



中国科学院大学
University of Chinese Academy of Sciences



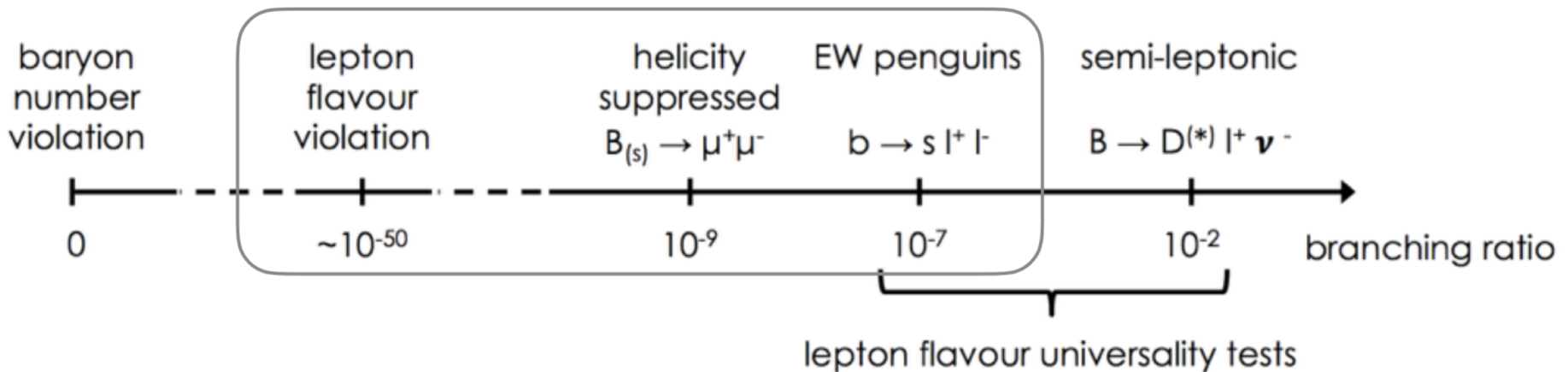
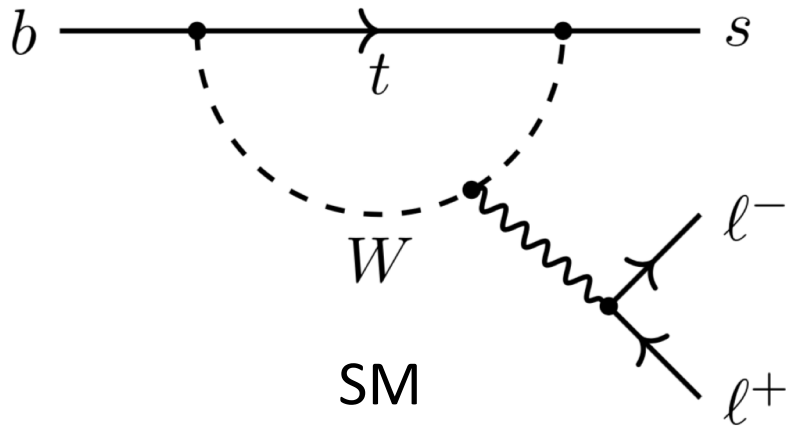
Rare decays & lepton flavor universality test

Jibo HE/何吉波(UCAS)

CLHCP2019 @ 大连理工大学 (DLUT)

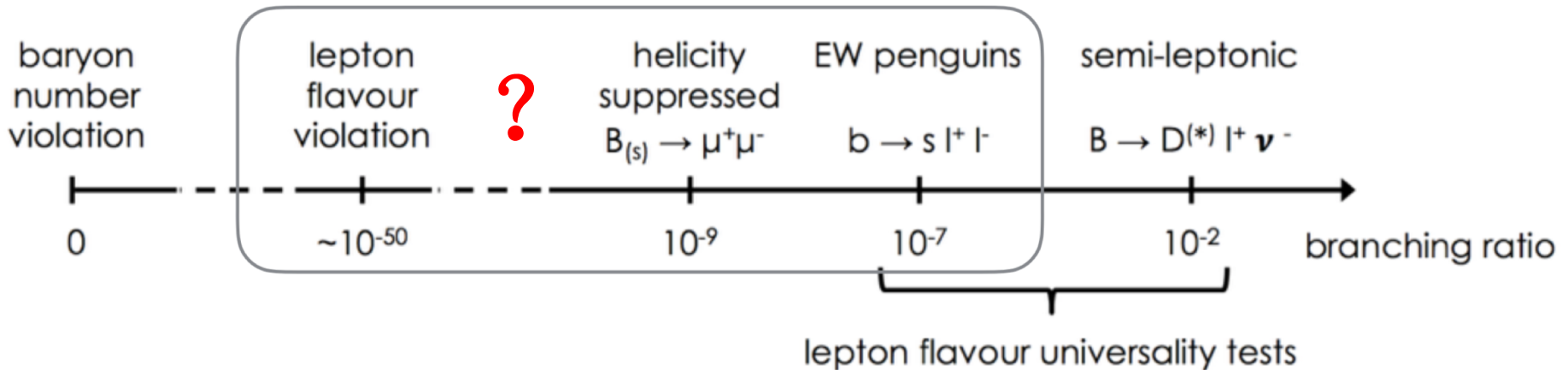
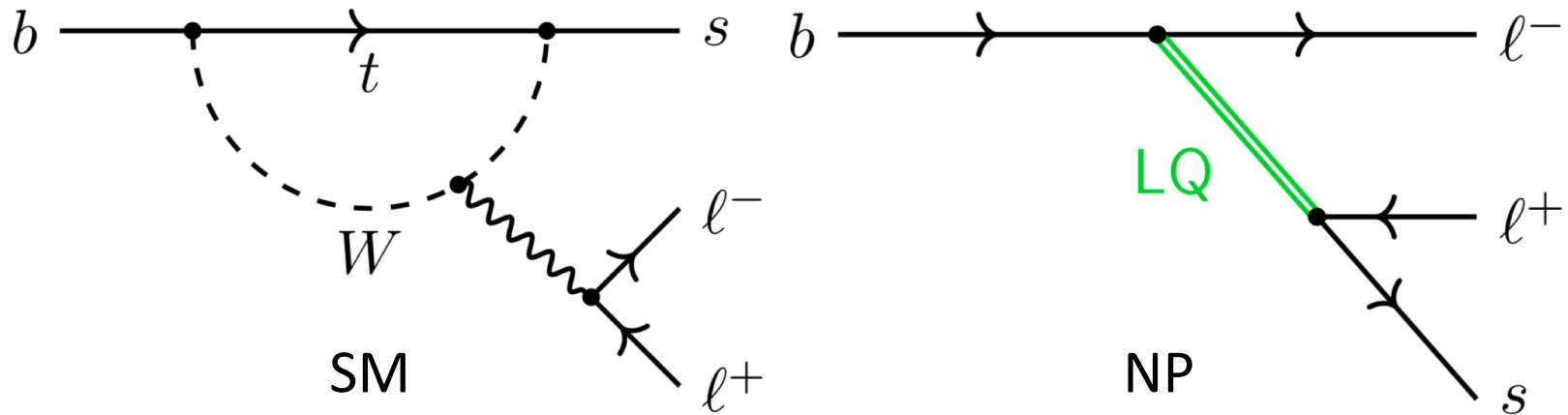
Introduction

- Rare decays: suppressed in SM.



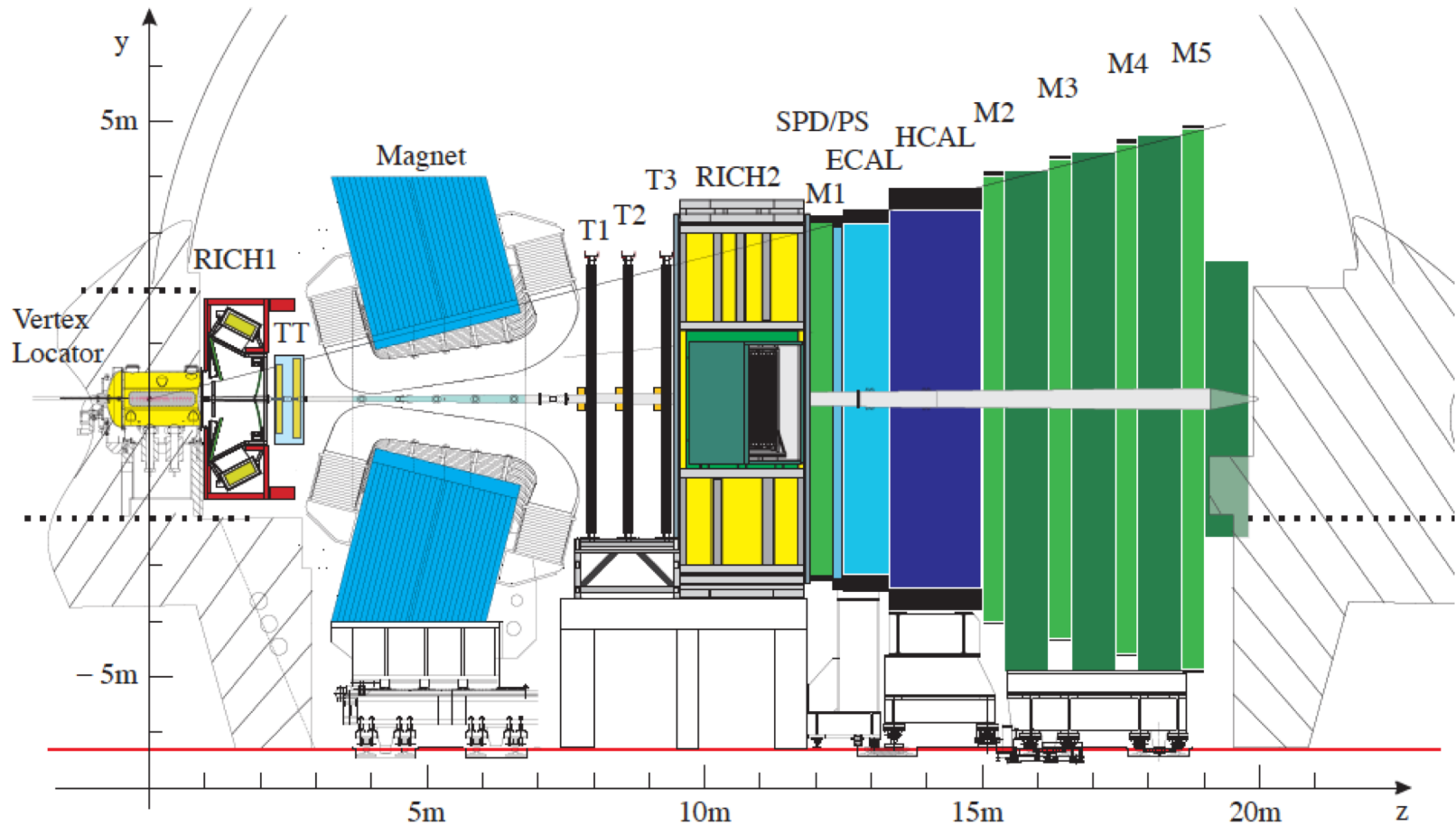
Introduction

- Rare decays: suppressed in SM. **New Physics?**

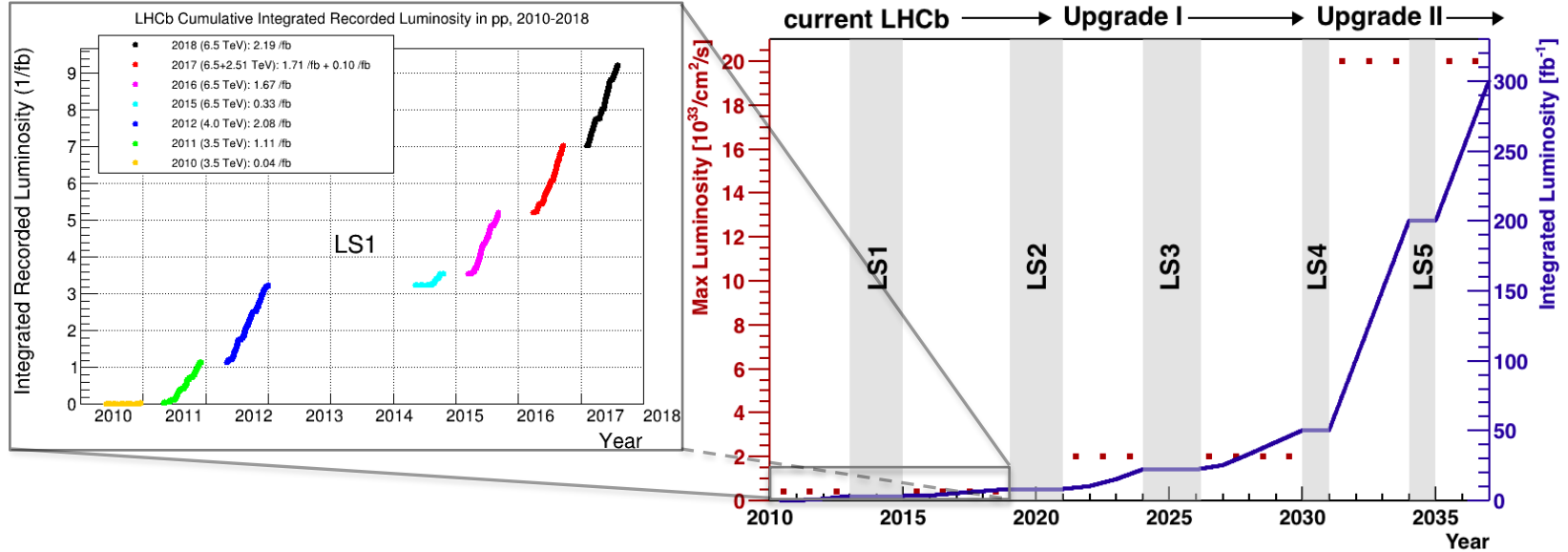


The LHCb experiment

- Dedicated to **precision study** of b/c -hadrons



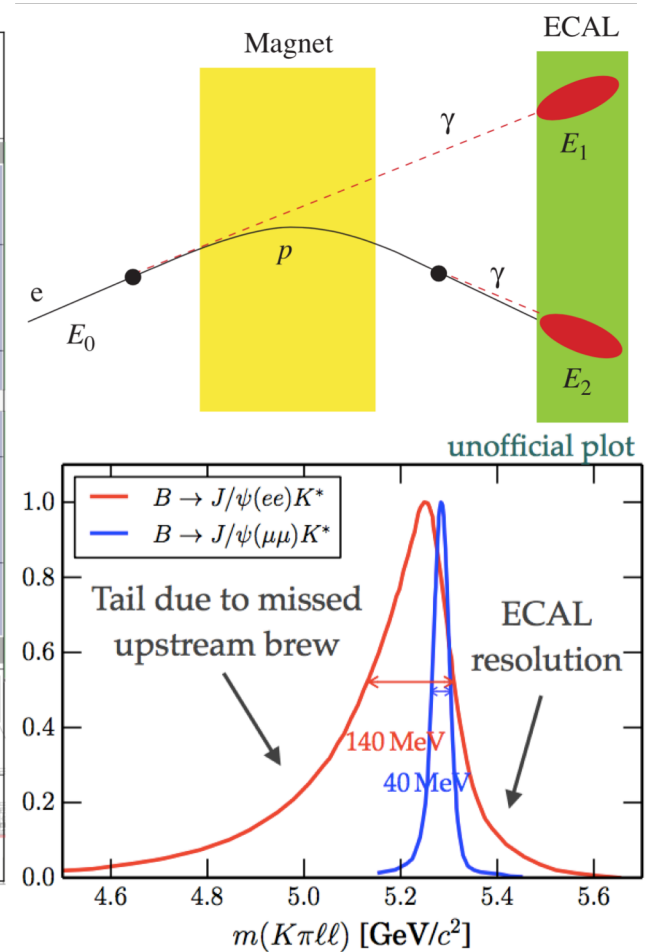
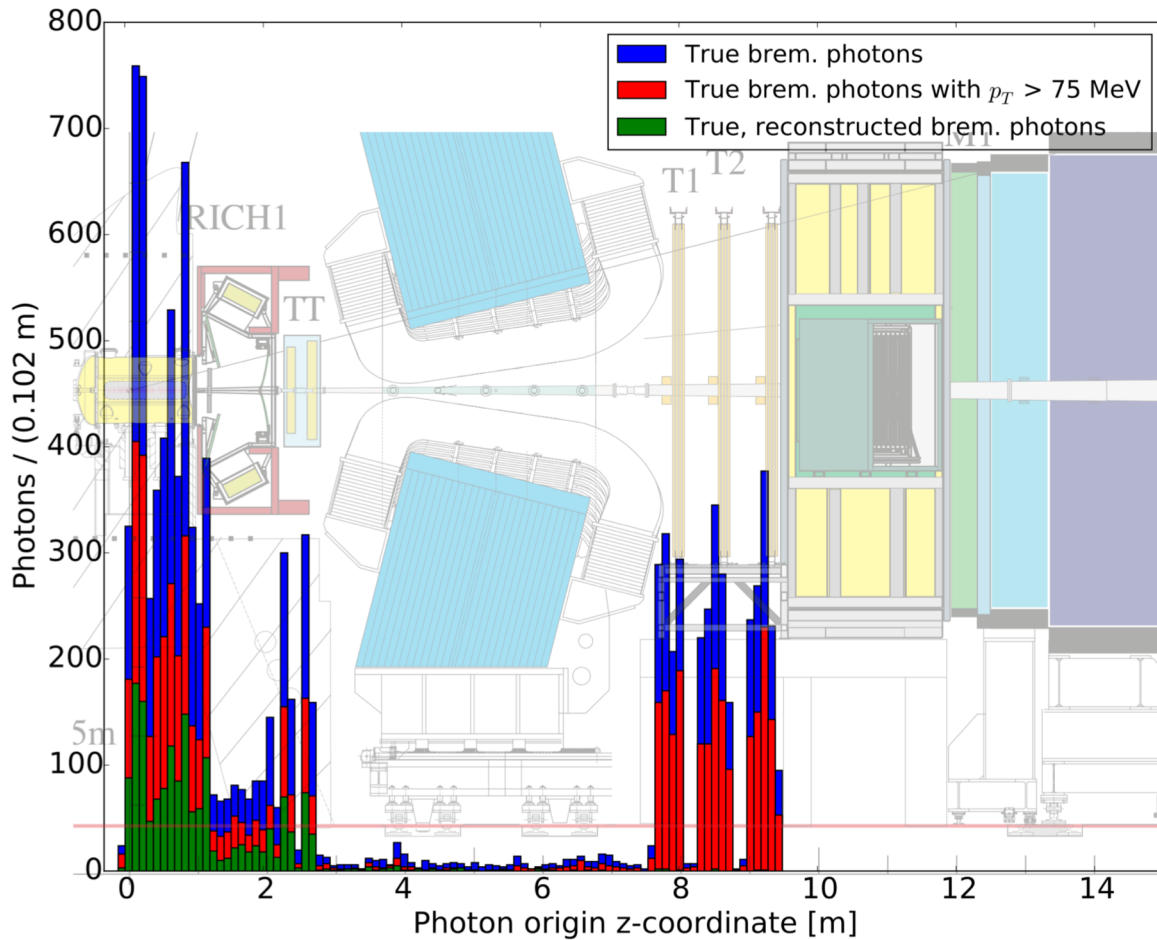
LHCb luminosity prospects



LHC era			HL-LHC era	
Run 1 (2010-12)	Run 2 (2015-18)	Run 3 (2021-24)	Run 4 (2027-30)	Run 5+ (2031+)
3 fb ⁻¹	6 fb ⁻¹	23 fb ⁻¹	46 fb ⁻¹	>300 fb ⁻¹ ??
		Phase-1 Upgrade!!	Phase-1b Upgrade!?	Phase-2 Upgrade??

* See Prof. J.C. Wang's talk on Sunday for the LHCb upgrades

Bremsstrahlung corrections

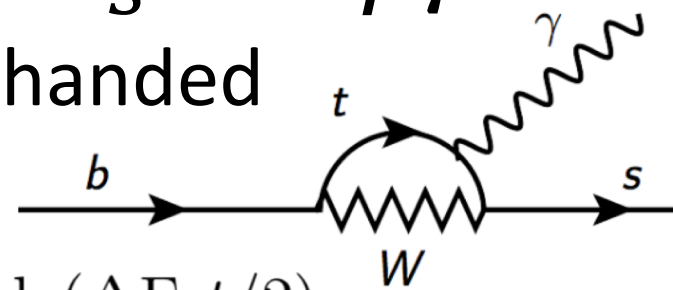


Rare decays at LHCb

- Radiative
 - $B_s^0 \rightarrow \phi\gamma, \Lambda_b^0 \rightarrow \Lambda\gamma, B^+ \rightarrow K^+\pi^+\pi^-\gamma$
- Rare charm
 - $D^0 \rightarrow \mu^+\mu^-, \Lambda_c^+ \rightarrow p\mu^+\mu^-$
- Rare strange
 - $K_S^0 \rightarrow \mu^+\mu^-, \Sigma^+ \rightarrow p\mu^+\mu^-$
- Very rare decays
 - $B_{(s)}^0 \rightarrow \mu^+\mu^-, B_{(s)}^0 \rightarrow \tau^+\tau^-, B_{(s)}^0 \rightarrow \mu^+\mu^-\mu^+\mu^-$
- Lepton flavor violation
 - $B_{(s)}^0 \rightarrow \tau^+\mu^-, B_{(s)}^0 \rightarrow e^+\mu^-, \tau^+ \rightarrow \mu^+\mu^-\mu^+$
- Electroweak penguin
 - $B^0 \rightarrow K^{*0}\mu^+\mu^-, \text{LFU}$

Photon polarization in $B_S^0 \rightarrow \phi\gamma$

- Photons in $b \rightarrow s\gamma$ mainly left-handed
- Time-dependent signal rate

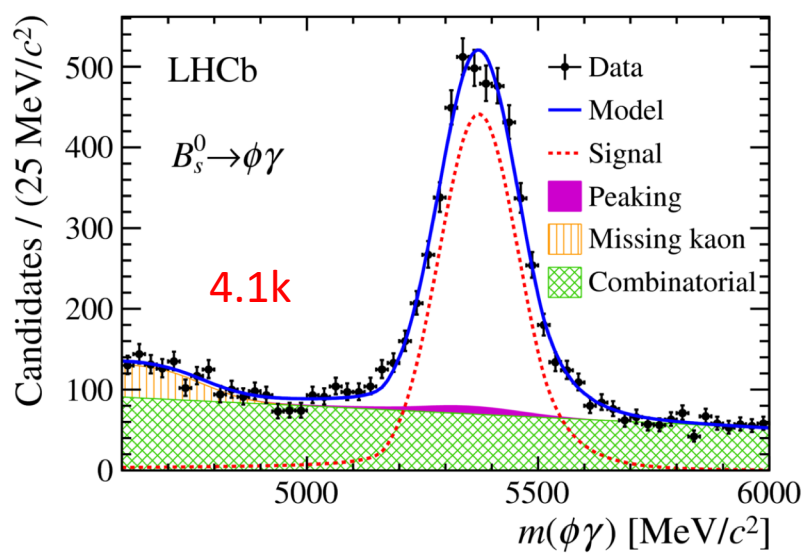
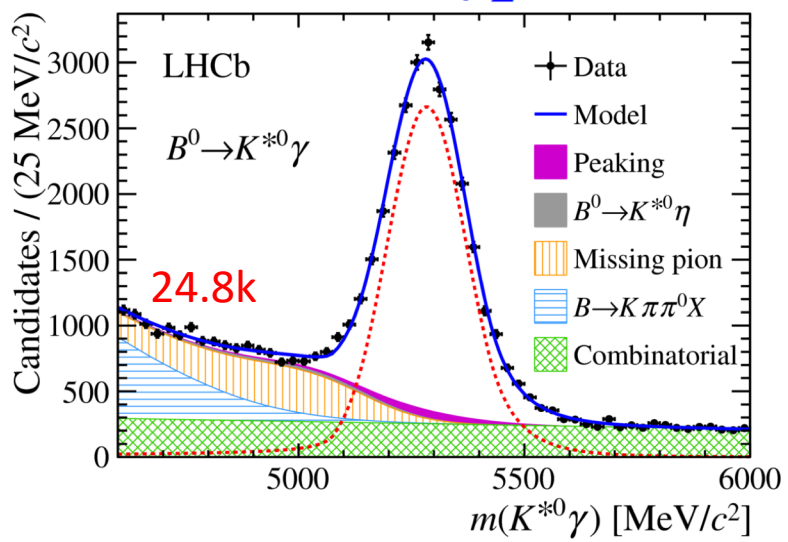


$$\mathcal{P}(t) \propto e^{-\Gamma_s t} \left\{ \cosh(\Delta\Gamma_s t/2) - \mathcal{A}^\Delta \sinh(\Delta\Gamma_s t/2) + \zeta C \cos(\Delta m_s t) - \zeta S \sin(\Delta m_s t) \right\}$$

with

$$\mathcal{A}^\Delta \propto 2 \frac{\gamma_R}{\gamma_L} \cdot \mathcal{A}_{SM}^\Delta = 0.05 \pm 0.03$$

[PRL 118 (2017) 021801]



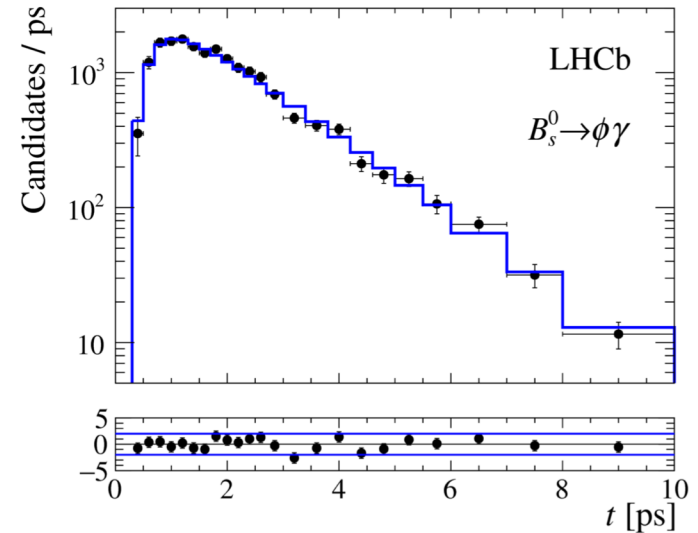
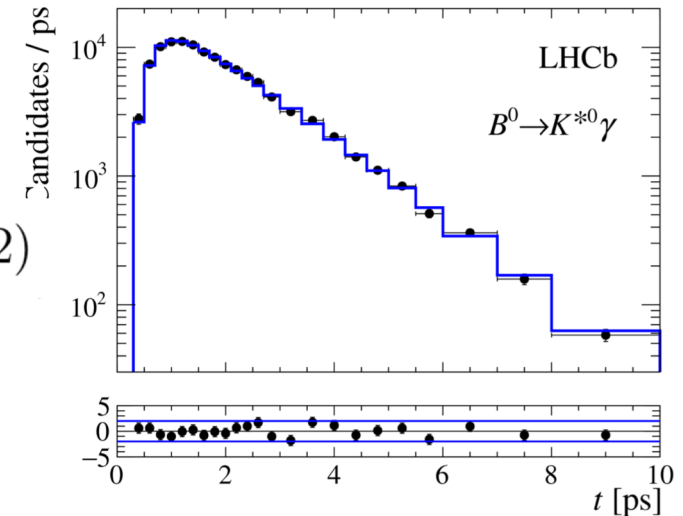
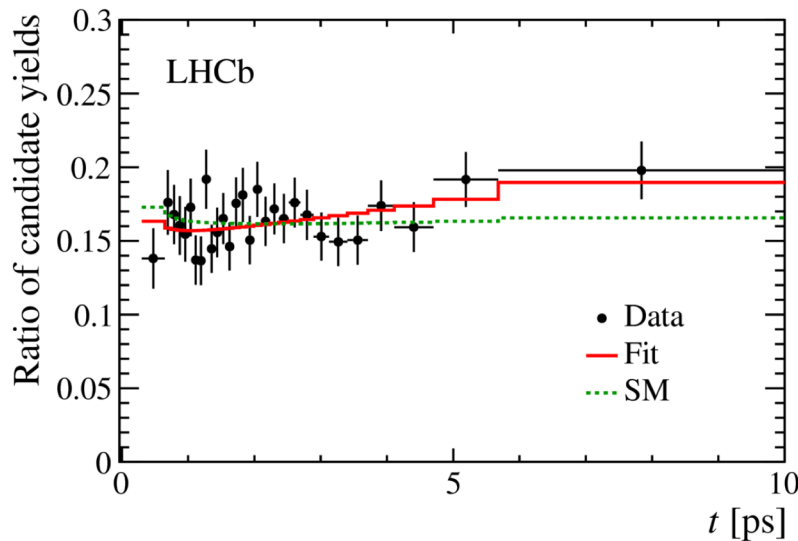
$B_S^0 \rightarrow \phi\gamma$, untagged analysis

- Assuming equal mixture of B_S^0 / \bar{B}_S^0 , simplified

$$\mathcal{P}(t) \propto e^{-\Gamma_s t} \{ \cosh(\Delta\Gamma_s t/2) - \mathcal{A}^\Delta \sinh(\Delta\Gamma_s t/2) \}$$

- Measured

$$\mathcal{A}^\Delta = -0.98^{+0.46+0.23}_{-0.52-0.20}$$



$B_s^0 \rightarrow \phi\gamma$, tagged analysis

- Same dataset, with flavor-tagging

$$\mathcal{P}(t) \propto e^{-\Gamma_s t} \left\{ \cosh(\Delta\Gamma_s t/2) - \mathcal{A}^\Delta \sinh(\Delta\Gamma_s t/2) + \zeta C \cos(\Delta m_s t) - \zeta S \sin(\Delta m_s t) \right\}$$

$$\mathcal{A}_{\phi\gamma}^\Delta \approx \frac{\text{Re}(e^{-i\phi_s} C_7 C_7')}{|C_7|^2 + |C_7'|^2} \quad S_{\phi\gamma}^\Delta \approx \frac{\text{Im}(e^{-i\phi_s} C_7 C_7')}{|C_7|^2 + |C_7'|^2}$$

- First measurement of S/C in radiative B_s^0 decay

$$S_{\phi\gamma} = 0.43 \pm 0.30 \pm 0.11,$$

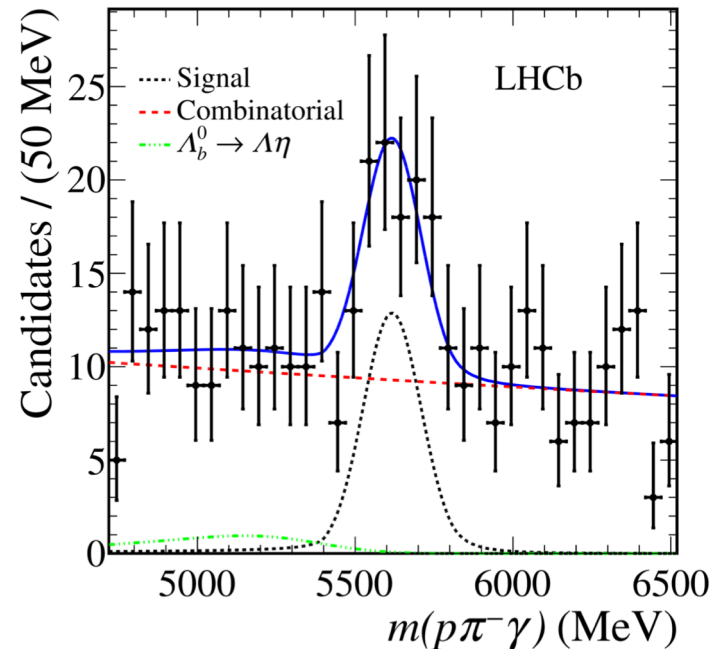
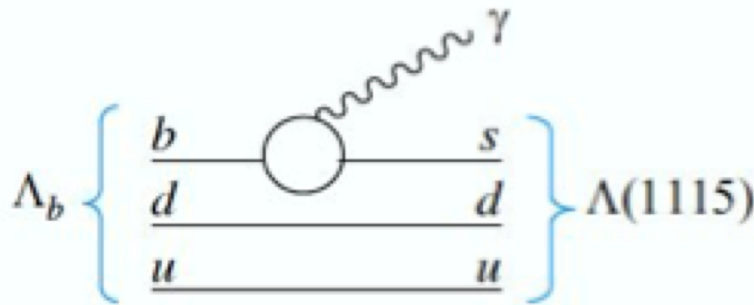
$$C_{\phi\gamma} = 0.11 \pm 0.29 \pm 0.11,$$

$$\mathcal{A}_{\phi\gamma}^\Delta = -0.67^{+0.37}_{-0.41} \pm 0.17.$$

Observation of $\Lambda_b^0 \rightarrow \Lambda \gamma$

- Baryonnic $b \rightarrow s \gamma$ not observed yet. Upper limit set by CDF, $\mathcal{B} < 1.9 \times 10^{-3}$ [CDF, PRD 66 (2002) 112002]

- In SM, $\mathcal{B} \sim 0.06 - 1 \times 10^{-5}$



- First observation, BR:

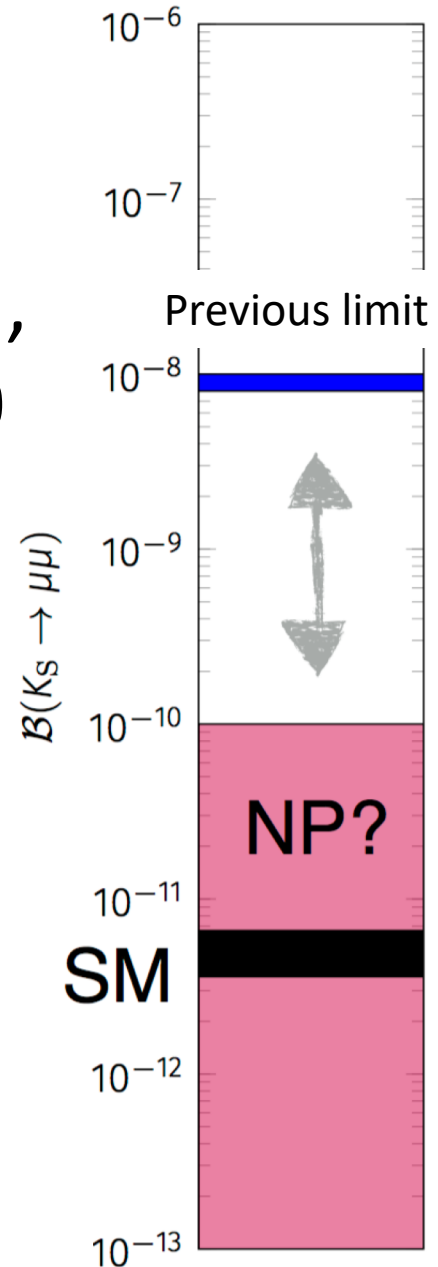
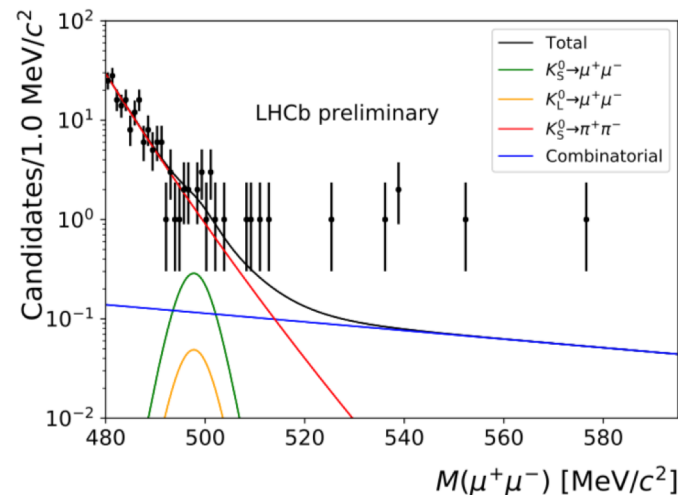
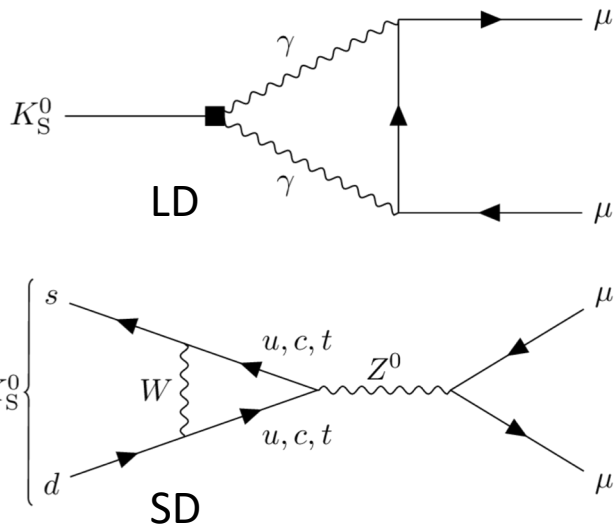
$$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda \gamma) = (7.1 \pm 1.5 \pm 0.6 \pm 0.7) \times 10^{-6}$$

$$K_S^0 \rightarrow \mu^+ \mu^-$$

- SM predicts: $\mathcal{B} = (5.2 \pm 1.5_{\text{LD}}) \times 10^{-12}$, can be enhanced by up to factor 100

- $K_S^0 \rightarrow \pi^+ \pi^-$: control channel, main Bkg

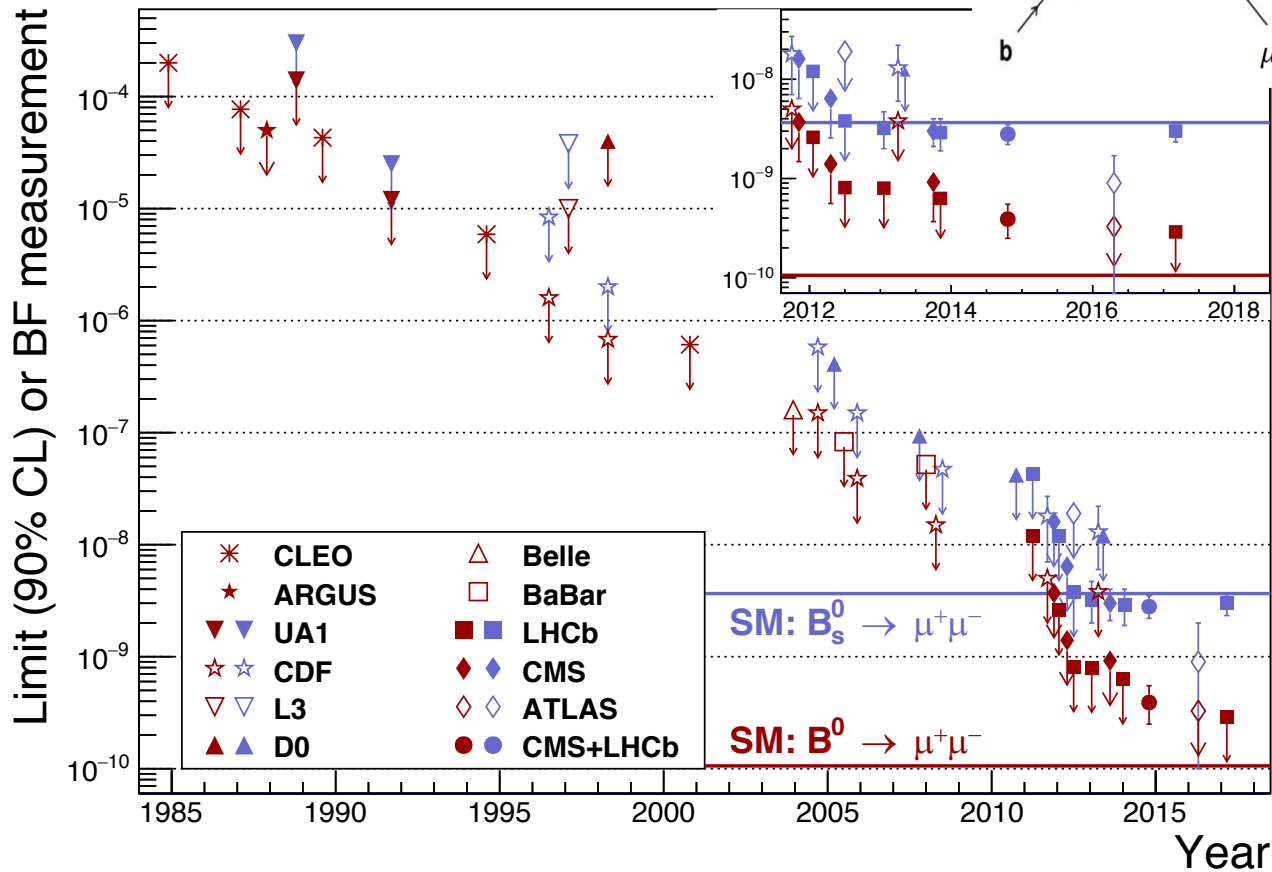
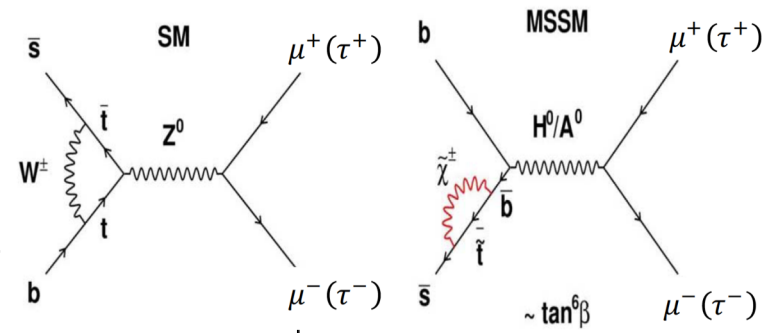
$$\mathcal{B}(K_S^0 \rightarrow \mu^+ \mu^-) < 2.1 (2.4) \times 10^{-10} \text{ at } 90 (95)\% \text{ CL}$$



[LHCb-CONF-2019-002]

$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

- Road to $B_{(s)}^0 \rightarrow \mu^+ \mu^-$

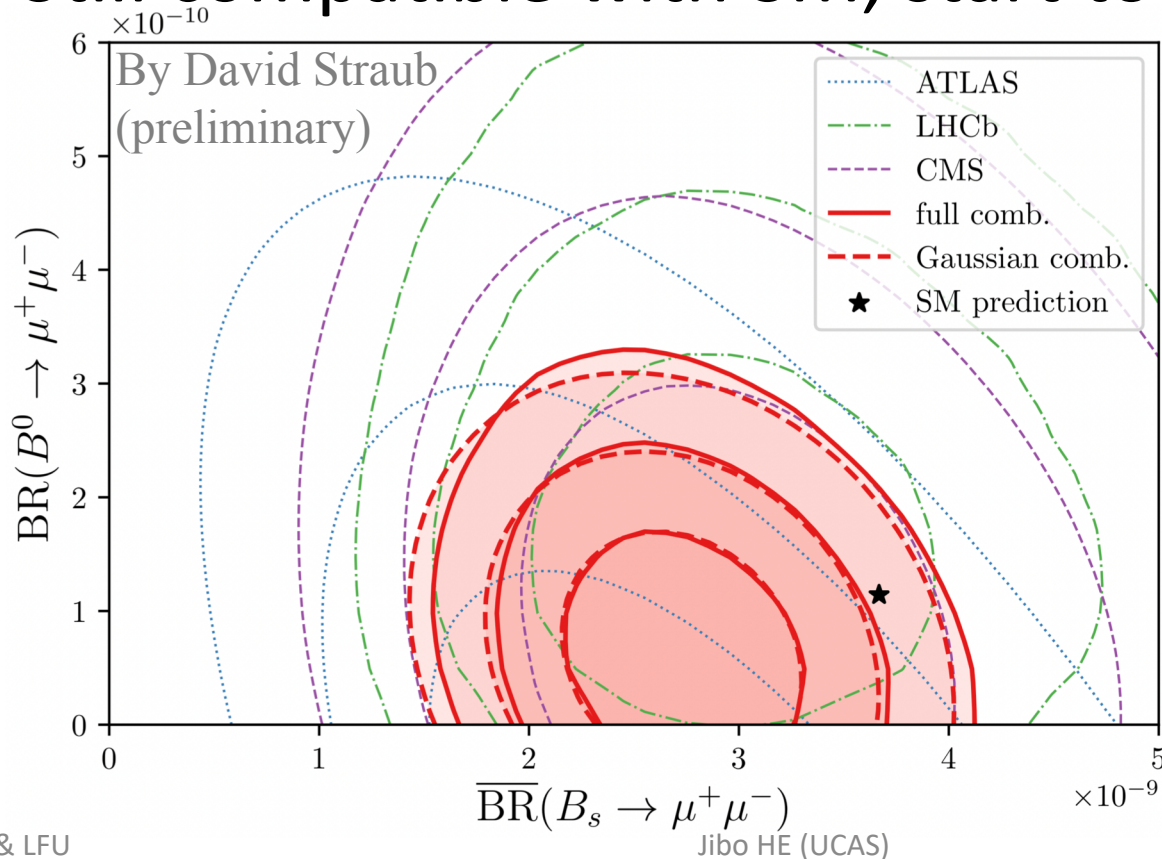


$B_{(s)}^0 \rightarrow \mu^+ \mu^-$, latest results

- $B_s^0 \rightarrow \mu^+ \mu^-$ observed in single experiment(s)

LHCb (4.6 fb^{-1}): 7.8σ , ATLAS (26 fb^{-1}): 4.6σ , CMS (61 fb^{-1}): 5.6σ

- Still compatible with SM, start to be interesting



[LHCb, PRL 118 (2017) 191801]

[ATLAS, JHEP 04 (2019) 098]

[CMS, CMS-PAS-BPH-16-004]

$B_S^0 \rightarrow \mu^+ \mu^-$ effective lifetime

- B_S^0 mixing \Rightarrow effective τ

$$\tau_{\mu\mu} = \frac{\tau_{B_S}}{(1 - y_s^2)} \frac{1 + 2y_s A_{\Delta\Gamma} + y_s^2}{1 + y_s A_{\Delta\Gamma}}$$

$A_{\Delta\Gamma} = 1$ in SM

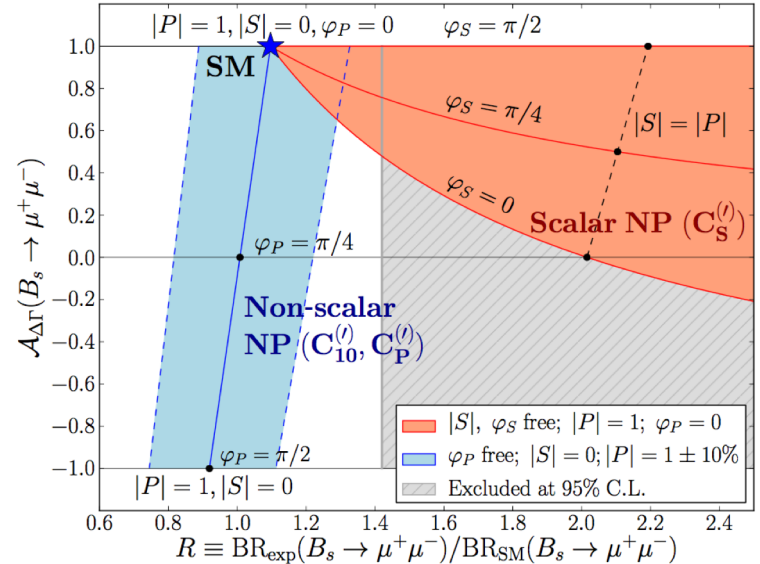
$$y_s \equiv \tau_{B_S} \Delta\Gamma_s / 2$$

- First measurement, not yet sensitive to $A_{\Delta\Gamma}$

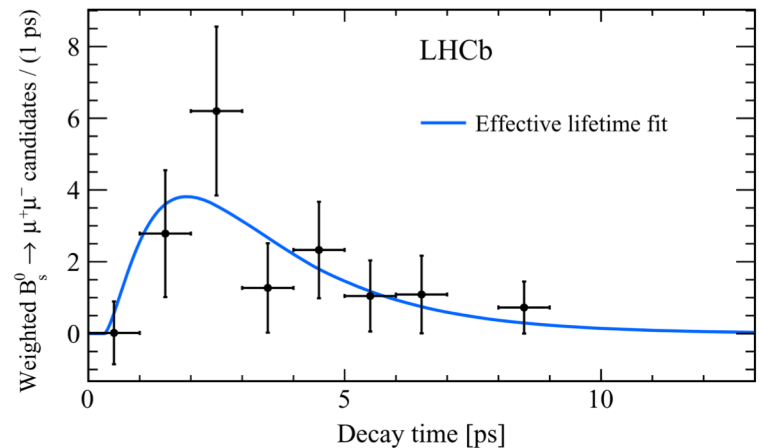
$$\tau(B_S^0 \rightarrow \mu^+ \mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

$$1.70^{+0.61}_{-0.44} \text{ ps}$$

[CMS-PAS-BPH-16-004]



[De Bruyn *et al.*, PRL 109 (2012) 041801]



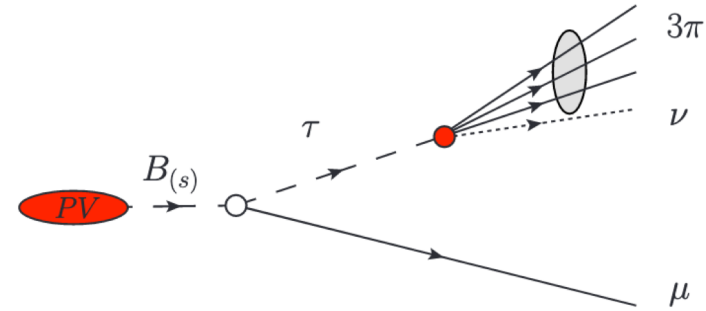
$$B_{(s)}^0 \rightarrow \tau^+ \mu^-$$

- LFV, highly suppressed in SM, $\mathcal{B} \sim O(10^{-54})$, may be enhanced by NP models
 - Z' , up to 10^{-8}
 - Leptoquarks, $10^{-9} - 10^{-5}$
 - Pati-Salam gauge model, $10^{-4} - 10^{-6}$
- Best limit given by Babar
$$\mathcal{B}(B^0 \rightarrow \tau^+ \mu^-) < 2.2 \times 10^{-5} \text{ at 90\% CL}$$

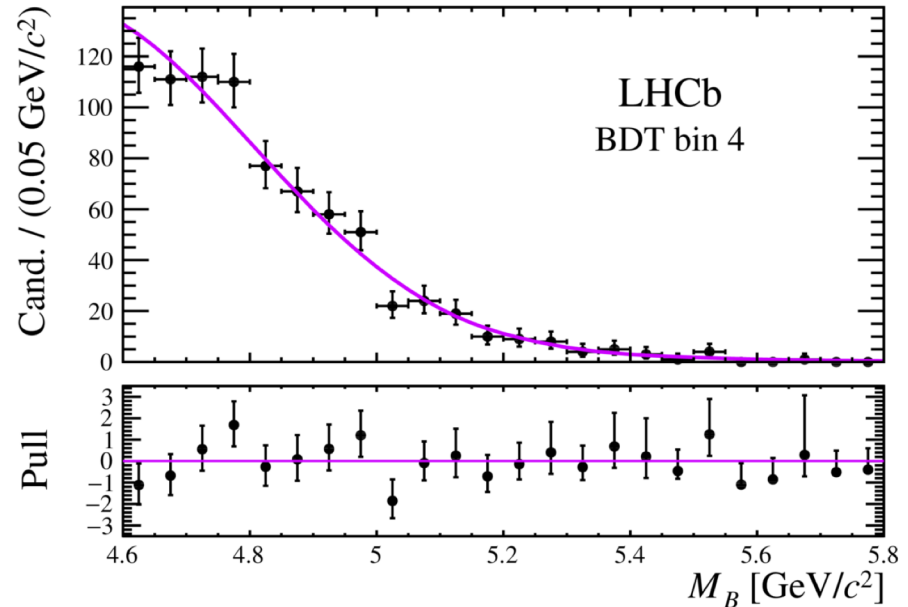
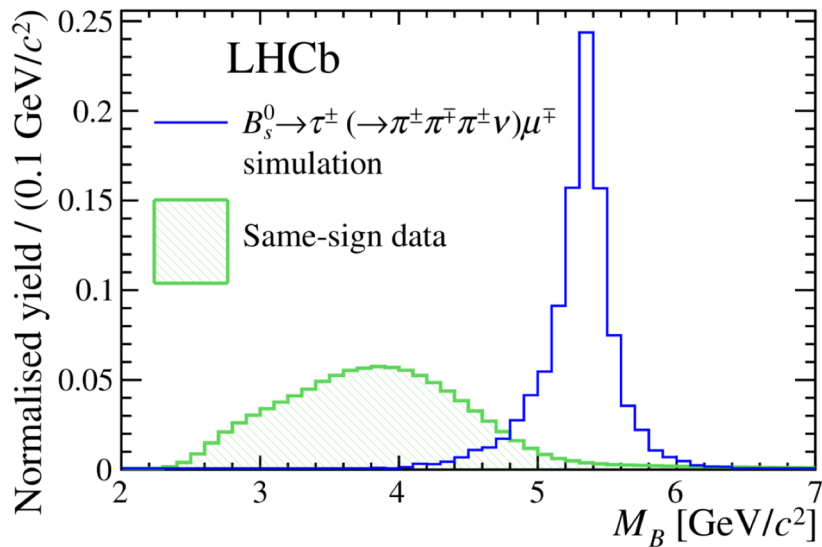
[Babar, PRD 77 (2008) 091104]

$$B_{(s)}^0 \rightarrow \tau^+ \mu^-$$

- Using $\tau^- \rightarrow 3\pi\nu_\tau(a_1)$ mode
- Normalized to $B^0 \rightarrow D^- \pi^+$



[arXiv:1905.06614]

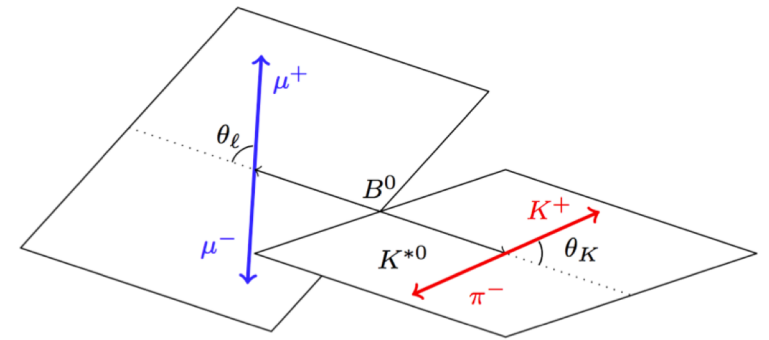
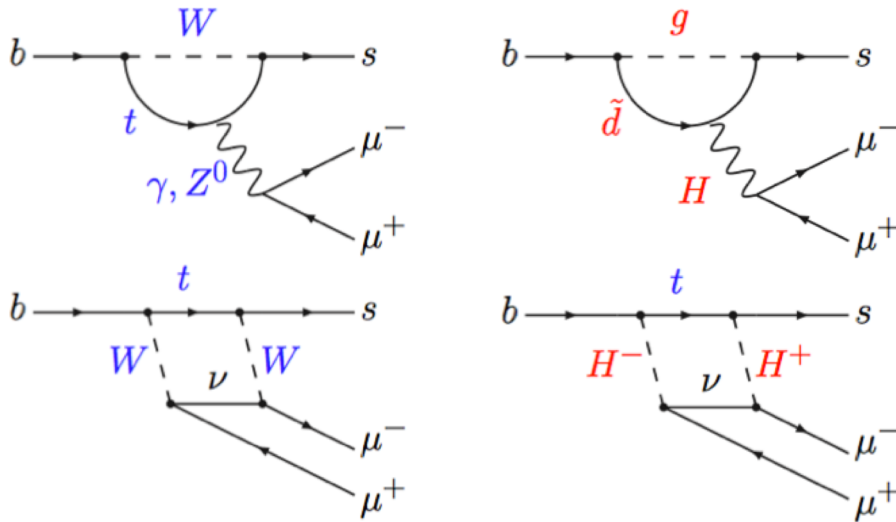


$$\mathcal{B}(B^0 \rightarrow \tau^+ \mu^-) < 1.4 \times 10^{-5} \text{ at 95\% CL}$$

$$\mathcal{B}(B_s^0 \rightarrow \tau^+ \mu^-) < 4.2 \times 10^{-5} \text{ at 95\% CL}$$

$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$

- Rates and angular distributions sensitive to NP

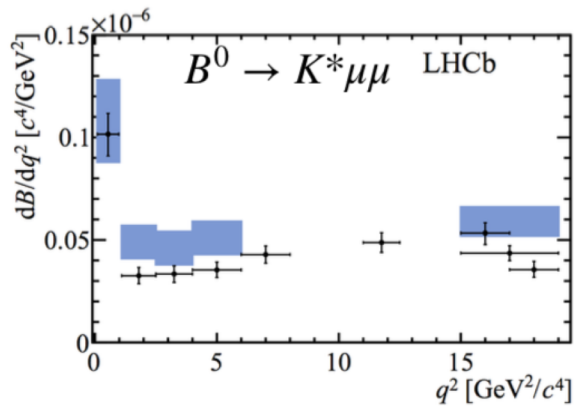


$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

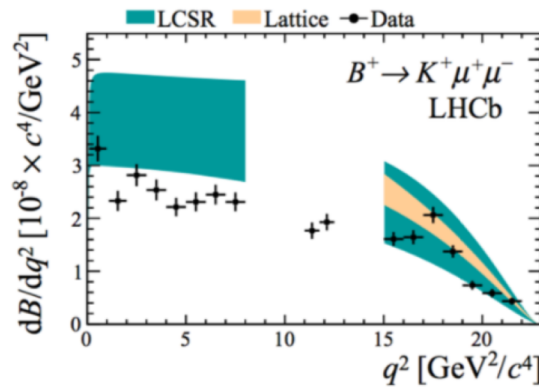
Branching fraction of $b \rightarrow s \ell^+ \ell^-$

- Some tensions seen

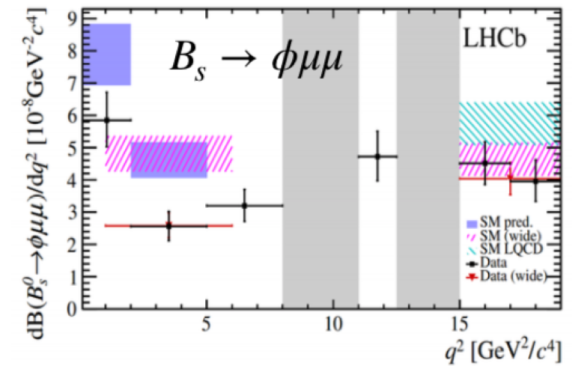
JHEP 11 (2016) 047



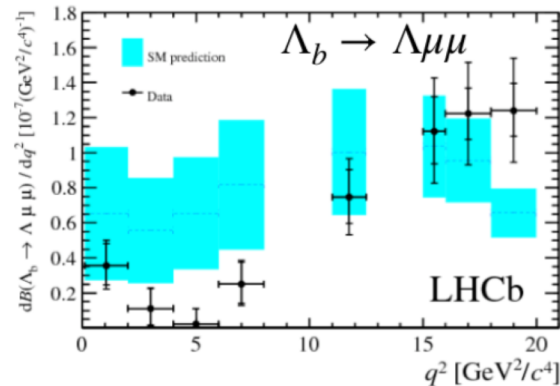
JHEP 06 (2014) 133



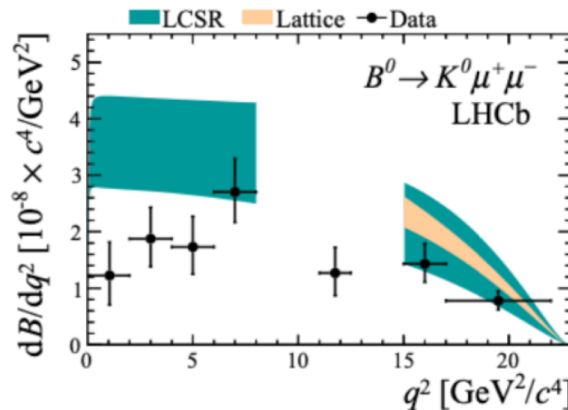
JHEP 09 (2015) 179



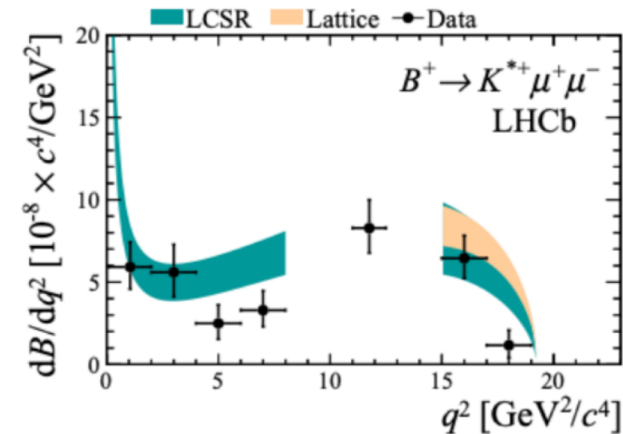
JHEP 06 (2015) 115



JHEP 06 (2014) 133

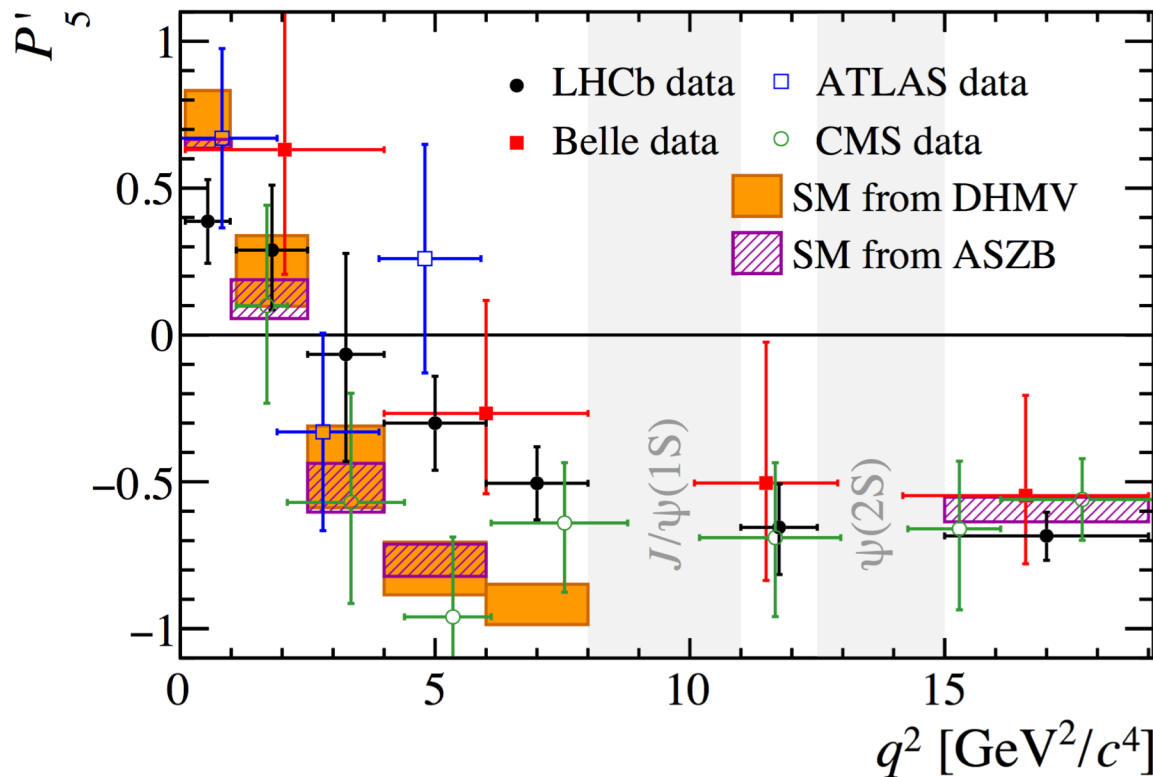


JHEP 06 (2014) 133



$$B^0 \rightarrow K^{*0} \mu^+ \mu^- : P'_5$$

- $P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$, less form-factor dependent
- Also measured by Belle, ATLAS, CMS



[LHCb, JHEP 02 (2016) 104]

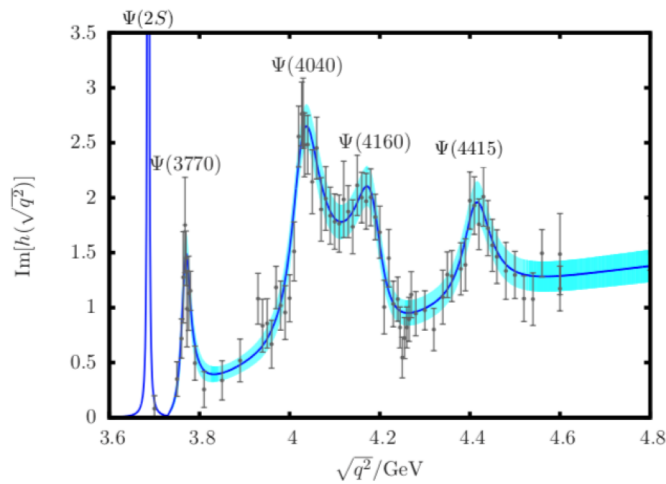
[Belle, PRL 118 (2017) 111801]

[ATLAS, JHEP 10 (2018) 047]

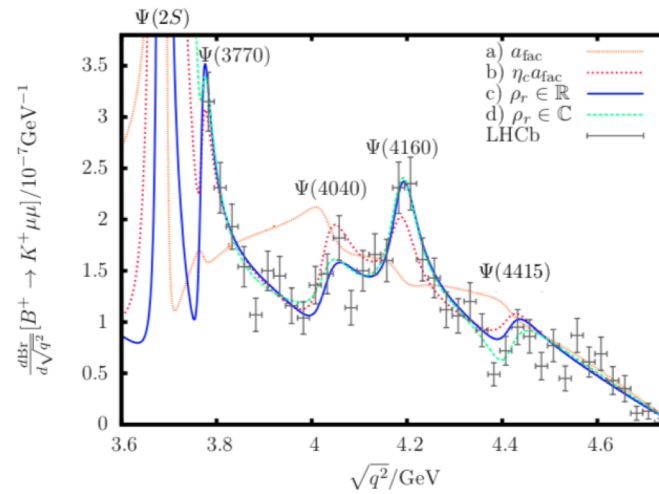
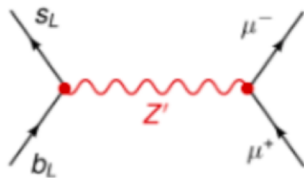
[CMS, PLB 781 (2018) 517]

New physics, or QCD?

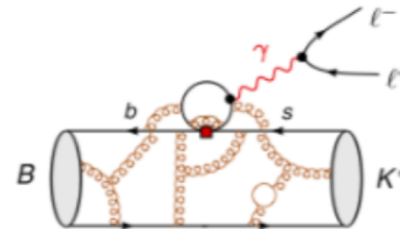
- Charm loop effects? [Lyon, Zwicky, arXiv:1406.0566]
 - ▶ Large non-factorisable effects (or NP) required to have consistent picture between BESII $e^+e^- \rightarrow$ hadrons data and the LHCb result



Optimist's view point

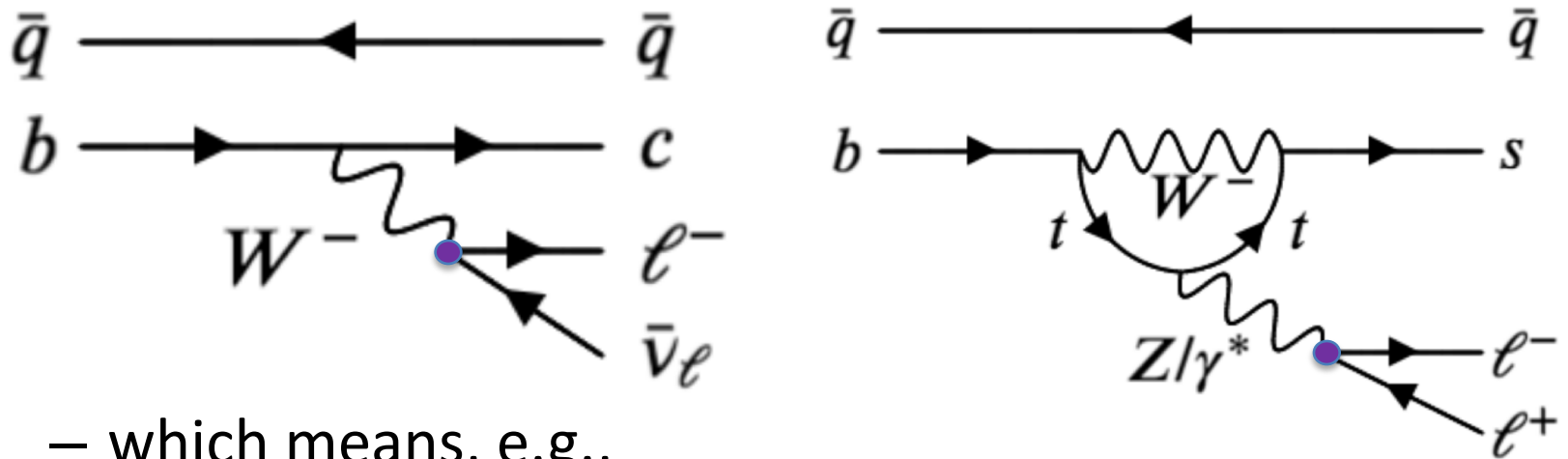


Pessimist's view point



Lepton flavor universality

- Three lepton families (e, μ, τ) have identical couplings to the gauge bosons



$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)} = 1$$

- Lepton flavor universality violation? **New Physics!**

Experimental test of LFU

- Well established in SM, e.g. $W \rightarrow l\nu$
 - Some tension

[LEP, PR 532 (2013) 119]

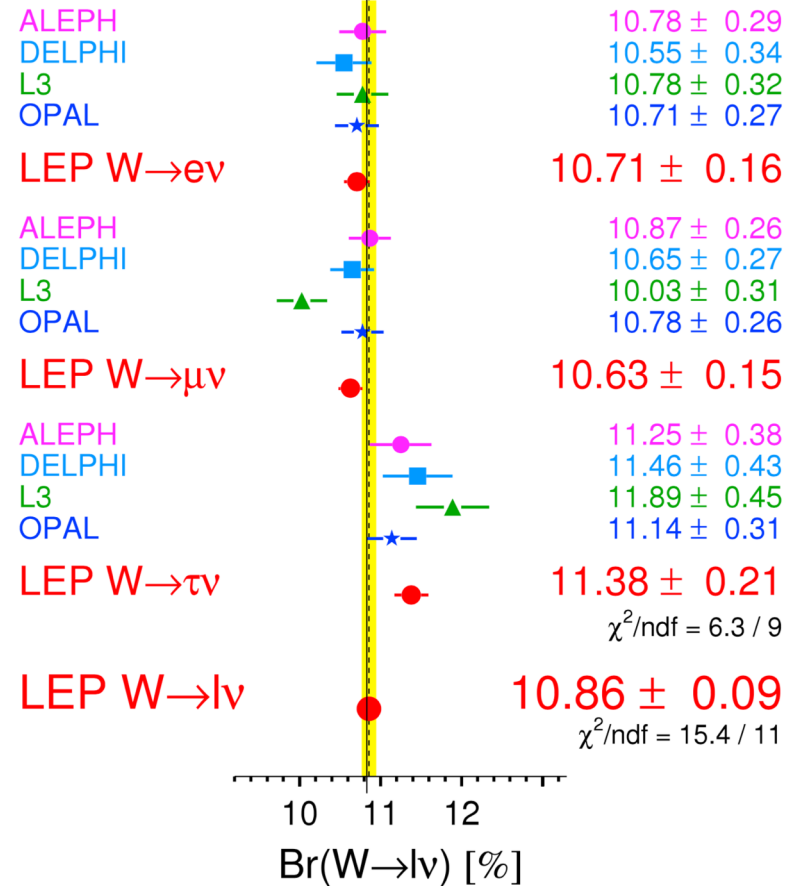
$$\mathcal{B}(W \rightarrow \mu\bar{\nu}_\mu) / \mathcal{B}(W \rightarrow e\bar{\nu}_e) = 0.993 \pm 0.019,$$

$$\mathcal{B}(W \rightarrow \tau\bar{\nu}_\tau) / \mathcal{B}(W \rightarrow e\bar{\nu}_e) = 1.063 \pm 0.027,$$

$$\mathcal{B}(W \rightarrow \tau\bar{\nu}_\tau) / \mathcal{B}(W \rightarrow \mu\bar{\nu}_\mu) = 1.070 \pm 0.026.$$

$$\frac{2\mathcal{B}(W \rightarrow \tau\bar{\nu}_\tau)}{\mathcal{B}(W \rightarrow e\bar{\nu}_e) + \mathcal{B}(W \rightarrow \mu\bar{\nu}_\mu)} = 1.066 \pm 0.025 \quad (2.6\sigma)$$

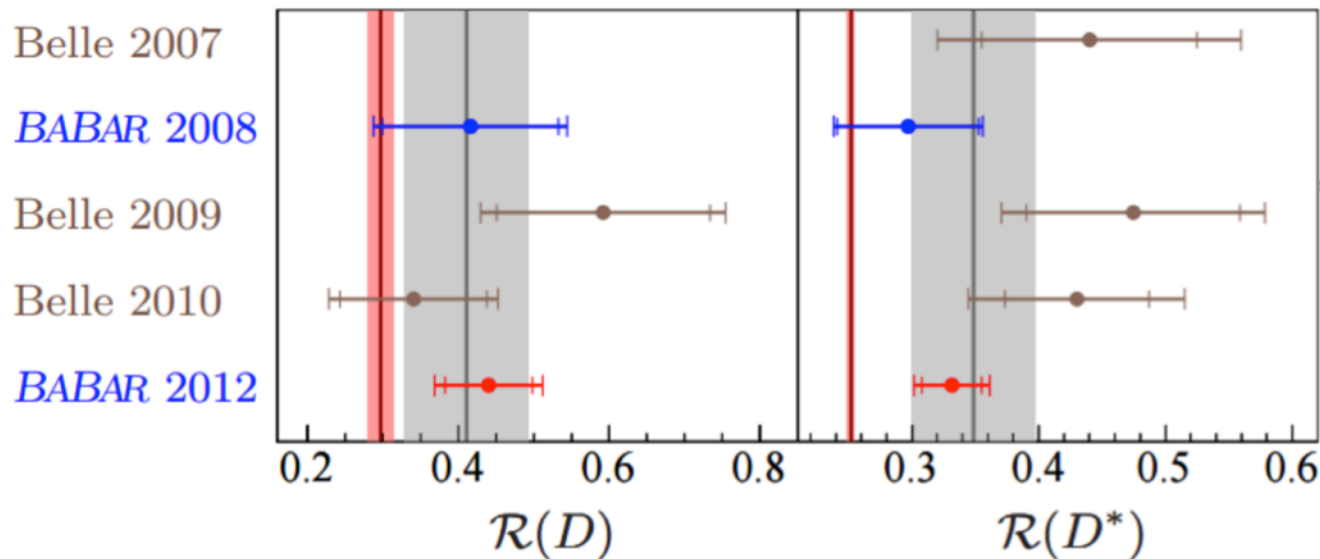
W Leptonic Branching Ratios



LFU in B system, pre-LHCb

- $\mathcal{R}(D^{(*)})$, Babar reported deviation of $\sim 3.2 \sigma$

$$\mathcal{R}(D^{(*)}) \equiv \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)} \quad [\text{Babar, PRD 88 (2013) 072012}]$$

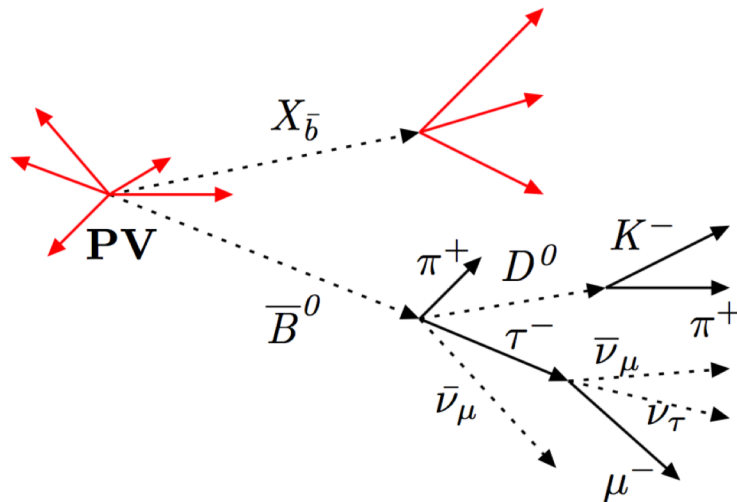


- No deviation seen in FCNC $b \rightarrow sll$ decays

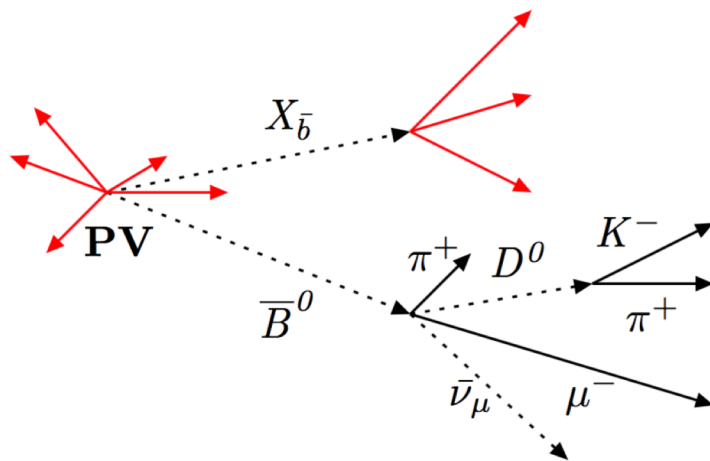
R(D*) using muonic τ decays

- Measure R(D*) using muonic τ decays
 - Pros: $\mathcal{B}(\tau \rightarrow \mu X) \sim 17.4\%$, B vertex rec'ible
 - Cros: no τ vertex

Signal ($B^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$)



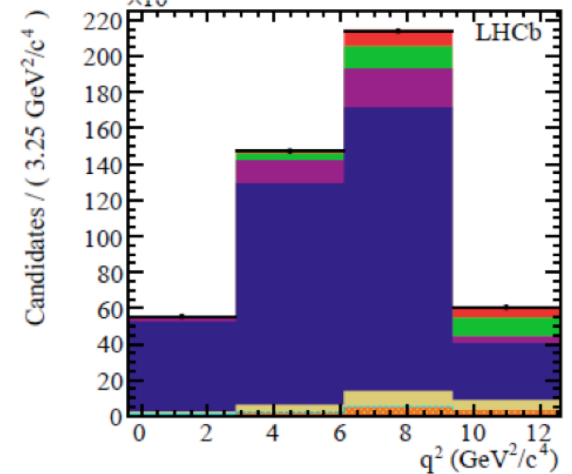
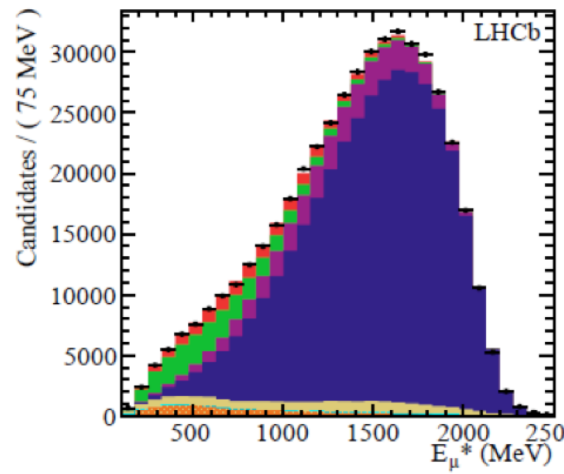
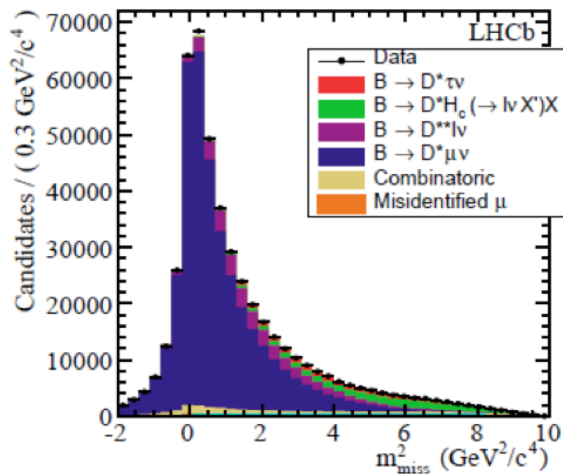
Normalisation ($B^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$)



R(D*), results

- 3D fits, $\mathcal{R}_{D^*} = 0.336 \pm 0.027 \pm 0.030$
 - Signal yields: $16\,500 \pm 1\,670$

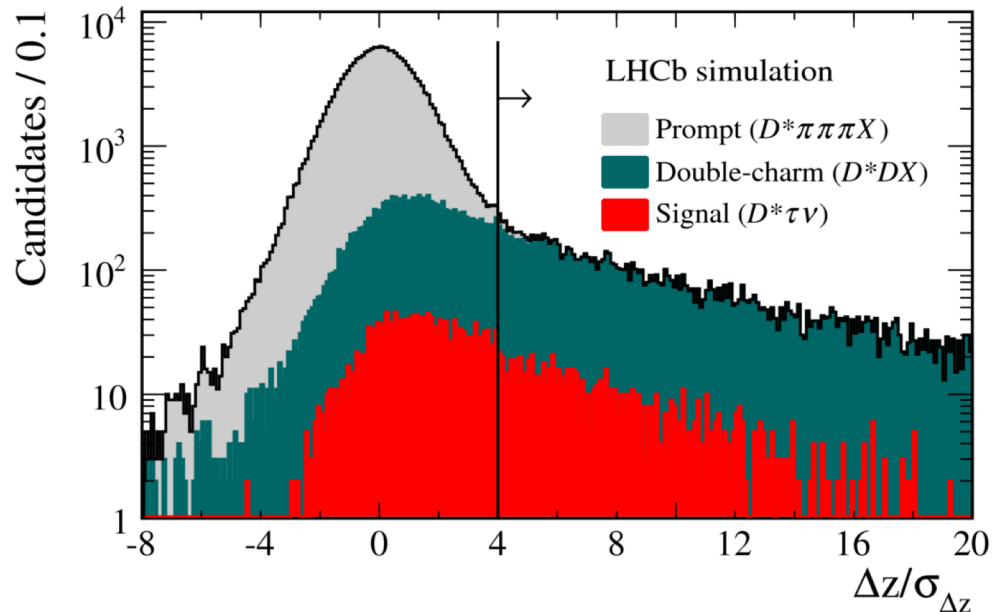
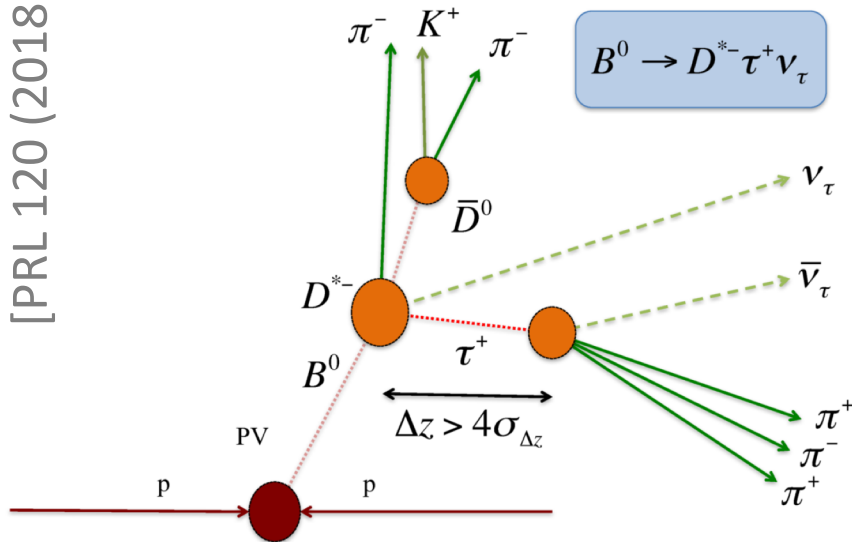
[PRL 115 (2015) 118003]



R(D^{*}) using 3-prong τ decays

- Measure R(D^{*}) using 3-prong τ decays
 - Pros: $\mathcal{B}(\tau \rightarrow 3\pi^\pm X) \sim 9\% + 4\% (\geq 1\pi^0)$, B/τ vertex rec'ible
 - Cros: soft π^\pm , bkg; different from norm. decay

[PRL 120 (2018) 171802]



R(D*), results

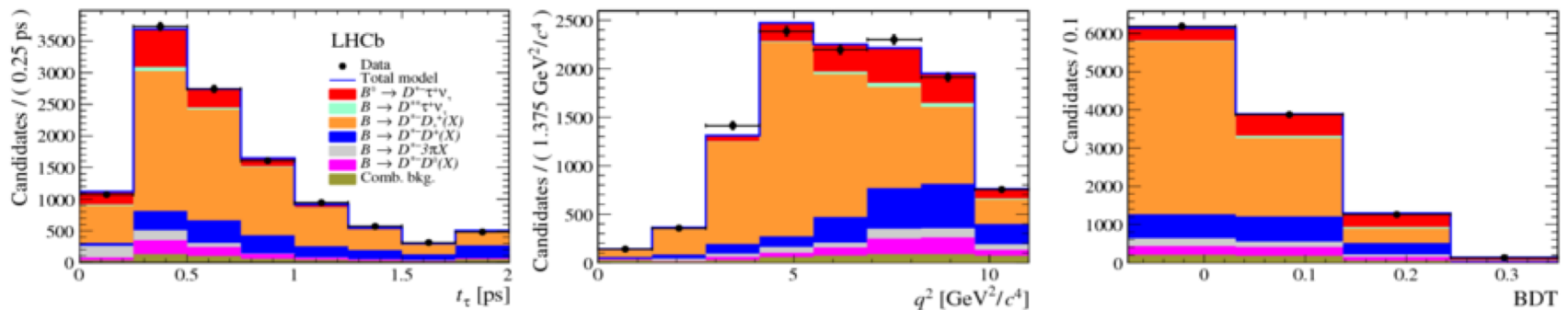
- Normalized to $B^0 \rightarrow D^{*-} 3\pi$

$$R_{had}(D^*) = \frac{\mathcal{B}(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau)}{\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)} \quad R(D^*) = R_{had}(D^*) \times \frac{\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^- \nu_\mu)}$$

- 3D fits, $R(D^*) = 0.286 \pm 0.019 \pm 0.025 \pm 0.021$

– Signal yields: 1273 ± 85

c.f. muonic: $16\,500 \pm 1\,670$



[PRL 120 (2018) 171802]

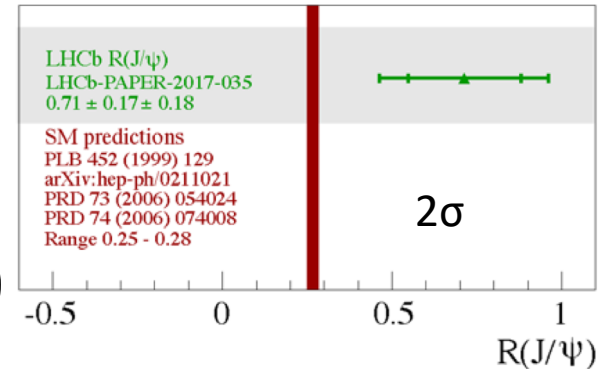
R(J/ψ) using muonic τ decays

- Measure R(J/ψ) using muonic τ decays

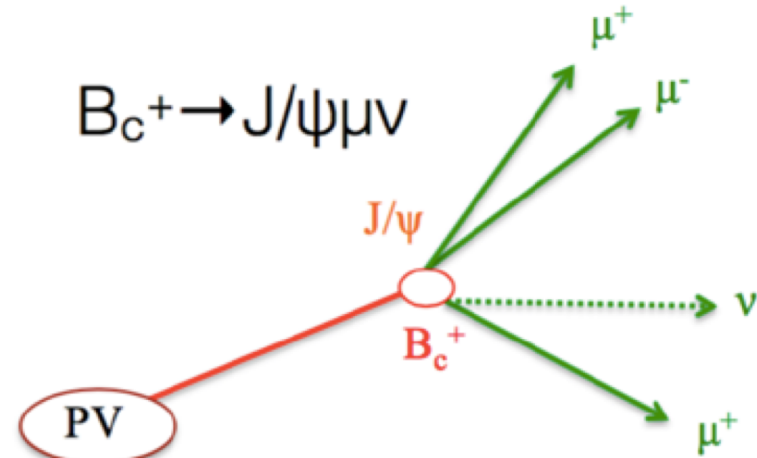
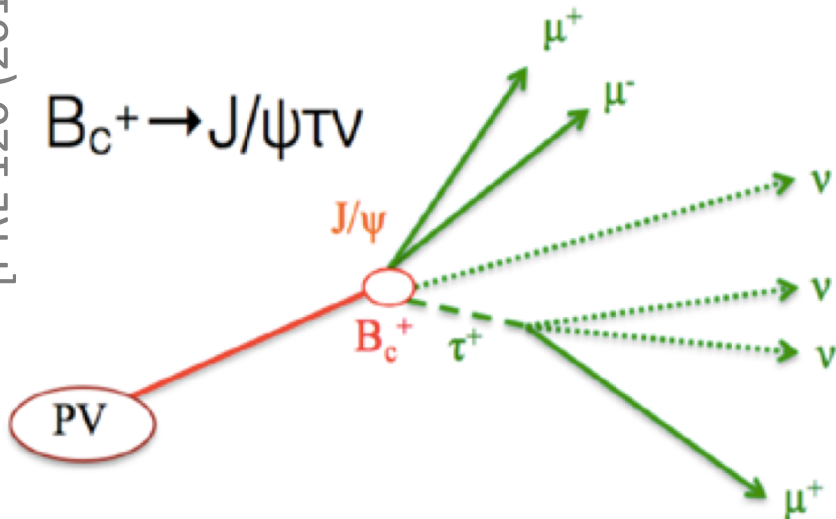
- Pros: 3μ , $\mathcal{B}(\tau \rightarrow \mu X) \sim 17.4\%$

- Cons: small $\sigma(B_c^+)$, no τ vertex

- Run-I, 1400 ± 300 signal (3σ)

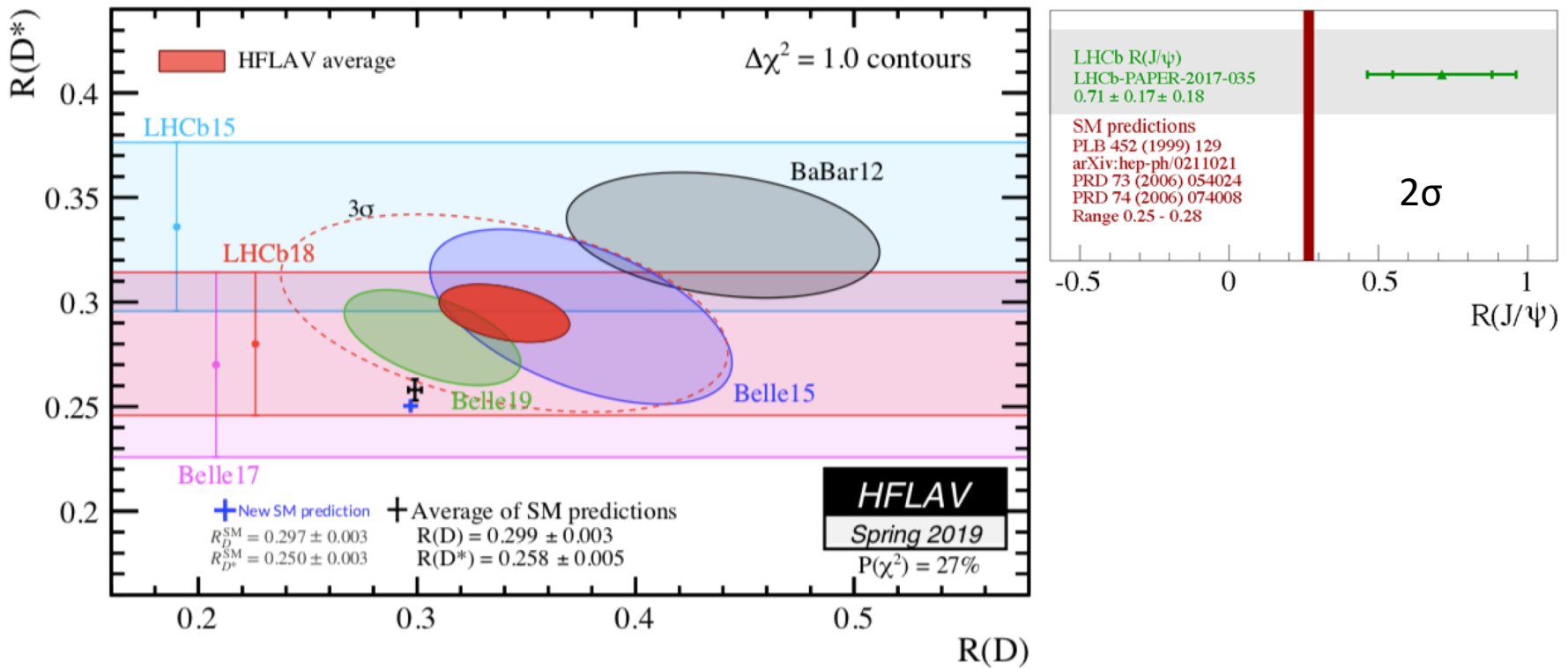


[PRL 120 (2018) 121801]



Summary of LFU in $b \rightarrow cl\nu$ decays

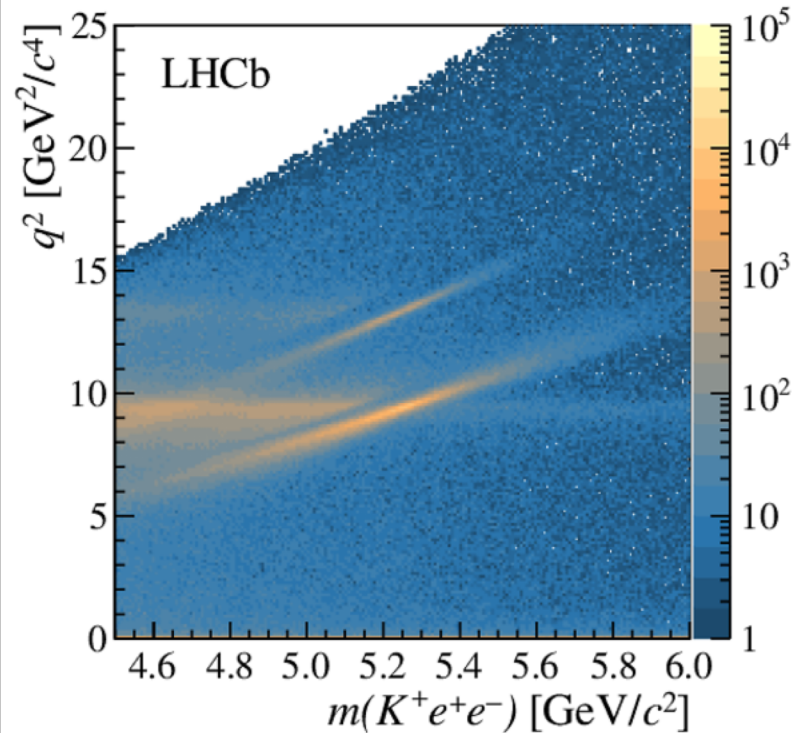
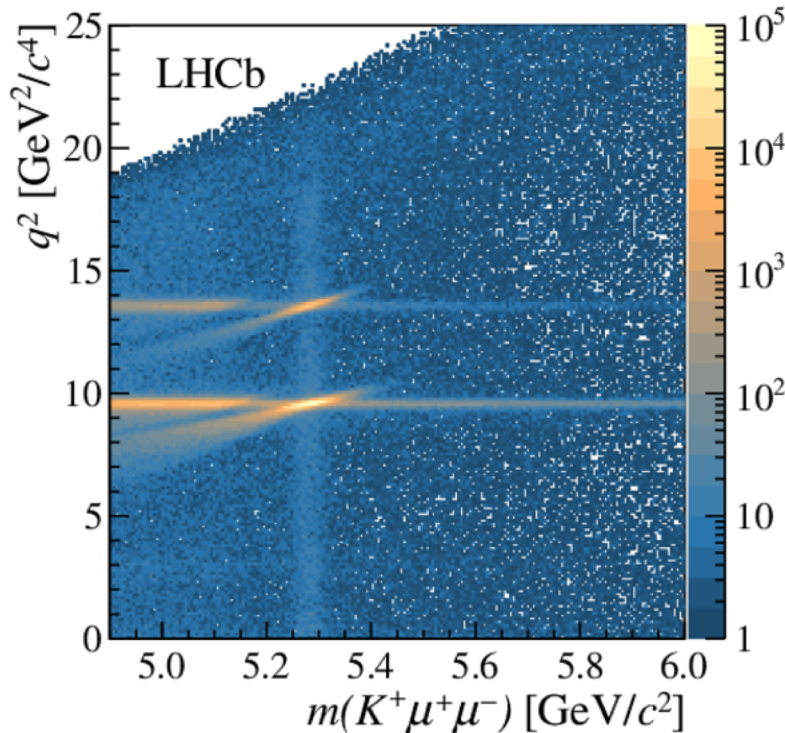
- Deviations from SM seen by Babar/Belle/LHCb



R(K), introduction

- Double ratio to control systematics

$$\mathcal{R}_K = \left(\frac{\mathcal{N}_{K^+\mu^+\mu^-}}{\mathcal{N}_{K^+e^+e^-}} \right) \left(\frac{\mathcal{N}_{J/\psi(e^+e^-)K^+}}{\mathcal{N}_{J/\psi(\mu^+\mu^-)K^+}} \right) \left(\frac{\varepsilon_{K^+e^+e^-}}{\varepsilon_{K^+\mu^+\mu^-}} \right) \left(\frac{\varepsilon_{J/\psi(\mu^+\mu^-)K^+}}{\varepsilon_{J/\psi(e^+e^-)K^+}} \right)$$



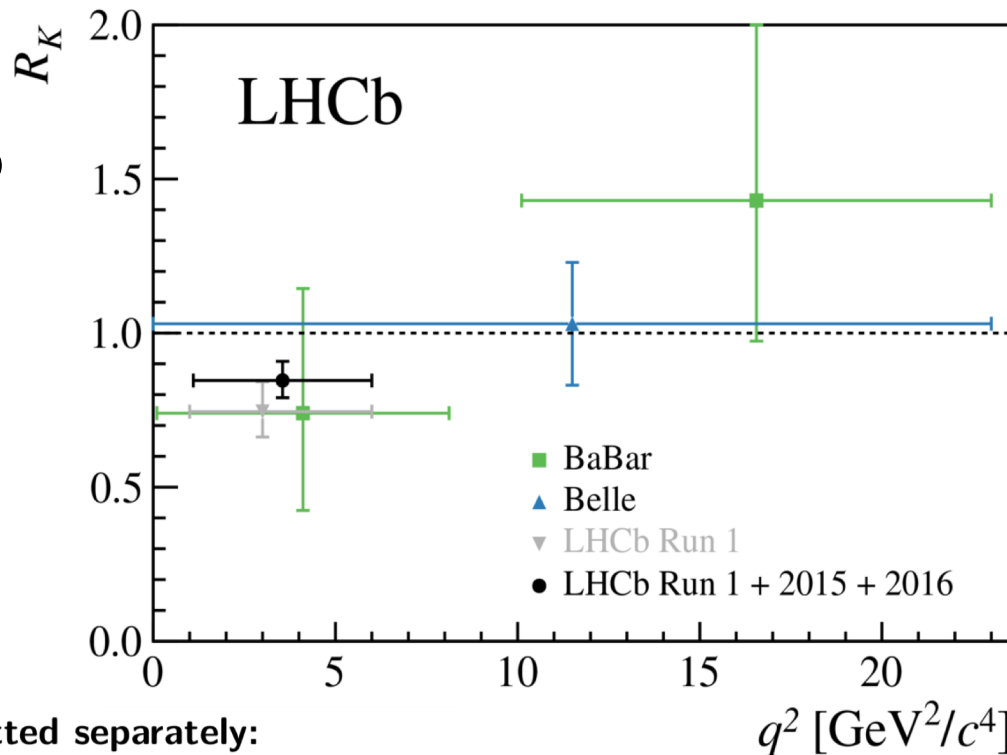
[PRL 122 (2019) 191801]

R(K), new results

- Include 2015+2016

$$R_K = 0.846^{+0.060+0.016}_{-0.054-0.014}$$

$\sim 2.5\sigma$ from SM



If instead the Run 1 and Run 2 were fitted separately:

$$R_{K \text{ Run 1}}^{\text{new}} = 0.717^{+0.083+0.017}_{-0.071-0.016}, \quad R_{K \text{ Run 2}} = 0.928^{+0.089+0.020}_{-0.076-0.017},$$

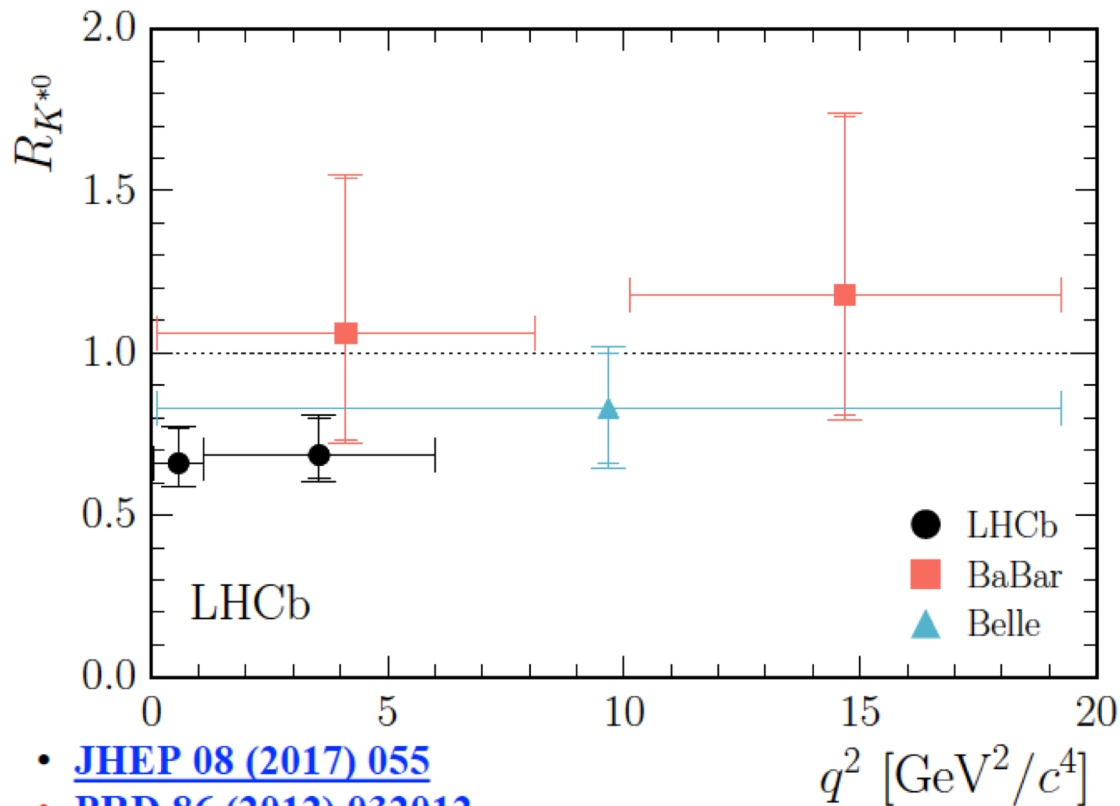
$$R_{K \text{ Run 1}}^{\text{old}} = 0.745^{+0.090}_{-0.074} \pm 0.036 \quad (\text{PRL113(2014)151601}),$$

Compatibility taking correlations into account:

- ▶ Previous Run 1 result vs. this Run 1 result (new reconstruction selection): $< 1 \sigma$;
- ▶ Run 1 result vs. Run 2 result: 1.9σ .

$R(K^{*0})$, results with Run-I data

- Deviations from SM seen by LHCb ($\sim 2.4\sigma$)



- [JHEP 08 \(2017\) 055](#)
- [PRD 86 \(2012\) 032012](#)
- [PRL 103 \(2009\) 171801](#)

Prospects

- LHCb upgrades (2025: 23 fb⁻¹, Upgrade-II: 300 fb⁻¹)

Observable	Current LHCb	LHCb 2025	Belle-II	LHCb Upgrade-II	ATLAS & CMS
$R_K(1 < q^2 < 6 \text{ GeV})$	0.1	0.025	0.036	0.007	
$R_{K^*}(1 < q^2 < 6 \text{ GeV})$	0.1	0.031	0.032	0.008	
R_ϕ, R_{pK}		0.08, 0.06		0.02, 0.02	
$\frac{\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)}$	90%	34%		10%	21%
$\tau_{B_s^0 \rightarrow \mu^+ \mu^-}$	22%	8%		2%	4%?
$R(D^*)$	0.026	0.0072	0.005	0.002	
$R(J/\psi)$	0.24	0.071		0.02	

[CERN-LHCC-2018-027]

Summary

- LHCb performed the world-leading measurements of rare decays and LFU:
 - Radiative, e.g., $B_S^0 \rightarrow \phi\gamma$, $\Lambda_b^0 \rightarrow \Lambda\gamma$
 - Rare strange, e.g., $K_S^0 \rightarrow \mu^+\mu^-$
 - Very rare decays, e.g., $B_{(s)}^0 \rightarrow \mu^+\mu^-$
 - LFV, e.g., $B_{(s)}^0 \rightarrow \tau^+\mu^-$
 - Electroweak penguin, e.g., $B^0 \rightarrow K^{*0}\mu^+\mu^-$, $\mathcal{R}_{K^{(*)0}}$
 - LFU in semi-leptonic decay, \mathcal{R}_{D^*}
- Your suggestions are always appreciated!