



Tel Aviv University
特拉维夫大学

Exotics with Heavy Quarks

Marek Karliner, Tel Aviv University
based on joint work with Jon Rosner

CEPC Workshop, PKU, Beijing, July 2 2019

5 narrow exotic states close to meson-meson thresholds

state	mass MeV	width MeV	$\bar{Q}Q$ decay mode	phase space MeV	nearby threshold	ΔE MeV
$X(3872)$	3872	< 1.2	$J/\psi \pi^+ \pi^-$	495	$\bar{D}D^*$	< 1
$Z_b(10610)$	10608	21	$\Upsilon \pi$	1008	$\bar{B}B^*$	2 ± 2
$Z_b(10650)$	10651	10	$\Upsilon \pi$	1051	\bar{B}^*B^*	2 ± 2
$Z_c(3900)$	3900	24 – 46	$J/\psi \pi$	663	$\bar{D}D^*$	24
$Z_c(4020)$	4020	8 – 25	$J/\psi \pi$	783	\bar{D}^*D^*	6
\times					$\bar{D}D$	
\times					$\bar{B}B$	

- masses and widths approximate
- quarkonium decays mode listed have max phase space
- offset from threshold for orientation only, v. sensitive to exact mass

The Z_Q resonances decay into

$$\bar{Q}Q\pi$$

\implies must contain both $\bar{Q}Q$ and $\bar{q}q$, $q = u, d$

\implies manifestly exotic

$X(3872)$: a mixture of $\bar{D}D^*$ and $\chi_{c1}(2P)$

tetraquarks or a “hadronic molecules” ?

The molecule idea has a long history:

Voloshin Okun (1976),

de Rujula, Georgi Glashow (1977)

Tornqvist, Z. Phys. C61,525 (1993)

all states close to two-meson thresholds

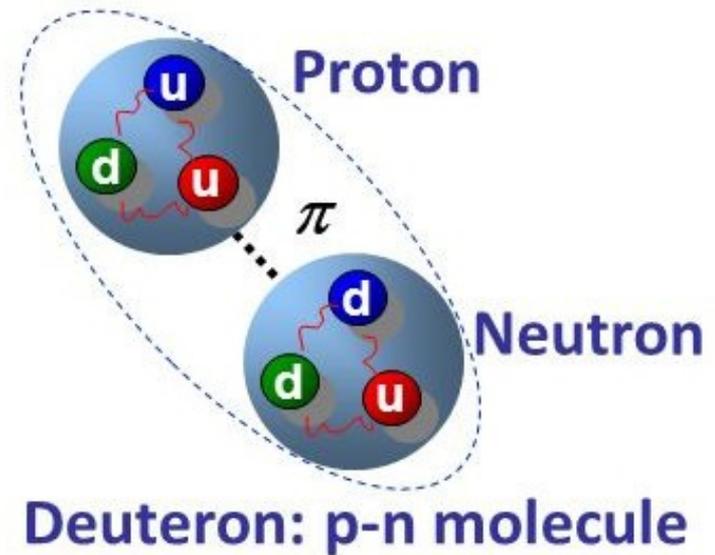
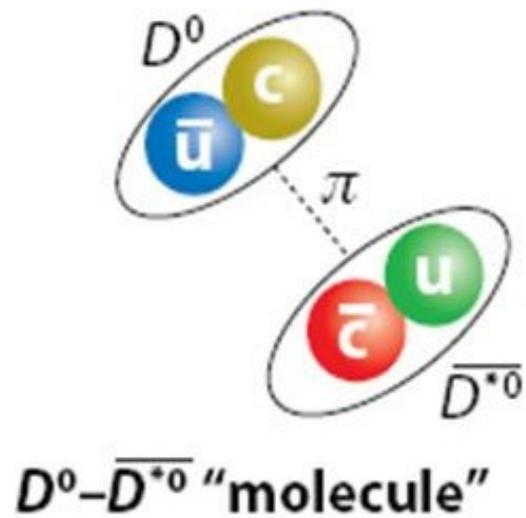
despite large phase space (hundreds of MeV)

narrow widths in decays into $\bar{Q}Q\pi$

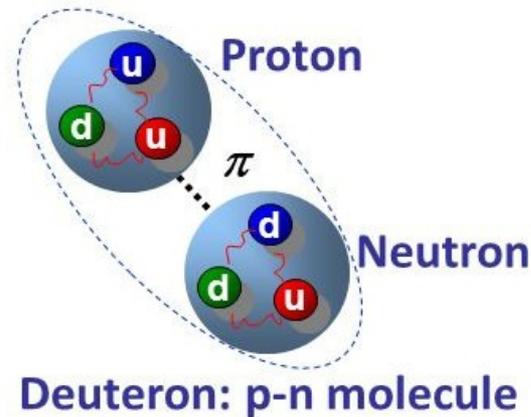
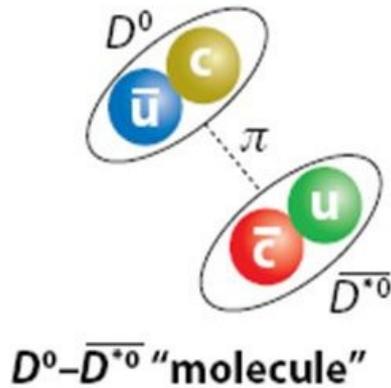
\implies very small overlap of wave functions: $|\langle i|f\rangle|^2 \ll 1$

strong hint in favor of molecular interpretation

Hadronic molecules: deuteron-like



Hadronic molecules: deuteron-like

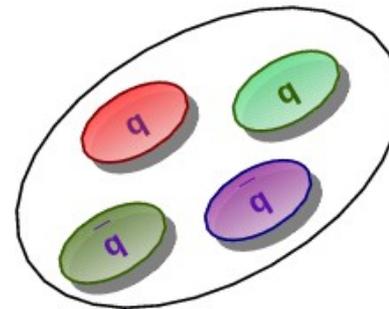
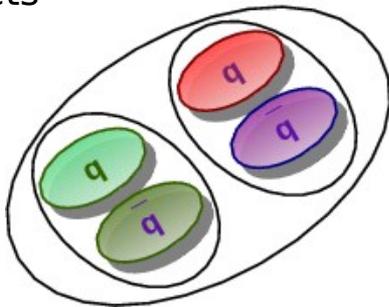


Tetraquarks: same 4 quarks, but tightly bound:

Hadronic Molecule

Tetraquark

two color singlets attract through residual forces



each quark sees color charges of all the other quarks

Belle, PRL 116, 212001 (2016):

$$\frac{\Gamma(Z_b(10610) \rightarrow \bar{B}B^*)}{\Gamma(Z_b(10610) \rightarrow \Upsilon(1S)\pi)} \approx \frac{86\%}{0.54\%} = \mathcal{O}(100)$$

despite 1000 MeV of phase space

for $\Upsilon(1S)\pi$ vs few MeV for $\bar{B}B^*$!

overlap of Z_c wave function with $J/\psi\pi$

much smaller than with $\bar{D}D \Rightarrow$ indicates an extended object

also

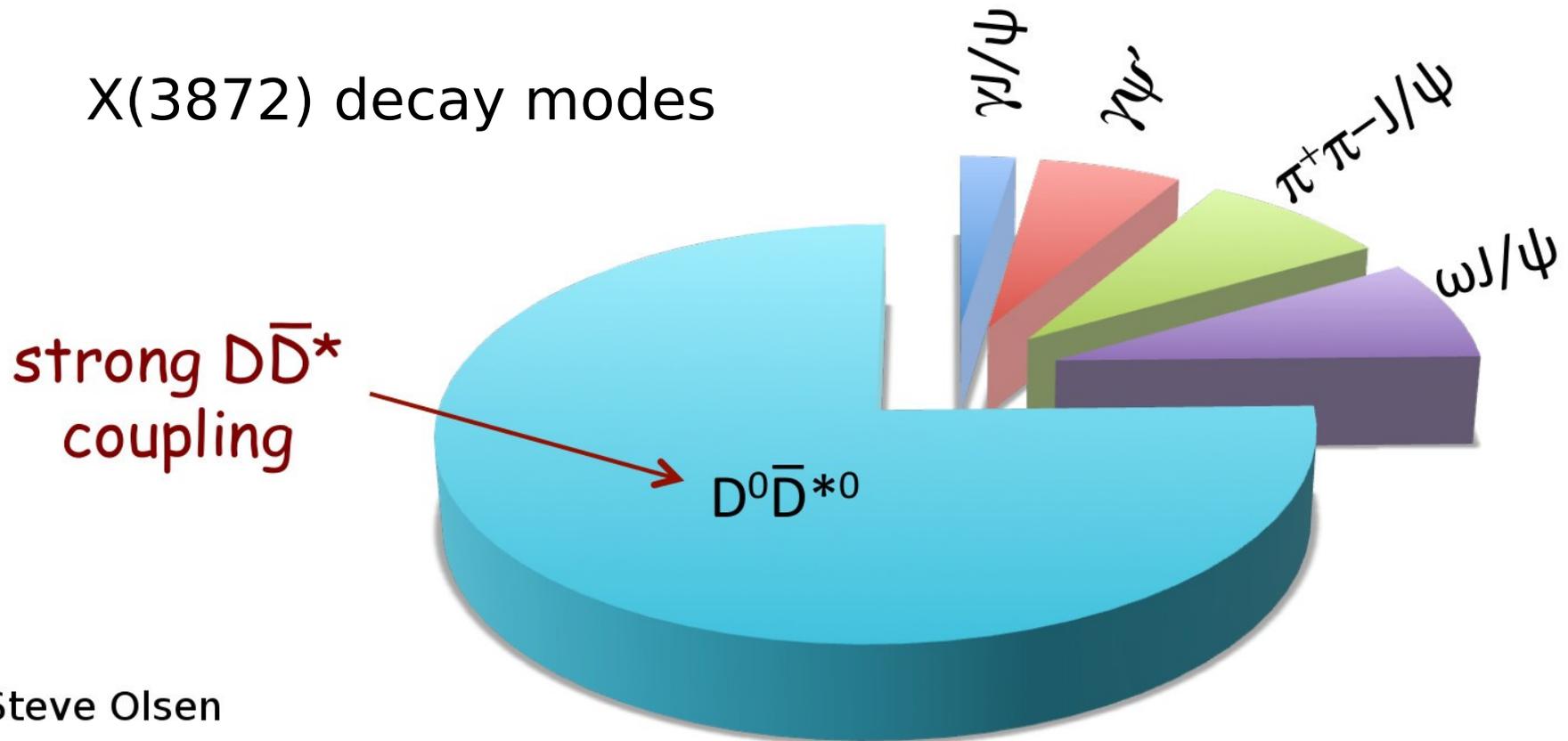
$$\frac{\Gamma(Z_c(3885) \rightarrow \bar{D}D^*)}{\Gamma(Z_c(3885) \rightarrow J/\psi\pi)} = 6.2 \pm 1.1 \pm 2.7$$

(BESIII/Yu-Ping Guo @EQCD, Jinan 6/2015)

BR-s of $X(3872)$ to J/ψ and pions vs “fall apart” mode $\bar{D}D^*$

$$\text{BR}(\bar{D}D^*) \gg \text{BR}(J/\psi + X)$$

$X(3872)$ decay modes



Steve Olsen

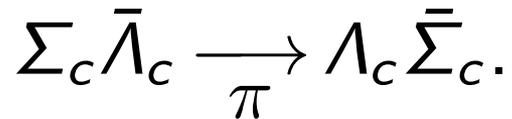
4 pieces of experimental evidence in support of molecular interpretation of Z_Q and $X(3872)$:

1. masses near thresholds and J^P of S-wave
2. narrow width despite very large phase space
3. $\text{BR}(\text{fall apart mode}) \gg \text{BR}(\text{quarkonium} + X)$
4. no states which require binding through 3 pseudoscalar coupling

necessary* conditions for existence of a resonance

(a) both hadrons heavy, as $E_{kin} \sim 1/\mu_{RED}$

(b) both couple to pions;
one of them can have $l = 0$, e.g.



(c) $\Gamma(h_1) + \Gamma(h_2) \ll \Gamma(\text{molecule})$

* may not be sufficient

the binding mechanism can in principle
apply to any two heavy hadrons
which couple to isospin
and satisfy these conditions,
be they mesons or baryons

doubly-heavy hadronic molecules:

most likely candidates with $Q\bar{Q}'$, $Q = c, b$, $\bar{Q}' = \bar{c}, \bar{b}$:

$D\bar{D}^*$, $D^*\bar{D}^*$, D^*B^* , $\bar{B}B^*$, \bar{B}^*B^* ,

$\Sigma_c\bar{D}^*$, $\Sigma_c B^*$, $\Sigma_b\bar{D}^*$, $\Sigma_b B^*$, **the lightest of new kind**

$\Sigma_c\bar{\Sigma}_c$, $\Sigma_c\bar{\Lambda}_c$, $\Sigma_c\bar{\Lambda}_b$, $\Sigma_b\bar{\Sigma}_b$, $\Sigma_b\bar{\Lambda}_b$, and $\Sigma_b\bar{\Lambda}_c$.

$c\bar{c}$ and $b\bar{b}$ states decay strongly to $\bar{c}c$ or $\bar{b}b$ and $\pi^-(s)$

$b\bar{c}$ and $c\bar{b}$ states decay strongly to B_c^\pm and $\pi^-(s)$

QQ' candidates – dibaryons:

$\Sigma_c\Sigma_c$, $\Sigma_c\Lambda_c$, $\Sigma_c\Lambda_b$, $\Sigma_b\Sigma_b$, $\Sigma_b\Lambda_b$, and $\Sigma_b\Lambda_c$.

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like a whole new periodic table

prediction of doubly heavy baryon with hidden charm:

$$\Sigma_c \bar{D}^* \equiv \Theta_{\bar{c}c}, \quad m_{\Theta_{\bar{c}c}} \approx 4460 \text{ MeV},$$

possible decay mode: $\Theta_{cc} \rightarrow J/\psi p$

$(S_1 \cdot S_2) (l_1 \cdot l_2)$ interaction: $l = 1/2 \rightarrow J = 3/2$

S-wave $\rightarrow J^P = 3/2^-$

small overlap of molecular state with $J/\psi p$

\Rightarrow narrow width \lesssim few tens of MeV

despite > 400 MeV phase space

$\Theta_{\bar{c}c}$ minimal quark content: $\bar{c}c uud$

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$\Theta_{\bar{c}c}$ minimal quark content: $\bar{c}c uud \equiv P_c(4450)$

a molecule, not a tightly-bound pentaquark

Thresholds for $Q\bar{Q}'$ molecular states

Channel	Minimum isospin	Minimal quark content ^{a,b}	Threshold (MeV) ^c	Example of decay mode
$D\bar{D}^*$	0	$c\bar{c}q\bar{q}$	3875.8	$J/\psi \pi\pi$
$D^*\bar{D}^*$	0	$c\bar{c}q\bar{q}$	4017.2	$J/\psi \pi\pi$
D^*B^*	0	$c\bar{b}q\bar{q}$	7333.8	$B_c^+ \pi\pi$
$\bar{B}B^*$	0	$b\bar{b}q\bar{q}$	10604.6	$\Upsilon(nS)\pi\pi$
\bar{B}^*B^*	0	$b\bar{b}q\bar{q}$	10650.4	$\Upsilon(nS)\pi\pi$
$\Sigma_c\bar{D}^*$	1/2	$c\bar{c}qqq'$	4462.4	$J/\psi p$
$\Sigma_c B^*$	1/2	$c\bar{b}qqq'$	7779.5	$B_c^+ p$
$\Sigma_b\bar{D}^*$	1/2	$b\bar{c}qqq'$	7823.0	$B_c^- p$
$\Sigma_b B^*$	1/2	$b\bar{b}qqq'$	11139.6	$\Upsilon(nS)p$
$\Sigma_c\bar{\Lambda}_c$	1	$c\bar{c}qq' \bar{u}\bar{d}$	4740.3	$J/\psi \pi$
$\Sigma_c\bar{\Sigma}_c$	0	$c\bar{c}qq' \bar{q}\bar{q}'$	4907.6	$J/\psi \pi\pi$
$\Sigma_c\bar{\Lambda}_b$	1	$c\bar{b}qq' \bar{u}\bar{d}$	8073.3 ^d	$B_c^+ \pi$
$\Sigma_b\bar{\Lambda}_c$	1	$b\bar{c}qq' \bar{u}\bar{d}$	8100.9 ^d	$B_c^- \pi$
$\Sigma_b\bar{\Lambda}_b$	1	$b\bar{b}qq' \bar{u}\bar{d}$	11433.9	$\Upsilon(nS)\pi$
$\Sigma_b\bar{\Sigma}_b$	0	$b\bar{b}qq' \bar{q}\bar{q}'$	11628.8	$\Upsilon(nS)\pi\pi$

^aIgnoring annihilation of quarks.

^bPlus other charge states when $I \neq 0$.

^cBased on isospin-averaged masses.

^dThresholds differ by 27.6 MeV.

New Exotic Meson and Baryon Resonances from Doubly Heavy Hadronic Molecules

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We predict several new exotic doubly heavy hadronic resonances, inferring from the observed exotic bottomoniumlike and charmoniumlike narrow states $X(3872)$, $Z_b(10610)$, $Z_b(10650)$, $Z_c(3900)$, and $Z_c(4020/4025)$. We interpret the binding mechanism as mostly molecularlike isospin-exchange attraction between two heavy-light mesons in a relative S -wave state. We then generalize it to other systems containing two heavy hadrons which can couple through isospin exchange. The new predicted states include resonances in meson-meson, meson-baryon, baryon-baryon, and baryon-antibaryon channels. These include those giving rise to final states involving a heavy quark $Q = c, b$ and antiquark $\bar{Q}' = \bar{c}, \bar{b}$, namely, $D\bar{D}^*$, $D^*\bar{D}^*$, D^*B^* , $\bar{B}B^*$, \bar{B}^*B^* , $\Sigma_c\bar{D}^*$, $\Sigma_c B^*$, $\Sigma_b\bar{D}^*$, $\Sigma_b B^*$, $\Sigma_c\bar{\Sigma}_c$, $\Sigma_c\bar{\Lambda}_c$, $\Sigma_c\bar{\Lambda}_b$, $\Sigma_b\bar{\Sigma}_b$, $\Sigma_b\bar{\Lambda}_b$, and $\Sigma_b\bar{\Lambda}_c$, as well as corresponding S -wave states giving rise to QQ' or $\bar{Q}\bar{Q}'$.

DOI: 10.1103/PhysRevLett.115.122001

PACS numbers: 14.20.Pt, 12.39.Hg, 12.39.Jh, 14.40.Rt

Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays

R. Aaij *et al.**

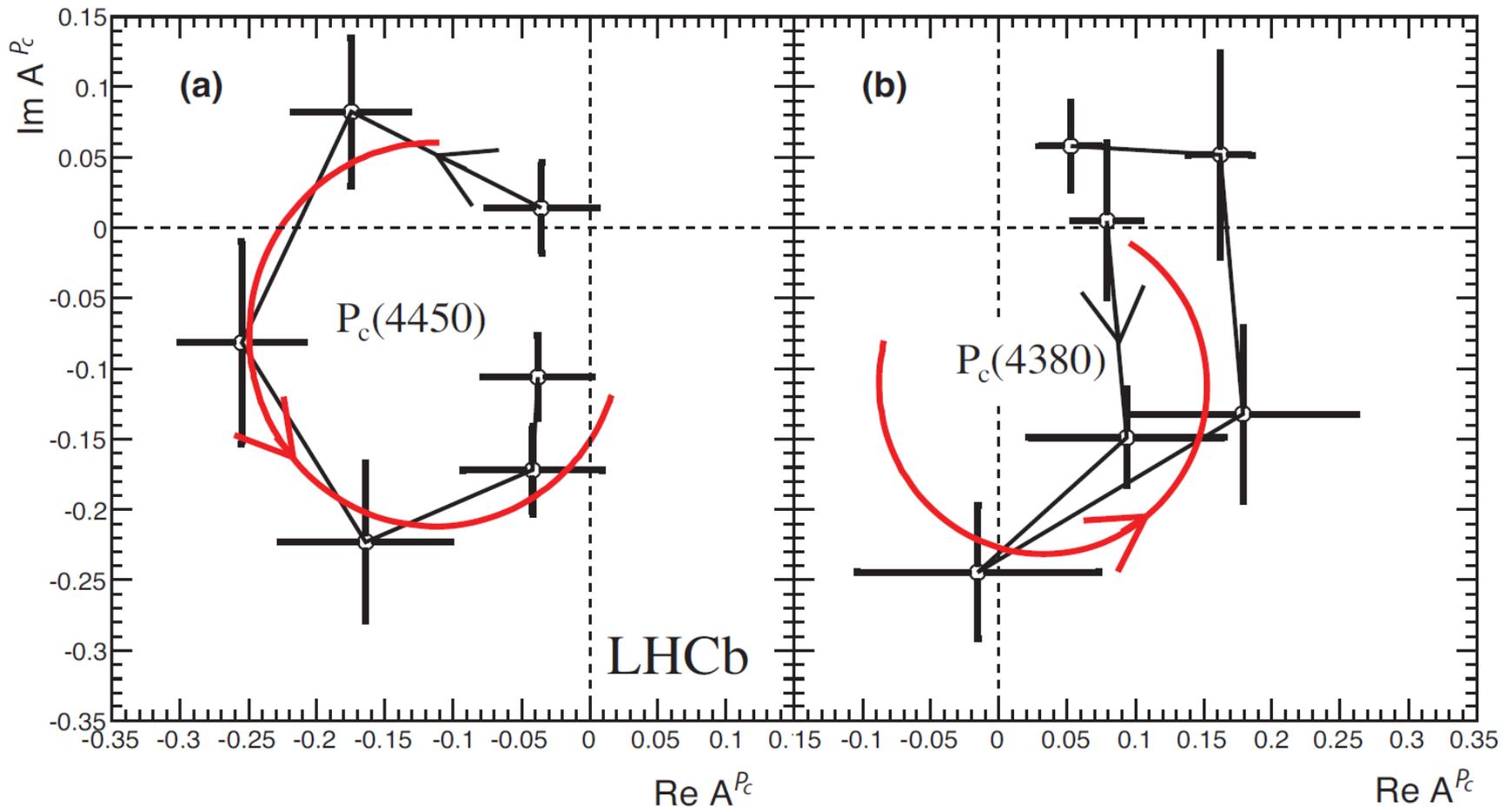
(LHCb Collaboration)

(Received 13 July 2015; published 12 August 2015)

Observations of exotic structures in the $J/\psi p$ channel, which we refer to as charmonium-pentaquark states, in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays are presented. The data sample corresponds to an integrated luminosity of 3 fb^{-1} acquired with the LHCb detector from 7 and 8 TeV pp collisions. An amplitude analysis of the three-body final state reproduces the two-body mass and angular distributions. To obtain a satisfactory fit of the structures seen in the $J/\psi p$ mass spectrum, it is necessary to include two Breit-Wigner amplitudes that each describe a resonant state. The significance of each of these resonances is more than 9 standard deviations. One has a mass of $4380 \pm 8 \pm 29 \text{ MeV}$ and a width of $205 \pm 18 \pm 86 \text{ MeV}$, while the second is narrower, with a mass of $4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ and a width of $39 \pm 5 \pm 19 \text{ MeV}$. The preferred J^P assignments are of opposite parity, with one state having spin $3/2$ and the other $5/2$.

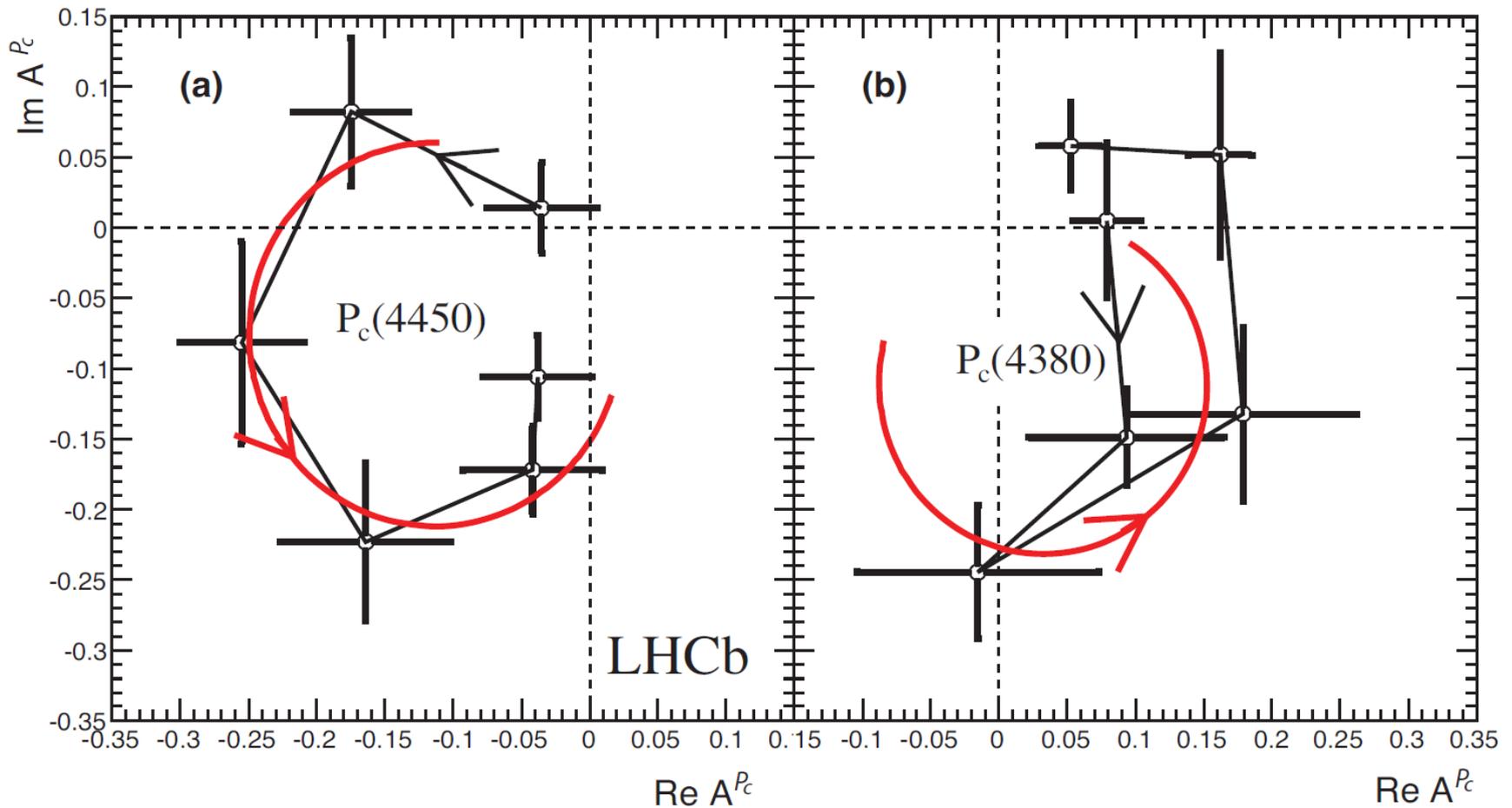
DOI: 10.1103/PhysRevLett.115.072001

PACS numbers: 14.40.Pq, 13.25.Gv



$P_c(4450)$: predicted,
 narrow: $\Gamma = 39 \pm 5 \pm 19$,
 10 MeV from $\Sigma_c \bar{D}^*$ threshold
 perfect Argand plot: a molecule

$P_c(4380)$: not predicted,
 wide: $\Gamma = 205 \pm 18 \pm 86$ MeV,
 Argand plot not resonance-like
 ???



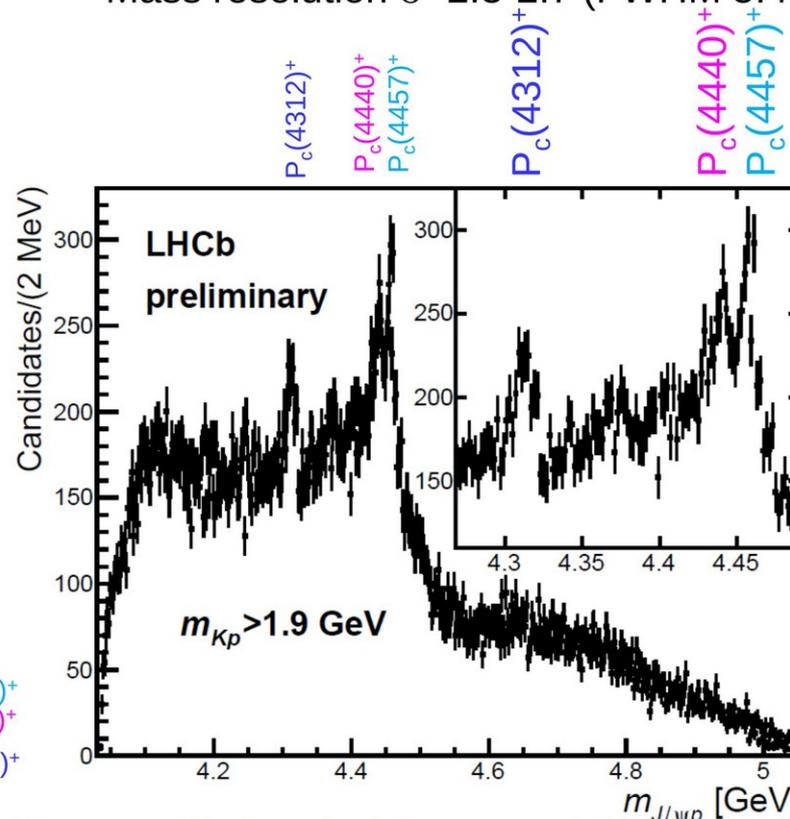
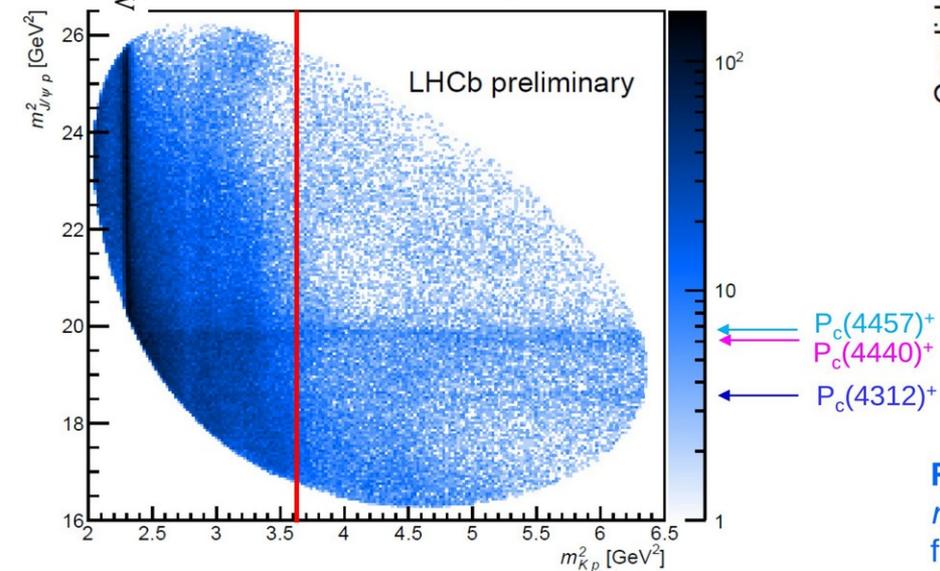
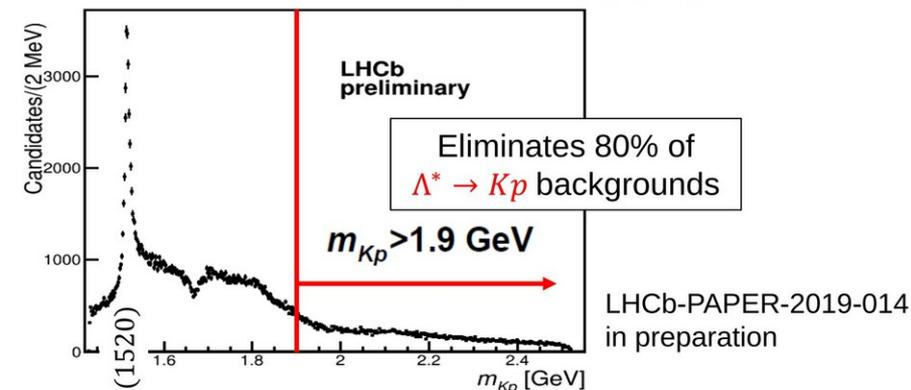
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 ???

$P_c(4450)$ might be just the first of many “heavy deuterons”

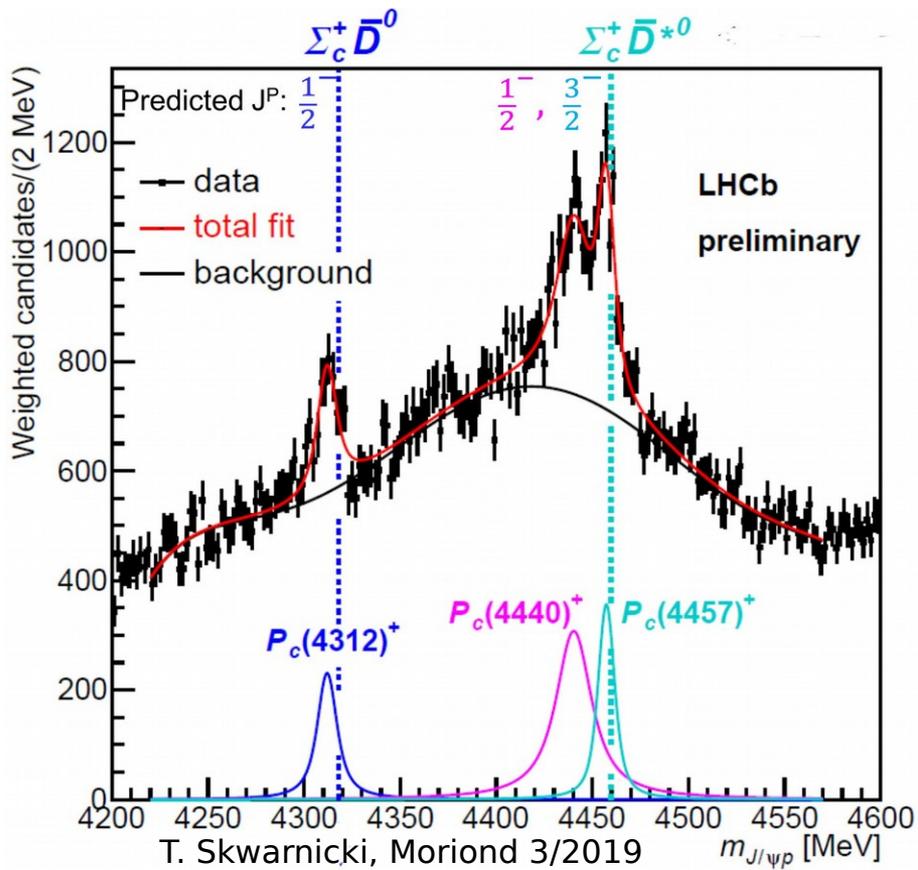
Narrow $P_c^+ \rightarrow J/\psi p$ peaks with Λ^* suppression

Mass resolution $\sigma=2.3\text{-}2.7$ (FWHM 5.4-6.4) MeV

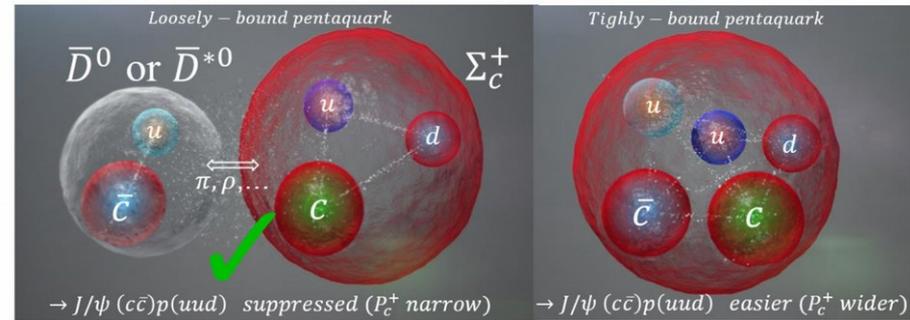


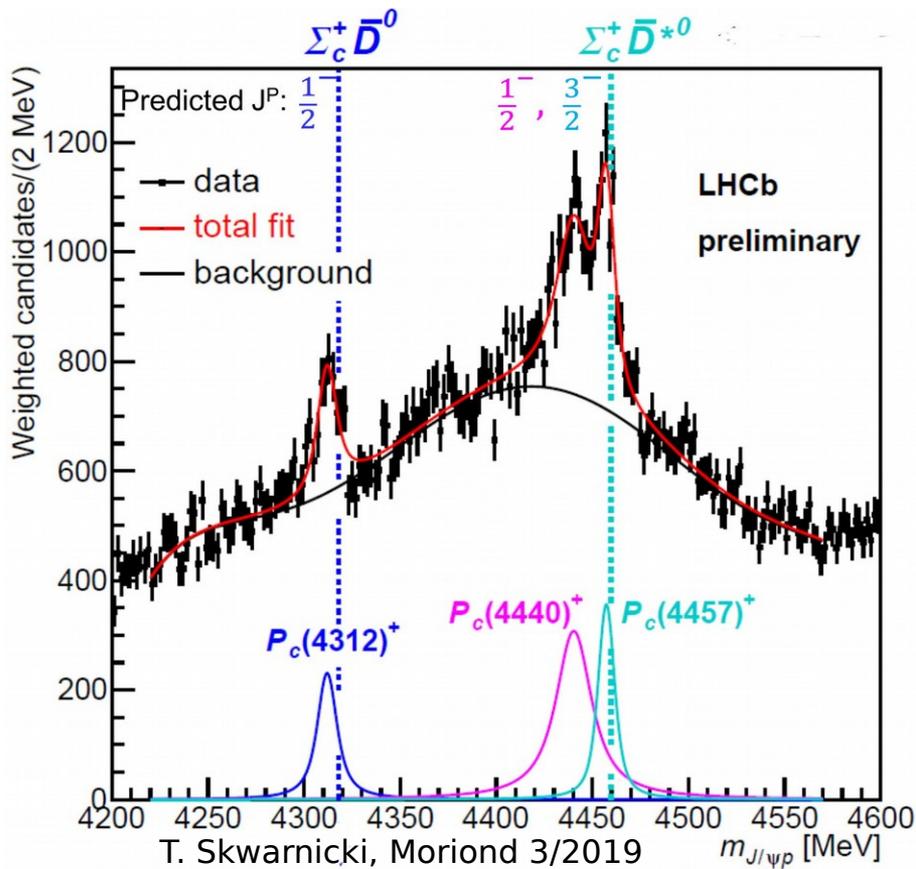
Proper amplitude analysis faces new challenges: must consider $m_{J/\psi p}$ resolution effects, large statistics and sub-percent precision in fit fractions required in the amplitude model – work in progress

State	M [MeV]	Γ [MeV]	(95% CL)	\mathcal{R} [%]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$	(< 27)	$0.30 \pm 0.07^{+0.34}_{-0.09}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$	(< 49)	$1.11 \pm 0.33^{+0.22}_{-0.10}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$	(< 20)	$0.53 \pm 0.16^{+0.15}_{-0.13}$

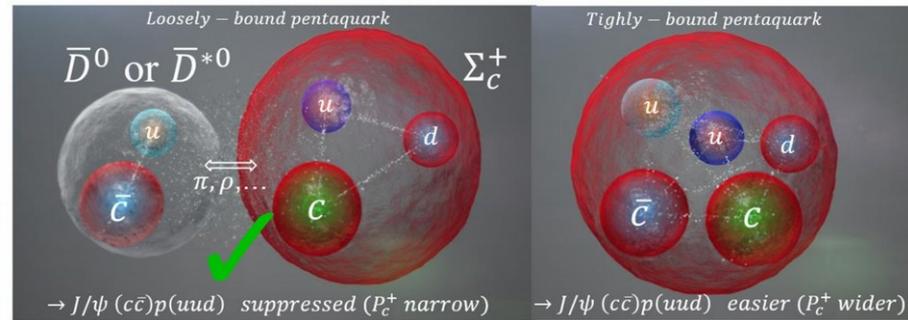


The near-threshold masses and the narrow widths of $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$ favor “molecular” pentaquarks with meson-baryon substructure!





The near-threshold masses and the narrow widths of $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$ favor “molecular” pentaquarks with meson-baryon substructure!



observe all 3 S-wave states:

$$\Sigma_c \bar{D}; \quad J^P = \frac{1}{2}^-$$

$$\Sigma_c \bar{D}^*; \quad J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

for $Q \rightarrow \infty$ 4 more S-wave states:

$$\Sigma_c^* \bar{D}; \quad J^P = \frac{3}{2}^-$$

$$\Sigma_c^* \bar{D}^*; \quad J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

Open Questions

- LHCb: new narrow states slightly below $\Sigma_c \bar{D}(\bar{D}^*)$ thresholds; highly suggestive of molecules

Several interesting issues:

- Additional 4 $\Sigma_c^* \bar{D}(\bar{D}^*)$ states ?
- Decay into $\Lambda_c \bar{D}$?
- So far no signal in $\gamma p \rightarrow J/\psi p$ photoproduction
- If $P_c(4312)$ $\Sigma_c \bar{D}$ molecule, why no $D\bar{D}$ molecule?
- $X(3872) \ll 1$ MeV from $\bar{D}D^*$ threshold
 Z_b -s ~ 2 MeV from $\bar{B}B^*$, \bar{B}^*B^*
deuteron 2.2 MeV below pn
so why are P_c -s 5 ÷ 22 MeV below $\Sigma_c \bar{D}(\bar{D}^*)$?
- $P_c(4440)$ and $P_c(4457)$: likely $\Sigma_c \bar{D}^*$, $S = \frac{1}{2}, \frac{3}{2}$
17 MeV spin splitting \gg deuteron ($S=1$) vs. pn $S=0$
- lattice ?

Test via photoproduction

MK & J. Rosner, arXiv:1508.01496

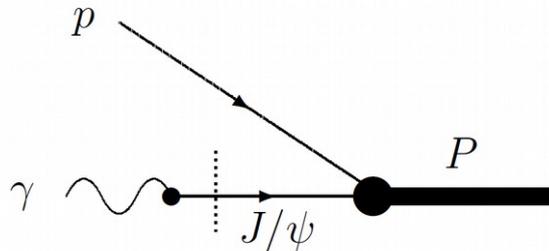
Q. Wang, X. H. Liu and Q. Zhao, arXiv:1508.00339

V. Kubarovsky and M. B. Voloshin, arXiv:1508.00888

LHCb: new exotic resonances in $J/\psi p$ channel:

\implies natural candidates for photoproduction

- estimate $\sigma(\gamma p \rightarrow P_c \rightarrow J/\psi p)$ from vector dominance:



- $E_\gamma = 10 \text{ GeV} \implies$ CLAS12 & GlueX @JLab & ...

- $\sigma \sim 50 \text{ nb} \gg \sigma_{\text{diffractive}} \sim 1 \text{ nb}$

Test via photoproduction

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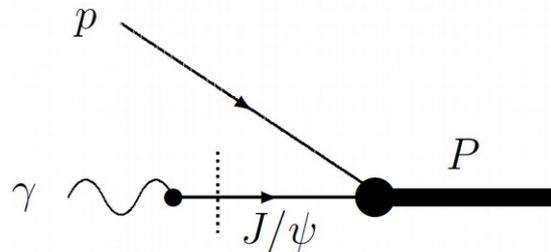
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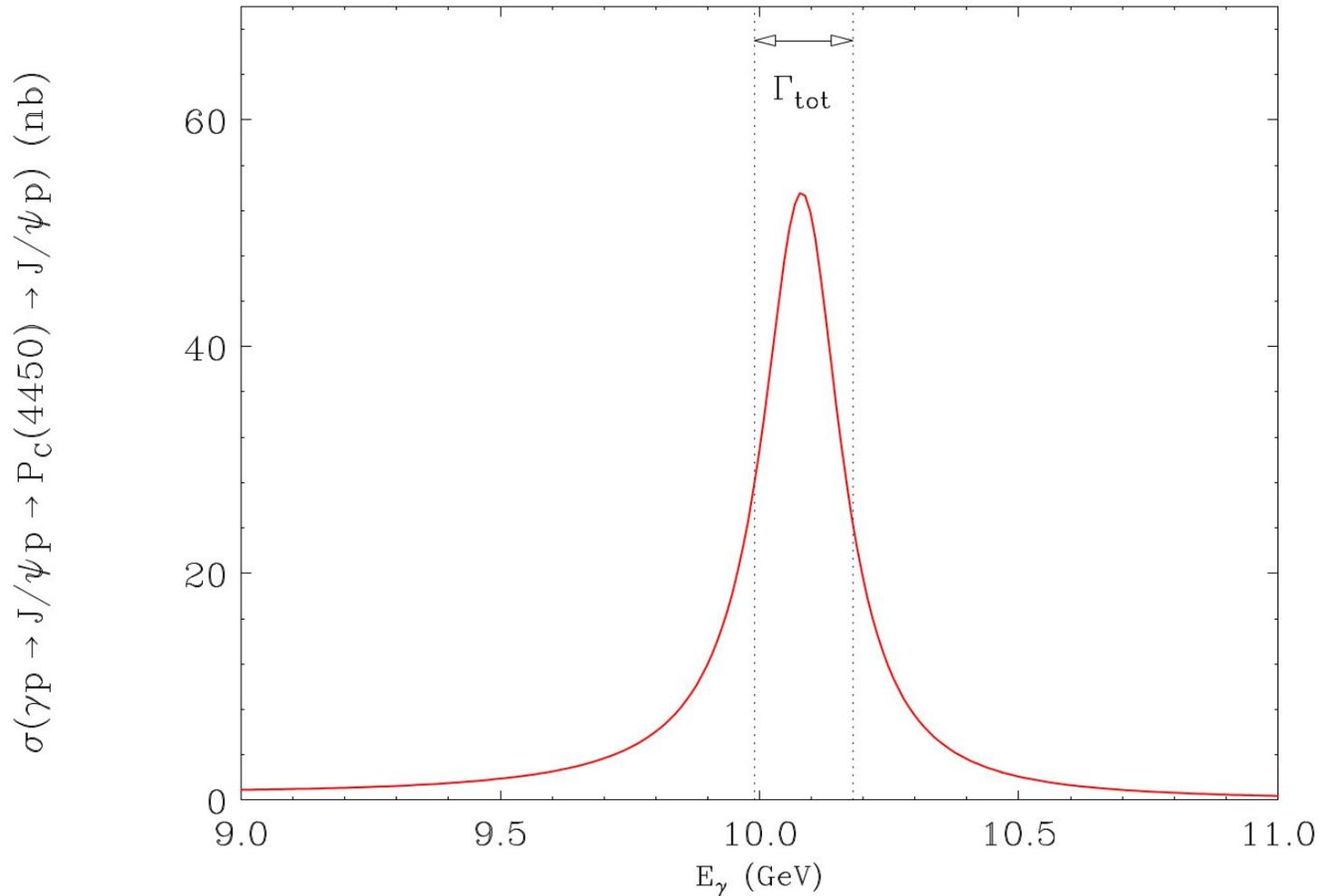


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- $\sigma \sim 50 \text{ nb} \gg \sigma_{\text{diffractive}} \sim 1 \text{ nb}$

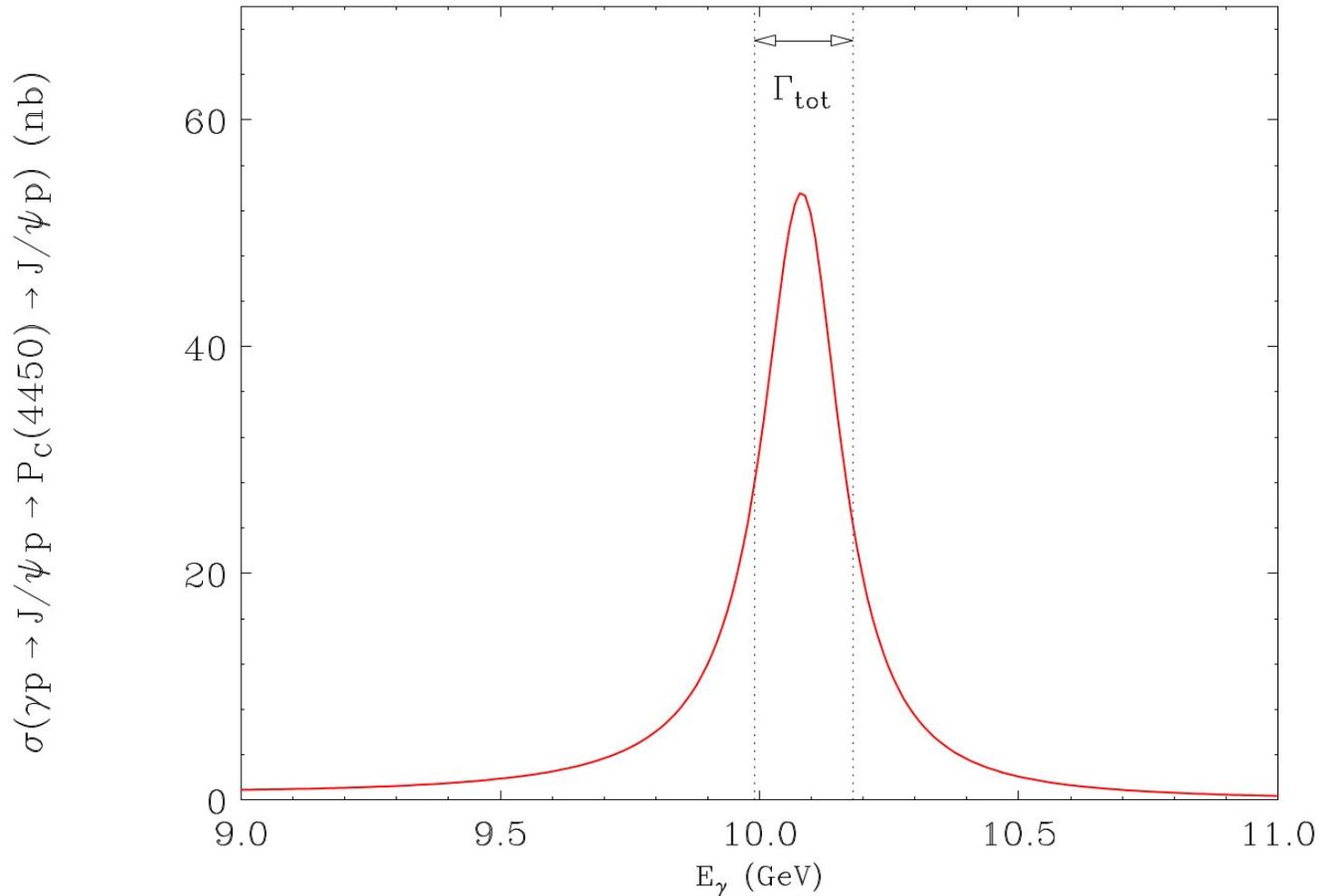
Now can also look for $P_c(4312)$ in $\gamma N \rightarrow J/\psi N$!

$$E_\gamma = 9.44 \text{ GeV}$$



Cross section for resonant photoproduction $\gamma p \rightarrow J/\psi p \rightarrow P_c(4450) \rightarrow J/\psi p$, assuming $B_{\text{out}} = 0.1$, plotted as function of the incident photon energy E_γ . The vertical dotted lines indicate the width of the $P_c(4450)$ resonance.

Ongoing expts at JLab



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Ongoing expts at Jlab
possible $c \rightarrow b$ analogue?

doubly heavy baryons QQq :

$ccq, bcq, bbq, \quad q = u, d$

must exist, and now have been seen

fascinating challenge for EXP & TH

Original

LHCb saw thousands of B_c -s

\implies should see $bcq, ccq, \text{etc.}$

- Phenomenological approach
- Identify eff. d.o.f. & their interactions
- Extract model parameters from exp
- Then use them to make predictions

Baryons with two heavy quarks: Masses, production, decays, and detection

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(Received 5 September 2014; published 10 November 2014)

The large number of B_c mesons observed by LHCb suggests a sizable cross section for producing doubly heavy baryons in the same experiment. Motivated by this, we estimate masses of the doubly heavy $J = 1/2$ baryons Ξ_{cc} , Ξ_{bb} , and Ξ_{bc} , and their $J = 3/2$ hyperfine partners, using a method which accurately predicts the masses of ground-state baryons with a single heavy quark. **We obtain $M(\Xi_{cc}) = 3627 \pm 12$ MeV, $M(\Xi_{cc}^*) = 3690 \pm 12$ MeV, $M(\Xi_{bb}) = 10162 \pm 12$ MeV, $M(\Xi_{bb}^*) = 10184 \pm 12$ MeV, $M(\Xi_{bc}) = 6914 \pm 13$ MeV, $M(\Xi'_{bc}) = 6933 \pm 12$ MeV, and $M(\Xi_{bc}^*) = 6969 \pm 14$ MeV.** As a byproduct, we estimate the hyperfine splitting between B_c^* and B_c mesons to be 68 ± 8 MeV. We discuss P-wave excitations, production mechanisms, decay modes, lifetimes, and prospects for detection of the doubly heavy baryons.

DOI: [10.1103/PhysRevD.90.094007](https://doi.org/10.1103/PhysRevD.90.094007)

PACS numbers: 14.20.Lq, 14.20.Mr, 12.40.Yx

3627 \pm 12 MeV

Observation of the doubly charmed baryon Ξ_{cc}^{++}

LHCb collaboration[†]

Abstract

A highly significant structure is observed in the $\Lambda_c^+ K^- \pi^+ \pi^+$ mass spectrum, where the Λ_c^+ baryon is reconstructed in the decay mode $p K^- \pi^+$. The structure is consistent with originating from a weakly decaying particle, identified as the doubly charmed baryon Ξ_{cc}^{++} . The mass, measured relative to that of the Λ_c^+ baryon, is found to be 3621.40 ± 0.72 (stat) ± 0.27 (syst) ± 0.14 (Λ_c^+) MeV/ c^2 , where the last uncertainty is due to the limited knowledge of the Λ_c^+ mass. The state is observed in a sample of proton-proton collision data collected by the LHCb experiment at a center-of-mass energy of 13 TeV, corresponding to an integrated luminosity of 1.7 fb⁻¹, and confirmed in an additional sample of data collected at 8 TeV.

3621+-1 MeV

doubly heavy baryons: mass predictions

TABLE XVIII. Summary of our mass predictions (in MeV) for lowest-lying baryons with two heavy quarks. States without a star have $J = 1/2$; states with a star are their $J = 3/2$ hyperfine partners. The quark q can be either u or d . The square or curved brackets around cq denote coupling to spin 0 or 1.

State	Quark content	$M(J = 1/2)$	$M(J = 3/2)$
$[\Sigma]_{cc}^{(*)}$	ccq	3627 ± 12	3690 ± 12
$[\Sigma]_{bc}^{(*)}$	$b[cq]$	6914 ± 13	6969 ± 14
$[\Sigma]'_{bc}$	$b(cq)$	6933 ± 12	...
$[\Sigma]_{bb}^{(*)}$	bbq	10162 ± 12	10184 ± 12

LHCb: 3621 ± 1

doubly heavy baryons predicted lifetimes (fs)

Baryon	This work	[28]	[51]	[71]	[72]
$\Xi_{cc}^{++} = ccu$	185	430 ± 100	460 ± 50	500	~ 200
$\Xi_{cc}^{+} = ccd$	53	120 ± 100	160 ± 50	150	~ 100
$\Xi_{bc}^{+} = bcu$	244	330 ± 80	300 ± 30	200	—
$\Xi_{bc}^{0} = bcd$	93	280 ± 70	270 ± 30	150	—
$\Xi_{bb}^{0} = bbu$	370	—	790 ± 20	—	—
$\Xi_{bb}^{-} = bbd$	370	—	800 ± 20	—	—

[28] K. Anikeev, D. Atwood, F. Azfar, S. Bailey, C. W. Bauer, W. Bell, G. Bodwin, E. Braaten *et al.*, *Workshop on B Physics at Conferences C99-09-23.2 and C00-02-24 (Batavia, IL, Fermilab, 2001)*, arXiv:hep-ph/0201071.

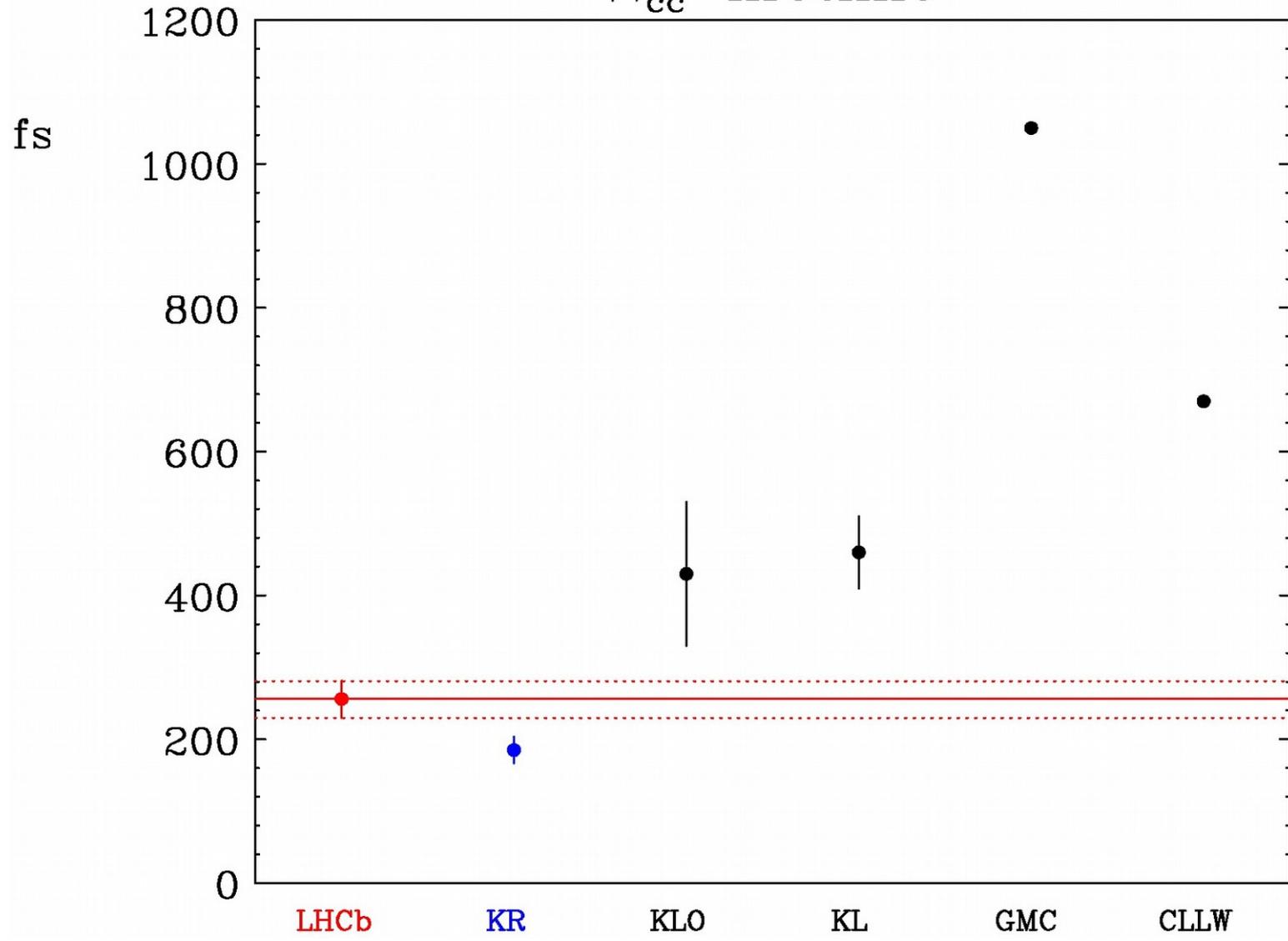
[71] J. D. Bjorken, Fermilab Report No. FERMILAB-PUB-86-189-T, <http://lss.fnal.gov/archive/1986/pub/fermilab-pub-86-189-t.pdf>.

[72] M. A. Moinester, *Z. Phys. A* **355**, 349 (1996).

[51] V. V. Kiselev and A. K. Likhoded, *Usp. Fiz. Nauk* **172**, 497 (2002) [*Sov. Phys. Usp.* **45**, 455 (2002)].

recently measured by LHCb:

Ξ_{cc}^{++} lifetime



$$\tau(\Xi_{cc}^{++}) = 256^{+21}_{-22} \pm 14 \text{ fs}$$

masses of doubly-heavy baryons:
use same toolbox that predicted
b baryon masses.

ccq mass calculation

sum of :

- $2m_c$
- V_{cc} in 3_c^*
- $V_{HF}(cc)$
- $V_{HF}(cq)$
- m_q

ccq mass calculation

sum of :

- $2m_c$
 - V_{cc} in 3_c^*
 - $V_{HF}(cc)$
 - $V_{HF}(cq)$
 - m_q
- } no exp info !

Effective masses

in mesons:

$$m_u^m = m_d^m = m_q^m = 310 \text{ MeV}, \quad m_c^m = 1663.3 \text{ MeV}$$

in baryons:

$$m_u^b = m_d^b = m_q^b = 363 \text{ MeV}, \quad m_c^b = 1710.5 \text{ MeV}$$

$V(cc)$ from $V(c\bar{c})$:

$$\bar{M}(c\bar{c} : 1S) \equiv [3M(J/\psi) + M(\eta_c)]/4 = 3068.6 \text{ MeV}$$

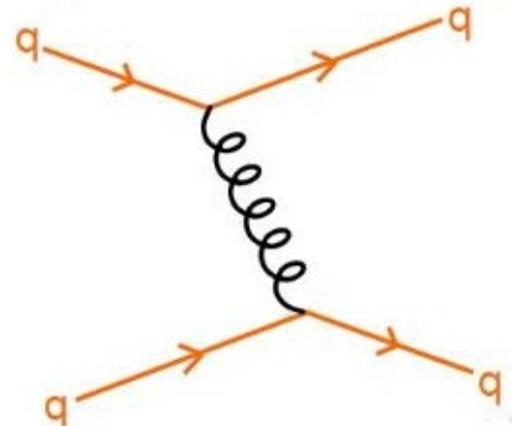
$$V(c\bar{c}) = \bar{M}(c\bar{c} : 1S) - 2m_c^m = -258.0 \text{ MeV.}$$

$$V(cc) = \frac{1}{2} V(c\bar{c}) = -129.0 \text{ MeV.}$$

in weak coupling follows
from color algebra in $1g_x$

here a dynamical assumption:

$V(cc)$ and $V(c\bar{c})$ factorize
into color \times space



gluon exchange by 2 quarks

$V_{HF}(cc)$ from $V_{HF}(c\bar{c})$:

$$V_{HF}(cc) = \frac{a_{cc}}{m_c^2}$$

$$V_{HF}(c\bar{c}) = M(J/\psi) - M(\eta_c) = 113.2 \text{ MeV} = \frac{4a_{c\bar{c}}}{m_c^2}$$

assume $a_{cc} = \frac{1}{2}a_{c\bar{c}}$,

$$\Rightarrow \frac{a_{cc}}{m_c^2} = 1/2 \cdot \frac{M(J/\psi) - M(\eta_c)}{4} = 14.2 \text{ MeV}$$

Contributions to Ξ_{cc} mass

Contribution	Value (MeV)
$2m_c^b + m_q^b$	3783.9
cc binding	-129.0
$a_{cc}/(m_c^b)^2$	14.2
$-4a/m_q^b m_c^b$	-42.4
Total	3627 ± 12

The ± 12 MeV error estimate from
ave. error for Qqq baryons

The same theoretical toolbox
that led to the accurate Ξ_{cc} mass prediction
now predicts

a stable, deeply bound $bb\bar{u}\bar{d}$ tetraquark,

215 MeV below BB^* threshold

the first manifestly exotic stable hadron



Discovery of the Doubly Charmed Ξ_{cc} Baryon Implies a Stable $bb\bar{u}\bar{d}$ Tetraquark

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Recently, the LHCb Collaboration discovered the first doubly charmed baryon $\Xi_{cc}^{++} = ccu$ at 3621.40 ± 0.78 MeV, very close to our theoretical prediction. We use the same methods to predict a doubly bottom tetraquark $T(bb\bar{u}\bar{d})$ with $J^P = 1^+$ at 10389 ± 12 MeV, 215 MeV below the $B^-\bar{B}^{*0}$ threshold and 170 MeV below the threshold for decay to $B^-\bar{B}^0\gamma$. The $T(bb\bar{u}\bar{d})$ is therefore stable under strong and electromagnetic interactions and can only decay weakly, the first exotic hadron with such a property. On the other hand, the mass of $T(cc\bar{u}\bar{d})$ with $J^P = 1^+$ is predicted to be 3882 ± 12 MeV, 7 MeV above the D^0D^{*+} threshold and 148 MeV above the $D^0D^+\gamma$ threshold. $T(bc\bar{u}\bar{d})$ with $J^P = 0^+$ is predicted at 7134 ± 13 MeV, 11 MeV below the \bar{B}^0D^0 threshold. Our precision is not sufficient to determine whether $bc\bar{u}\bar{d}$ is actually above or below the threshold. It could manifest itself as a narrow resonance just at threshold.

DOI: 10.1103/PhysRevLett.119.202001

Calculation of tetraquark $bb\bar{u}\bar{d}$ mass

build on accuracy of the Ξ_{cc} mass prediction

$$V(bb) = \frac{1}{2} V(\bar{b}b)$$

to obtain lowest possible mass, assume:

- $bb\bar{u}\bar{d}$ in S -wave
- $\bar{u}\bar{d}$: $\mathbf{3}_c$ “good” antidiq., $S=0$, $l=0$
(it's the lightest one)

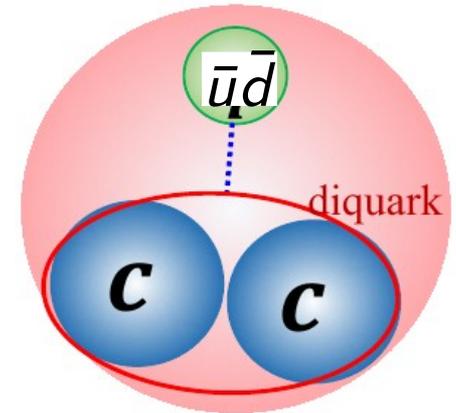
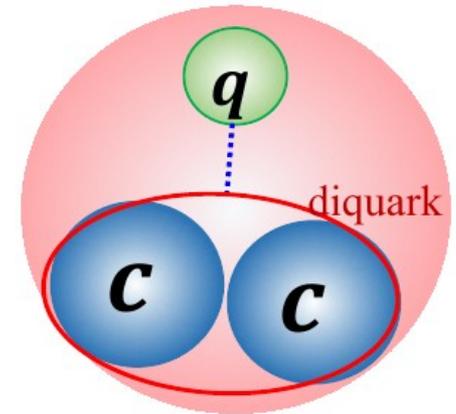
$\Rightarrow bb$ must be $\bar{\mathbf{3}}_c$; Fermi stats: spin 1

$(bb)_{s=1} (\bar{u}\bar{d})_{s=0} \Rightarrow J^P = 1^+$.

$\Rightarrow (bb) (\bar{u}\bar{d})$ very similar to bbq baryon:

$$q \leftrightarrow (\bar{u}\bar{d})$$

bbq baryon



Ξ_{cc} discovery \Rightarrow quantitative validation

qualitatively $E_{binding} \sim \alpha_s^2 M_Q$

so for $M_Q \rightarrow \infty$

$QQ\bar{u}\bar{d}$ must be bound

Contributions to mass of $(bb\bar{u}\bar{d})$ Tq with $J^P = 1^+$

Contribution	Value (MeV)
$2m_b^b$	10087.0
$2m_q^b$	726.0
$a_{bb}/(m_b^b)^2$	7.8
$-3a/(m_q^b)^2$	-150.0
bb binding	-281.4
Total	10389.4 ± 12

Contributions to mass of $(cc\bar{u}\bar{d})$ Tq with $J^P = 1^+$

Contribution	Value (MeV)
$2m_c^b$	3421.0
$2m_q^b$	726.0
$a_{cc}/(m_c^b)^2$	14.2
$-3a/(m_q^b)^2$	-150.0
cc binding	-129.0
Total	3882.2 ± 12

7 MeV above $D^0 D^{+*}$ threshold,

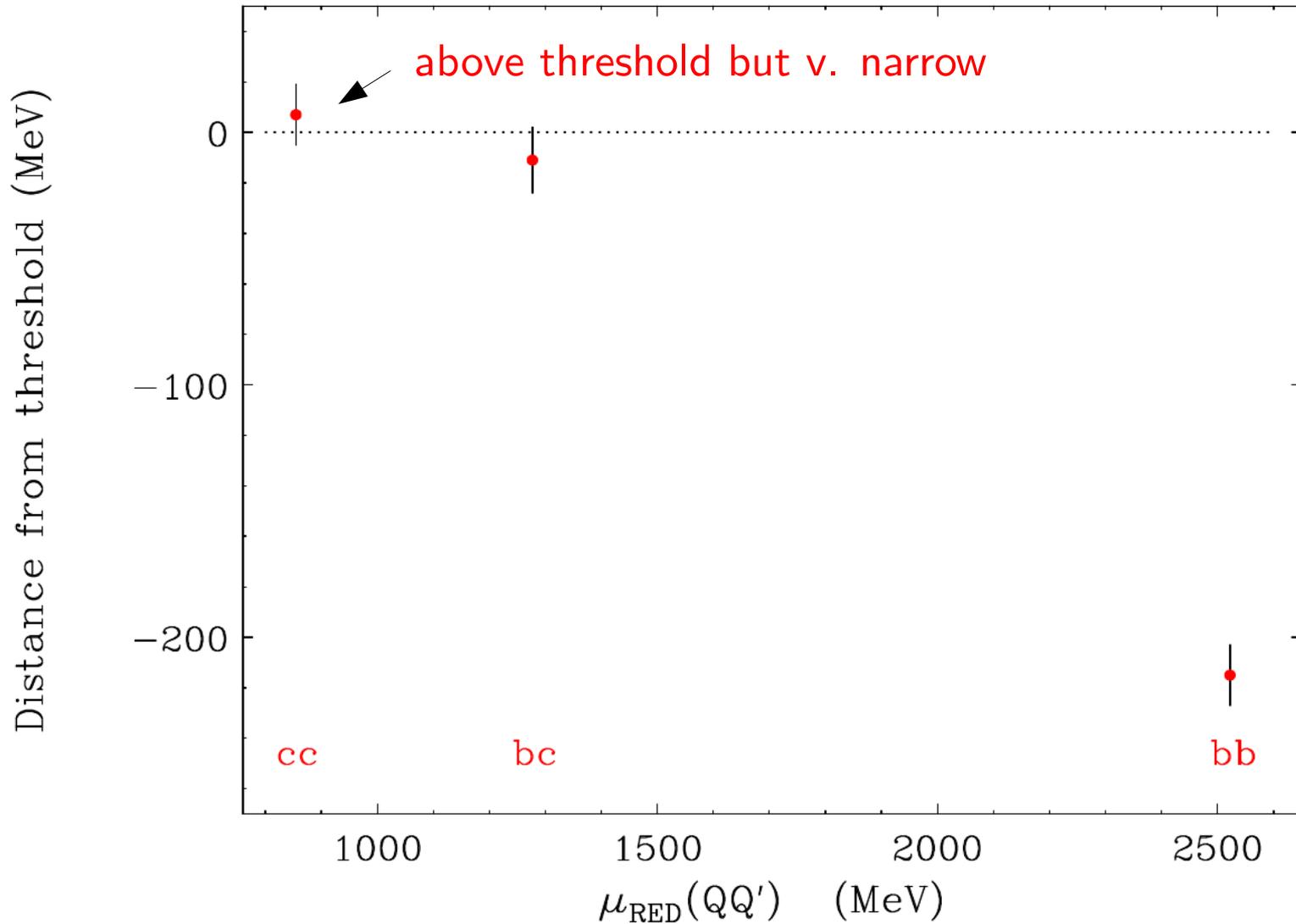
but if use measured $M(X_{cc}^{++}) \Rightarrow$ only 1 MeV above $D^0 D^{+*}$

Contributions to mass of $(bc\bar{u}\bar{d})$ Tq^* with $J^P = 0^+$

Contribution	Value (MeV)
$m_b^b + m_c^b$	6754.0
$2m_q^b$	726.0
$-3a_{bc}/(m_b^b m_c^b)$	-25.5
$-3a/(m_q^b)^2$	-150.0
bc binding	-170.8
Total	7133.7 ± 13

*lowest-mass bc diquark has $S=0$, so $J=0$

Distance of the $QQ'\bar{u}\bar{d}$ Tq masses
from the relevant two-meson thresholds (MeV).



Tetraquark production

$$\sigma(pp \rightarrow T(bb\bar{u}\bar{d}) + X) \lesssim \sigma(pp \rightarrow \Xi_{bb} + X)$$

same bottleneck: $\sigma(pp \rightarrow \{bb\} + X)$

hadronization:

$$\left. \begin{array}{l} \{bb\} \rightarrow \{bb\}q \\ \{bb\} \rightarrow \{bb\}\bar{u}\bar{d} \end{array} \right\} \begin{array}{l} P(\bar{u}\bar{d}) \lesssim P(q) \\ \mathbf{3}_c \qquad \mathbf{3}_c \end{array}$$

LHCb observed $ccu = \Xi_{cc}^{++}$

$$\sigma(pp \rightarrow \Xi_{bb} + X) = (b/c)^2 \cdot \sigma(pp \rightarrow \Xi_{cc} + X)$$

$\Rightarrow \Xi_{bb}$ and $T(bb\bar{u}\bar{d})$ accessible,
with much more $\int \mathcal{L} dt$

Tetraquark production

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LHCb observed $ccu = \Xi_{cc}^{++}$

$$\sigma(pp \rightarrow \Xi_{bb} + X) = (b/c)^2 \cdot \sigma(pp \rightarrow \Xi_{cc} + X)$$

$\Rightarrow \Xi_{bb}$ and $T(bb\bar{u}\bar{d})$ accessible,
with much more $\int \mathcal{L} dt$

$T(cc\bar{u}\bar{d})$
likely narrow
accessible

now

Inclusive signature of (bbx): displaced B_c

T. Gershon & A. Poluektov JHEP 1901 (2019) 019

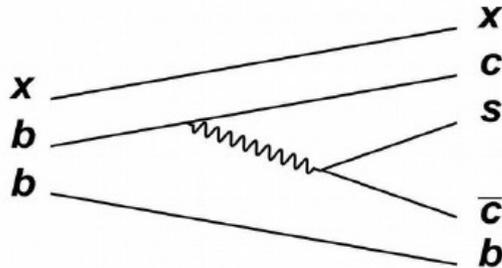
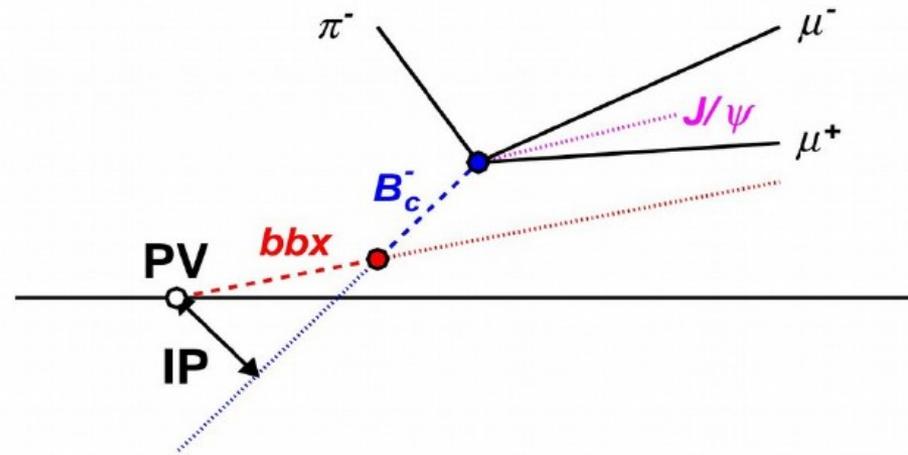


Diagram for production of a B_c^- meson from a double beauty hadron decay.



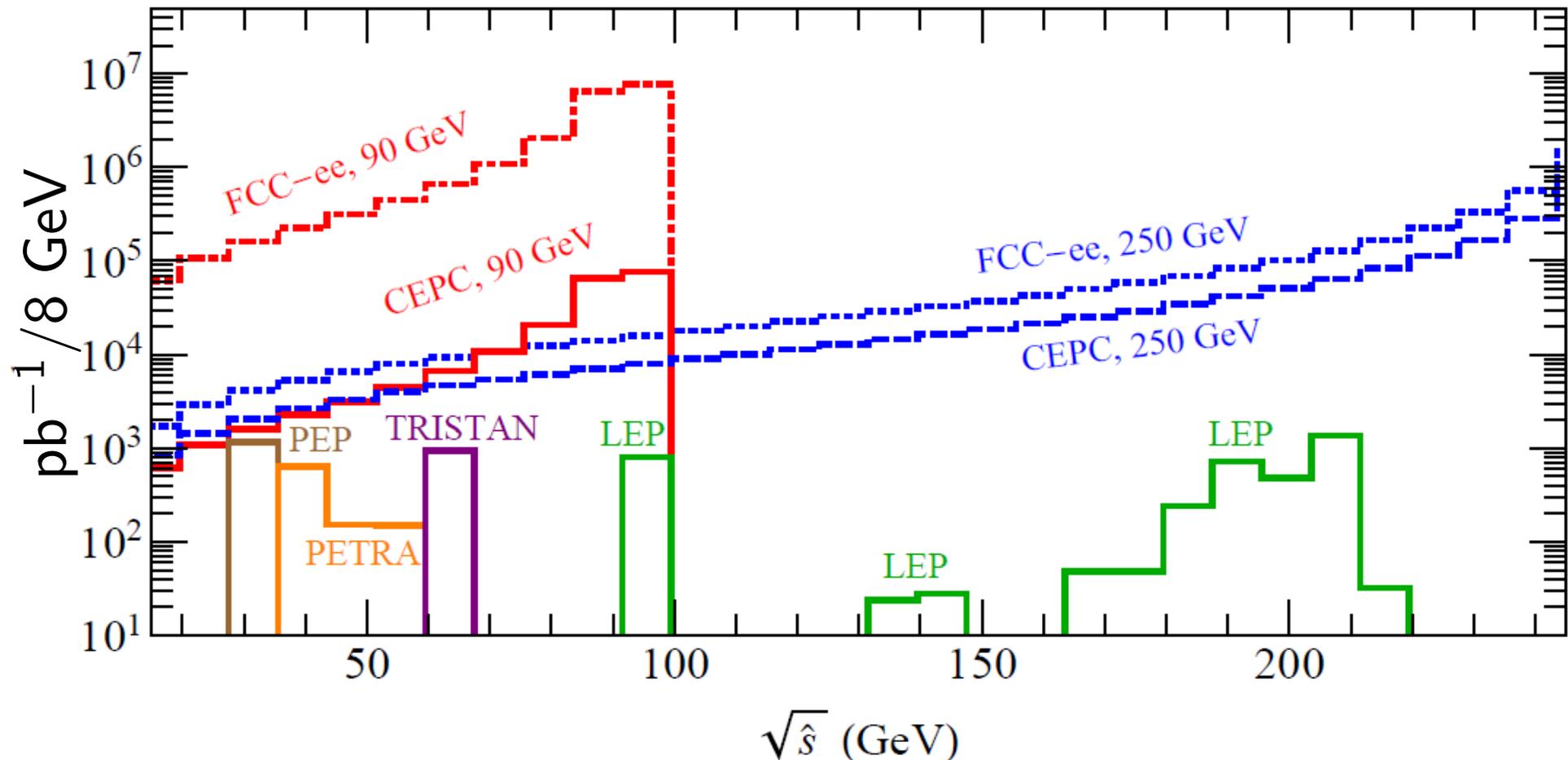
$\mathcal{O}(1\%)$ of all B_c -s @LHC come from bbx

- major enhancement of eff. bbx rate
- bbq or $bb\bar{u}\bar{d}$?

incl. $\sigma(bb\bar{x})$:
heavy ions $\gg pp$

\Rightarrow displaced B_c @ALICE & RHIC !

CEPC radiative return integrated luminosity



Integrated luminosity from past low energy e^+e^- colliders at their nominal center-of-mass energies compared to the effective luminosity through radiative return from future e^+e^- colliders at $\sqrt{\hat{s}} = 90$ or 250 GeV

gaps filled in and much more

crude estimate of $bb\bar{u}\bar{d}$ lifetime

$$M_{initial} = M(bb\bar{u}\bar{d}) = 10,389.4 \text{ MeV}$$

$$M_{final} = M(\bar{B}) + M(D) = 7,144.5 \text{ MeV},$$

$$W^{-*} \rightarrow e\bar{\nu}_e, \mu\bar{\nu}_\mu, \tau\bar{\nu}_\tau, 3 \text{ colors of } \bar{u}\bar{d} \text{ and } \bar{c}s,$$

a kinematic suppression factor

$$F(x) = 1 - 8x + 8x^3 - x^4 + 12x^2 \ln(1/x),$$

$$x \equiv \{[M(\bar{B}) + M(D)]/M(bb\bar{u}\bar{d})\}^2,$$

$|V_{cb}| = 0.04$, factor of 2 to count each decaying b quark.

$$\Rightarrow \Gamma(bb\bar{u}\bar{d}) = \frac{18 G_F^2 M(bb\bar{u}\bar{d})^5}{192\pi^3} F(x) |V_{cb}|^2 = 17.9 \times 10^{-13} \text{ GeV},$$

$$\tau(bb\bar{u}\bar{d}) = 367 \text{ fs.}$$

$bb\bar{u}\bar{d}$ decay channels

(a) “standard process” $bb\bar{u}\bar{d} \rightarrow cb\bar{u}\bar{d} + W^{*-}$.

$(bb\bar{u}\bar{d}) \rightarrow D^0 \bar{B}^0 \pi^-, D^+ B^- \pi^-$

$(bb\bar{u}\bar{d}) \rightarrow J/\psi K^- \bar{B}^0, J/\psi \bar{K}^0 B^-.$

$(bb\bar{u}\bar{d}) \rightarrow \Omega_{bc} \bar{p}, \Omega_{bc} \bar{\Lambda}_c, \Xi_{bc}^0 \bar{p}, \Xi_{bc}^0 \bar{\Lambda}_c$

In addition, a rare process where *both* $b \rightarrow c\bar{c}s$,

$(bb\bar{u}\bar{d}) \rightarrow J/\psi J/\psi K^- \bar{K}^0.$

striking signature: $2J/\psi$ -s from same 2ndary vertex

(b) The W -exchange $b\bar{d} \rightarrow c\bar{u}$

e.g. $(bb\bar{u}\bar{d}) \rightarrow D^0 B^-.$

no stable light exotics

unlike $bb\bar{u}\bar{d}$,
stable light exotics do not exist,
as $E_{kin} \propto 1/m_q$ too large

e.g. proposed deeply bound
 $uuddss$ @ 1860-1880 MeV

recently ruled out by BaBar,
arXiv:1810.04724

a deeply bound compact $uuddss$ dibaryon ?

advertised as dark matter candidate

(Glennys Farrar)

- prehistory: $\Lambda\Lambda$ H dibaryon, $B=81$ MeV (R.L. Jaffe 1976)
optimization of color-magnetic forces, $SU(3)_F$ symm.
 $SU(3)_F$ breaking \implies binding marginal
1242 citations, but H not seen by exp. nor lattice
- attempt at renaissance as dark matter candidate
for stability **needs $B > 2(m_s - m_u) \sim 200$ MeV !**
bounds on DM interaction **require $r < 0.2$ fm $= r_p/4.4$**
 $\implies \Delta p > 1$ GeV for each quark!

$T(bb\bar{u}\bar{d})$ Summary

- stable, deeply bound $bb\bar{u}\bar{d}$ tetraquark
- $J^P = 1^+$, $M(bb\bar{u}\bar{d}) = 10389 \pm 12$ MeV
- 215 MeV below BB^* threshold
- first manifestly exotic stable hadron
- $(bb\bar{u}\bar{d}) \rightarrow \bar{B}D\pi^-, J/\psi\bar{K}\bar{B},$
 $J/\psi J/\psi K^- \bar{K}^0, D^0 B^-$
- $(bc\bar{u}\bar{d})$: $J^P = 0^+$, borderline bound
7134 \pm 13 MeV, 11 MeV below $\bar{B}^0 D^0$
- $(cc\bar{u}\bar{d})$: $J^P = 1^+$, borderline unbound
3882 \pm 12 MeV, 7 MeV above the $D^0 D^{*+}$

two v. different types of exotics:

$$Q\bar{Q}q\bar{q}$$
$$QQ\bar{q}\bar{q}$$

e.g.

$$Z_b(10610)$$
$$T(bb\bar{u}\bar{d})$$
$$\bar{B}B^*$$

molecule

tightly-bound

tetraquark

likely a general rule

Exotics with $\bar{Q}Q$ vs. QQ : very different

$$V(\bar{Q}Q) = 2V(QQ), \text{ hundreds of MeV}$$

but *only* if $\bar{Q}Q$ color singlet

$\Rightarrow \bar{Q}Q$ can immediately hadronize

\Rightarrow exotics: \bar{Q} in one hadron and Q in the other

\Rightarrow deuteron-like "hadronic molecules"

vs. QQ *never* a color singlet,

\Rightarrow tightly bound exotics, tetraquarks

$T(bb\bar{u}\bar{d})$:

$$m_b \approx 5 \text{ GeV}$$

$$\Rightarrow R(bb) \sim 0.2 \text{ fm}$$

$$V(r) = -\frac{\alpha_s(r)}{r} + \sigma r$$

$$\Rightarrow B(bb) \approx -280 \text{ MeV}$$

tightly bound, but $\bar{3}_c$,
so cannot disengage from $\bar{u}\bar{d}$

$Z_b(10610)$: $b\bar{b}u\bar{d}$

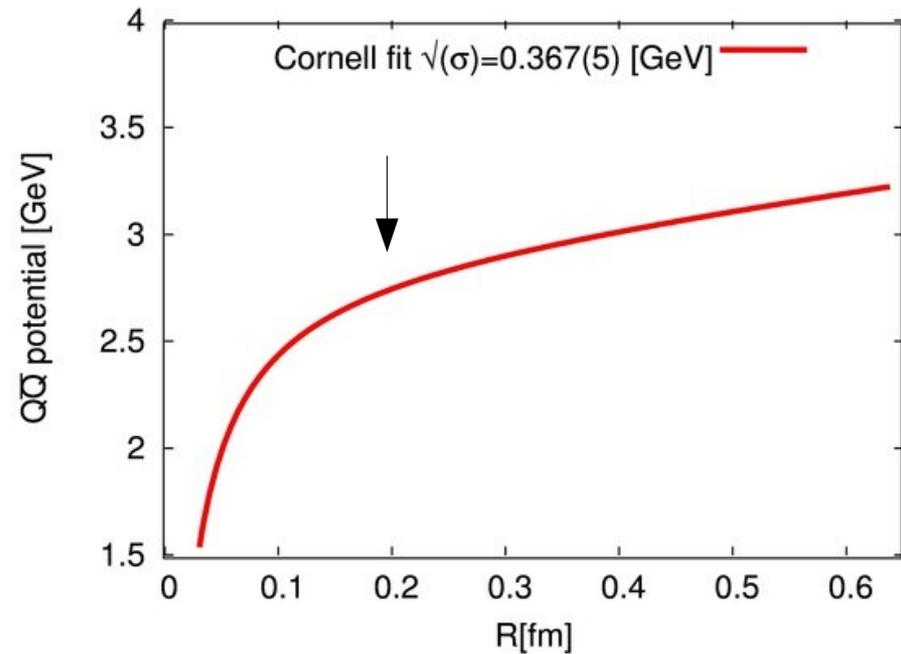
if $b\bar{b}$ compact \Rightarrow color singlet:

decouple from $u\bar{d}$, $Z_b \rightarrow \gamma\pi^+$

so only semi-stable config.,

“hadronic molecule:” $\bar{B}B^* \sim 1 \text{ GeV}$ above $\gamma\pi$

yet narrow $\sim 15 \text{ MeV}$, because $R(\bar{B}B^*)/R(\gamma) \gg 1$



very different!

$T(bb\bar{u}\bar{d})$:

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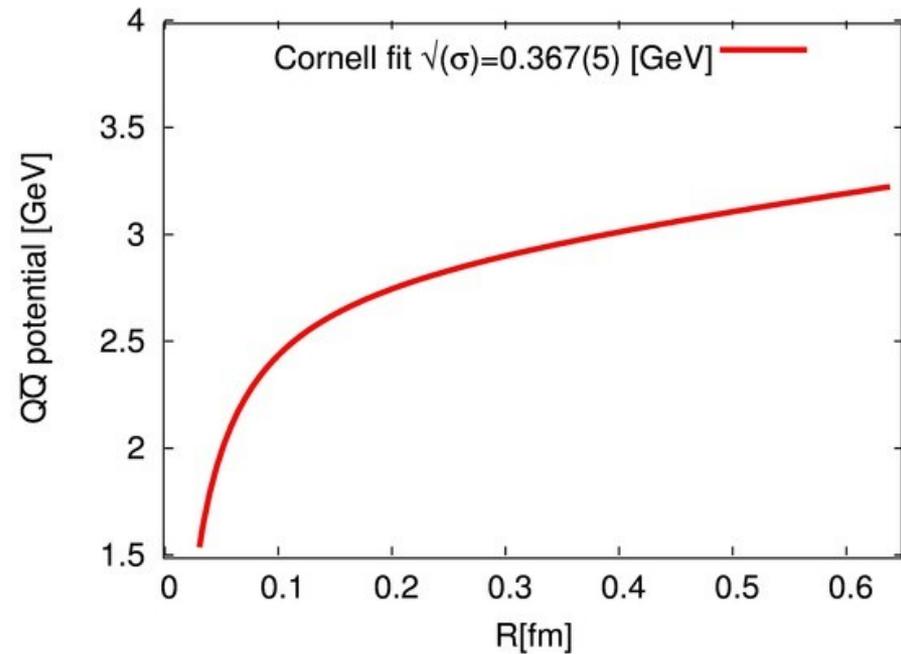
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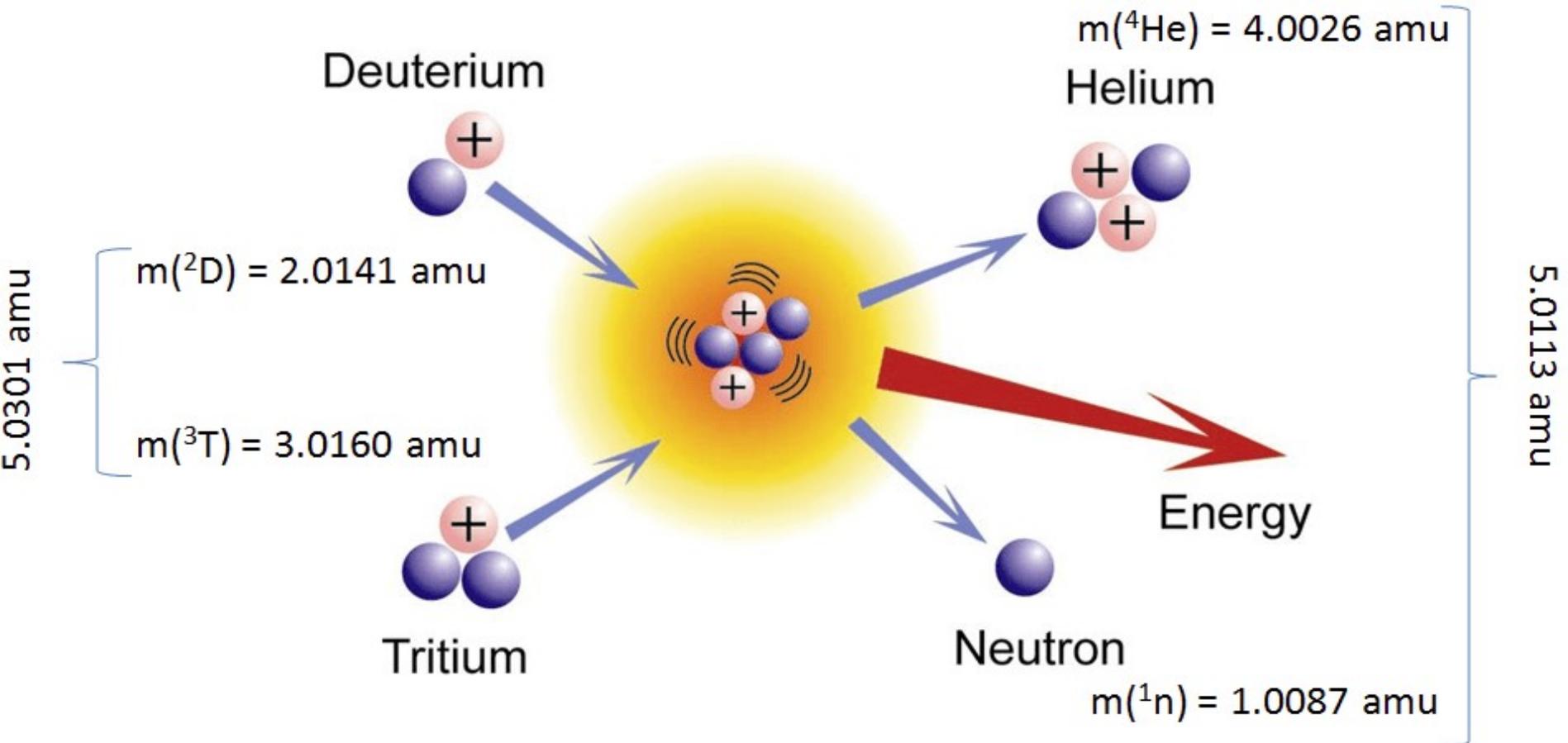
bottom line: $T(bb\bar{u}\bar{d})$ a tetraquark, $Z_b(b\bar{b}u\bar{d})$ a molecule



very different!

Quark-level analogue of nuclear fusion with doubly-heavy baryons

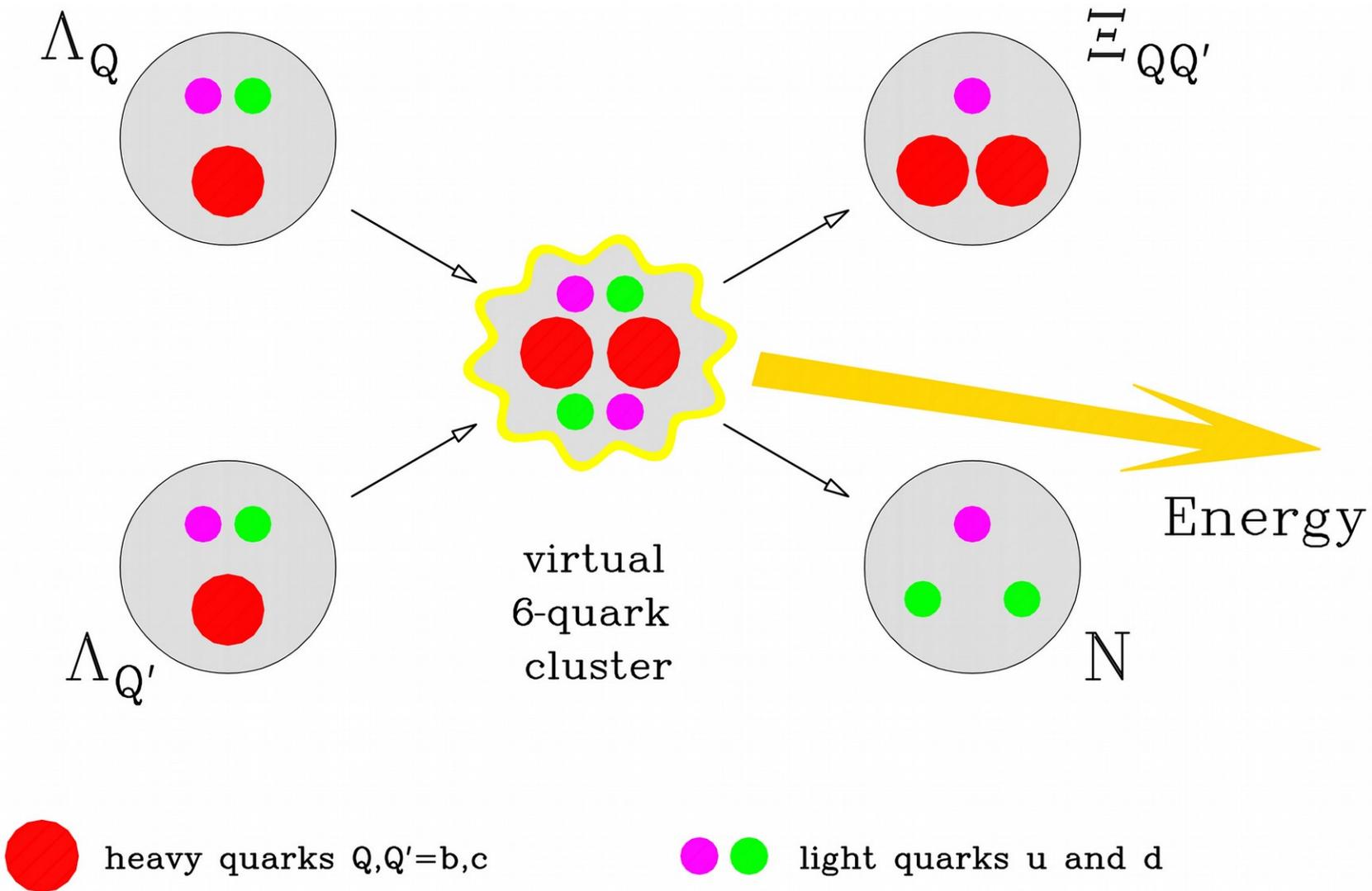
DT fusion: $DT \rightarrow {}^4\text{He} n$

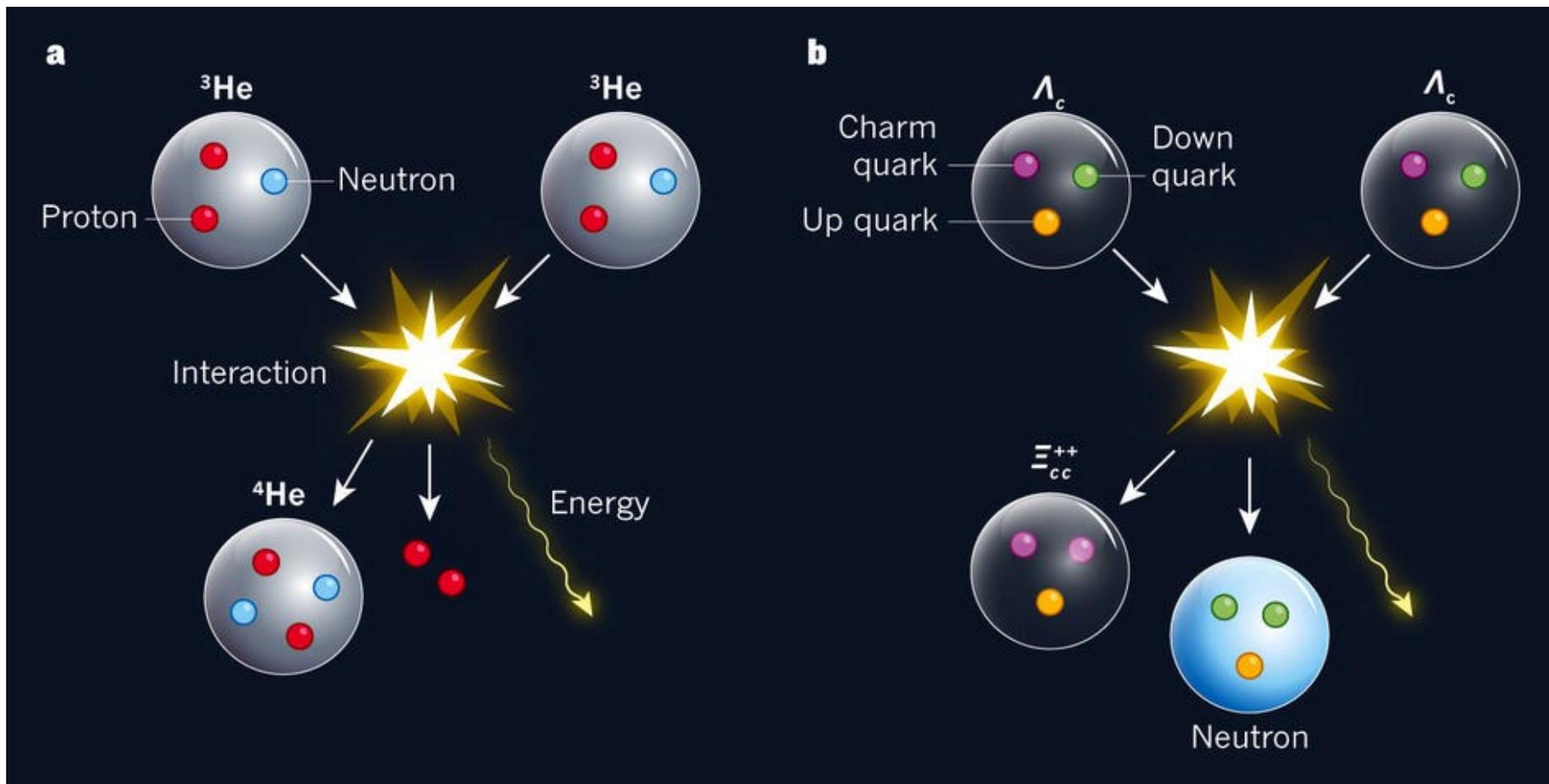


$$Q = 0.0188 \text{ amu} \times 931.481 \text{ MeV/amu} = 17.5 \text{ MeV}$$

Nuclear fusion reactions w. light nuclei

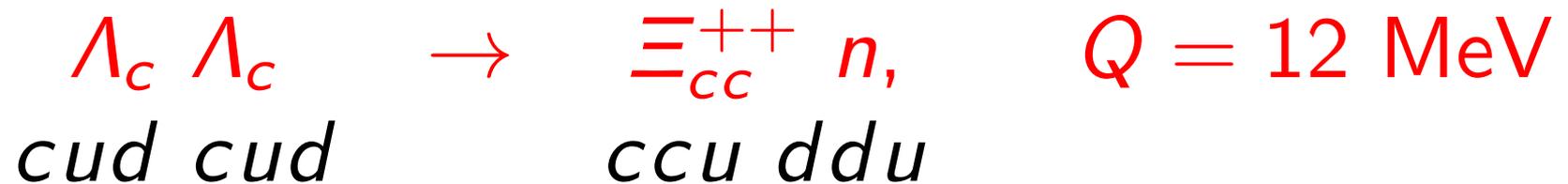






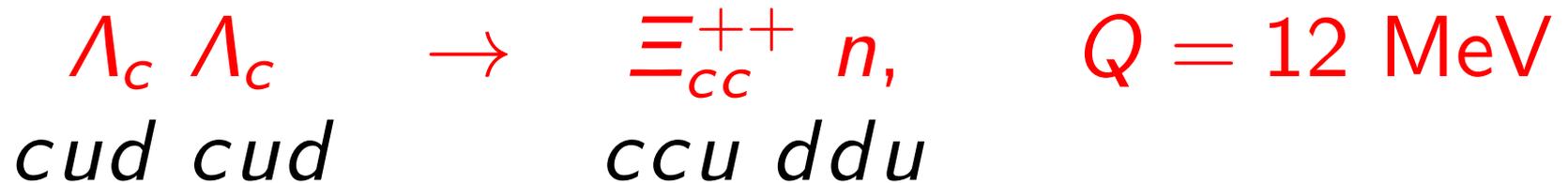
LHCb measured $M(X_{cc}^{++}) = 3621.4 \pm 0.78 \text{ MeV}$

\Rightarrow Q -value of the reaction:

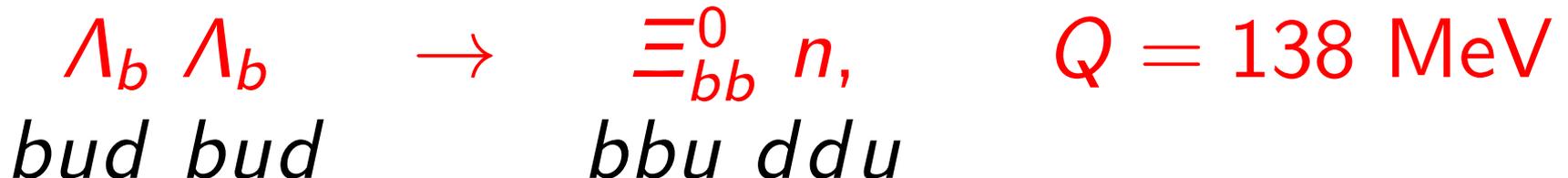


LHCb measured $M(X_{cc}^{++}) = 3621.4 \pm 0.78$ MeV

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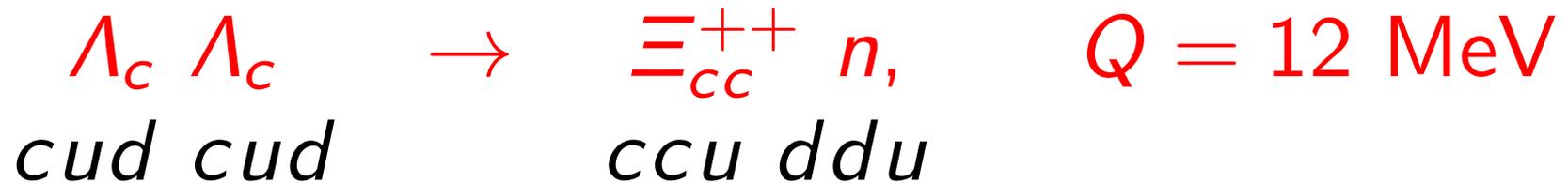


robust estimate of Ξ_{bb}^0 mass, so expect

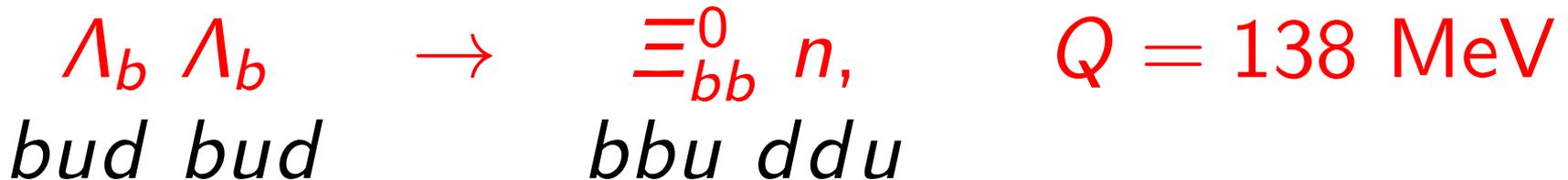


LHCb measured $M(X_{cc}^{++}) = 3621.4 \pm 0.78$ MeV

\Rightarrow Q-value of the reaction:



robust estimate of Ξ_{bb}^0 mass, so expect



But no chain reaction, as $\tau(Q) \sim 10^{-13}$ sec

Nature,
Nov 2, 2017

Quark-level analogue of nuclear fusion with doubly heavy baryons

Marek Karliner¹ & Jonathan L. Rosner²

The essence of nuclear fusion is that energy can be released by the rearrangement of nucleons between the initial- and final-state nuclei. The recent discovery¹ of the first doubly charmed baryon Ξ_{cc}^{++} , which contains two charm quarks (c) and one up quark (u) and has a mass of about 3,621 mega-electronvolts (MeV) (the mass of the proton is 938 MeV) also revealed a large binding energy of about 130 MeV between the two charm quarks. Here we report that this strong binding enables a quark-rearrangement, exothermic reaction in which two heavy baryons (A_c) undergo fusion to produce the doubly charmed baryon Ξ_{cc}^{++} and a neutron n ($A_c A_c \rightarrow \Xi_{cc}^{++} n$), resulting in an energy release of 12 MeV. This reaction is a quark-level analogue of the deuterium–tritium nuclear fusion reaction ($DT \rightarrow {}^4\text{He } n$). The much larger binding energy (approximately 280 MeV) between two bottom quarks (b) causes the analogous reaction with bottom quarks ($A_b A_b \rightarrow \Xi_{bb}^0 n$) to have a much larger energy release of about 138 MeV. We suggest some experimental setups in which the highly exothermic nature of the fusion of two heavy-quark baryons might manifest itself. At present, however, the very short lifetimes of the heavy bottom and charm quarks preclude any practical applications of such reactions.

The mass of the doubly charmed baryon Ξ_{cc}^{++} observed in the LHCb experiment¹ 3621.40 ± 0.78 MeV is consistent with several predictions², including that of $3,627 \pm 12$ MeV (an extensive list of other predictions can be found in refs 1 and 2). The essential insight of ref. 2 is the large binding energy B of the two heavy quarks (the charm c or bottom b quarks) in a baryon, $B(cc) = 129$ MeV and $B(bb) = 281$ MeV. To a very good approximation, this binding energy is half of the quark–antiquark binding energy in their bound states, which are known as quarkonia. This ‘half’ rule is exact in the one-gluon-exchange limit and has now been validated by the measurement of the Ξ_{cc}^{++} mass. Its successful extension beyond weak coupling implies that the heavy quark potential factorizes into a colour-dependent and a space-dependent part, with the latter being the same for quark–quark and quark–antiquark pairs. The relative factor of 1/2 then results from the colour algebra, just as in the weak-coupling limit.

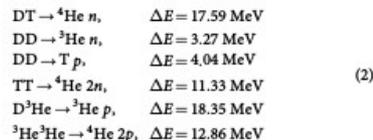
The large binding energy between heavy quarks has some important implications, such as the existence of a stable $bb\bar{u}\bar{d}$ tetraquark (where \bar{u} and \bar{d} are antiup and antidown quarks, respectively) with spin–parity³ $J^P = 1^+ 215$ MeV below the $B^- \bar{B}^{*0}$ threshold and 170 MeV below the threshold for decay to $B^- \bar{B}^{*0} \gamma$, where B^- is a spinless meson composed of $b\bar{u}$, \bar{B}^{*0} is a spin-1 meson composed of $b\bar{d}$, B^0 is a spinless meson composed of $b\bar{d}$ and γ is a photon. Another important consequence is the existence of a quark-level analogue of nuclear fusion. Consider the quark-rearrangement reaction



where the quarks are indicated below each baryon. This is a fusion of two singly heavy baryons into a doubly heavy baryon and a nucleon.

The masses of all of the particles in reaction (1) are known and the energy release ΔE is 12 MeV, as shown in Table 1.

The exothermic reaction (1) is the quark-level analogue of the well known exothermic nuclear fusion reactions between the lightest nuclei, which contain two or three nucleons⁴, with quarks playing the part of the nucleons, hadrons playing the part of the nuclei and the doubly heavy baryon playing the part of ${}^4\text{He}$:



where D denotes a deuteron, T represents a triton and p stands for proton. Reaction (1) involves two hadrons with three quarks each, rather than two nuclei with two or three nucleons each, as shown schematically in Fig. 1, which also depicts the analogous reactions $A_Q A_{Q'} \rightarrow \Xi_{QQ} N$, where $Q, Q' \in \{b, c\}$. The energy release ΔE of reaction (1) is of a similar order of magnitude to those of reactions (2).

Table 1 lists the ΔE values for four reactions $A_Q A_{Q'} \rightarrow \Xi_{QQ} N$, where $Q, Q' \in \{s, c, b\}$. The trend is clear: ΔE increases monotonically with increasing quark mass. The reaction



is endothermic with $\Delta E = -23$ MeV. Reaction (1) is exothermic with $\Delta E = +12$ MeV, whereas the reaction



is expected to be strongly exothermic with $\Delta E = +138 \pm 12$ MeV. Finally, the reaction



is expected to have $\Delta E = +50 \pm 13$ MeV, between the values for the cc and bb reactions (1) and (4). The latter two estimates of ΔE (for reactions (4) and (5)) rely on predictions of the Ξ_{bb} and Ξ_{bc} masses².

As already mentioned, the dominant effect that determines ΔE is the binding between two heavy quarks. Because these quarks interact through an effective two-body potential, their binding is determined by their reduced mass, $\mu_{\text{red}} = m_Q m_{Q'} / (m_Q + m_{Q'})$, where m_Q and $m_{Q'}$ are the masses of the individual quarks. In Fig. 2, we plot ΔE versus $\mu_{\text{red}}(QQ')$. The effective quark masses are as in ref. 2: $m_s = 538$ MeV, $m_c = 1,710.5$ MeV and $m_b = 5,043.5$ MeV. The straight-line fit $\Delta E = -44.95 + 0.0726\mu_{\text{red}}$ (dot-dashed line) describes the data well, which shows that, to a good approximation, ΔE depends linearly on the reduced mass.

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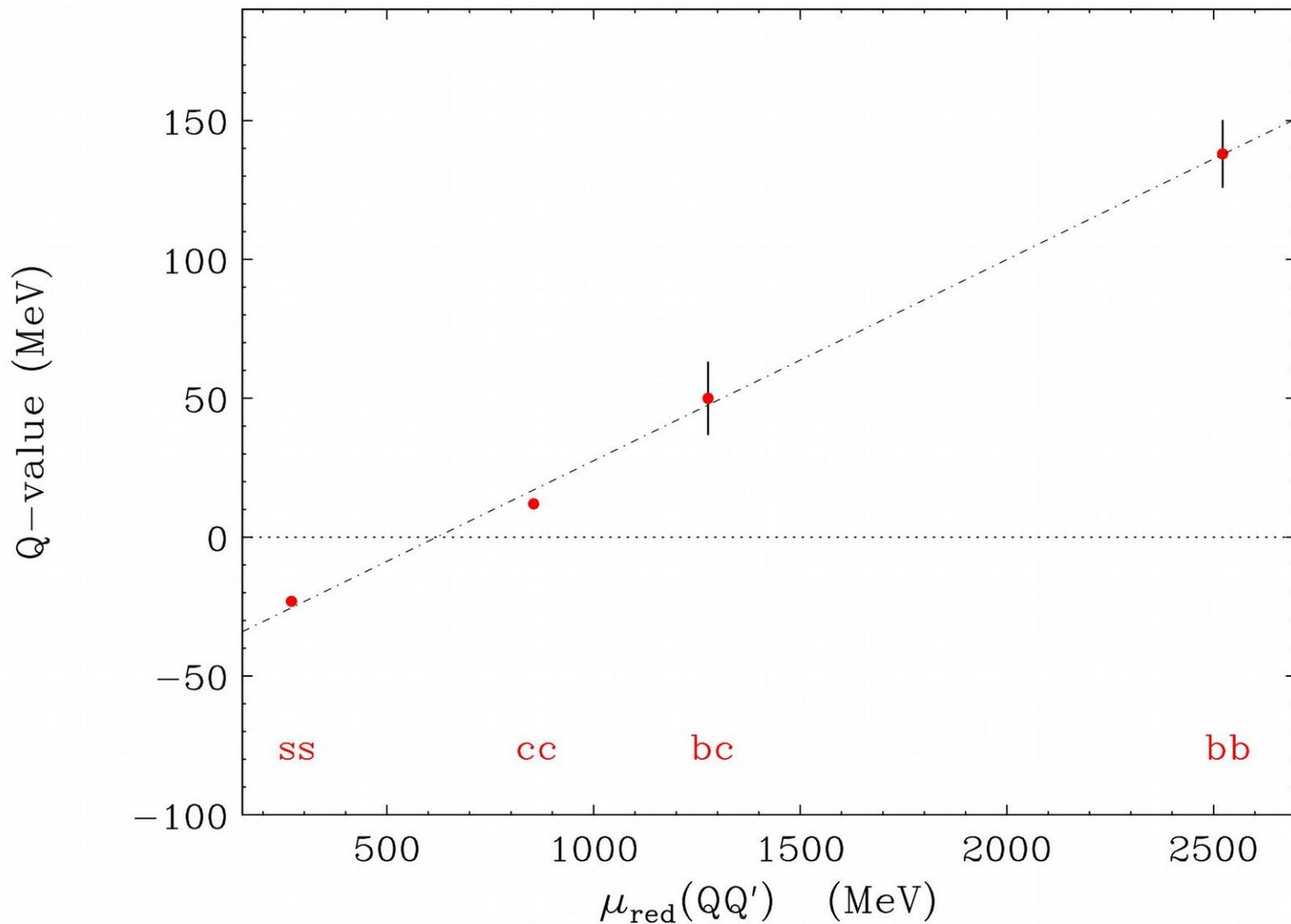
Table I
 Q value in the reaction $\Lambda_Q \Lambda_{Q'} \rightarrow \Xi_{QQ'} N$, $Q, Q' = s, c, b$.

Observable (MeV)	$Q, Q' = s$	$Q, Q' = c$	$Q, Q' = b$	$Q = b, Q' = c$
$M(\Lambda_Q)$	1115.7	2286.5	5619.6	5619.6, 2286.5
$M(\Xi_{QQ'})$	1314.9 ^a	3621.4 ± 0.78	10162 ± 12 ^b	6917 ± 13 ^c
Q -value	−23.1	$+12.0 \pm 0.78$	$+138 \pm 12$	$+50 \pm 13$

^aTo optimize the Q -value we take here $\Xi^0(ssu)$, $N=n$, because $M[\Xi^-(ssd)]$ is 7 MeV larger.

^b Ξ_{bb} mass prediction from Ref. [2].

^cAverage of the two values in Table XI of Ref. [2].



Q -value in the quark-level fusion reactions $\Lambda_Q \Lambda_{Q'} \rightarrow \Xi_{QQ'} N$, $Q, Q' = s, c, b$, plotted against the reduced masses of the doubly-heavy diquarks $\mu_{\text{red}}(QQ')$. The dot-dashed line denotes a linear fit $Q = -44.95 + 0.0726 \mu_{\text{red}}$.

doubly-strange hypernuclei @ JPARC,
cf. Tuesday plenary by Hirokazu Tamura

$s \Rightarrow b$ analogue ?

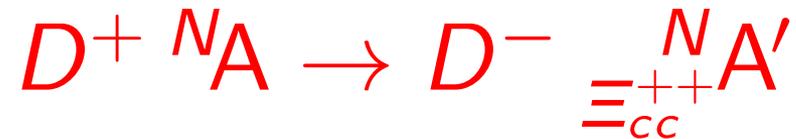
$E(bb) \approx 280 \text{ MeV} \Rightarrow$ v. high Q -value

extremely challenging exp:

$$\tau(B^-) = 1.6 \times 10^{-12} \text{ s},$$

$$\tau(B^-) \cdot c \approx 0.5 \text{ mm}$$

Maybe also charm analogue



both bottom and charm
in heavy ion collisions ?

Possible similar mechanisms in DM sector

QCD-like theories w. confined “dark quarks” \tilde{q}, \tilde{Q}
 $m_{\tilde{q}} \lesssim \Lambda_{\widetilde{QCD}}$, $m_{\tilde{Q}}$ v. large

in many scenarios \tilde{Q} stable, unlike Q in SM

\Rightarrow *stable* tightly-bound $\tilde{Q}\tilde{Q}\tilde{q}$

\Rightarrow chain reaction involving \tilde{Q} -level fusion

SUMMARY

- narrow exotics with $Q\bar{Q}$:
 $\bar{D}D^*$, \bar{D}^*D^* , $\bar{B}B^*$, \bar{B}^*B^* , $\Sigma_c\bar{D}^*$ molecules
- *heavy deuterons*: $\Sigma_c D^*$: LHCb $P_c(4450) \Rightarrow$ photoproduction
 $\Sigma_c B^*$, $\Sigma_b \bar{D}^*$, $\Sigma_b B^*$
- doubly charmed baryon found exactly where predicted
 $\Xi_{cc}^{++}(ccu) \Rightarrow (bcq), (bbq)$
- *stable $bb\bar{u}\bar{d}$ tetraquark*: LHCb!
- $cc\bar{c}\bar{c}$ @ $6,192 \pm 25$ MeV, $bb\bar{b}\bar{b}$ @ $18,826 \pm 25$ MeV $\Rightarrow 4\ell$
- *quark-level analogue of nuclear fusion*
- possible similar mechanisms in dark matter sector

exciting new spectroscopy awaiting discovery