

# NEW OBSERVABLES IN QUARKONIUM PRODUCTION

## ACCESSING DOUBLE PARTON SCATTERINGS WITH ASSOCIATED-QUARKONIUM PRODUCTION



**J.P. Lansberg**

IPN Orsay – Paris-Sud U. –CNRS/IN2P3 – Université Paris-Saclay  
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# Part I

## Introduction

# Approaches to (Inclusive) Quarkonium Production

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  - 3 COLOUR OCTET MECHANISM (encapsulated in NRQCD): **higher Fock states** of the mesons taken into account;  $Q\bar{Q}$  can be produced in octet states with different quantum # as the meson; bleaching with semi-soft gluons ?

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- However, as we will now see, **these offer new ways to study DPS**

## Part II

# New observables in quarkonium production

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See section 3 of JPL, arXiv:1903.09185 [hep-ph]

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$J/\psi+J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CS dominant) + DPS + gluon TMD
$J/\psi+D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to $J/\psi$ fragmentation) + DPS
$J/\psi+\Upsilon$	D0	(N)LO	LO ?	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi+\text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi+Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi+W$	ATLAS	LO	NLO	NLO (?)	Prod. Mechanism (CO dominant) + DPS
$J/\psi$ vs mult.	ALICE, CMS (+UA1)	--	--	--	
$J/\psi+b$	-- (LHCb, D0, CMS ?)	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$\Upsilon+D$	LHCb	LO	LO ?	LO	DPS
$\Upsilon+\gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
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JPL, H.-S. Shao PRL 111, 122001 (2013); PLB 751 (2015) 479; CMS JHEP 1409 (2014) 094; ATLAS EPJC (2017) 77:76

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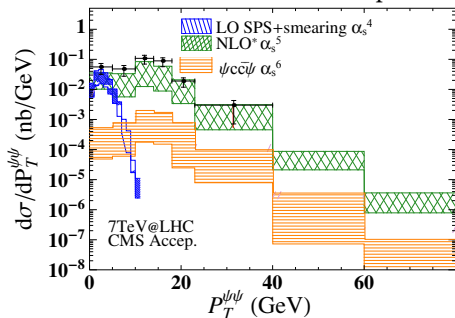
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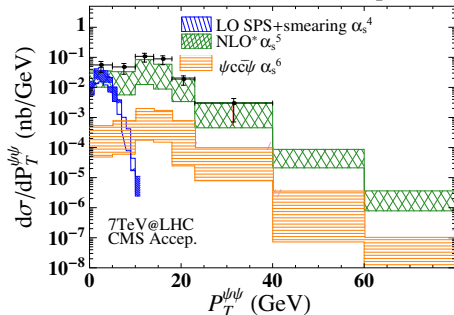
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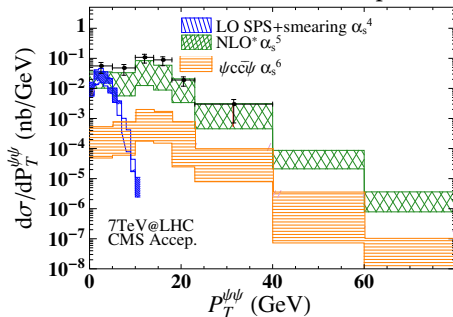


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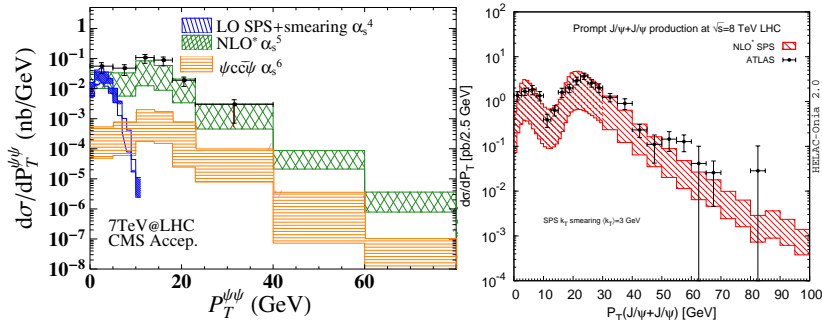


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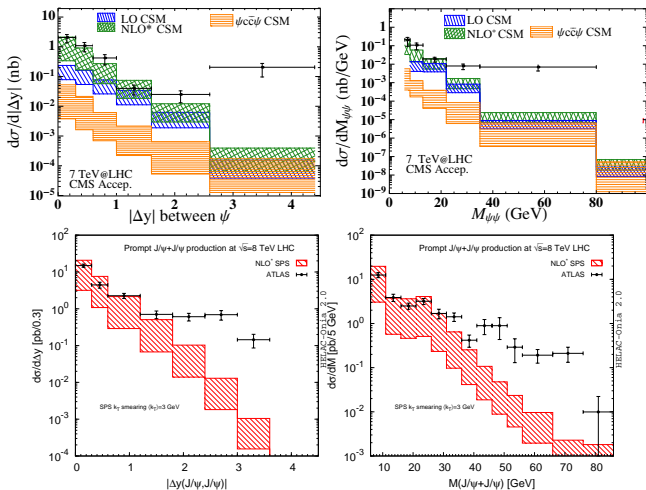
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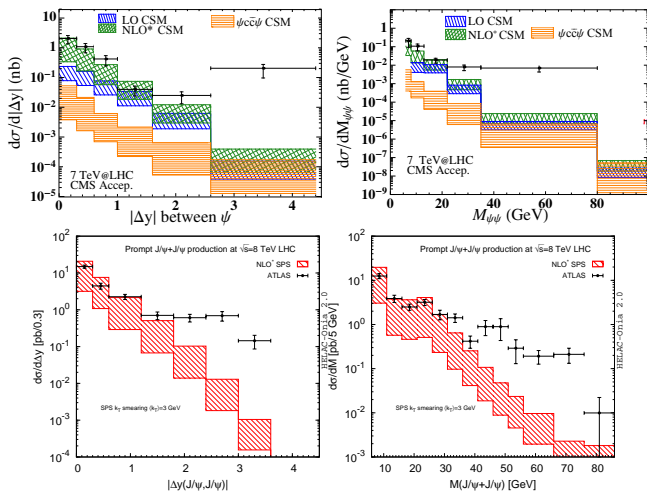


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The most natural solution for this excess is the independent production of two  $J/\psi$

→ double parton scattering



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NB: Agreement not perfect with the ATLAS kinematical distributions  
(yet bins at large  $M_{\psi\psi}$  and  $\Delta y$  contain very few events)

# Predictions: excited states and more

JPL, H.-S. Shao PLB 751 (2015) 479; JPL 1903.09185



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	(CSM) SPS	Low $P_T$ DPS	High $P_T$ DPS
$F_{\psi\psi}^{\psi'}$	50%	15%	15%
$F_{\psi\psi}^{\chi_c}$	small	25%	50%

- Based on up-to-date feed-down values ( $J/\psi$  is **80% direct at low  $P_T$** )

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- $J/\psi + \eta_c$  can also tell something about DPS and about  $\sigma_{\text{eff}}$

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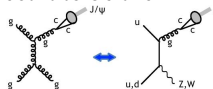
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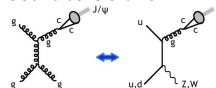
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ATLAS inclusive	$1.6 \pm 0.4$	$0.10^{+0.03}_{-0.03}$	$0.19^{+0.05}_{-0.04}$	0.46

The theoretical uncertainty for the (N)LO SPS is from the renormalisation and factorisation scales. All quantities are in units of pb.

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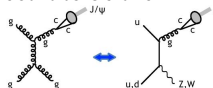
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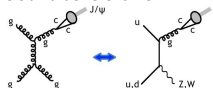
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- However presence of a **peak at  $\Delta\phi = \pi$**  in the azimuthal spectrum

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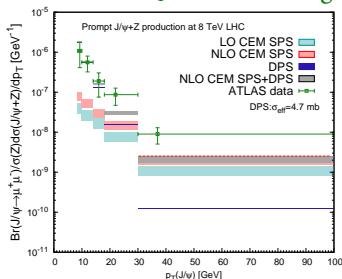


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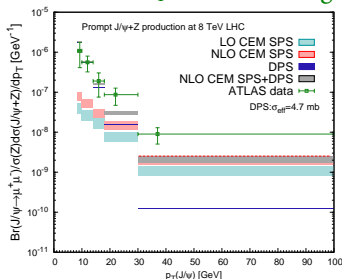
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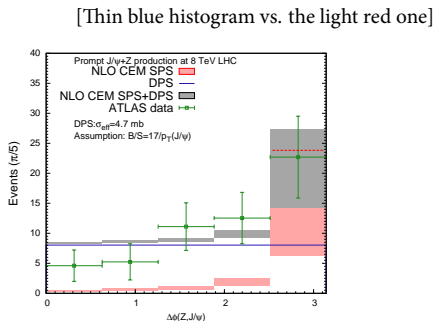
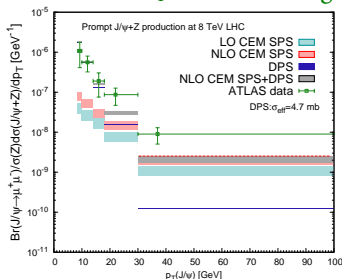
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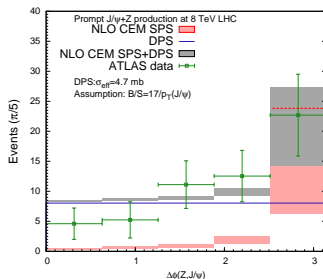
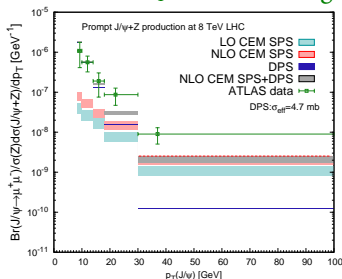
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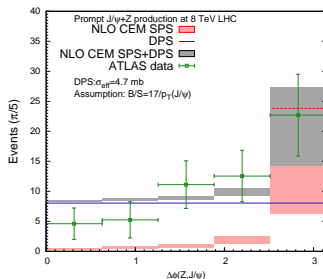
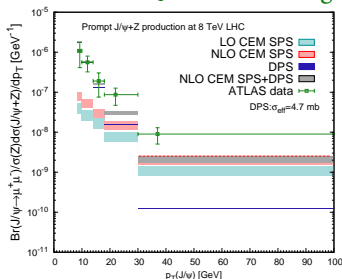
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- We are waiting for an ATLAS update to confirm our explanation

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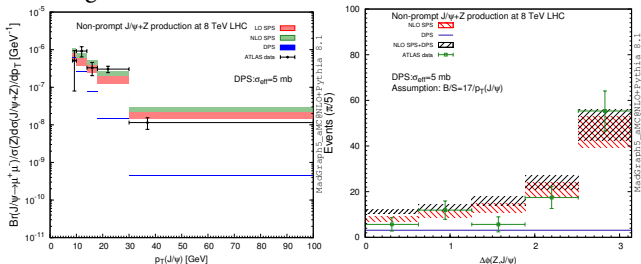
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- Interesting check that nothing went wrong with the prompt analysis
- SPS predictions were absent at the time of the publication. We filled this gap in the literature using MADGRAPH5\_AMC@NLO and PYTHIA 8.1.



Differential cross section/distributions for non-prompt  $J/\psi + Z$  production:  $p_T$  distribution of  $J/\psi$  (left) and azimuthal angle distribution (right)

- **Good agreement.** Owing to the data uncertainties at low  $P_T$ , we cannot constrain  $\sigma_{\text{eff}}$  more than with a **lower limit, 5.0 mb**, at 68 % CL.

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	exp	LO CEM SPS	NLO CEM SPS	DPS ( $\sigma_{\text{eff}} \simeq 15 \text{ mb}$ )
ATLAS inclusive	$4.5^{+1.9}_{-1.5} \text{ pb}$	$0.16 \pm 0.05$	$0.28 \pm 0.07$	1.7

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- we obtain (for the cross section)

	exp	LO CEM SPS	NLO CEM SPS	DPS ( $\sigma_{\text{eff}} \simeq 15 \text{ mb}$ )
ATLAS inclusive	$4.5^{+1.9}_{-1.5} \text{ pb}$	$0.16 \pm 0.05$	$0.28 \pm 0.07$	1.7

The theoretical uncertainty for the (N)LO SPS is from the renormalisation and factorisation scales. All quantities are in units of pb.

- This gives a  **$2+\sigma$  discrepancy** without DPS contribution. The discrepancy rises up to  $3+\sigma$  with the differential x-section: **evidence for DPS** (see next)
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# Our re-analysis of $W+\text{prompt } J/\psi$ at NLO and with DPS

- Similarly to  $Z+\text{prompt } J/\psi$ , **significant tensions** between the ATLAS measurement and the SPS NRQCD yields: normalisation,  $P_T$  and  $\Delta\phi$  distributions

ATLAS Collaboration, JHEP 1404 (2014) 172  
L. Gang et al., PRD 83 (2011) 014001  
J.P. Lansberg, C. Lorce, PLB 726 (2013) 218

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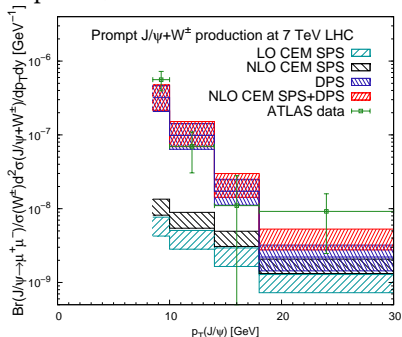
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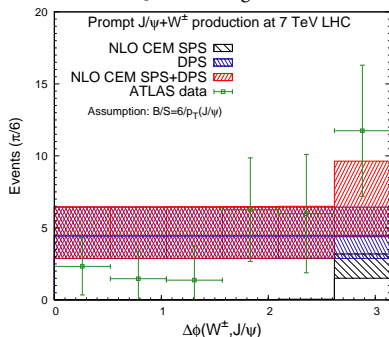
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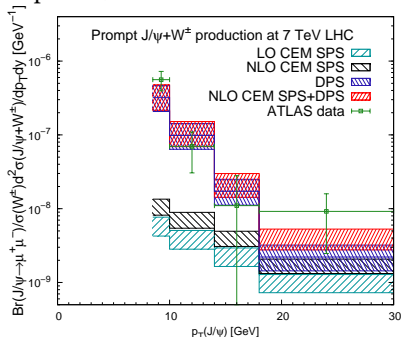
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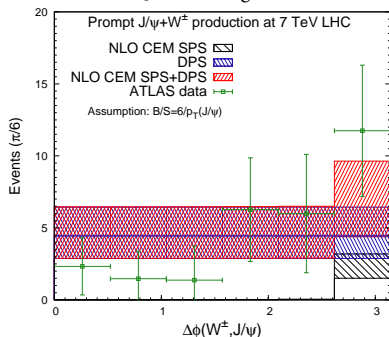
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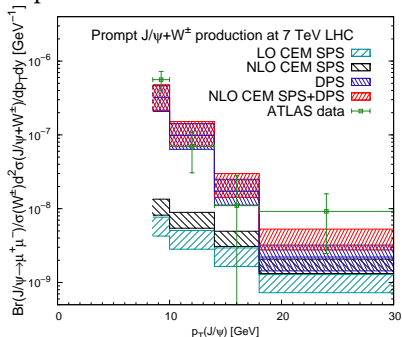
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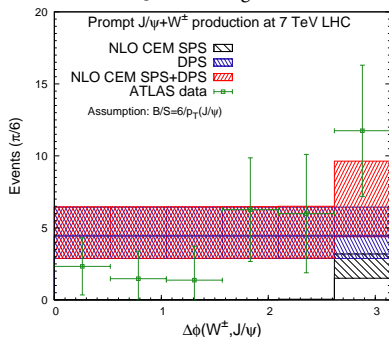
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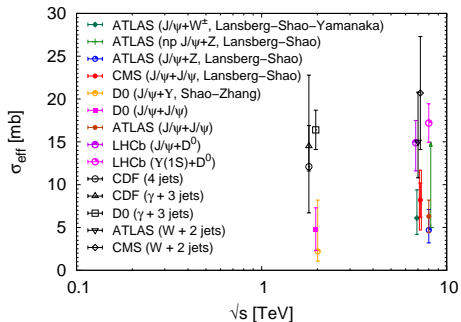
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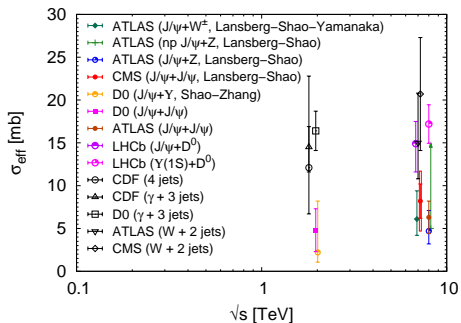
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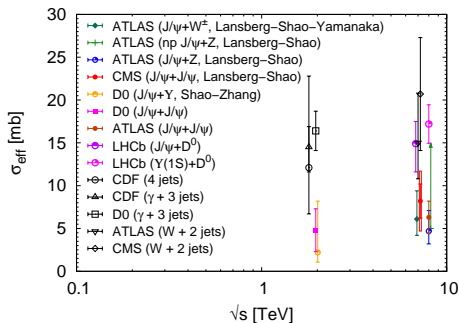


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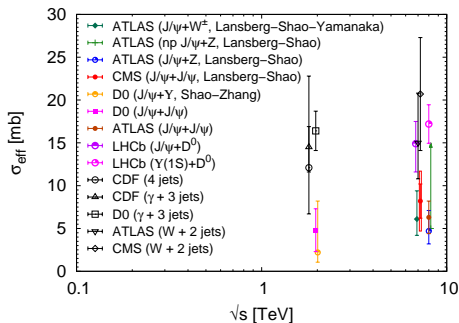
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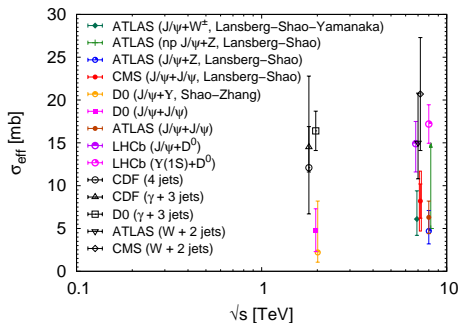
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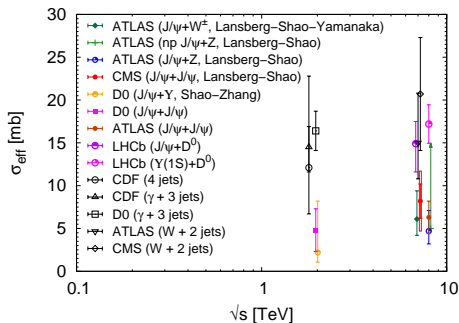
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D0 PRL 116 (2016) 082002 + H.S. Shao - Y. J. Zhang PRL 117 (2016) 062001

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- Except for both LHCb extractions, all the quarkonium-based extraction point at very small  $\sigma_{\text{eff}}$  values: dependence on the flavour, the rapidity or the scale(s) ?

# Part III

## Conclusion

# Summary



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- Beside the production-mechanism debate, quarkonia already allow us to probe the parton correlation through DPS studies
- They also start to tell us new information on the gluon Transverse Momentum Distribution distributions

e.g. JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217

## NLOAccess

Virtual Access: Automated perturbative NLO calculations for heavy ions and quarkonia (NLOAccess)

[General description](#) [Participants](#) [Tasks](#) [Links and resources](#)

### GENERAL DESCRIPTION

#### Objectives:

NLOAccess will give access to automated tools generating scientific codes allowing anyone to evaluate observables -such as production rates or kinematical properties - of scatterings involving hadrons. The automation and the versatility of these tools are such that these scatterings need not to be pre-coded. In other terms, it is possible that a random user may request for the first time the generation of a code to compute characteristics of a reaction which nobody thought of before. NLOAccess will allow the user to test the code and then to download to run it on its own computer. It essentially gives access to a dynamical library.

[Show more](#)

This project has been included in the STRONG2020 submission for EU funding.

🔍 To search type and hit enter



## Automated perturbative NLO calculation with HELAC-Onia Web

### Welcome to HELAC-Onia Web!

HELAC-Onia is an automatic matrix element generator for the calculation of the heavy quarkonium helicity amplitudes in the framework of NRQCD factorization. The program is able to calculate helicity amplitudes of multi P-wave quarkonium states production at hadron colliders and electron-positron colliders by including new P-wave off-shell currents. Besides the high efficiencies in computation of multi-leg processes within the Standard Model, HELAC-Onia is also sufficiently numerical stable in dealing with P-wave quarkonia and P-wave color-octet intermediate states.

Already registered to the portal? Please login.

Do you not have an account? Make a registration request.

# Part IV

## Backup



# CEM vs. CSM vs. COM in a little more details

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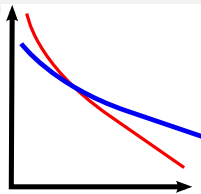
## 3 COLOUR OCTET MECHANISM

- one non-perturbative parameter per Fock State
- expansion in  $v^2$ ; series can be truncated
- the phenomenology partly depends on this
- HQSS relates some non-perturbative parameters to each others and to a specific quarkonium polarisation

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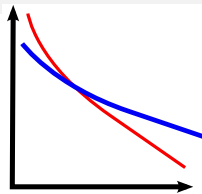
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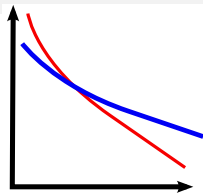
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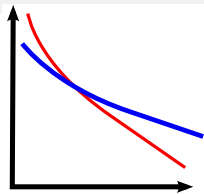


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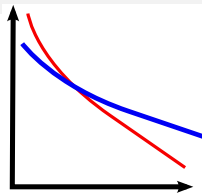
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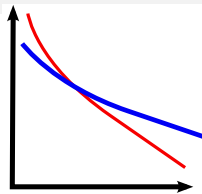
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- Polarisation:  ${}^1S_0^{[8]}$  : unpolarised;  ${}^3S_1^{[8]}$  &  ${}^3P_J^{[8]}$  : transverse



$\psi$  data: a little less hard than the blue curve

# QCD corrections to the CEM $P_T$ dependence

JPL, H.S. Shao JHEP 1610 (2016) 153

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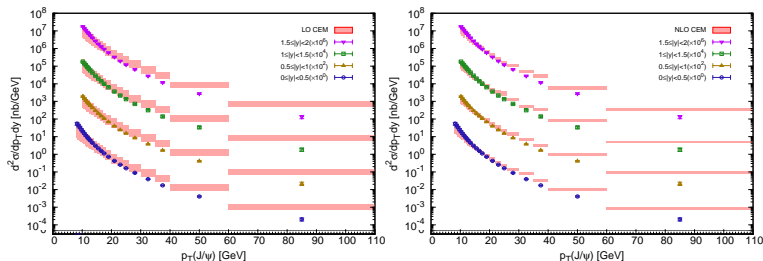
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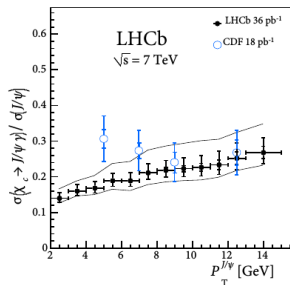
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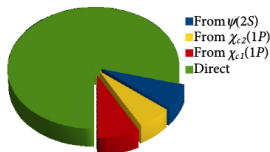


# Feed downs from the excited states

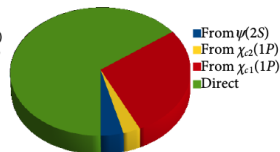
JPL, arXiv:1903.09185 [hep-ph]



(a)



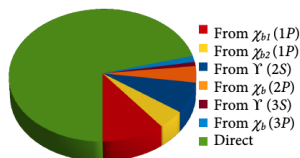
(b) Low  $P_T$   $J/\psi$



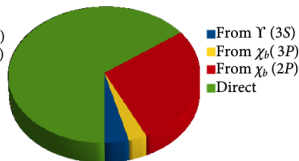
(c) High  $P_T$   $J/\psi$

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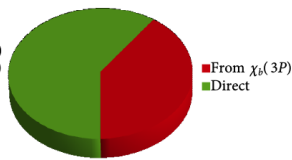
JPL, arXiv:1903.09185 [hep-ph]



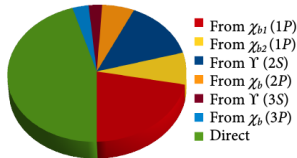
(a) Low  $P_T$   $\Upsilon(1S)$



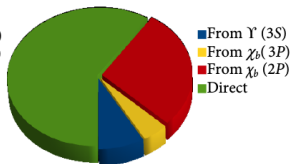
(b) Low  $P_T$   $\Upsilon(2S)$



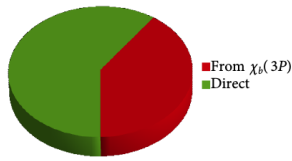
(c) Low  $P_T$   $\Upsilon(3S)$



(d) High  $P_T$   $\Upsilon(1S)$



(e) High  $P_T$   $\Upsilon(2S)$



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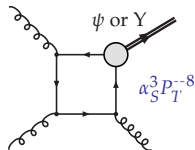
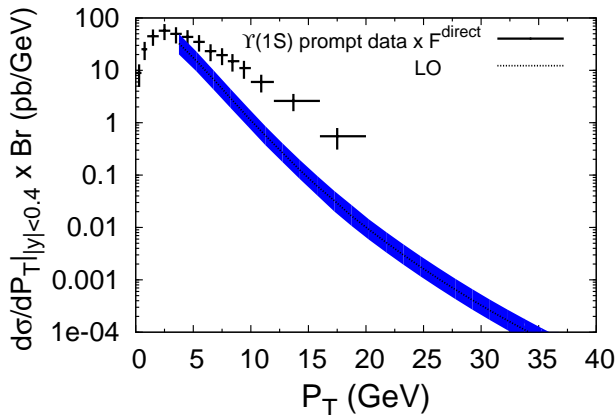
# QCD corrections to the CSM for $\Upsilon$ at colliders

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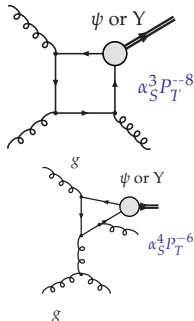
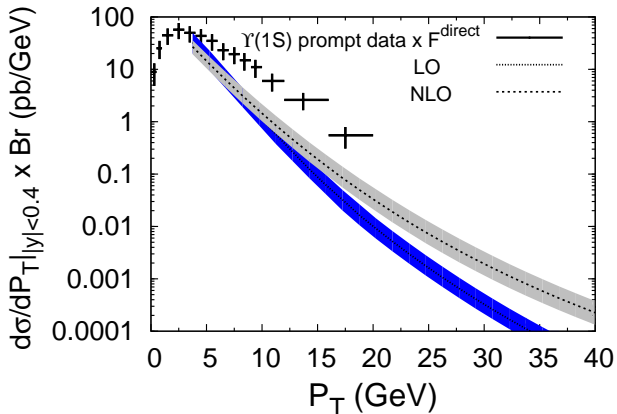
P.Artoisenet, J.Campbell, JPL, F.Maltoni, F. Tramontano, Phys. Rev. Lett. 101, 152001 (2008)

CDF PRL 88 (2002) 161802; LHCb EPJC 72 (2012) 2025



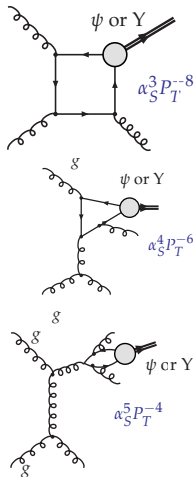
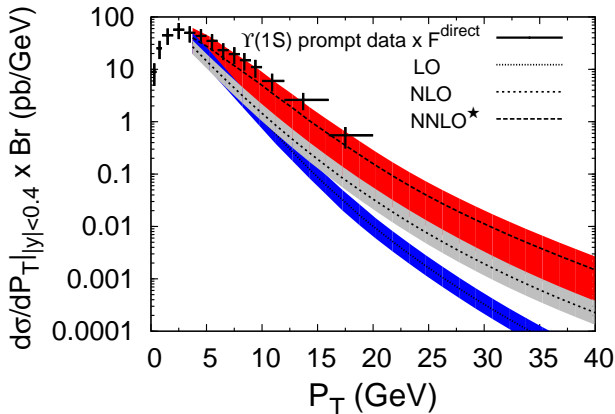
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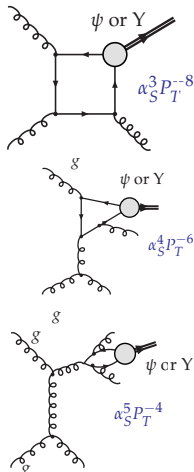
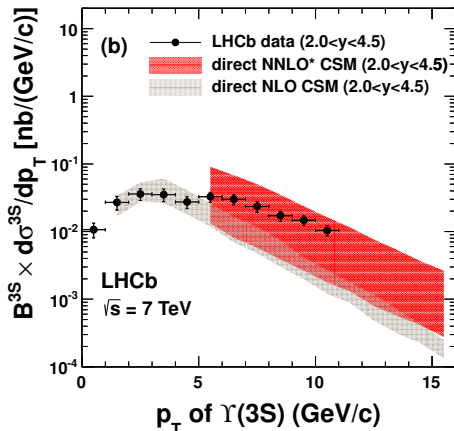


Attention: the NNLO\* is not a complete NNLO  
 See a recent study by H.S. Shao JHEP 1901 (2019) 112



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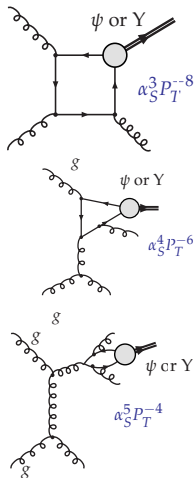
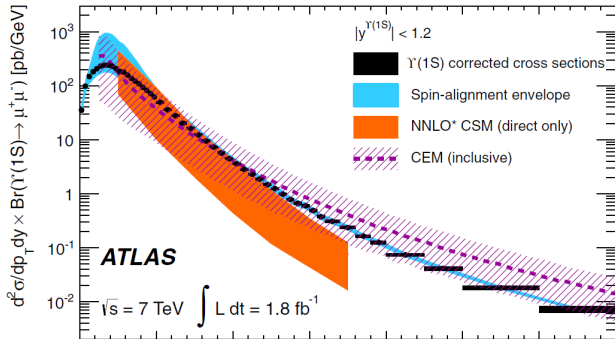
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$\Upsilon(3S)$ : 60 % direct;  $\Upsilon(2S)$ : 60-70 % direct;  $\Upsilon(1S)$ : 50-70 % direct

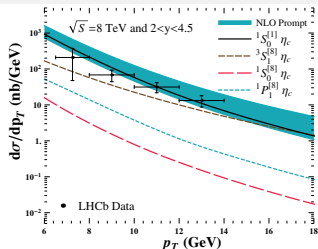
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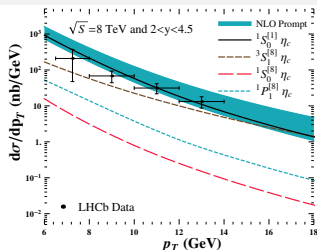
CSM theory curve extrapolated to prompt:  $\times 2$

# The last piece in the puzzle: the $\eta_c$



Data LHCb : EPJC 75 (2015) 311 (plot from H. Hanet *et al.* PRL 114 (2015) 092005)

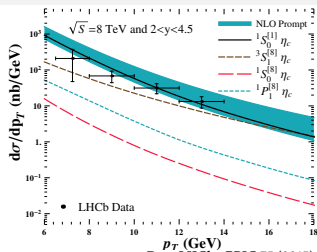
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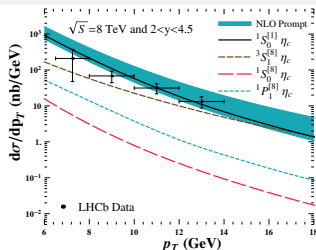


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via Heavy-Quark Spin Symmetry :  $\langle J/\psi (1S_0^{[8]}) \rangle = \langle \eta_c (3S_1^{[8]}) \rangle < 1.46 \times 10^{-2} \text{ GeV}^3$

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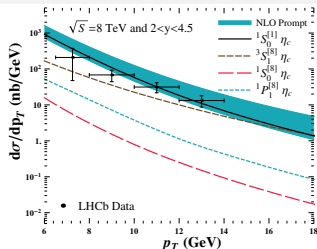


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JPL, H.S. Shao, H.F. Zhang, PLB 786 (2018) 342



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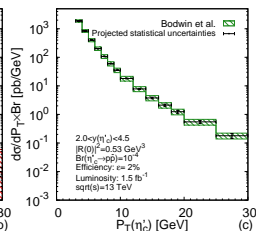
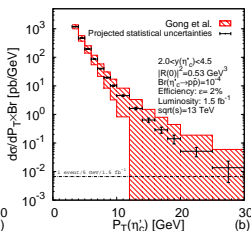
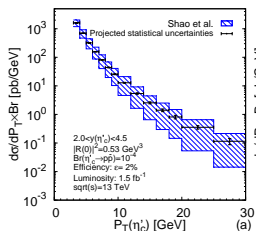
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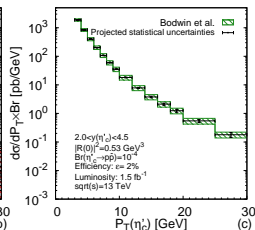
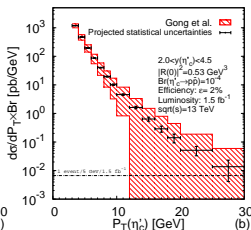
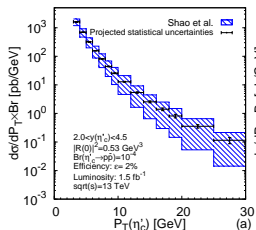
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→ Belle-II data on the inclusive  $\psi(2S)$  production will also be crucial



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## On the importance of understanding low- $P_T$ production

- If color is bleaching at short distances (Color Singlet Model), low- $P_T$  quarkonia can be used to extract the distribution of **linearly polarised gluon in unpolarised protons**,  $h_1^{\perp g}(x, k_T, \mu)$  D. Boer, C. Pisano, PRD 86 (2012) 094007
- Different **nuclear suppression** depending on how the pair hadronizes J.W. Qiu, J. P. Vary, X.F. Zhang, PRL 88 (2002) 232301
- **Saturation effects** depend on the colour state of the propagating pair D. Kharzeev, *et al.* PRL 102 (2009) 152301; F. Dominguez, *et al.* PLB 710 (2012) 182; Y.Q. Ma, *et al.* PRD 92 (2015) 071901
- Most of the proton-nucleus and nucleus-nucleus collision data lie at  $P_T \lesssim m_Q$
- In the QGP, do quarkonia behave more like colorful gluons  
or colorless photons ?
- If regeneration is at work, how does it happen ? statistically ? according to the charm-quark distribution in the charmonium (wave-function) ?
- etc ...

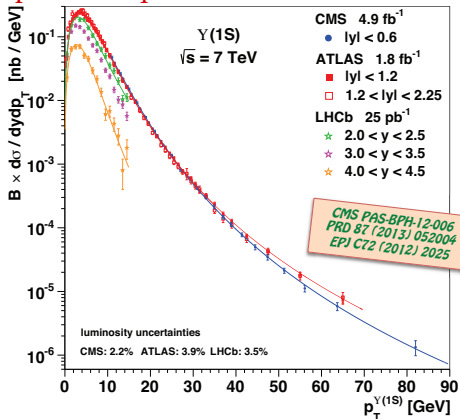
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Also because, some very high  $P_T$  quarkonia which we study can be **as rare as a few millionth of the produced quarkonia**



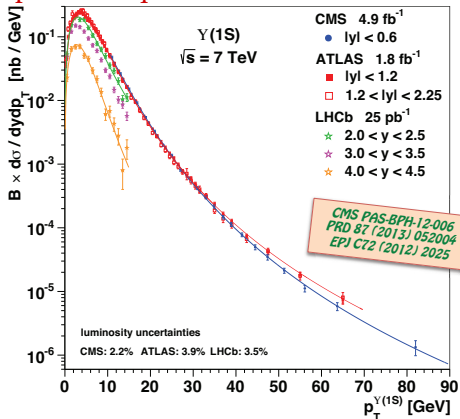
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Most probably the production of a  $Y$  with  $P_T = 90 \text{ GeV}$ , even also  $20 \text{ GeV}$ , has very few things to do with the bulk of  $Y$

# Comparison with the new LHCb data at 13 TeV

LHCb JHEP06(2017)047

$\sigma(\psi\psi)$ nb	no $P_T$ cut	$P_T > 1$ GeV	$P_T > 3$ GeV
NLO* CS	$15.4 \pm 2.2^{+51}_{-12}$	$14.8 \pm 1.7^{+53}_{-12}$	$6.8 \pm 0.6^{+22}_{-5}$
NLO CS	$11.9^{+4.6}_{-3.2}$	—	—
DPS [ $\sigma_{\text{eff}} = 14.5 \pm 1.7^{+1.7}_{-2.3}$ mb]	$8.1 \pm 0.9^{+1.6}_{-1.3}$	$7.5 \pm 0.8^{+1.5}_{-1.2}$	$4.9 \pm 0.5^{+1.0}_{-0.8}$
Data	$15.2 \pm 1.0 \pm 0.9$	$13.5 \pm 0.9 \pm 0.9$	$8.3 \pm 0.6 \pm 0.5$

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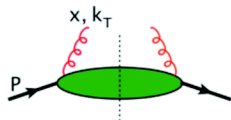
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- **Agreement** between CSM NLO and data
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- **REMINDER:** it is not an option to "switch off"/ignore the NLO CS contribution [parameter free]
- Yet, **room for DPS**; however tension if  $\sigma_{\text{eff}} \simeq 7$  mb
- **Tension between LHCb and other di- $J/\psi$  extractions** [rapidity effect ?]

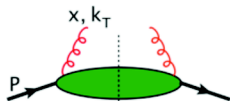
# Gluon TMDs in unpolarised protons



# Gluon TMDs in unpolarised protons

- Gauge-invariant definition:

$$\Phi_g^{\mu\nu}(x, \mathbf{k}_T, \zeta, \mu) \equiv \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + k_T) \cdot \xi} \langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]} F^{n\mu}(\xi) \mathcal{U}'_{[\xi, 0]} | P \rangle \Big|_{\xi \cdot P' = 0}$$

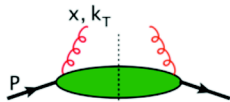


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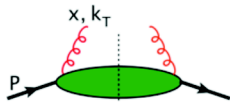
- Parametrisation:

$$\Phi_g^{\mu\nu}(x, \mathbf{k}_T, \zeta, \mu) = -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g(x, k_T, \mu) - \left( \frac{k_T^\mu k_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{\mathbf{k}_T^2}{2M_p^2} \right) h_1^{\perp g}(x, k_T, \mu) \right\} + \text{suppr.}$$

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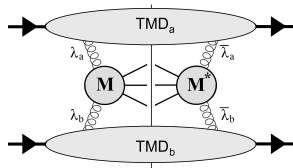
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- $f_1^g$ : TMD distribution of **unpolarised** gluons
- $h_1^{\perp g}$ : TMD distribution of **linearly polarised** gluons

[Helicity-flip distribution]

# $gg$ fusion in arbitrary unpolarised process [colourless final state]

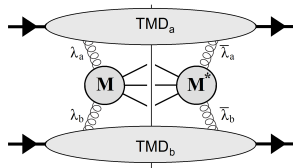
$$d\sigma^{gg} \propto$$



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$$d\sigma^{gg} \propto \underbrace{F_1}_{\lambda_a, \lambda_b} \left( \sum_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b}^* \right) \mathcal{C}[f_1^g f_1^g]$$

$\Rightarrow$  helicity non-flip, azimuthally independent



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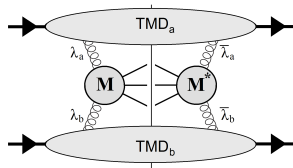
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$$\underbrace{\left( \sum_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b}^* \right)}_{F_1} \mathcal{C}[f_1^g f_1^g]$$

$\Rightarrow$  helicity non-flip, **azimuthally independent**

$$+ \underbrace{\left( \sum_{\lambda} \hat{\mathcal{M}}_{\lambda, \lambda} \hat{\mathcal{M}}_{-\lambda, -\lambda}^* \right)}_{F_2} \mathcal{C}[w_0 \times h_1^{\perp g} h_1^{\perp g}]$$

$\Rightarrow$  double helicity flip, **azimuthally independent**



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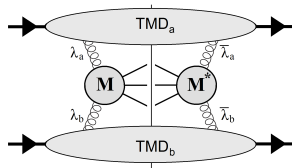
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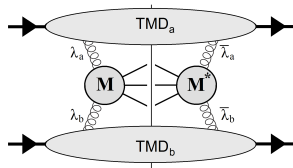
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None are measured so far ...

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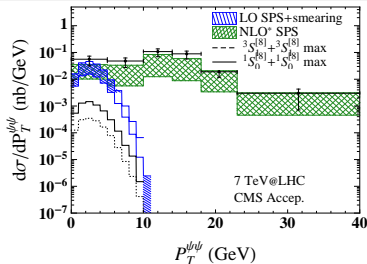
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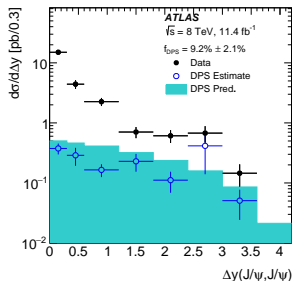
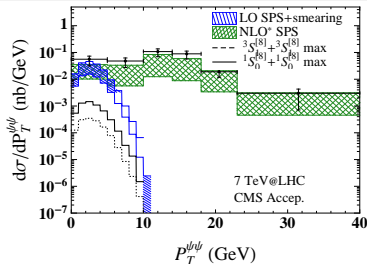
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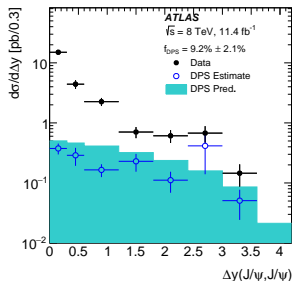
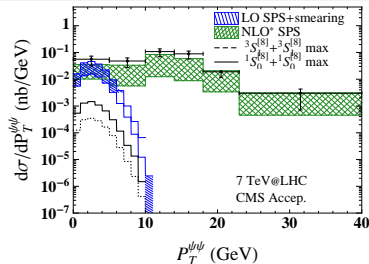
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- DPS in LHCb data [kinematical distributions well controlled : independent scatterings]



# What's special about double vector onium production ?

JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217



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$$F_4 = F_1 \text{ at large } M_{QQ}$$

$\Rightarrow$  di- $J/\psi$  (or di- $\Upsilon$ ) **maximise** the observability of **cos 4 $\phi$**  modulations  
in a kinematical region where **data are already taken** !

# TMD modelling : $f_1^g$ and the relevance of the LHCb data

JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217

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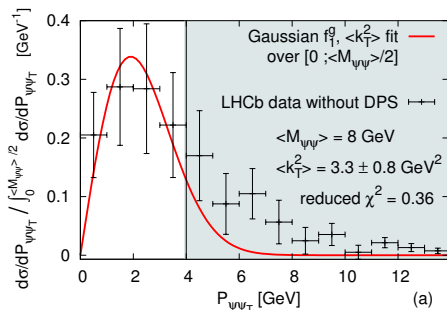
JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217

- $f_1^g$  modelled as a Gaussian in  $\vec{k}_T$  :  $f_1^g(x, \vec{k}_T^2) = \frac{g(x)}{\pi \langle k_T^2 \rangle} \exp\left(\frac{-\vec{k}_T^2}{\langle k_T^2 \rangle}\right)$   
where  $g(x)$  is the usual collinear PDF
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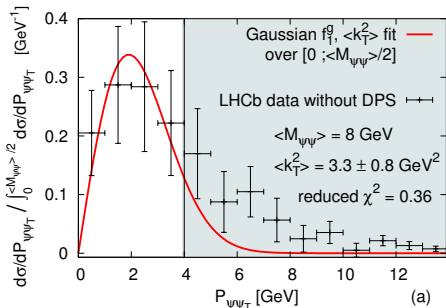
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by fitting  $\mathcal{C}[f_1^g f_1^g]$  over the normalised LHCb  $d\sigma/dP_{\psi\psi_T}$  spectrum at 13 TeV  
from which we have subtracted the DPS yield determined by LHCb



# TMD modelling : $f_1^g$ and the relevance of the LHCb data

JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217

- $f_1^g$  modelled as a Gaussian in  $\vec{k}_T$  :  $f_1^g(x, \vec{k}_T^2) = \frac{g(x)}{\pi \langle k_T^2 \rangle} \exp\left(\frac{-\vec{k}_T^2}{\langle k_T^2 \rangle}\right)$   
where  $g(x)$  is the usual collinear PDF
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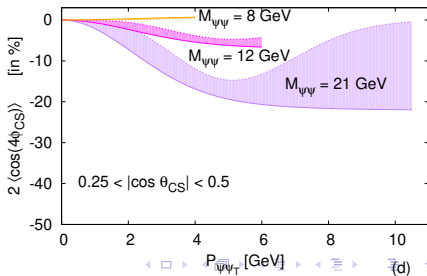
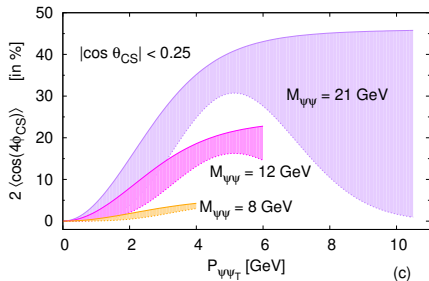
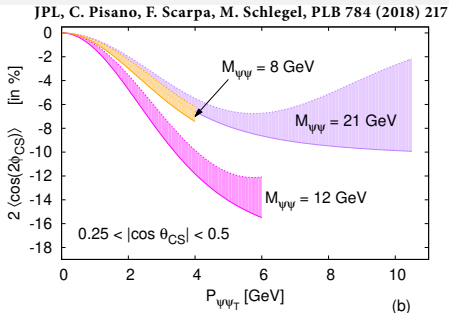
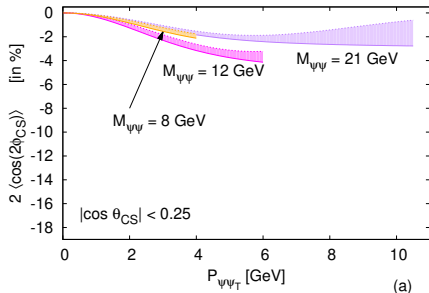
- Integration over  $\phi \Rightarrow \cos(n\phi)$ -terms cancel out
- $F_2 \ll F_1 \Rightarrow$  only  $\mathcal{C}[f_1^g f_1^g]$  contributes to the cross-section
- No evolution so far:  $\langle k_T^2 \rangle \sim 3 \text{ GeV}^2$   
accounts both for non-perturbative and perturbative broadenings at a scale close to  $M_{\psi\psi} \sim 8 \text{ GeV}$
- Disentangling such (non-)perturbative effects requires **data at different scales**

# Expected azimuthal asymmetries

JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784 (2018) 217



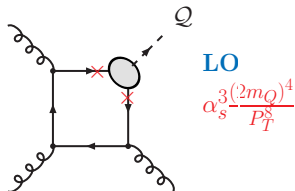
# Expected azimuthal asymmetries



# Basic pQCD approach: the Colour Singlet Model (CSM)

C.-H. Chang, NPB172, 425 (1980); R. Baier & R. Rückl Z. Phys. C 19, 251(1983);

⇒ Perturbative creation of 2 quarks  $Q$  and  $\bar{Q}$  BUT

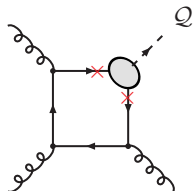


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- ⇒ in a  $^3S_1$  state (for  $J/\psi$ ,  $\psi'$  and  $\Upsilon$ )



LO

$$\alpha_s^3 \frac{(2m_Q)^4}{P_T^8}$$

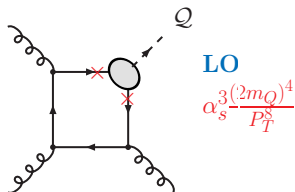
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⇒ Non-perturbative binding of quarks



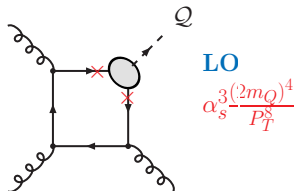
→ Schrödinger wave function

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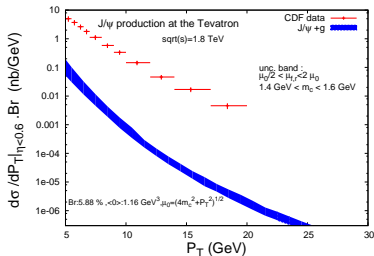
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⇒ Non-perturbative binding of quarks

→ Schrödinger wave function



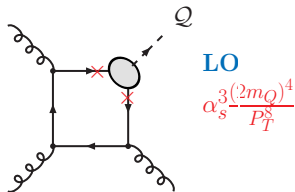
CDF, PRL 79:572 & 578,1997

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C.-H. Chang, NPB172, 425 (1980); R. Baier & R. Rückl Z. Phys. C 19, 251(1983);

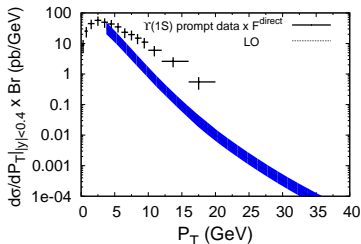
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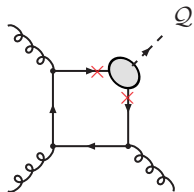
CDF, PRL 88:161802,2002

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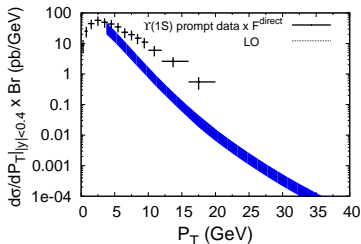


LO

$$\propto_s^3 \frac{(2m_Q)^4}{P_T^8}$$

⇒ Non-perturbative binding of quarks

→ Schrödinger wave function



⇒ Large QCD corrections from new topologies reduce the gap with data at mid and large  $P_T$

# The LO CSM accounts for the $P_T$ -integrated yield

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010; JPL, PoS(ICHEP 2010), 206 (2010); NPA 910-911 (2013) 470

→ The yield vs.  $\sqrt{s}, y$



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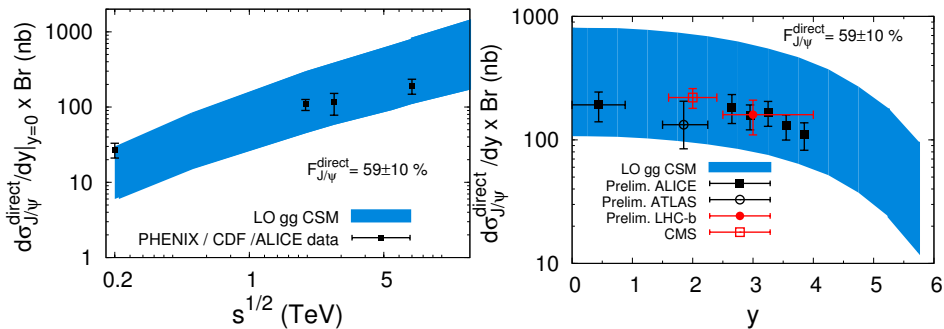
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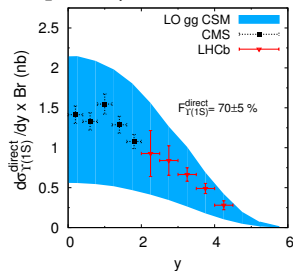


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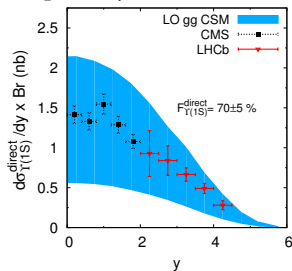
CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

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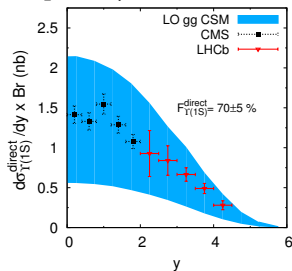
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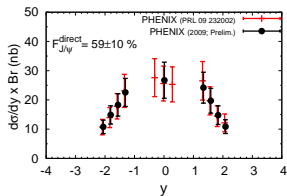
CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

- Unfortunately, very large th. uncertainties: masses, scales ( $\mu_R, \mu_F$ ), gluon PDFs at low  $x$  and  $Q^2, \dots$
- Earlier claims that CSM contribution to  $d\sigma/dy$  was small were based on the **incorrect assumption that  $\chi_c$  feed-down was dominant**

## NLO CSM at RHIC

 $\rightarrow J/\psi$ 

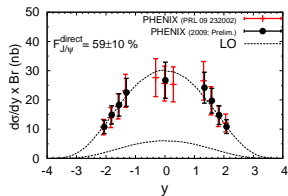
S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.



## NLO CSM at RHIC

 $\rightarrow J/\psi$ 

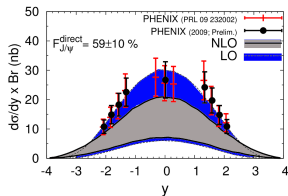
S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.

LO:  $gg \rightarrow J/\psi g$

# NLO CSM at RHIC

→  $J/\psi$

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.



**NLO:**  $gg \rightarrow J/\psi gg, gq \rightarrow J/\psi gq, \dots$

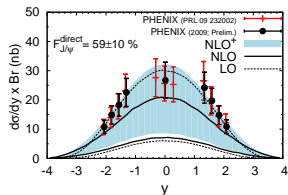
using the matrix elements from J.Campbell, F. Maltoni, F. Tramontano, PRL 98:252002,2007



## NLO CSM at RHIC

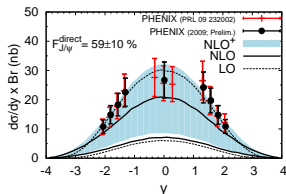
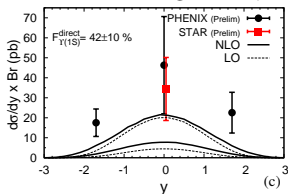
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NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$

## NLO CSM at RHIC

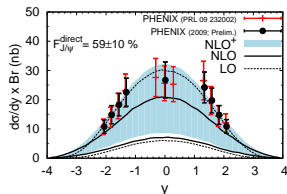
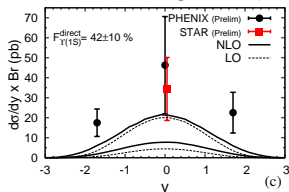
S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.

 $\rightarrow J/\psi$ NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$  $\rightarrow \Upsilon^*$ 

\* Sorry: I should update these plots (updated data and fraction is about 60%)

## NLO CSM at RHIC

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.

 $\rightarrow J/\psi$ NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$  $\rightarrow \Upsilon^*$ 

A priori, good convergence NLO w.r.t. LO

\* Sorry: I should update these plots (updated data and fraction is about 60%)



## Analysis of charmonium production at fixed-target experiments in the NRQCD approach

F. Maltoni<sup>a</sup>, J. Spengler<sup>b</sup>, M. Bargiotti<sup>c</sup>, A. Bertin<sup>c</sup>, M. Bruschi<sup>c</sup>, S. De Castro<sup>c</sup>, L. Fabbri<sup>c</sup>,  
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- At  $\alpha_S^2$ , one only has CO contributions

$$2 \rightarrow 1 \text{ processes} : q + \bar{q} \rightarrow Q\bar{Q}[^3S_1^{[8]}] \text{ and } g + g \rightarrow Q\bar{Q}[^1S_0^{[8]}, ^3P_{J=0,1,2}^{[8]}]$$



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$$g + g \rightarrow Q\bar{Q}[^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{J=0,2}^{[8]}] + g, \quad g + q(\bar{q}) \rightarrow Q\bar{Q}[^1S_8^{[0]}, ^3S_1^{[8]}, ^3P_{J=0,2}^{[8]}] + q(\bar{q})$$

$$q + \bar{q} \rightarrow Q\bar{Q}[^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{J=0,1,2}^{[8]}] + g \text{ and } \mathbf{g + g \rightarrow Q\bar{Q}[^3S_1^{[1]}] + g}$$



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- Done with **NRQCD LDMEs fitted at LO on  $P_T$  spectra from CDF ( $\simeq 2$  TeV)**

Table 1

Reference NRQCD matrix elements for charmonium production. The color-singlet matrix elements are taken from the potential model calculation of [14, 15]. The color-octet matrix elements have been extracted from the CDF data [16] in Ref. [17]

$H$	$\langle \mathcal{O}_8^H \rangle$	$\langle \mathcal{O}_8^H[{}^3S_1] \rangle$	$\langle \mathcal{O}_8^H[{}^1S_0^{(8)}] \rangle = \langle \mathcal{O}_8[{}^3P_0^{(8)}] \rangle / m_c^2$
$J/\psi$	1.16 GeV <sup>3</sup>	$1.19 \times 10^{-2}$ GeV <sup>3</sup>	$1.0 \times 10^{-2}$ GeV <sup>3</sup>
$\psi(2S)$	0.76 GeV <sup>3</sup>	$0.50 \times 10^{-2}$ GeV <sup>3</sup>	$0.42 \times 10^{-2}$ GeV <sup>3</sup>
$\chi_{c0}$	0.11 GeV	$0.31 \times 10^{-2}$ GeV <sup>3</sup>	–



# NLO NRQCD up to RHIC II

## Abstract

We present an analysis of the existing data on charmonium hadro-production based on non-relativistic QCD (NRQCD) calculations at the next-to-leading order (NLO). All the data on  $J/\psi$  and  $\psi(2S)$  production in fixed-target experiments and on  $pp$  collisions at low energy are included. We find that *the amount of color-octet contribution needed to describe the data is about 1/10 of that found at the Tevatron.*

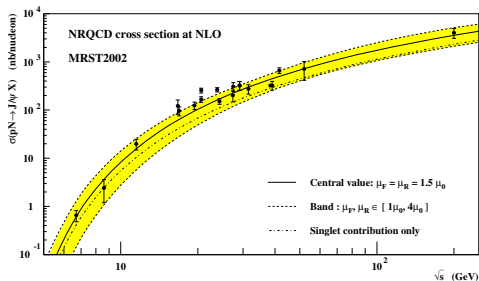
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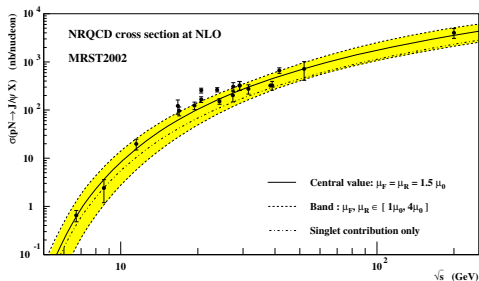


# NLO NRQCD up to RHIC II

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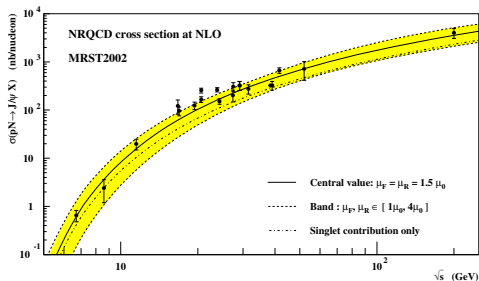
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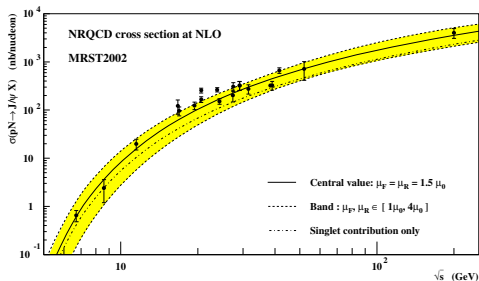
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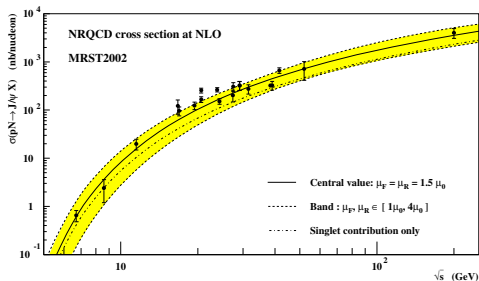
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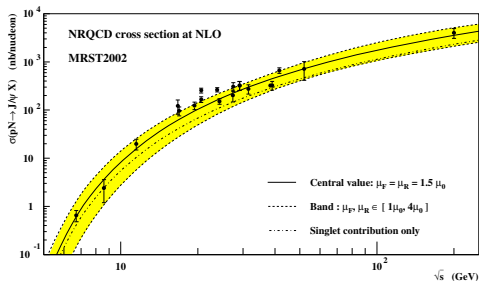
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# What we did

[Y. Feng, JPL, J.X. Wang, EPJC (2015)75:313]

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  - LHC data
- **constant** feed-down (FD) fractions

- $F_{J/\psi}^{\text{direct}} = 60 \pm 10\%$

- $F_{\Upsilon(1S)}^{\text{direct}} = 66 \pm 10\%$

- $F_{\Upsilon(1S+2S+3S)}^{\text{direct}} = 60 \pm 10\%$

- Uncertainty on  $F^{\text{direct}}$  combined in quadrature with that of data

*Arguable but accounts for a possible energy dependence of the FD fraction*

# What we did II

We used LDMEs **fitted at NLO/one loop on the  $P_T$  spectra**

	Ref.	$\langle \mathcal{O}_{J/\psi}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{J/\psi}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{J/\psi}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $J/\psi$	Y.-Q. Ma, <i>et al.</i> PRL 106 (2011) 042002.	$-2.0 \times 10^{-3}$	$7.8 \times 10^{-2}$	0
		$2.1 \times 10^{-2}$	$3.5 \times 10^{-2}$	$5.8 \times 10^{-3}$
		$4.1 \times 10^{-2}$	0	$1.1 \times 10^{-2}$
	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$-2.2 \times 10^{-2}$	$9.7 \times 10^{-2}$	$-4.6 \times 10^{-3}$
	M. Butenschoen, B. Kniehl. PRD (2011) 051501	$-9.1 \times 10^{-2}$	$3.0 \times 10^{-2}$	$1.7 \times 10^{-3}$

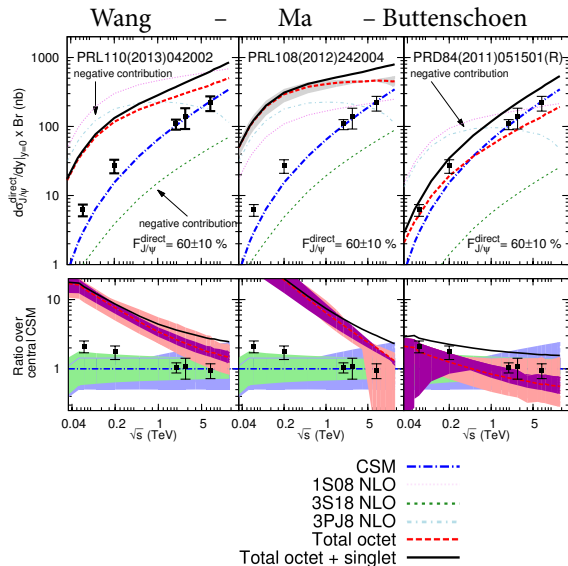
  

	Ref.	$\langle \mathcal{O}_{\psi(2S)}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{\psi(2S)}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{\psi(2S)}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $\psi'$	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$9.5 \times 10^{-3}$	$-1.2 \times 10^{-4}$	$3.4 \times 10^{-3}$
		$-4.8 \times 10^{-3}$	$2.9 \times 10^{-2}$	0
		$7.9 \times 10^{-3}$	$5.6 \times 10^{-3}$	$3.2 \times 10^{-3}$
	Y.-Q. Ma, <i>et al.</i> PRL 106 (2011) 042002	$1.1 \times 10^{-2}$	0	$3.9 \times 10^{-3}$

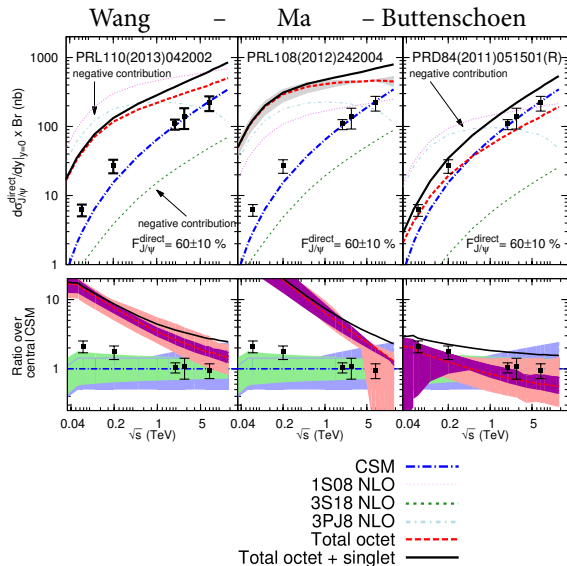
	Ref.	$\langle \mathcal{O}_{\Upsilon(1S)}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{\Upsilon(1S)}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{\Upsilon(1S)}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $\Upsilon(1S)$	B. Gong, <i>et al.</i> PRL 112 (2014) 3, 032001.	$-10.36 \times 10^{-2}$	$11.15 \times 10^{-2}$	$-4.1 \times 10^{-2}$

[We have also added the fit of G.T. Bodwin, *et al.*, PRL 113, 022001 (2014) even though it is based on a fragmentation function approach]

Results for the  $J/\psi$ 

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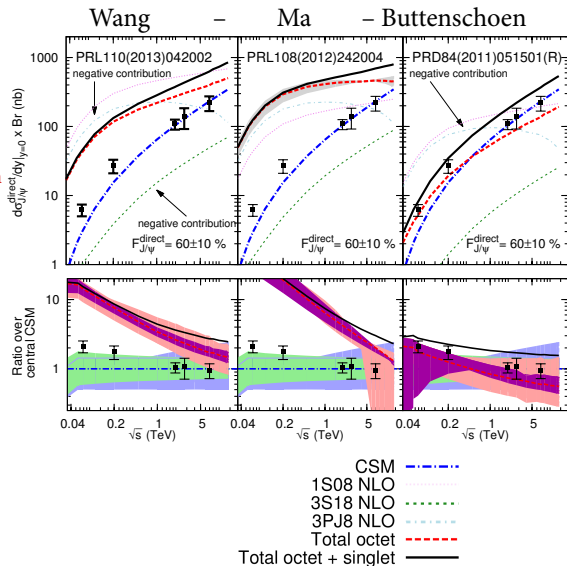
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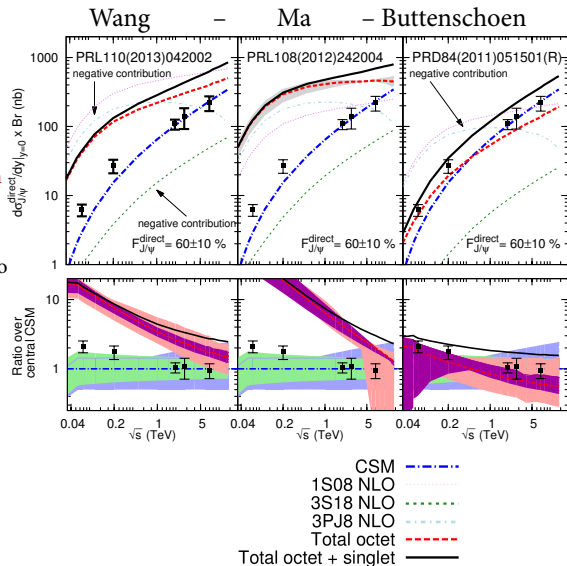
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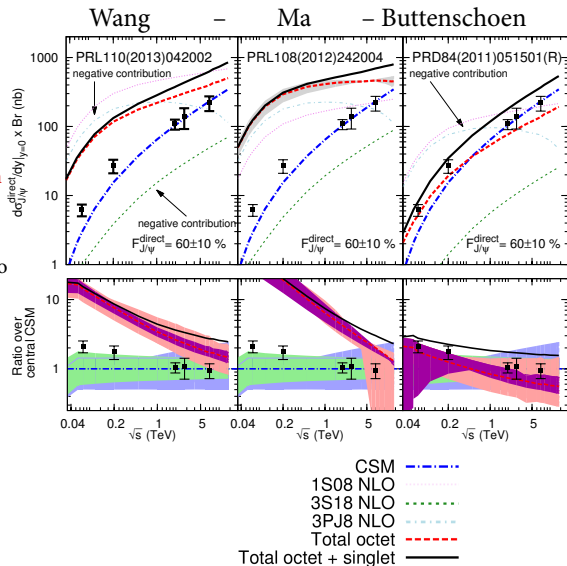
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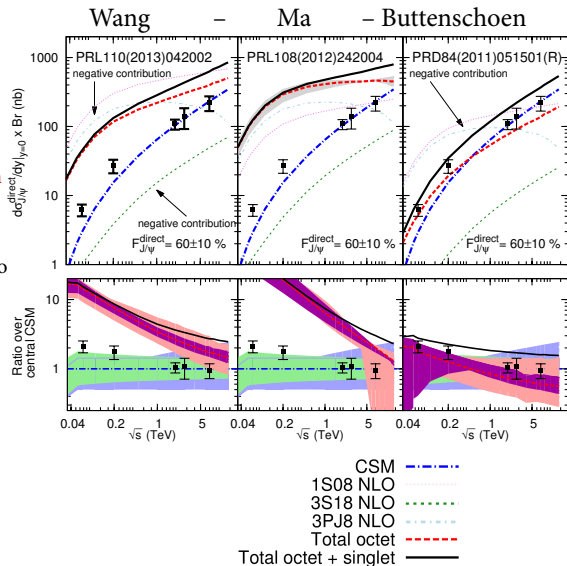
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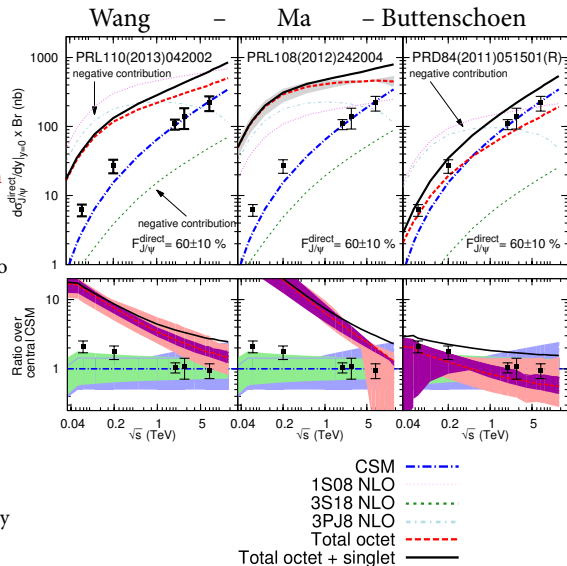
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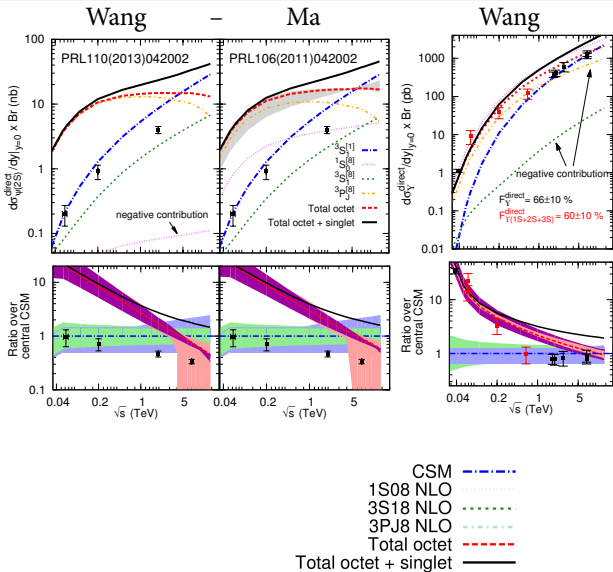
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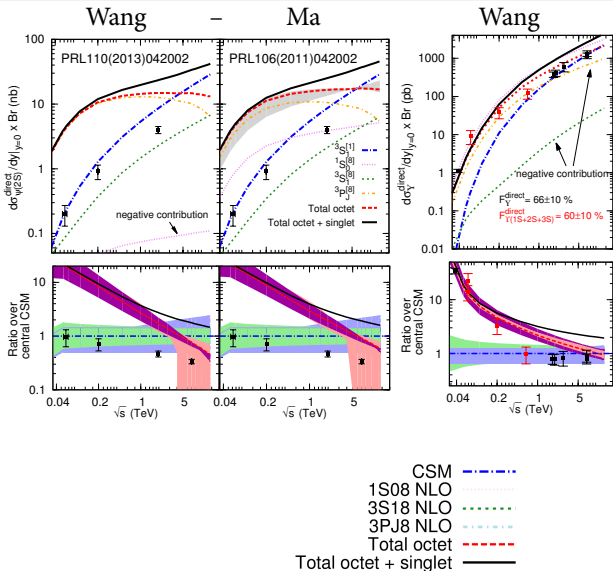
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- Not a surprise since **the CSM alone accounts well for the data**; adding any contribution creates a “surplus”



Results for the  $\psi'$  and  $\Upsilon$ 

Results for the  $\psi'$  and  $\Upsilon$ For  $\psi(2S)$ 

- Worse than for  $J/\psi$
- CSM even tends to overshoot at large  $\sqrt{s}$  – yet in agreement within uncertainties (lower panel)
- CO dominated by the  $^3P_J^{[8]}$  channel which nearly shows an unphysical behavior

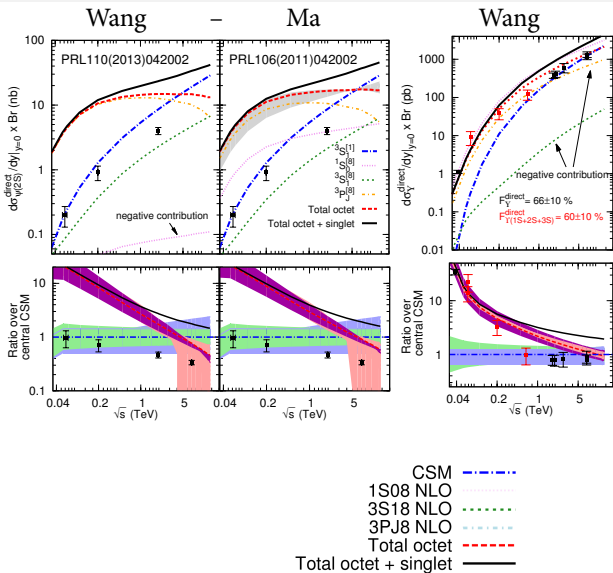


Results for the  $\psi'$  and  $Y$ For  $\psi(2S)$ 

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For  $Y(1S)$ 

- Reasonable trend for  $Y$
- CSM is doing a perfect job in the TeV range – note that the RHIC points moved down
- On the other hand, CO needed at low  $\sqrt{s}$ ? High  $x$  gluon pdf underestimated?





# A glimmer of hope: Low $P_T$ $\chi_{Q1}/\chi_{Q2}$

LHCb, JHEP 10(2013)115 & JHEP 1410 (2014) 88 ; CMS, EPJC, 72, 2257 (2012); ATLAS, JHEP 07(2014)154

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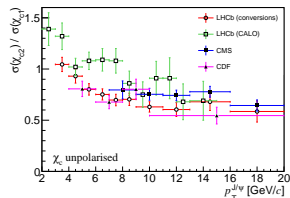
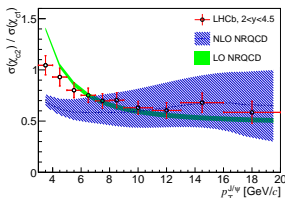
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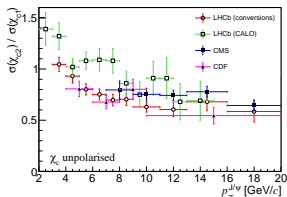
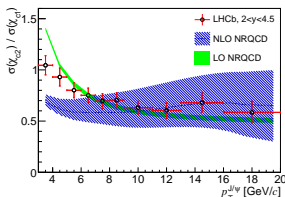


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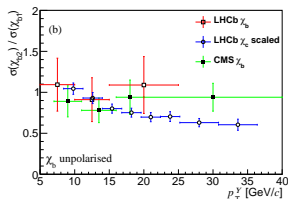
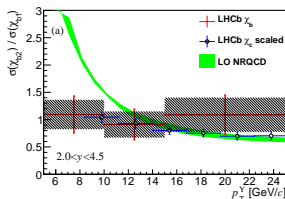
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$\chi_b$

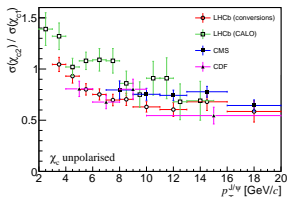
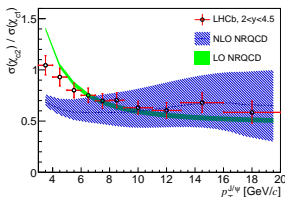


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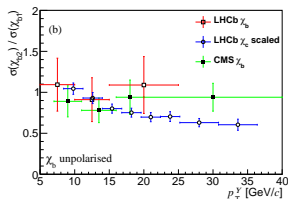
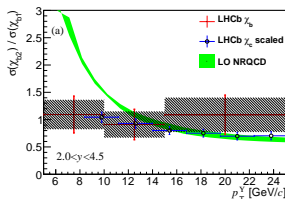
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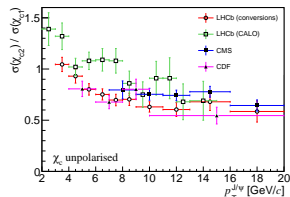
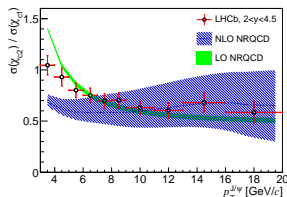
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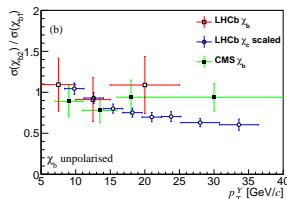
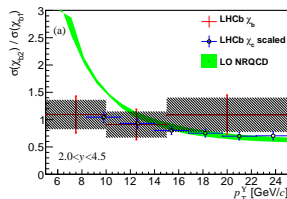
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$\chi_b$



- The Landau-Yang suppression shows up for  $\chi_c$  in the Low  $P_T/m_Q$  region
- The nature (quantum #) of the produced final state seems still relevant !

# Basics of the Colour Evaporation Model

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- Based on Quark-Hadron duality argument, one writes

H. Fritzsch, PLB 67 (1977) 217; F. Halzen, PLB 69 (1977) 105

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M. Bedjidian, [...], R. Vogt *et al.*, hep-ph/0311048

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J. F. Amundson, *et al.* PLB 372 (1996)

$$F_{J/\psi}^{\text{direct}} = \frac{1}{9} \frac{2J_\psi + 1}{\sum_i (2J_i + 1)} = \frac{1}{45},$$

most of the data could accounted for !

- Ramona Vogt's fits roughly give the same number for direct  $J/\psi$ 's

M. Bedjidian, [...], R. Vogt *et al.*, hep-ph/0311048

- It can easily be check by MCFM at NLO for instance

<http://mcfm.fnal.gov/>

# NRQCD Ersatz of the CEM

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$$\begin{aligned}
 \langle \mathcal{O}_{3S_1}(^3S_1^{[1]}) \rangle &= 3 \times \langle \mathcal{O}_{3S_1}(^1S_0^{[1]}) \rangle, \\
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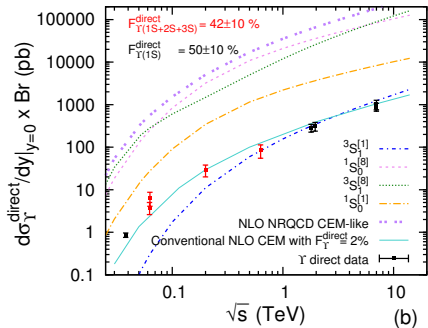
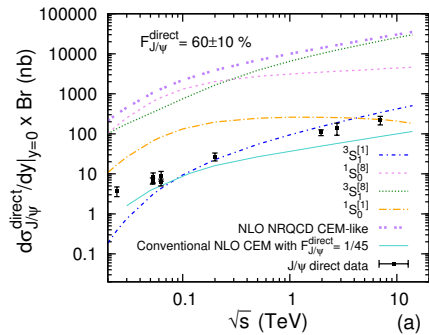
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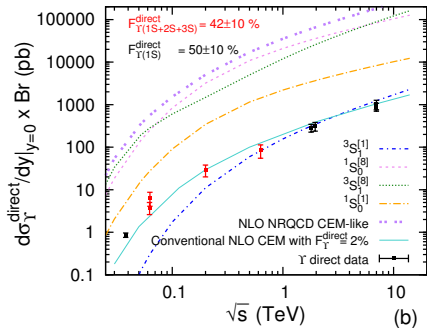
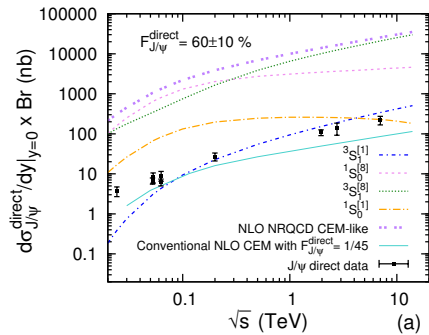
- If, as it should be in NRQCD,  $\langle \mathcal{O}_{3S_1}(^3S_1^{[1]}) \rangle$  is the usual CS LDME, *i.e.*  $\frac{2N_C}{4\pi} (2J+1) |R(0)|^2$ , everything is fixed



## CEM results

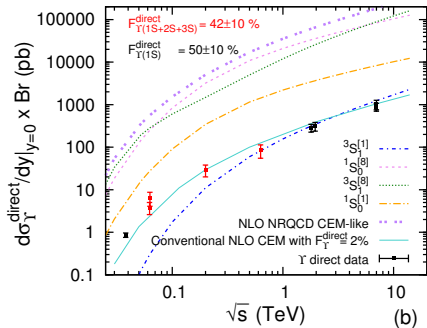
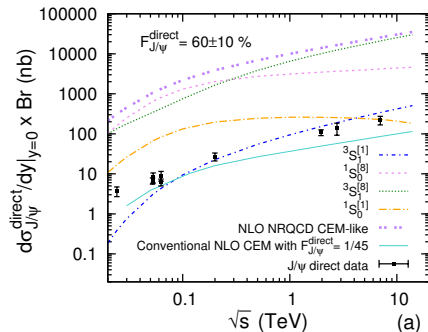


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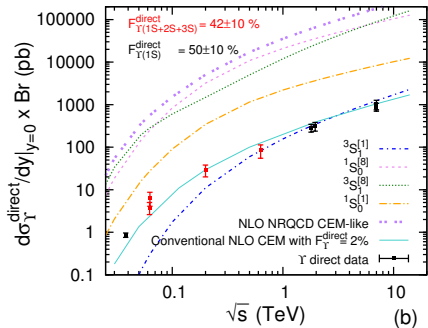
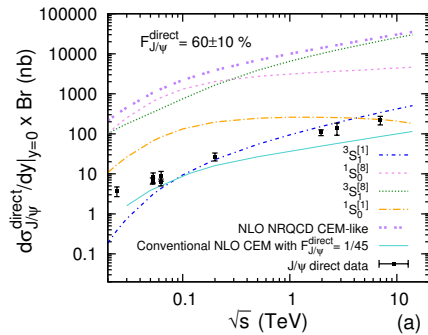
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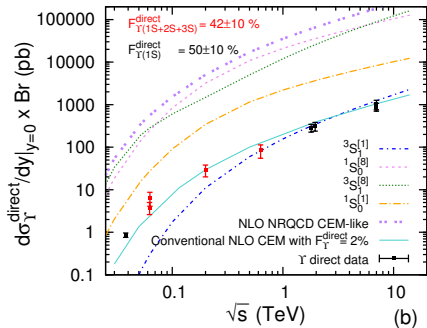
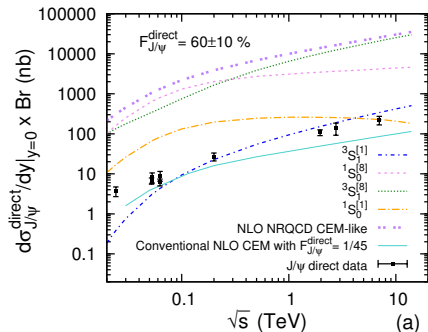
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- NRQCD-like CEM badly overshoots the data
  - Expected since CO LDMEs are as large as the CS, whereas the hard parts tend to be larger.
  - Weird energy behaviour
- Conventional CEM does a pretty good job
  - No th. uncertainty shown
  - “Natural” value of  $F_{J/\psi}^{\text{direct}}$  is ok