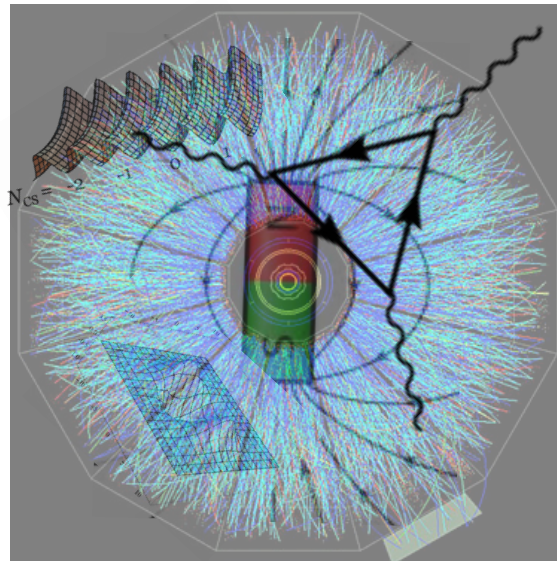


# Quantifying CME in Heavy Ion Collisions

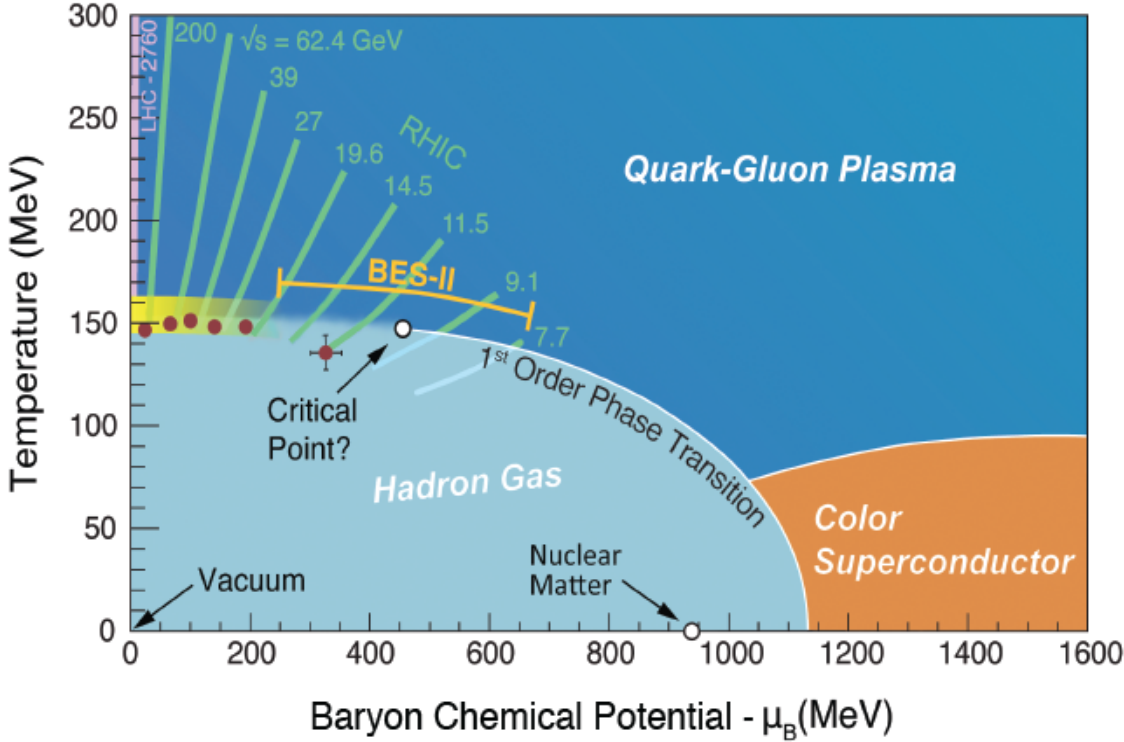


**Jinfeng Liao**



**BEST**  
COLLABORATION

# Beam Energy Scan: Mapping Out Phases of QCD



*\* Establishing a chiral QGP at higher energy via anomalous chiral effects*  
*\* Searching for chiral critical point & 1st-order transition at lower energy*

**NSFC Key Projects: Fudan, SDU, THU, USTC, CCNU,...**



**Beam Energy Scan Theory (BEST) Collaboration:**  
**BNL, IU, LBNL, McGill U, Michigan State U, MIT, NCSU, OSU, Stony Brook U, U Chicago, U Conn, U Huston, UIC**

# A Recent Review: Collectivity, Criticality, Chirality

## Mapping the Phases of Quantum Chromodynamics with Beam Energy Scan

Adam Bzdak<sup>a</sup>, ShinIchi Esumi<sup>b</sup>, Volker Koch<sup>c</sup>, Jinfeng Liao<sup>d,e</sup>, Mikhail Stephanov<sup>f</sup>, Nu Xu<sup>c,e</sup>

<sup>a</sup>*AGH University of Science and Technology, Faculty of Physics and Applied Computer Science, 30-059 Krakow, Poland*

<sup>b</sup>*Tomonaga Center for the History of the Universe, University of Tsukuba, Tsukuba, Ibaraki 305, Japan*

<sup>c</sup>*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA*

<sup>d</sup>*Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA*

<sup>e</sup>*Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan, 430079, China*

<sup>f</sup>*Physics Department, University of Illinois at Chicago, 845 W. Taylor St., Chicago IL 60607-7059, USA*

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### Abstract

We review the present status of the search for a phase transition and critical point as well as anomalous transport phenomena in Quantum Chromodynamics (QCD), with an emphasis on the Beam Energy Scan program at the Relativistic Heavy Ion Collider at Brookhaven National Laboratory. We present the conceptual framework and discuss the observables deemed most sensitive to a phase transition, QCD critical point, and anomalous transport, focusing on fluctuation and correlation measurements. Selected experimental results for these observables together with those characterizing the global properties of the systems created in heavy ion collisions are presented. We then discuss what can be already learned from the currently available data about the QCD critical point and anomalous transport as well as what additional measurements and theoretical developments are needed in order to discover these phenomena.

**Keywords:** Heavy Ion Collision, Beam Energy Scan, QCD Phase Diagram, Critical Point, Chiral Magnetic Effect

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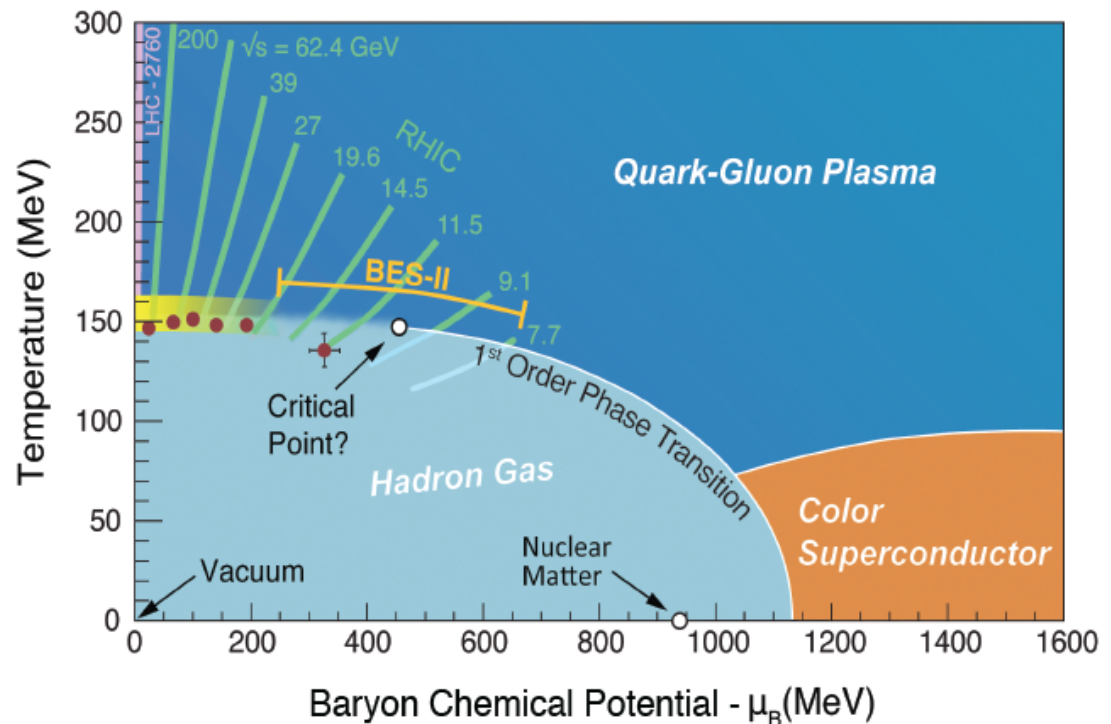
arXiv:1906.00936

# INT Program 2020

## *Chirality and Criticality: Novel Phenomena in Heavy Ion Collisions*

*May 11 – June 5, 2020 (May18~22 workshop week)*

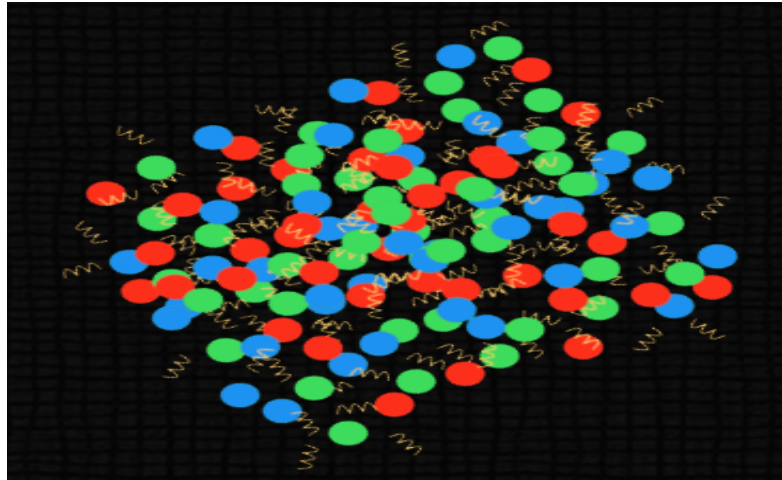
*Organizers: J. Liao, M. Stephanov, H.-U. Yee, Z. Xu*



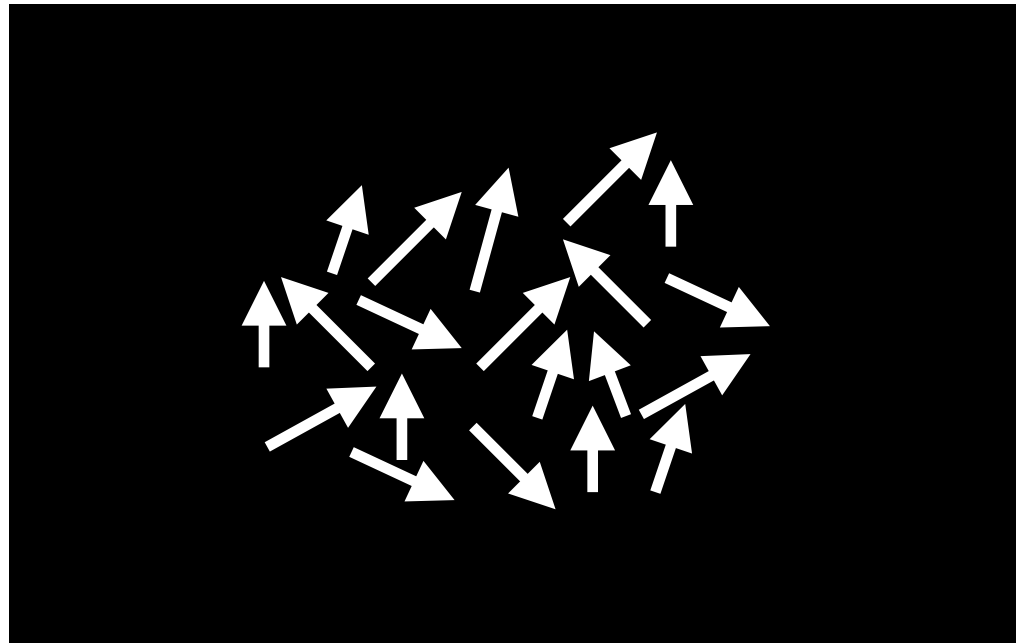


# A New Paradigm: Quantum Fluid of Spin

*A nearly perfect fluid  
(of energy-momentum)*

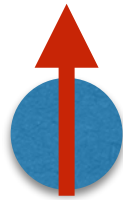


*What happens to the spin  
DoF in the fluid???*



# Spin: Chirality, Vorticity and Magnetic Field

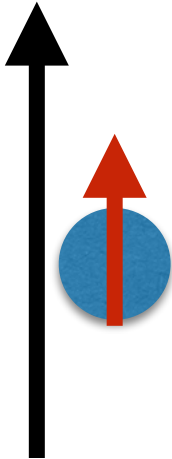
*SPIN  
UP*



*SPIN  
DOWN*

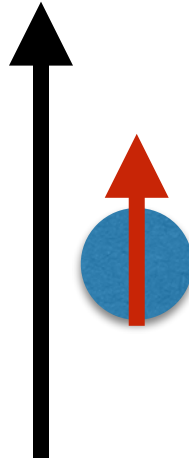


$\vec{B}$



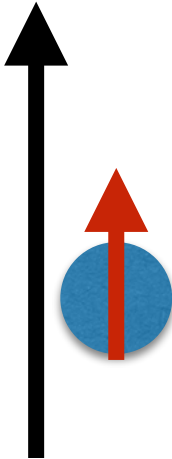
**Magnetic  
Polarization**

$\vec{\omega}$



**Rotational  
Polarization**

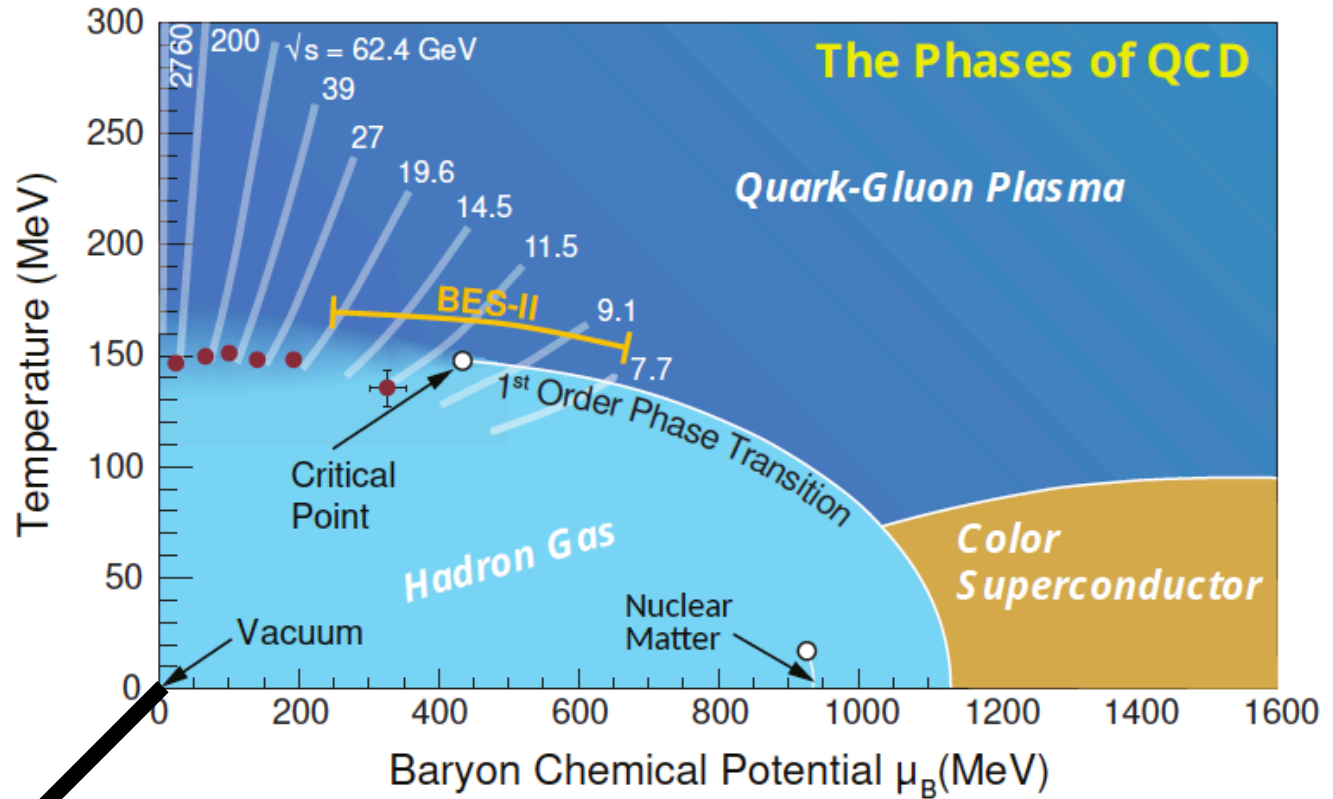
$\vec{P}$



**Chirality  
Polarization**

Interesting interplay  $\rightarrow$  highly nontrivial phenomena!

# QCD Matter under New Extreme Conditions



$\vec{B}$   
 $\vec{\omega}$   
 $N_5$  (or  $\mu_5$ )

**QCD matter under extremely strong vorticity and magnetic fields!**

# Chirality 2019 @ Tsinghua Beijing, Apr 2019

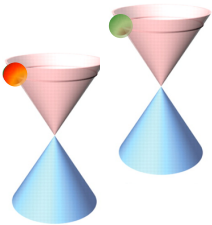


***~100 people, 4.5 days***

***Chirality 2015,2016,2017 @ UCLA  
Chirality 2018 @ Univ. Florence  
Chirality 2019 @ Tsinghua Univ.***

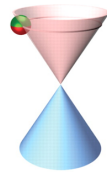
# Interdisciplinary Interests

**Weyl semimetal**  
(non-degenerated bands)

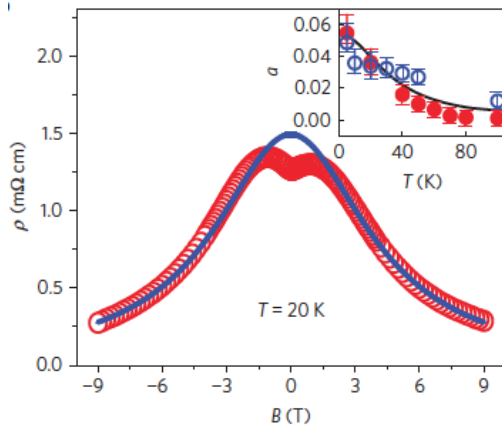


TaAs  
NbAs  
NbP  
TaP

**Dirac semimetal**  
(doubly degenerated bands)

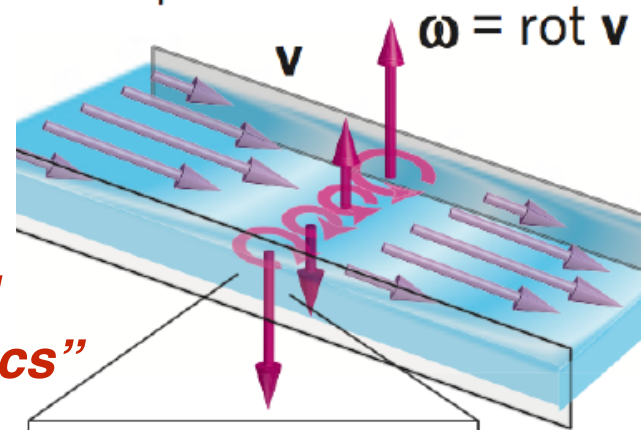


ZrTe<sub>5</sub>  
Na<sub>3</sub>Bi,  
Cd<sub>3</sub>As<sub>2</sub>

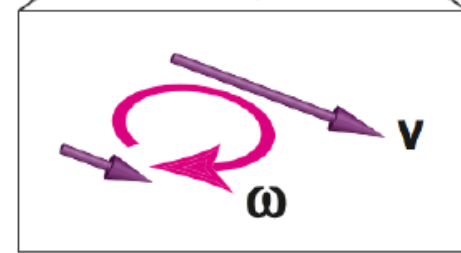


“Spin hydrodynamic generation”  
Takahashi, *et al.* Nat. Phys. (2016)

Liquid flow



“Fluid  
Spintronics”



nature  
physics

LETTERS

PUBLISHED ONLINE: 8 FEBRUARY 2016 | DOI: 10.1038/NPHYS3648

Chiral magnetic effect in ZrTe<sub>5</sub>

Qiang Li<sup>1\*</sup>, Dmitri E. Kharzeev<sup>2,3\*</sup>, Cheng Zhang<sup>1</sup>, Yuan Huang<sup>4</sup>, I. Pletikosić<sup>1,5</sup>, A. V. Fedorov<sup>6</sup>,  
R. D. Zhong<sup>1</sup>, J. A. Schneeloch<sup>1</sup>, G. D. Gu<sup>1</sup> and T. Valla<sup>1\*</sup>

**Condensed matter, cold atomic gases, neutron stars,  
cosmology, plasma physics, etc**  
**[Chiral Matter workshops @ RIKEN, NTU]**




# Recent Reviews on Chirality Related Topic


Progress in Particle and Nuclear Physics 88 (2016) 1–28

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Contents lists available at ScienceDirect

 Progress in Particle and Nuclear Physics

journal homepage: [www.elsevier.com/locate/ppnp](http://www.elsevier.com/locate/ppnp)




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Review

Chiral magnetic and vortical effects in high-energy nuclear collisions—A status report

D.E. Kharzeev<sup>a,b</sup>, J. Liao<sup>c,d,\*</sup>, S.A. Voloshin<sup>e</sup>, G. Wang<sup>f</sup>

<sup>a</sup> Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA  
<sup>b</sup> Department of Physics and RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973-5000, USA  
<sup>c</sup> Physics Department and Center for Exploration of Energy and Matter, Indiana University, 727 E Third Street, Bloomington, IN 47405, USA  
<sup>d</sup> RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA  
<sup>e</sup> Department of Physics and Astronomy, Wayne State University, 666 W. Hancock, Detroit, MI 48201, USA  
<sup>f</sup> Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

 CrossMark

**Prog. Part. Nucl. Phys. 88, 1 (2016)[arXiv:1511.04050 [hep-ph]].**

**Fukushima, arXiv:1812.08886, PPNP2019.**

**Zhao, Wang, arXiv:1906.11413, PPNP2019.**

**Hattori, Huang, Nucl. Sci. Tech., 28 (2017) no.2, 26.**

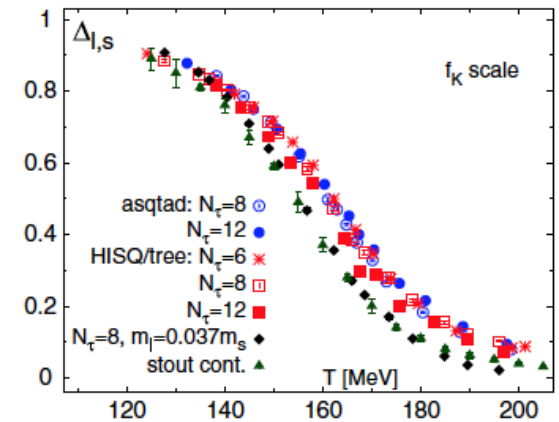
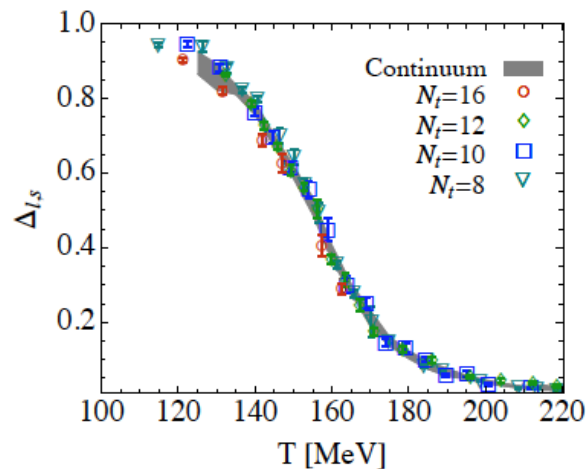
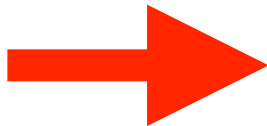
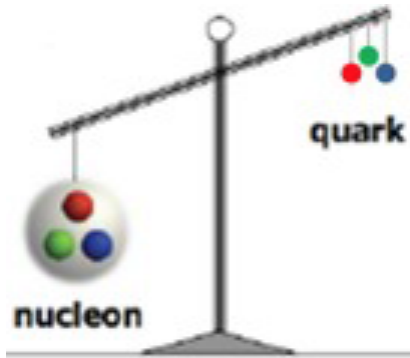
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# Chiral Magnetic Effect: Many-Body Physics of Chirality, Anomaly, Topology

---

# Chiral Symmetry Restoration

*\* Spontaneously broken chiral symmetry in the vacuum is a fundamental property of QCD.*



*\* A chirally symmetric quark-gluon plasma at high temperature is an equally fundamental property of QCD!*

**Could we see direct experimental evidence for that?**

# Chiral Symmetry: Quantum Anomaly

*Chiral anomaly is a fundamental aspect of QFT with chiral fermions.*

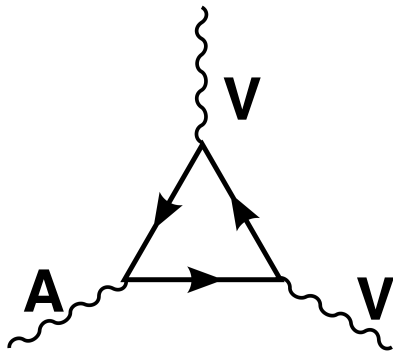
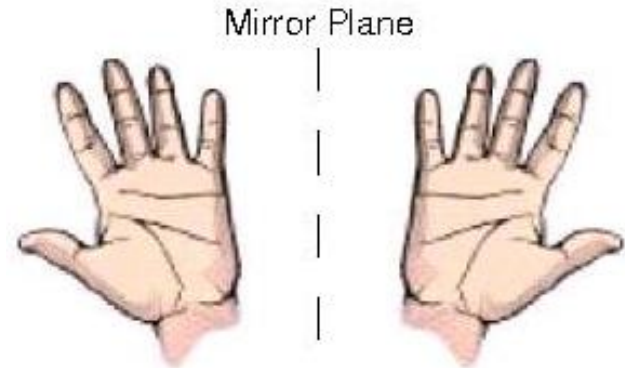
**Classical symmetry:**

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$

$$\partial_\mu J_5^\mu = 0$$



[e.g.  $\pi^0 \rightarrow 2 \text{ gamma}$ ]

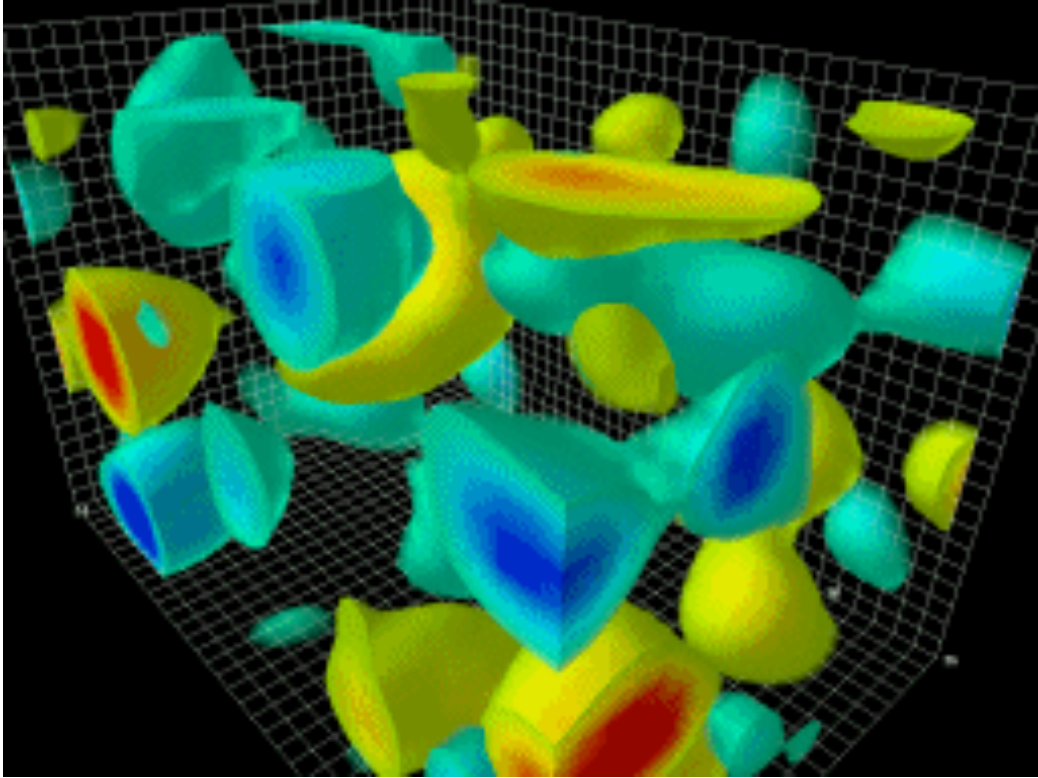
**Broken at QM level:**

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

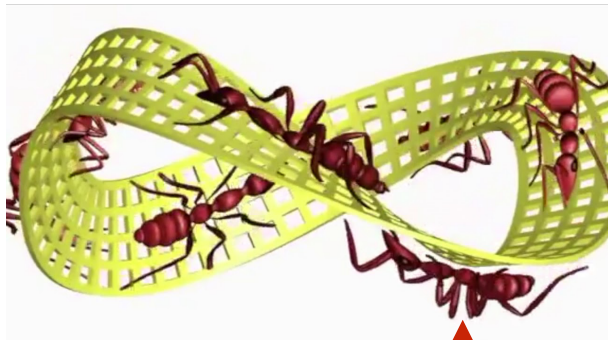
$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$

- \*  $C_A$  is universal anomaly coefficient
- \* Anomaly is intrinsically QUANTUM effect

# From Gluon Topology to Quark Chirality



$$Q_w = \frac{1}{32\pi^2} \int d^4x (gG_a^{\mu\nu}) \cdot (g\tilde{G}_{\mu\nu}^a)$$



**Quarks**

$$N_5(t \rightarrow +\infty) - N_5(t \rightarrow -\infty) = \frac{g^2}{16\pi^2} \int dt d^3\mathbf{r} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a$$

**QCD anomaly: gluon topology  $\rightarrow$  chirality imbalance**

$$N_R - N_L = N_5 = 2Q_w$$

**Net chirality  $\leftrightarrow$  topo fluctuations & chiral restoration**



# Chiral Magnetic Effect (CME): Macroscopic Chiral Anomaly

Chirality & Anomaly & Topology

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

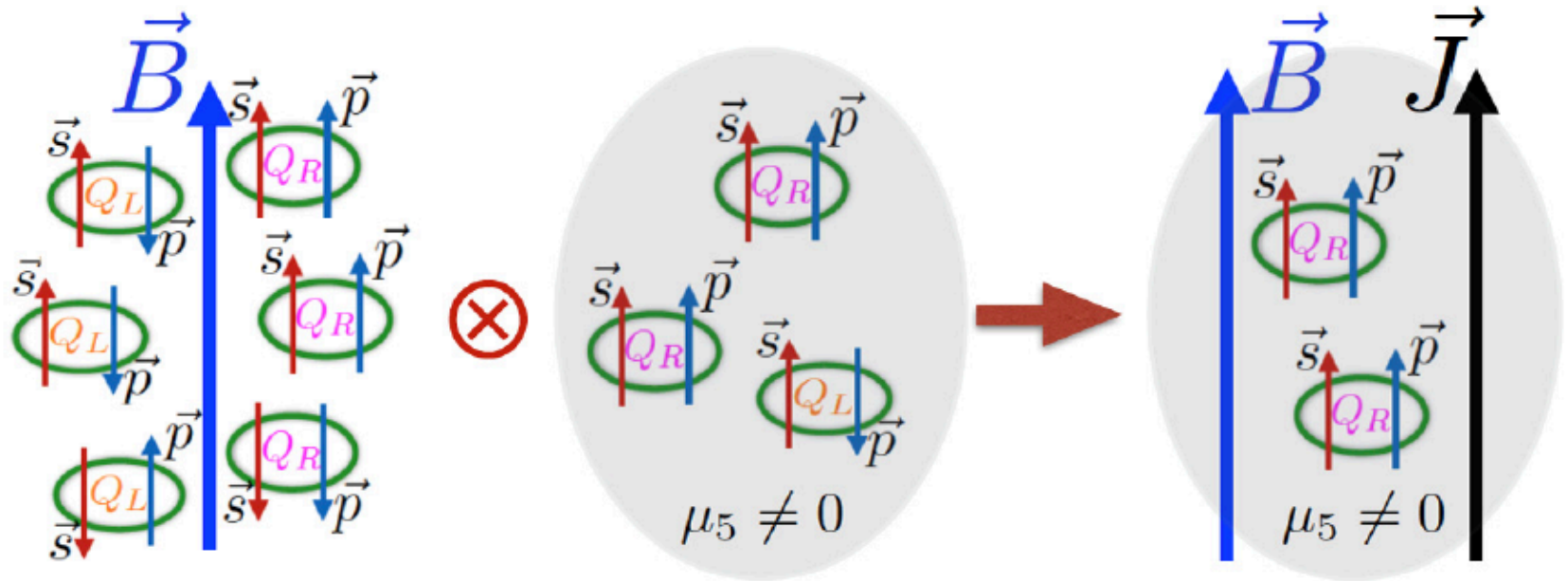
Electric  
Current

Magnetic  
Field

Q.M. Transport

[Kharzeev, Fukushima, Warringa, McLerran, ...]

# Intuitive Picture of CME



## Intuitive understanding of CME:

Magnetic polarization  $\rightarrow$   
correlation between micro.  
**SPIN & EXTERNAL FORCE**



Chiral imbalance  $\rightarrow$   
correlation between directions of  
**SPIN & MOMENTUM**



**Transport current along magnetic field**

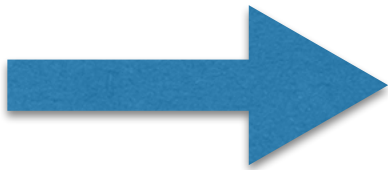
$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

# Chiral Transport Theory

**Usual (classical) transport equation:**

$$\left\{ \partial_t + \dot{\mathbf{x}} \cdot \vec{\nabla}_{\mathbf{x}} + \dot{\mathbf{p}} \cdot \vec{\nabla}_{\mathbf{p}} \right\} f^{(c)}(t, \mathbf{x}, \mathbf{p}) = C[f^{(c)}] ,$$

$$\dot{\mathbf{x}} = \mathbf{v} = \vec{\nabla}_{\mathbf{p}} E_{\mathbf{p}} , \quad \dot{\mathbf{p}} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B}) .$$



**Chiral transport equation:**

$$\left\{ \partial_t + \mathbf{G}_{\mathbf{x}} \cdot \nabla_{\mathbf{x}} + \mathbf{G}_{\mathbf{p}} \cdot \nabla_{\mathbf{p}} \right\} f^{(q)}(t, \mathbf{x}, \mathbf{p}) = C[f^{(q)}] ,$$

$$\mathbf{G}_{\mathbf{x}} = \frac{1}{\sqrt{G}} \left[ \tilde{\mathbf{v}} + \hbar q (\tilde{\mathbf{v}} \cdot \mathbf{b}_{\chi}) \mathbf{B} + \hbar q \tilde{\mathbf{E}} \times \mathbf{b}_{\chi} \right] , \quad \mathbf{G}_{\mathbf{p}} = \frac{q}{\sqrt{G}} \left[ \tilde{\mathbf{E}} + \tilde{\mathbf{v}} \times \mathbf{B} + \hbar q (\tilde{\mathbf{E}} \cdot \mathbf{B}) \mathbf{b}_{\chi} \right]$$

[Son, Yamamoto; Stephanov, Yin; Chen, Wang, et al; Hidaka, Pu, Yang; Mueller, Venugopalan; Huang, Shi, Jiang, JL, Zhuang; ...]

# Fluid Dynamics That Knows Left & Right

## Normal Hydrodynamics

$$\partial_\mu J^\mu = 0$$

$$J^\mu = nu^\mu + \nu^\mu$$

*Viscous  
Current*

$$\nu^\mu = \frac{\sigma T}{2} \Delta^{\mu\nu} \partial_\nu \left( \frac{\mu}{T} \right) + \frac{\sigma}{2} E^\mu$$

*Diffusion  
Conduction*



## Anomalous Hydrodynamics

$$\partial_\mu J^\mu = C_A E^\mu B_\mu$$

*Anomaly*

$$J^\nu = nu^\mu + \nu^\mu + \nu_a^\mu$$

*Viscous  
Current      Anomalous  
Current*

$$\nu^\mu = \frac{\sigma T}{2} \Delta^{\mu\nu} \partial_\nu \left( \frac{\mu}{T} \right) + \frac{\sigma}{2} E^\mu$$

*Diffusion  
Conduction*

$$\nu_a^\mu = \xi_B B^\mu + \xi \omega^\mu$$

*CME  
CVE*

[Son, Surowka; Kharzeev, Yee; Hidaka, Yang; Shi, JL, et al; ...]

***A new type of hydrodynamics with macro. quantum effect!***

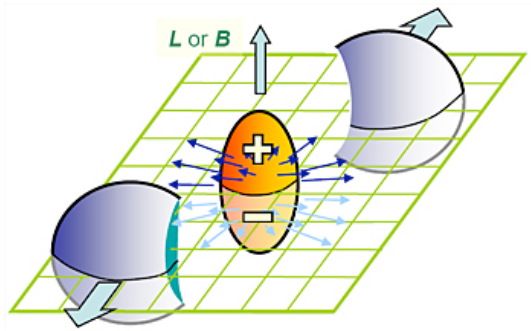
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# Extreme Vorticity and Magnetic Field

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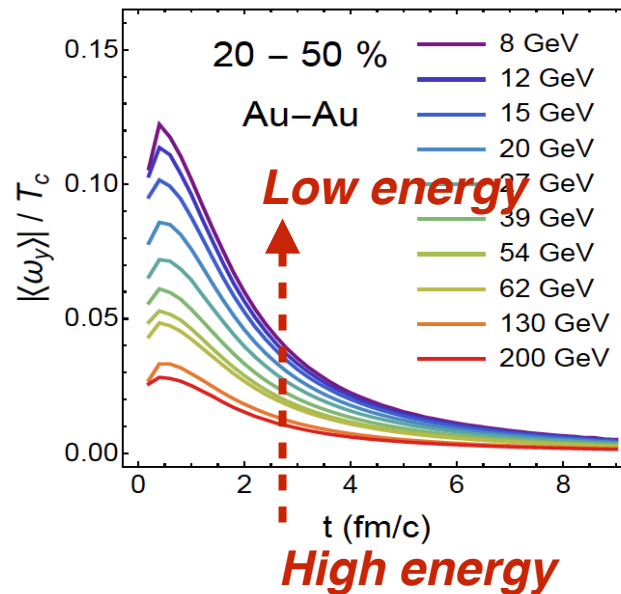
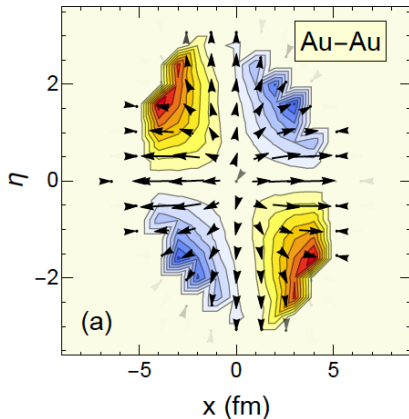
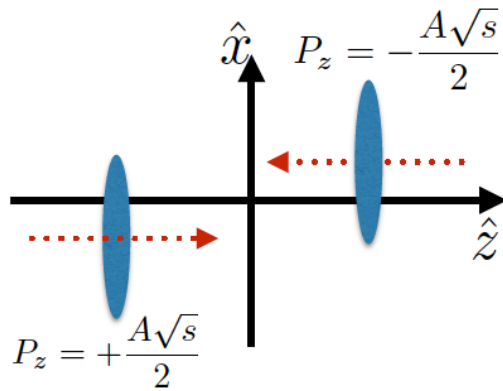


# Rotating Quark-Gluon Plasma

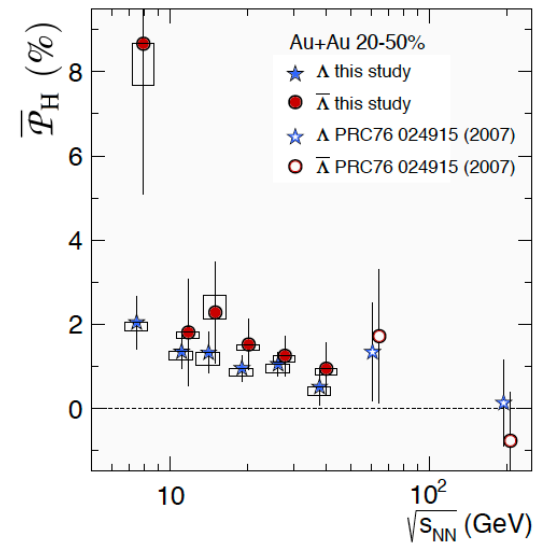


$$L_y = \frac{Ab\sqrt{s}}{2} \sim 10^{4\sim 5} \hbar$$

**Angular momentum  $\rightarrow$  nontrivial vorticity structure and spin polarization effect**



**Jiang, Lin, JL, PRC2016**

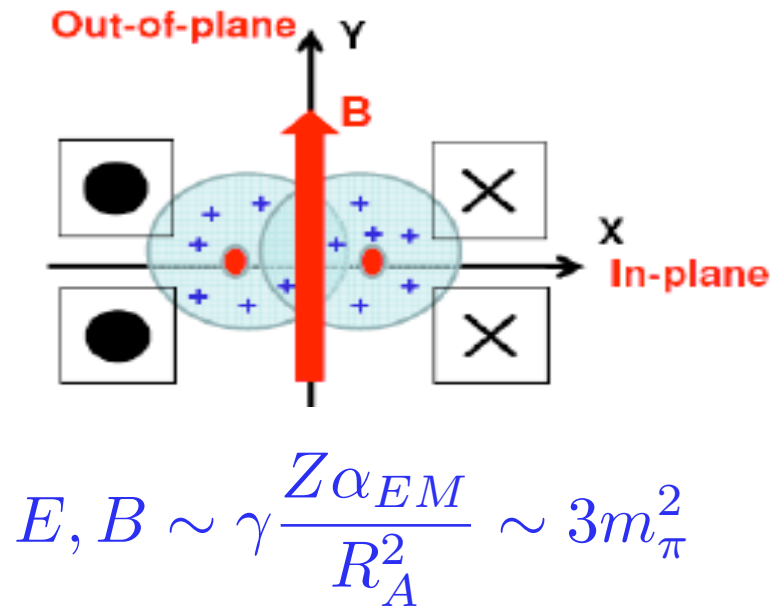
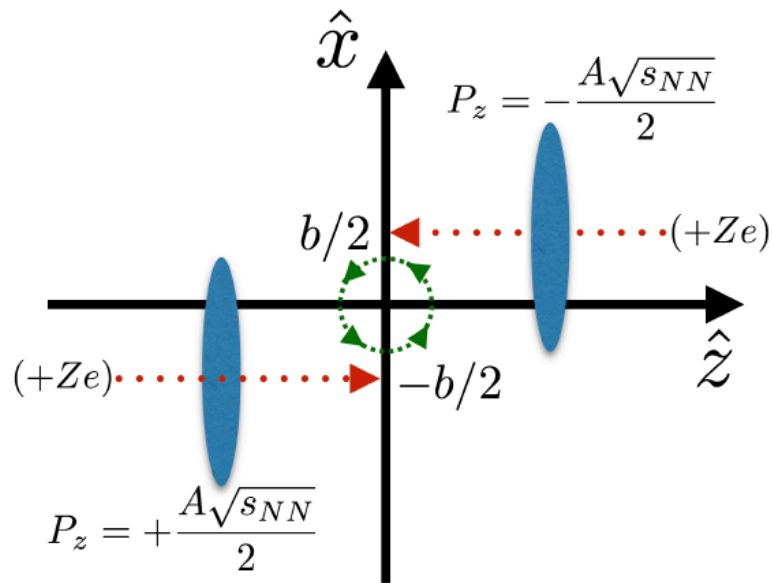


**STAR, Nature 2017**

**[See talks yesterday]**

# Strong Electromagnetic Fields

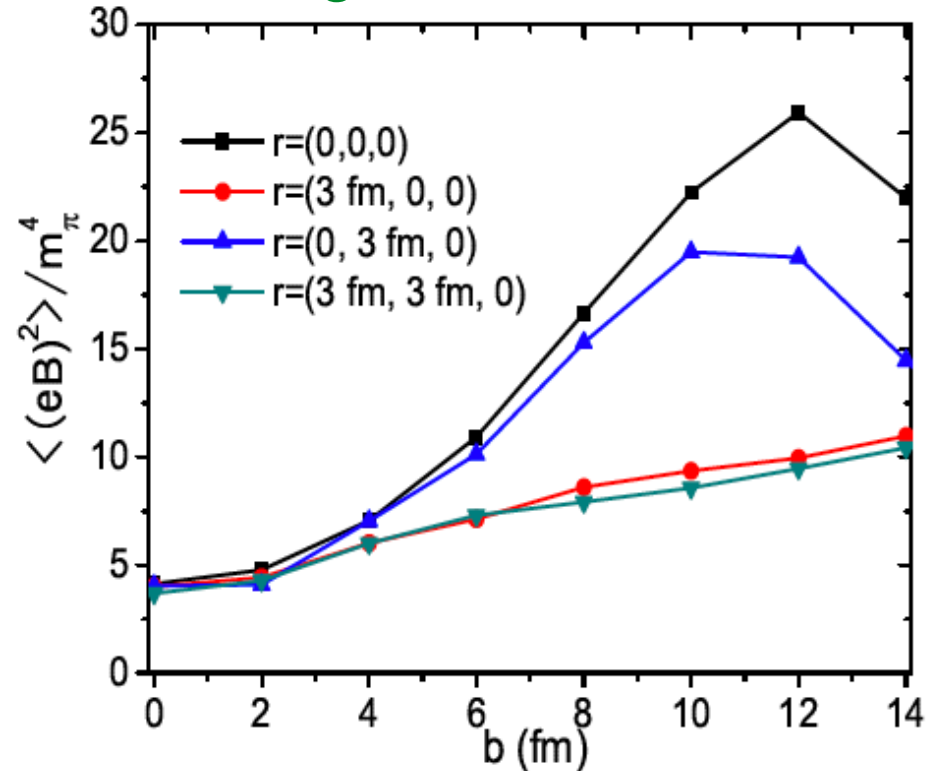
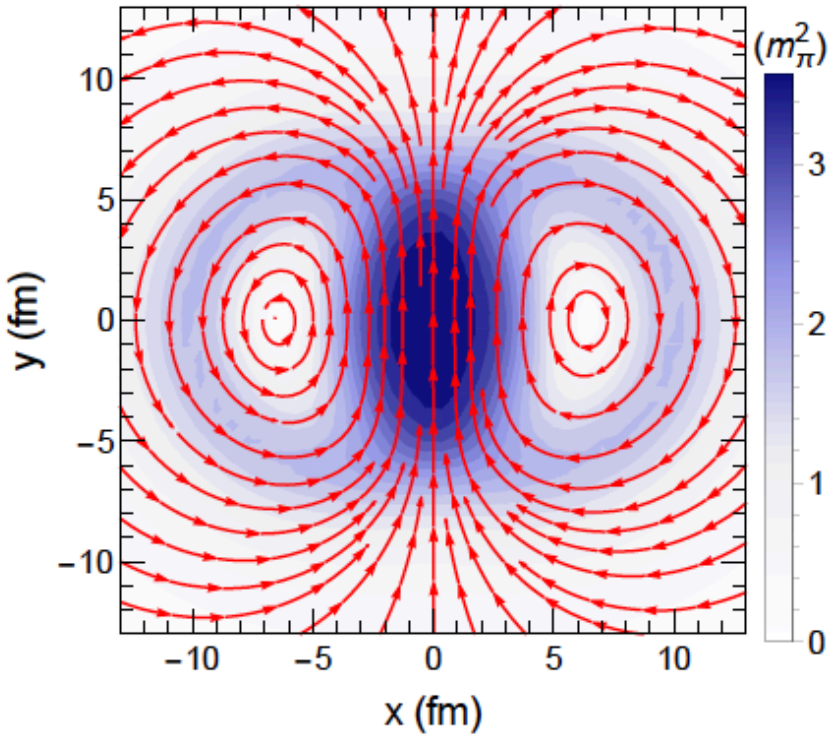
*The angular momentum together with large (+Ze) nuclear charge  
 → strong magnetic field!*



- Strongest B field (and strong E field as well) naturally arises!  
 [Kharzeev, McLerran, Warringa; Skokov, et al; Bzdak-Skokov;  
**Deng-Huang**; Skokov-McLerran; Tuchin; ...]
- “Out-of-plane” orientation (approximately)  
**[Bloczynski-Huang-Zhang-Liao]**

# Strong Electromagnetic Fields

Huang, Liao, et al PLB2012



**Quantitative simulations confirm the existence of such extreme fields!**

**[Many interesting B-field induced effects: di-electron; polarization splitting; quarkonium  $v_2$ ; D meson  $v_1$ ; ...]**

# Strong Electromagnetic Fields

Physics Letters B 718 (2013) 1529–1535



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Contents lists available at SciVerse ScienceDirect

Physics Letters B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



Azimuthally fluctuating magnetic field and its impacts on observables in heavy-ion collisions

Huang, Liao, et al PLB2012

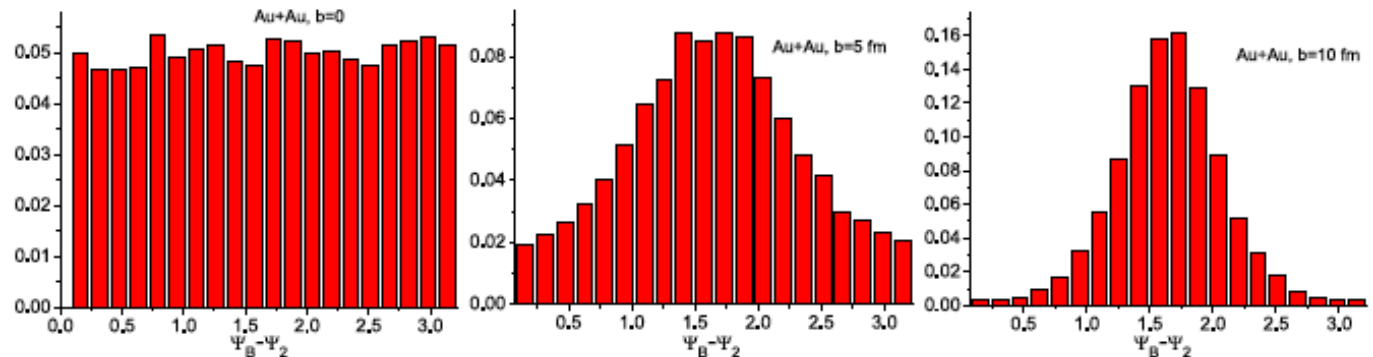
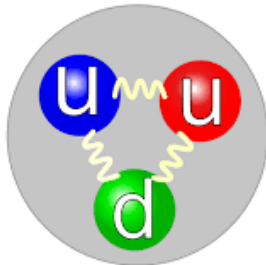
John Błoczyński<sup>a</sup>, Xu-Guang Huang<sup>a,\*</sup>, Xilin Zhang<sup>a</sup>, Jinfeng Liao<sup>a,b</sup>

<sup>a</sup> Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

<sup>b</sup> RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA

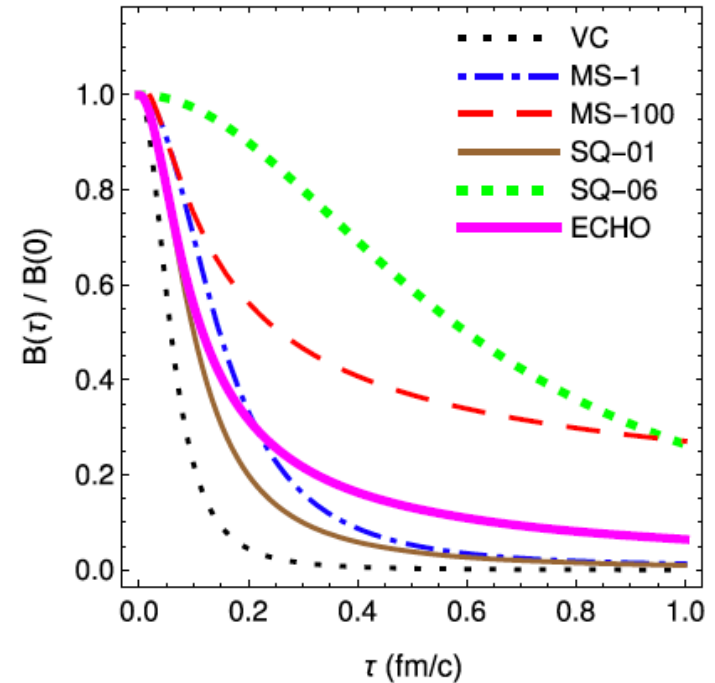
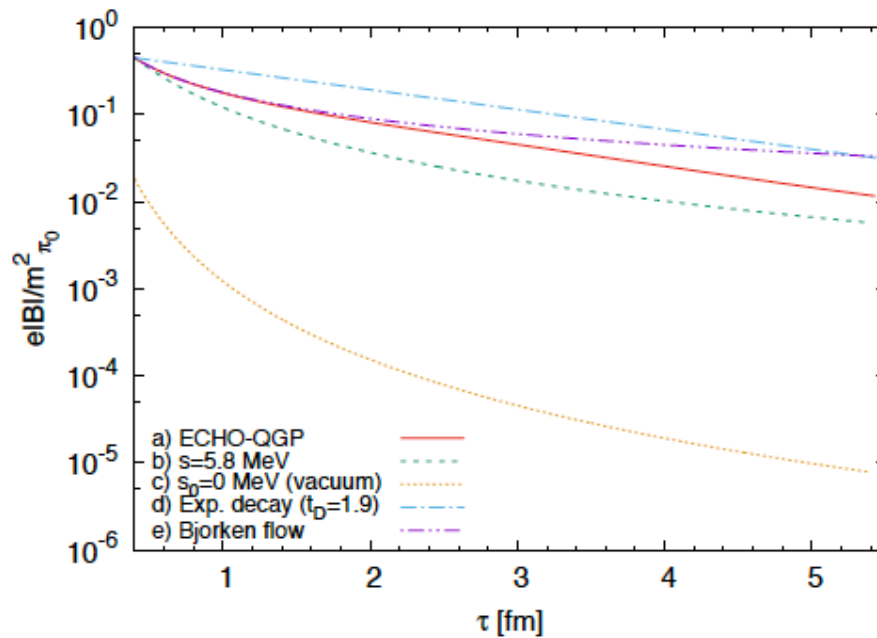
*Two very important points in this paper:*

- \* azimuthal correlation/de-correlation between  $B$  field and geometry*
- \* finite size of proton must be taken into account*



# Dynamical Magnetic Fields

**Magnetic field may last much longer than vacuum field due to plasma medium feedback effect.**



**\* Ideal RMHD simulations (ECHO-QGP) [Inghirami, et al, 1609.03042]**

**See also works by:**

**Deng, Huang; Q. Wang, et al; Tuichin; Skokov, McLerran; ...**

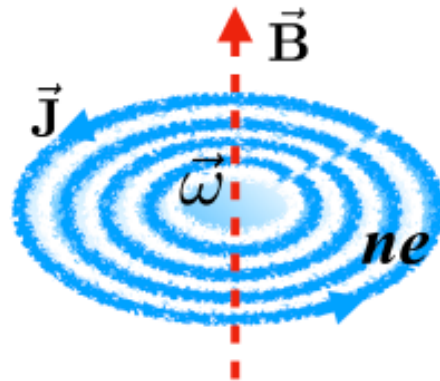
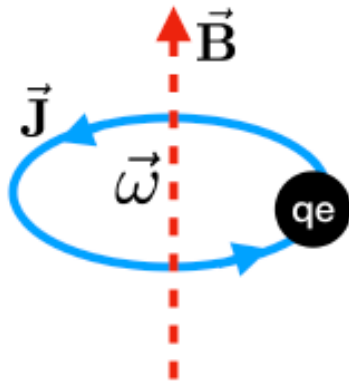


# Toward Synergy of B and Rotation

*A possible new mechanism: charged fluid + rotation → magnetic field*

*Simple example: single charged particle that is swirling*

$$B_0 = B_z(\rho = 0) = \frac{I}{2R_0} = \frac{(qe)\omega_0}{4\pi R_0}$$



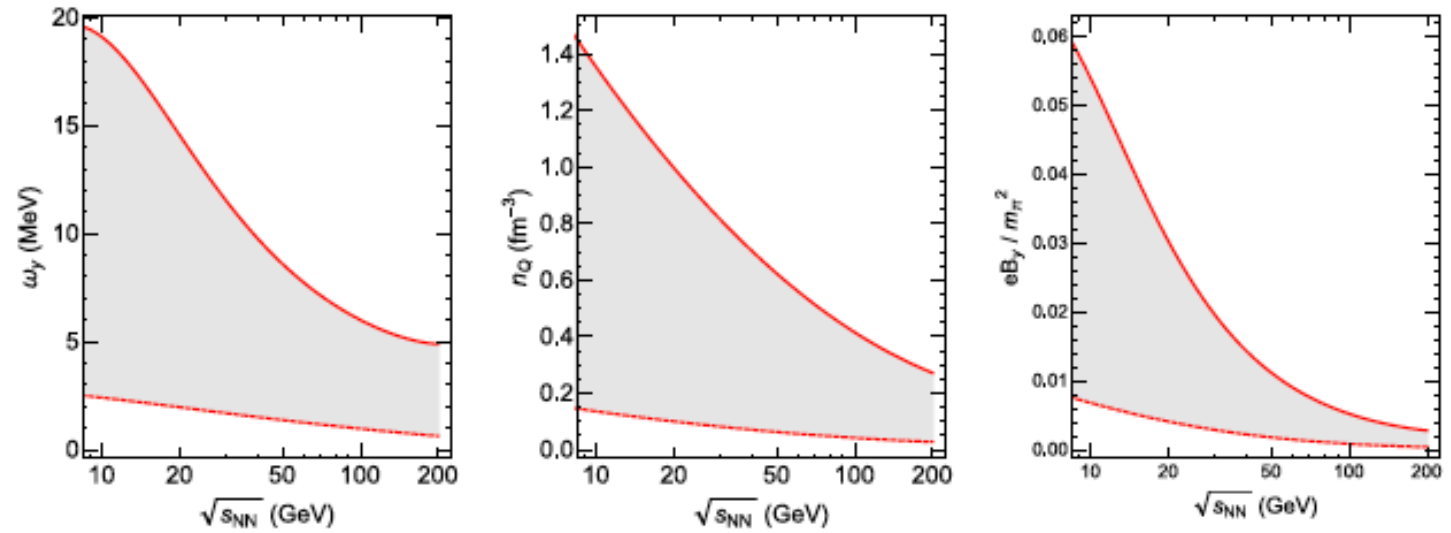
$$e\bar{B} = \frac{e^2}{4\pi} nA\bar{\omega}$$

*A more relevant example:  
Charged fluid vortex*

$$\begin{aligned} n e \omega^\mu &= \epsilon^{\mu\nu\rho\sigma} u_\nu \omega_{\rho\sigma} \\ &= 2\epsilon^{\mu\nu\rho\sigma} u_\nu \partial_\rho \partial^\lambda F_{\lambda\sigma} \\ &= \epsilon^{\mu\nu\rho\sigma} u_\nu \square F_{\rho\sigma}. \end{aligned}$$

*[X. Guo, JL, E. Wang: arXiv:1904.04704]*

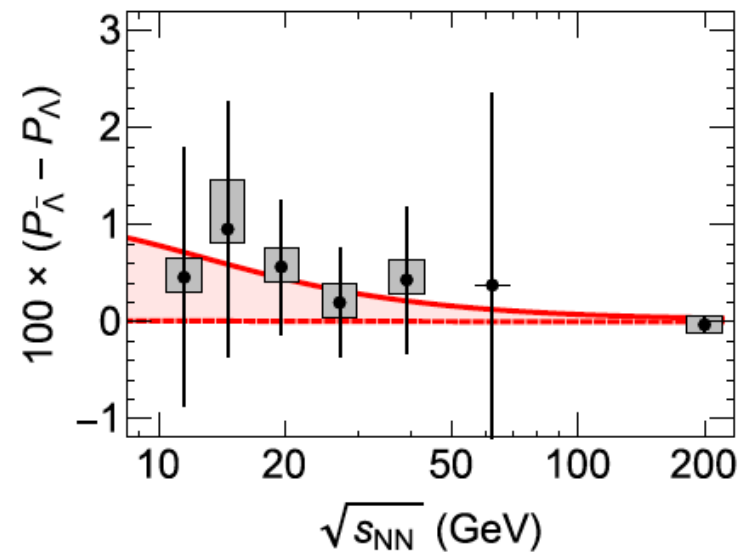
# New Mechanism for Long-Lived B Field



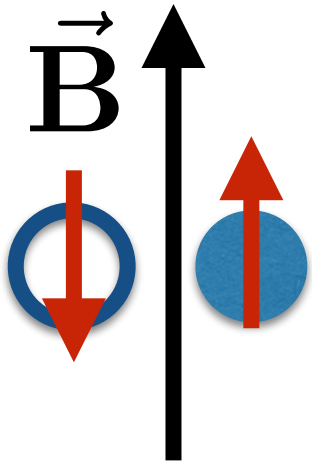
$$e\bar{B} = \frac{e^2}{4\pi} n A \bar{\omega}$$

**Important at low beam energy!**

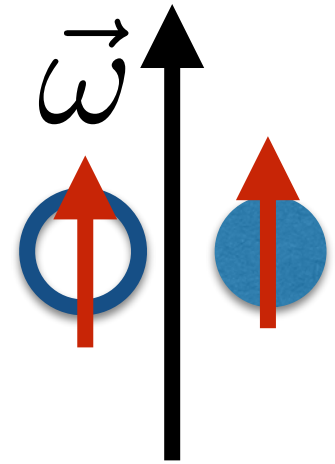
**Maybe induce considerable polarization splitting!**



# Magnetic Field Induced Polarization



$$S^\mu = -\frac{1}{8m} \epsilon^{\mu\nu\rho\sigma} p_\nu \varpi_{\rho\sigma}$$



For Lambda:

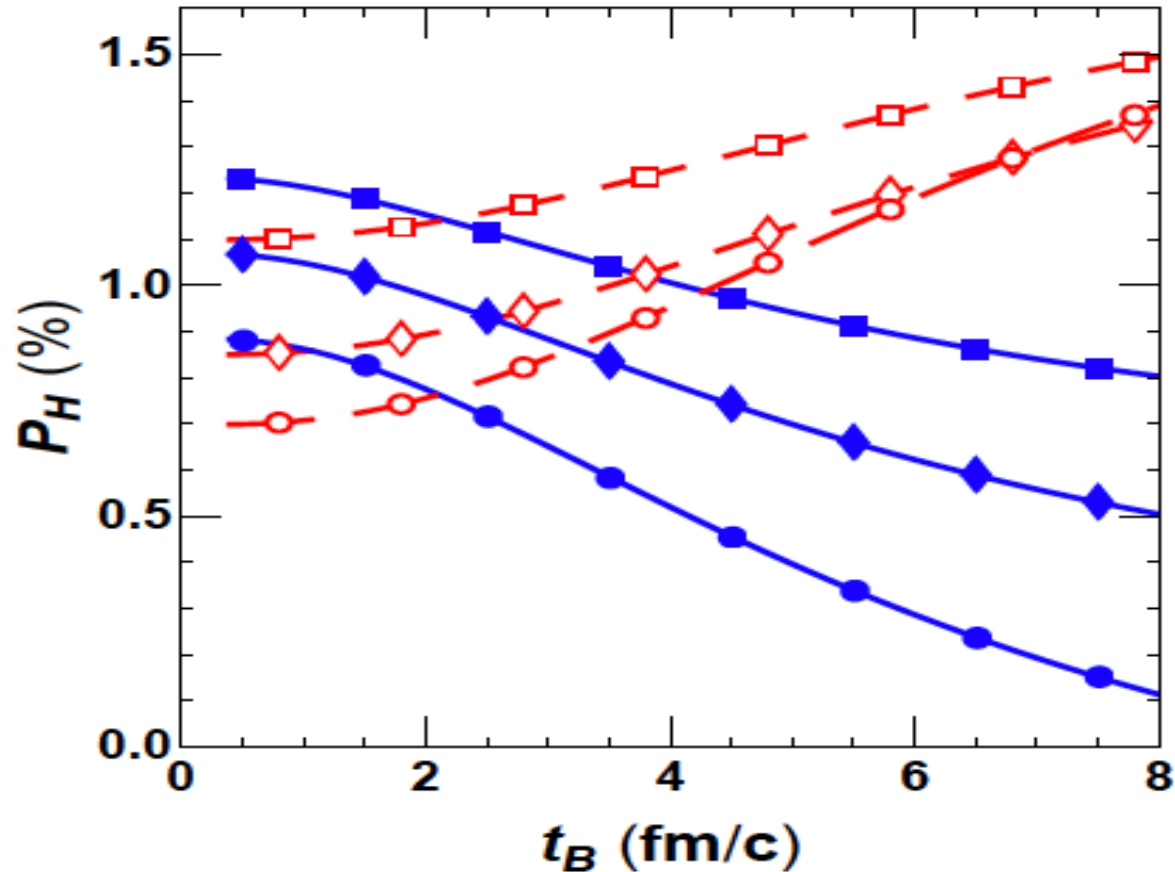
$$\varpi_{\rho\sigma} \rightarrow \left[ \varpi_{\rho\sigma} - 2 \left( \frac{0.61}{2M_p} \right) \frac{eF_{\rho\sigma}}{T} \right]$$

For anti-Lambda:

$$\varpi_{\rho\sigma} \rightarrow \left[ \varpi_{\rho\sigma} + 2 \left( \frac{0.61}{2M_p} \right) \frac{eF_{\rho\sigma}}{T} \right]$$

[Yu Guo, Shengqin Feng, Shuzhe Shi, JL, 1905.12613]

# Magnetic Field Induced Polarization



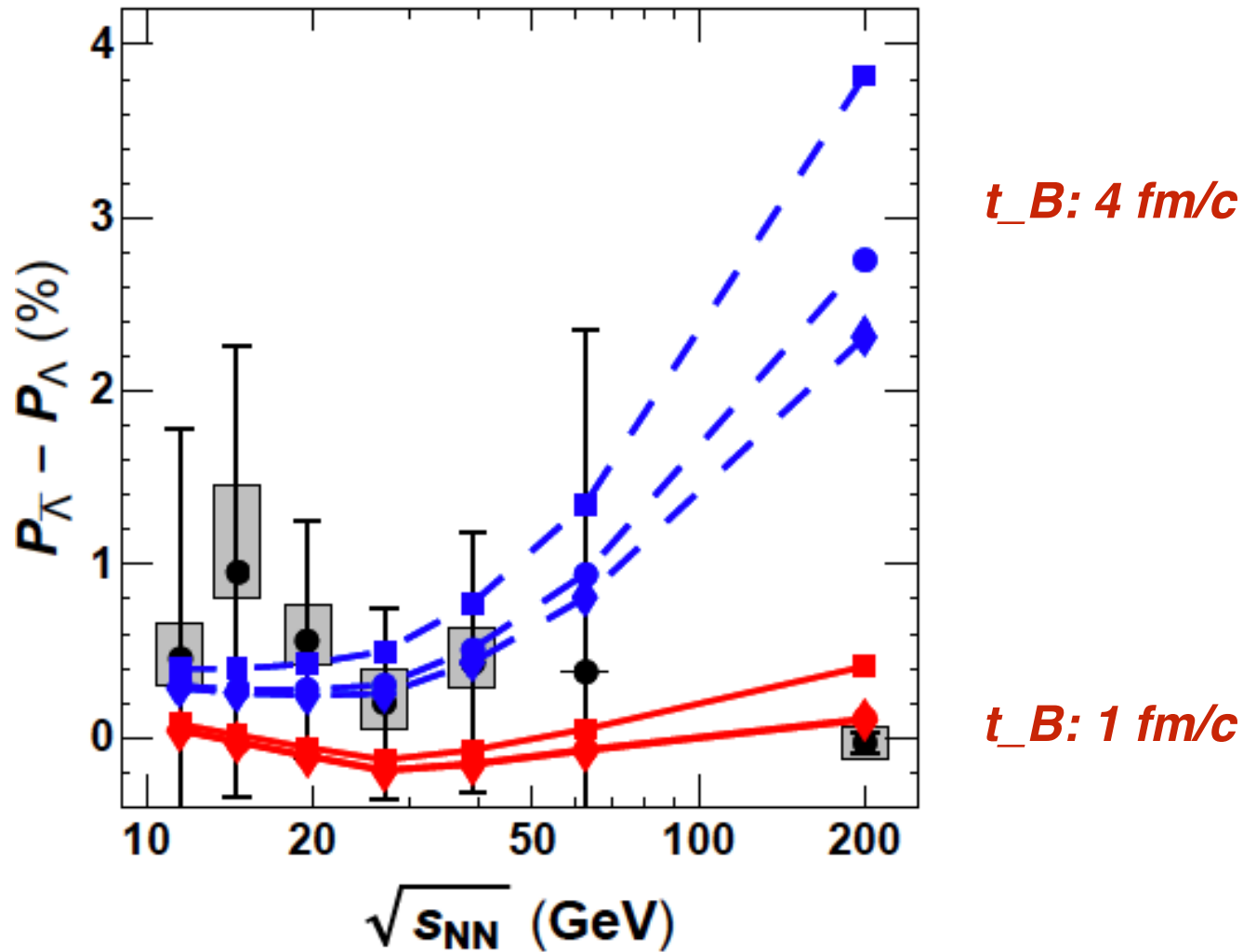
Type-1: ,  $F_B(t_B, t) \equiv \frac{1}{1+(t-t_0)^2/t_B^2}$  (see e.g. [63, 64]);

Type-2:  $F_B(t_B, t) \equiv \frac{1}{[1+(t-t_0)^2/t_B^2]^{3/2}}$  (see e.g. [48]);

Type-3:  $F_B(t_B, t) \equiv e^{-|t-t_0|/t_B}$  (see e.g. [43]).

[Yu Guo, Shengqin Feng, Shuzhe Shi, JL, 1905.12613]

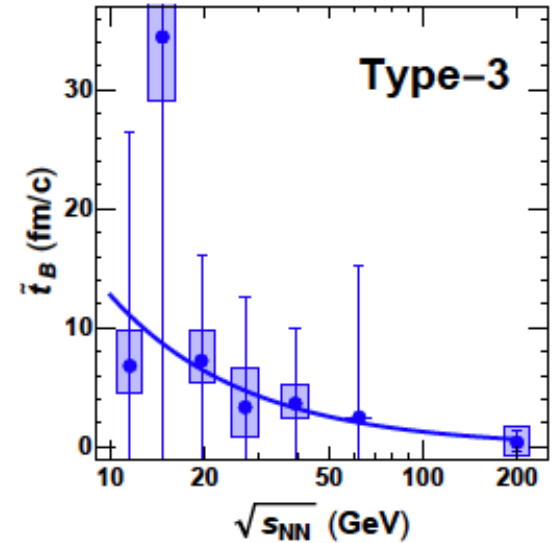
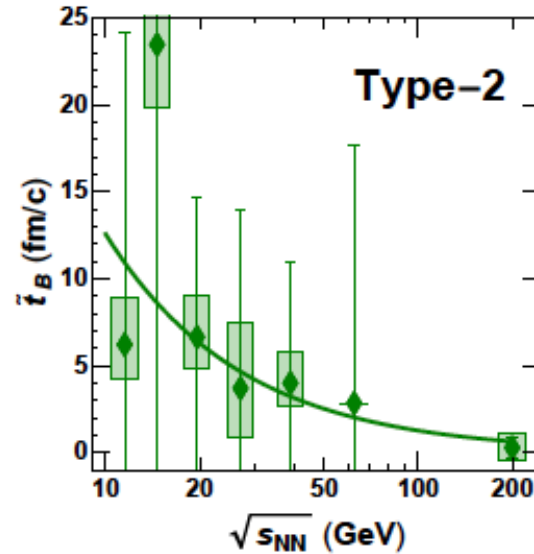
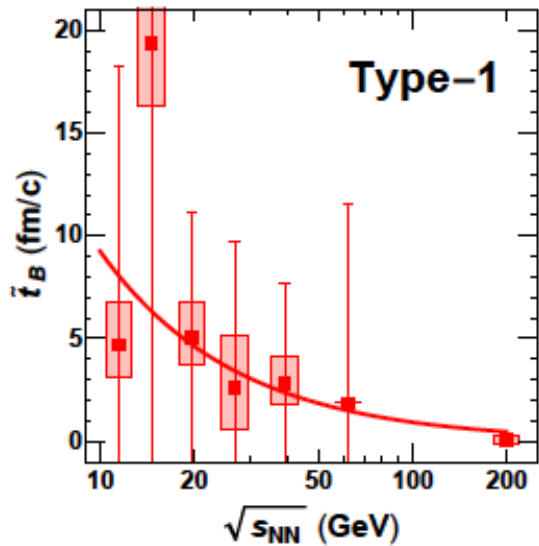
# Magnetic Field Induced Polarization



[Yu Guo, Shengqin Feng, Shuzhe Shi, JL, 1905.12613]

# Magnetic Field Induced Polarization

We extract optimal  $t_B$  at each beam energy according to observed polarization splitting.



$$t_B \simeq \frac{115 \text{ GeV} \cdot \text{fm}/c}{\sqrt{s_{NN}}}$$

*Much longer than vacuum field:*

$$t_{vac} \simeq \frac{26 \text{ GeV} \cdot \text{fm}/c}{\sqrt{s_{NN}}}$$

*Indicating significant in-medium magnetic fields due to medium effect!*

---

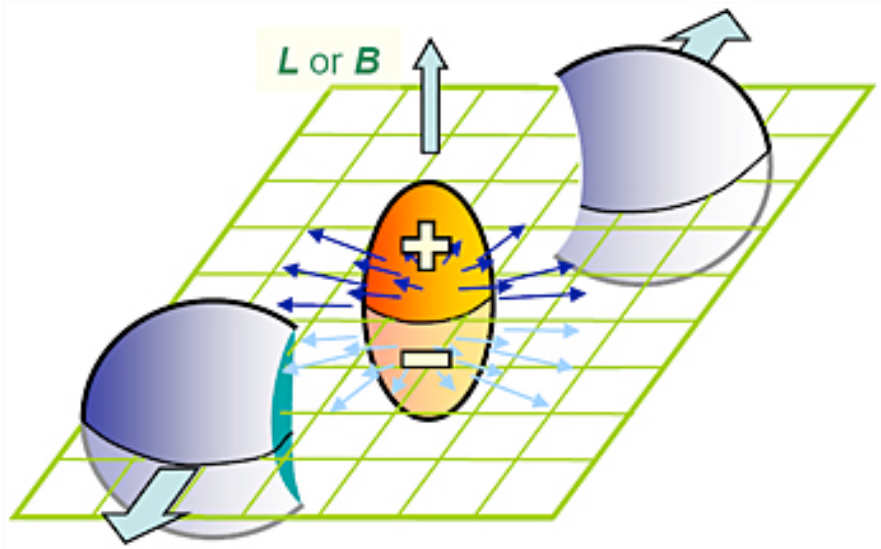
# Search for CME at RHIC & LHC

---

[See Fuqiang's talk]



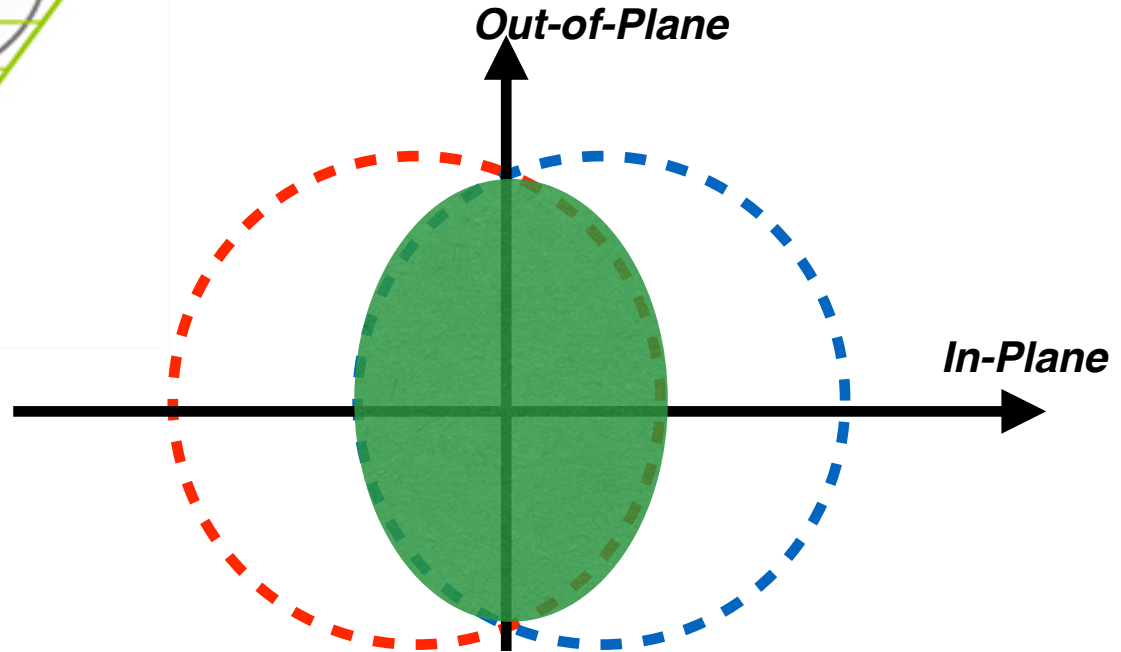
# Search for CME in Heavy Ion Collisions



*The quark-gluon plasma is a subatomic CHIRAL MATTER.*

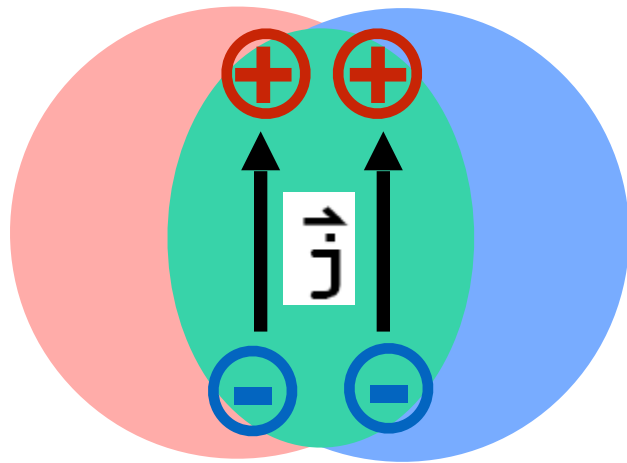
Can we observe CME in heavy ion collisions??

$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$



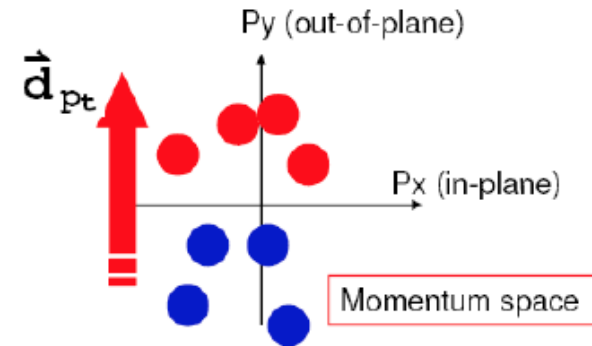
- 1) (nearly) chiral quarks
- 2) chirality imbalance
- 3) strong magnetic field

# From CME Current to Charge Separation



$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$

*strong radial blast:  
position  $\rightarrow$  momentum*



*Charge Separation or  
Electric Dipole in Pt Space  
(along out-of-plane)*

[Kharzeev 2004; Kharzeev, McLerran, Warringa, 2008; ...]

$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B$$

**Very difficult measurement:**

- \* **Zero average, only nonzero variance;**
- \* **Correlation measurement with significant backgrounds;**
- \* **Signal likely very small**

# Fighting with Backgrounds

*A two-component decomposition model:*

$$\gamma = \kappa v_2 F - H$$

F: Bulk Background

$$\delta = F + H$$

H: Possible Pure CME Signal =  $(a_{1,CME})^2$

*Bzdak, Koch, JL, 2012*

$$H_{SS} - H_{OS} \leftrightarrow 2(a_1)^2$$

*Many interesting proposals of new observables!*

**Vary  $v_2$  for fixed B:**

*AuAu v.s. UU;*

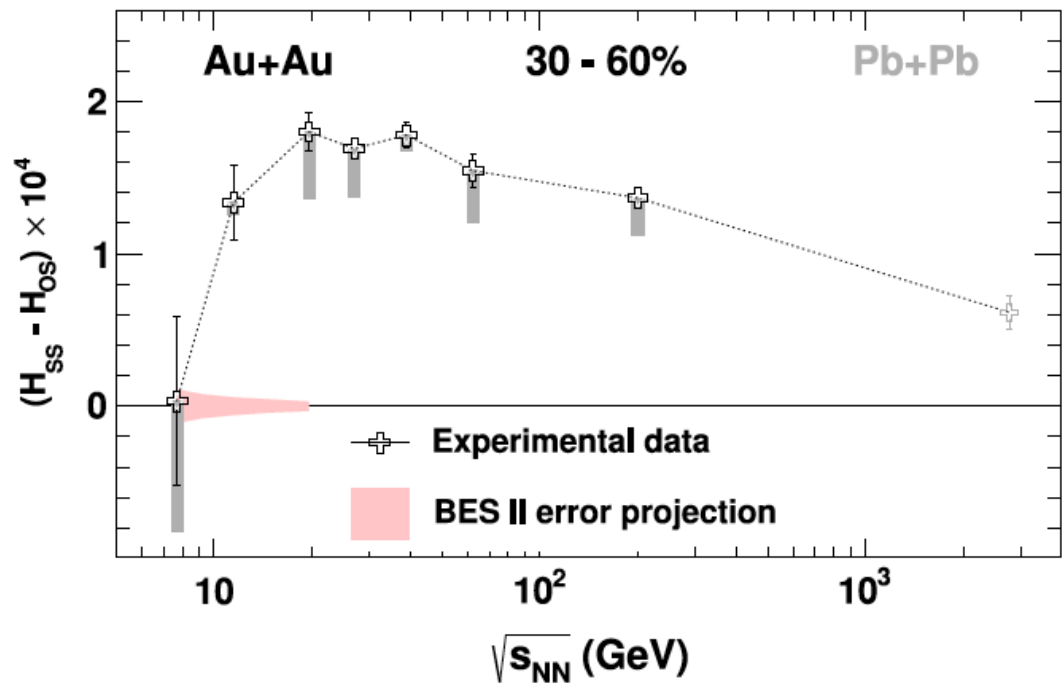
*Varying event-shape;*

*2-component subtraction.*

**Vary B for fixed  $v_2$ :**

*Isobaric collisions with*

*RuRu v.s. ZrZr*

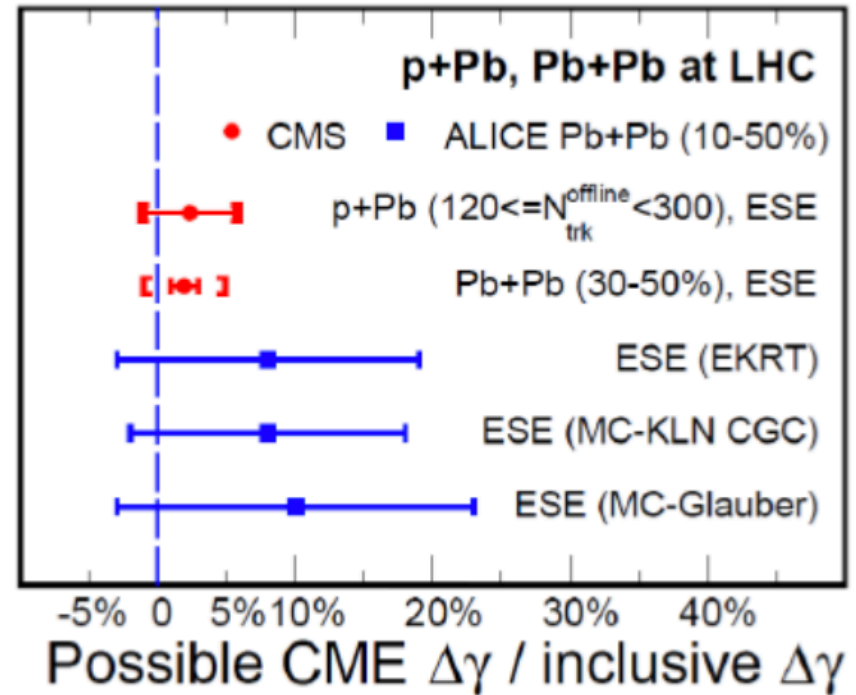
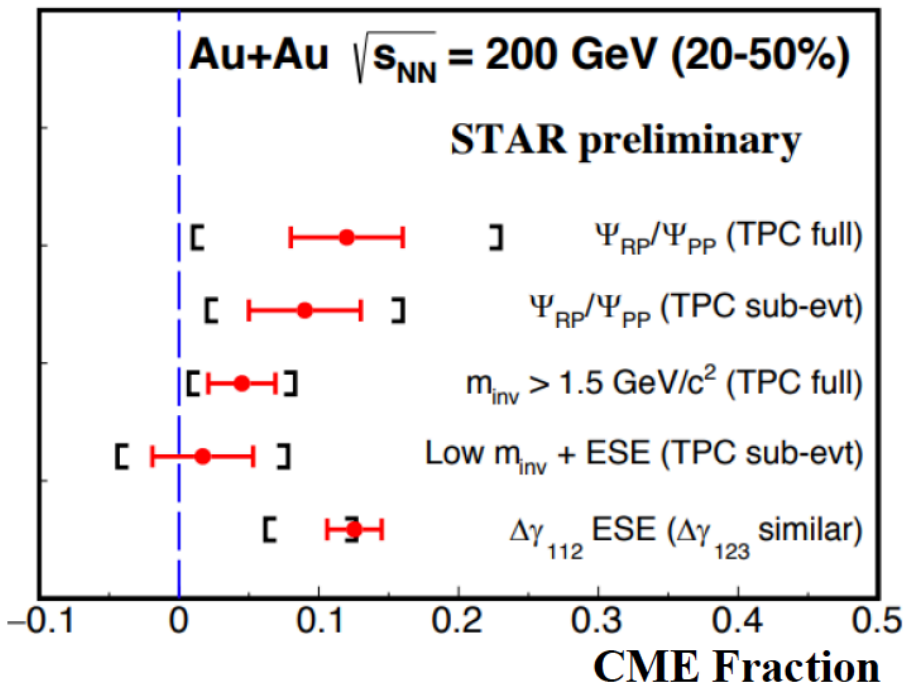


**STAR PRL2014**

# Current Experimental Status for CME

**Key challenge: weak signal versus strong backgrounds.**

**Many new measurements at RHIC and LHC:  
gamma correlator + certain procedure to constrain backgrounds**



**Lacey, Magdy, et al: R-correlator consistent with a 1~1% at RHIC**

**Current data provide encouraging hints, esp. @ RHIC energy!**

**Need quantitative modeling of signal+bkg to help exp search!**

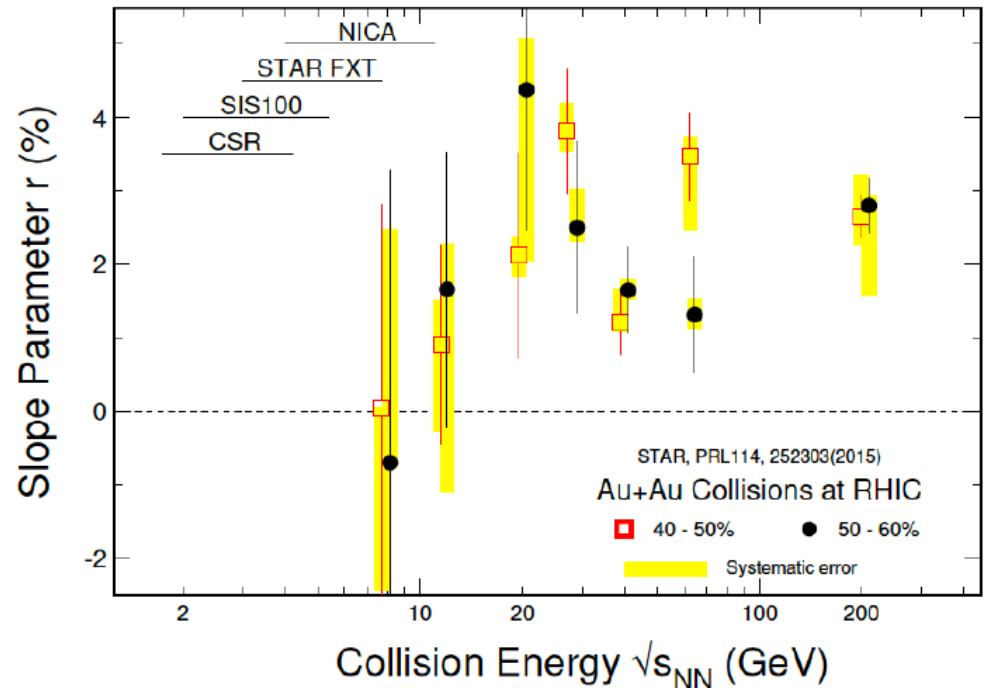
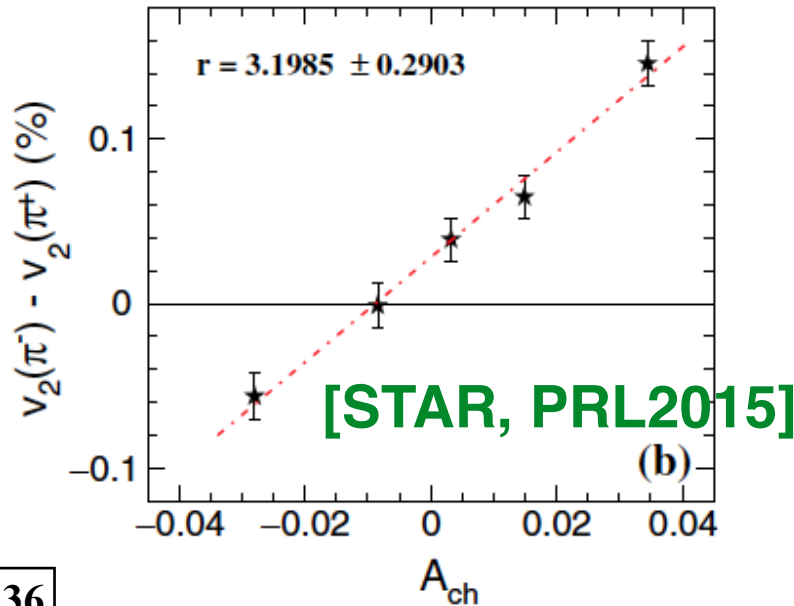
# Chiral Magnetic Wave

*CMW → charge quadrupole of QGP → elliptic flow splitting*

[Burnier, Kharzeev, JL, Yee, PRL2011; & arXiv: 1208.2537]

$$v_2^- - v_2^+ = r_e A$$

*charge quadrupole  
due to CMW transport*



*A consistent trend as CME:  
Turning-off at low energy*

---

# Quantitative Modeling of CME

---

# Integrate CME into Bulk Evolution

***\* Approach based on fluid dynamics (AVFD)***

***— our focus in this talk***

***\* Approach based on transport models.***

***— AMPT based***

***(Guoliang Ma, Yugang Ma, and collaborators)***

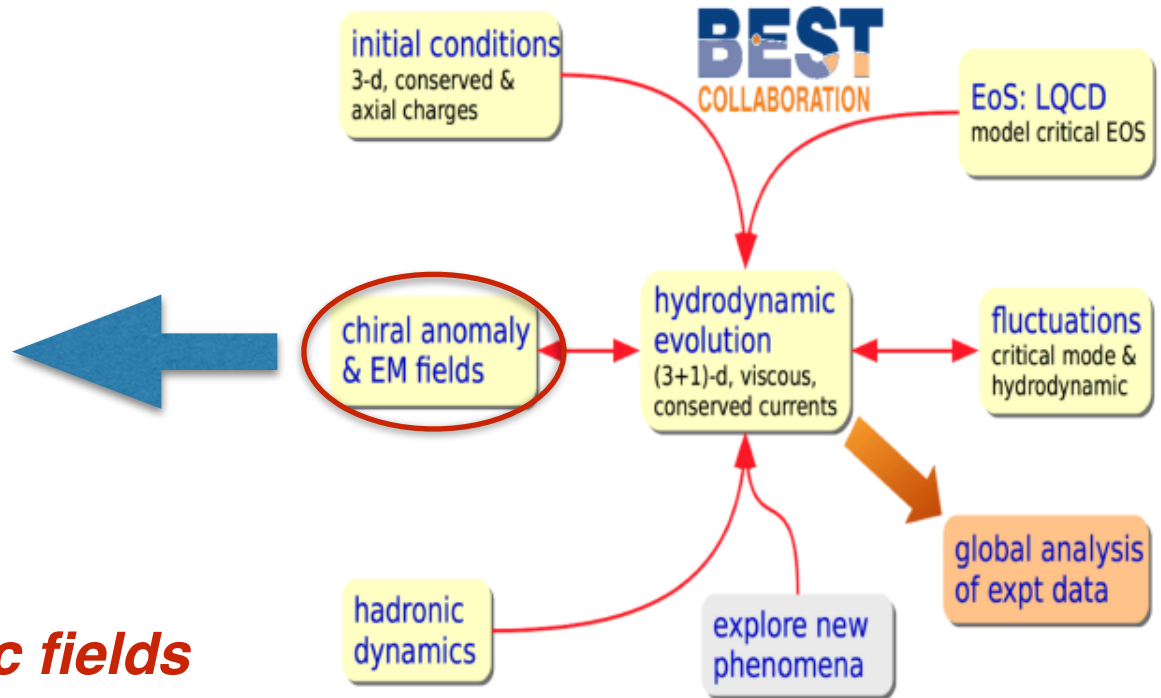
***— Chiral kinetic transport based***

***(Che-ming Ko and collaborators)***

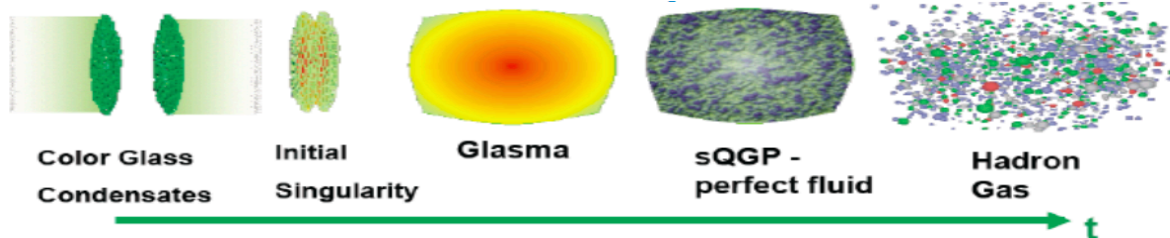


# Beam Energy Scan Theory (BEST) Collaboration

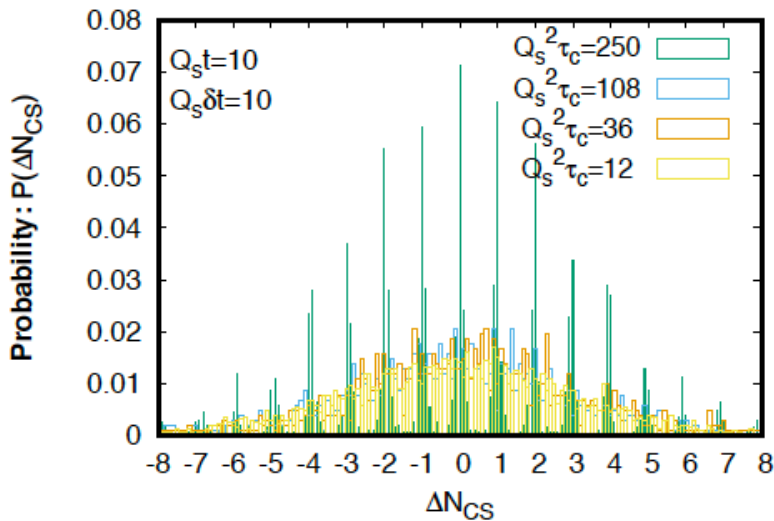
## CME Working Group



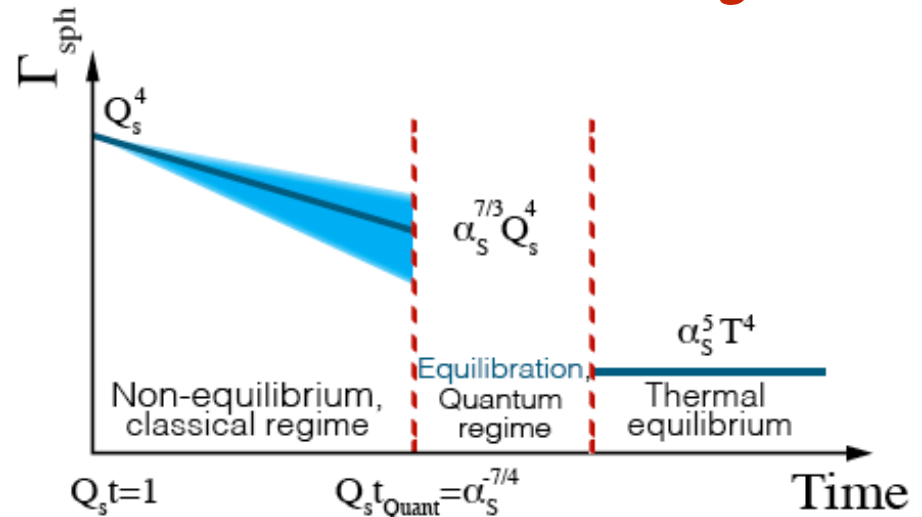
- *Initial conditions*
- *Dynamical magnetic fields*
- *Non-equilibrium anomalous transport coefficient*
- *Fluid dynamics framework with anomalous current*
- *Quantification of both signal and backgrounds*



# Axial Charge Initial Conditions



**Important information at the initial stages**



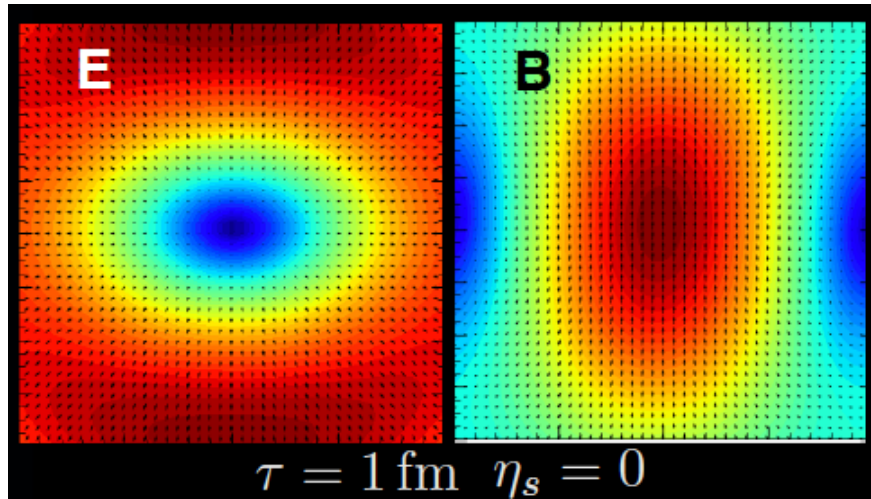
**In the glasma framework:**

- \* **Computed topological Chern-Simons number evolution**
- \* **Extracted significant non-equilibrium sphaleron rate**
- \* **Anomalous transport during the pre-thermal stage**

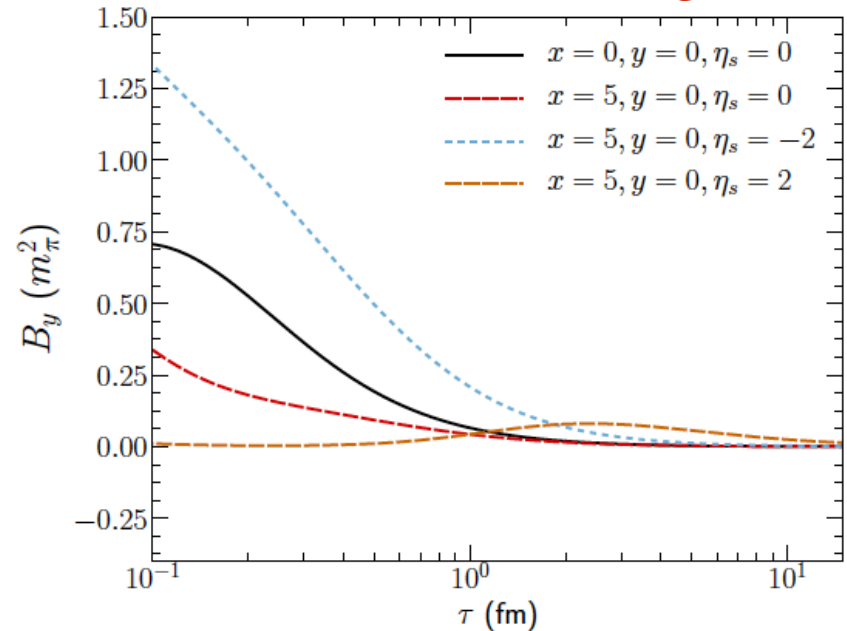
**[Mace, Schliting, Venugopalan, PRD2016;  
Mace, Muller, Schliting, Sharma, PRD2017]**

**Will be integrated into the initial condition for further modeling of CME during hydro stage**

# Dynamical Magnetic Fields



**Important information at the initial stages**



**A significant step forward toward full magneto-hydrodynamics (MHD)**

**Code package available:**

**<https://bitbucket.org/bestcollaboration/heavy-ion-em-fields>**

**[Gursoy, Kharzeev, Rajagopal, Shen, et al, PRC2018]**

**A viable and practical way to integrate dynamical B field!**

# Attempting Anomalous Hydro

Physics Letters B 756 (2016) 42–46

Contents lists available at ScienceDirect

Physics Letters B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



ELSEVIER



Hydrodynamics with chiral anomaly and charge separation in relativistic heavy ion collisions



Yi Yin<sup>a,\*</sup>, Jinfeng Liao<sup>b,c</sup>

<sup>a</sup> Physics Department, Brookhaven National Laboratory, Upton, NY 11973, USA

<sup>b</sup> Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B, Sampson Lane, Bloomington, IN 47408, USA

<sup>c</sup> RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA

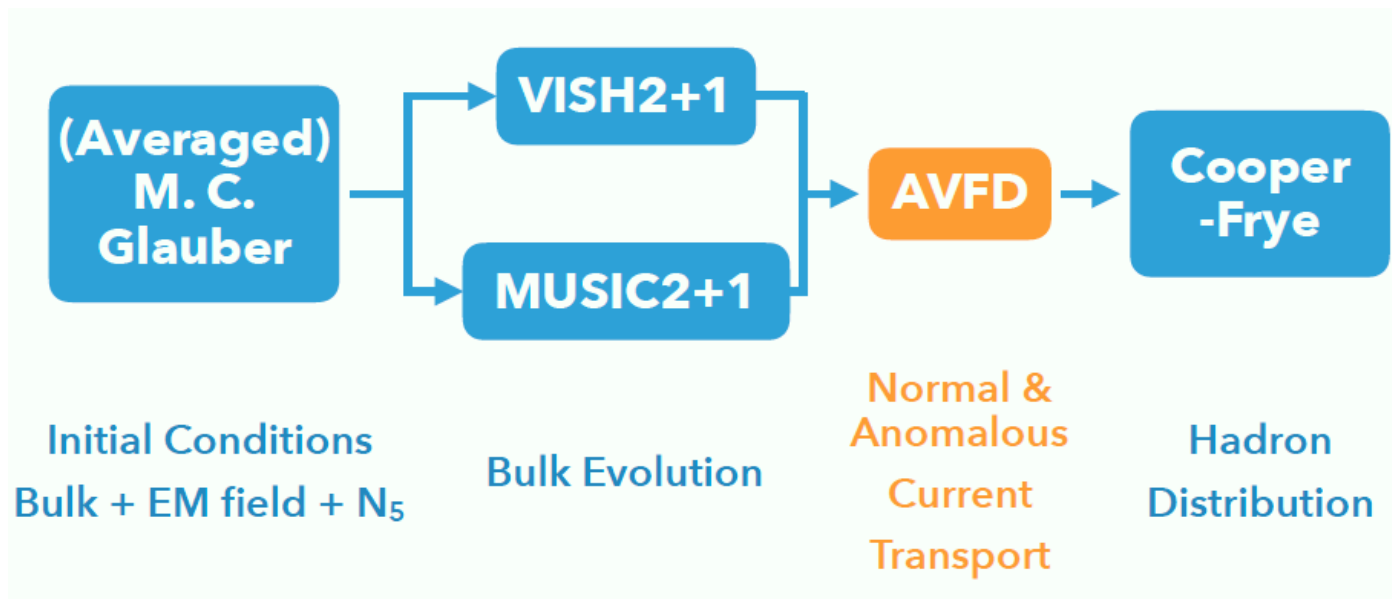
***A good first try: albeit assuming ideal hydro charge transport.  
To be consistent and realistic: need viscous + anomalous***

***[Yin, Liao, PLB2016]***

# AVFD Framework

**Establishment of Anomalous-Viscous Fluid Dynamics (AVFD):  
Hydrodynamical realization of CME in HIC.**

**[newest developments: EBE-AVFD; AVFD+axial dynamics; AVFD+LCC]**



**We now have a versatile tool to quantitatively understand and answer many important questions about CME in heavy ion collisions!**

**[S. Shi, JL, et al: arXiv:1611.04586; arXiv:1711.02496]**

# AVFD Framework



*Note: bulk properties  
fully data-validated*

[arXiv:1611.04586; arXiv:1711.02496]

$$D_\mu J_R^\mu = + \frac{N_c q^2}{4\pi^2} E_\mu B^\mu \quad D_\mu J_L^\mu = - \frac{N_c q^2}{4\pi^2} E_\mu B^\mu$$

$$J_R^\mu = n_R u^\mu + v_R^\mu + \frac{N_c q}{4\pi^2} \mu_R B^\mu$$

$$J_L^\mu = n_L u^\mu + v_L^\mu - \frac{N_c q}{4\pi^2} \mu_L B^\mu$$

**CME**

**Viscous Effect**

$$\Delta^{\mu\nu} d v_{R,L}^\nu = - \frac{1}{\tau_{\text{rlx}}} (v_{R,L}^\mu - v_{\text{NS}}^\mu)$$

$$v_{\text{NS}}^\mu = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_\nu \frac{\mu}{T} + \frac{\sigma}{2} q E^\mu$$

**arXiv:1611.04586**

# Quantifying the chiral magnetic effect from anomalous-viscous fluid dynamics<sup>\*</sup>

Yin Jiang(姜寅)<sup>1</sup> Shuzhe Shi(施舒哲)<sup>2</sup> Yi Yin(尹伊)<sup>3</sup> Jinfeng Liao(廖劲峰)<sup>2,4;1</sup>

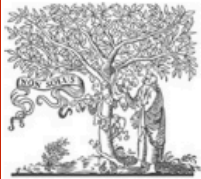
<sup>1</sup> School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

<sup>2</sup> Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

<sup>3</sup> Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

<sup>4</sup> Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan 430079, China

Annals of Physics 394 (2018) 50–72

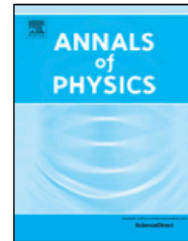


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journal homepage: [www.elsevier.com/locate/aop](http://www.elsevier.com/locate/aop)



Anomalous chiral transport in heavy ion collisions from Anomalous-Viscous Fluid Dynamics



Shuzhe Shi<sup>a,\*</sup>, Yin Jiang<sup>b,c</sup>, Elias Lilleskov<sup>d,a</sup>, Jinfeng Liao<sup>a,e,\*</sup>

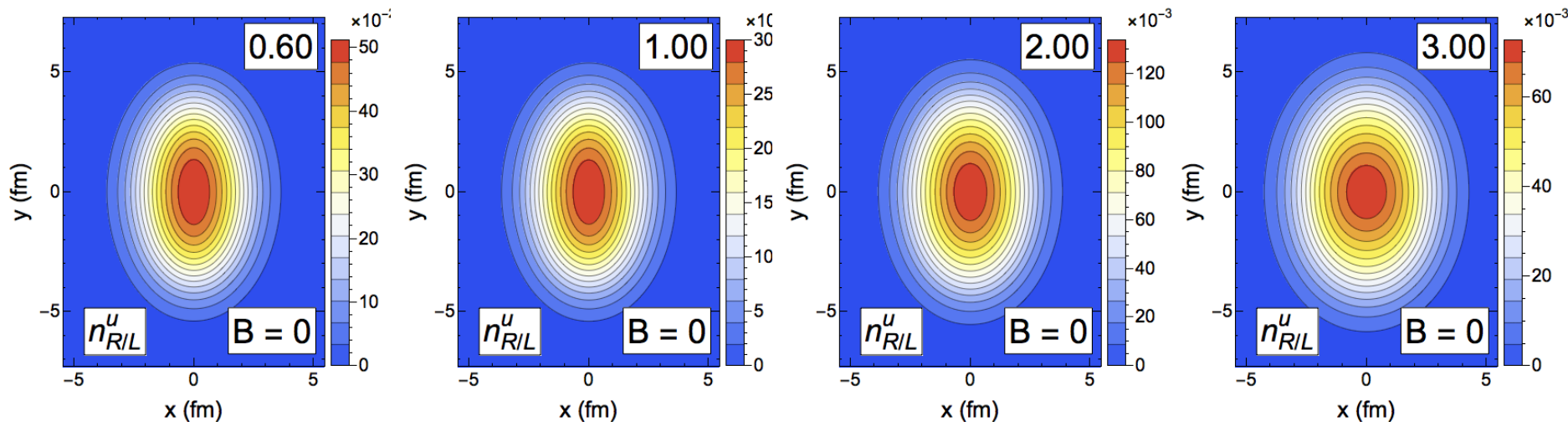
**Shuzhe Shi**  
**(McGill; PhD @ IUB)**

**Yin Jiang (Beihang),**  
**Yi Yin (MIT),**  
**Elias Lilleskov (REU)**

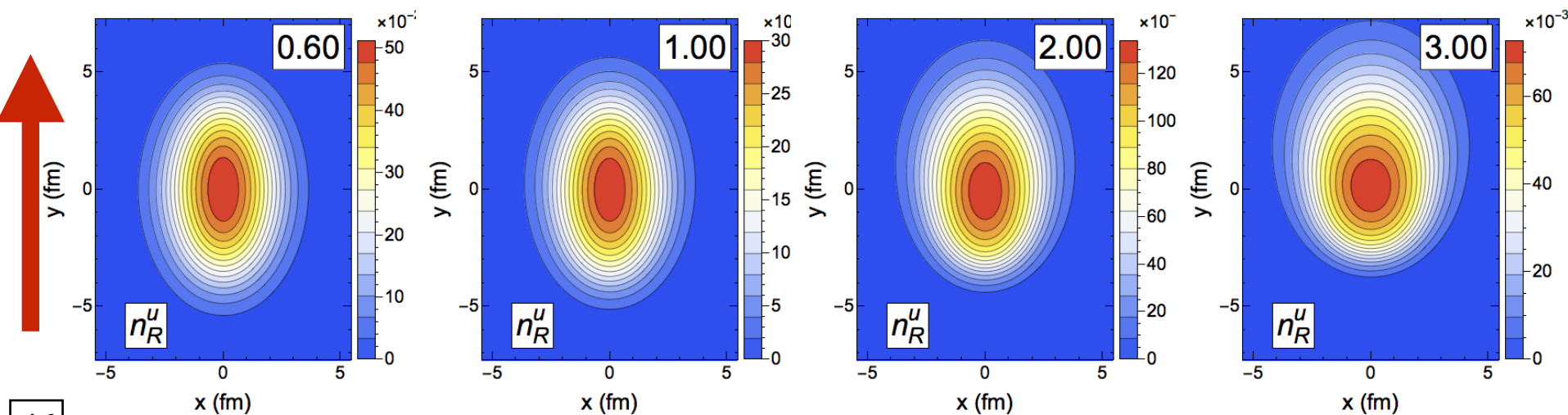
**arXiv:1711.02496**



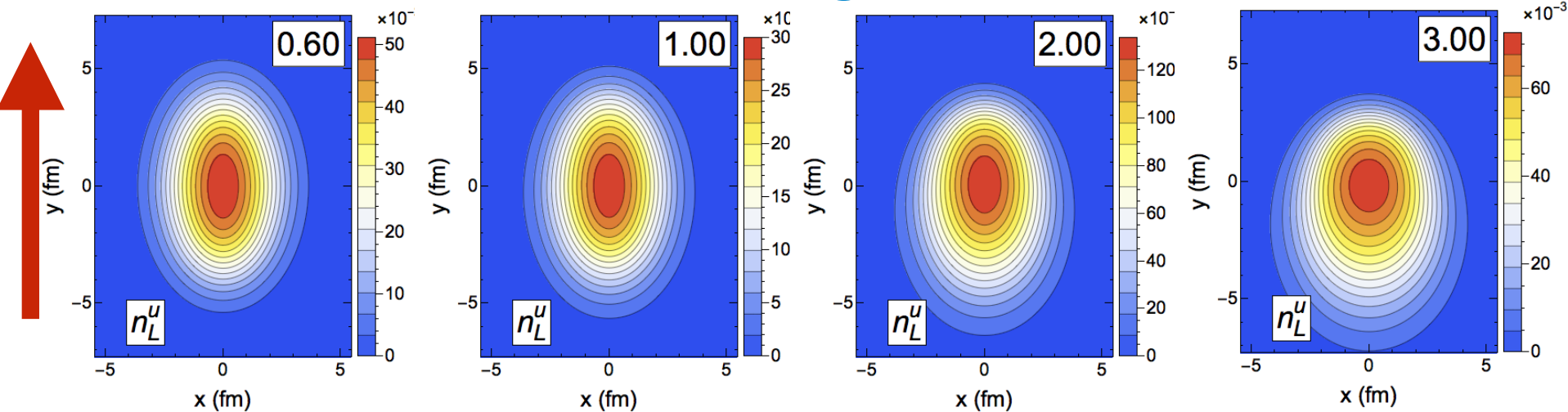
# Demonstrating the AVFD



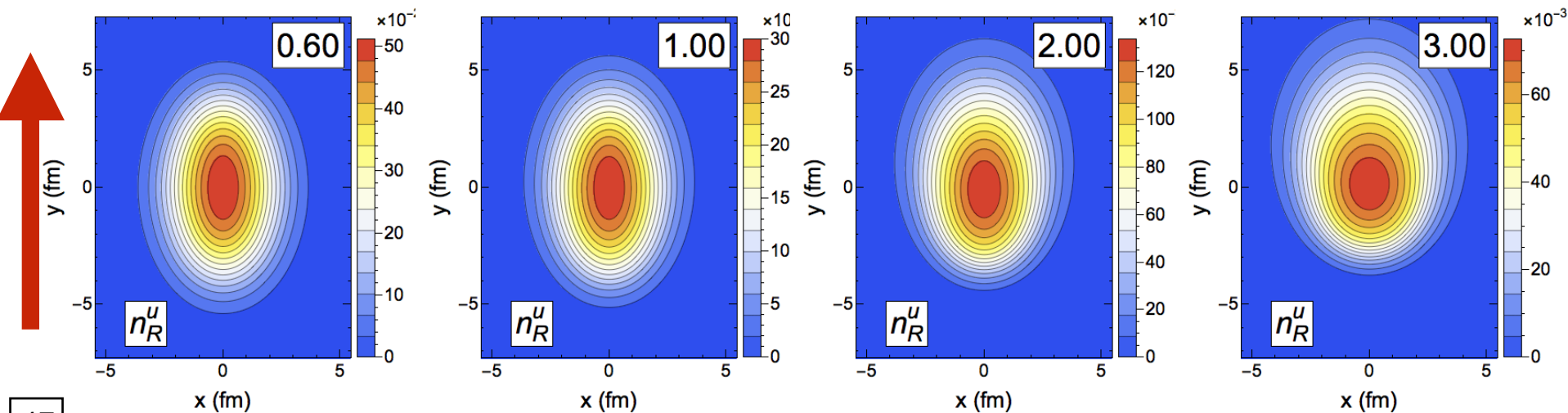
Upper: NO magnetic field  
Lower: with B field (along y+ direction)



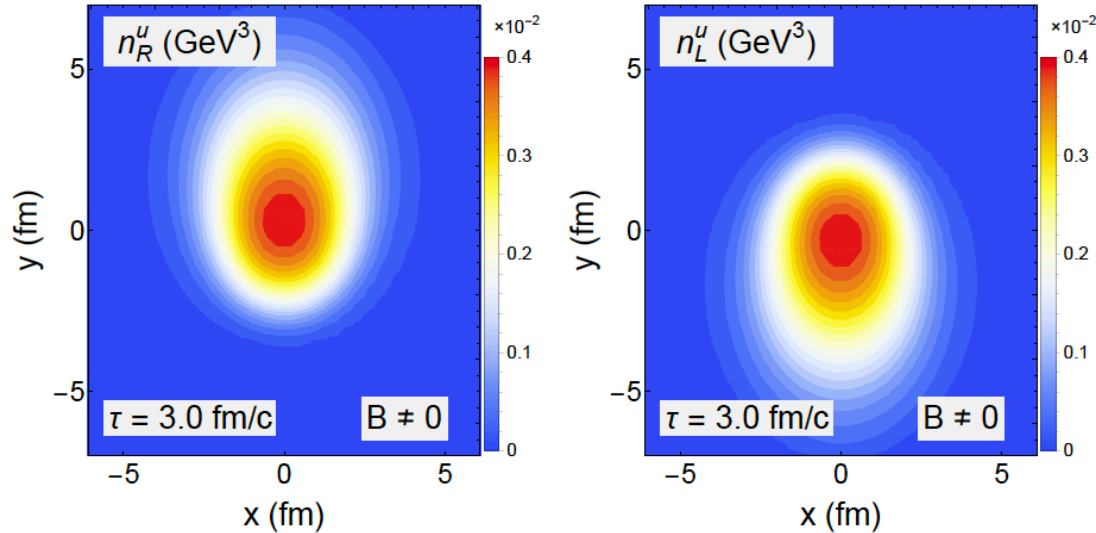
# Demonstrating the AVFD



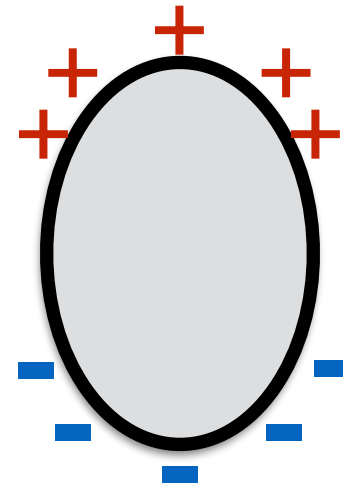
Upper: Left-Handed (LH), with B field (along y+ direction)  
Lower: Right-Handed (RH), with B field (along y+ direction)



# The Charge Separation from AVFD



$$E \frac{dN}{d^3p}(x^\mu, p^\mu) = \frac{g}{(2\pi)^3} \int_{\Sigma_{fo}} p^\mu d^3\sigma_\mu f(x, p)$$



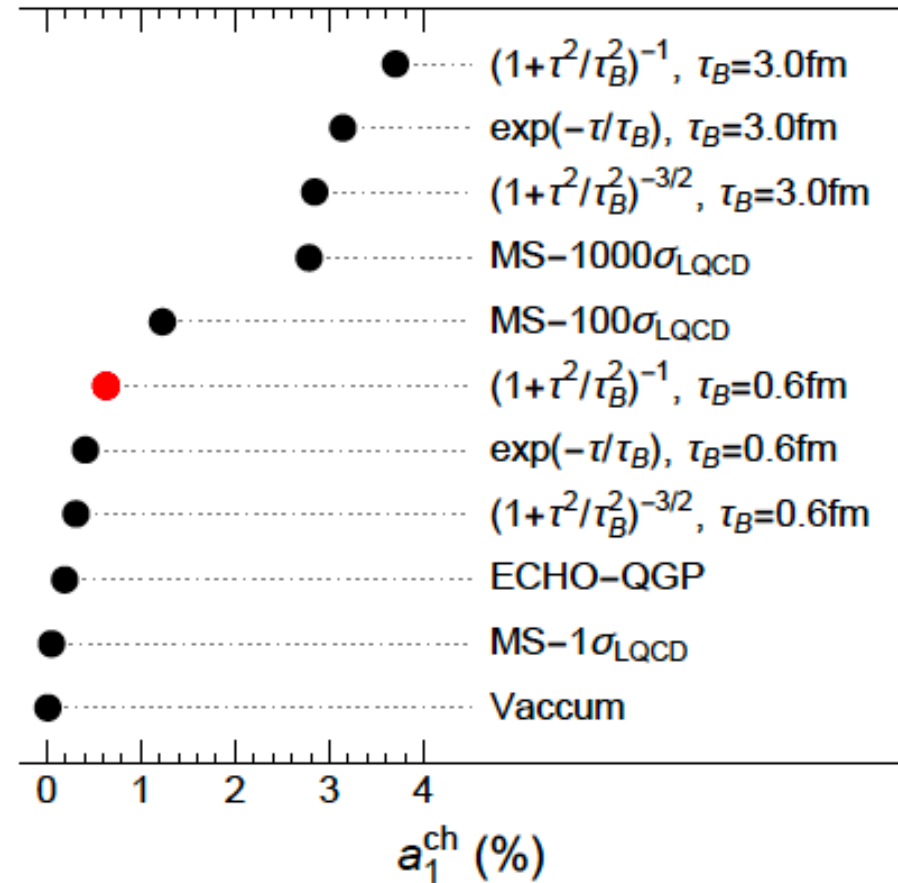
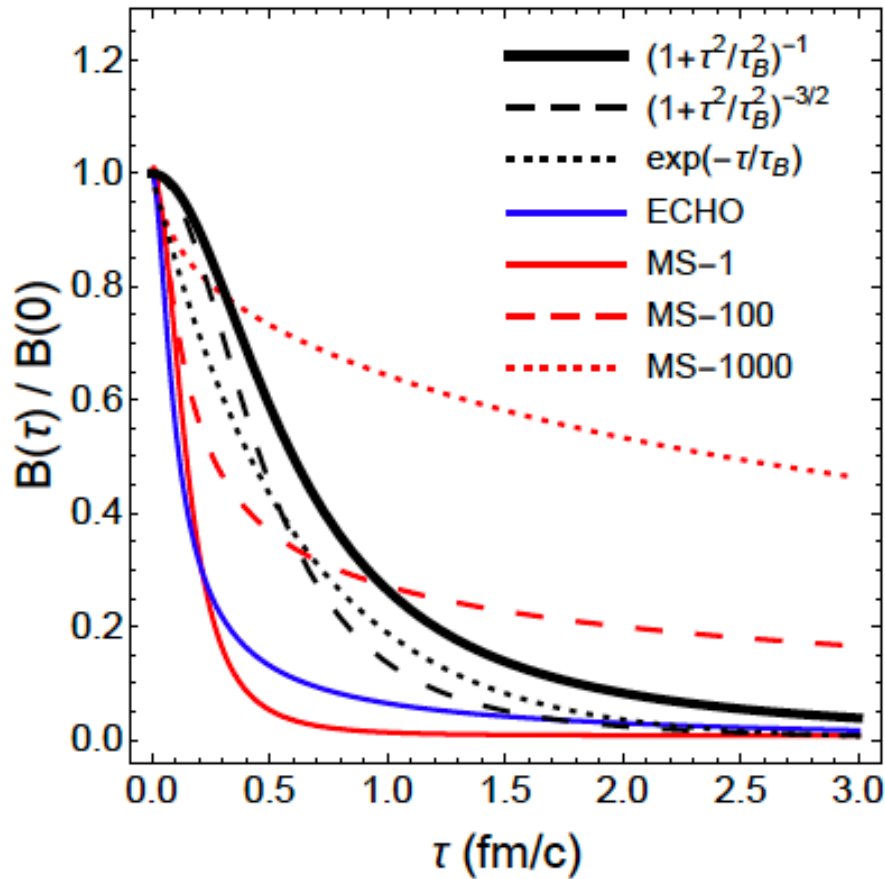
**Chirality imbalance  $\rightarrow$  R/L  
asymmetry  $\rightarrow$  charge asymmetry**

**B field  $\otimes \mu_5 \Rightarrow$  current  $\Rightarrow$  dipole (charge separation)**

$$dN_{\pm}/d\phi \propto 1 + 2 a_{1\pm} \sin(\phi - \psi_{RP}) + \dots$$

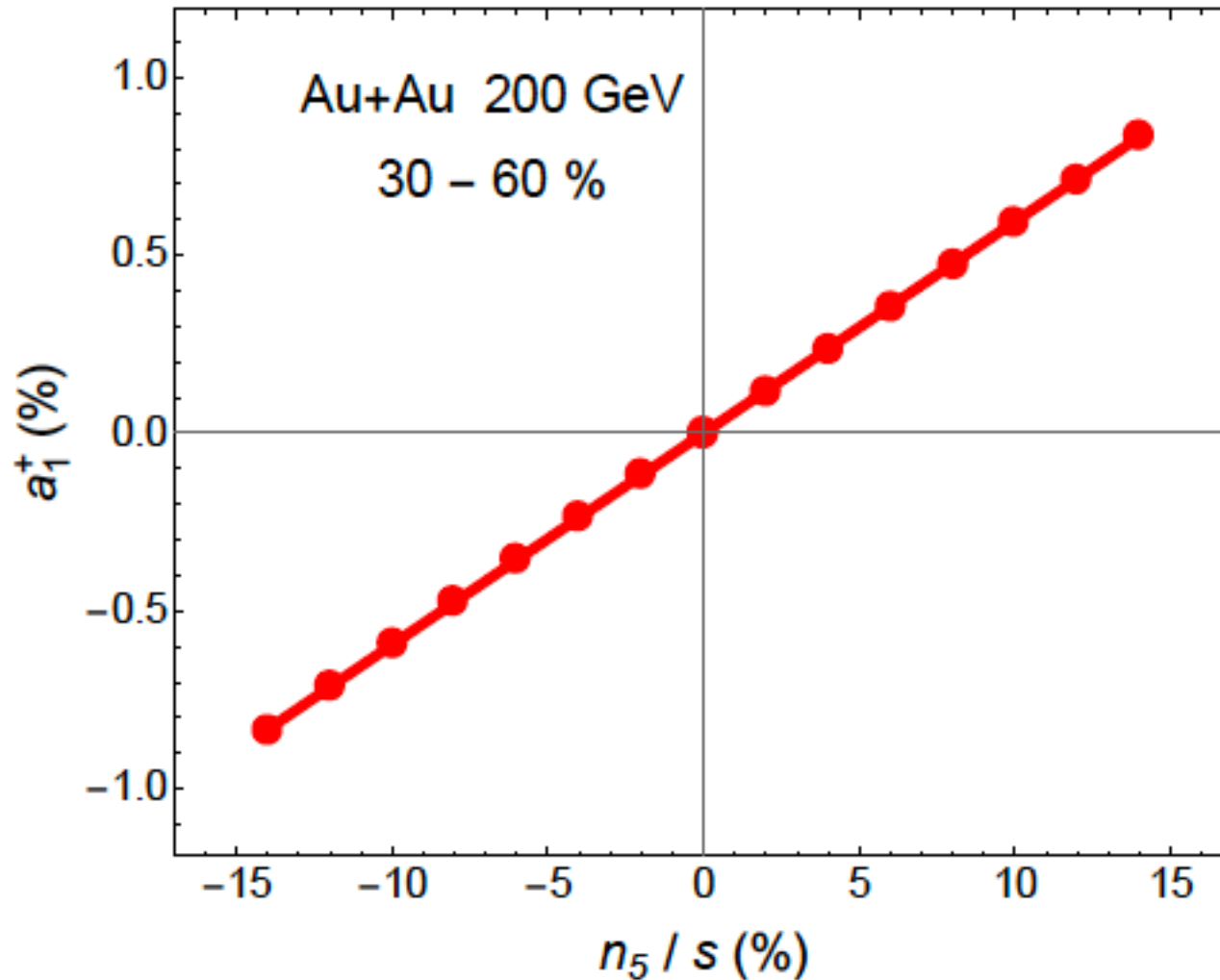
$$H_{SS} - H_{OS} \leftrightarrow 2(a_1)^2$$

# The Influence of the Magnetic Field



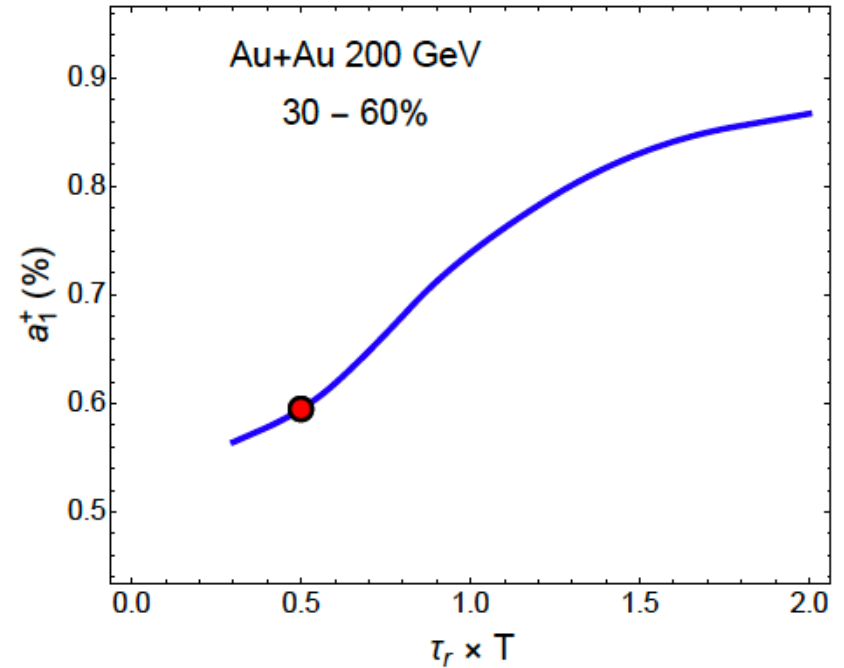
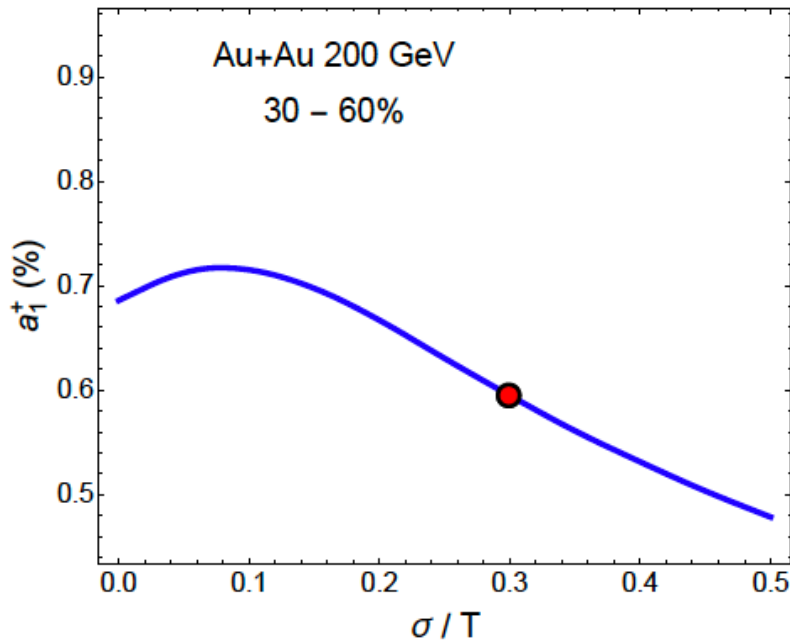
**Strong influence by B field evolution;  
Significant theoretical uncertainty!**

# The Axial Charge Initial Condition



**Very sensitive to initial axial charge;  
Significant theoretical uncertainty!**

# The Influence of the Viscous Transport

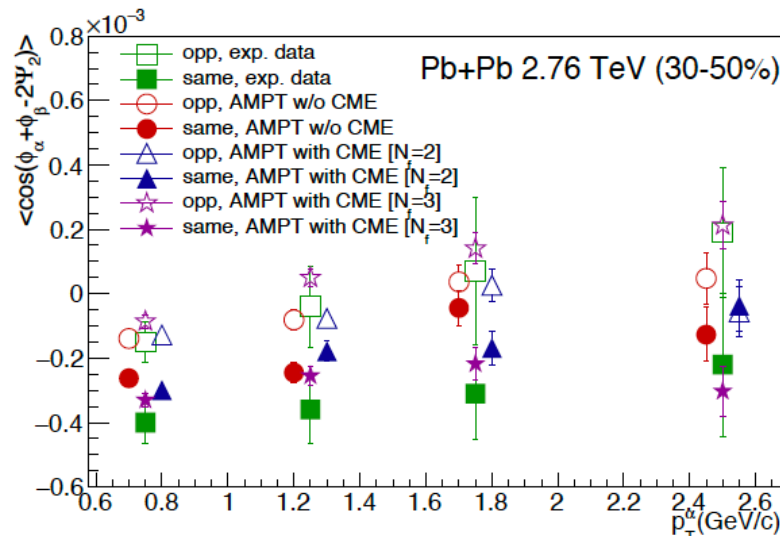
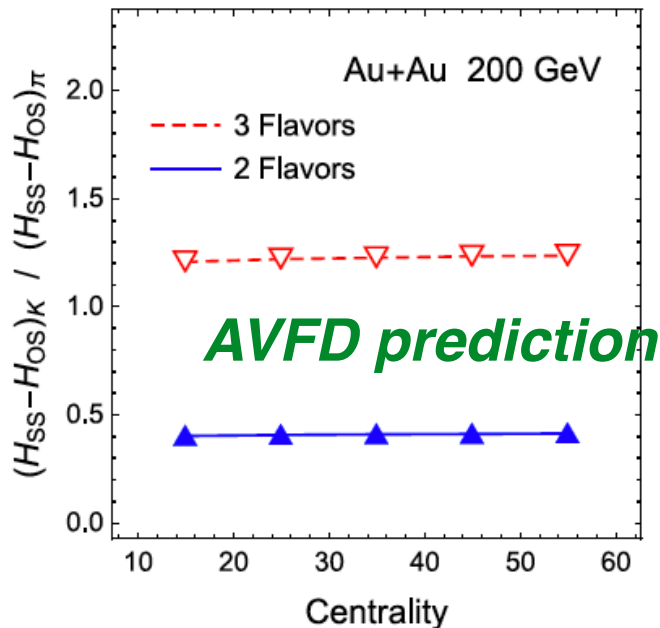


$$\Delta_{\nu}^{\mu} d v_{R,L}^{\nu} = -\frac{1}{\tau_{rlx}} (v_{R,L}^{\mu} - v_{NS}^{\mu})$$

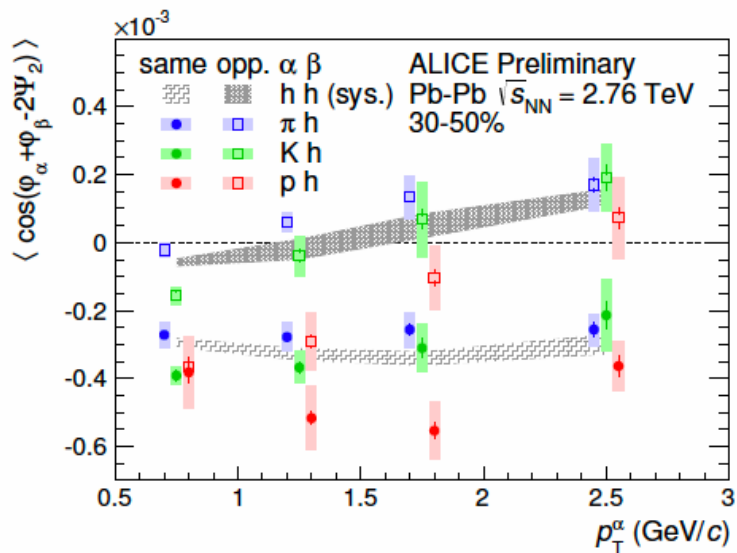
$$v_{NS}^{\mu} = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_{\nu} \frac{\mu}{T} + \frac{\sigma}{2} q E^{\mu}$$

**First calibration for the influence of the viscous transport on charge separation signal!**

# Flavor Dependence



*Huang, Ma, Ma, PRC2018*



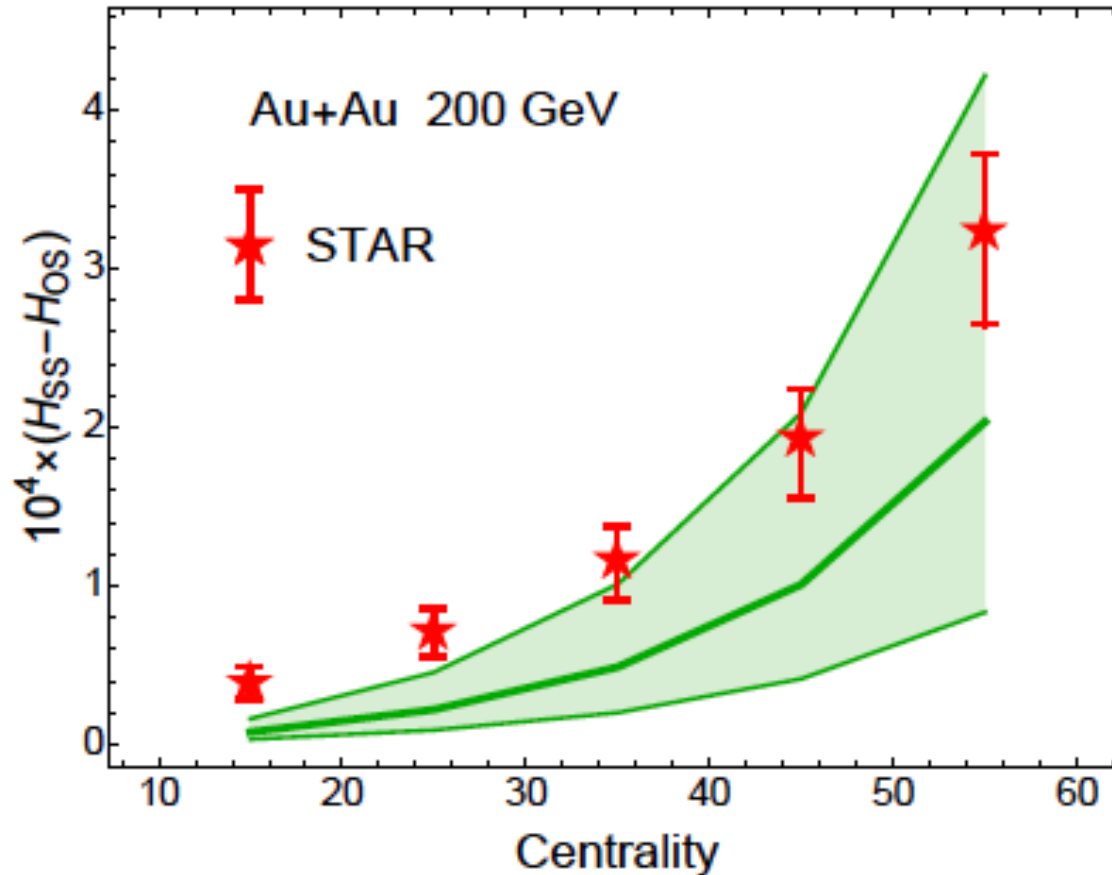
ALI-PREL-88970

**ALICE 2.76TeV**

**Kaons are sensitive  
to anomalous  
transport of s-quarks.**



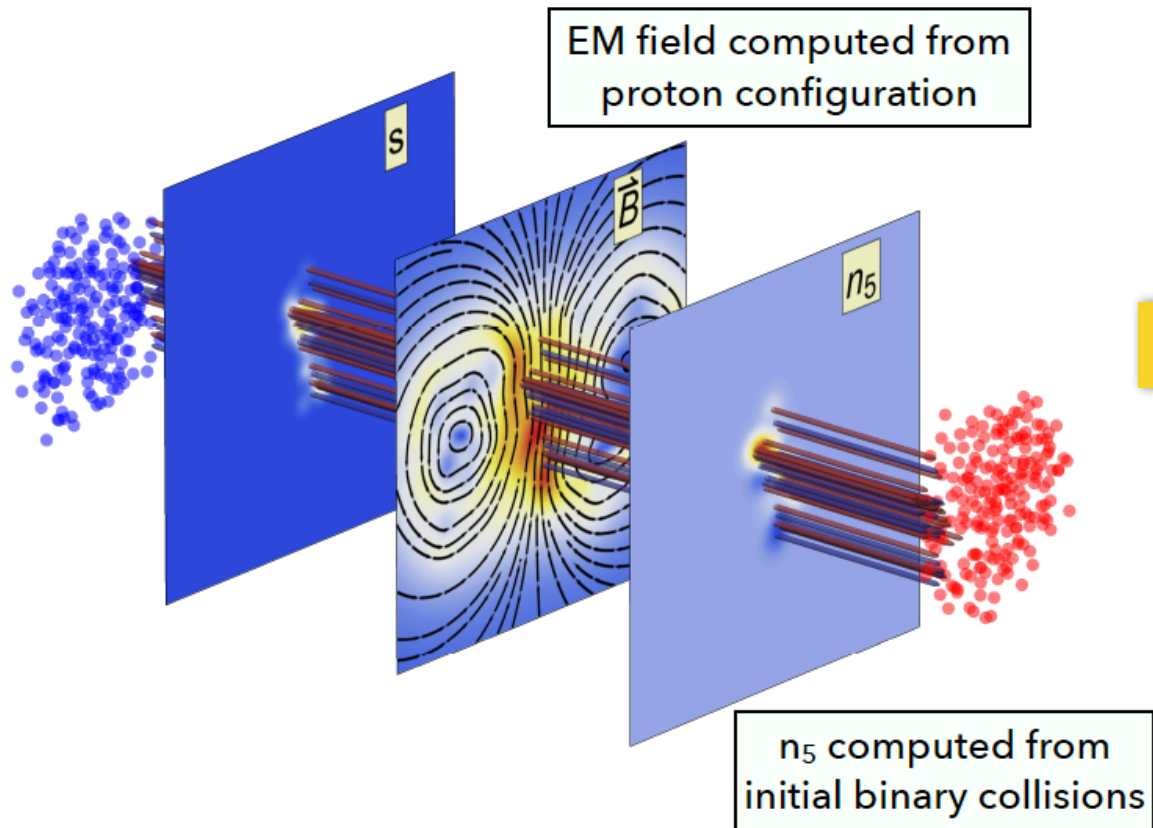
# AVFD for AuAu Collisions



*CME is quantitatively viable for describing relevant experimental observable.*

*[A lot of detailed results in:  
Shi, Yin, JL, ..., arXiv:1611.04586; arXiv:1711.02496]*

# Event-By-Event AVFD



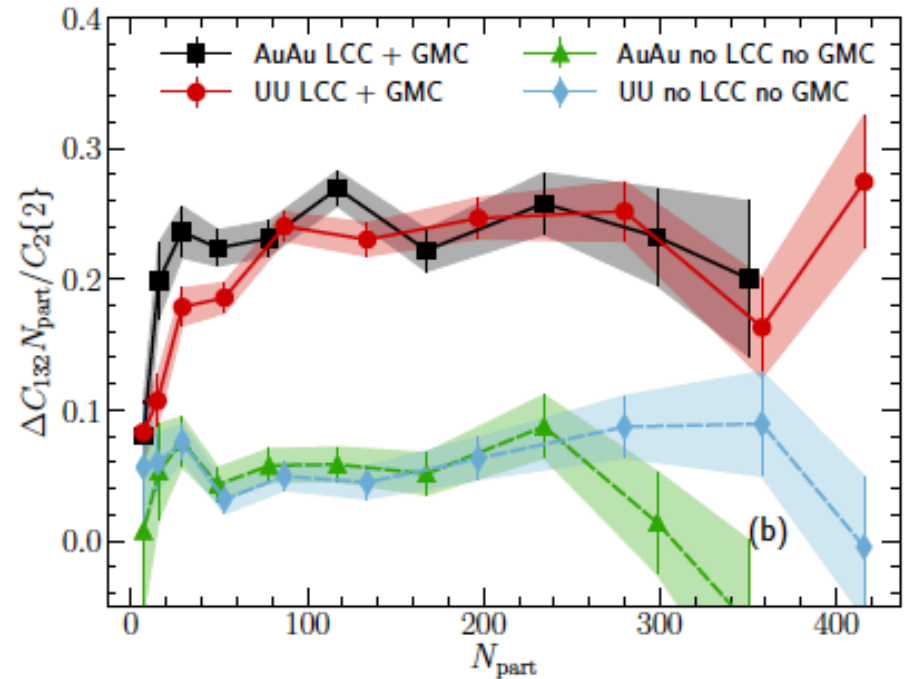
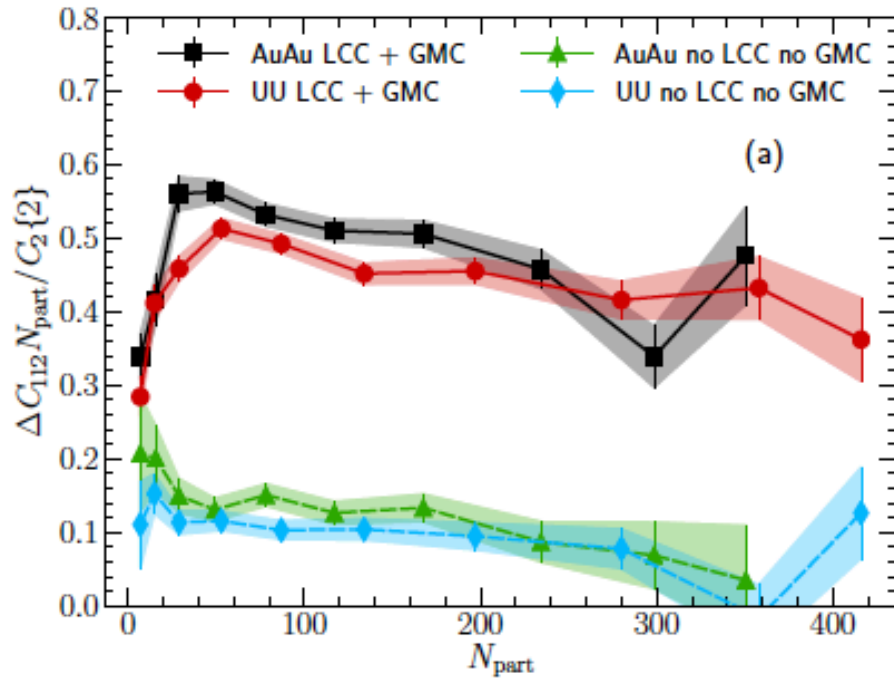
## ***Include EBE fluctuations:***

- ▶ Initial Conditions
- ▶ Statistic @ Freeze-out
- ▶ Hadron Cascade  
(~ *half of all bkg.*)

***Important for better understanding:***  
\* *Interplay between signal and BKG;*  
\* *Experimental analysis methods*

*Shuzhe Shi, Hui Zhang, Defu Hou, JL, to appear soon; QM2018 proceedings.*

# Implementing Local Charge Conservation (LCC)



*To quantify background correlations in state-of-art hydro framework*

*[Schenke, Shen, Tribedy, 2019]*

*New development of particlization: the best way to quantify LCC*

*[Koch, Oliinychenko, 2019]*

# EBE-AVFD+LCC: Event Shape Engineering

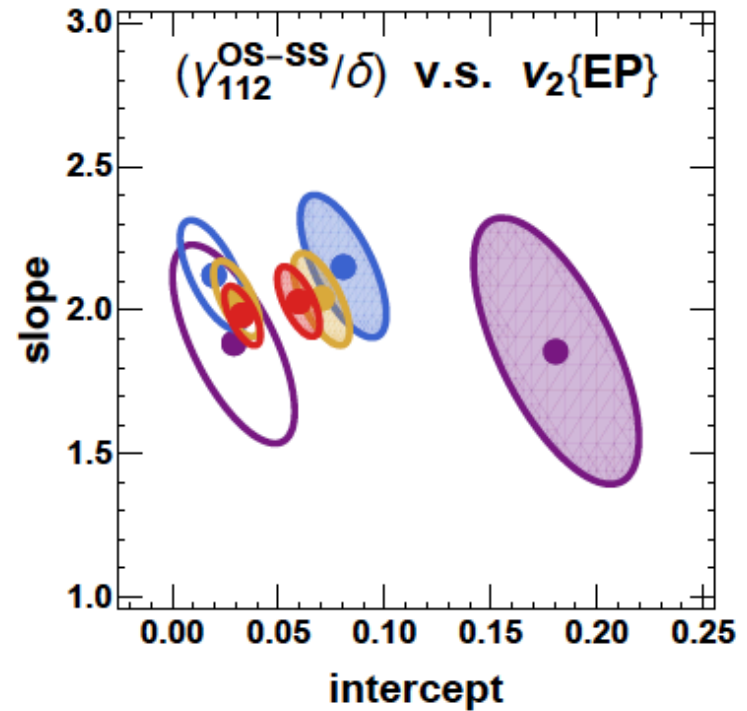
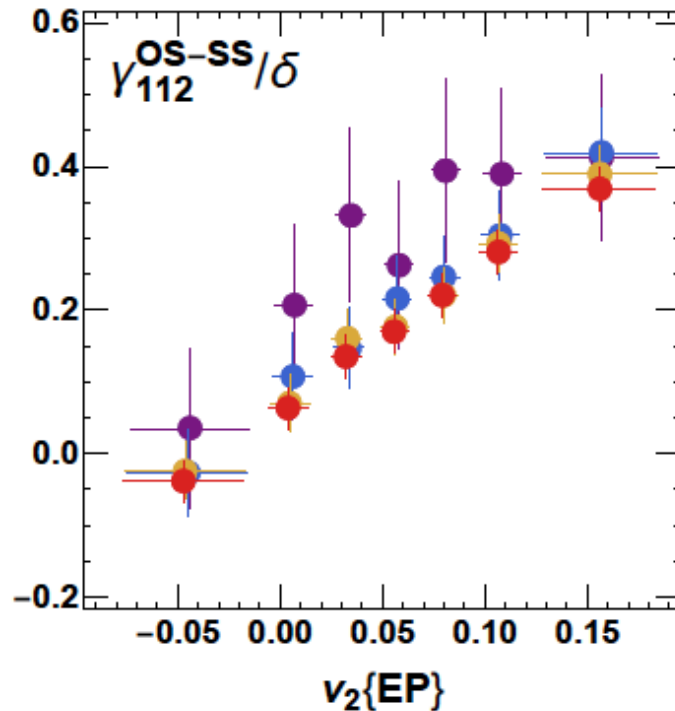
$$\gamma = \kappa v_2 F - H$$

$$\delta = F + H$$

filled: w/ CME

open: w/o CME

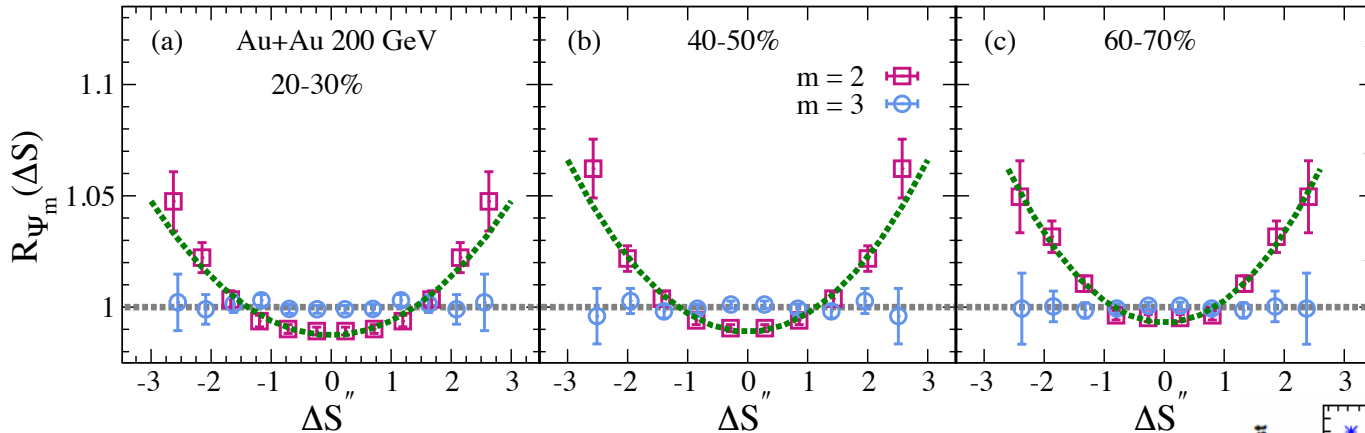
$$P_{\text{LCC}} = 0.00, 0.33, 0.67, 1.00$$



**First time: full characterization of signal + known major backgrounds**

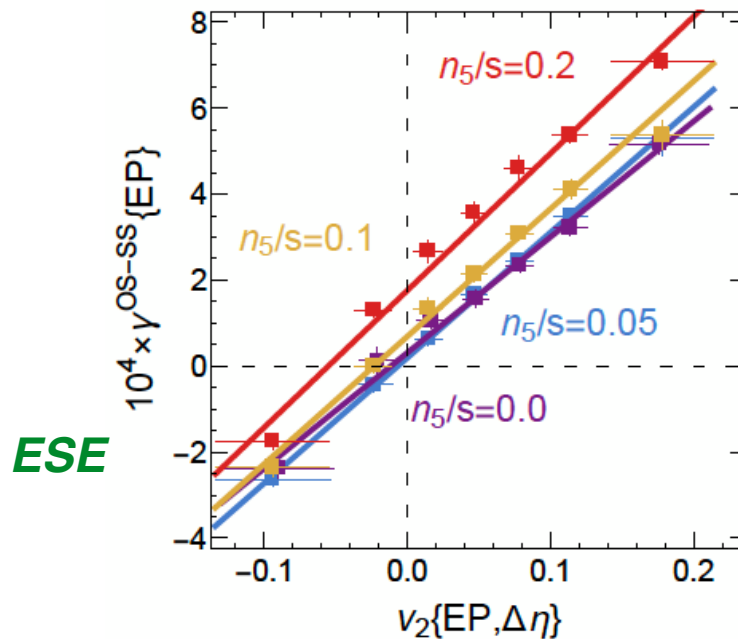
**[Shi, JL, et al, in prepration.]**

# EBE-AVFD for Testing Observables

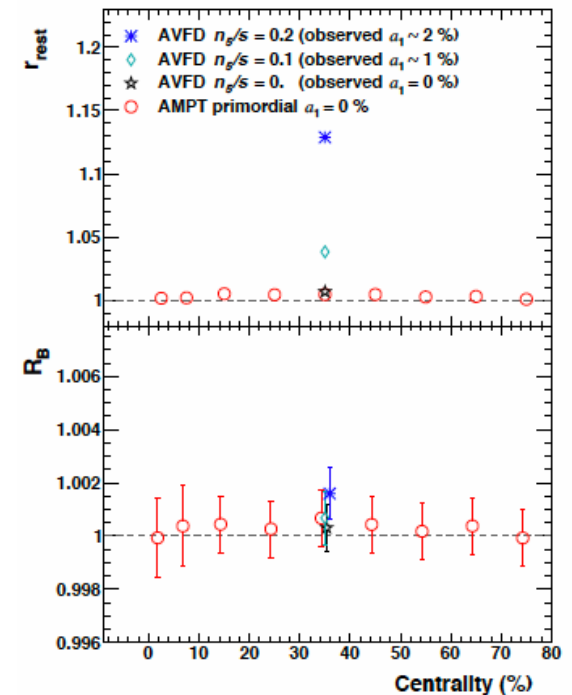


Lacey, Nagdy,  
 et al

Tang



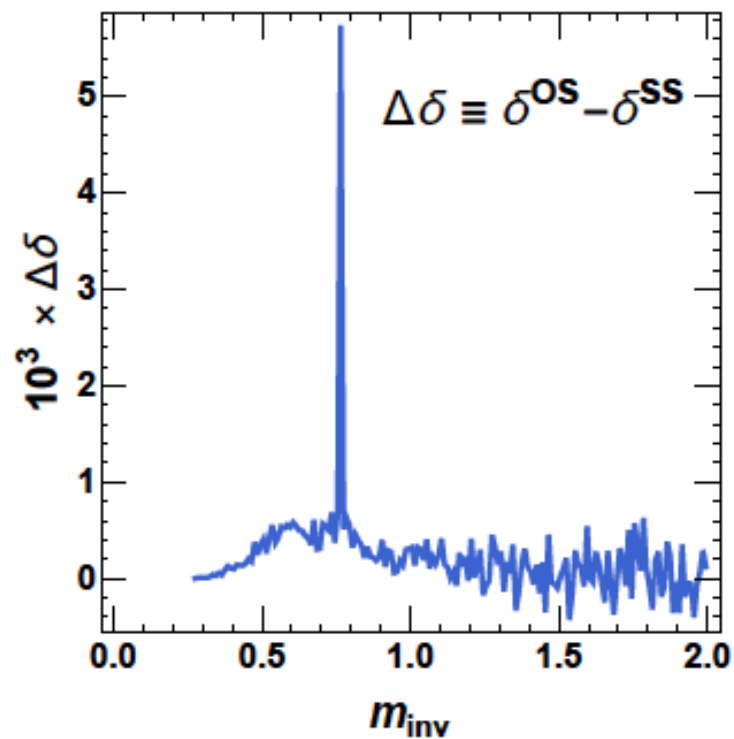
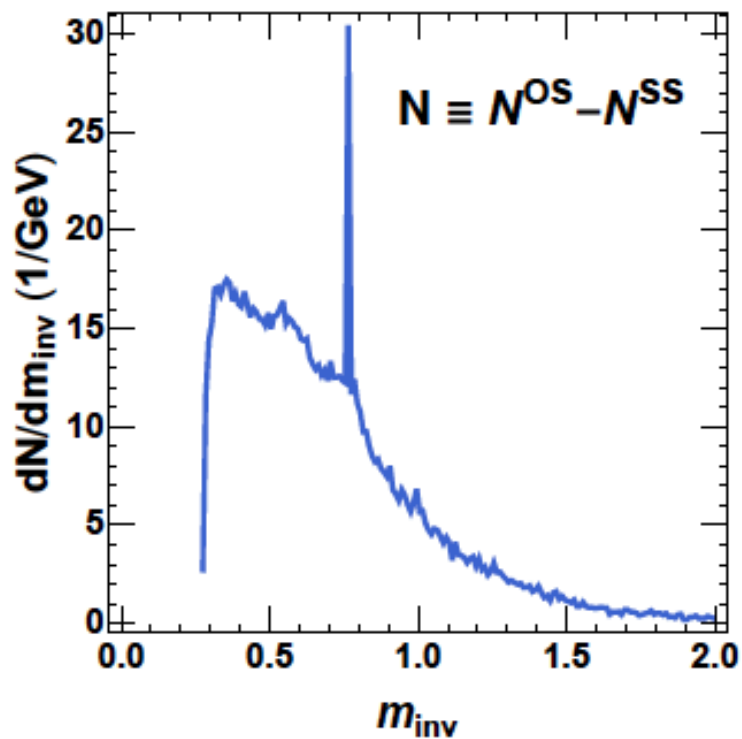
ESE



Now a key tool for understanding different observables' responses and sensitivity to signal and backgrounds

# EBE-AVFD for Testing Observables

## Invariant mass methods



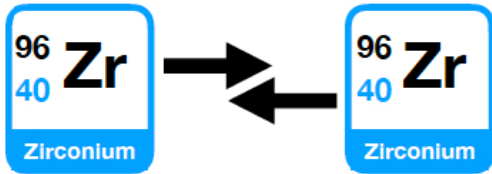
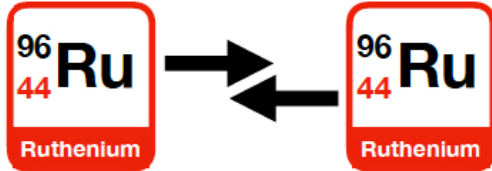
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# Isobaric Collision

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# A Decisive Experiment: Isobaric Collisions

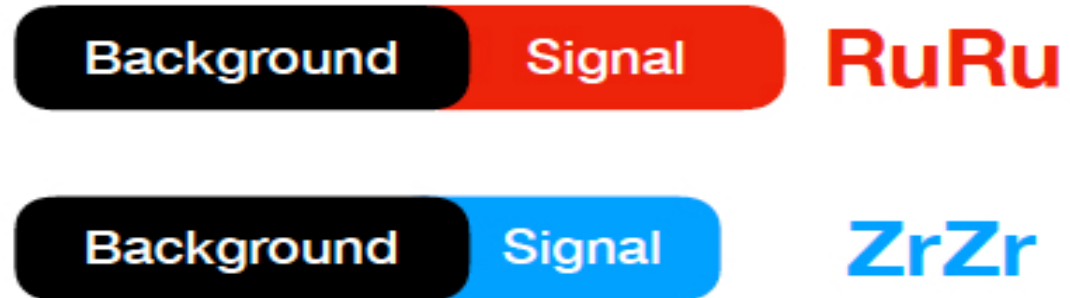
*New opportunity of potential discovery: Isobaric Collision @ RHIC*



[Koch, et al, arXiv: 1608.00982]

***Charge Asymmetry  
Correlation Measurement***

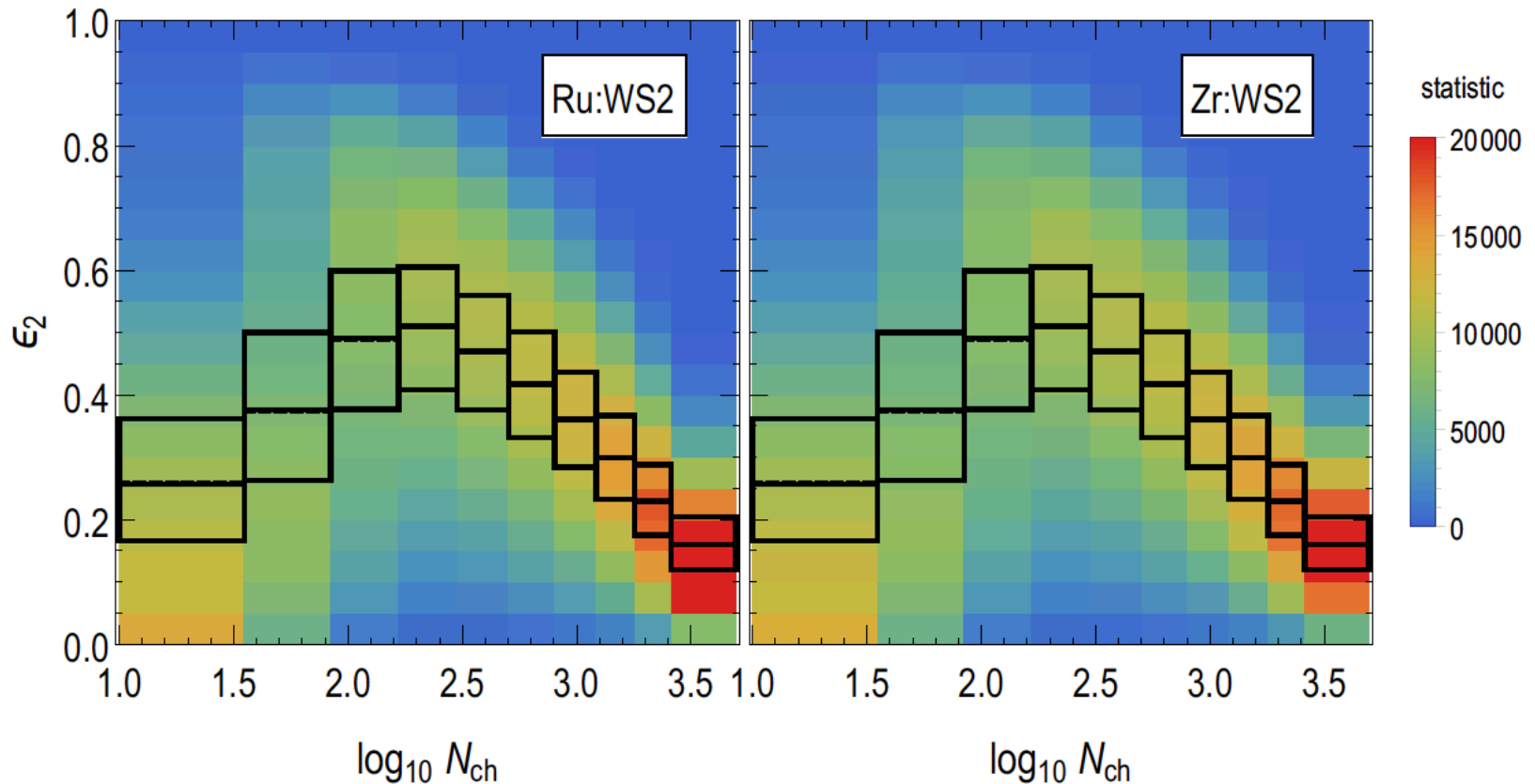
***Key idea: contrasting  
two systems with  
identical bulk,  
varied magnetic fields.***



***~2 billion data collected successfully in RHIC 2018 run;  
processing and analysis underway!***



# Isobars: How to Choose Identical Systems?

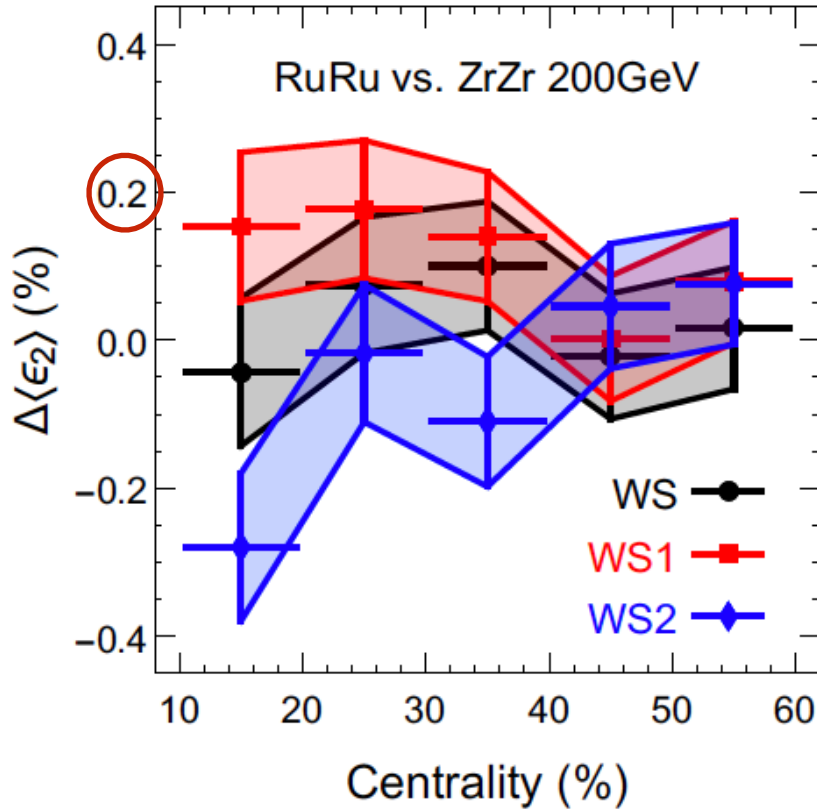


***Insight from initial conditions:  
joint cut on Multiplicity-Eccentricity***

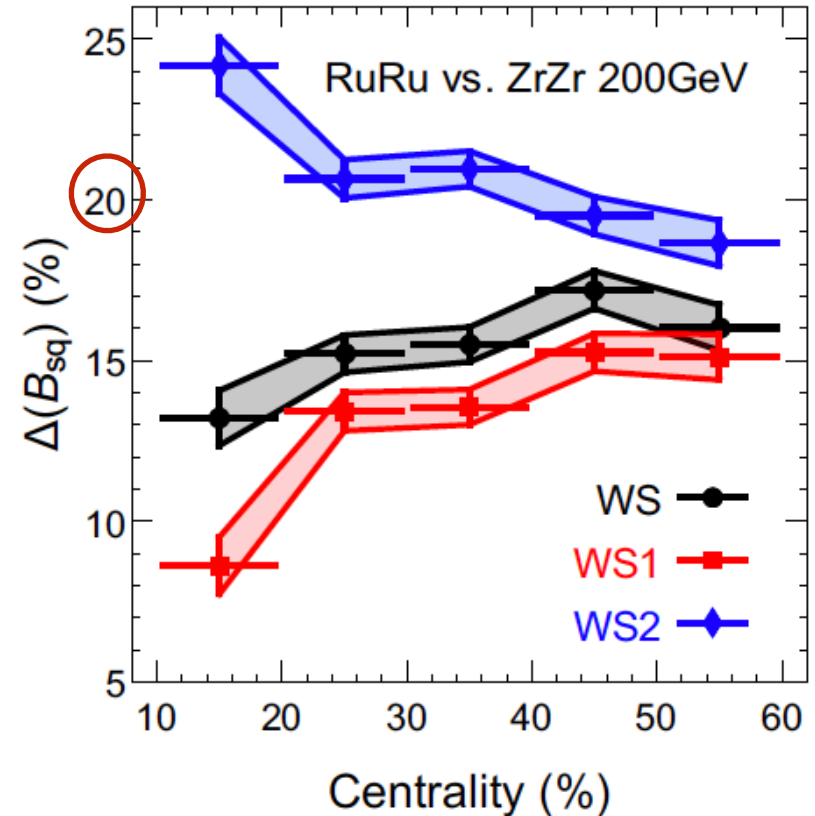
***[Shi, Zhang, Hou, JL, arXiv:1807.05604; paper in preparation]***

# Isobars: How to Choose Identical Systems?

**Eccentricity is guaranteed the same!**

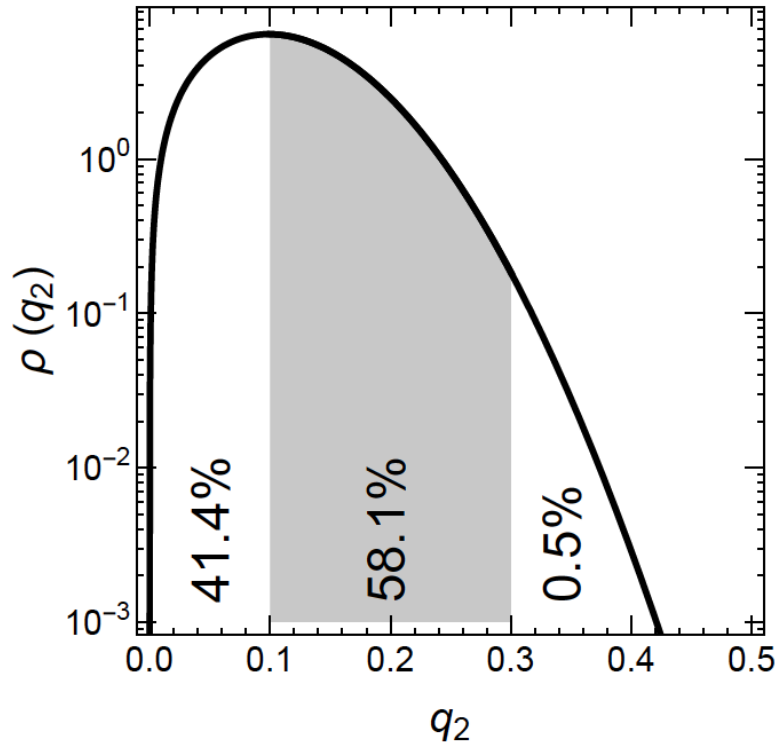


**B field differs by 12~20% !**



**Joint multiplicity-geometry cut:  
Vanishing difference in bulk properties,  
Sizable difference in magnetic fields!!!**

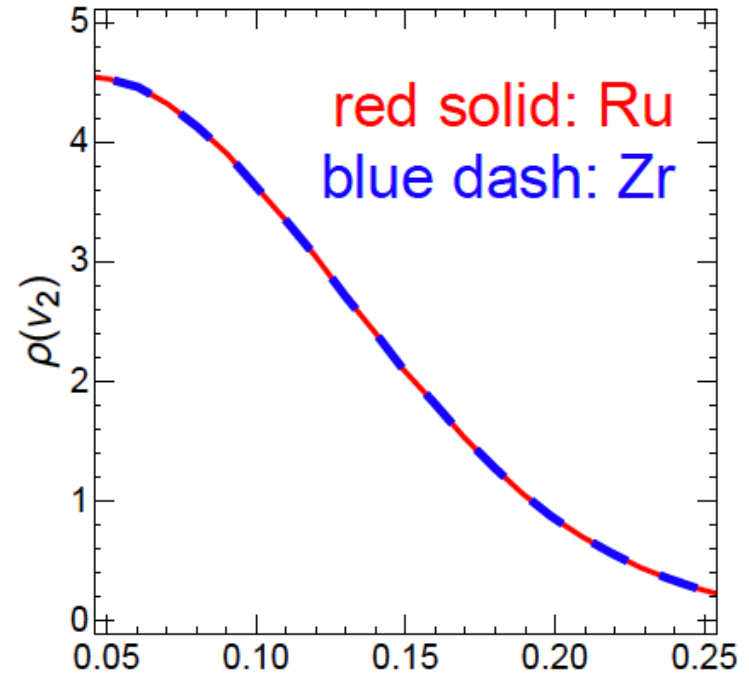
# Analyzing Actual EBE-AVFD Events for Isobars



**Millions of EBE-AVFD events:  
Subject to joint-cut**

$$64 < N_{\text{ch}, |y| < 1} < 96$$

$$0.1 < q_2 < 0.3$$



**Post-selection  
double-check:  
Identical  $v_2$  !**

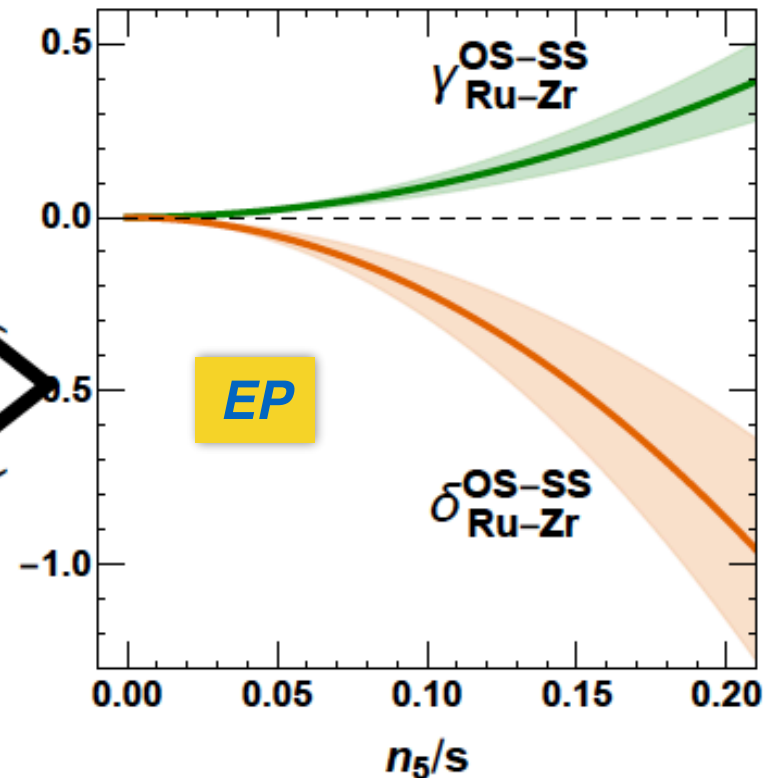
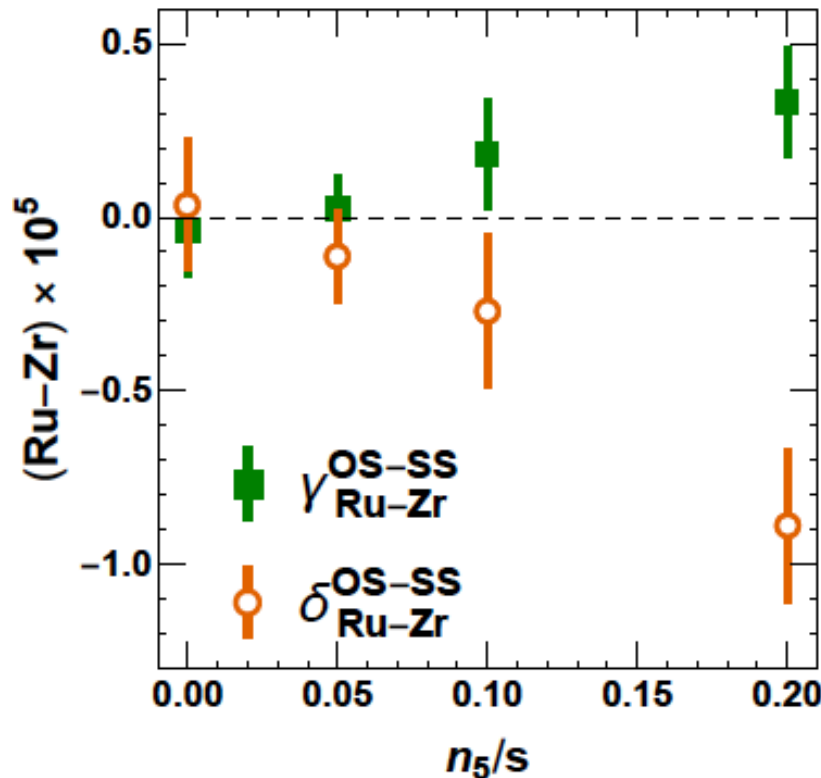
***Guaranteed to have two  
identical sample of isobar  
events for contrast!***

# $-1 < \eta < 1$ AVFD Predictions for Isobars

$64 < N_{\text{ch}} < 96$

$0.05 < v_2^{\text{ref}} < 0.25$

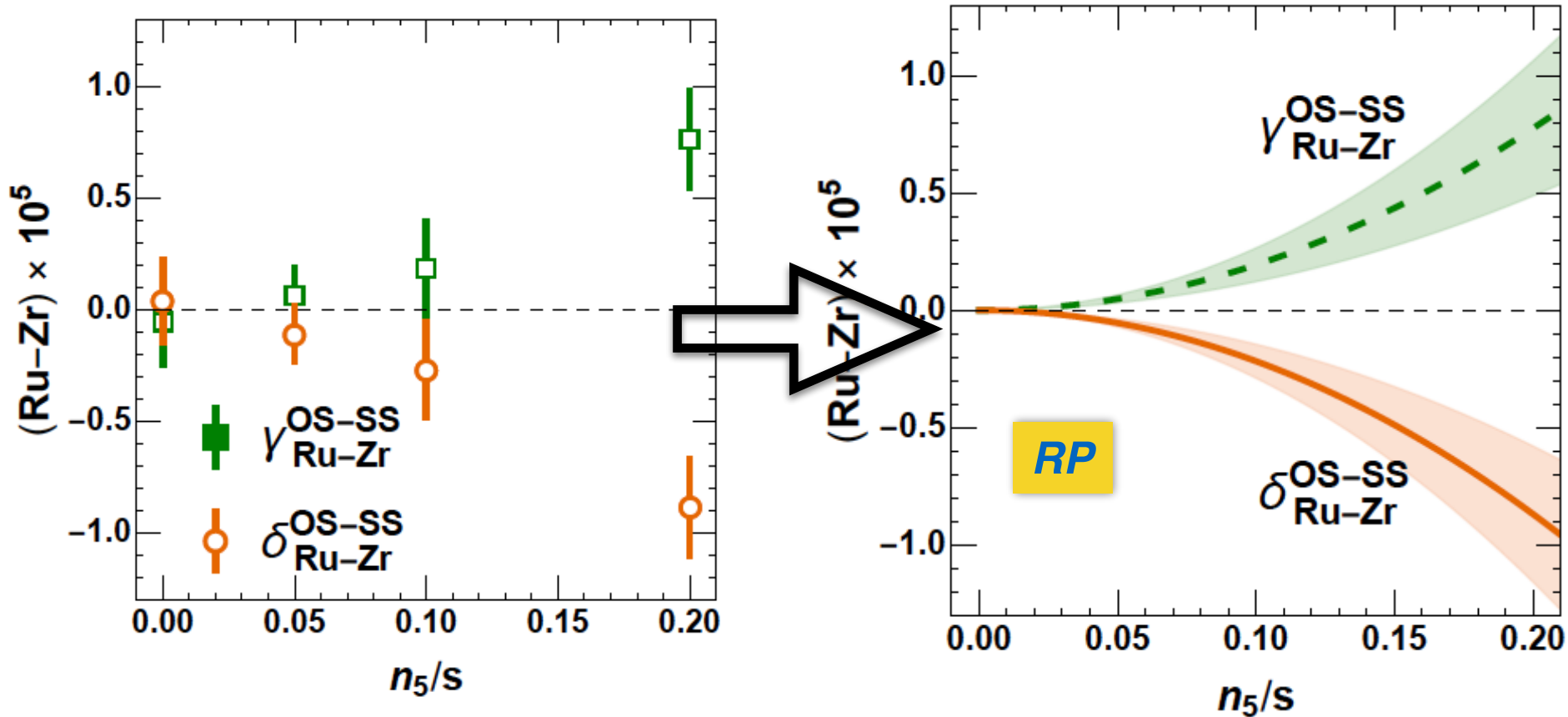
Statistics:  $10^7$  events in AVFD simulation  
 $\sim 3 \times 10^8$  events in experiment



**Look for absolute difference between isobars (after joint-cut)!**  
**Look for consistency between delta- and gamma-correlators!**

[Shi, Zhang, Hou, JL, arXiv:1807.05604; paper in preparation]

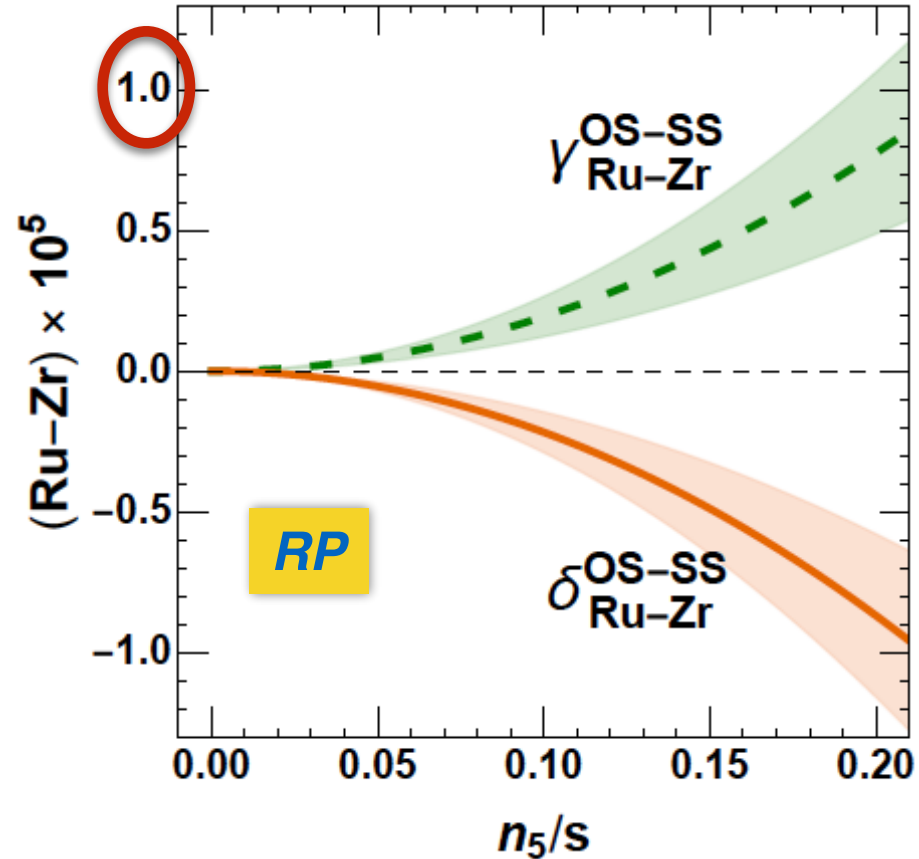
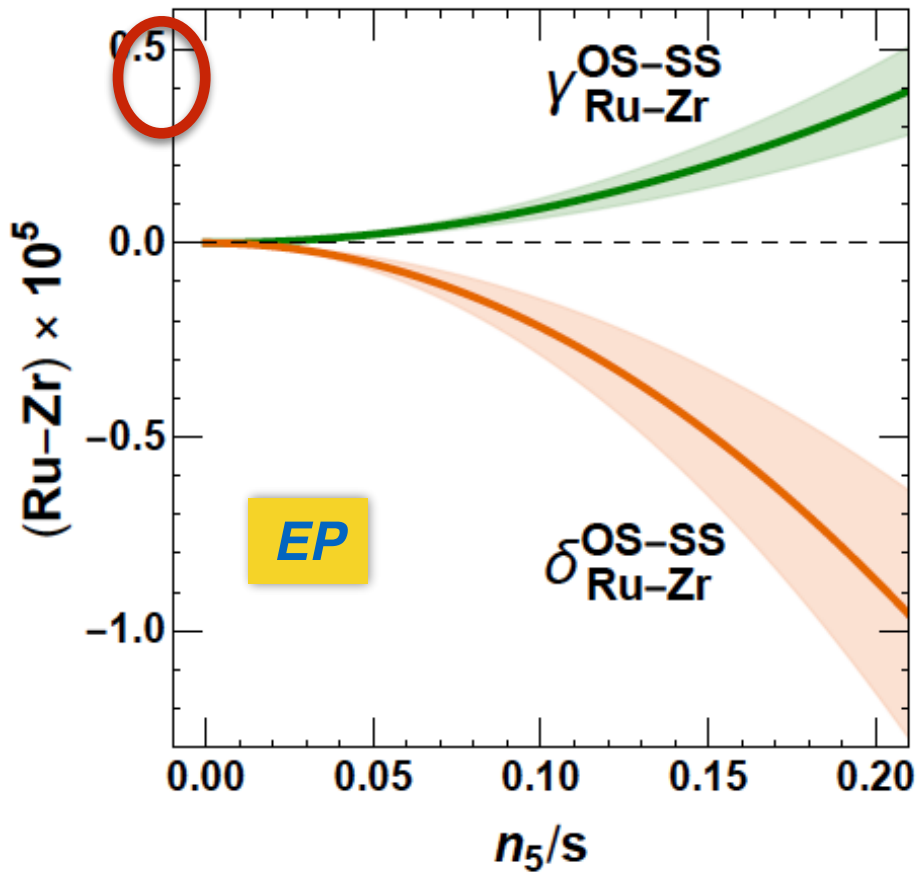
# AVFD Predictions for Isobars



**Look for absolute difference between isobars (after joint-cut)!**  
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[Shi, Zhang, Hou, JL, arXiv:1807.05604; paper in preparation]

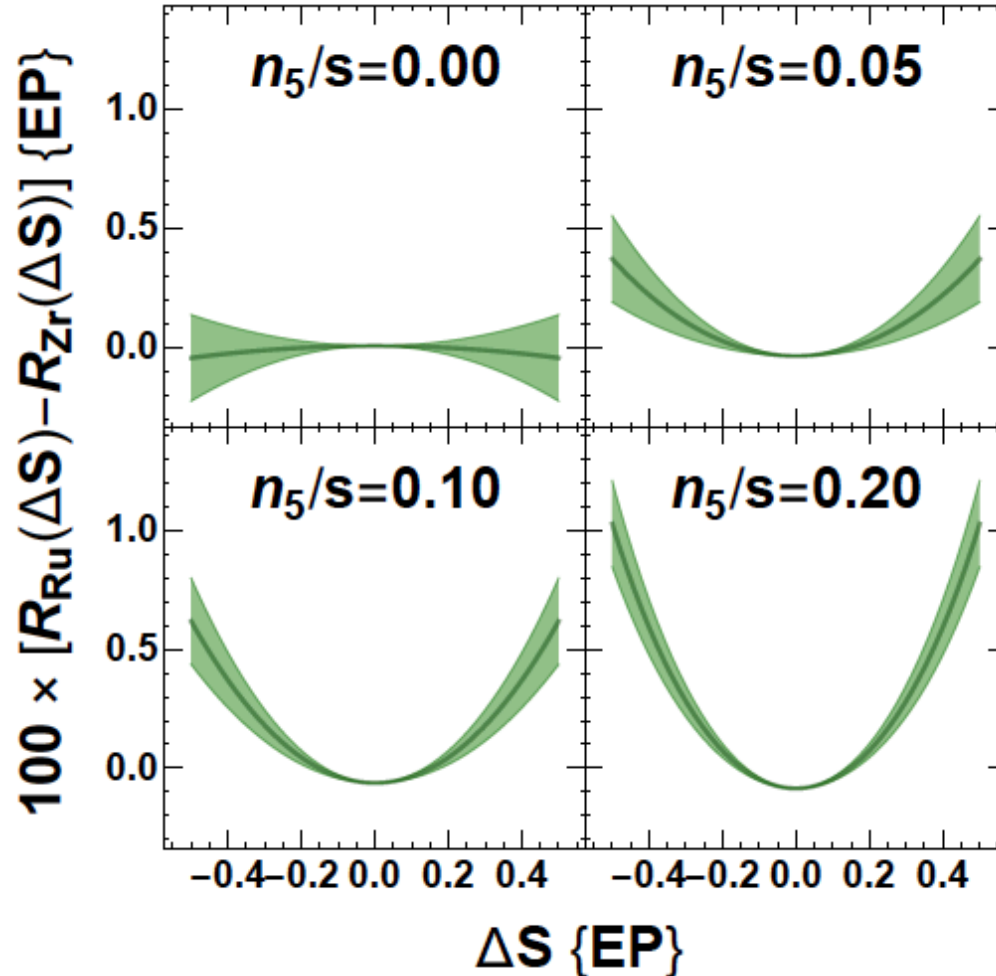
# AVFD Predictions for Isobars



**Look for absolute difference between isobars (after joint-cut)!**  
**Look for contrast between EP / RP!**

[Shi, Zhang, Hou, JL, arXiv:1807.05604; paper in preparation]

# AVFD Predictions for Isobars



***Look for absolute difference between isobars (after joint-cut)!***  
***Look for R-correlator shape!***

*[Shi, Zhang, Hou, JL, arXiv:1807.05604; paper in preparation]*

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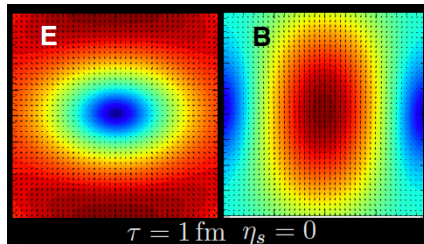
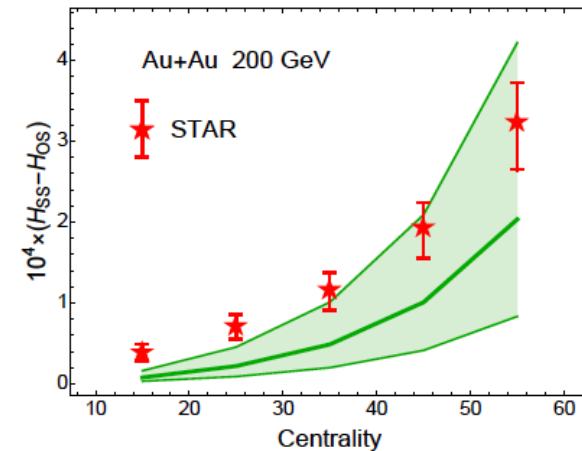
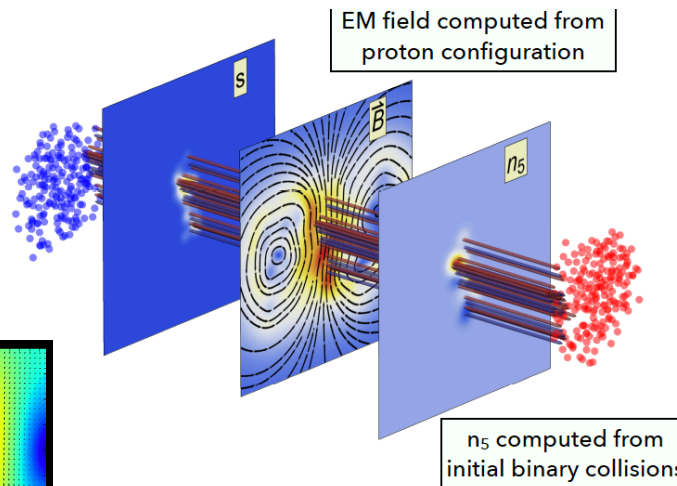
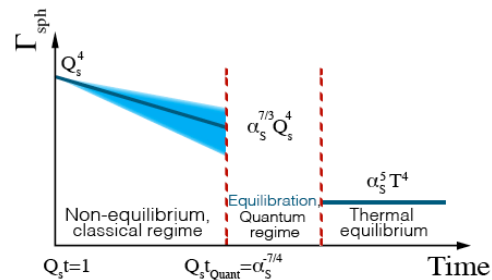
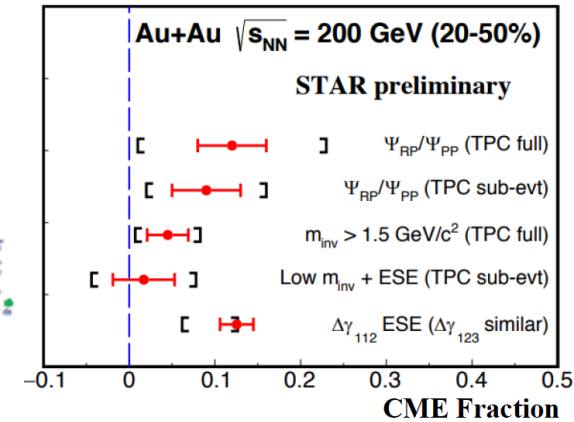
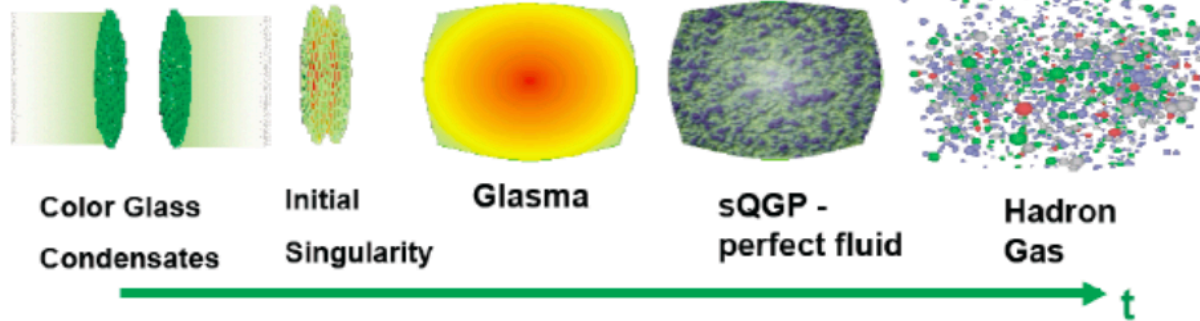
# Summary & Outlook

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# Summary: Toward Synergy of Key Ingredients

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$



**An exciting time:  
things are converging!**

# Outlook: Isobaric Collisions

**Charge Asymmetry  
Correlation Measurement**

Background

Signal

**RuRu**

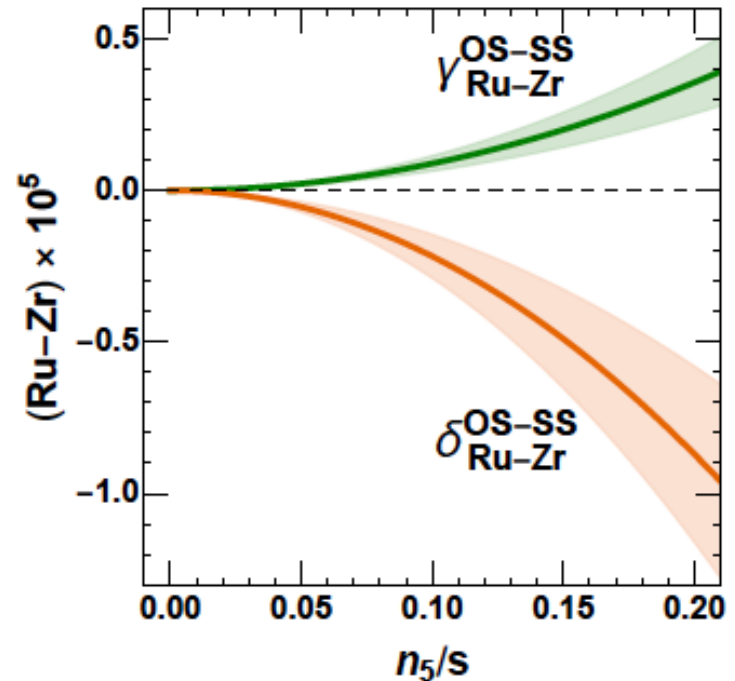
Background

Signal

**ZrZr**

- **Many observables: consistency?**
- **Very important: understanding observables & their relations!!**
- **Use sophisticated modeling tools (signal+bkg.) to help**

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$



**Exciting time(~2020): Stay tuned!**