

# Search for the QCD Critical Point in High Energy Heavy-ion Collisions

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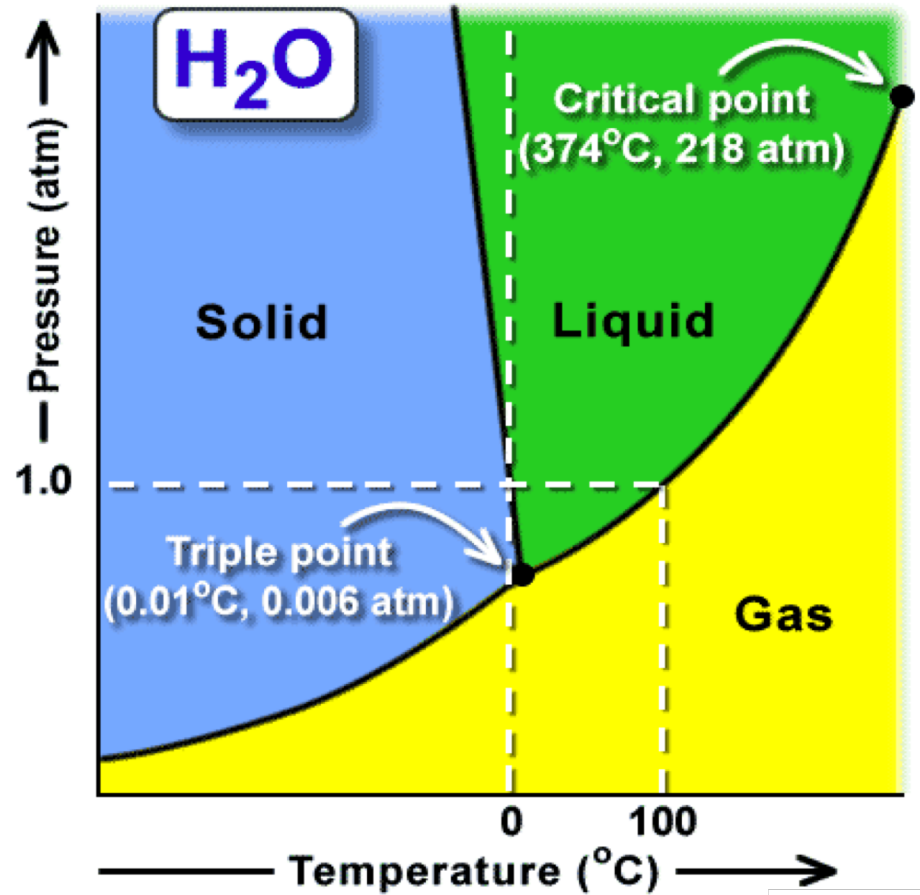


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Central China Normal University



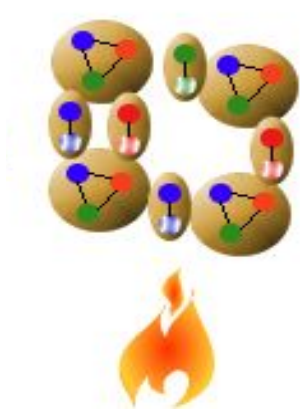
# Water



**Dominated by EM interactions**



# What will happen, if we Heat matter to trillion ( $10^{12}$ ) degree ?

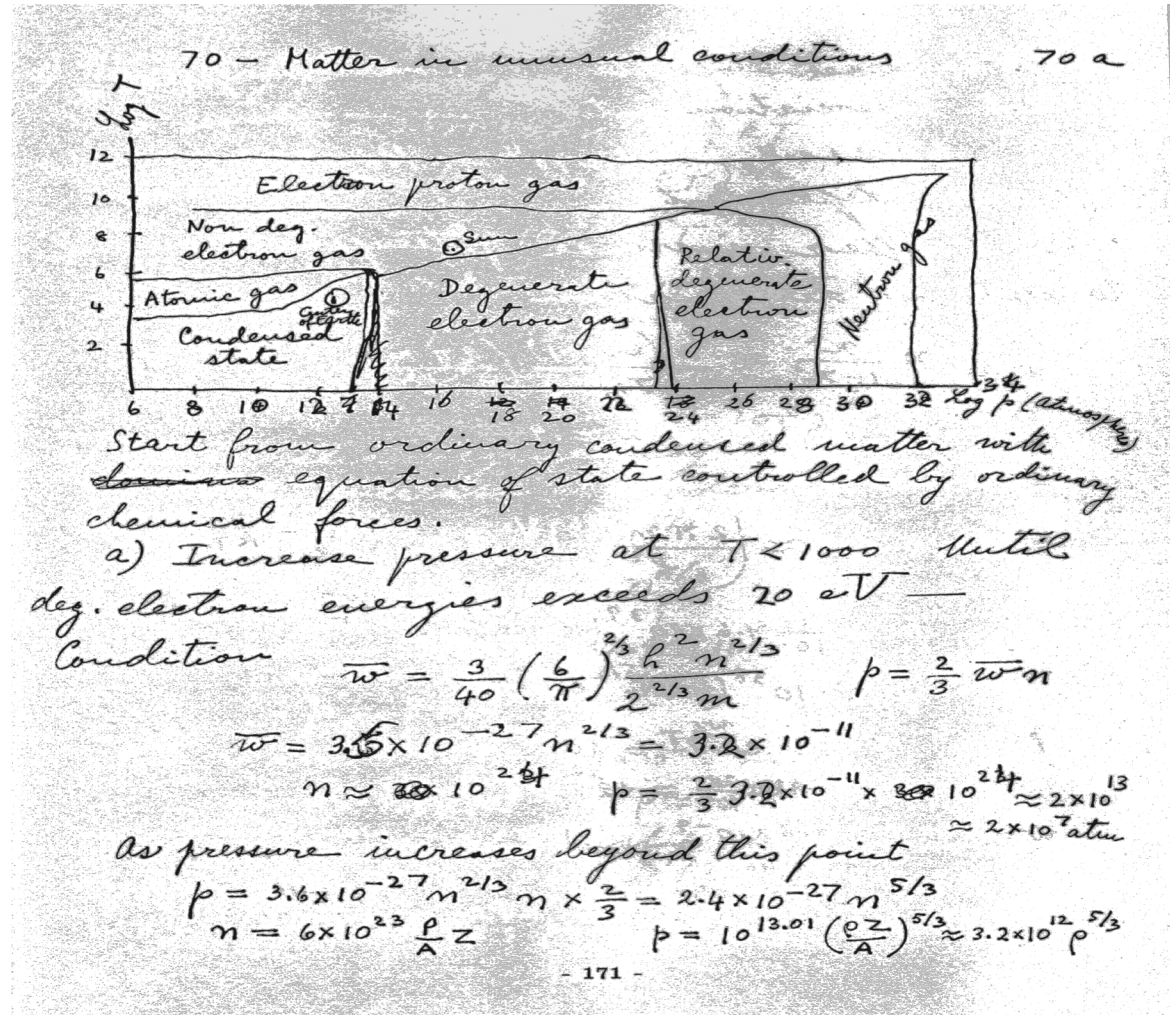


# Matter Under Extreme Condition (1953)

## E. Fermi: "Notes on Thermodynamics and Statistics" (1953)



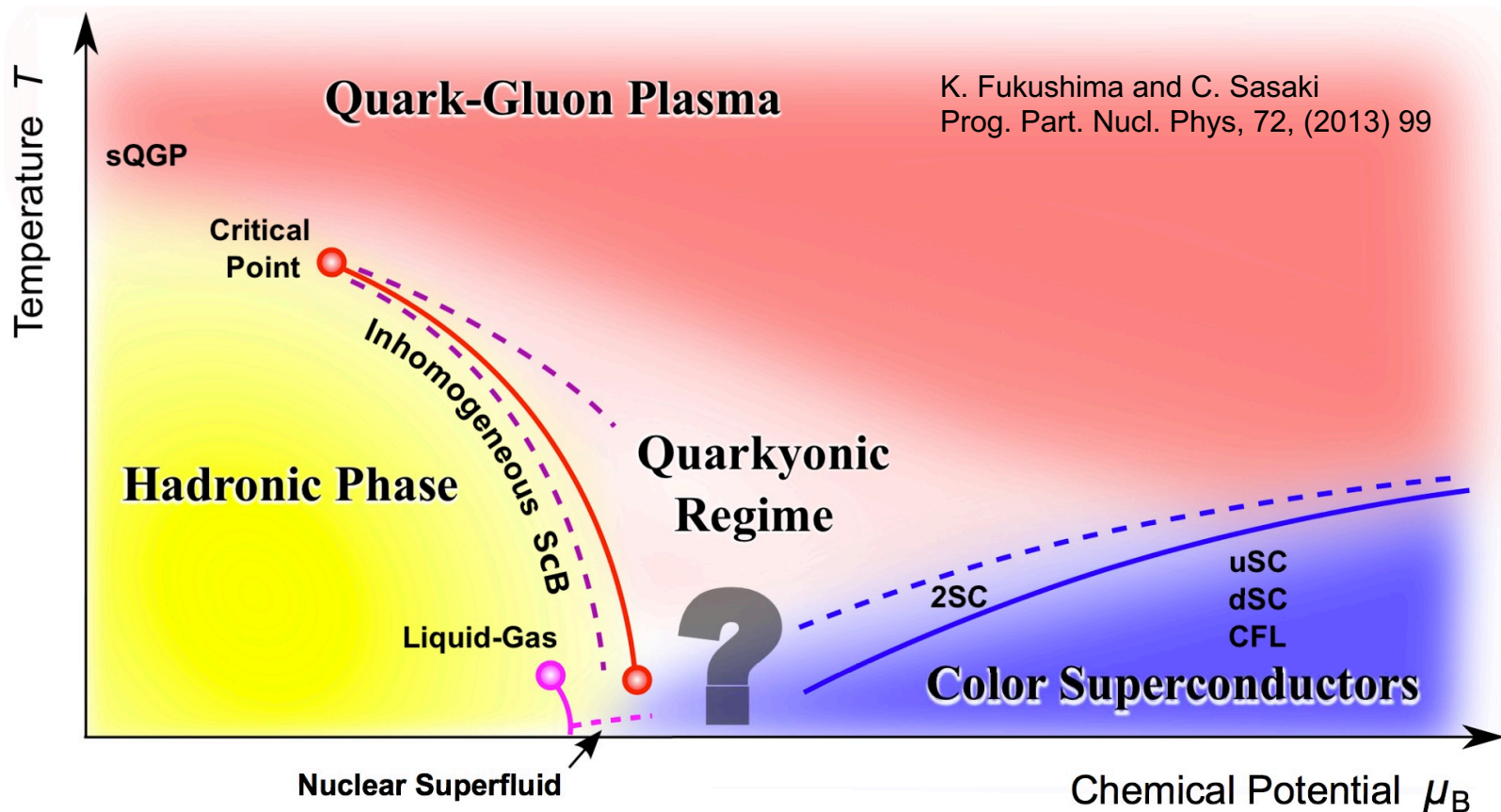
E. Fermi





# QCD Phase Diagram (2013)

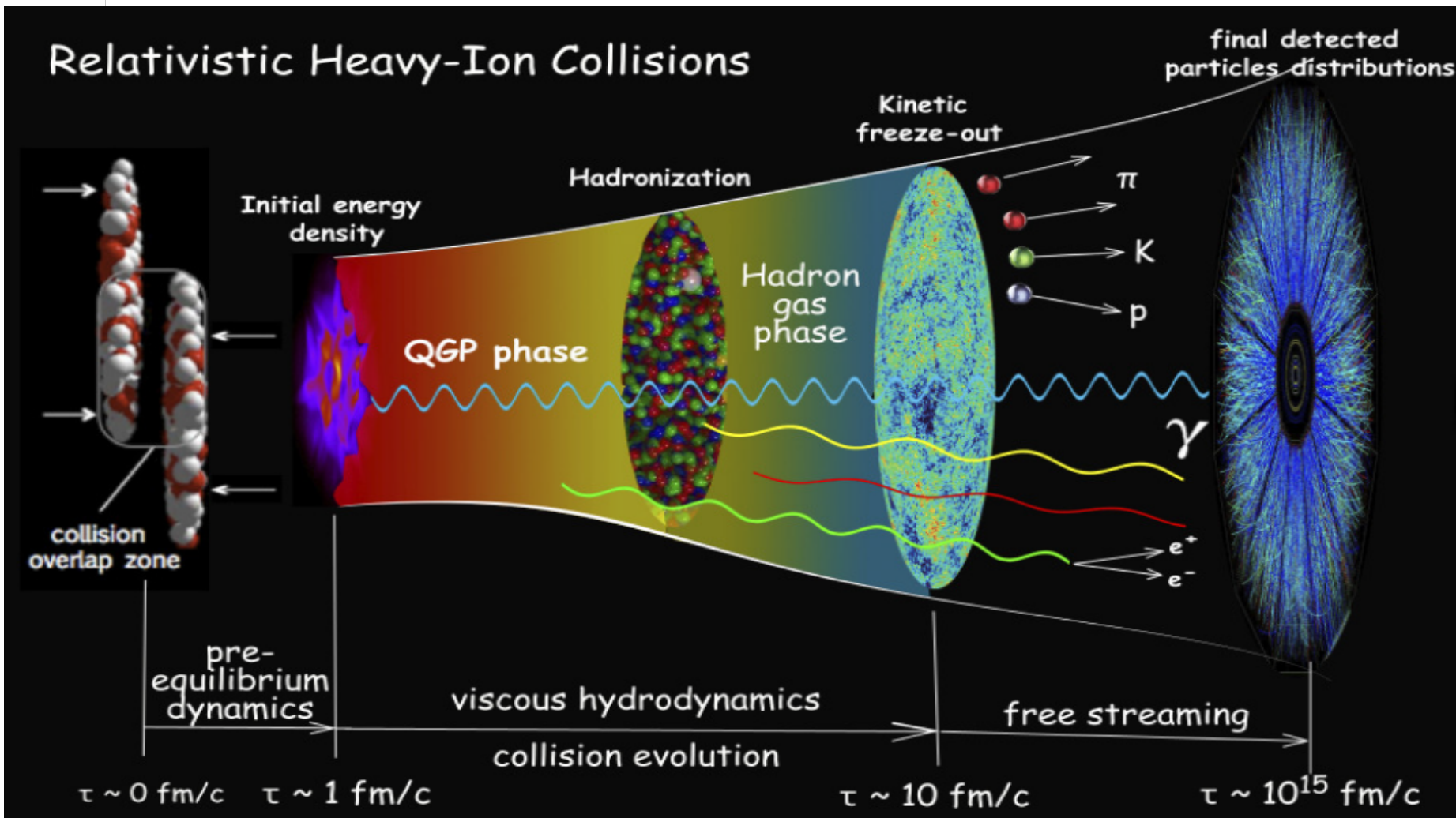
Very rich physics at high baryon density region.



1. High Temperature : Early Universe
2. High Baryon density : Neutron star etc.

1. 1<sup>st</sup> order Phase Transition ?
2. Critical point ?

# Relativistic Heavy-Ion Collisions



Relativistic heavy-ion collisions are a unique tool to create and study hot QCD matter and its phase transition under controlled conditions



# Location of CEP: Theoretical Prediction

## ➤ **Lattice QCD:**

1): Fodor&Katz, JHEP 0404,050 (2004):

$$(\mu_B^E, T_E) = (360, 162) \text{ MeV (Reweighting)}$$

2): Gavai&Gupta, NPA 904, 883c (2013)

$$(\mu_B^E, T_E) = (279, 155) \text{ MeV (Taylor Expansion)}$$

3): F. Karsch et al. NPA 956, 352 (2016).

$$(\mu_B^E / T_E > 2)$$

## ➤ **Dyson-Schwinger Equation (DSE):**

1): Y. X. Liu, et al., PRD90, 076006 (2014); 94, 076009 (2016). PRL

$$(\mu_B^E, T^E) = (372, 129) ; (262.3, 126.3) \text{ MeV} \\ (330, 128), L=2\text{fm} (450, 109)$$

2): Hong-shi Zong et al., JHEP 07, 014 (2014).

$$(\mu_B^E, T_E) = (405, 127) \text{ MeV}$$

3): C. S. Fischer et al., PRD90, 034022 (2014).

$$(\mu_B^E, T^E) = (504, 115) \text{ MeV}$$

## ➤ **Functional Renormalization Group (FRG):**

$$(\mu_B^E, T^E) = (635, 107) ; \text{Weijie Fu et al.}$$

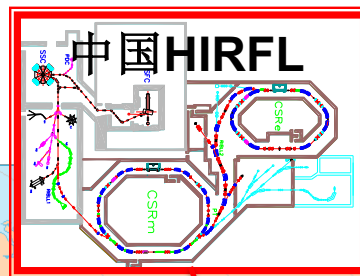
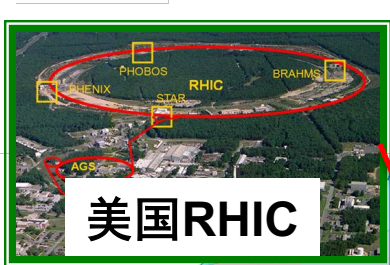
$$(\mu_B^E, T^E) = (780, 55); \text{Defu Hou et al. PRD96 (2017)}$$

➤ **PNJL**,  $(\mu_B^E, T^E) = (720, 90)$ , Mei Huang, et al. EPJC 79, 245 (2019).

$$\mu_B^E = 262 \sim 780 \text{ MeV}, T_E = 55 \sim 162 \text{ MeV}$$



# Exploring the QCD Phase Structure



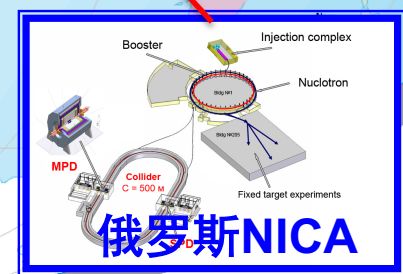
CEE !!!



2023

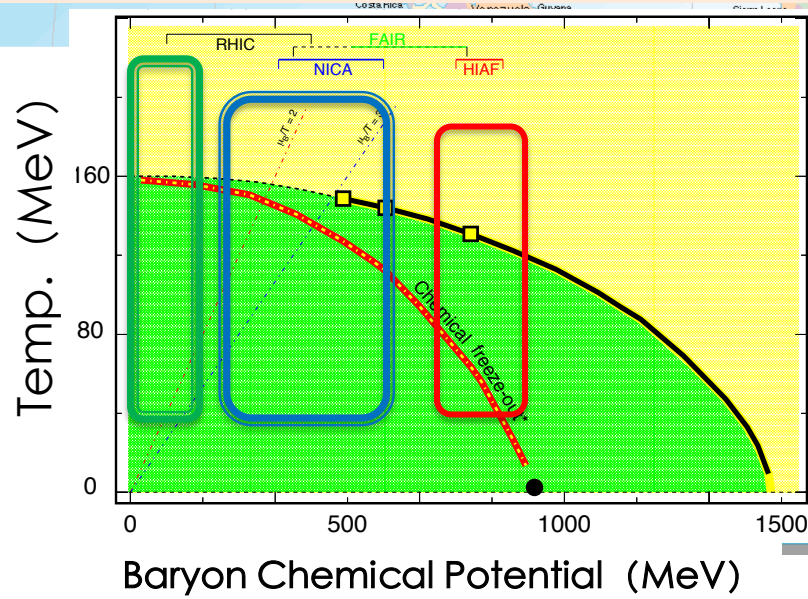


2025



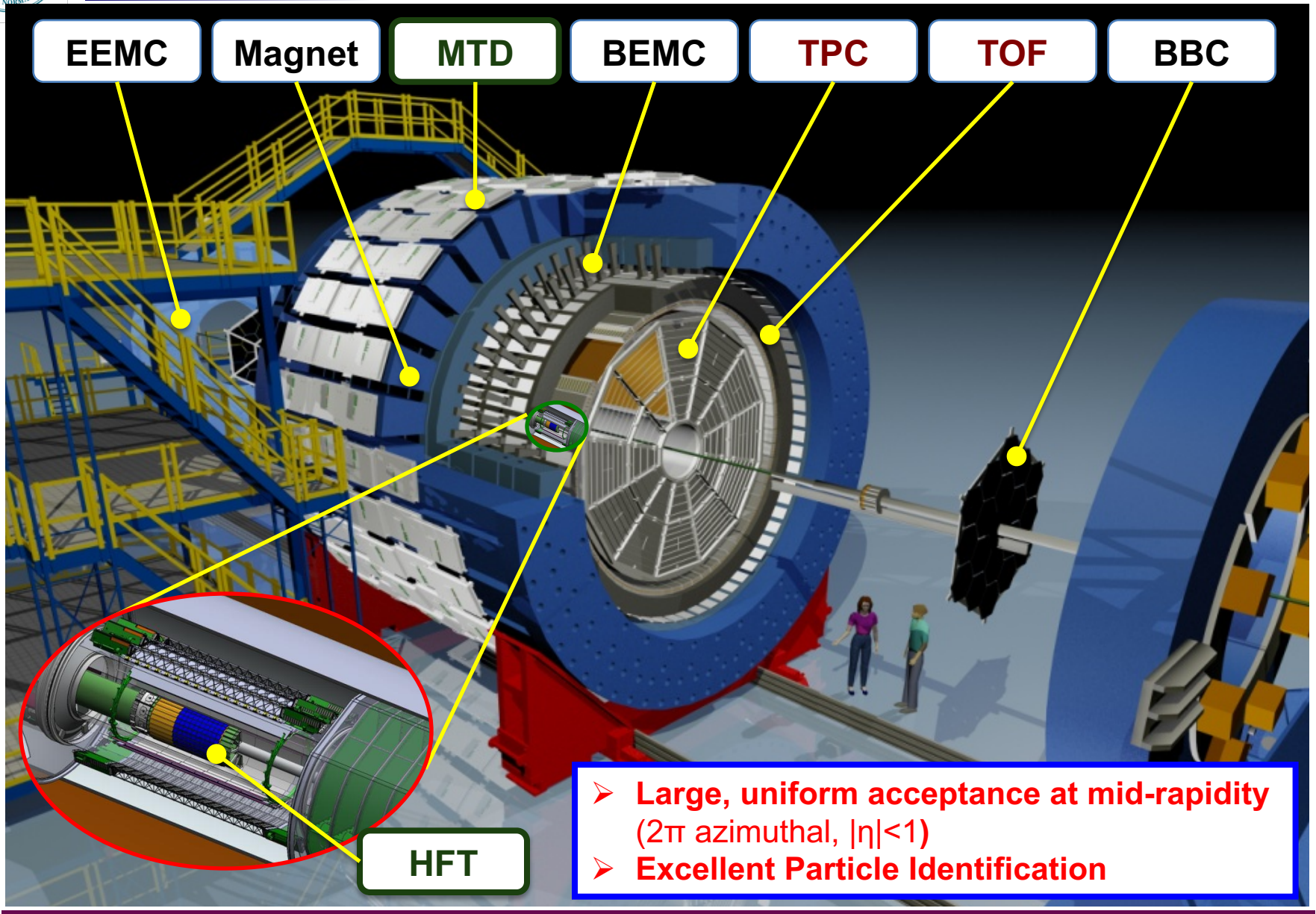
2023

Exploring QCD phase structure at High Baryon Density





# STAR Detector System

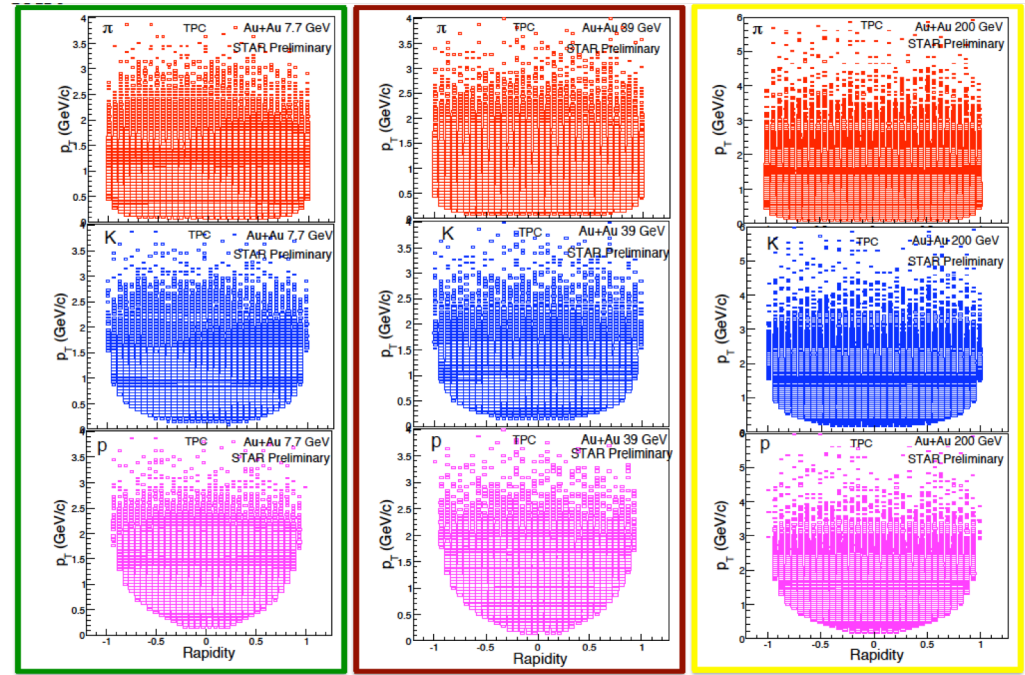




# RHIC Beam Energy Scan Phase I (2010-2017)

$\sqrt{s_{NN}}$ (GeV)	Year	Events ( $10^6$ )	* $\mu_B$ (MeV)	* $T_{CH}$ (MeV)
200	2010	238	25	166
62.4	2010	45	73	165
<b>54.4</b>	<b>2017</b>	<b>1200</b>	<b>83</b>	<b>165</b>
39	2010	86	112	164
27	2011	32	156	162
19.6	2011	15	206	160
14.5	2014	13	264	156
11.5	2010	7	316	152
7.7	2010	3	422	140

Uniform acceptance at Mid-rapidity



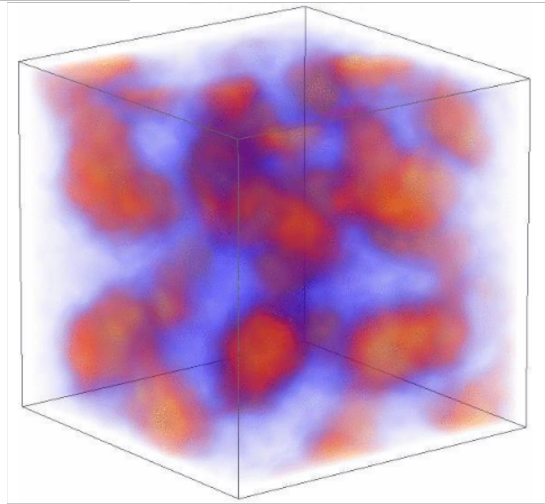
\*( $\mu_B, T_{CH}$ ) : J. Cleymans et al., PRC 73, 034905 (2006)

➤ Access the QCD phase diagram: vary collision energies/centralities.

**RHIC BES-I :  $20 < \mu_B < 420$  MeV**



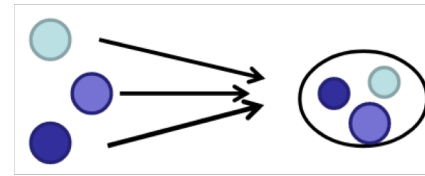
# Search for the QCD critical point



In the vicinity of critical point

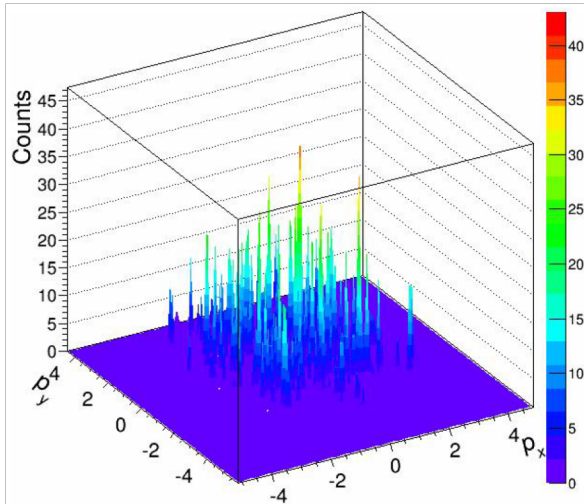


Large density fluctuations and long range corr.



**E-by-E conserved charge  
(B, Q, S) fluctuations**

**Baryon clustering:  
light nuclei production**



**Experimental Signatures:**

**Non-monotonic variation as a function of  
collision energy.**



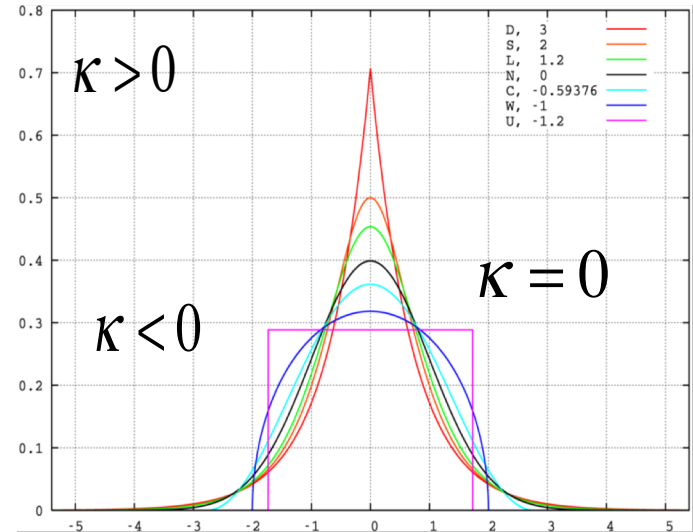
# Higher Moments of Conserved Quantities

Cumulants of the event-by-event net-proton, net-charge and net-kaon distributions.

➤ **Net-Proton:**  $N_p - N_{\bar{p}}$   
(Net-Baryon,  $B$ )

➤ **Net-Charge:**  $N_{Q^+} - N_{Q^-}$

➤ **Net-Kaon:**  $N_{K^+} - N_{K^-}$   
(Net-Strangeness,  $S$ )



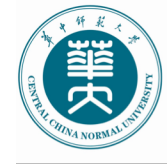
$$C_{2,q} \propto \xi^2, C_{3,q} \propto \xi^{4.5}, C_{4,q} \propto \xi^7$$

$$\frac{C_{4,q}}{C_{2,q}} = \kappa \sigma^2 \propto \xi^5$$

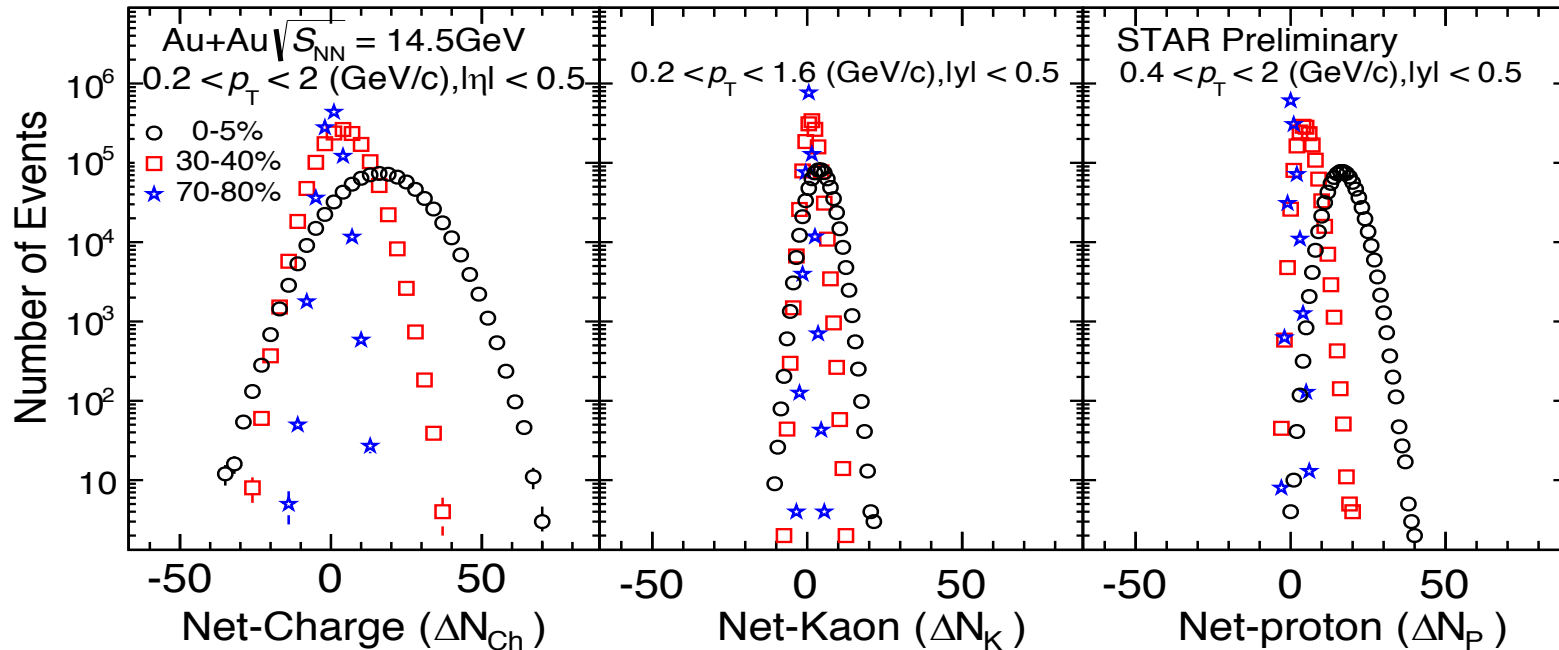
$$\frac{C_{3,q}}{C_{2,q}} = S \sigma \propto \xi^{9/4}$$

M. A. Stephanov, *Phys. Rev. Lett.* 102, 032301 (2009).

M. Asakawa, S. Ejiri and M. Kitazawa, *Phys. Rev. Lett.* 103, 262301 (2009).



# Data Analysis Methods



Analysis Methods used in the STAR coll.

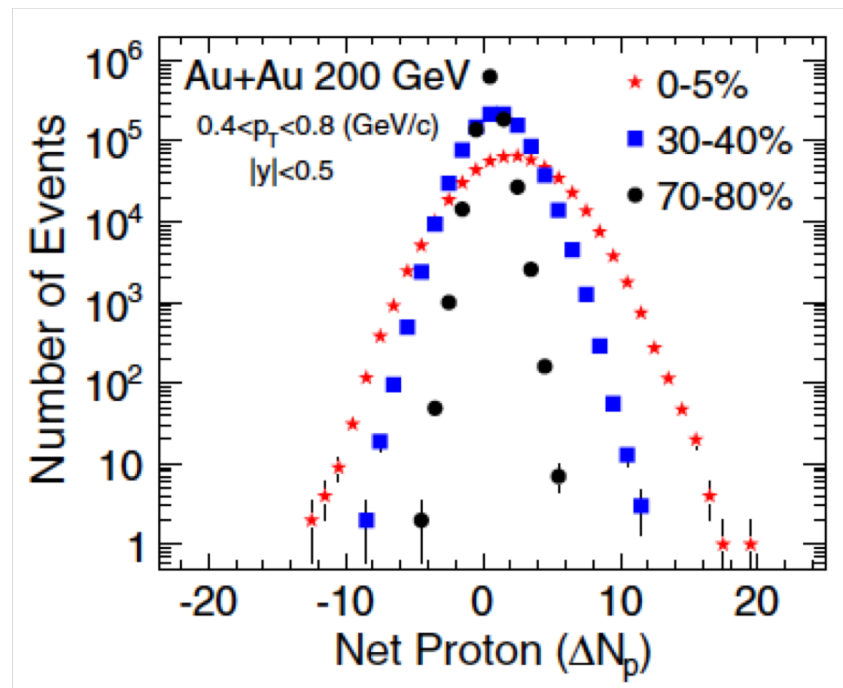
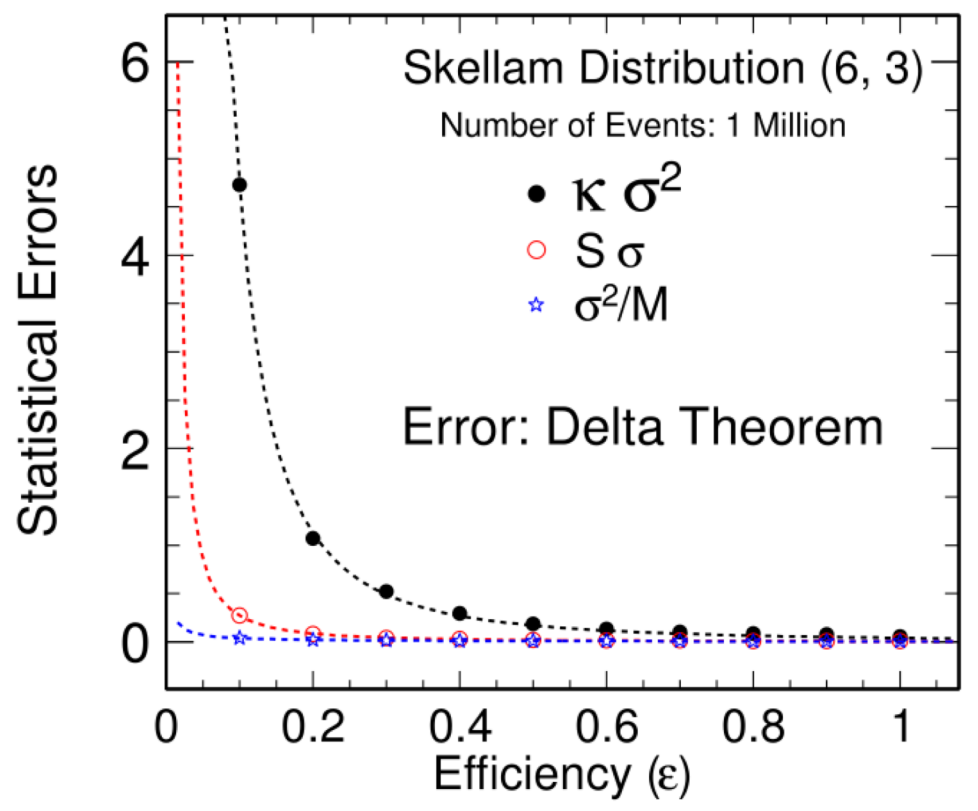
1. Statistical errors estimation : Delta theorem or bootstrap
2. Avoid auto-correlation effects: New centrality definition.
3. Suppress volume fluctuation: Centrality bin width correction
4. Finite detector efficiency correction (binomial response func.)

*Review Article : X. Luo and N. Xu, Nucl. Sci. Tech. 28, 112 (2017).*

X.Luo, J. Phys. G 39, 025008 (2012); A. Bzdak and V. Koch, PRC86, 044904 (2012); X.Luo, et al. J. Phys. G40, 105104(2013); X.Luo, Phys. Rev. C 91, 034907 (2015); A. Bzdak and V. Koch, PRC91, 027901 (2015). T. Nonaka et al., PRC95, 064912 (2017). M. Kitazawa and X. Luo, PRC96, 024910 (2017). X. Luo, T. Nonaka, PRC99, 044917 (2019);



# Statistical Errors Estimation and Properties

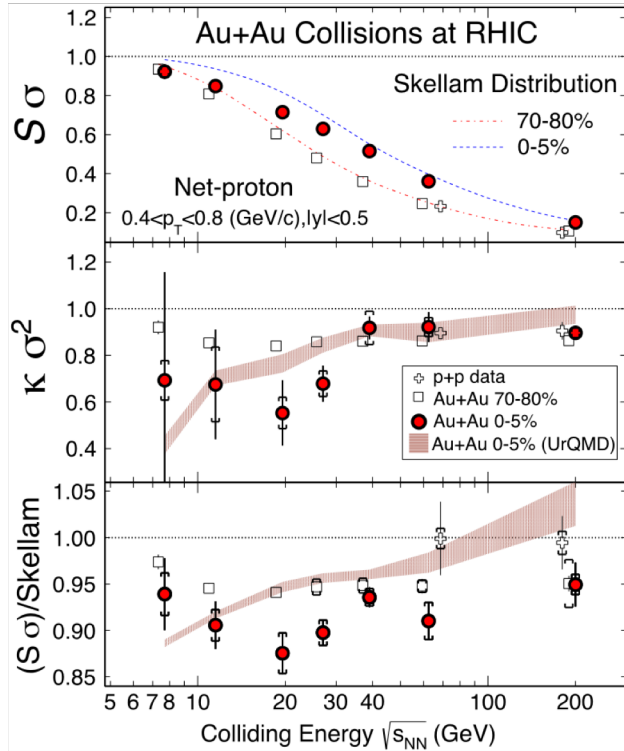


$$error(\kappa\sigma^2) \propto \frac{\sigma^2}{\varepsilon^2} \frac{1}{\sqrt{N_{evts}}}$$

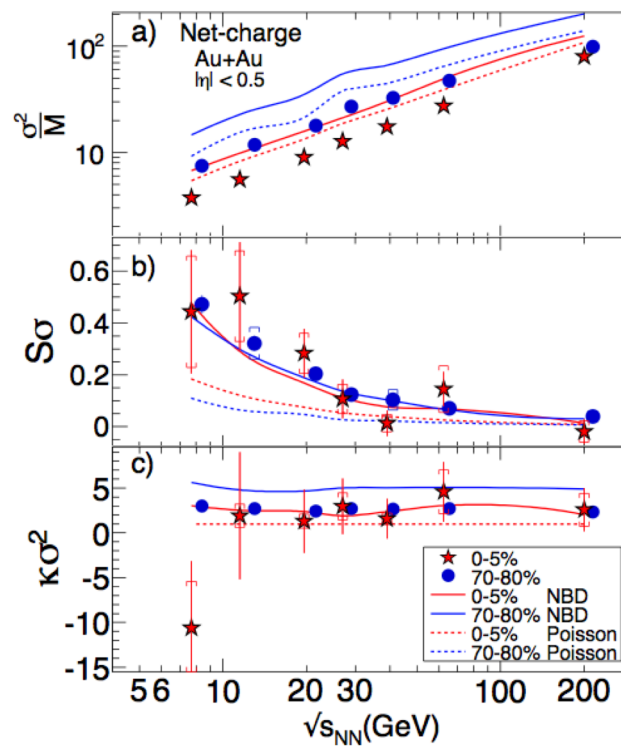
- X. Luo, *J. Phys. G* 39, 025008 (2012);
- X. Luo, *Phys. Rev. C* 91, 034907 (2015);
- X. Luo, T. Nonaka, *Phys. Rev. C* 99, 044917 (2019);

Statistical errors strongly depend on the : Width of the measured distributions ( $\sigma$ ) and the detector efficiency ( $\varepsilon$ ).

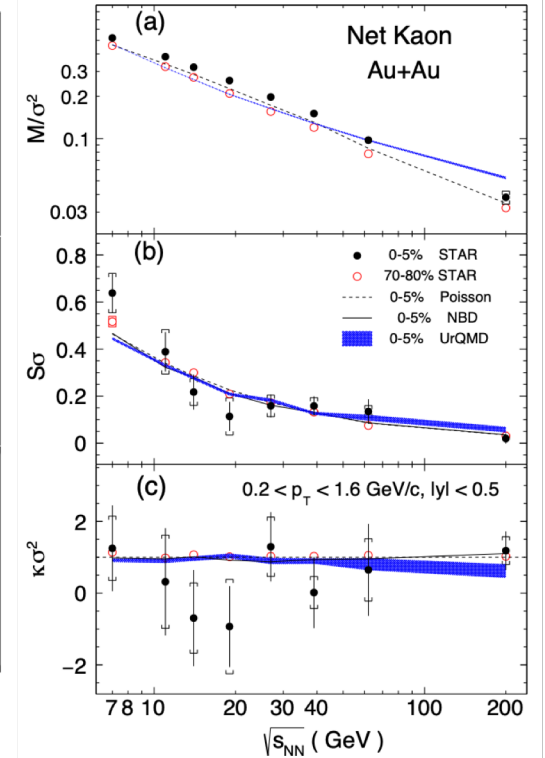
## Net-Proton



## Net-Charge



## Net-Kaon



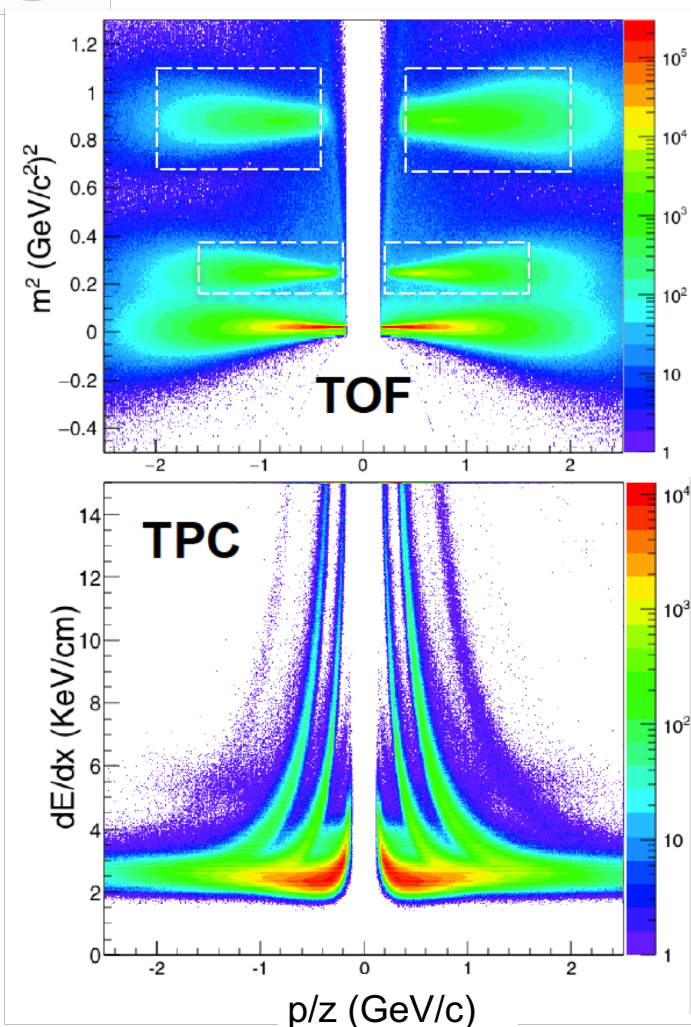
Phys. Rev. Lett. 105, 022302 (2010).  
Phys. Rev. Lett. 112, 032302 (2014).

Phys. Rev. Lett. 113 092301 (2014).

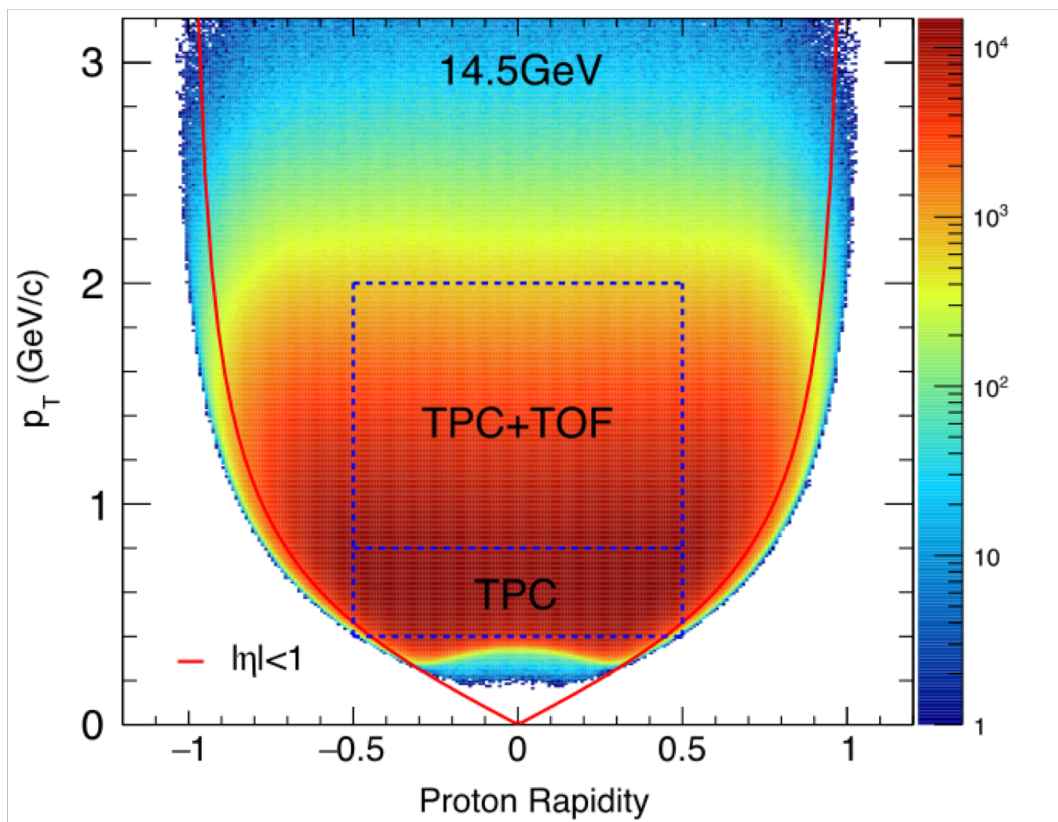
Phys. Lett. B 785, 551 (2018).

- Net-Proton :Both 3rd- and 4th-order fluctuations have their minima at  $\sqrt{s} = 19.6$  GeV.
- Net-charge and Net-kaon: large statistical errors, need more statistics.

# Extend $p_T$ coverage for (Anti-) Proton

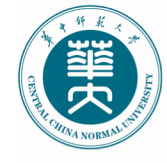


$|y| < 0.5$ ,  $0.4 < p_T < 0.8$  (TPC PID)  
 $0.8 < p_T < 2$  (TPC+TOF PID)



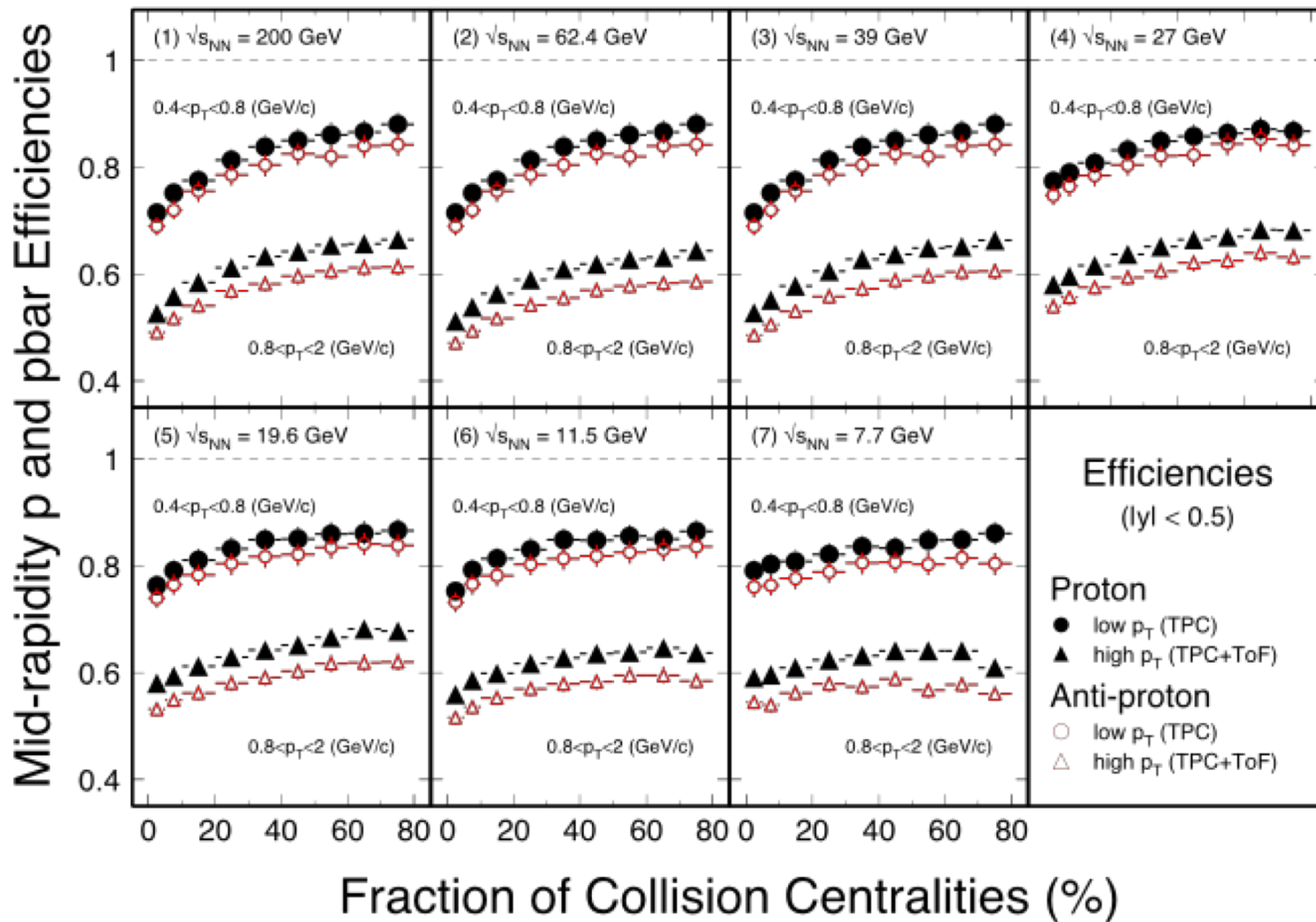
- $p_T$  region can be extended up to 2.0 GeV by using TOF as well as TPC.
- (Anti)proton statistics is doubled with respect to the published results.





# (Anti-) Proton Acceptance and Efficiencies

## Au + Au Collisions at RHIC



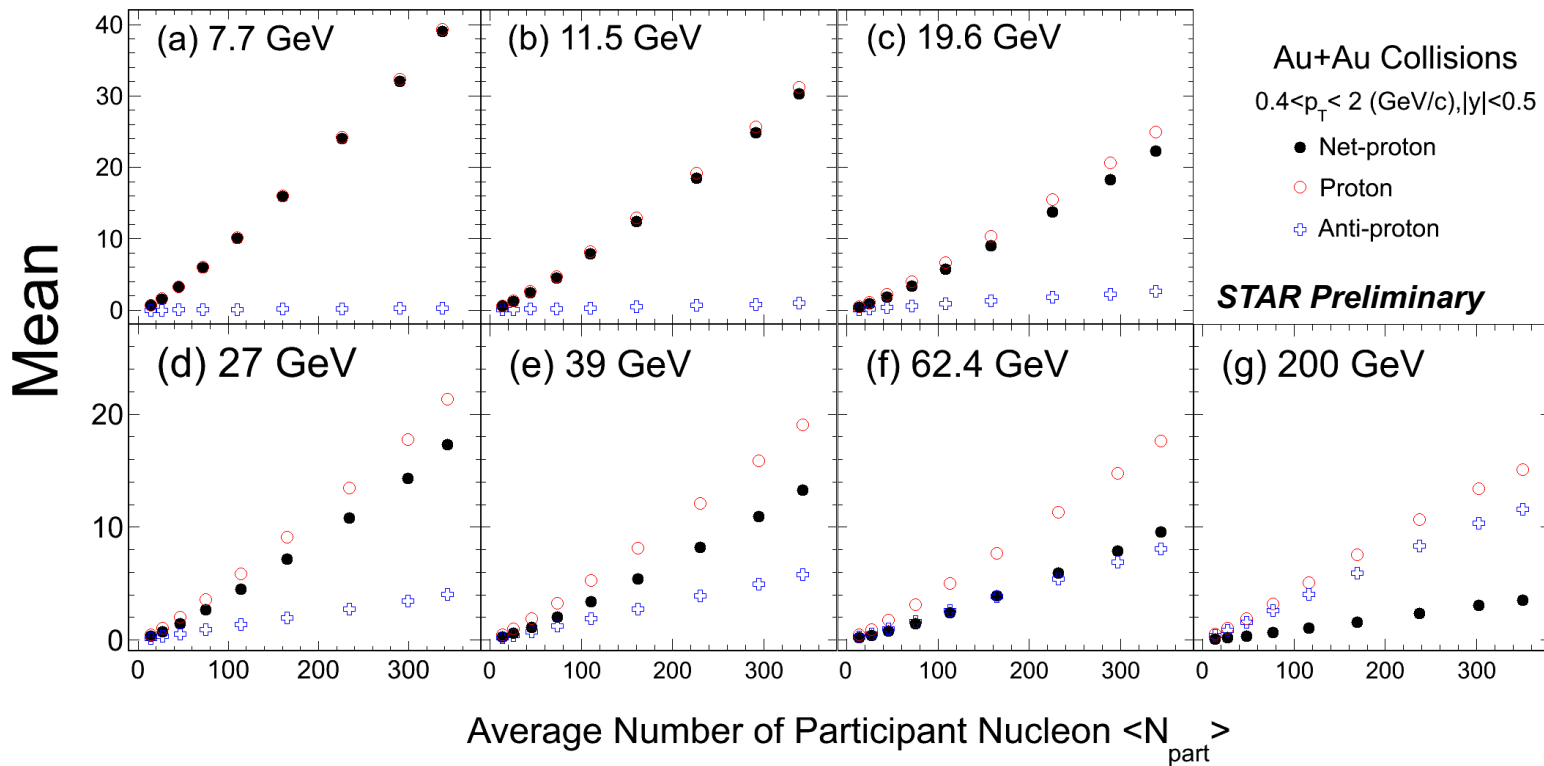
TPC

TPC+TOF

➤ Efficiency : Proton > Anti-proton, Low  $p_T$  > High  $p_T$ , low energy > High Energy, Peripheral > Central



# Results: Mean Net-p, p and pbar



- Mean Net-proton, proton and anti-proton number increase with  $\langle N_{part} \rangle$
- Net-proton number is dominated by protons at low energies and increases when energy decreases.  
(Interplay between baryon stopping and pair production)

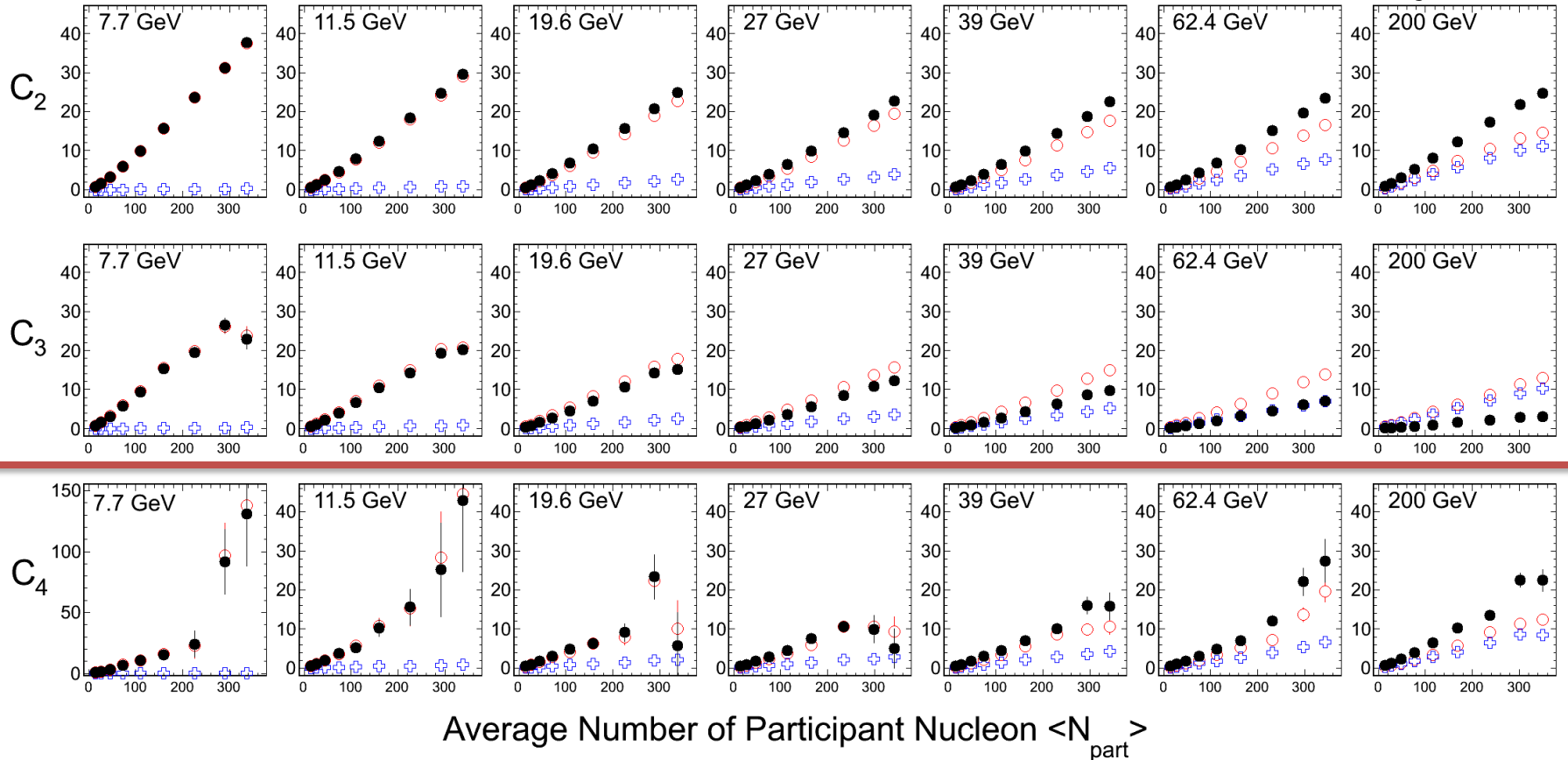


# Higher Order Cumulants for Net-p, p, pbar

Au+Au Collisions  $0.4 < p_T < 2$  (GeV/c),  $|y| < 0.5$

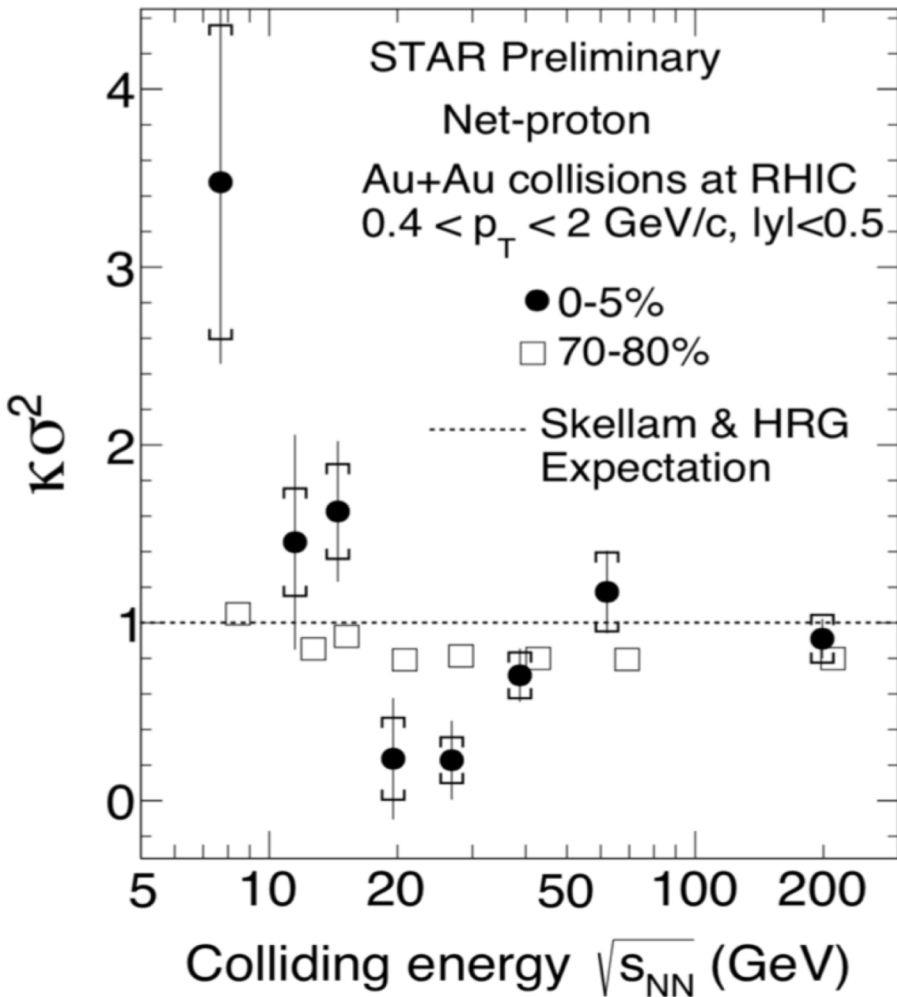
● Net-proton ○ Proton + Anti-proton

STAR Preliminary



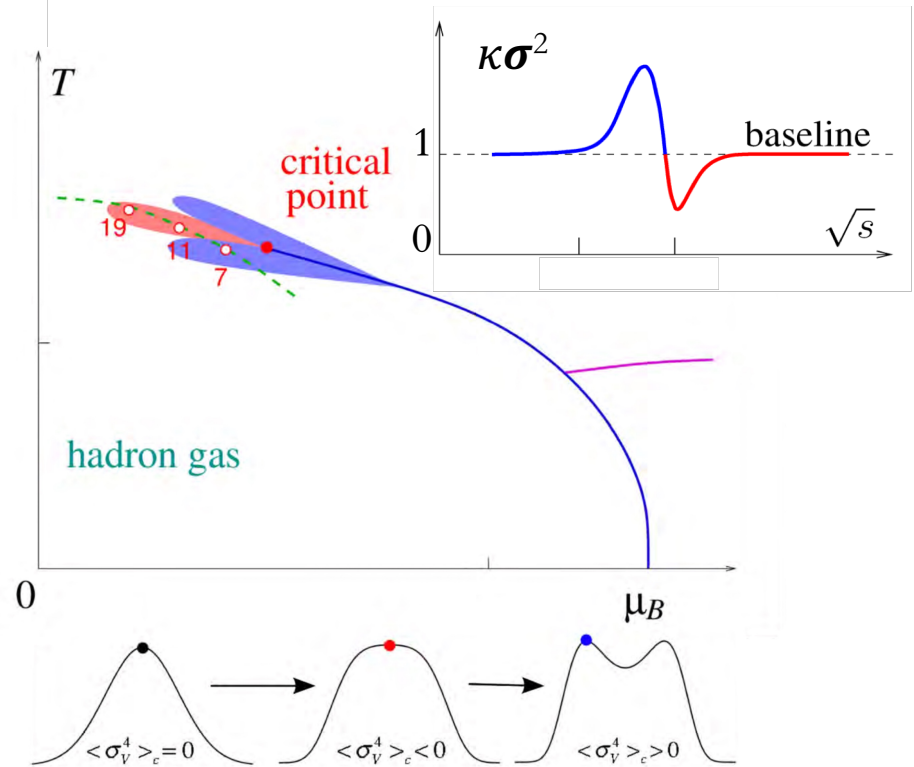
- In general, cumulants of Net-p, p and pbar are increasing with  $\langle N_{part} \rangle$ .
- The cumulants of net-proton distributions closely follow the proton cumulants when the colliding energy is decreasing.

# Fourth Order Net-Proton Fluctuations



STAR: Phys. Rev. Lett. 105, 022302 (2010).  
Phys. Rev. Lett. 112, 032302 (2014).  
PoS CPOD2014 (2015) 019.

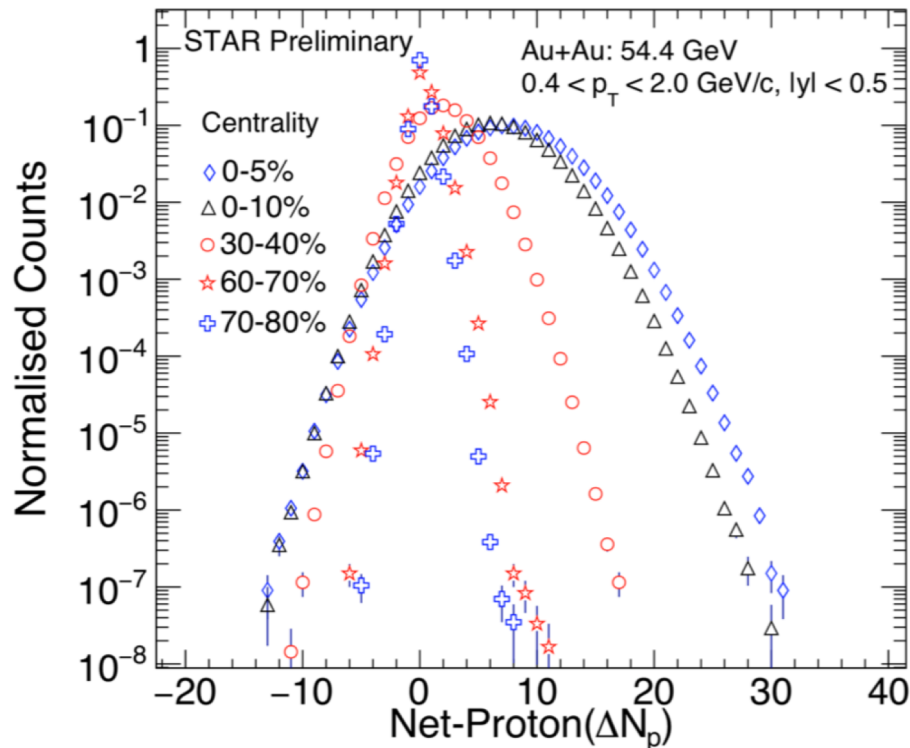
➤ First observation of the non-monotonic energy dependence of fourth order net-proton fluctuations. **Hint of entering Critical Region ?**



M. Stephanov, PRL107, 052301(2011)  
J. Phys. G: 38, 124147 (2011).

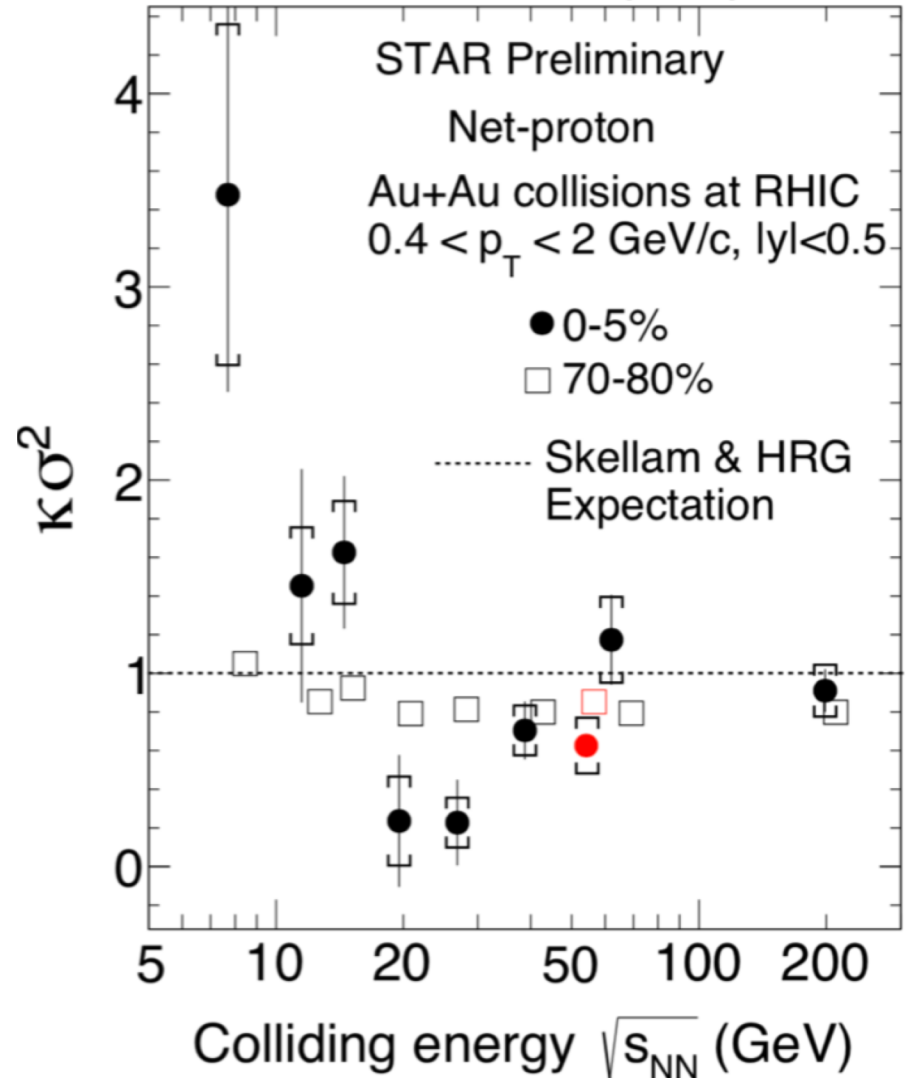


# New data set : 54.4 GeV (2017)

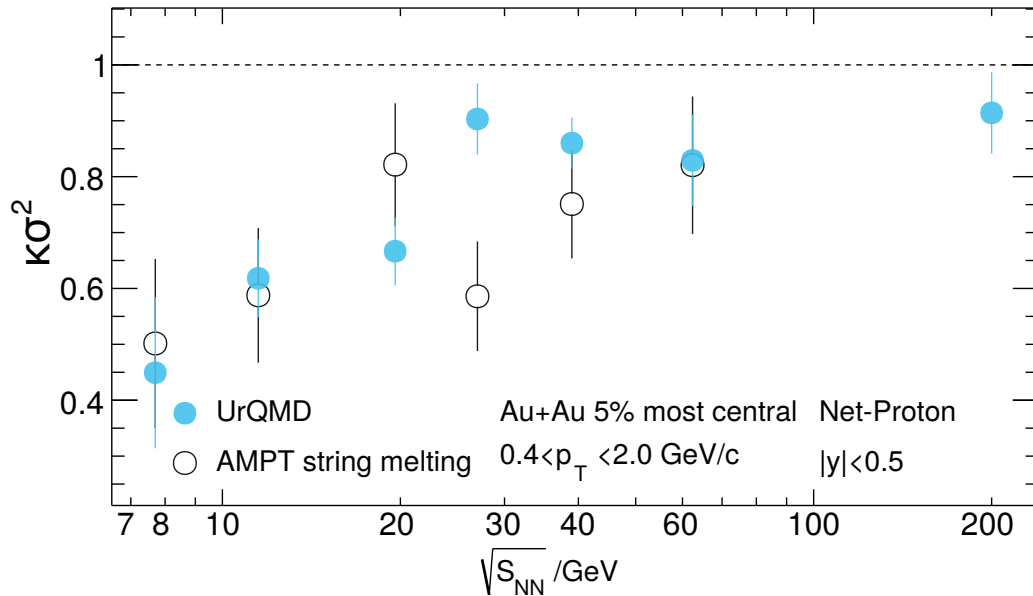


STAR, SQM 2019

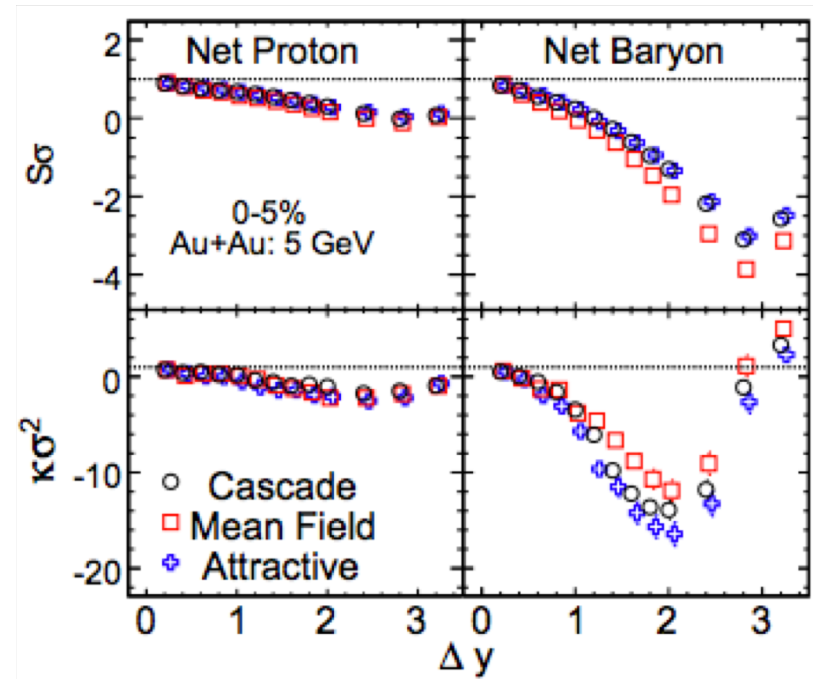
➤ Results at 54.4 GeV follow the trend well.



## UrQMD and AMPT models



## JAM model



- Transport model (no CP physics) results show monotonic energy dependence: dominated by baryon number conservations
- Mean field potential can not explain the enhancement of  $\kappa\sigma^2$  at low energy.

Z. Feckova, et al., PRC92, 064908(2015). J. Xu, et. al., PRC94, 024901(2016). X. Luo et al., NPA931, 808(14), P.K. Netrakanti et al. 1405.4617, NPA947, 248(2016), P. Garg et al. PLB 726, 691(2013). S. He, et. al., PLB762, 296 (2016). S. He, X. Luo, PLB 774, 623 (2017).



# Net-Proton Fluctuation Paper Plan

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Short Paper : Nature Physics

Long Paper : PRC

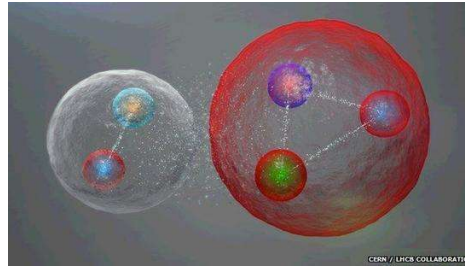
Paper draft are ready.  
Going through collaboration process

The two papers will be submitted  
to the journal simultaneously.

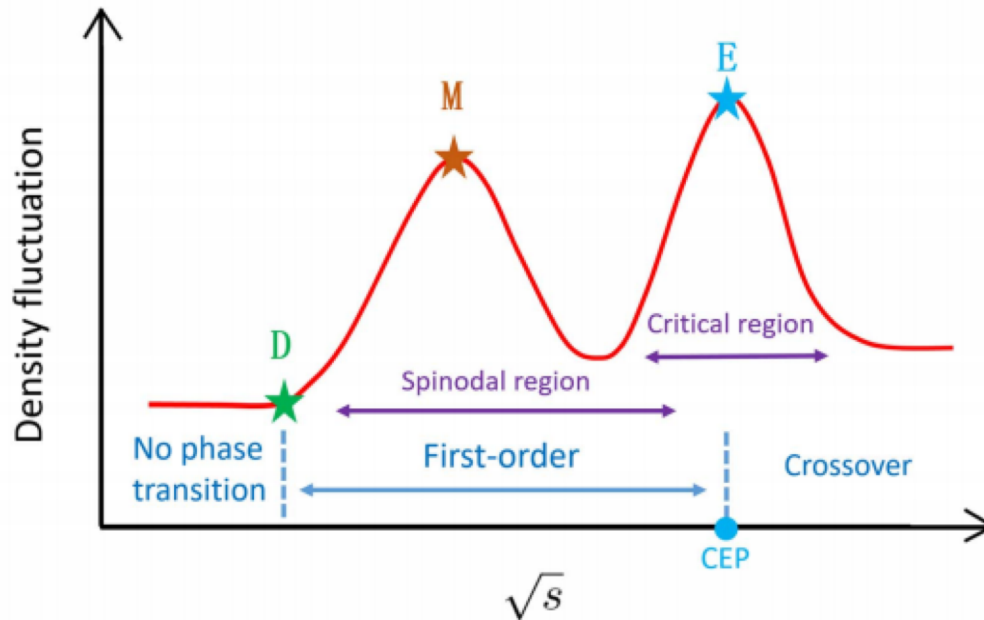


# New Observable for CP: Light Nuclei Production

Near CP or 1<sup>st</sup> order phase transition, baryon density fluctuation become large.



Light nuclei production  
(Baryon Clustering)



Coalescence + nucleon density flu.

$$N_d = \frac{3}{2^{1/2}} \left( \frac{2\pi}{m_0 T_{\text{eff}}} \right)^{3/2} N_p \langle n \rangle (1 + \alpha \Delta n),$$

$$N_{3H} = \frac{3^{3/2}}{4} \left( \frac{2\pi}{m_0 T_{\text{eff}}} \right)^3 N_p \langle n \rangle^2 [1 + (1 + 2\alpha) \Delta n],$$

$$N_t \cdot N_p / N_d^2 \approx g(1 + \Delta n)$$

Neutron density fluctuations:

$$\Delta n = \langle (\delta n)^2 \rangle / \langle n \rangle^2$$

K. J. Sun, L. W. Chen, C. M. Ko, Z. Xu, Phys. Lett. B774, 103 (2017).

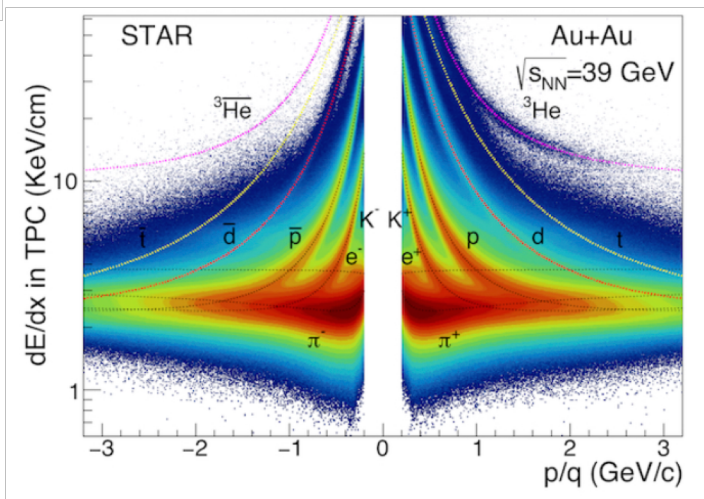
K. J. Sun, L. W. Chen, C. M. Ko, J. Pu, Z. Xu, Phys. Lett. B781, 499 (2018).

Edward Shuryak and Juan M. Torres-Rincon, arXiv:1805.04444

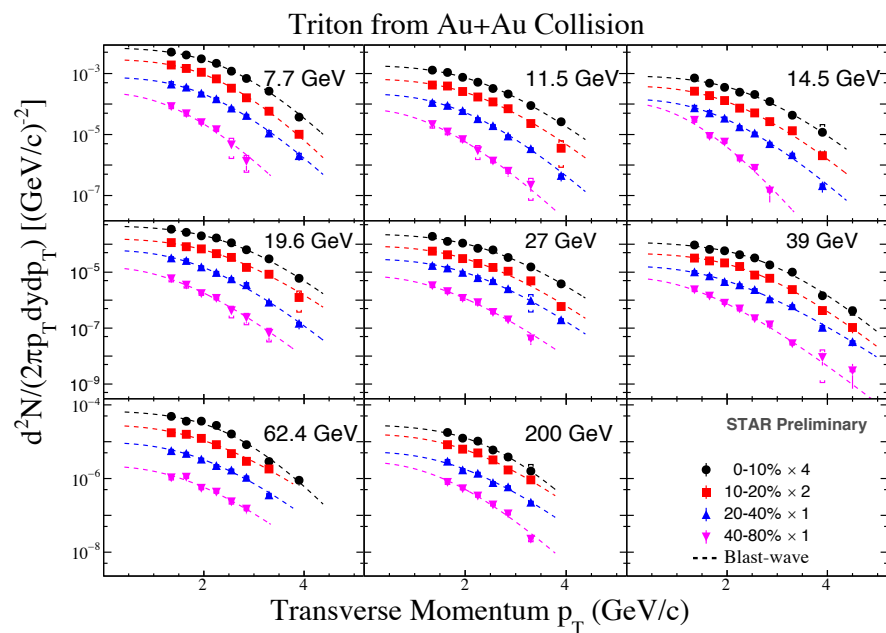
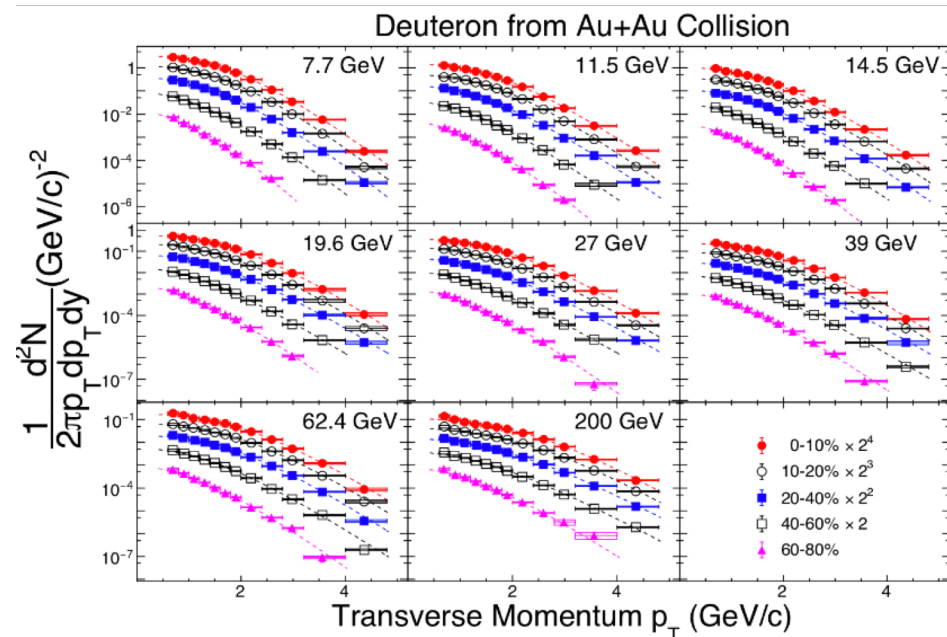
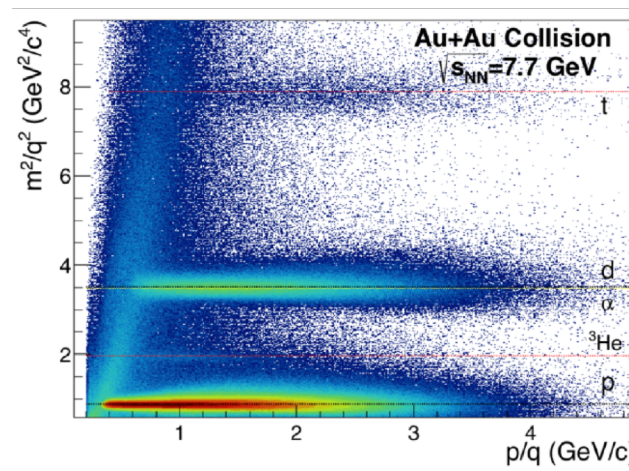


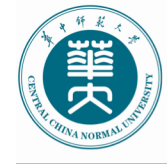


# Deuteron and triton production from BES-I at RHIC



STAR, PRC99, 064905 (2019)



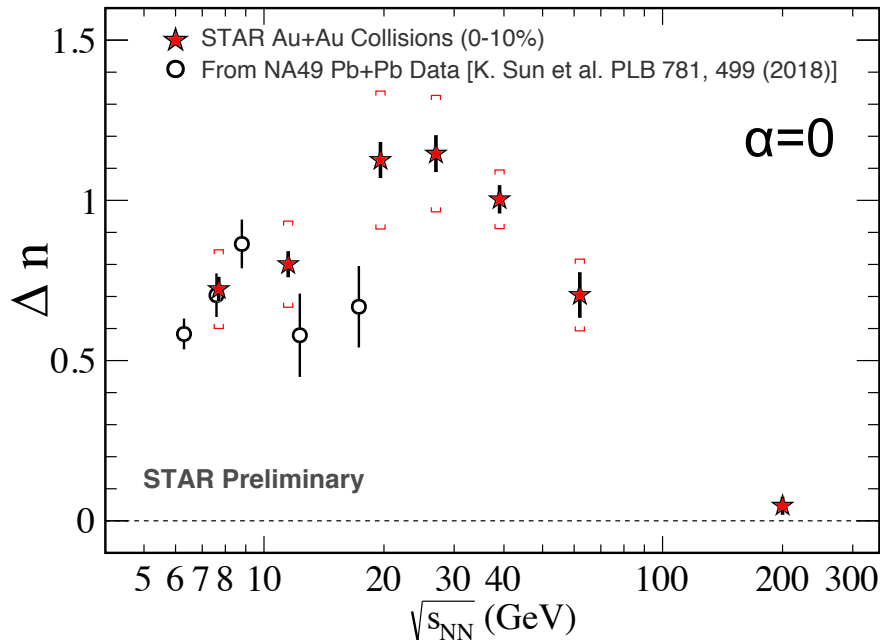


# Nucleon Density Fluctuations

- The particle ratios of light nuclei is sensitive to the **nucleon density fluctuation** at kinetic freeze-out. This conclusion is based on **coalescence model**.

$$N_d = \frac{3}{2^{\frac{1}{2}}} \left( \frac{2\pi}{m_0 T_{eff}} \right)^{3/2} N_p \langle n \rangle (1 + \alpha \Delta n)$$

$$N_t = \frac{3^{3/2}}{4} \left( \frac{2\pi}{m_0 T_{eff}} \right)^3 N_p \langle n \rangle^2 [1 + (1 + 2\alpha)\Delta n]$$



Dingwei Zhang, NN 2018

$$\frac{\langle (\delta n)^2 \rangle}{\langle n \rangle^2} = \Delta n = \frac{1}{g} \frac{N_t N_p}{N_d^2} - 1$$

$N_t$  : Triton yield,  $N_d$  : Deuteron yield  
 $N_p$  : Proton yield

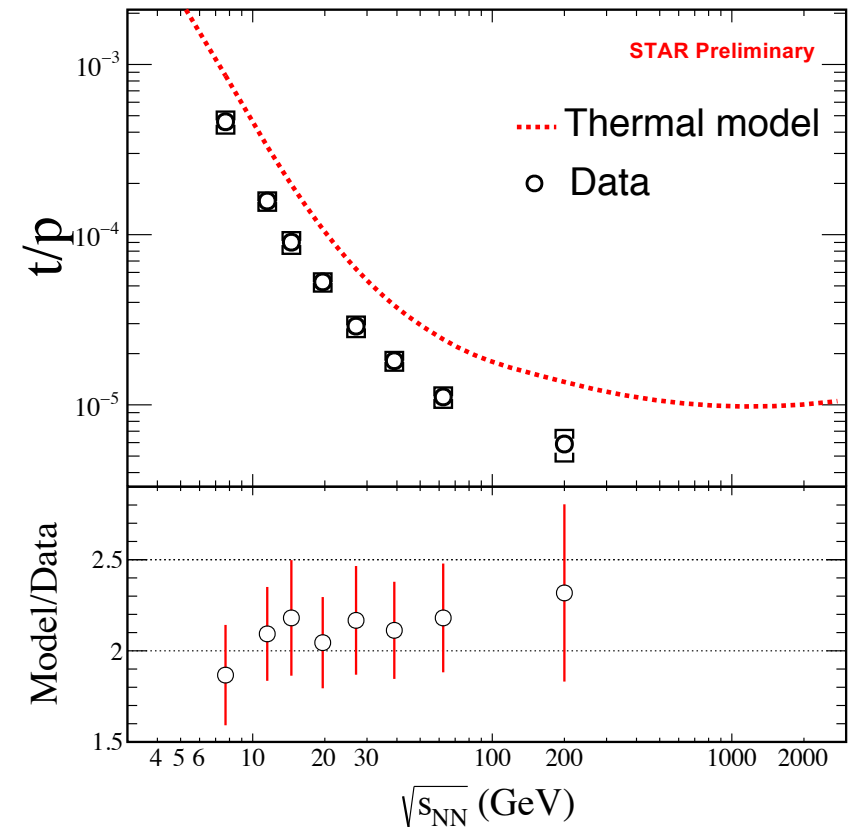
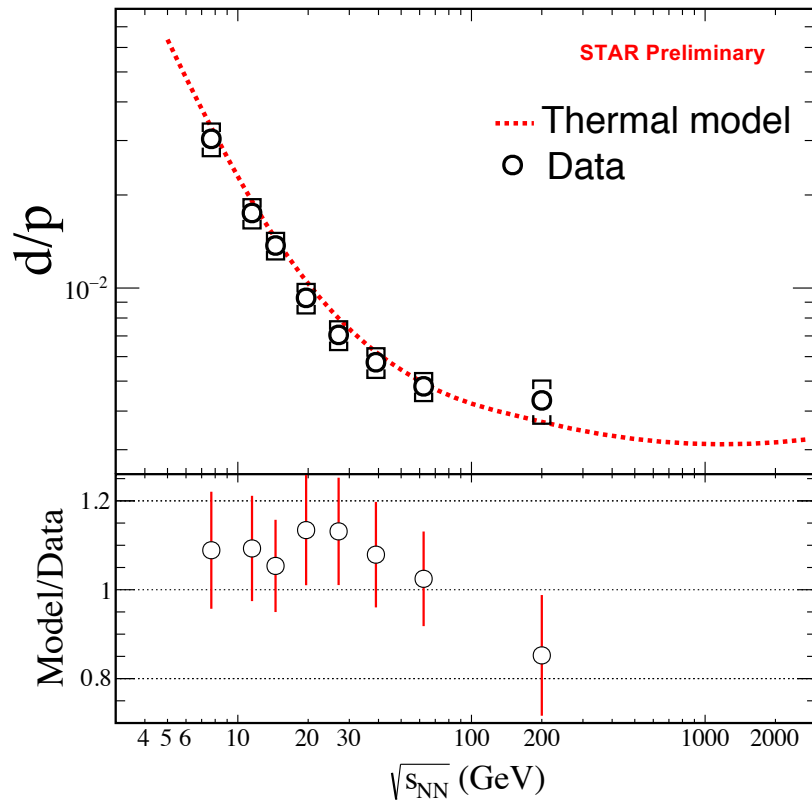
Neutron density fluctuation  $\Delta n$  shows a **non-monotonic behavior** on collision energy.

Peak around 20 GeV.

K. J. Sun, L. W. Chen, C. M. Ko, Z. Xu, Phys. Lett. B774, 103 (2017).  
 K. J. Sun, L. W. Chen, C. M. Ko, J. Pu, Z. Xu, Phys. Lett. B781, 499 (2018).  
 Edward Shuryak and Juan M. Torres-Rincon, NPA 982, 831 (2019)



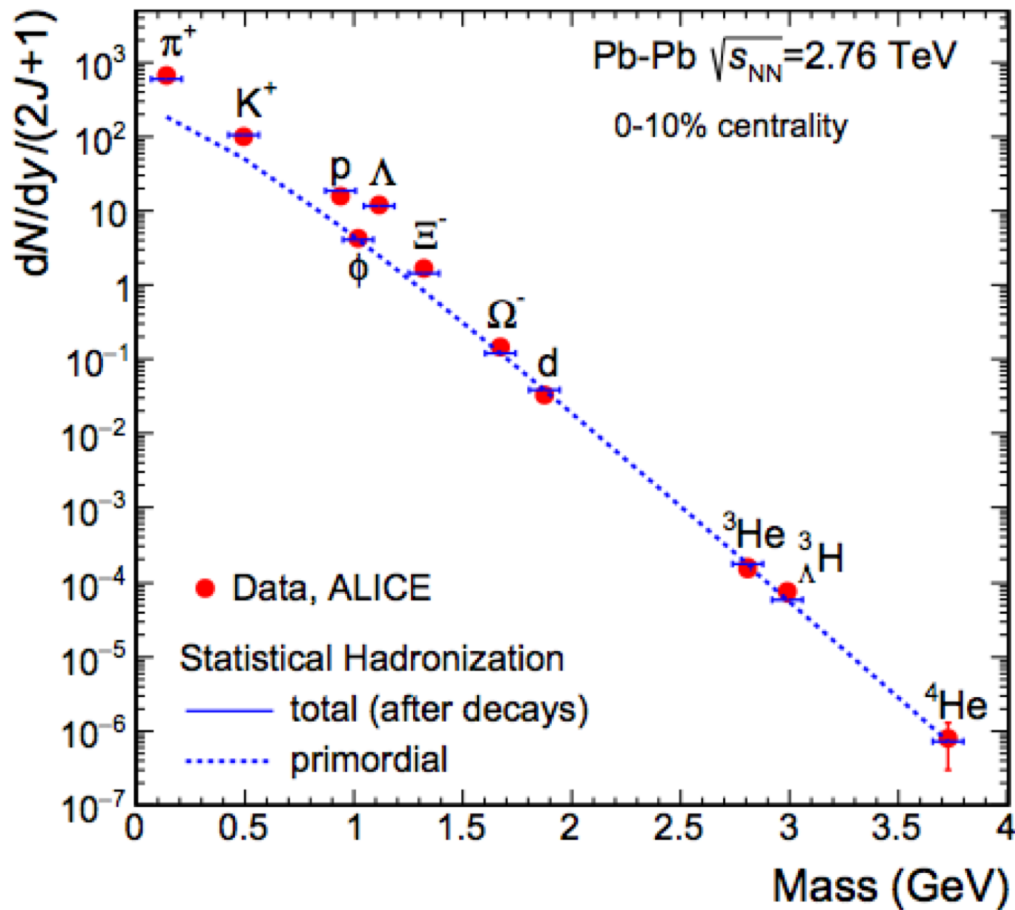
# Light Nuclei Yield Ratio Vs. Thermal model



➤ At RHIC energies, thermal model can describe the  $d/p$  ratios, but can not describe the  $t/p$  ratios.



# ALICE Data Vs. Thermal Model



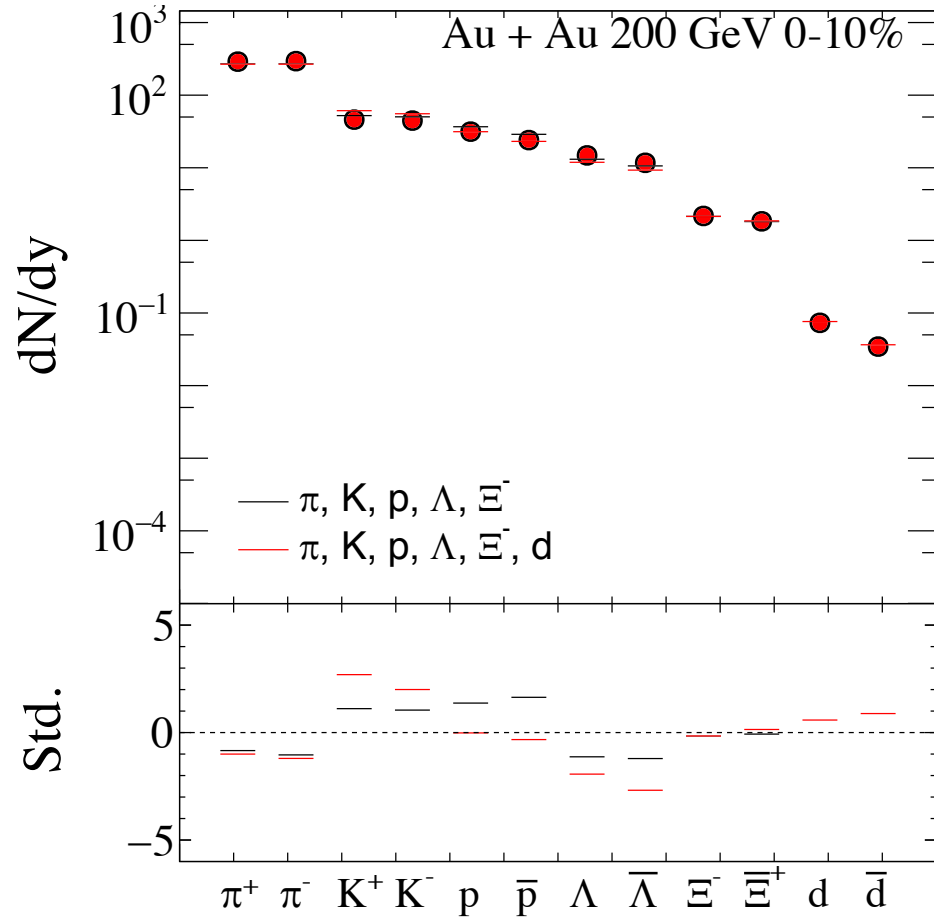
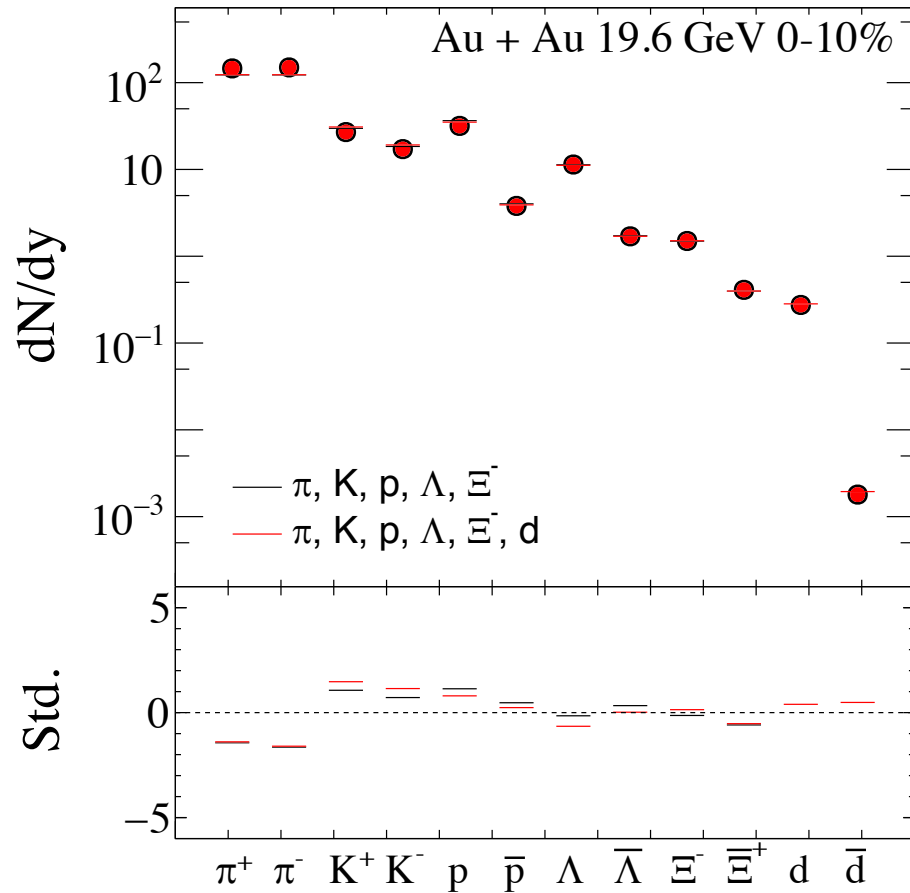
Why the yield of **triton** and even **alpha** can be well described by thermal model at LHC energies  
But not at RHIC energies ?

**Different production mechanism of light nuclei at RHIC and LHC energies ??**

A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nature 561, 321 (2018).



# Statistical thermal fit including light nuclei



Data are taken from :

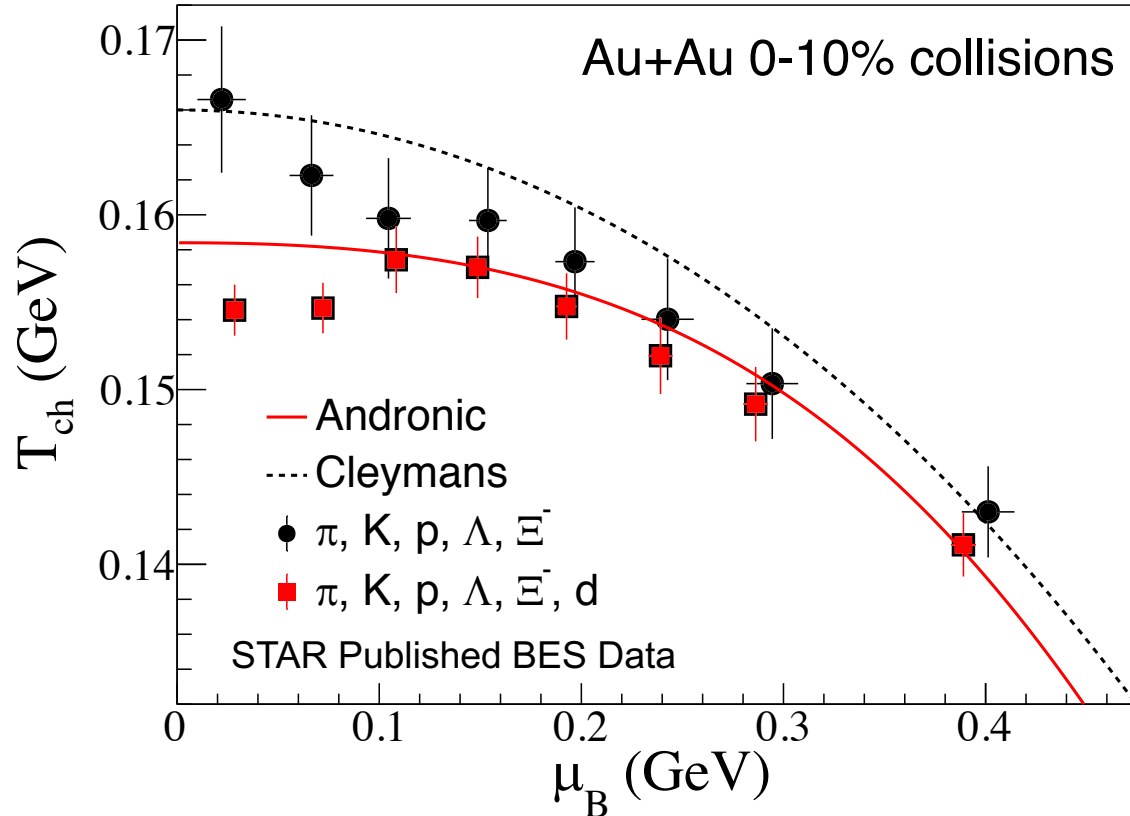
STAR, PRC 96,044904 (2017). (BES light hadrons)

STAR, PRC 99, 064905 (2019) (BES deuteron production)

STAR, arXiv:1906.03732, submitted to PRC (BES strangeness)



# Chemical freeze-out $T_{ch}$ Vs. $\mu_B$



Cleymans: J. Cleymans et al., PRC 73, 034905 (2006)

Andronic: A. Andronic, P. Braun-Munzinger, K. Redlich, J. Stachel, Nature 561, 321 (2018).

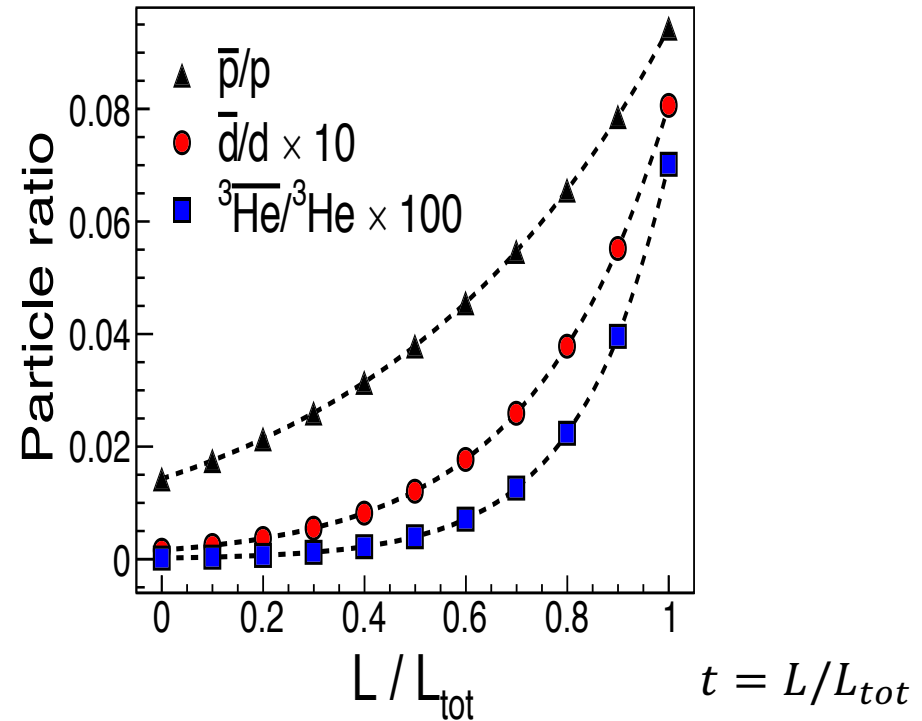
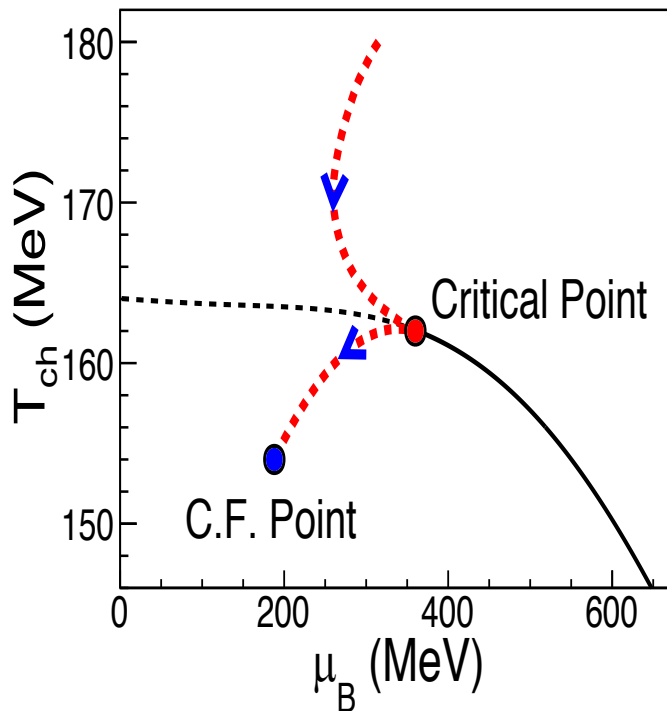
- Obtain lower chemical freeze-out temperature if we include the deuteron yield into the fitting.
- At 200 GeV,  $T_{ch} \sim 155$  MeV.



# QCD Critical Point Focusing Effects

QCD critical point focusing effect : critical point will serve as an attractor of the trajectory evolution in the  $T - \mu_B$  plane.

M. Asakawa, S. A. Bass B. Muller, C. Nonaka  
PRL 101, 122302 (2008)



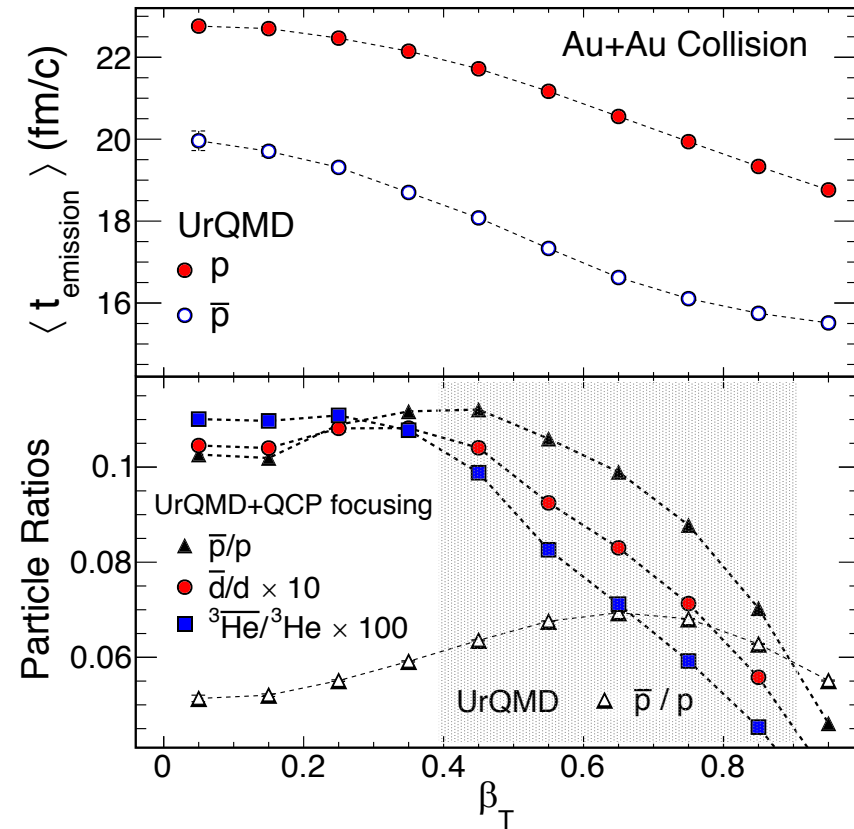
N. Yu, D. Zhang, and X. Luo arXiv:1812.04291

The particle emitting probability along the trajectory is assumed to be proportional to the particle density calculated from the thermal model with corresponding  $T$  and  $\mu_B$ .



# QCP Focusing Effects : Model Implementation

- $\beta_T - t$  distribution is from UrQMD central Au+Au collision at  $\sqrt{s_{NN}} = 19.6$  GeV.



➤ The  $\bar{p}/p$ ,  $\bar{d}/d$ , and  ${}^3\bar{\text{He}}/\text{He}$  **decrease with increasing  $\beta_T$**  with QCP focusing effect.

➤ This behavior is more easier to be observed for heavier particles

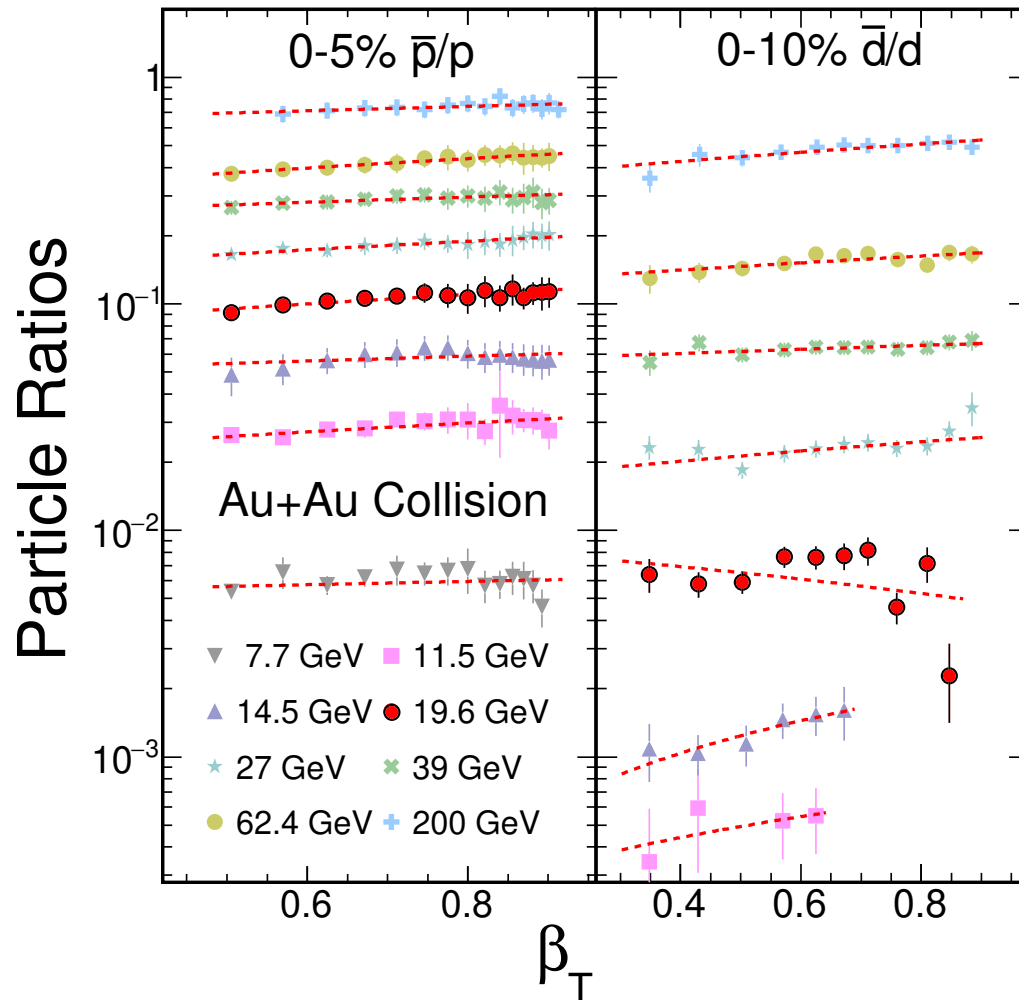
Can we observe the QCP focusing effects in HIC experiment ?

N. Yu, D. Zhang, and X. Luo arXiv:1812.04291

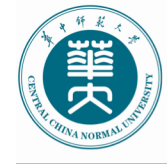




# Transverse velocity dependence of $\bar{d}/d$ ratio

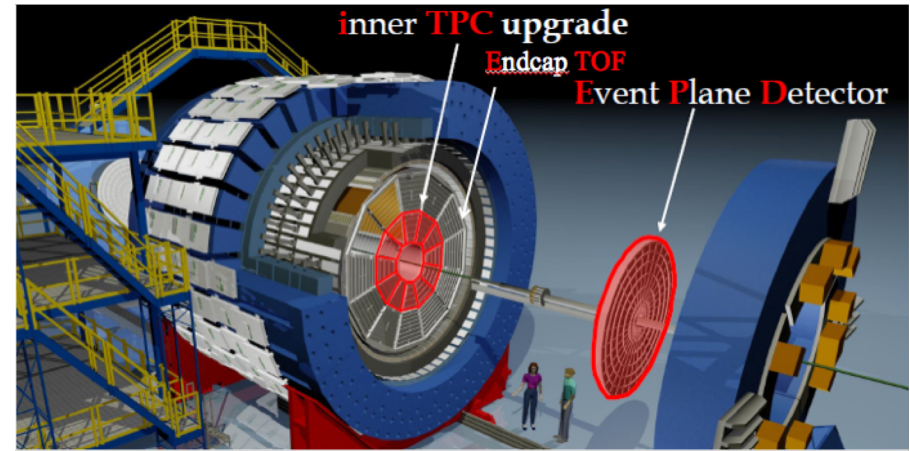


We indeed observe anomalous for  $\bar{d}/d$  ratio at 19.6 GeV measured by STAR. Will make more precise measurements in RHIC-BES-II.



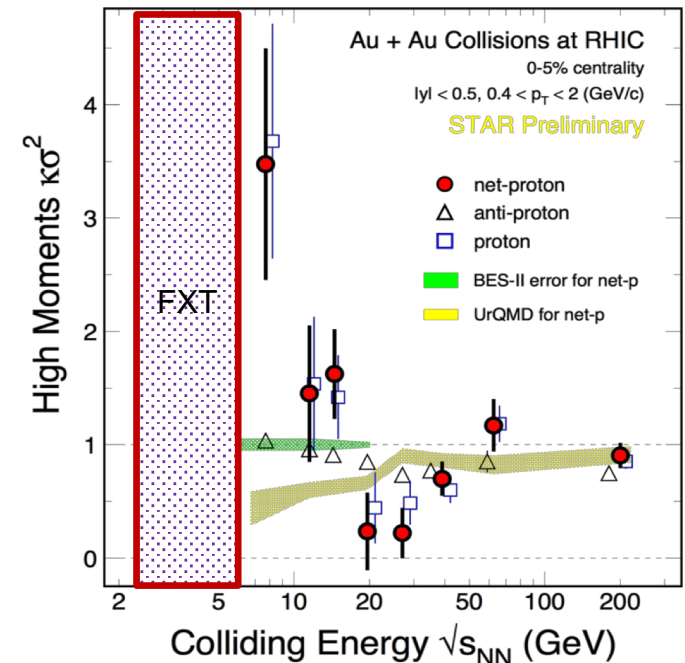
# BES-II at RHIC (2019-2021)

$\sqrt{s_{NN}}$ (GeV)	Events ( $10^6$ )	BES II / BES I
19.6	400	2019 / 2011
14.5	300	2019 / 2014
11.5	230	2020 / 2010
9.2	160	2020 / 2008
7.7	100	2021 / 2010
17.1	250	2021



- BES-II : 10-20 times higher statistics than BES-I.
- FIX-target mode :  $\sqrt{s_{NN}} = 3-7.7$  GeV (2018-2020).
- iTPC, ETOF, EPD upgrade completed.

- **Enlarge Acceptance** :  $\eta$  coverage from 1.0 to 1.5
- **Improve  $dE/dx$  and forward PID**
- **Improve centrality/event plane determination**





# Summary

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## Explore the QCD phase structure with Beam Energy Scan

- Fourth order net-proton fluctuations ( $C_4/C_2$ ) in central Au+Au collisions shows non-monotonic energy dependence, with a minimum around 20-30 GeV.
- Neutron density fluctuations in 0-10% central Au+Au collisions shows non-monotonic energy dependence with a peak around 20-30 GeV.
- $d\bar{b}/d$  vs.  $\beta_t$  show anomaly around 19.6 GeV.
- In BES-II, we can study the QCD phase structure with high precision at  $\sqrt{s_{NN}} = 7.7-19.6$  GeV (collider mode) and 3-7.7 GeV (Fix-target mode)

**Stay tuned for RHIC BES-II (2019-2021) !**

# QUARK MATTER 2019

Wuhan, China 4-9 November

## Workshop on the QCD Phase Structure at High Baryon Density Region

12-14 November 2019  
Central China Normal University  
Asia/Shanghai timezone

### Overview

[Scientific Programme](#)

[Timetable](#)

[Author List](#)

[Participant List](#)

[Registration](#)

[Registration Form](#)

[Travel Information](#)

In this workshop, we will focus on discussing the physics of QCD phase structure at high baryon density. It will cover recent experimental and theoretical developments and the perspective for future low energy heavy-ion collision experiments.

No registration fee is collected.

### Topics:

1. Search for the QCD critical point and Beam Energy Scan
2. Equation of state at high baryon density
3. Future low energy heavy-ion collision experiments

### Local Organizing Committee:

Xiaofeng Luo (CCNU), Co-chair

Nu Xu (CCNU/IMP/LBNL), Co-chair


Feng Liu (CCNU)

Shusu Shi (CCNU)

Yaping Wang (CCNU)

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 +86-27-67867975

## QM Satellite Meeting, Nov. 12-14, 2019



**Truth buried in the sands.  
Need to dig it out.**

***Thank you !***



# 2019-2021: BES II at RHIC

$\sqrt{s_{NN}}$ (GeV)	Events ( $10^6$ )	BES II / BES I	$\mu_B$ (MeV)	$T_{CH}$ (MeV)
200	238	2010	25	166
62.4	45	2010	73	165
54.4	<b>1000</b>	2017	90	165
39	86	2010	112	164
27	32 ( <b>1000</b> )	2011(2018)	156	162
19.6	<b>400</b> / 36	<b>2019</b> / 2011	206	160
<b>14.5</b>	<b>300</b> / 13	<b>2019</b> / 2014	264	156
11.5	<b>230</b> / 7	<b>2020</b> / 2010	315	152
9.2	<b>160</b> / 0.3	<b>2020</b> / 2008	355	140
7.7	<b>100</b> / 3	<b>2021</b> / 2010	420	140
17.1	<b>250</b>	<b>2021</b>	235	

Precise mapping the QCD phase diagram  **$200 < \mu_B < 420\text{MeV}$**