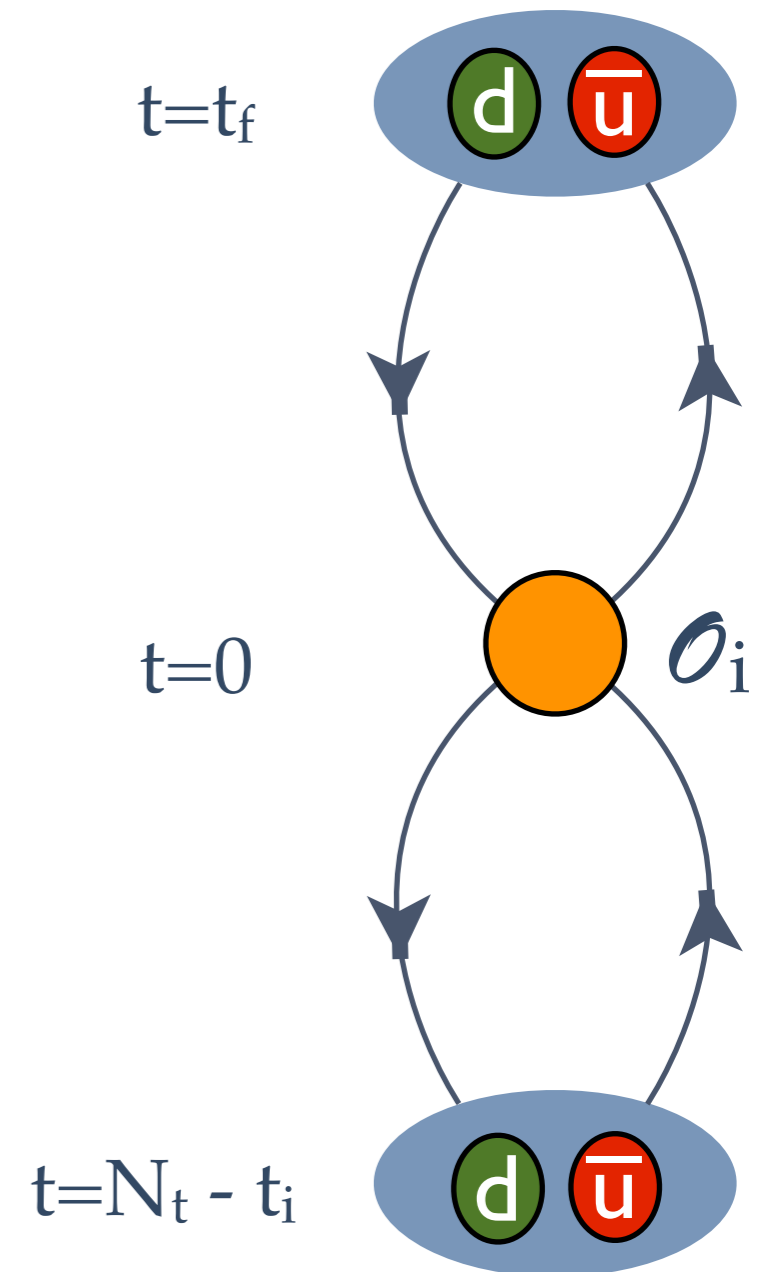


2.

$\pi^- \rightarrow \pi^+$ Transition:
no direct experimental input

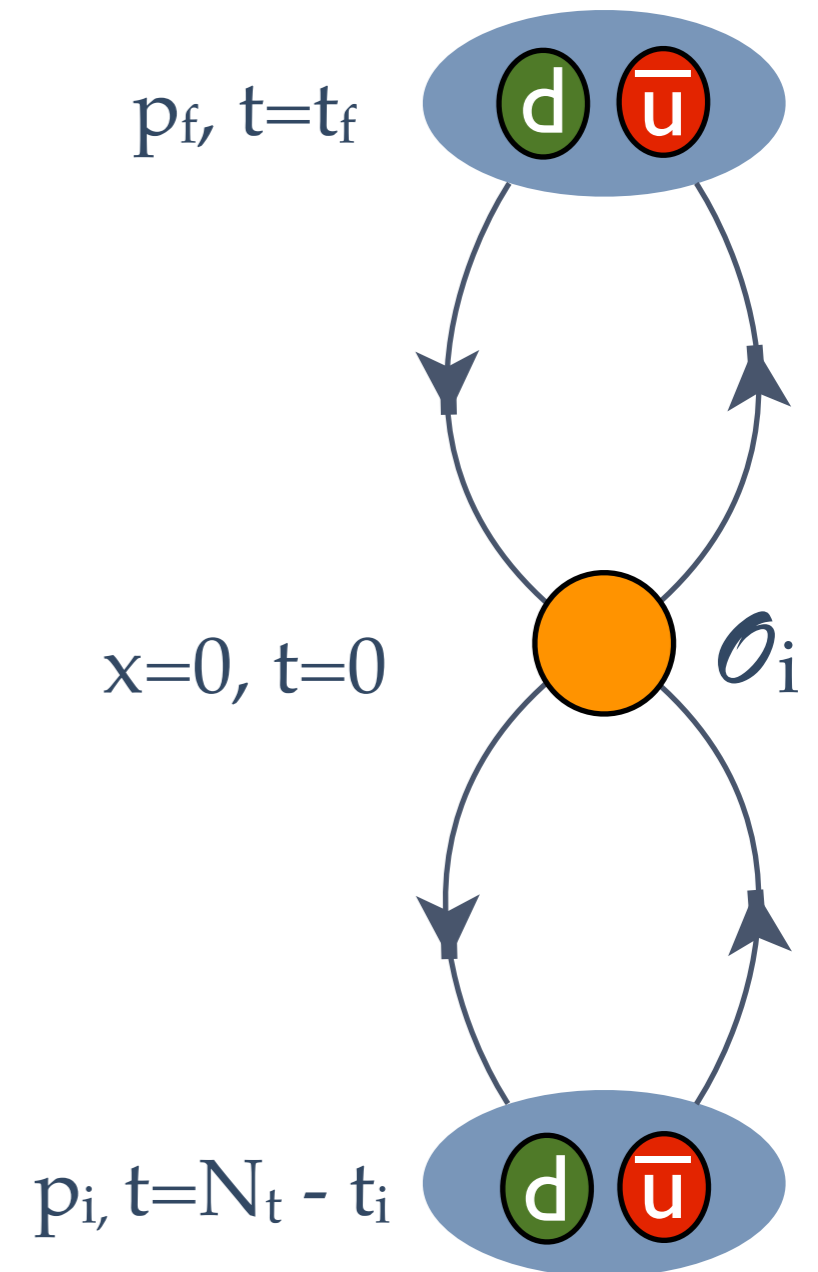
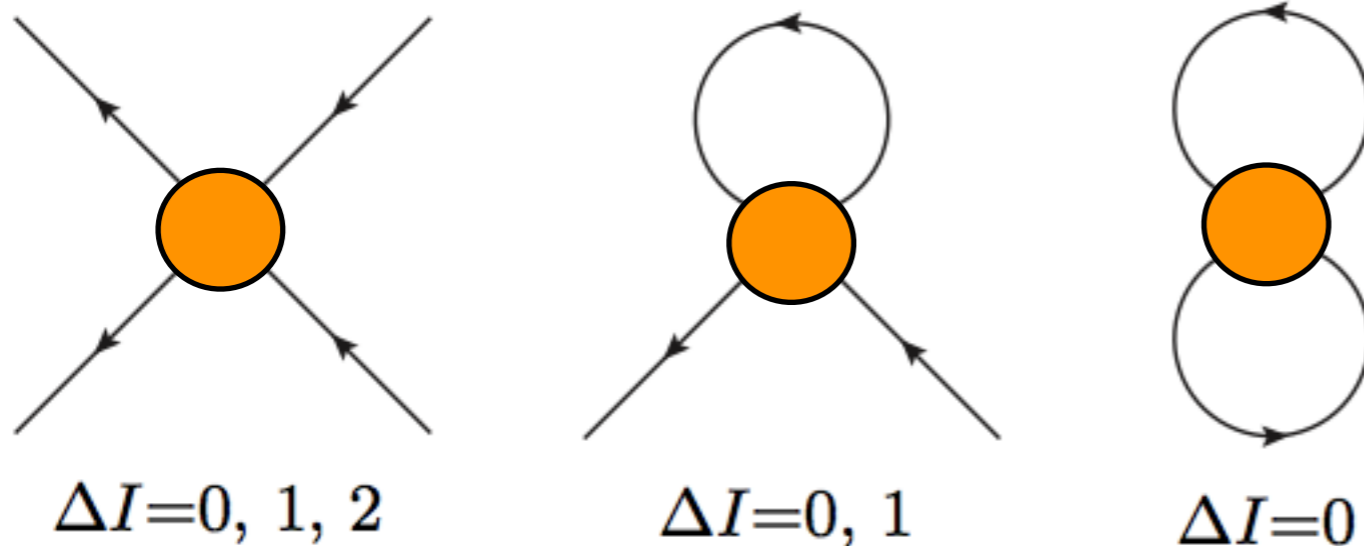
Long-range pion calculation

- Easy to compute pion physics on the lattice!
 - Clean signals
 - Single particle
- No 4-quark FH (yet!), so we'll use standard 3-pt



Long-range pion calculation

- Can perform exact momentum projection at source and sink
- $\Delta I = 2$ no disconnected pieces from operators



XPT:

$0\nu\beta\beta$ -decay ops.	$\mathcal{O}_{1+}^{\pm\pm}$	$\mathcal{O}_{2+}^{\pm\pm}$	$\mathcal{O}_{2-}^{\pm\pm}$	$\mathcal{O}_{3+}^{\pm\pm}$	$\mathcal{O}_{3-}^{\pm\pm}$	$\mathcal{O}_{4+}^{\pm\pm,\mu}$	$\mathcal{O}_{4-}^{\pm\pm,\mu}$	$\mathcal{O}_{5+}^{\pm\pm,\mu}$	$\mathcal{O}_{5-}^{\pm\pm,\mu}$
$\pi\pi ee$ LO	✓	✓	X	X	X	X	X	X	X
$\pi\pi ee$ NNLO	✓	✓	X	✓	X	X	X	X	X
$NN\pi ee$ LO	X	X	✓	X	X	✓	✓	✓	✓
$NN\pi ee$ NLO	X	✓	X	✓	X	✓	✓	✓	✓
$NNNNe e$ LO	✓	✓	X	✓	X	✓	✓	✓	✓

- Nine operators:
 - $\pi \rightarrow \pi$: only need parity even
 - Vector operators suppressed by m_e

$$\mathcal{O}_{1+}^{ab} = (\bar{q}_L \tau^a \gamma^\mu q_L)(\bar{q}_R \tau^b \gamma_\mu q_R),$$

$$\mathcal{O}_{2\pm}^{ab} = (\bar{q}_R \tau^a q_L)(\bar{q}_R \tau^b q_L) \pm (\bar{q}_L \tau^a q_R)(\bar{q}_L \tau^b q_R),$$

$$\mathcal{O}_{3\pm}^{ab} = (\bar{q}_L \tau^a \gamma^\mu q_L)(\bar{q}_L \tau^b \gamma_\mu q_L) \pm (\bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_R \tau^b \gamma_\mu q_R),$$

$$\mathcal{O}_{4\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \mp \bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_L \tau^b q_R - \bar{q}_R \tau^b q_L),$$

$$\mathcal{O}_{5\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \pm \bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_L \tau^b q_R + \bar{q}_R \tau^b q_L).$$

XPT:

$0\nu\beta\beta$ -decay ops.	$\mathcal{O}_{1+}^{\pm\pm}$	$\mathcal{O}_{2+}^{\pm\pm}$	$\mathcal{O}_{2-}^{\pm\pm}$	$\mathcal{O}_{3+}^{\pm\pm}$	$\mathcal{O}_{3-}^{\pm\pm}$	$\mathcal{O}_{4+}^{\pm\pm,\mu}$	$\mathcal{O}_{4-}^{\pm\pm,\mu}$	$\mathcal{O}_{5+}^{\pm\pm,\mu}$	$\mathcal{O}_{5-}^{\pm\pm,\mu}$
$\pi\pi ee$ LO	✓	✓	X	X	X	X	X	X	X
$\pi\pi ee$ NNLO	✓	✓	X	✓	X	X	X	X	X
$NN\pi ee$ LO	X	X	✓	X	X	✓	✓	✓	✓
$NN\pi ee$ NLO	X	✓	X	✓	X	✓	✓	✓	✓
$NNNNe e$ LO	✓	✓	X	✓	X	✓	✓	✓	✓

- Nine operators:
 - $\pi \rightarrow \pi$: only need parity even
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$$\mathcal{O}_{2\pm}^{ab} = (\bar{q}_R \tau^a q_L)(\bar{q}_R \tau^b q_L) \pm (\bar{q}_L \tau^a q_R)(\bar{q}_L \tau^b q_R),$$

$$\mathcal{O}_{3\pm}^{ab} = (\bar{q}_L \tau^a \gamma^\mu q_L)(\bar{q}_L \tau^b \gamma_\mu q_L) \pm (\bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_R \tau^b \gamma_\mu q_R),$$

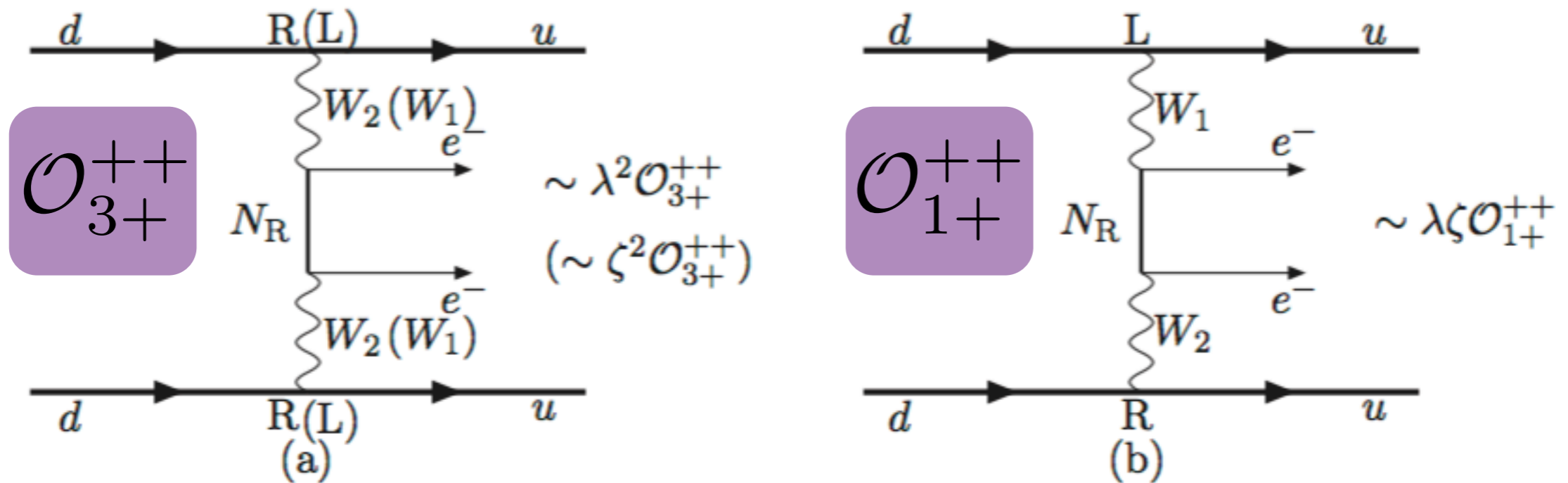
$$\mathcal{O}_{4\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \mp \bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_L \tau^b q_R \mp \bar{q}_R \tau^b q_L),$$

$$\mathcal{O}_{5\pm}^{ab,\mu} = (\bar{q}_L \tau^a \gamma^\mu q_L \pm \bar{q}_R \tau^a \gamma^\mu q_R)(\bar{q}_L \tau^b q_R + \bar{q}_R \tau^b q_L).$$

XPT:

$0\nu\beta\beta$ -decay ops.	$\mathcal{O}_{1+}^{\pm\pm}$	$\mathcal{O}_{2+}^{\pm\pm}$	$\mathcal{O}_{2-}^{\pm\pm}$	$\mathcal{O}_{3+}^{\pm\pm}$	$\mathcal{O}_{3-}^{\pm\pm}$	$\mathcal{O}_{4+}^{\pm\pm,\mu}$	$\mathcal{O}_{4-}^{\pm\pm,\mu}$	$\mathcal{O}_{5+}^{\pm\pm,\mu}$	$\mathcal{O}_{5-}^{\pm\pm,\mu}$
$\pi\pi ee$ LO	✓	✓	X	X	X	X	X	X	X
$\pi\pi ee$ NNLO	✓	✓	X	✓	X	X	X	X	X
$NN\pi ee$ LO	X	X	✓	X	X	✓	✓	✓	✓
$NN\pi ee$ NLO	X	✓	X	✓	X	✓	✓	✓	✓
$NNNN ee$ LO	✓	✓	X	✓	X	✓	✓	✓	✓

Left-right symmetric models



Contractions

- QCD interactions can mix colors below the electroweak scale
- Must add color mixed versions of Prezeau, Ramsey-Musolf, Vogel ops 1&2

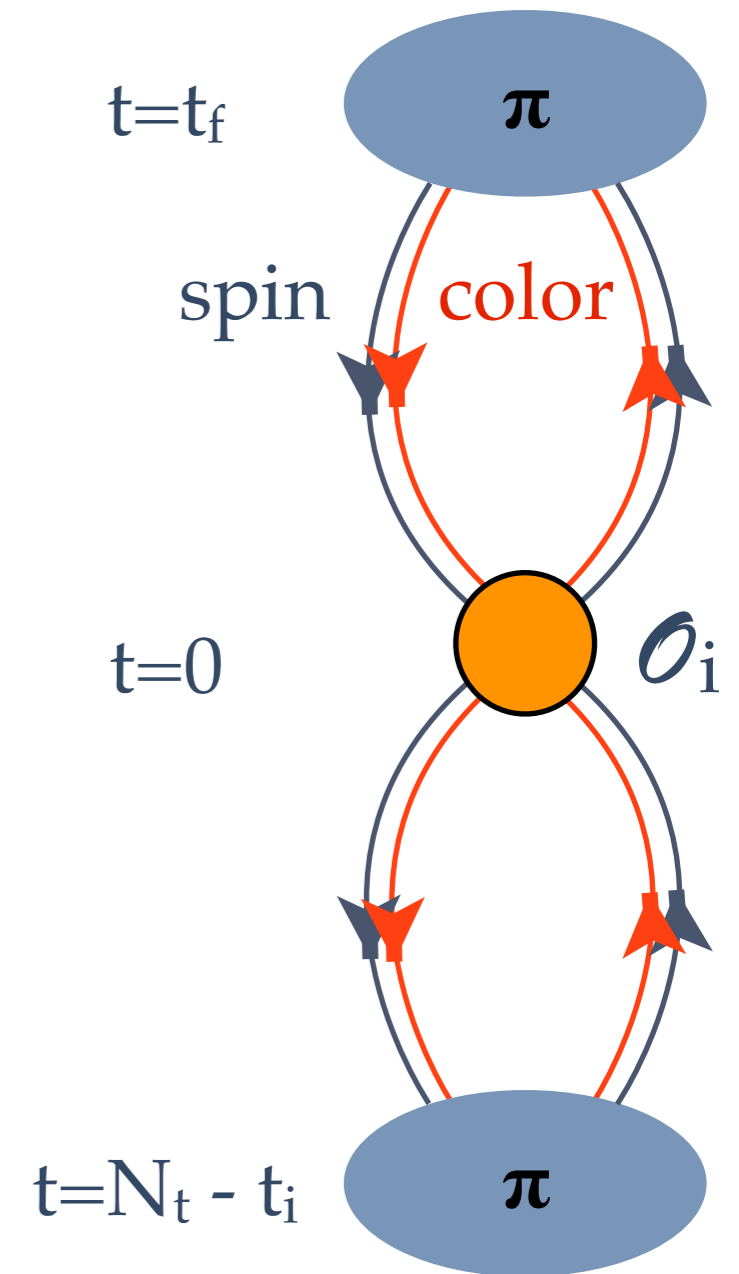
$$\mathcal{O}_{1+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_R \tau^- \gamma_\mu q_R]$$

$$\mathcal{O}'_{1+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_R \tau^- \gamma_\mu q_R]$$

$$\mathcal{O}_{2+}^{++} = (\bar{q}_R \tau^- q_L) [\bar{q}_R \tau^- q_L] + (\bar{q}_L \tau^- q_R) [\bar{q}_L \tau^- q_R]$$

$$\mathcal{O}'_{2+}^{++} = (\bar{q}_R \tau^- q_L) [\bar{q}_R \tau^- q_L] + (\bar{q}_L \tau^- q_R) [\bar{q}_L \tau^- q_R]$$

$$\mathcal{O}_{3+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_L \tau^- \gamma_\mu q_L] + (\bar{q}_R \tau^- \gamma^\mu q_R) [\bar{q}_R \tau^- \gamma_\mu q_R]$$



Contractions

- QCD interactions can mix colors below the electroweak scale
- Must add color mixed versions of Prezeau, Ramsey-Musolf, Vogel ops 1&2

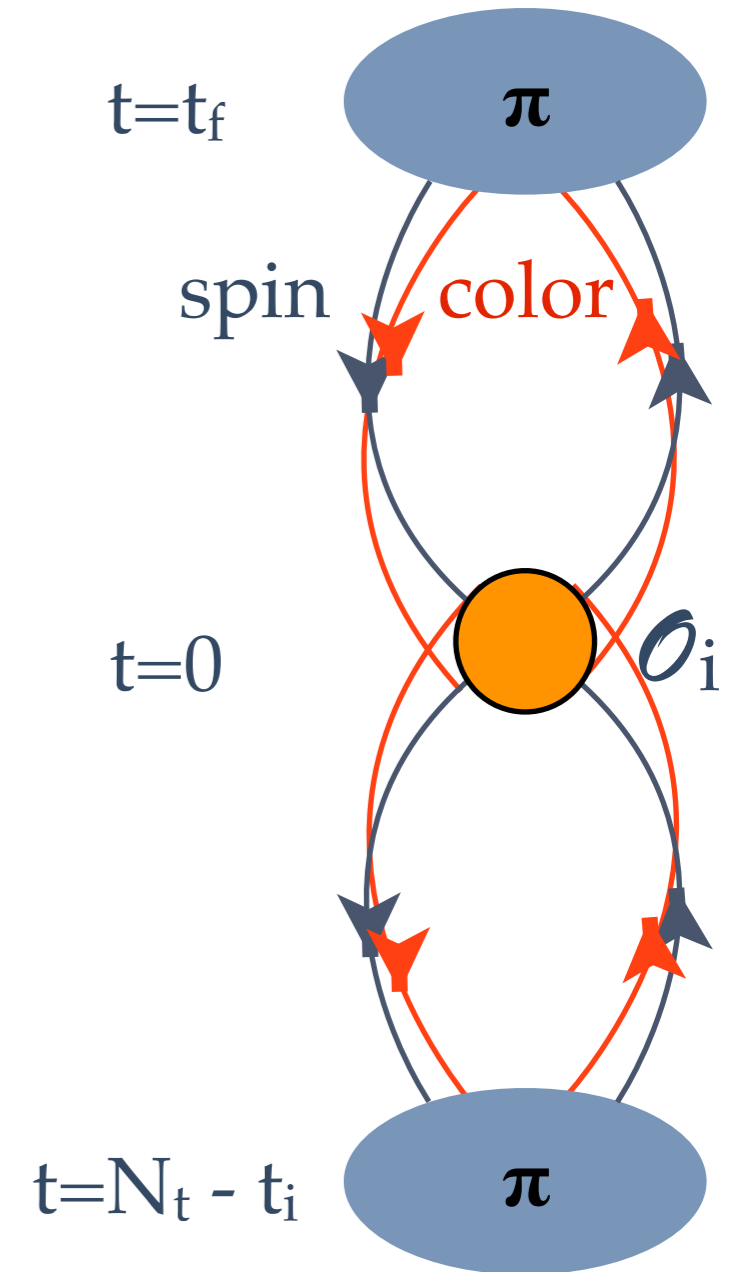
$$\mathcal{O}_{1+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_R \tau^- \gamma_\mu q_R]$$

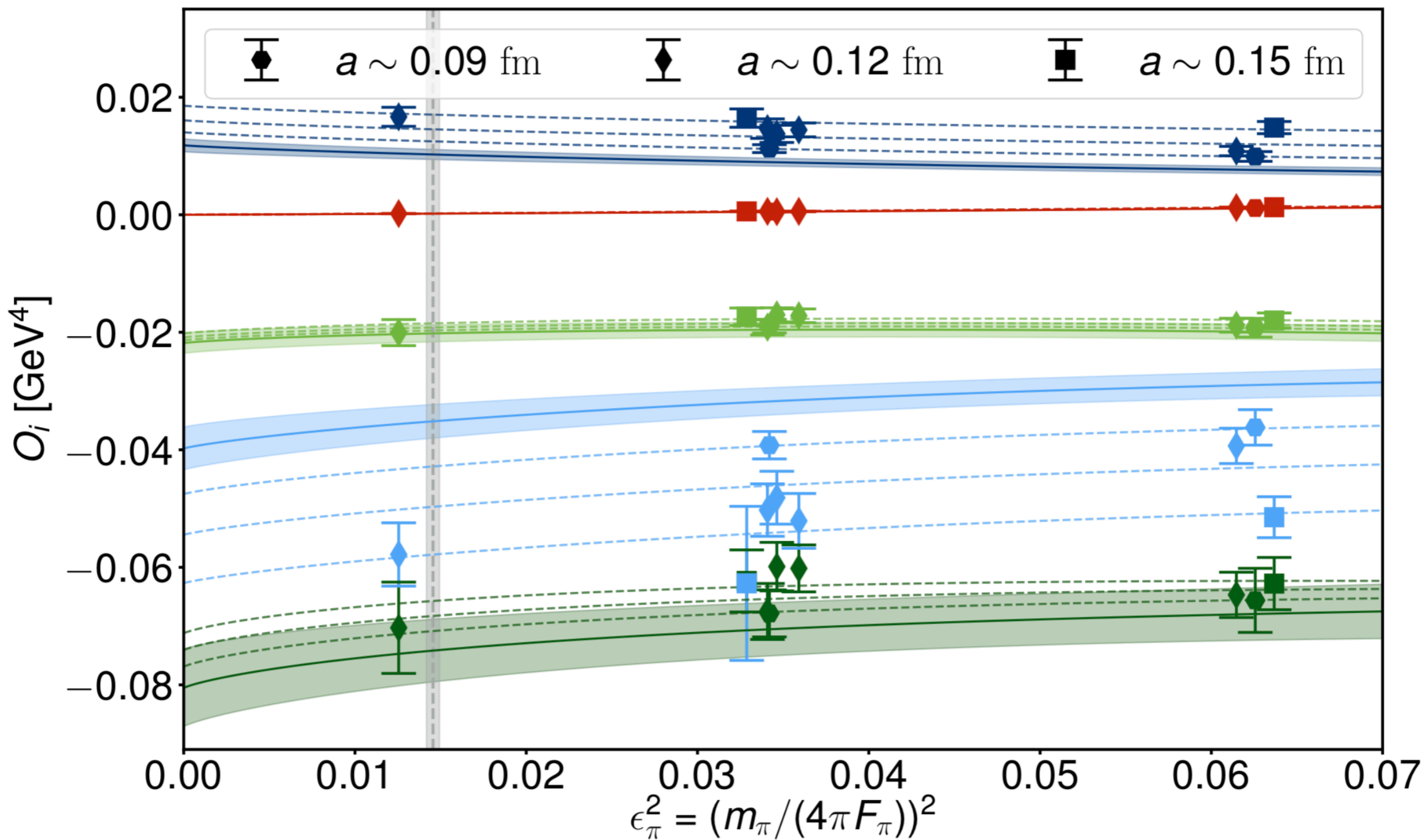
$$\mathcal{O}'_{1+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_R \tau^- \gamma_\mu q_R]$$

$$\mathcal{O}_{2+}^{++} = (\bar{q}_R \tau^- q_L) [\bar{q}_R \tau^- q_L] + (\bar{q}_L \tau^- q_R) [\bar{q}_L \tau^- q_R]$$

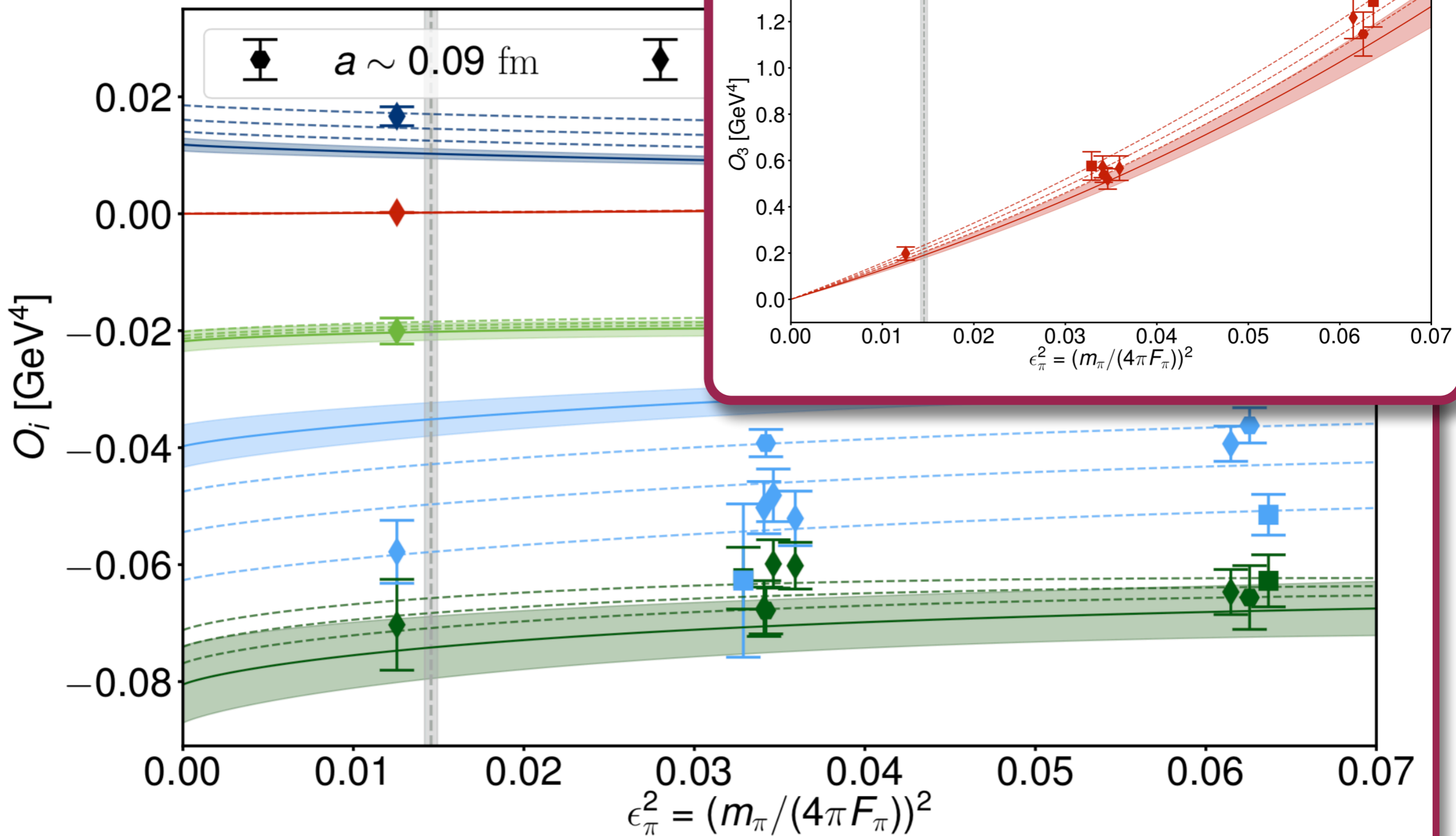
$$\mathcal{O}'_{2+}^{++} = (\bar{q}_R \tau^- q_L) [\bar{q}_R \tau^- q_L] + (\bar{q}_L \tau^- q_R) [\bar{q}_L \tau^- q_R]$$

$$\mathcal{O}_{3+}^{++} = (\bar{q}_L \tau^- \gamma^\mu q_L) [\bar{q}_L \tau^- \gamma_\mu q_L] + (\bar{q}_R \tau^- \gamma^\mu q_R) [\bar{q}_R \tau^- \gamma_\mu q_R]$$

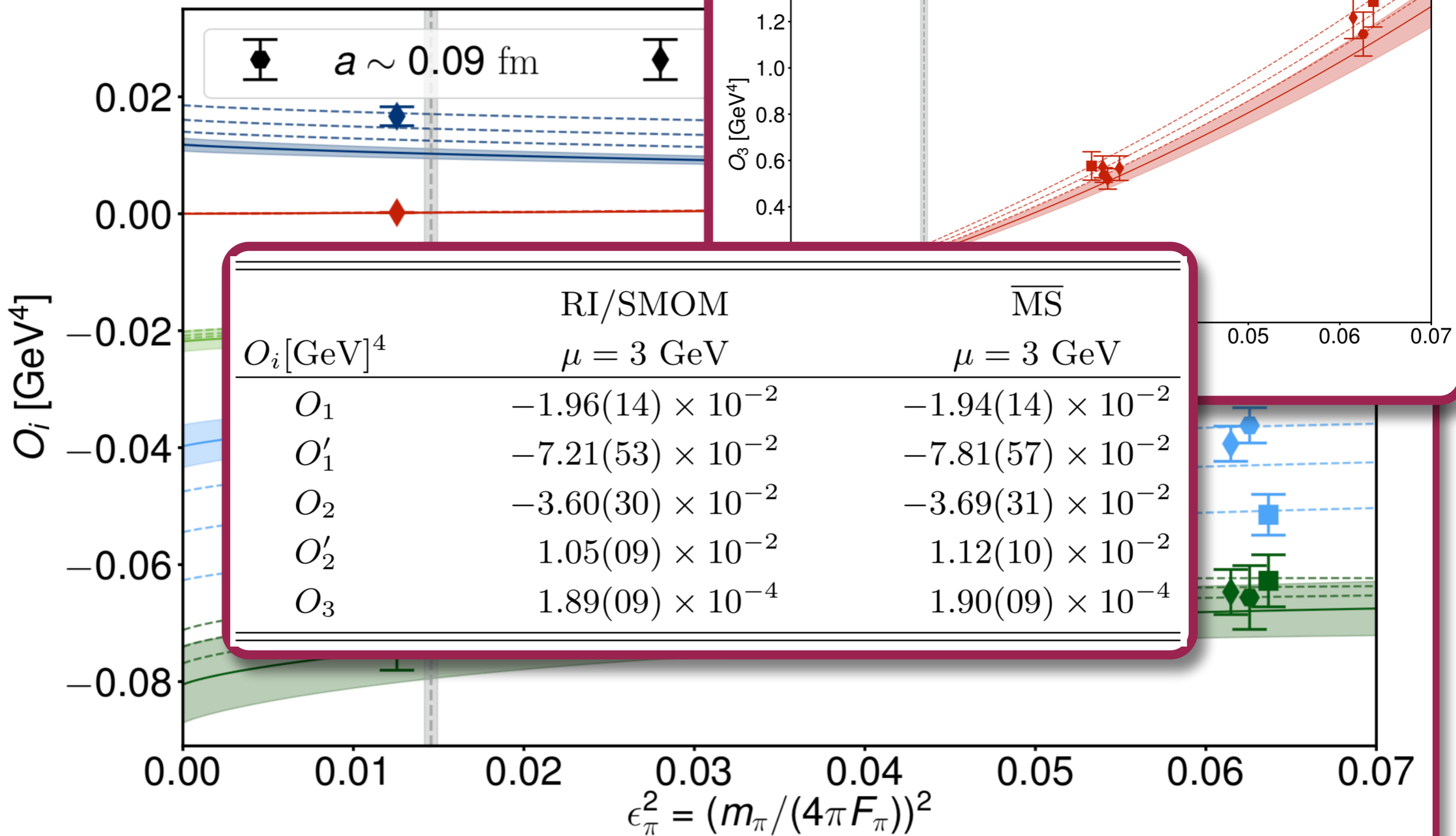




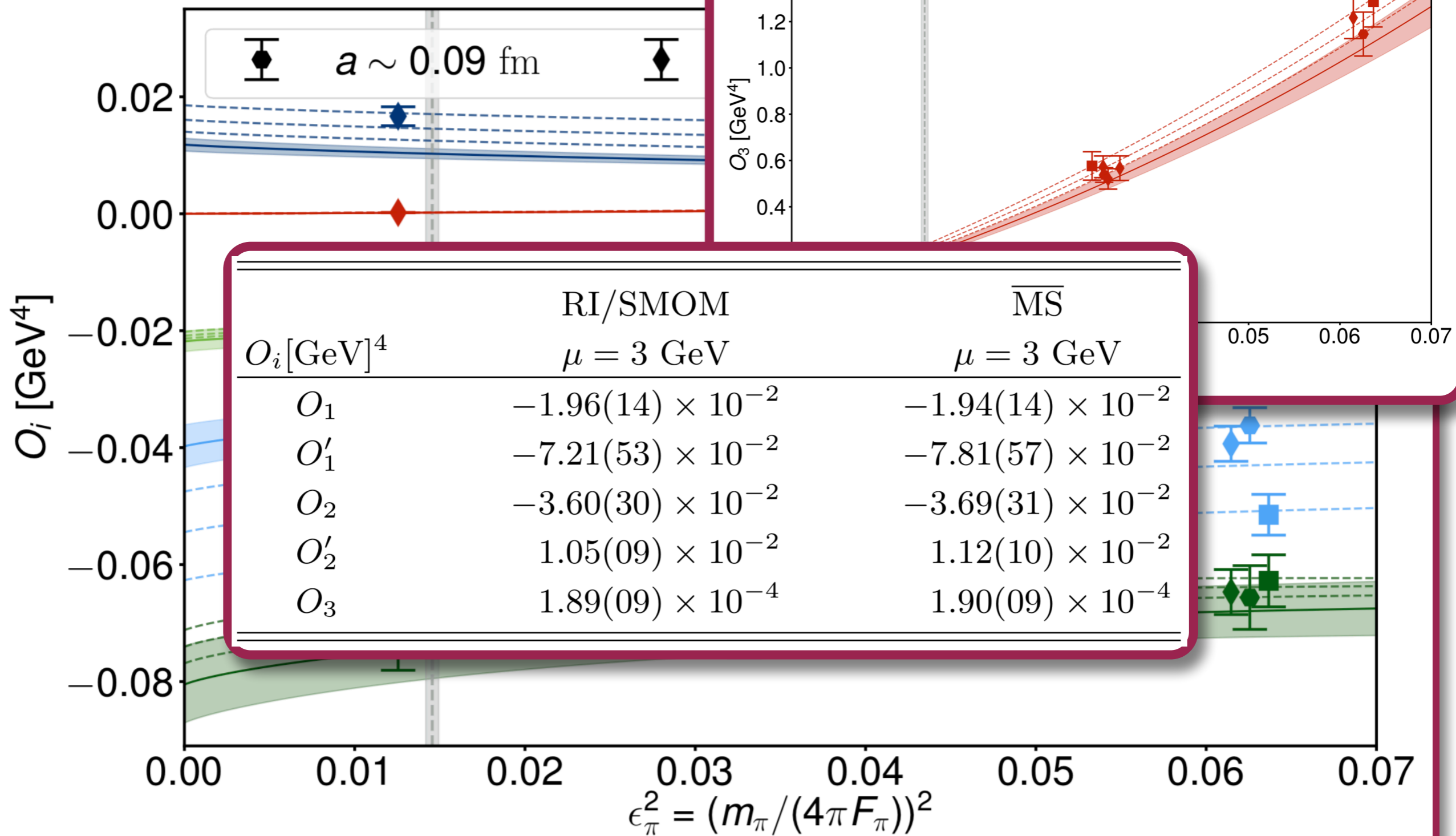
A.N., E. Berkowitz, H. Monge-Camacho, D. Brantley, N. Garron,
 C. C. Chang, E. Rinaldi, M. A. Clark, B. Joo, T. Kurth, B. Tiburzi,
 P. Vranas, A. Walker-Loud, PRL 121 (2018) no.17, 172501



A.N., E. Berkowitz, H. Monge-Camacho, D. Brantley, N. Garron,
 C. C. Chang, E. Rinaldi, M. A. Clark, B. Joo, T. Kurth, B. Tiburzi,
 P. Vranas, A. Walker-Loud, PRL 121 (2018) no.17, 172501



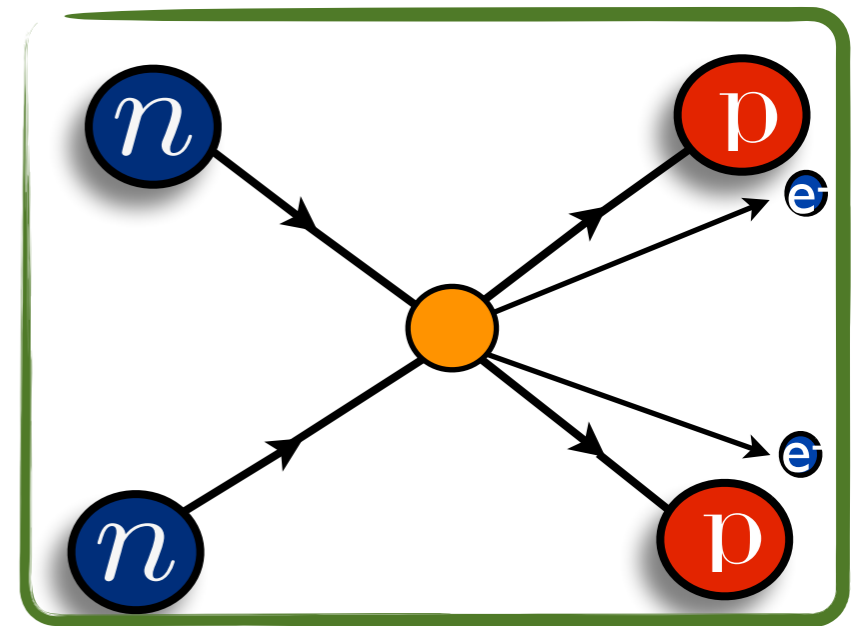
A.N., E. Berkowitz, H. Monge-Camacho, D. Brantley, N. Garron,
 C. C. Chang, E. Rinaldi, M. A. Clark, B. Joo, T. Kurth, B. Tiburzi,
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A.N., E. Berkowitz, H. Monge-Camacho, D. Brantley, N. Garron,
C. C. Chang, E. Rinaldi, M. A. Clark, B. Joo, T. Kurth, B. Tiburzi,
P. Vranas, A. Walker-Loud, PRL 121 (2018) no.17, 172501

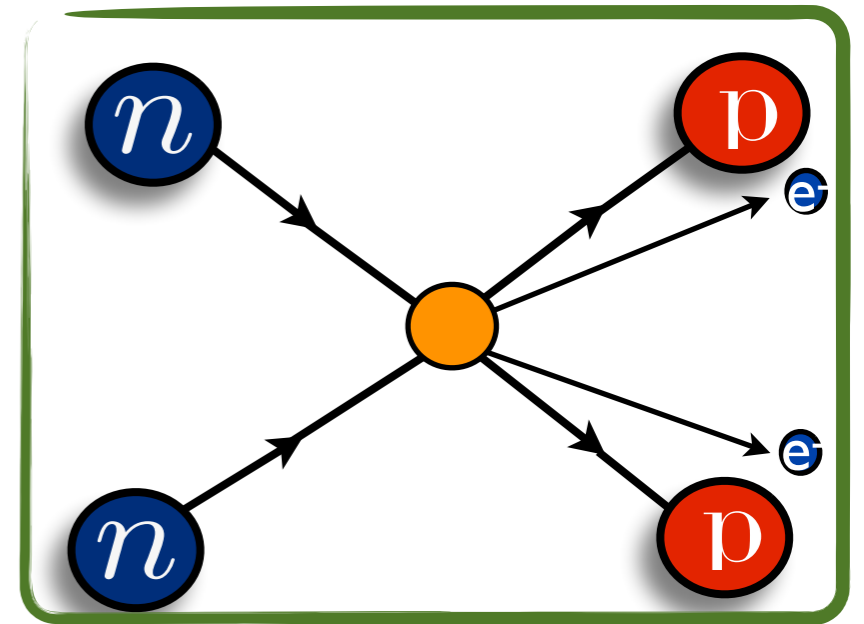
Agrees to 2σ with:
V. Cirigliano, W. Dekens, M. Graesser, E. Mereghetti
Phys.Lett. B769 (2017) 460-464

Full $nn \rightarrow pp$ transition

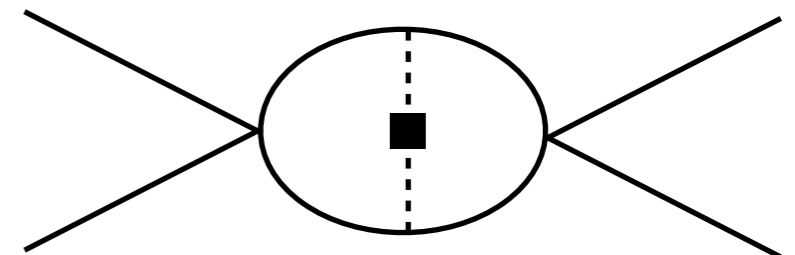
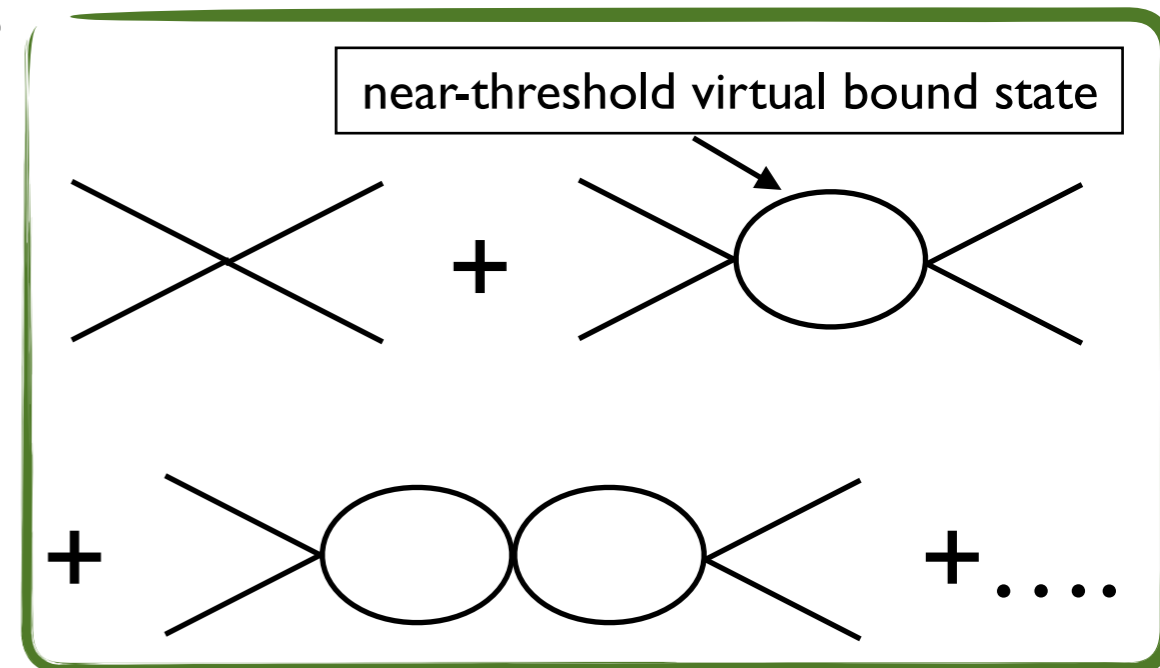


Full $nn \rightarrow pp$ transition

- Why calculate it?
 - Higher contributions formally NNLO (Weinberg counting)
 - Nuclear matrix elements currently have $\sim 100\%$ uncertainties
- The spin singlet channel is finely-tuned, leading to issues with Weinberg counting
- LO contribution vanishes for some BSM models
- Contact operator for standard double beta decay found to be important at heavy pion mass (NPLQCD '17)

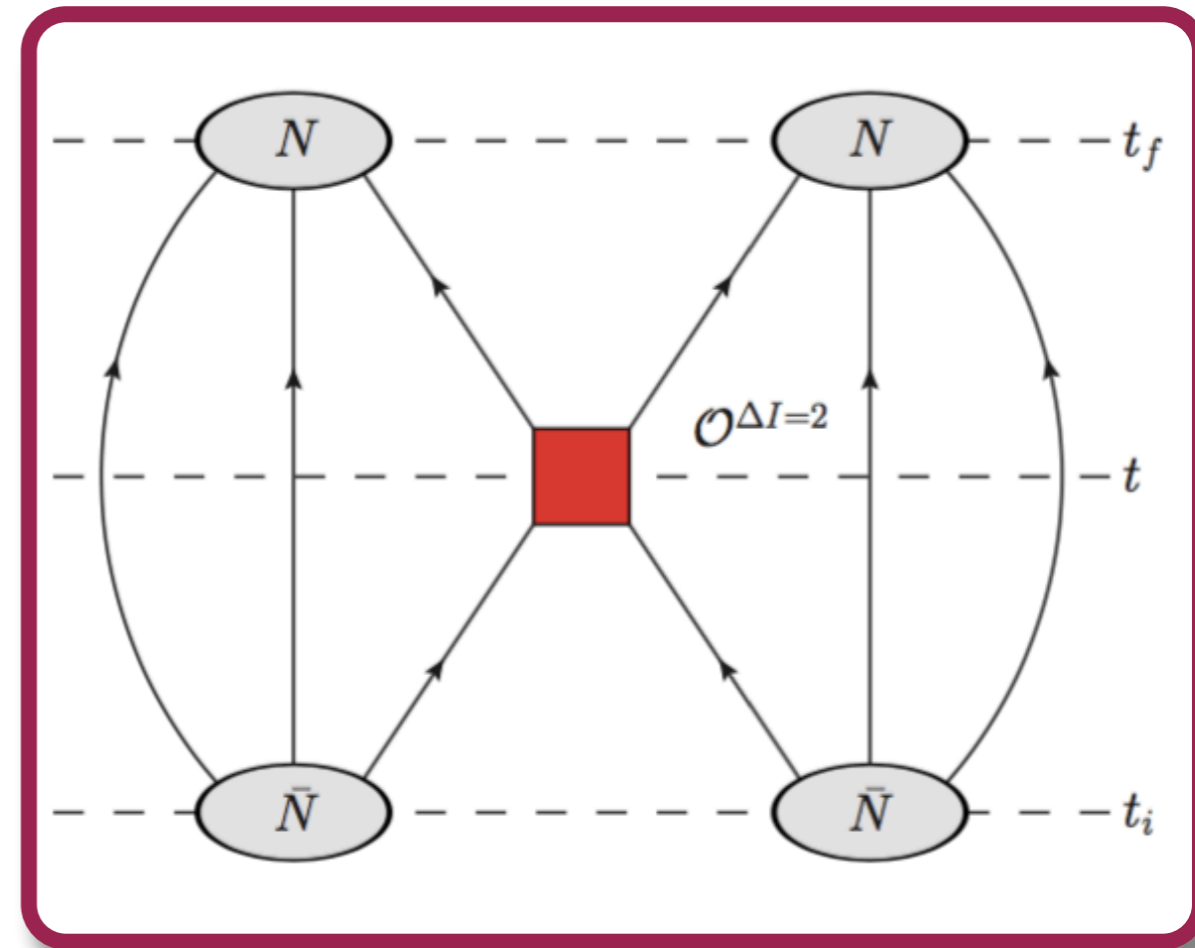


Cirigliano, V., Dekens, W.,
de Vries, J., Mereghetti, E., Graesser,
M., Pastore, S., van Kolck, U
arXiv:1802.10097



Full $nn \rightarrow pp$ transition

- Isospin limit: 576 contractions
Doi & Endres, Originos et. al., Günther et. al.
- Baryon signal-to-noise problem, small excited state energy splittings,
- Cannot fix all momenta
 - otherwise all-to-all propagators connect to 4-quark operator
 - stochastically project onto zero total momentum
- Need phase shifts to connect to infinite volume

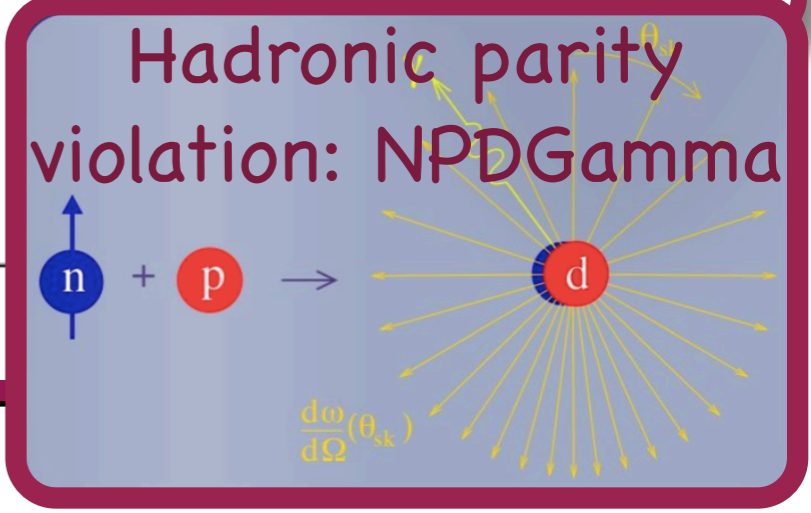
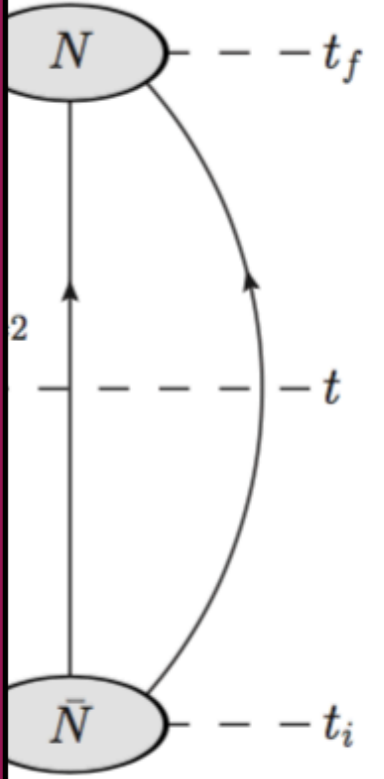
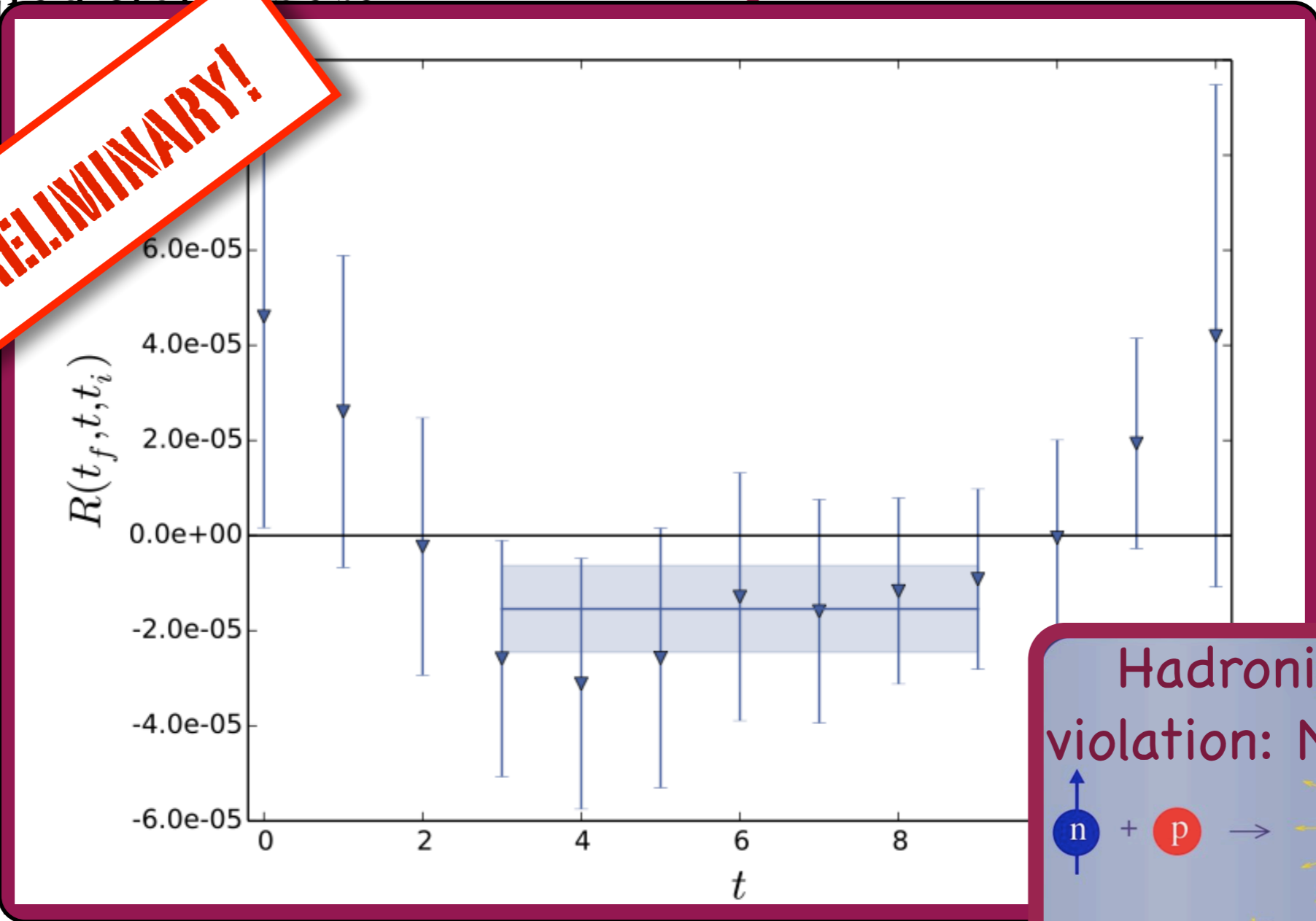


Full $nn \rightarrow p$ transition

Difficult, but not impossible!

- Isospin limit: 576 channels (Doi & Endres, Originos et. al.)
 - Baryon signal-to-noise ratio small excitation splittings
 - Cannot connect
 - other connect
 - stochastic moment
 - Need phase infinite volume
- R. Briceño, M.

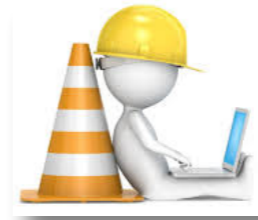
PRELIMINARY!



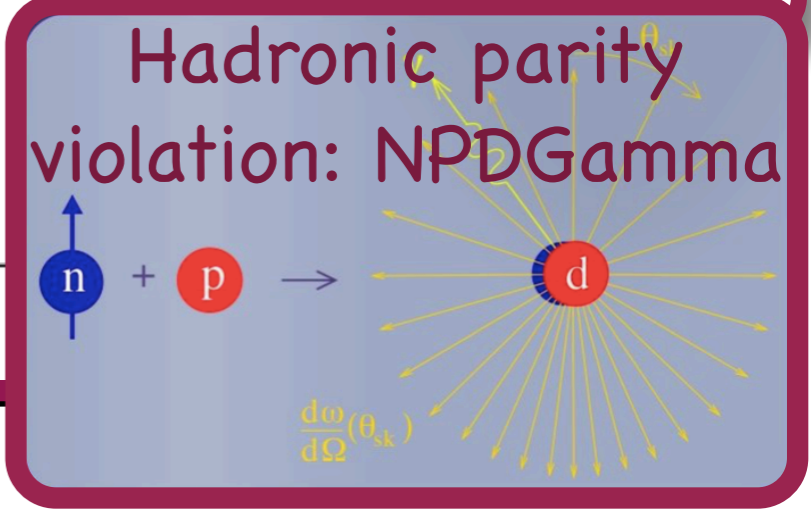
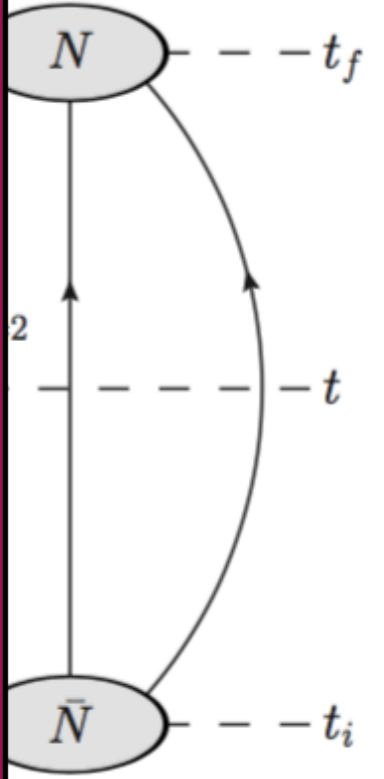
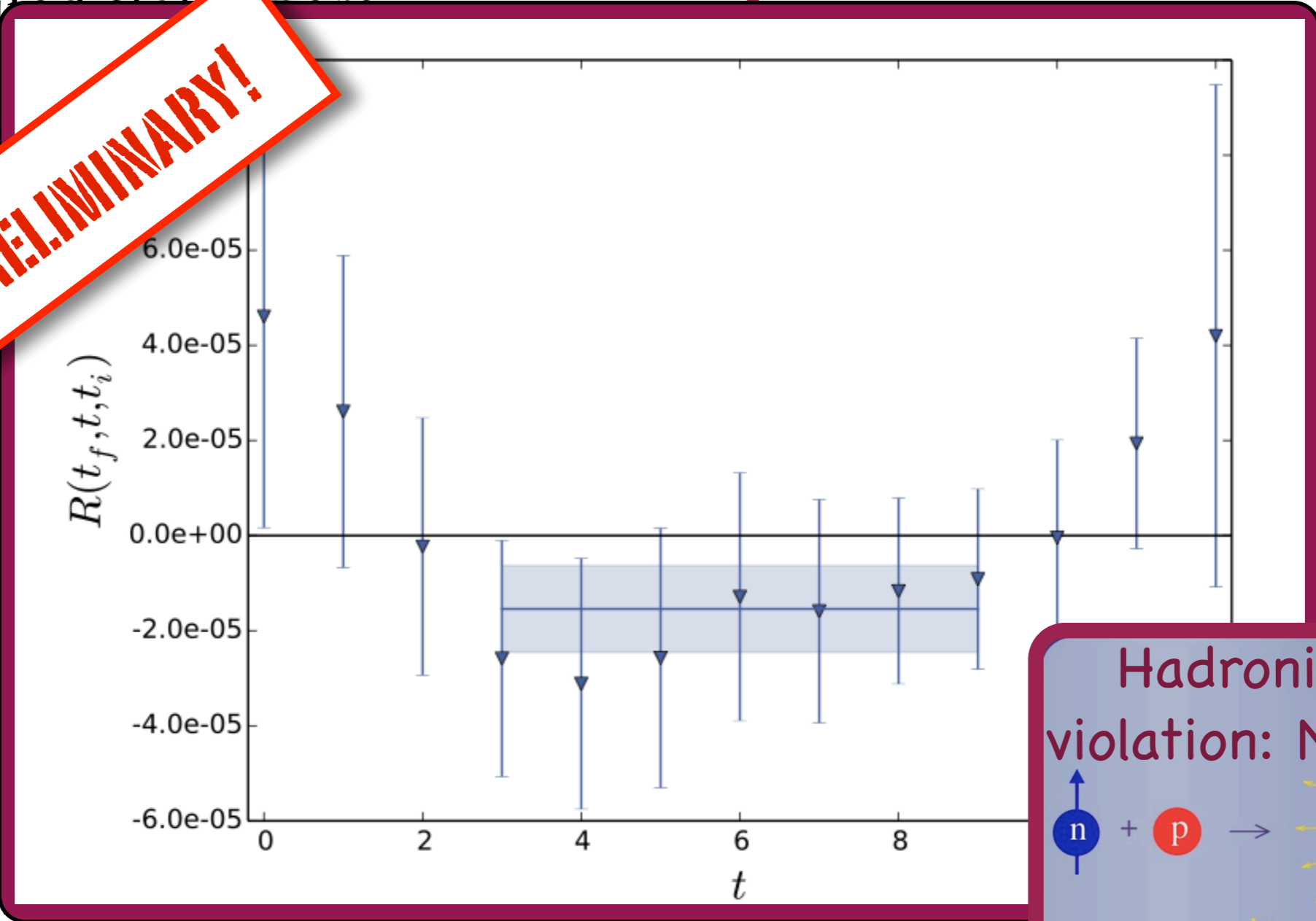
Full $nn \rightarrow p$ transition

- Isospin limit: 576 channels
Doi & Endres, Originos et. al.
 - Baryon signal-to-noise ratio
small excitations
splittings
 - Cannot
 - other
 - connect
 - stochastic
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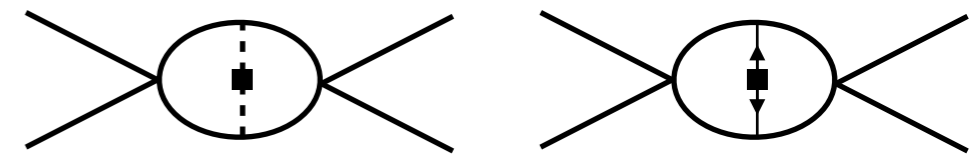
Difficult, but not impossible!
4-quark FH?
(Monge-Camacho Lattice 2018)



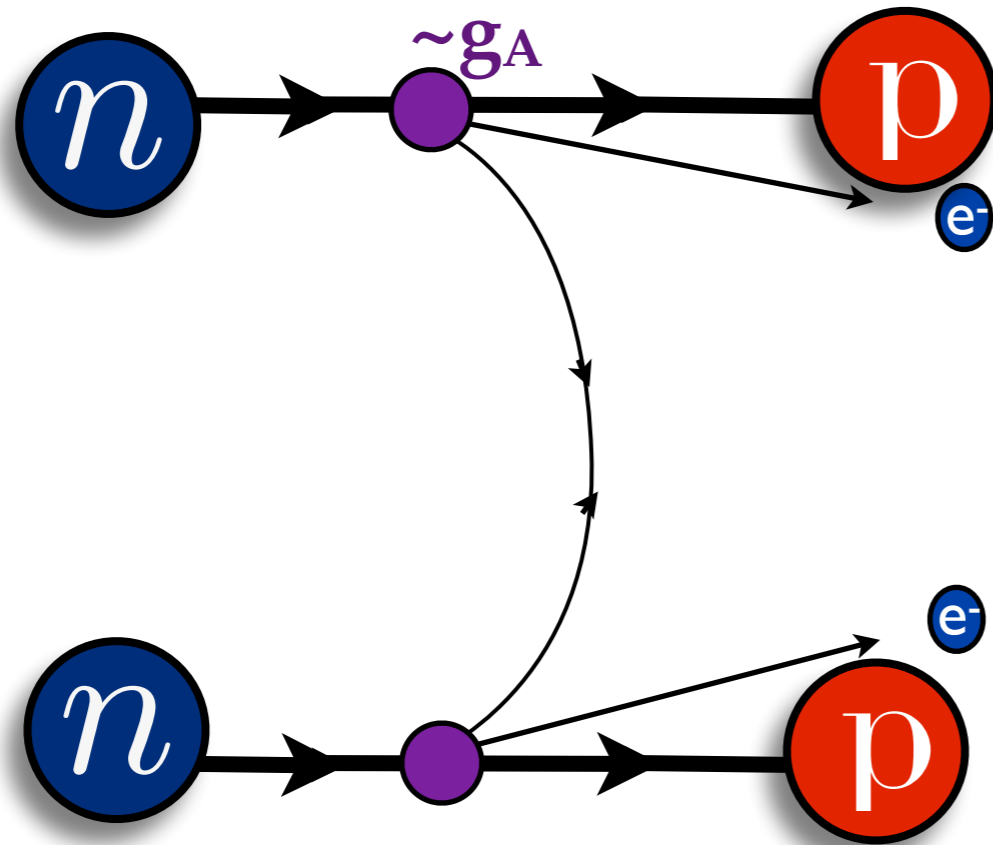
PRELIMINARY!



Full $nn \rightarrow pp$ transition

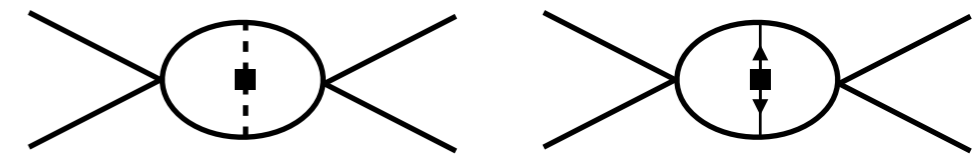


Cirigliano, V., Dekens, W., de Vries, J., Mereghetti, E., Graesser, M., Pastore, S., van Kolck, U
arXiv:1802.10097



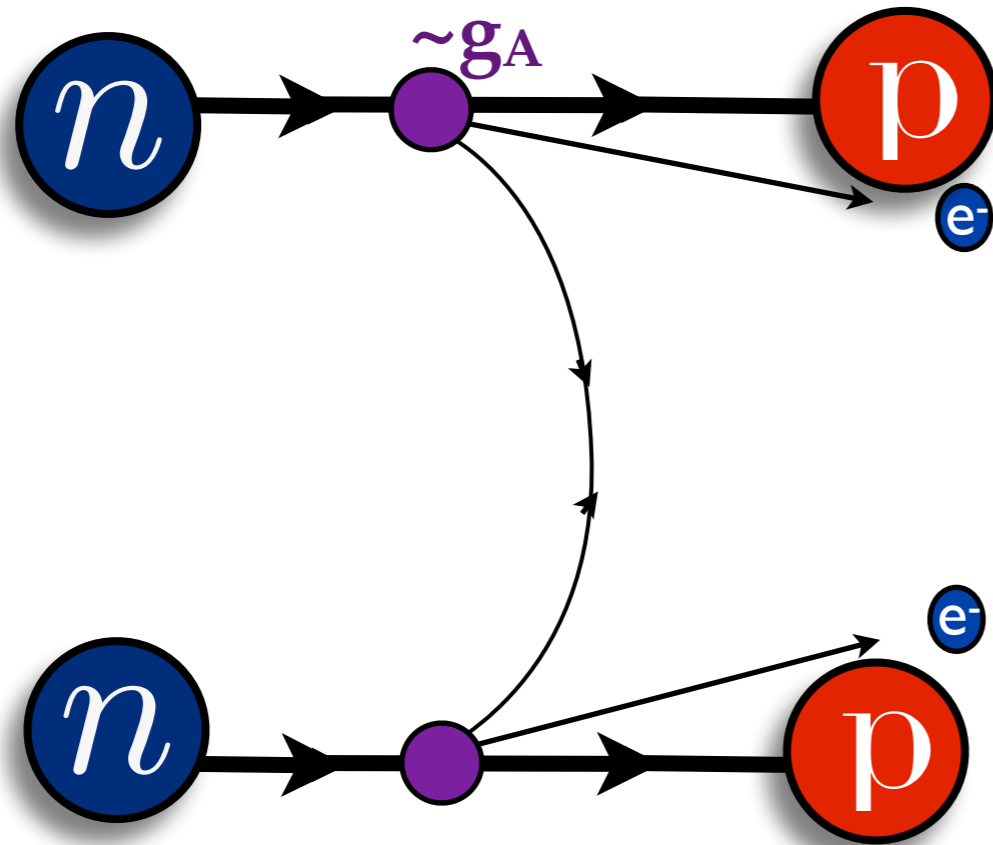
Long-range

Full $nn \rightarrow pp$ transition



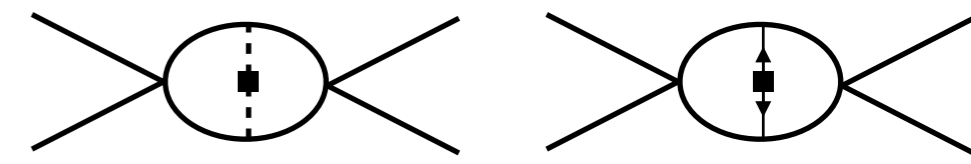
Cirigliano, V., Dekens, W., de Vries, J., Mereghetti, E., Graesser, M., Pastore, S., van Kolck, U
arXiv:1802.10097

- Work has begun to calculate full transition for light neutrino mechanism
- Why? Just as in short-range operator case, EFT may not be reliable



Long-range

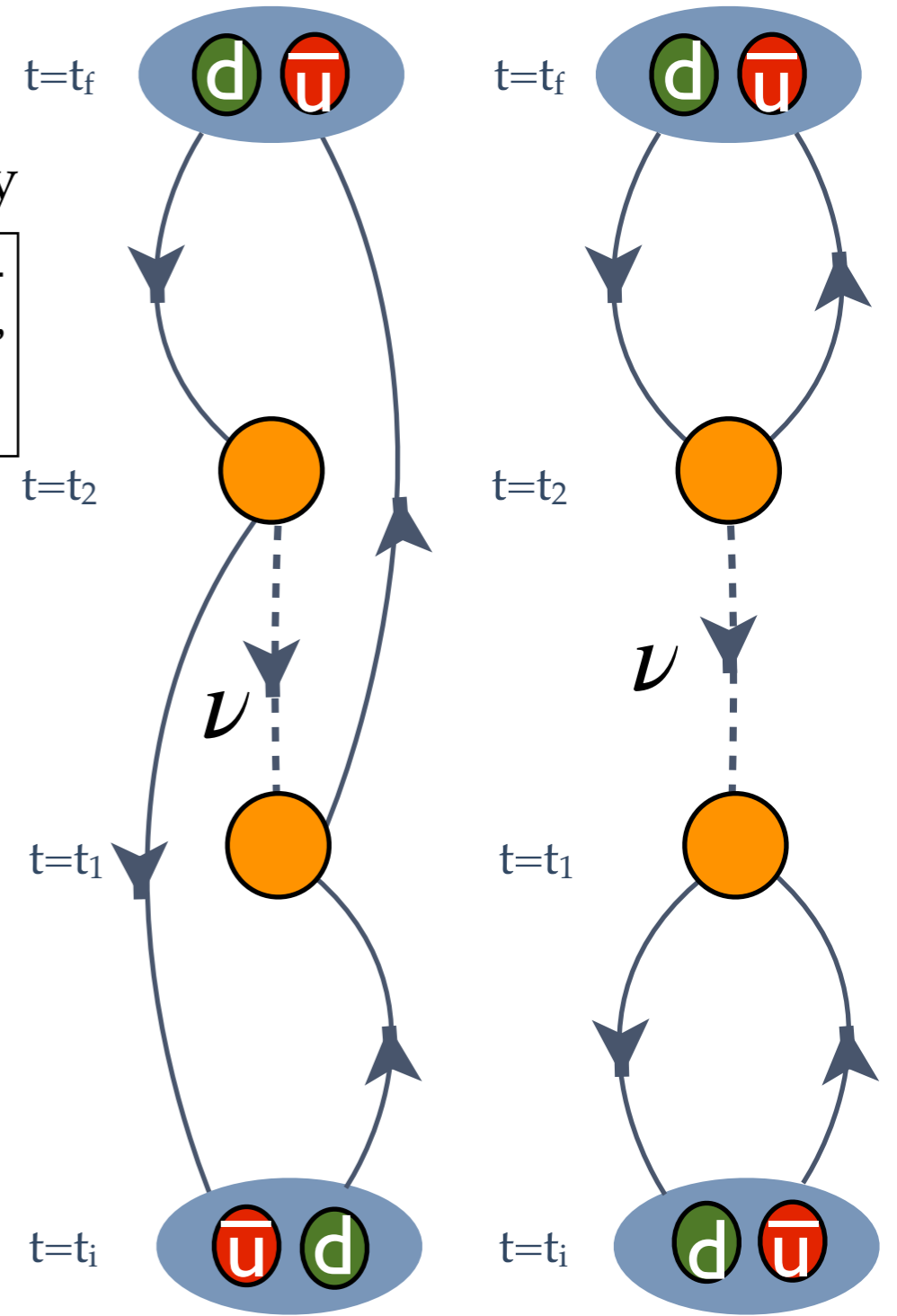
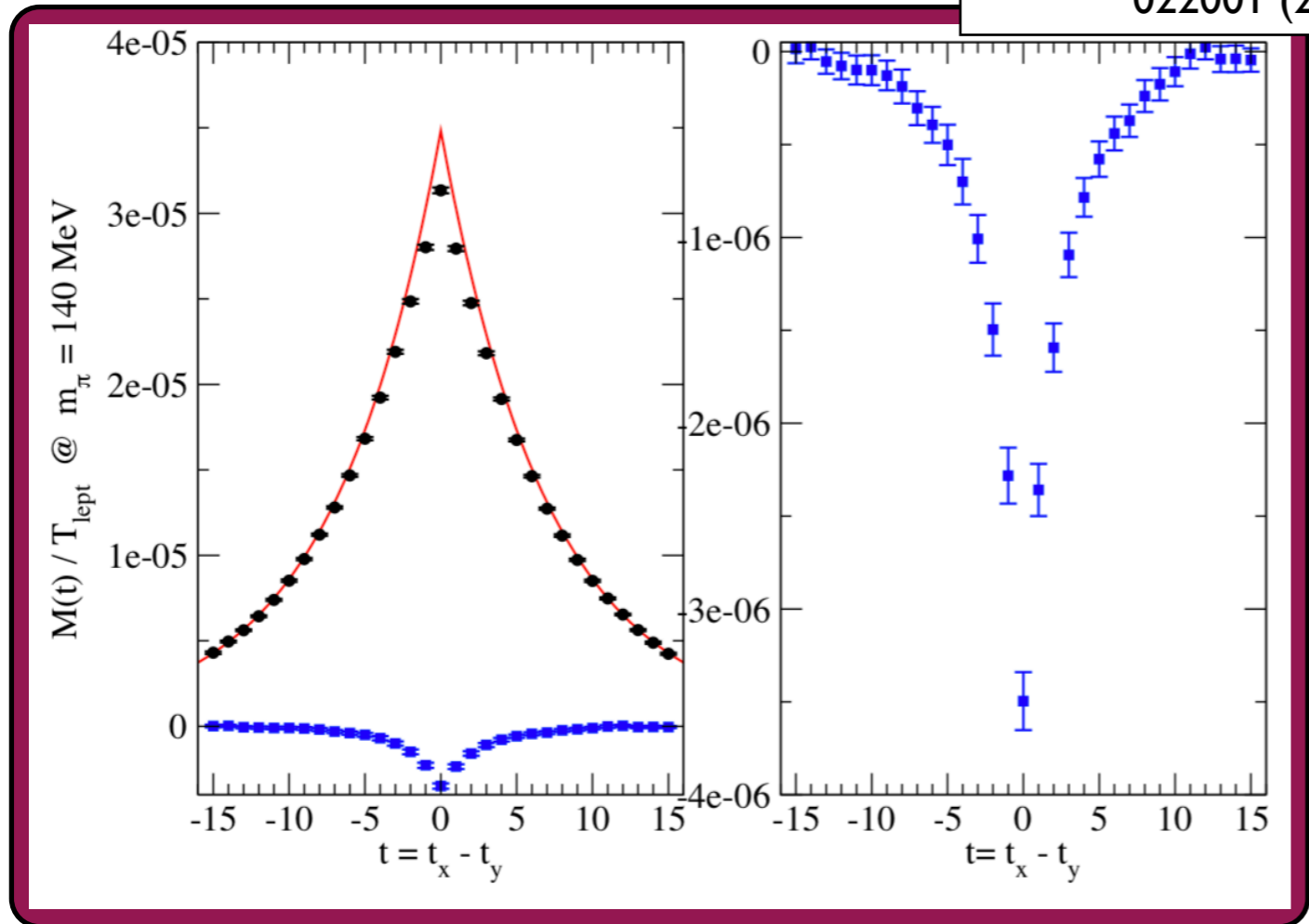
Full $nn \rightarrow pp$ transition

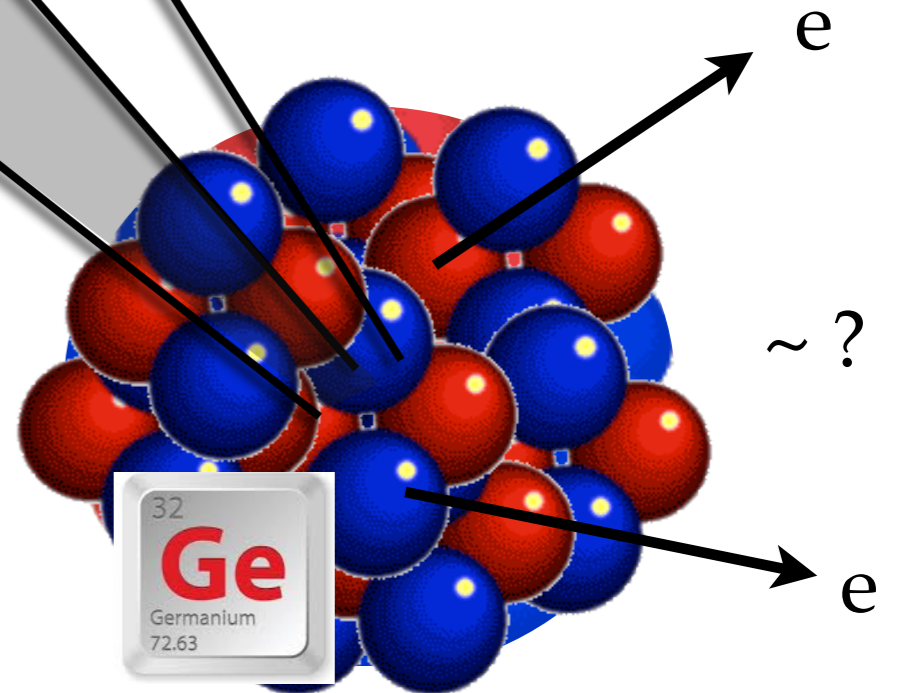
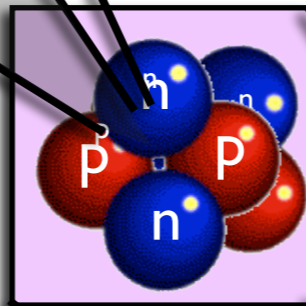
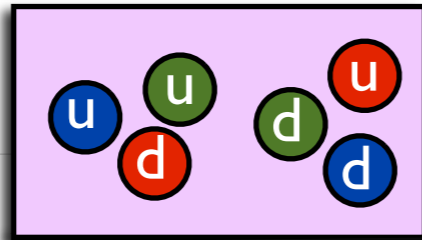


Cirigliano, V., Dekens, W., de Vries, J., Mereghetti, E., Graesser, M., Pastore, S., van Kolck, U
arXiv:1802.10097

- Work has begun to calculate full transition for light neutrino mechanism
- Why? Just as in short-range operator case, EFT may not be reliable
- Very difficult! both computationally and theoretically
- Start with $\pi^- \rightarrow \pi^+$ as a test
(see also Detmold & Murphy, Lattice 2018)

Xu Feng, Lu-Chang Jin, Xin-Yu Tuo, Shi-Cheng Xia,
Phys. Rev. Lett. 122, 022001 (2019)





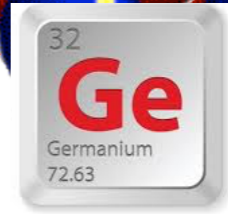
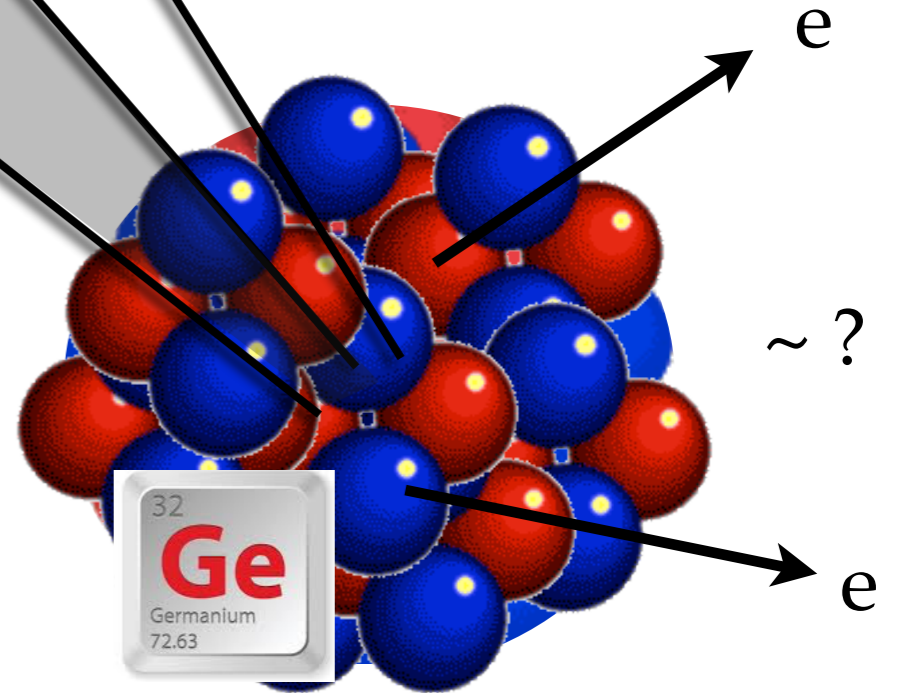
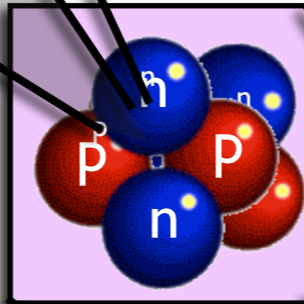
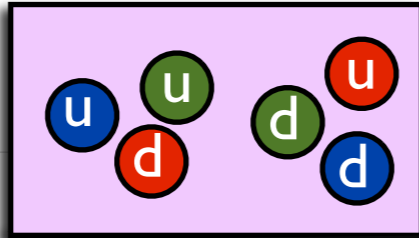
**Final step: match
onto many-body
models/EFT**

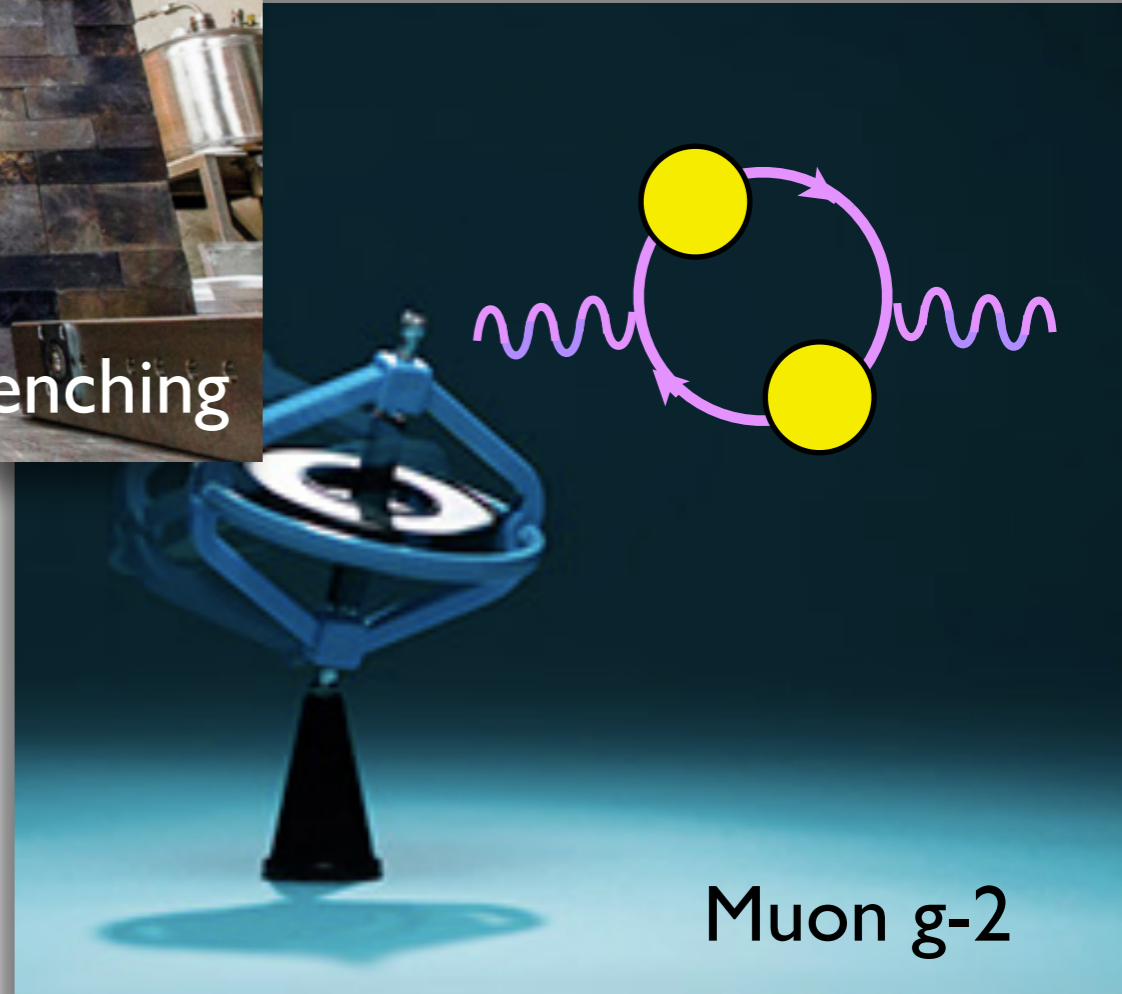
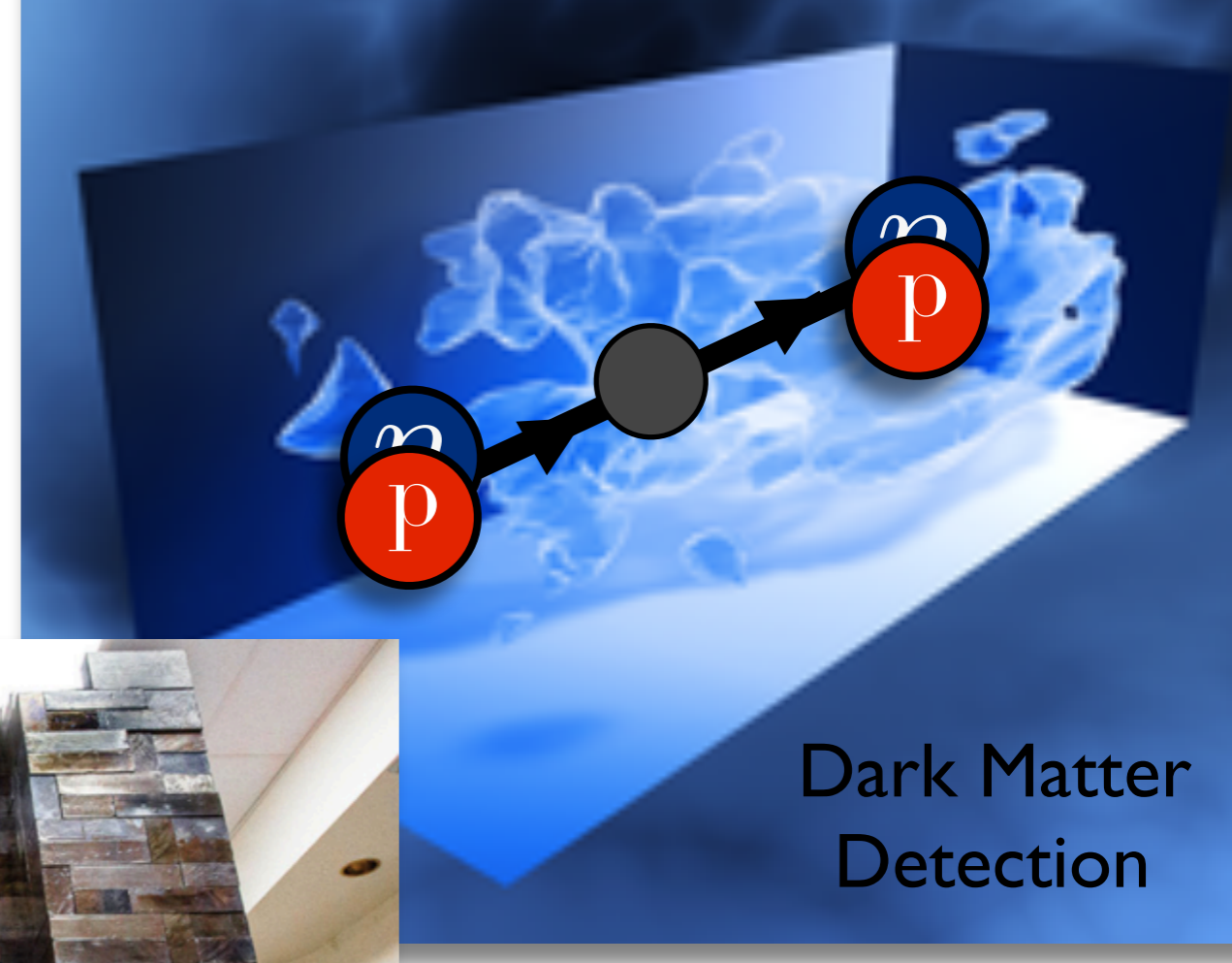
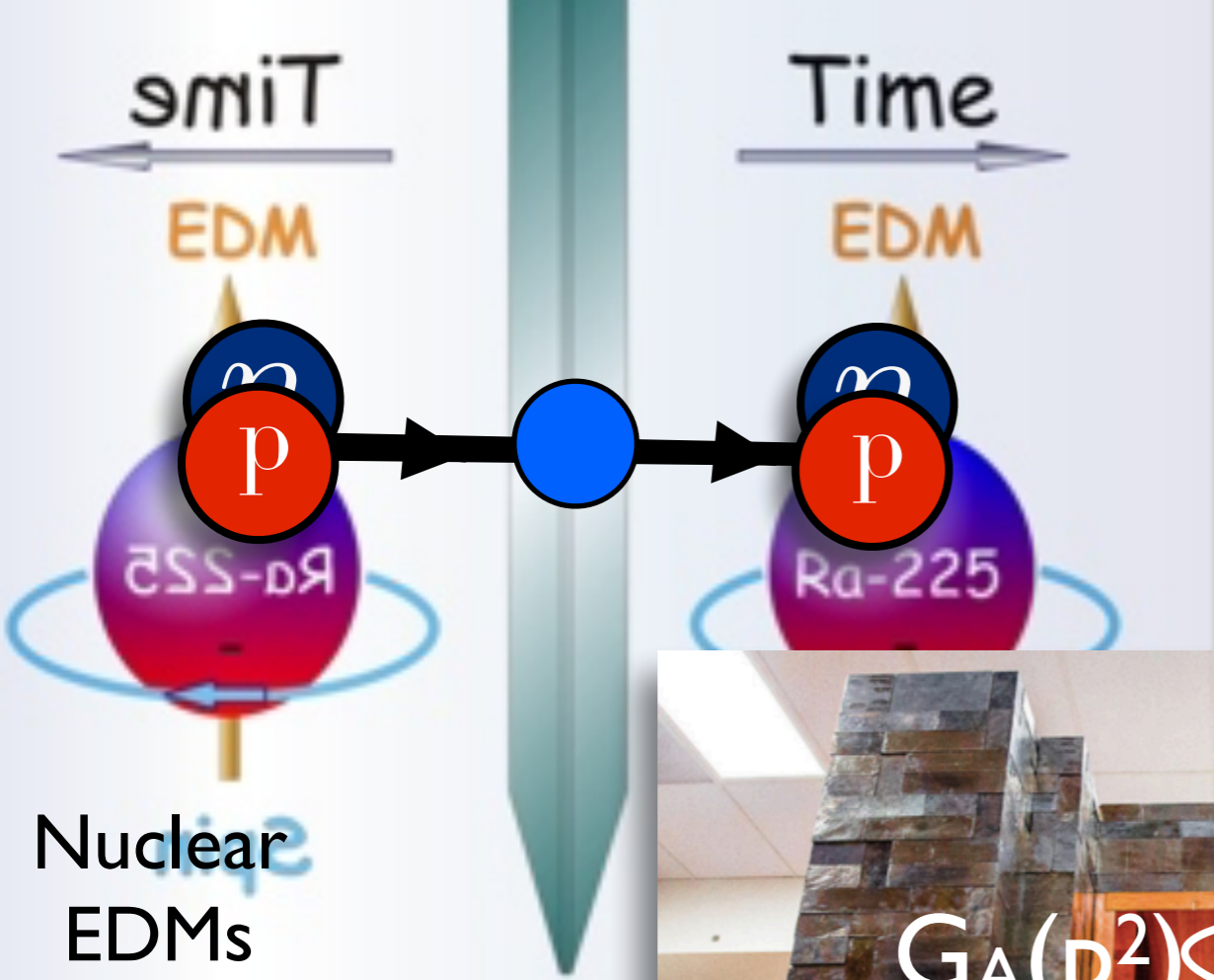


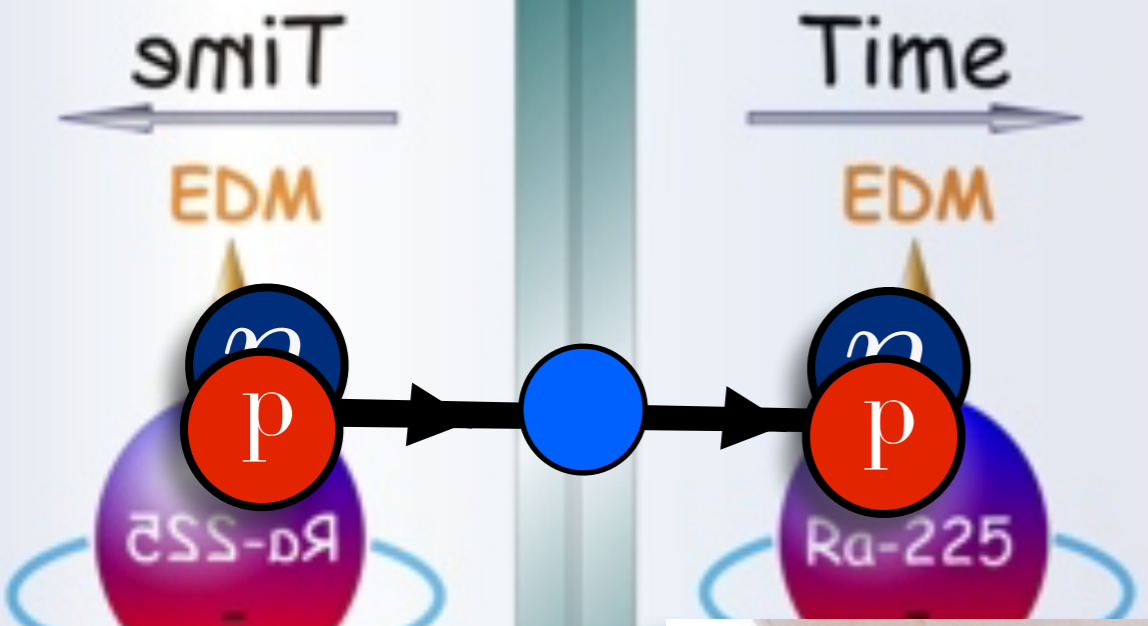
HOBET: W. Haxton, K. McElvain (T. Luu)



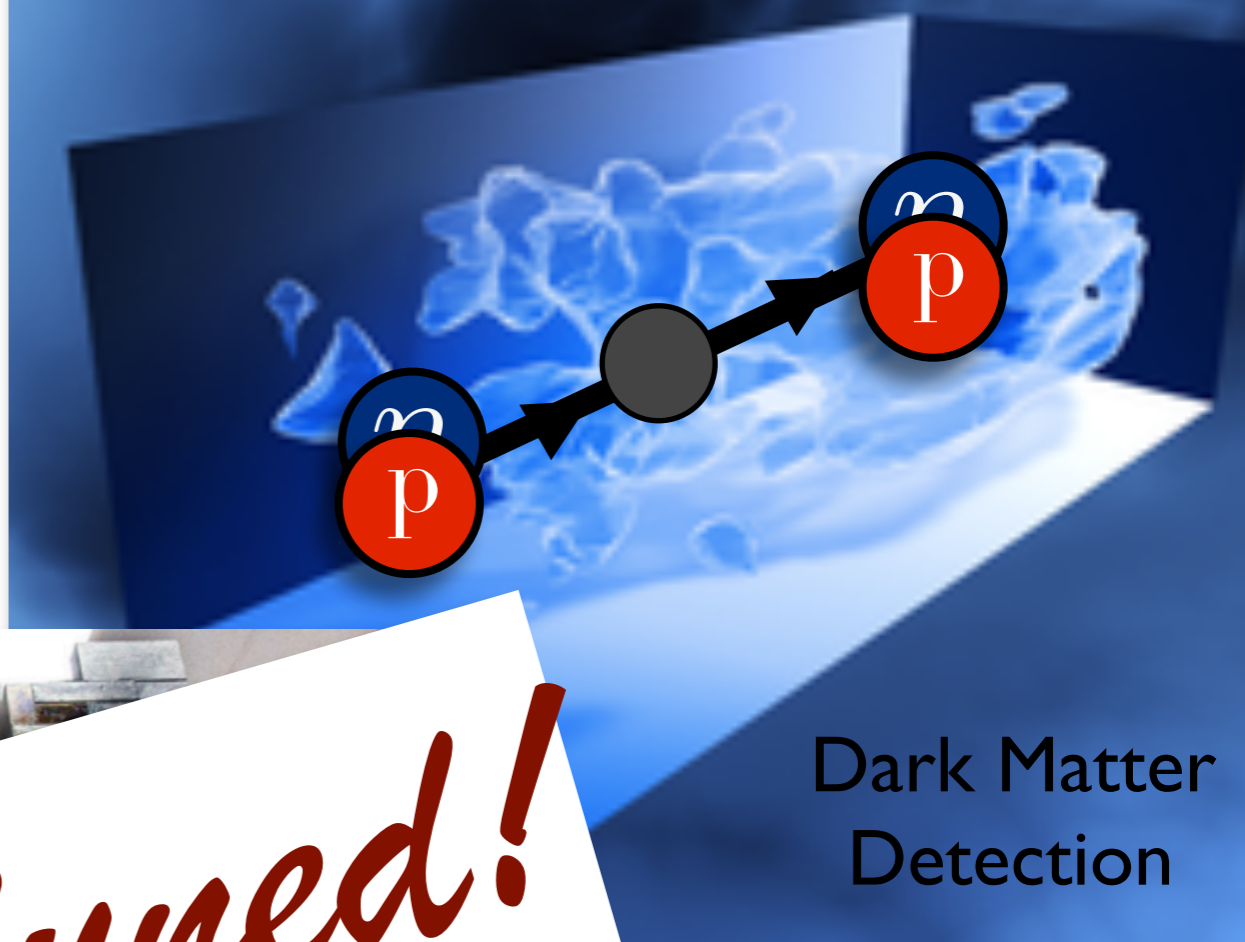
Bigstick: C. Johnson



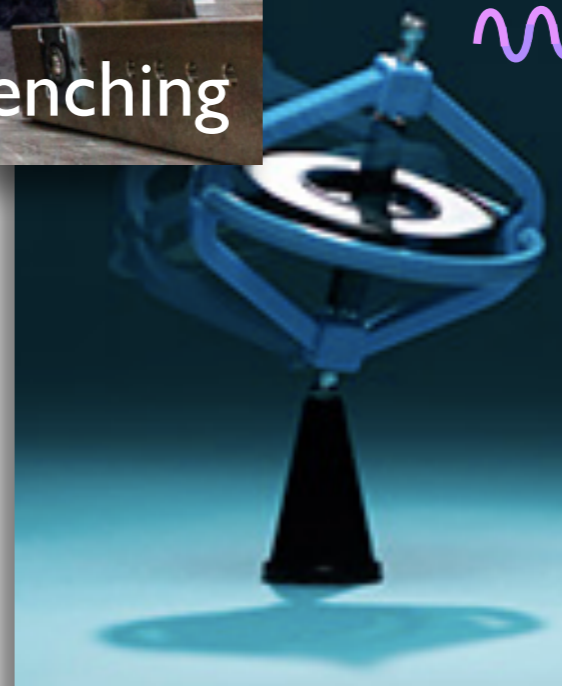
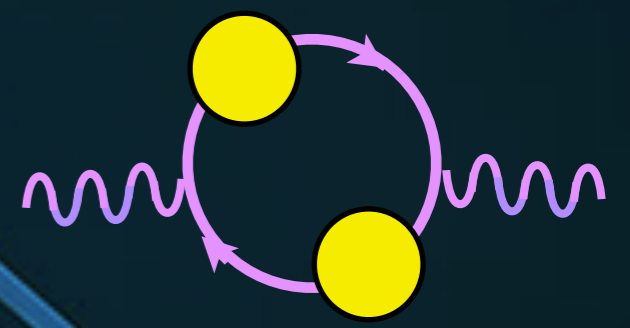
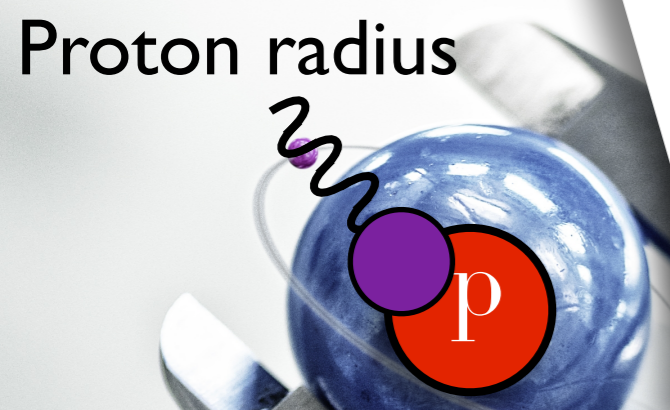




Nuclear EDMs



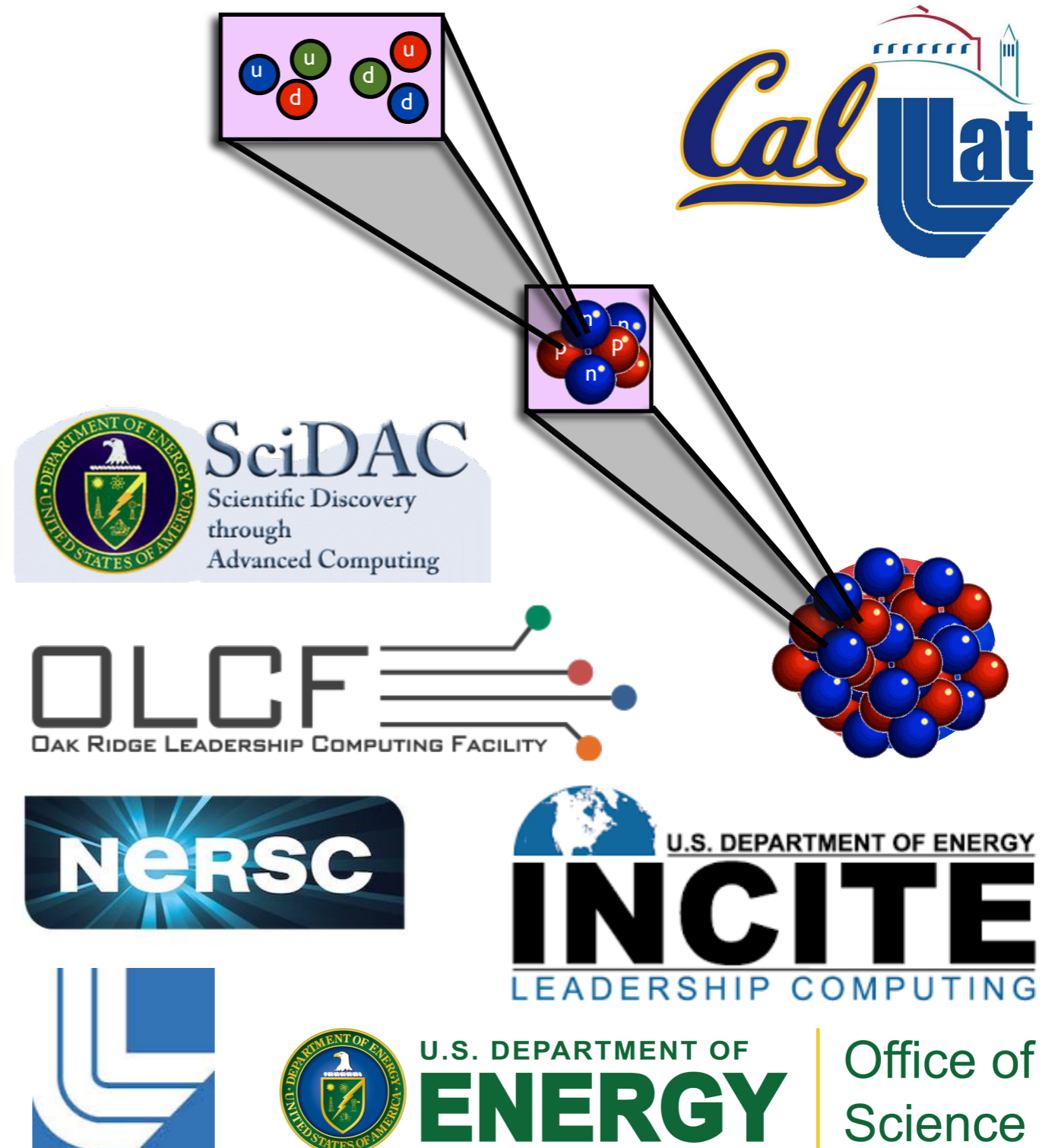
Stay Tuned!



Muon g-2

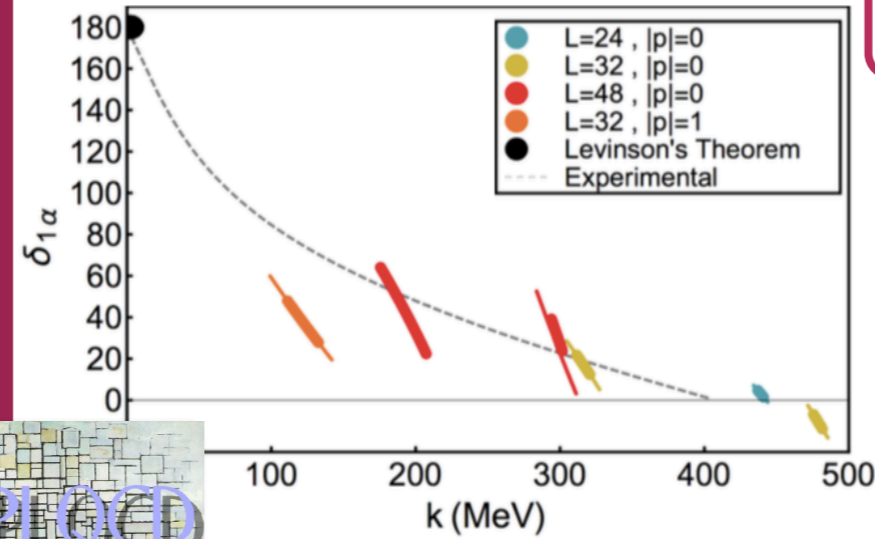
- RIKEN / LBL: C.C. Chang
- RIKEN / BNL: E. Rinaldi
- NERSC: T. Kurth
- Liverpool: N. Garron
- UW / INT C. Monahan
- nVidia: M.A. Clark
- JLab: B. Joo
- WM / JLab: K. Orginos
- CCNY: B. Tiburzi
- LBL / UCB: A. Walker-Loud
- Glasgow: C. Bouchard
- UNC: H. Monge-Camacho

- Jülich: E. Berkowitz
- LLNL: P. Vranas, A. Gambhir, D. Brantley

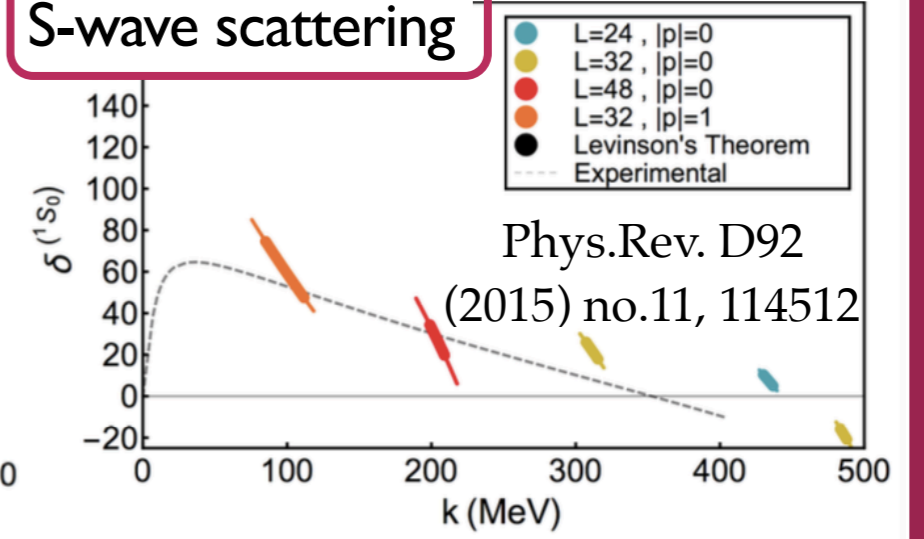


NN: status

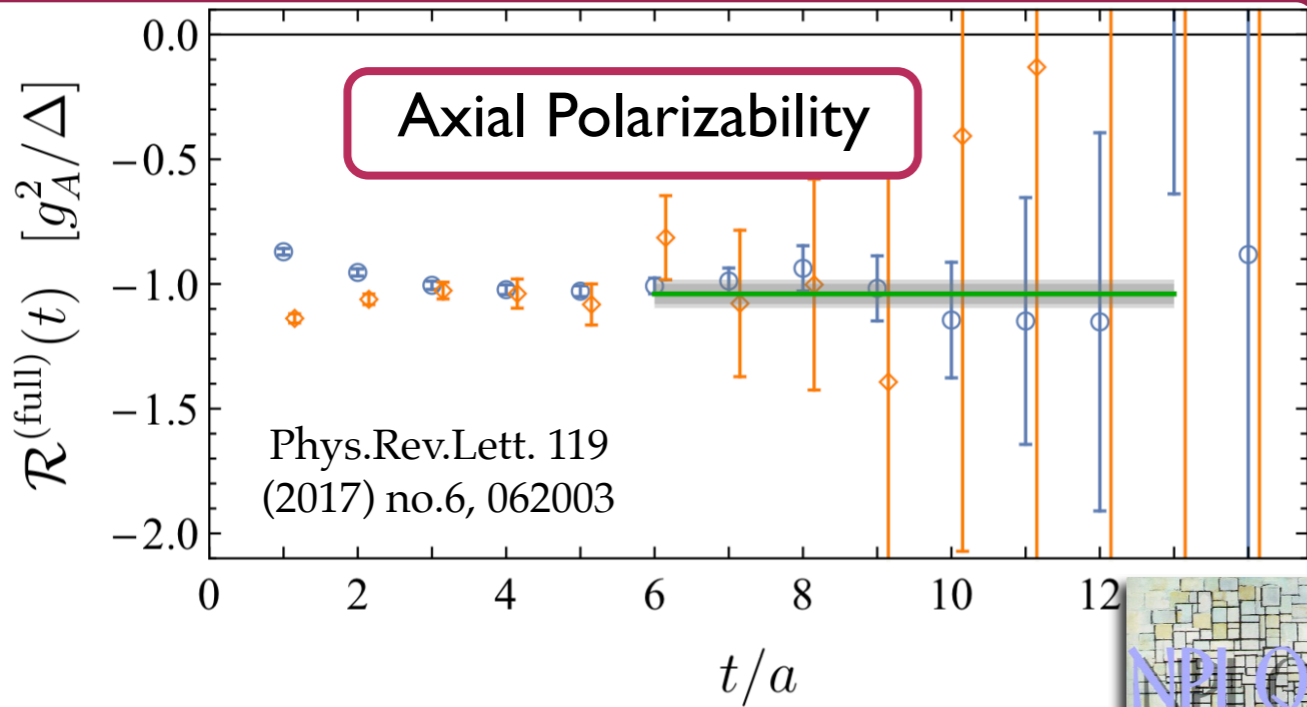
$m_\pi \sim 450 \text{ MeV}$



S-wave scattering



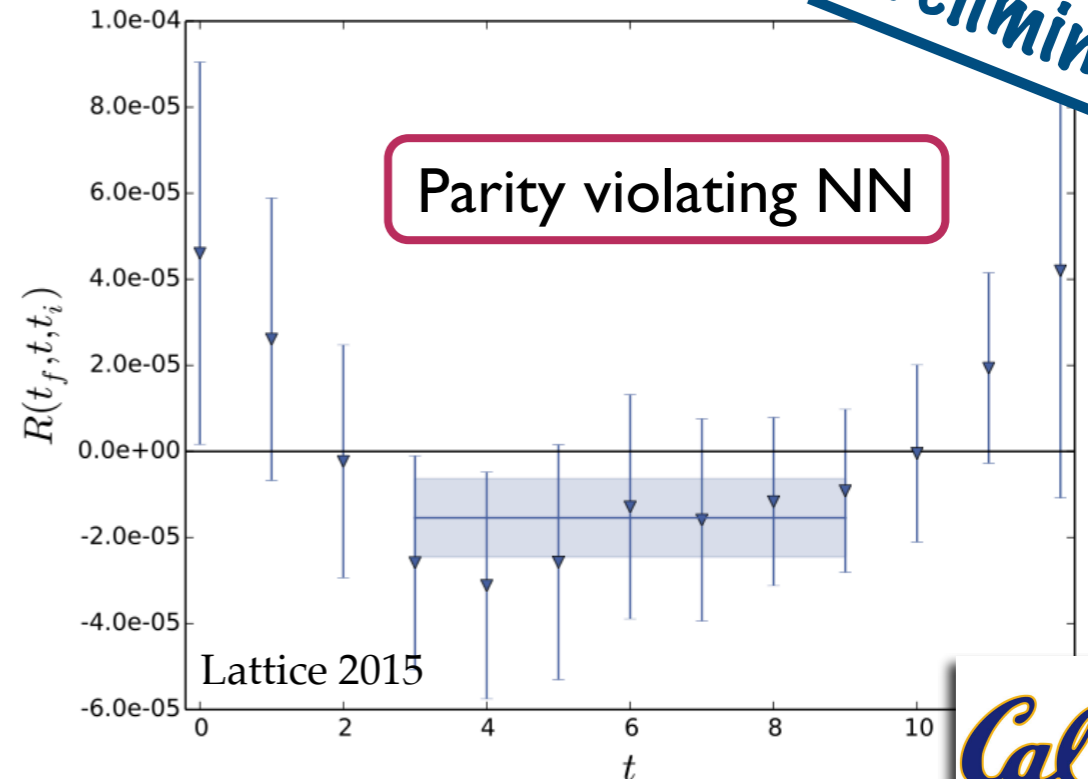
Phys.Rev. D92
(2015) no.11, 114512



Phys.Rev.Lett. 119
(2017) no.6, 062003



$m_\pi \sim 800 \text{ MeV}$



Parity violating NN

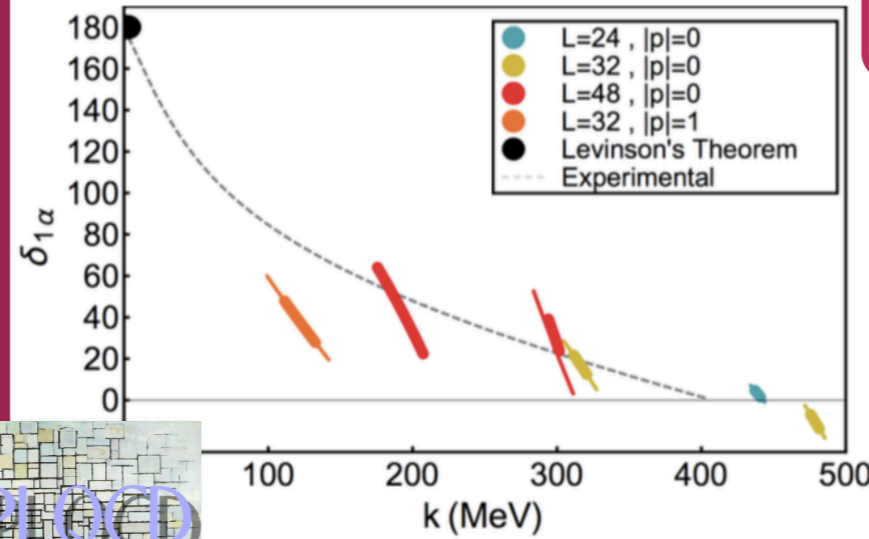
Lattice 2015

Preliminary

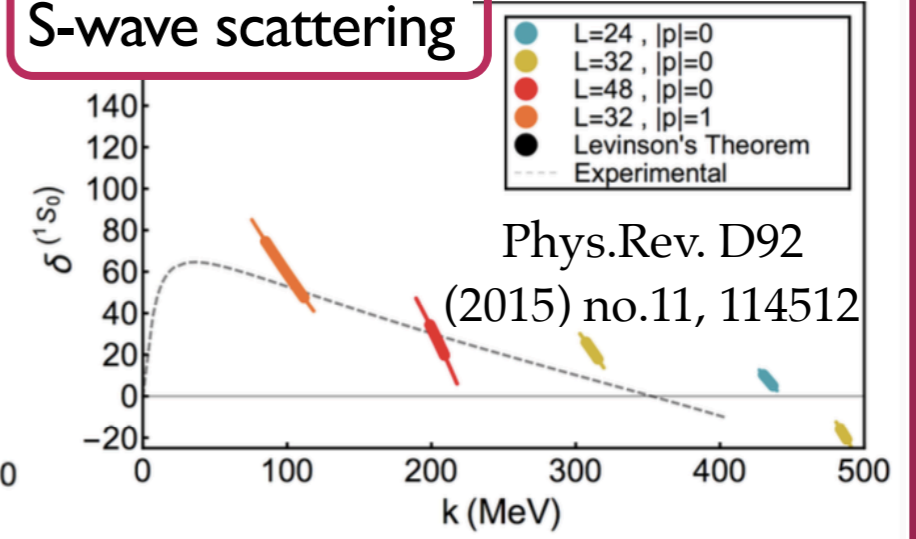


NN: status

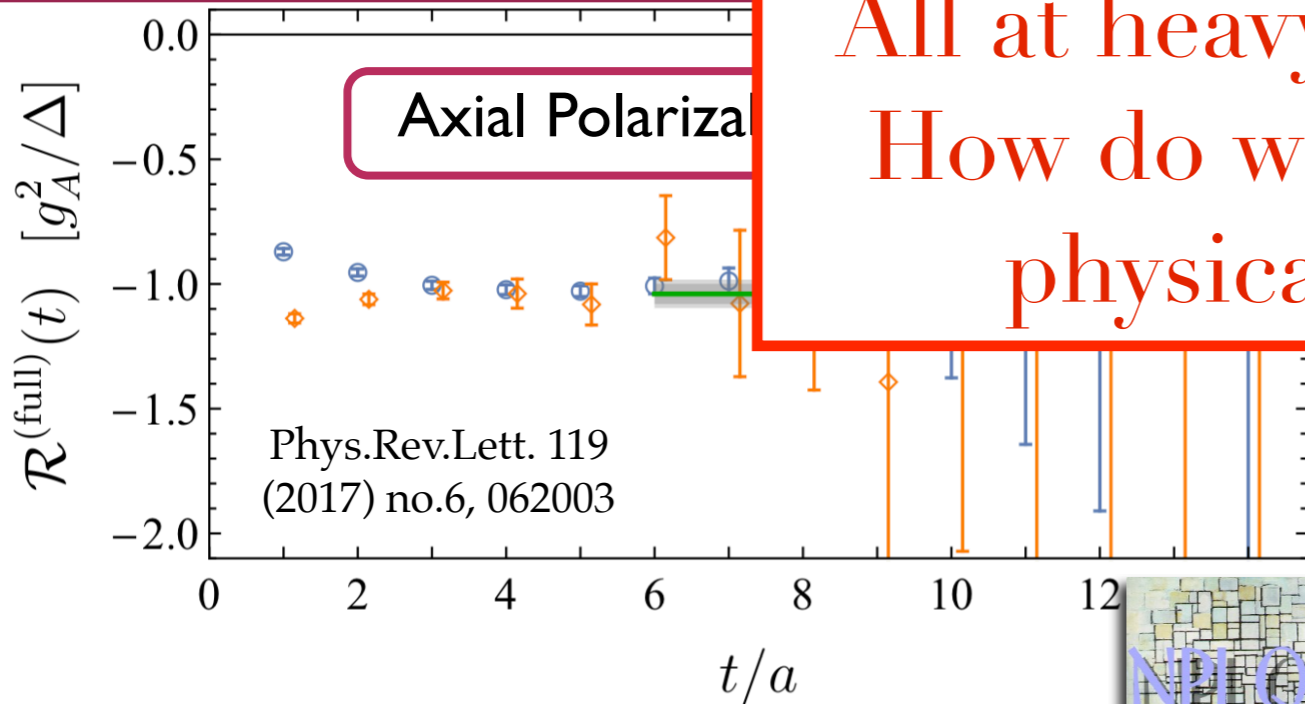
$m_\pi \sim 450 \text{ MeV}$



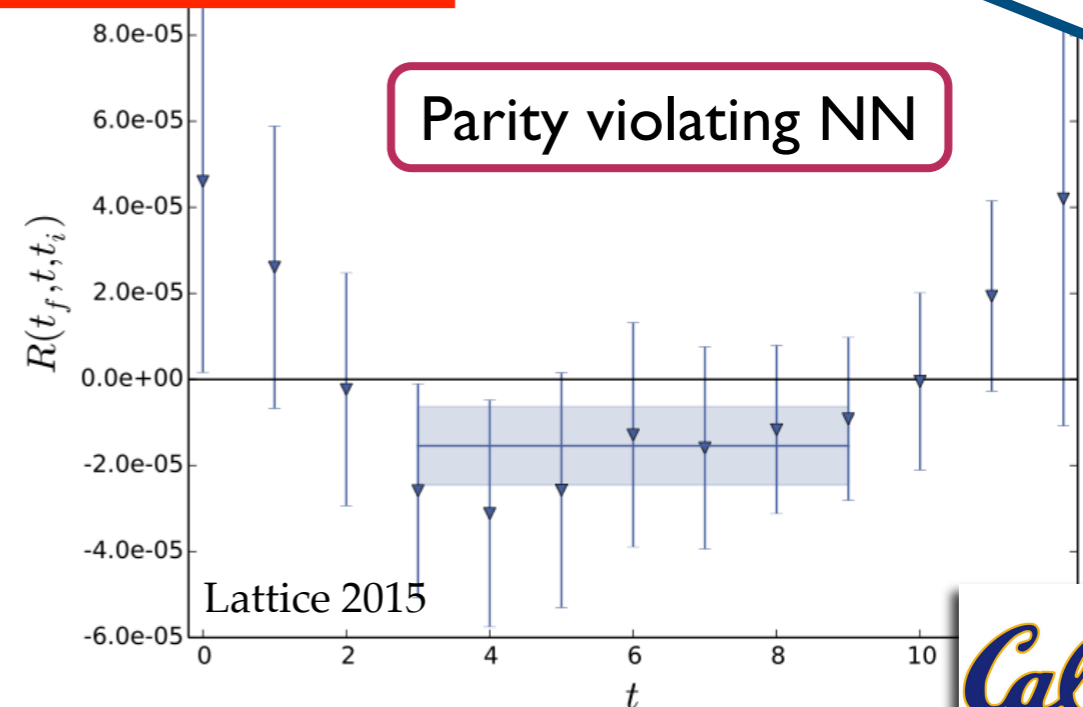
S-wave scattering



All at heavy pion mass.
 How do we get to the
 physical point?



$m_\pi \sim 800 \text{ MeV}$

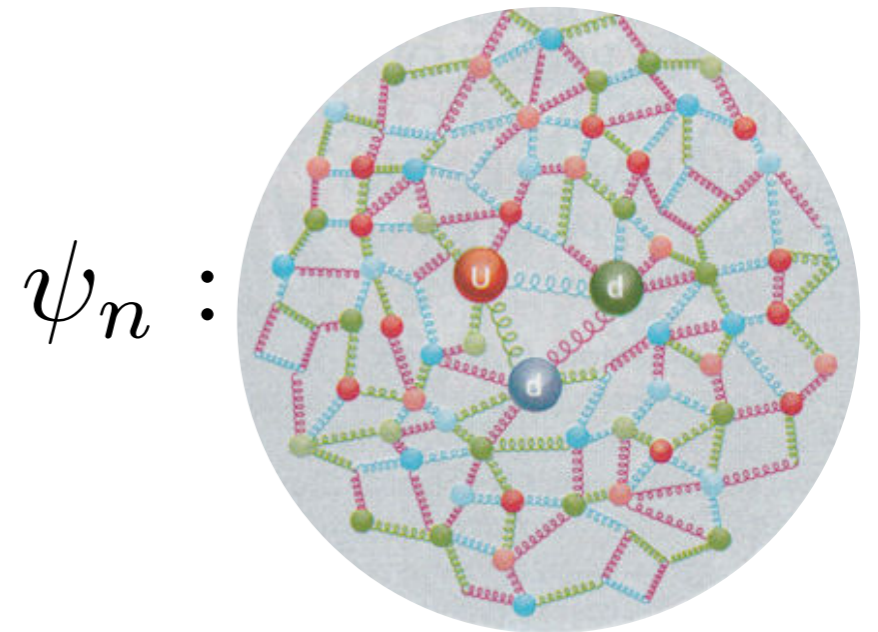
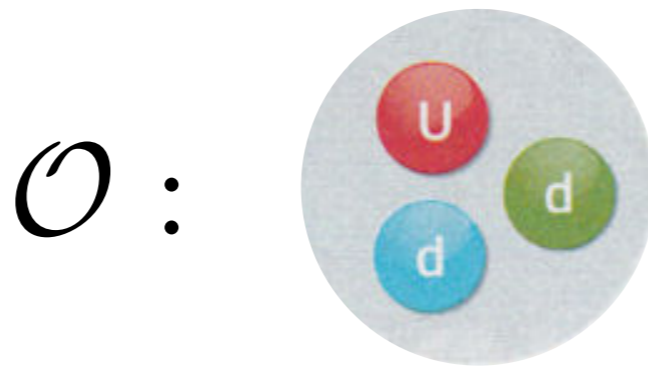


Preliminary



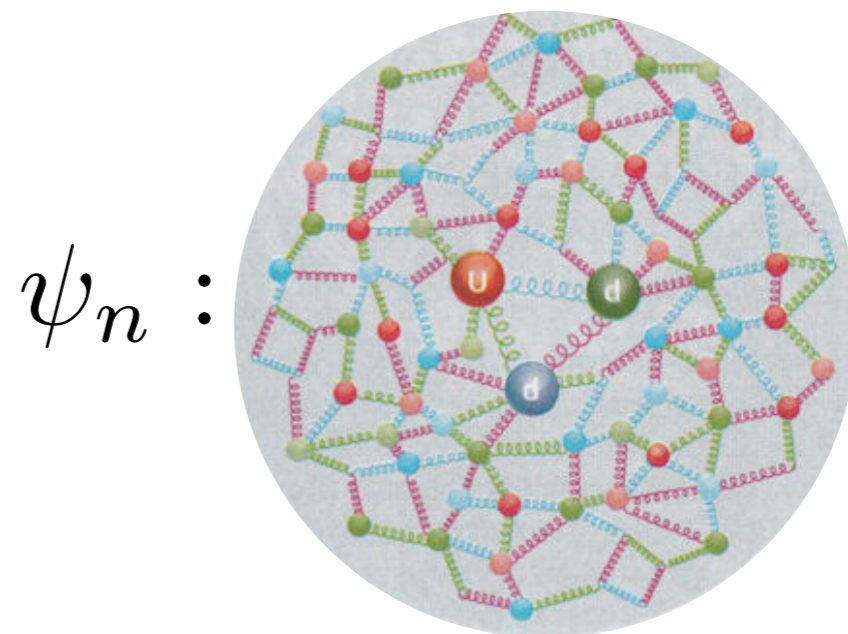
Lower pion mass?
Difficulty lies in
spectroscopy

$$\langle \mathcal{O}(t) \mathcal{O}^\dagger(0) \rangle = \langle \mathcal{O}(0) e^{-Ht} \mathcal{O}(0) \rangle = \sum_n |\langle 0 | \mathcal{O} | n \rangle|^2 e^{-E_n t}$$



Lower pion mass?
Difficulty lies in spectroscopy

$$\langle \mathcal{O}(t) \mathcal{O}^\dagger(0) \rangle = \langle \mathcal{O}(0) e^{-Ht} \mathcal{O}(0) \rangle = \sum_n |\langle 0 | \mathcal{O} | n \rangle|^2 e^{-E_n t}$$

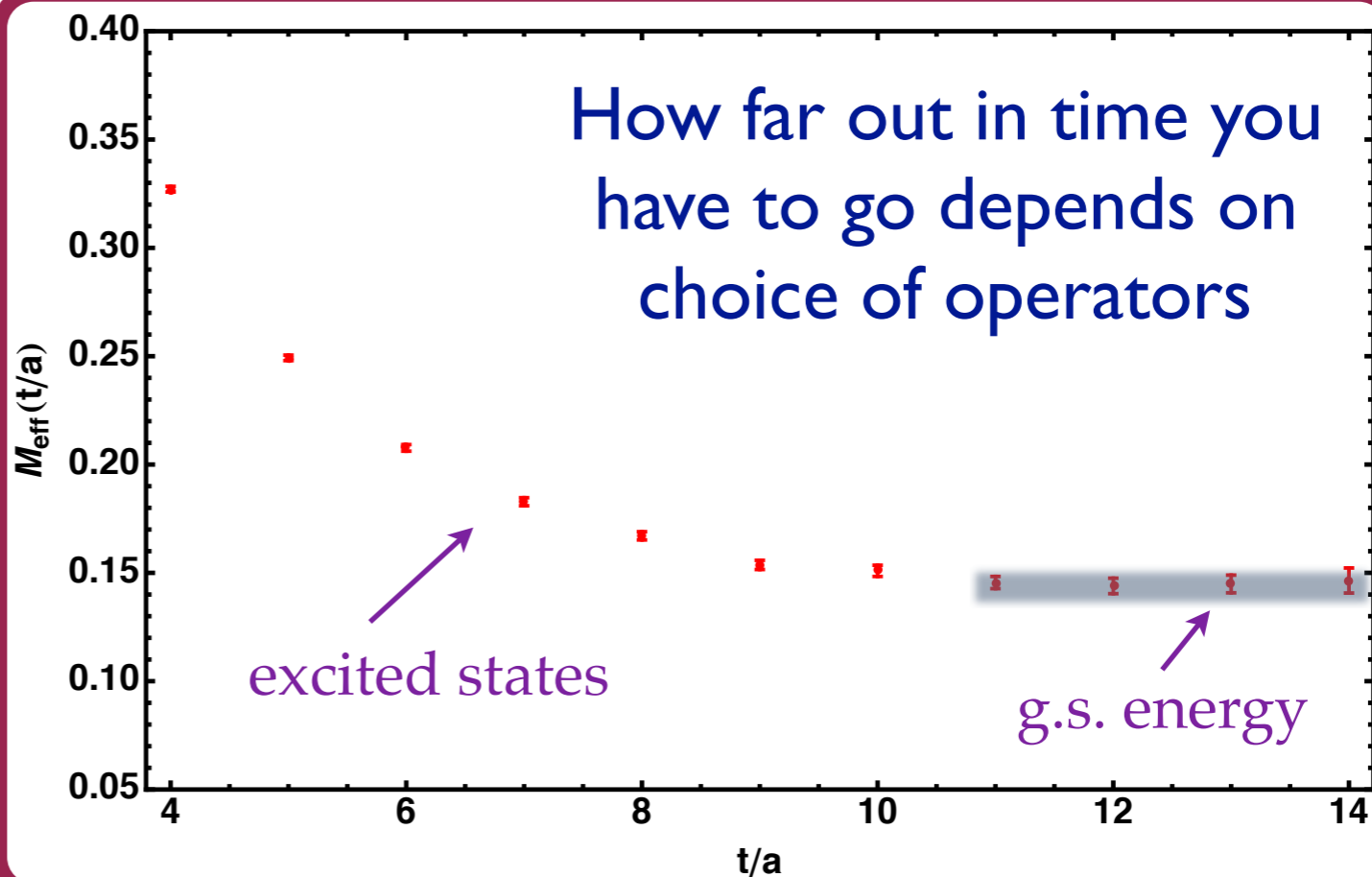


Effective mass

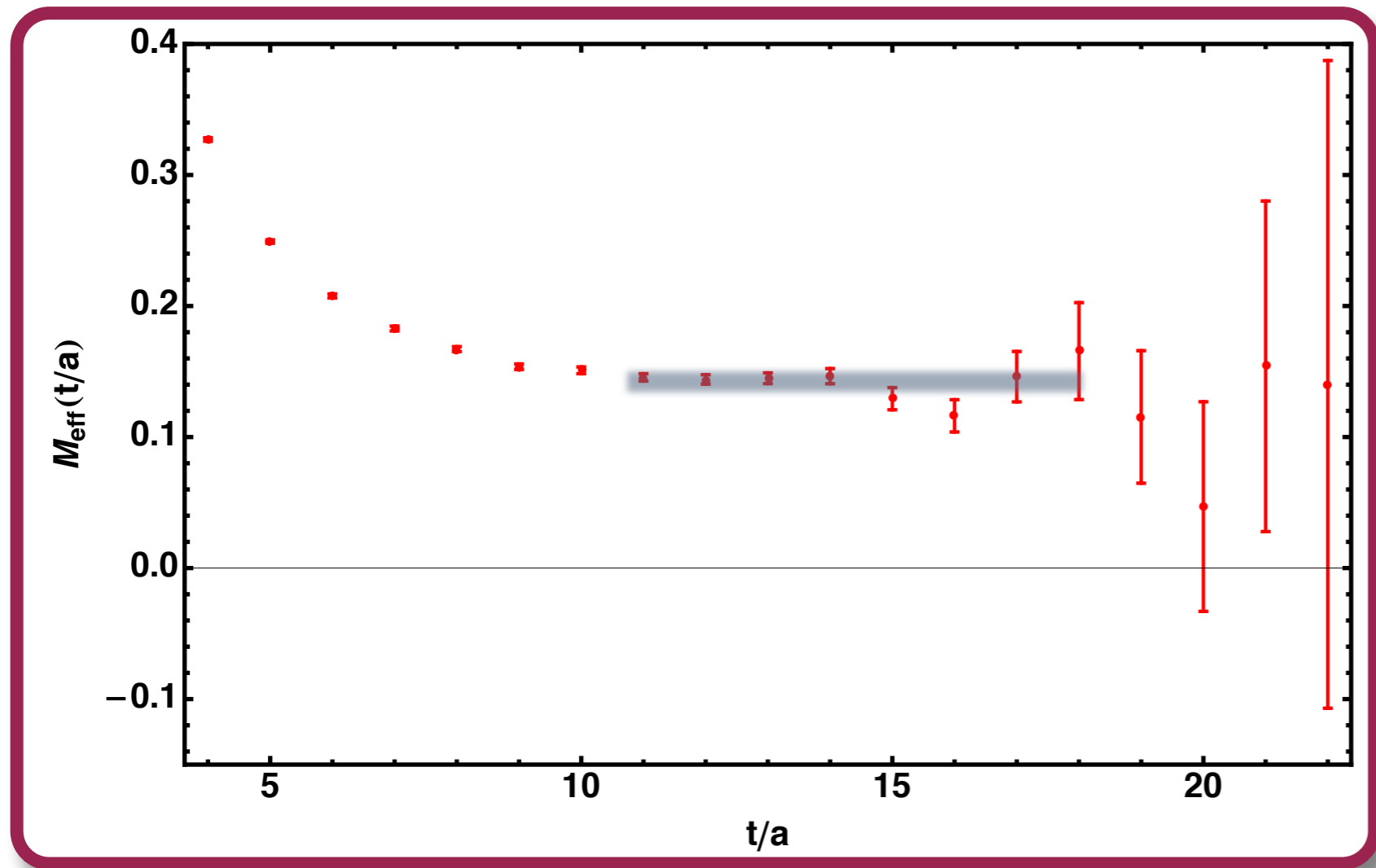
plot:

$$M_{\text{eff}} \equiv \ln \frac{C(t)}{C(t+1)}$$

$$\xrightarrow[t \rightarrow \infty]{} E_0$$

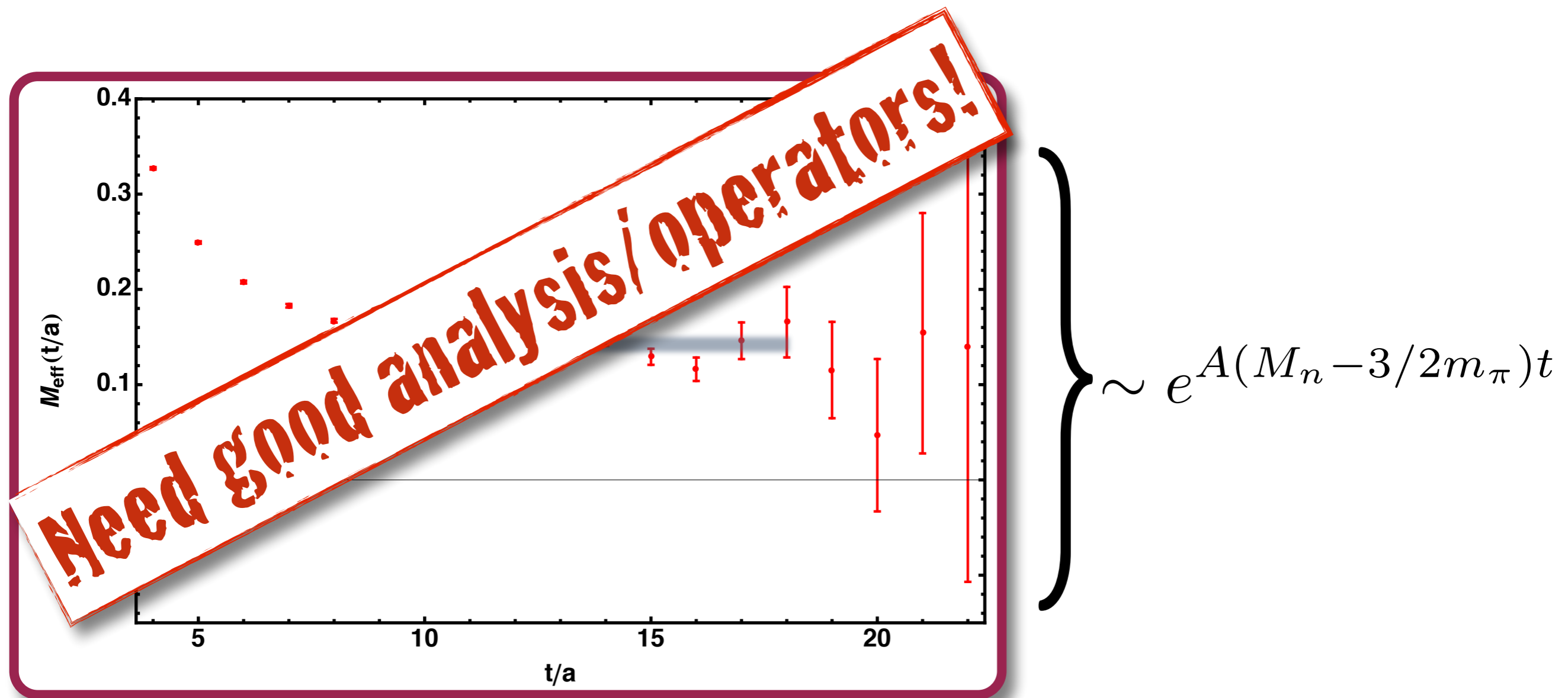


Nucleons: limited by signal-to-noise

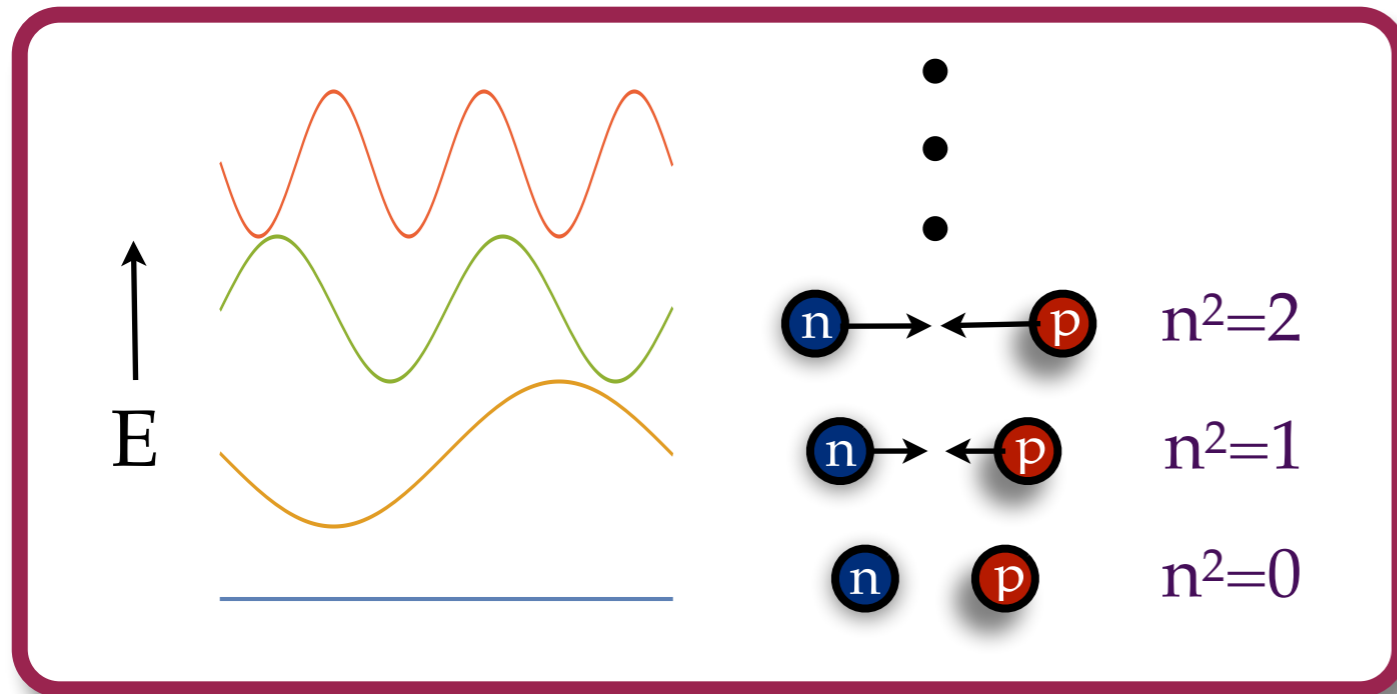


$$\left. \vphantom{\int} \right\} \sim e^{A(M_n - 3/2m_\pi)t}$$

Nucleons: limited by signal-to-noise



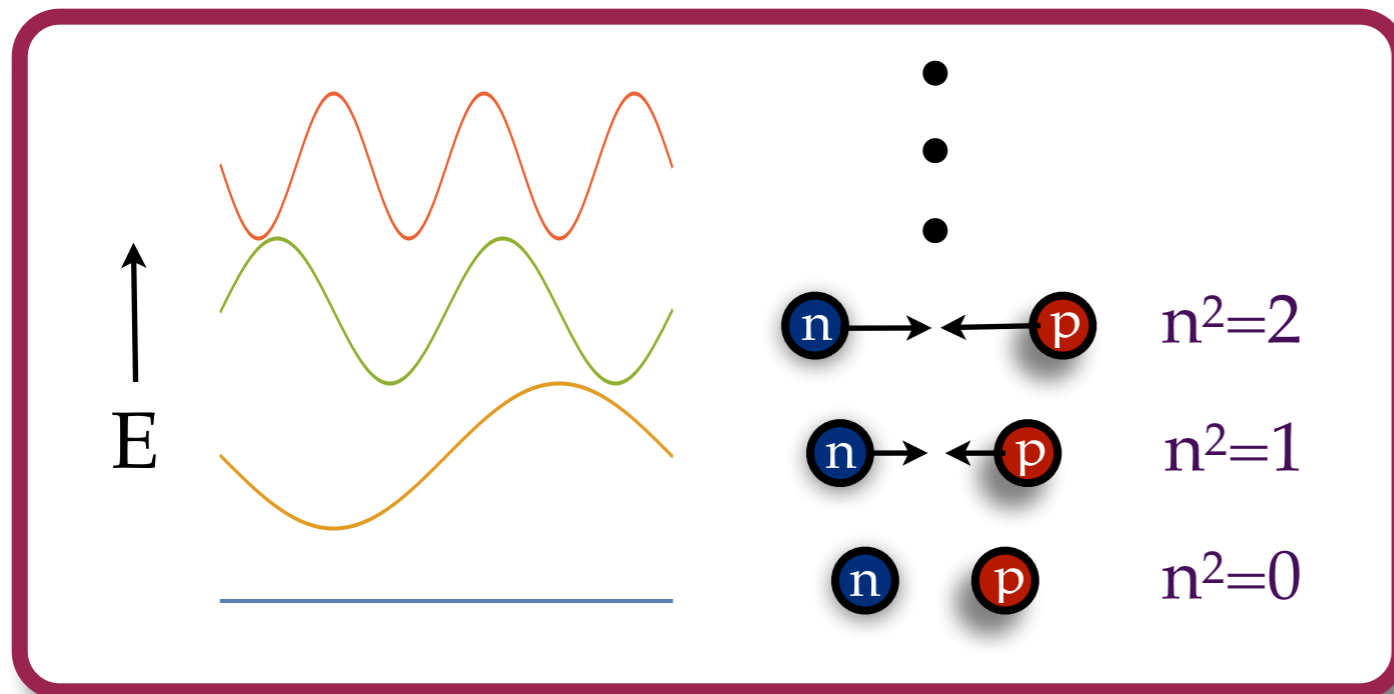
Excited state contamination



Elastic 2-body

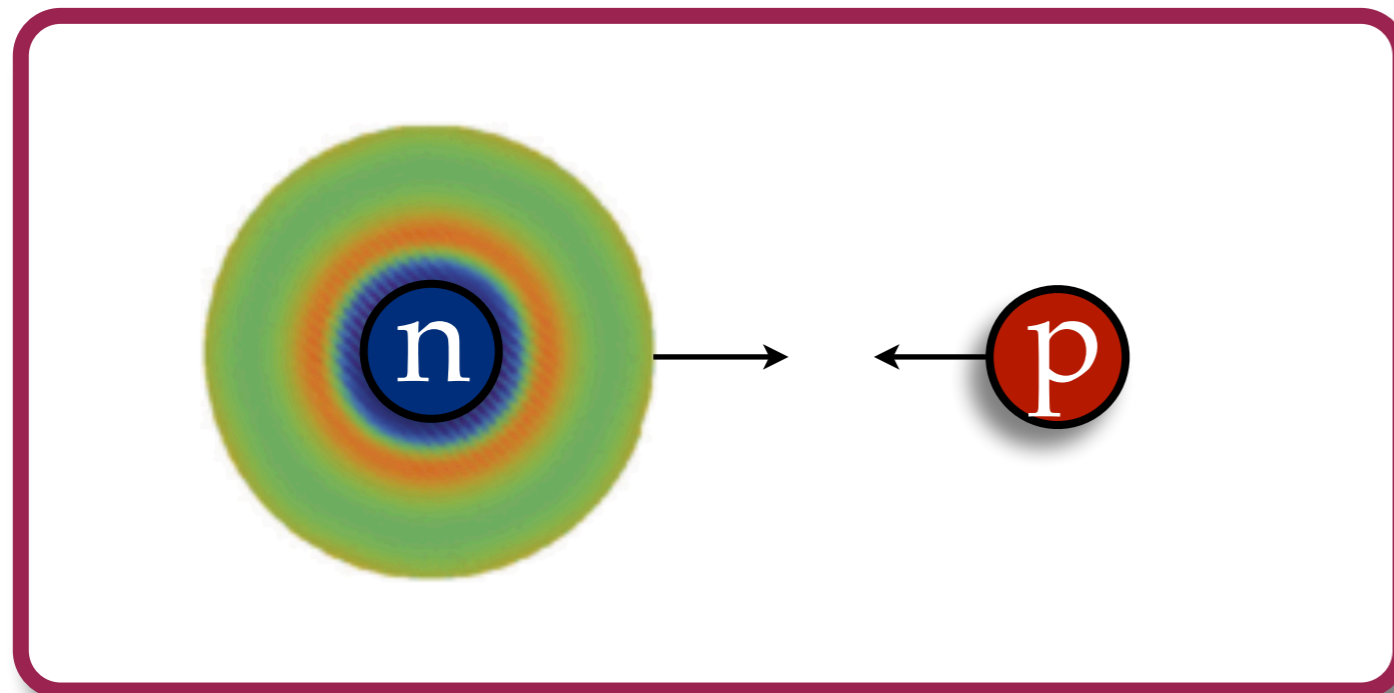
$\Delta E \sim 50 \text{ MeV}$

Excited state contamination



Elastic 2-body

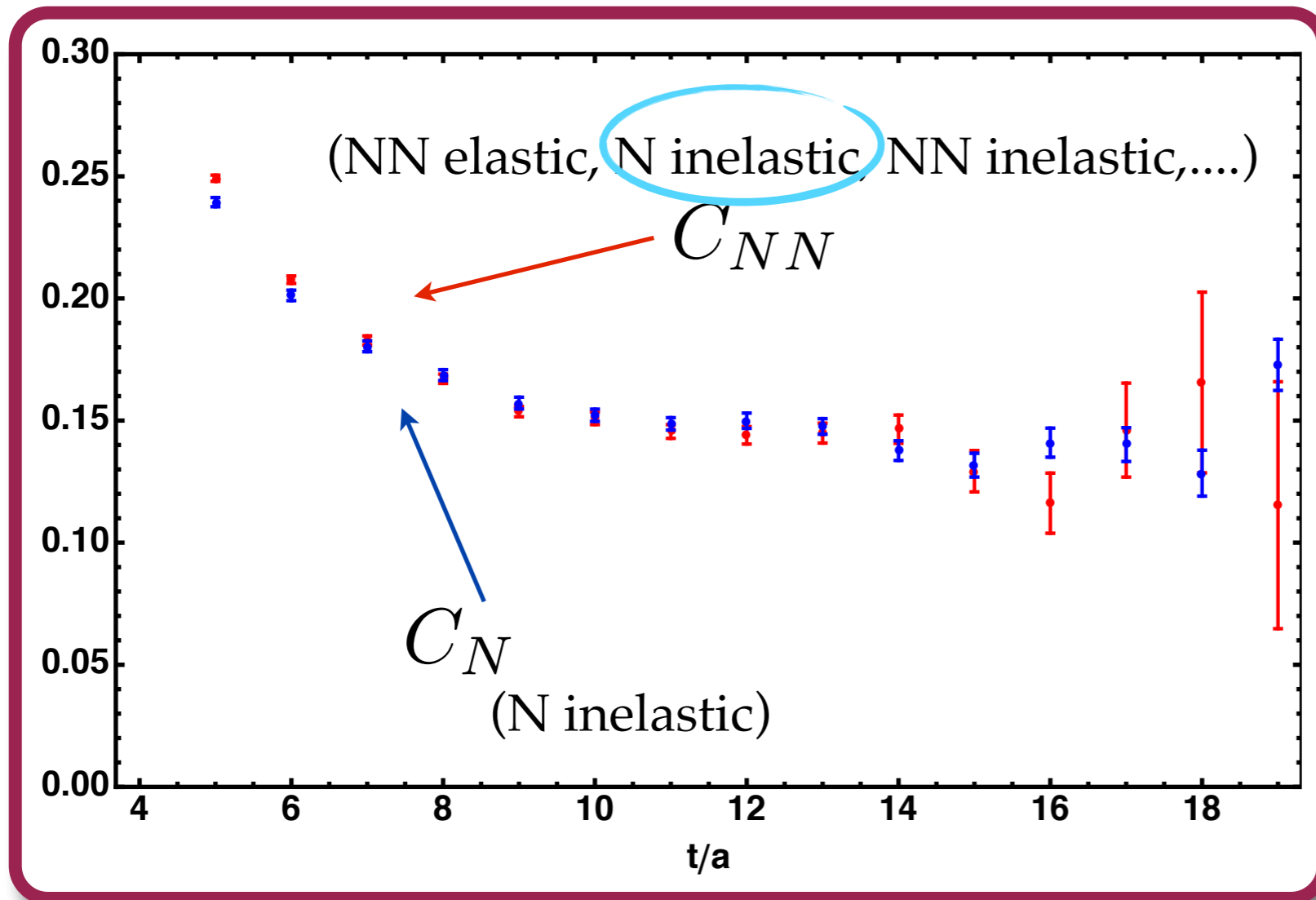
$$\Delta E \sim 50 \text{ MeV}$$



Inelastic single body

$$\Delta E \sim m_{\pi}$$

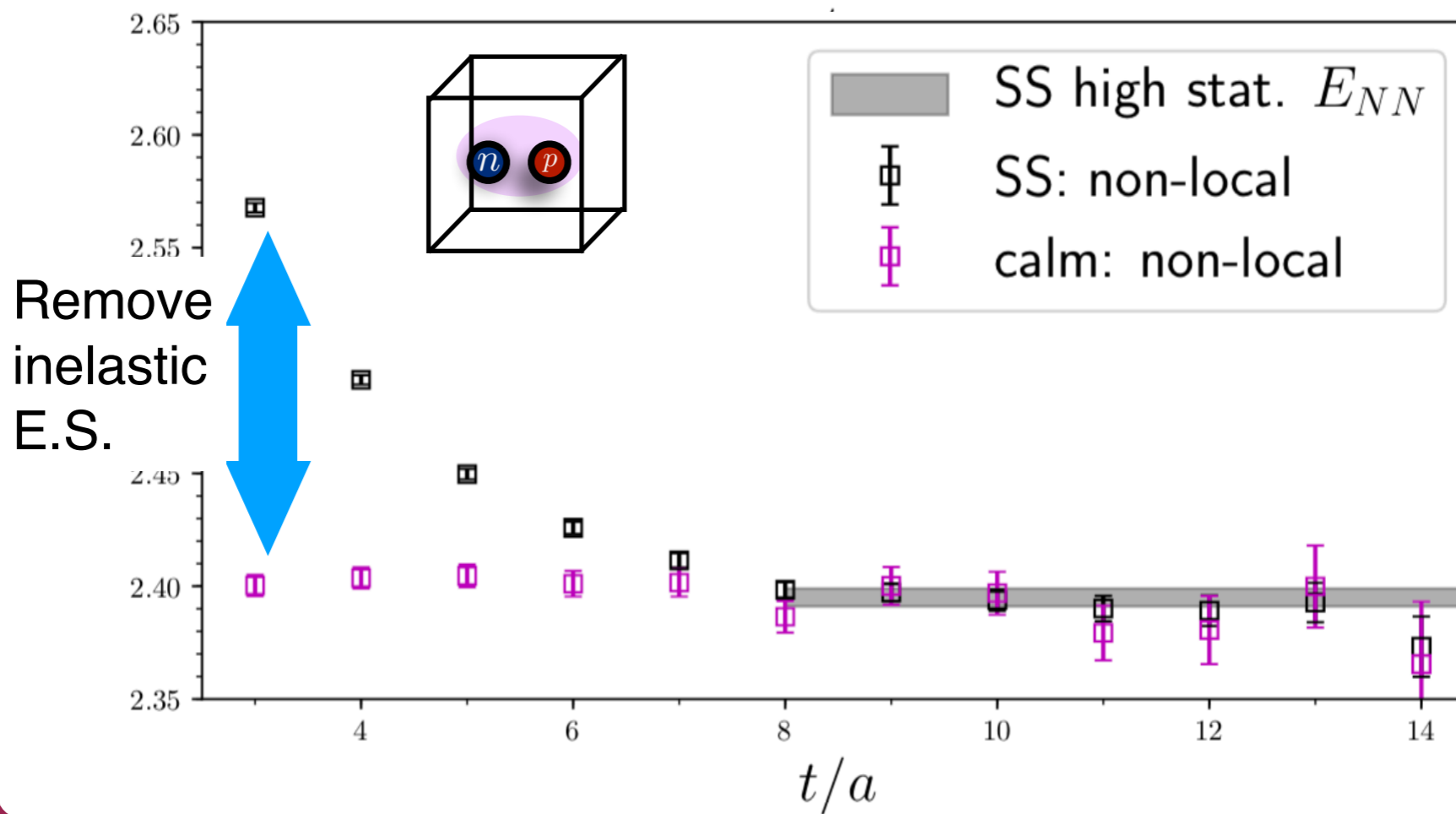
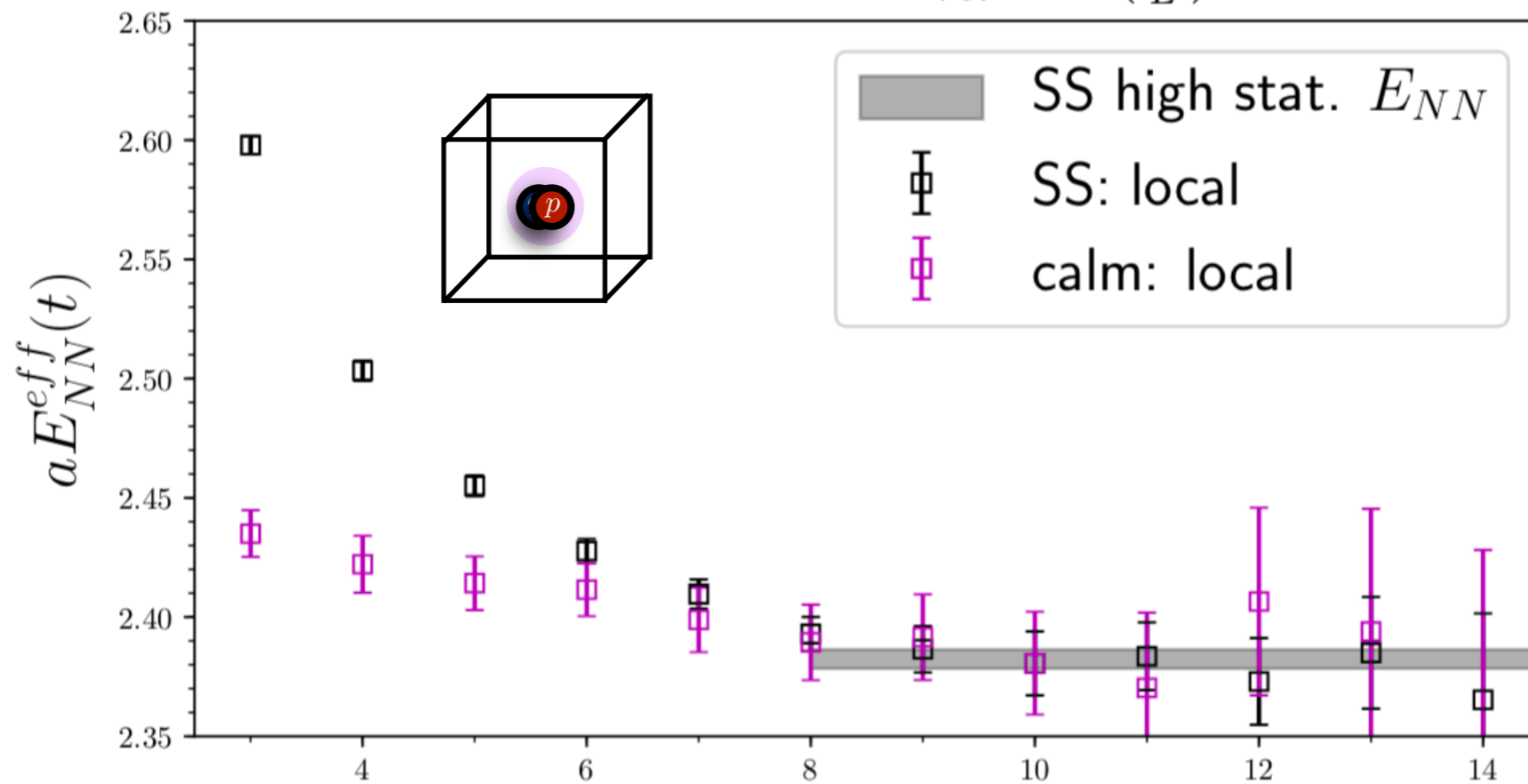
Improved NN



Long time behavior
of NN correlator
dominated by
inelastic single
nucleon excited state

→ Need to improve
single nucleon
interpolating
operator for earlier
plateaus

$$NN : T_1^+ : {}^3S_1 : p_{rel}^2 = 0 \left(\frac{2\pi}{L}\right)^2$$

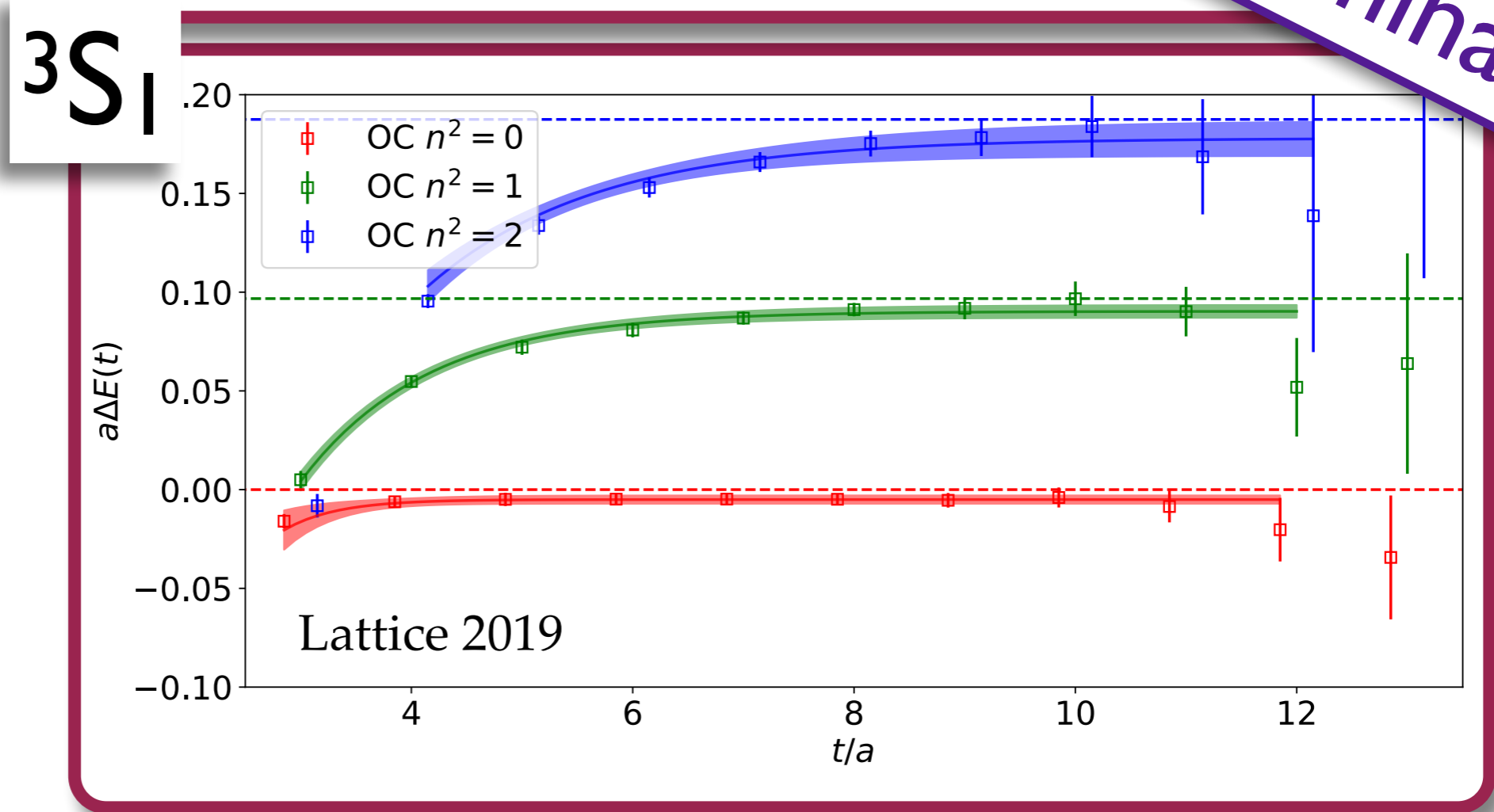
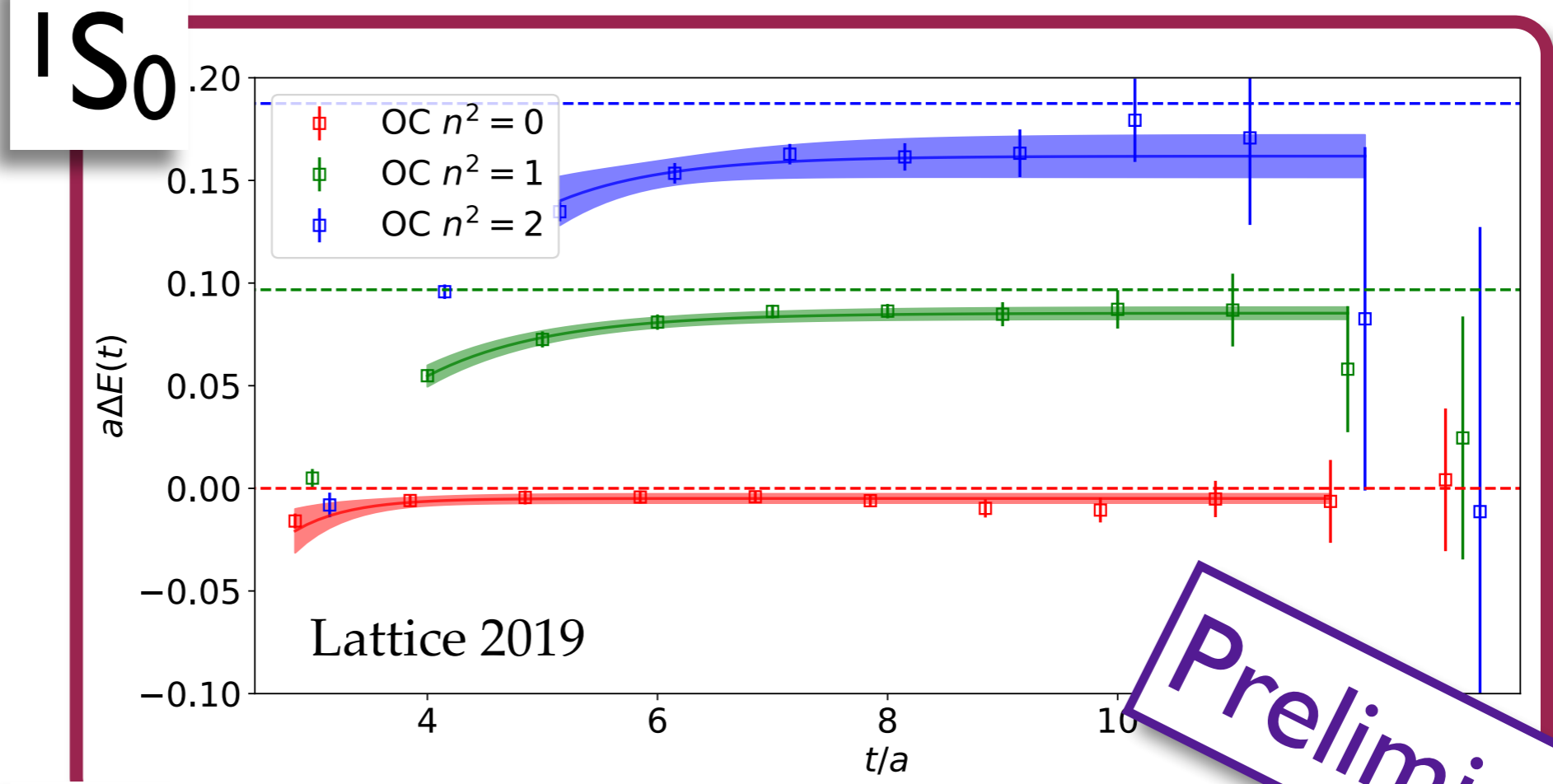


Remove elastic E.S.

Remove inelastic E.S.

Callat (2017)
Matrix Prony:
NPLQCD (2009)

Energy levels:
 $m_\pi \sim 350$ MeV
 (DWF on MILC
 HISQ ensembles)

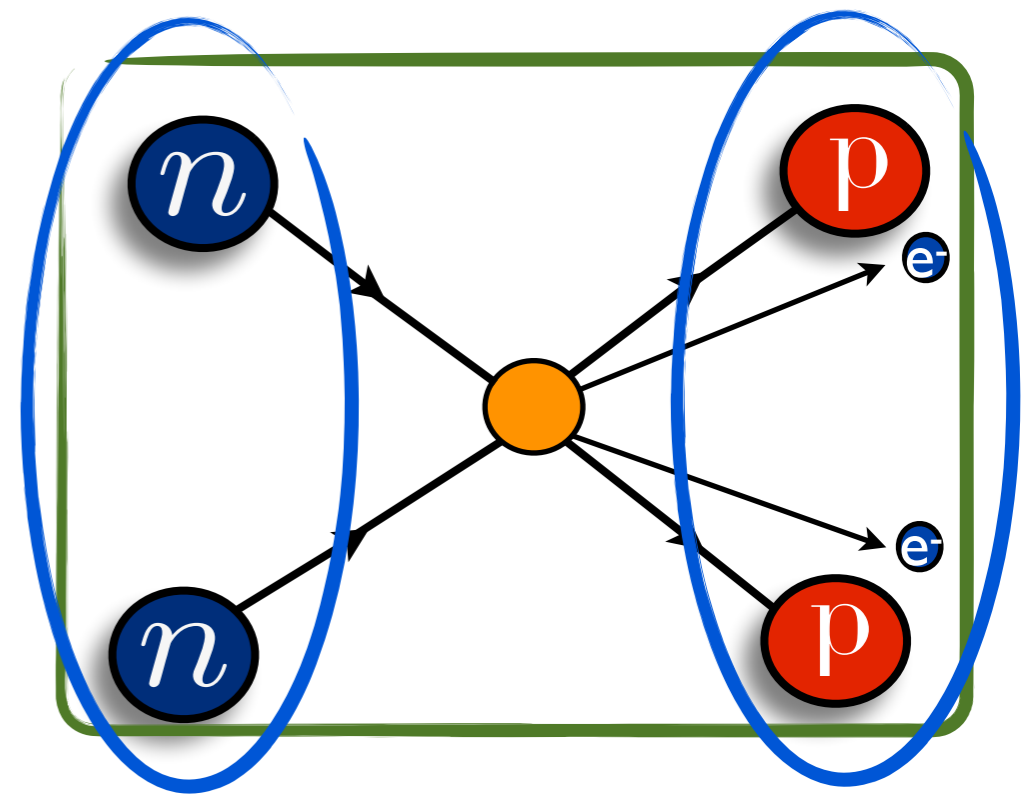


Preliminary



3.

Two-nucleon contact



- Some new developments:
 - Exponentially improved NN operators will allow us to lower the pion mass
 - HOBET in a periodic box
 - more direct path from finite volume lattice results to nuclear many-body techniques (with W. Haxton and K. McElvain)
- Results to come!



Summary

- LQCD can be used as a step toward connecting experimental signals to BSM models
- Nucleon axial charge
 - LQCD calculations are becoming reliably accurate and precise
 - Can be extended to calculate g_A quenching effects
- $\pi^- \rightarrow \pi^+ 0\nu\beta\beta$ matrix element
 - Complete LQCD calculation at the physical point of leading short-range contribution
 - To do: Plug the results into your favorite many-body calculation!
- Two-nucleon contact
 - Testing new method for two nucleon operators
 - Machinery in place for calculating 3-point function
 - Advances in calculating light neutrino contributions may lead to calculation of non-perturbative NN amplitudes

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- LLNL: P. Vranas
- NERSC: T. Kurth
- Jülich: E. Berkowitz
- BNL: E. Rinaldi
- nVidia: M.A. Clark
- JLab: B. Joo
- Plymouth: N. Garron
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