



# Higgs boson decay into four bottom quarks in the SM and beyond

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1905.04865, JG

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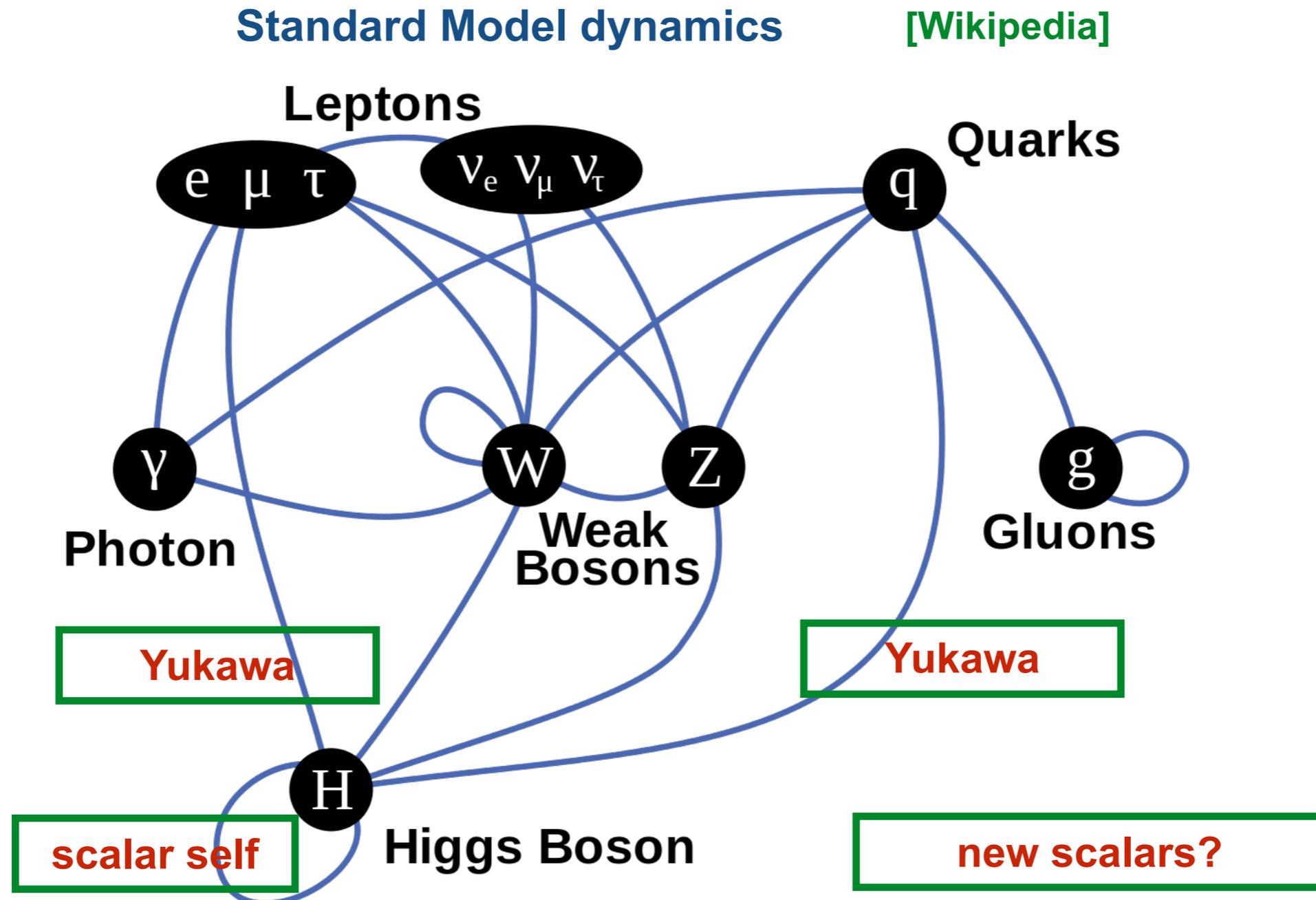
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# Post Higgs boson Era

- Study on properties of the Higgs boson including looking for further extensions has been one of the high priority in the next few decades

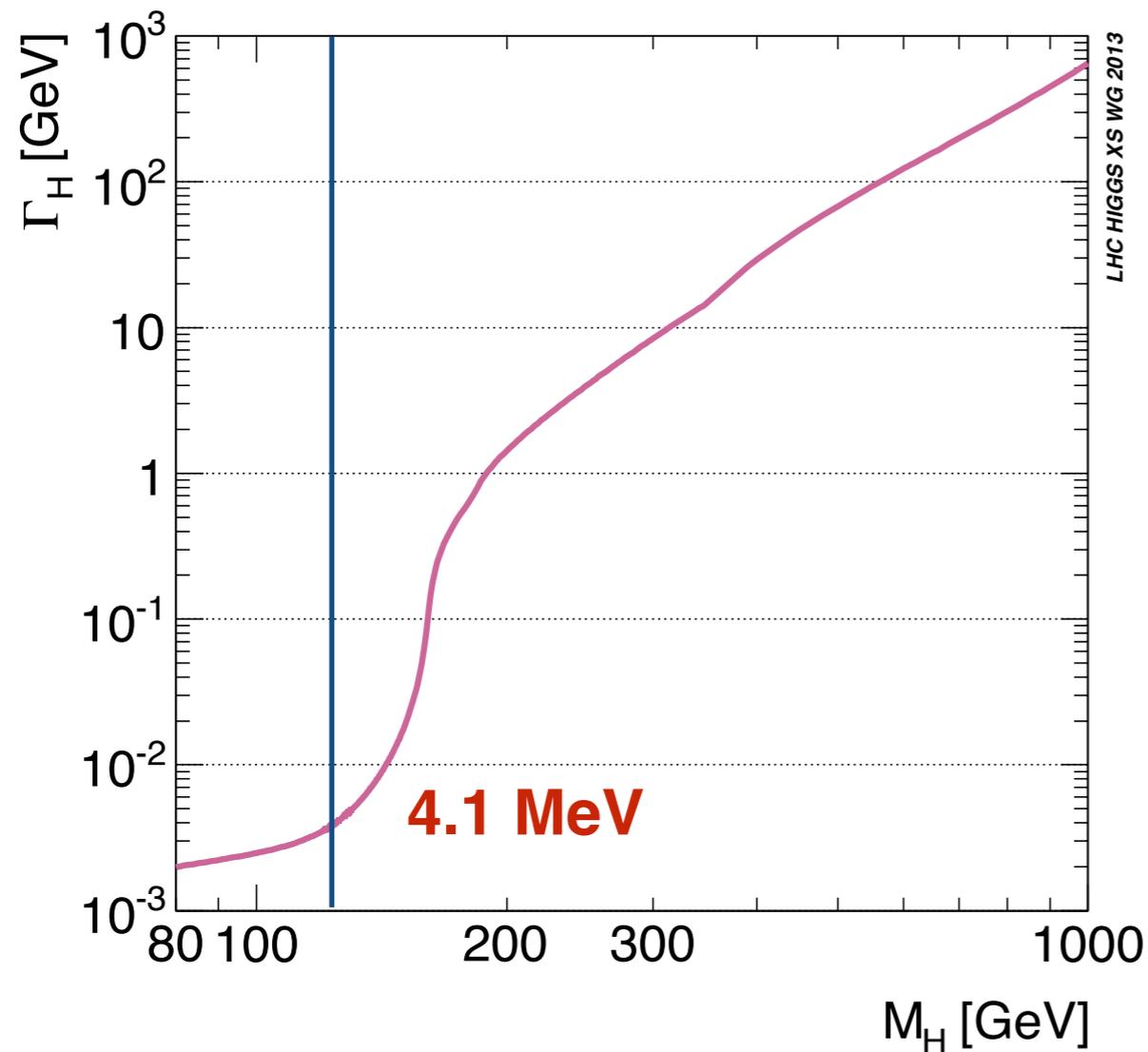


- ★ Higgs boson introduces new phenomenas for study of elementary particles, spin-0 particle, scalar self interactions, Yukawa interactions

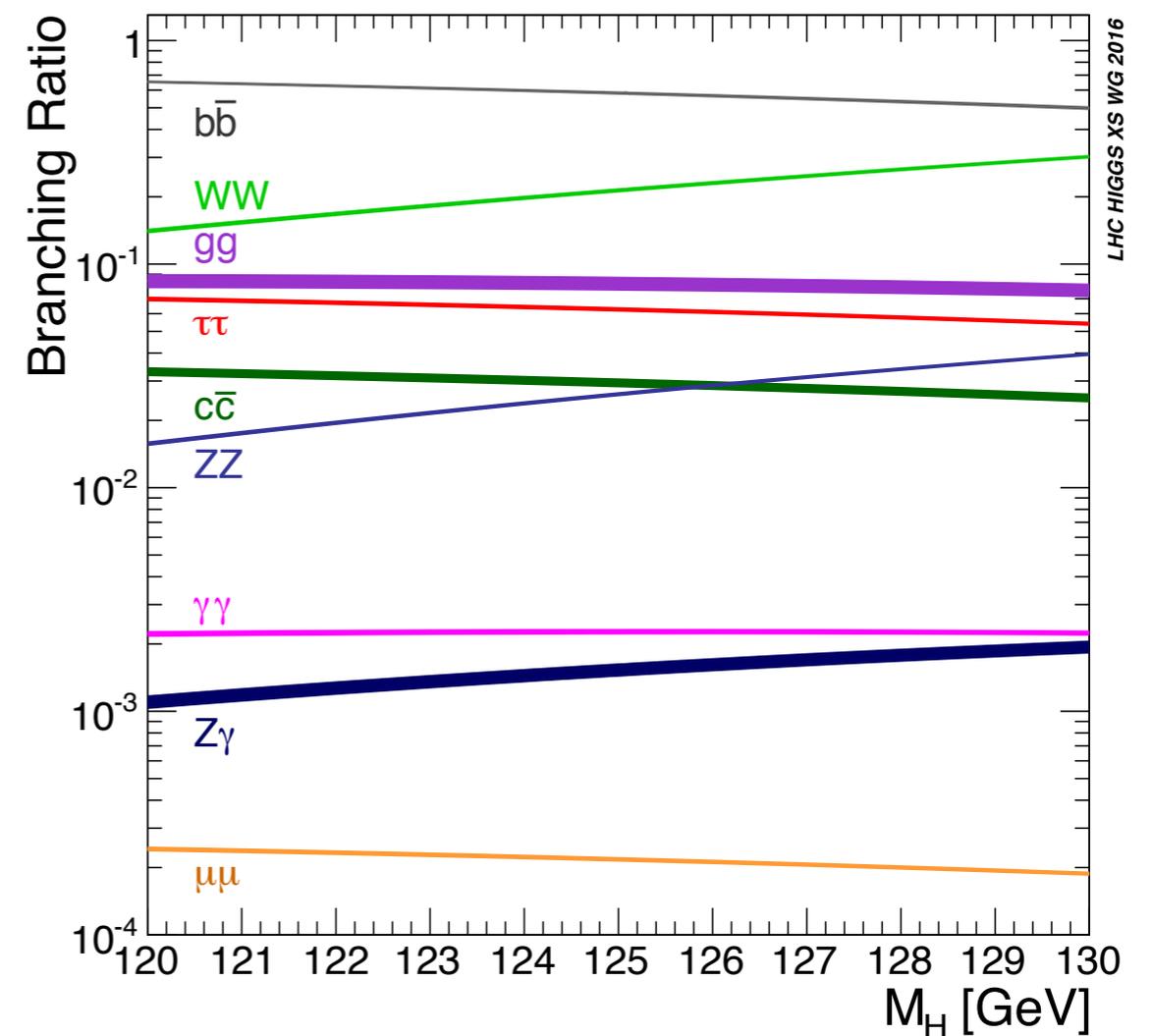
# Decays of the Higgs boson

- ◆ Higgs boson with a mass of 125 GeV decays dominantly to bottom quark pair via Yukawa  $y_b \sim 0.01$  resulting in small width  $\Gamma/m \sim 3 \times 10^{-5}$

total Width vs. mass



BRs vs. mass



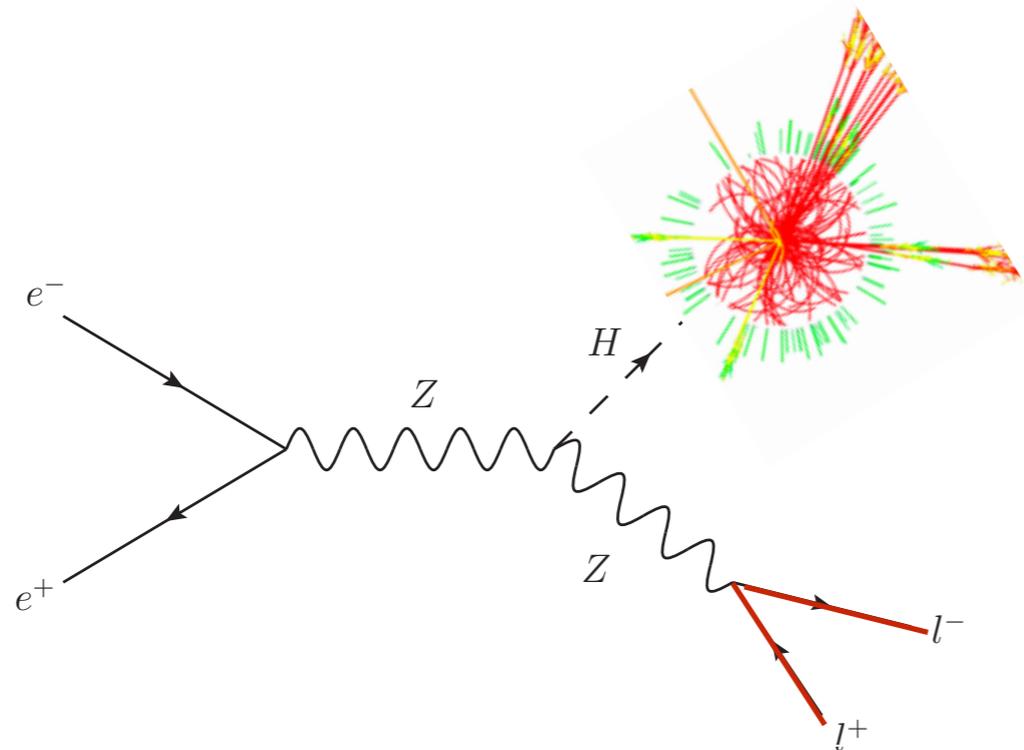
# Hadronic decays of the Higgs boson

- ◆ Higgs boson event of hadronic decays can be selected based on the recoil mass and be fully reconstructed

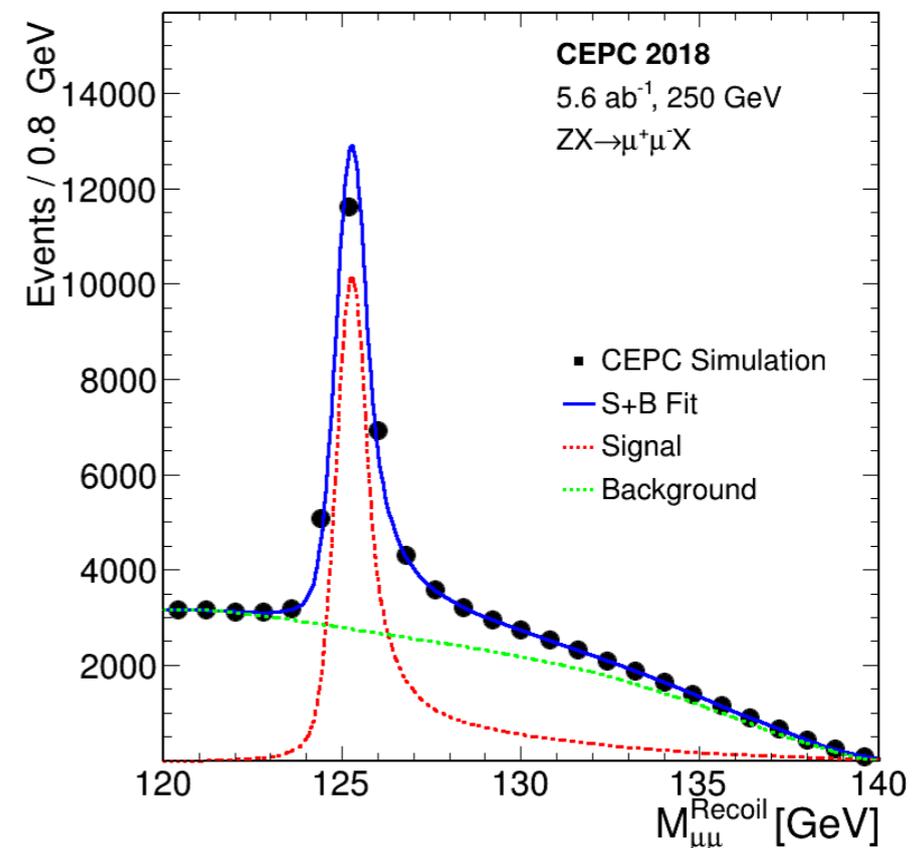
**SM event numbers assuming 250 GeV, 5 ab<sup>-1</sup> and Z to electrons and muons**

| $Z(l^+l^-)H(X)$ | $gg$ | $b\bar{b}$ | $c\bar{c}$ | $WW^*(4h)$ | $ZZ^*(4h)$ | $q\bar{q}$  |
|-----------------|------|------------|------------|------------|------------|-------------|
| $BR$ [%]        | 8.6  | 57.7       | 2.9        | 9.5        | 1.3        | $\sim 0.02$ |
| $N_{event}$     | 6140 | 41170      | 2070       | 6780       | 930        | 14          |

$$m_{recoil}^2 = s - 2E_{f\bar{f}}\sqrt{s} + m_{f\bar{f}}^2$$



- ★ full kinematic information allowing measurement of event shapes in Higgs rest frame



**[An + for CEPC, 2018]**

# Higgs measurements at CEPC

- ◆ CEPC Higgs factory can provide percent-level precision with model-independent measurement of various Higgs couplings

| Property                | Estimated Precision |         |
|-------------------------|---------------------|---------|
|                         | CEPC-v1             | CEPC-v4 |
| $m_H$                   | 5.9 MeV             | 5.9 MeV |
| $\Gamma_H$              | 2.7%                | 2.8%    |
| $\sigma(ZH)$            | 0.5%                | 0.5%    |
| $\sigma(\nu\bar{\nu}H)$ | 3.0%                | 3.2%    |

| Decay mode                            | $\sigma \times \text{BR}$ | BR      | $\sigma \times \text{BR}$ | BR      |
|---------------------------------------|---------------------------|---------|---------------------------|---------|
| $H \rightarrow b\bar{b}$              | 0.26%                     | 0.56%   | 0.27%                     | 0.56%   |
| $H \rightarrow c\bar{c}$              | 3.1%                      | 3.1%    | 3.3%                      | 3.3%    |
| $H \rightarrow gg$                    | 1.2%                      | 1.3%    | 1.3%                      | 1.4%    |
| $H \rightarrow WW^*$                  | 0.9%                      | 1.1%    | 1.0%                      | 1.1%    |
| $H \rightarrow ZZ^*$                  | 4.9%                      | 5.0%    | 5.1%                      | 5.1%    |
| $H \rightarrow \gamma\gamma$          | 6.2%                      | 6.2%    | 6.8%                      | 6.9%    |
| $H \rightarrow Z\gamma$               | 13%                       | 13%     | 16%                       | 16%     |
| $H \rightarrow \tau^+\tau^-$          | 0.8%                      | 0.9%    | 0.8%                      | 1.0%    |
| $H \rightarrow \mu^+\mu^-$            | 16%                       | 16%     | 17%                       | 17%     |
| $\text{BR}_{\text{inv}}^{\text{BSM}}$ | —                         | < 0.28% | —                         | < 0.30% |

[An + for CEPC, 2018]

- ★ different hadronic channels can be separated through jet identifications, e.g., heavy-flavor tagging, quark-gluon jet discrimination

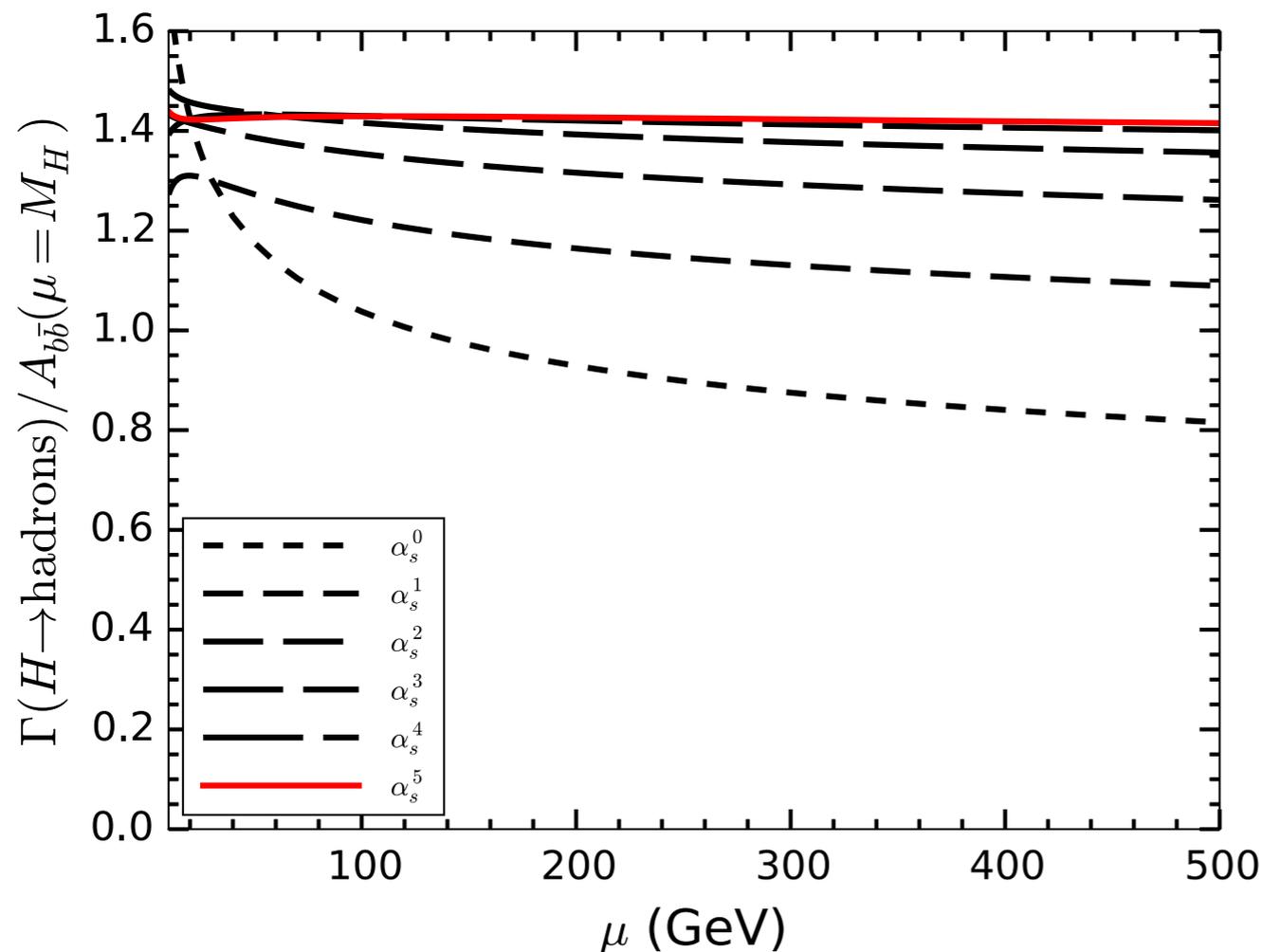
# Total hadronic decay width

- High precision theoretical predictions exist, full results known at  $O(\alpha_s^4)$ ; even higher order results exist for individual channels

## Higgs effective theory

$$\mathcal{L}_{\text{eff}} = -\frac{H^0}{v^0} (C_1[\mathcal{O}'_1] + C_2[\mathcal{O}'_2]) + \mathcal{L}'_{\text{QCD}} \quad \mathcal{O}'_1 = (G_{a,\mu\nu}^{0'})^2, \quad \mathcal{O}'_2 = m_b^{0'} \bar{b}^{0'} b^{0'}$$

$$\Gamma(H \rightarrow \text{hadrons}) = A_{b\bar{b}} [(C_2)^2 (1 + \Delta_{22}) + C_1 C_2 \Delta_{12}] + A_{gg} (C_1)^2 \Delta_{11}$$



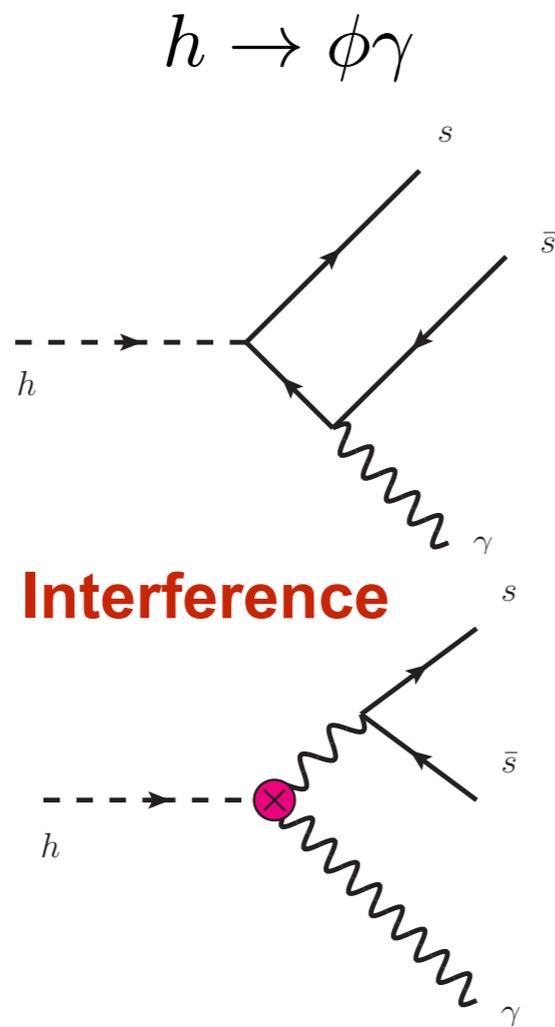
[Davies, Steinhauser, Wellmann, 2017]

[Herzog, Ruijl, Ueda, Vermaseren, Vogt, 2017]

# Exclusive hadronic decays

- Measuring Yukawa couplings of light-quarks at LHC are particularly challenging due to their smallness,  $y_s/y_b \sim 2\%$ , and huge QCD Bks

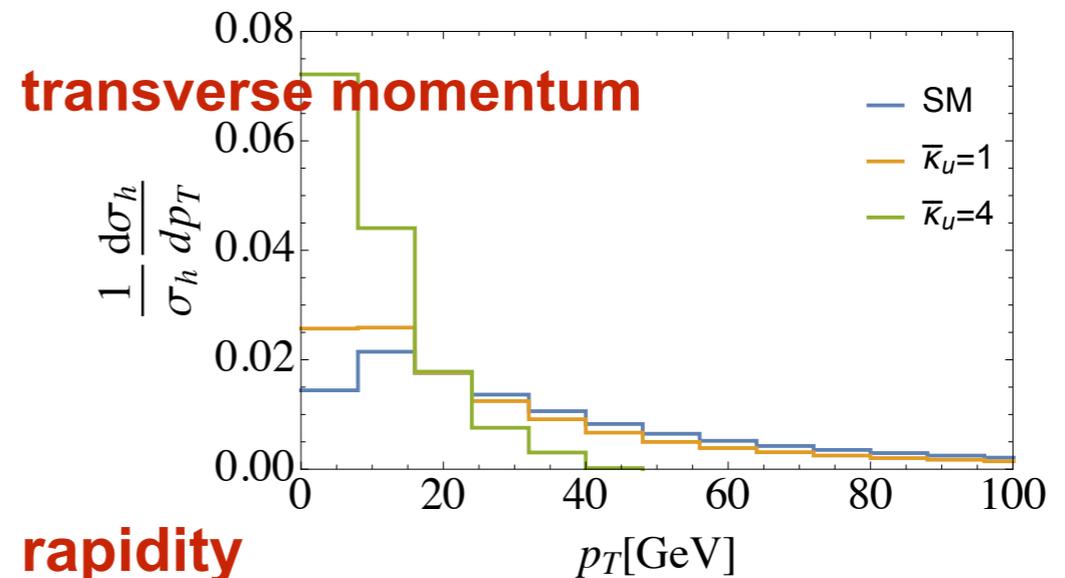
## exotic decays ( $BR \sim 10^{-6}$ )



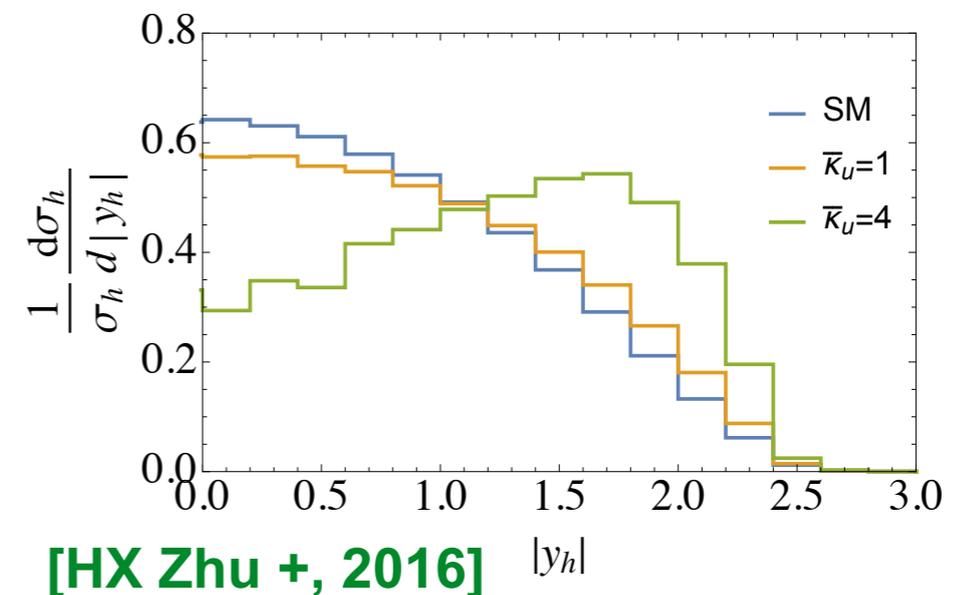
[Kagan +, 2014, 2016]

- ★ low sensitivity due to huge hadronic backgrounds

## Higgs kinematics



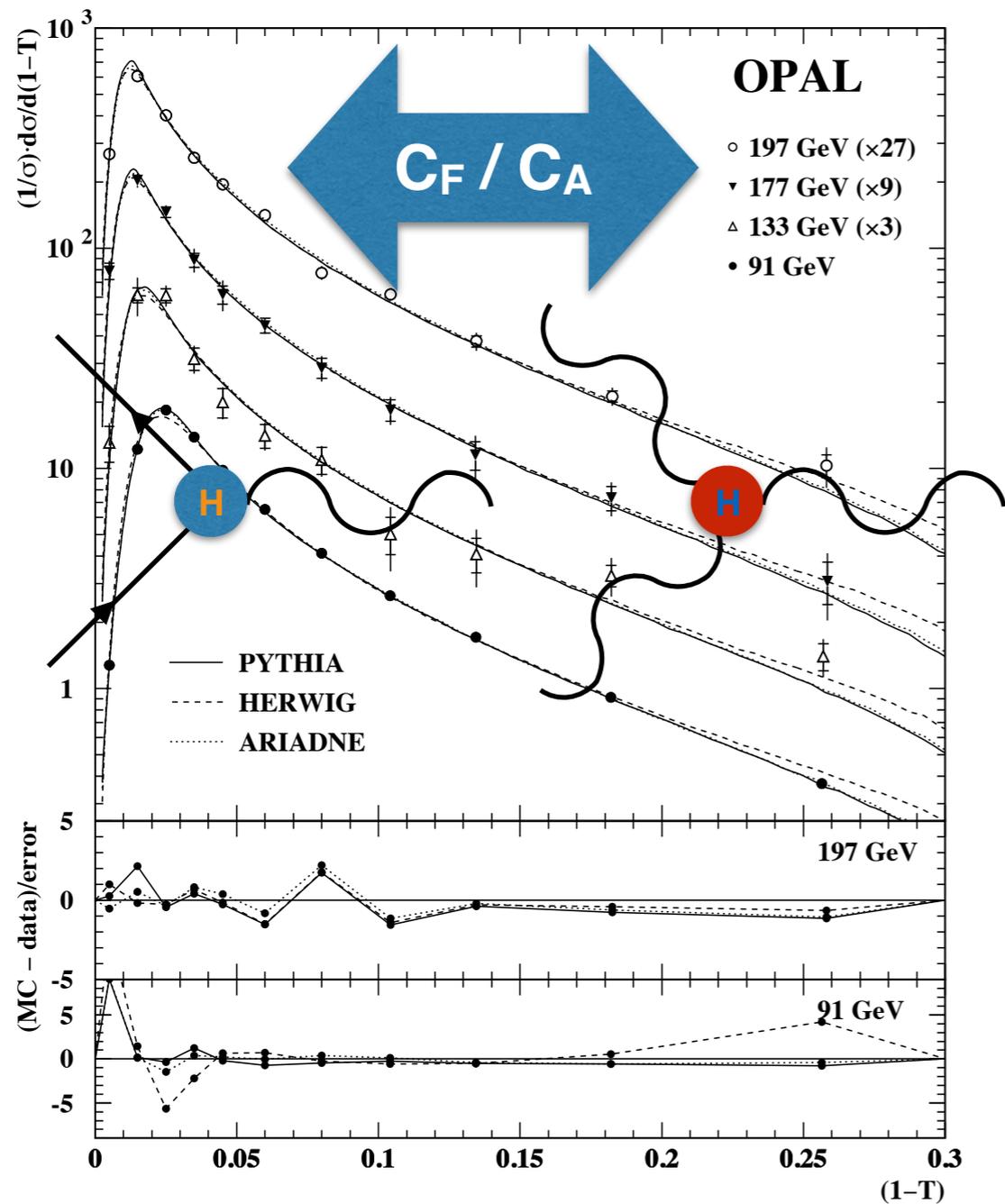
## rapidity



- ★ LHC/HL-LHC can probe Yukawa of u/d quarks to  $\sim 0.3 y_b$

# Exclusive hadronic decays

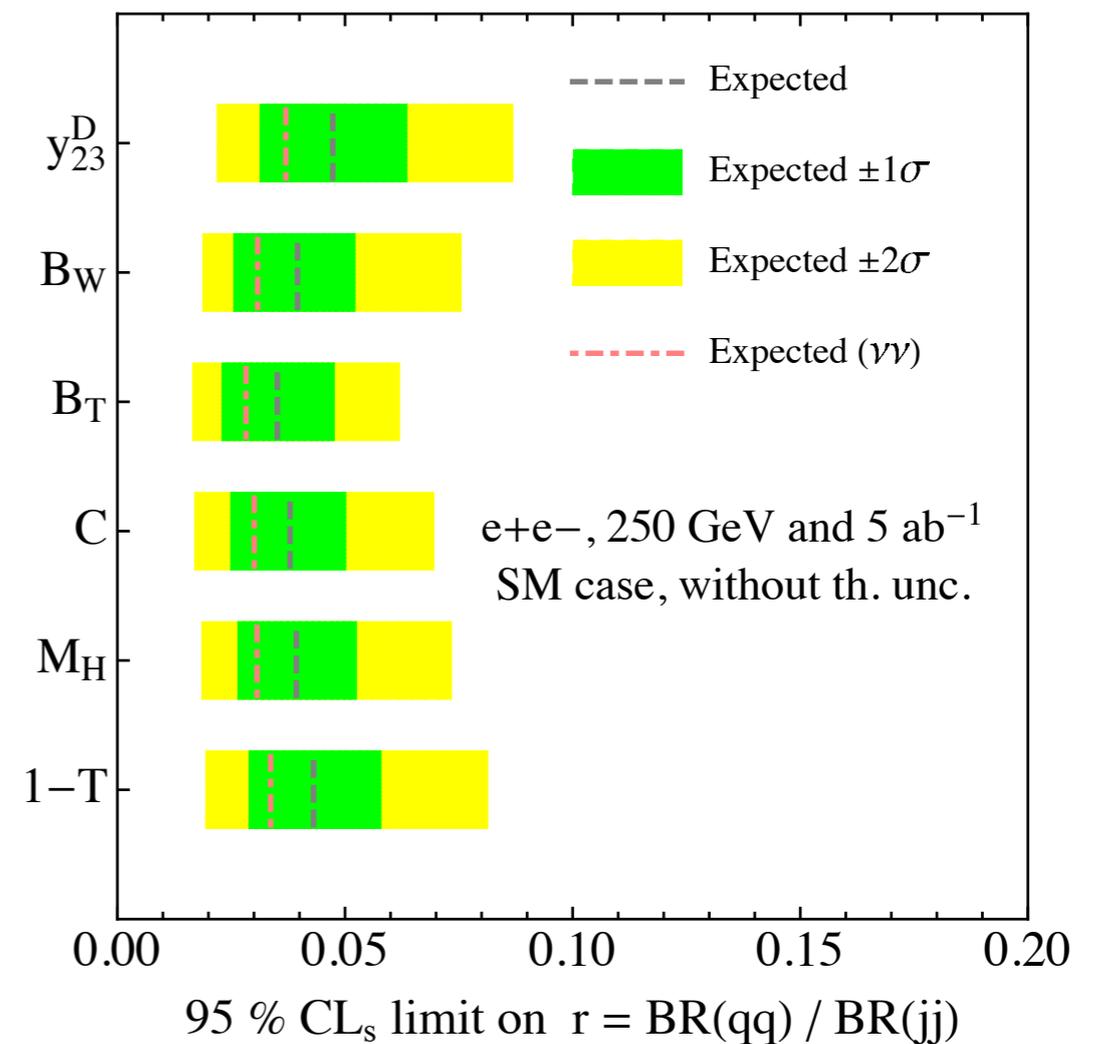
- Using hadronic event shapes to look for light-quark decay modes and Yukawa couplings; projected sensitivity for 250 GeV run with  $5 \text{ ab}^{-1}$



[OPAL, 2005]

**expected exclusion limit**

[JG, 1608.01746]

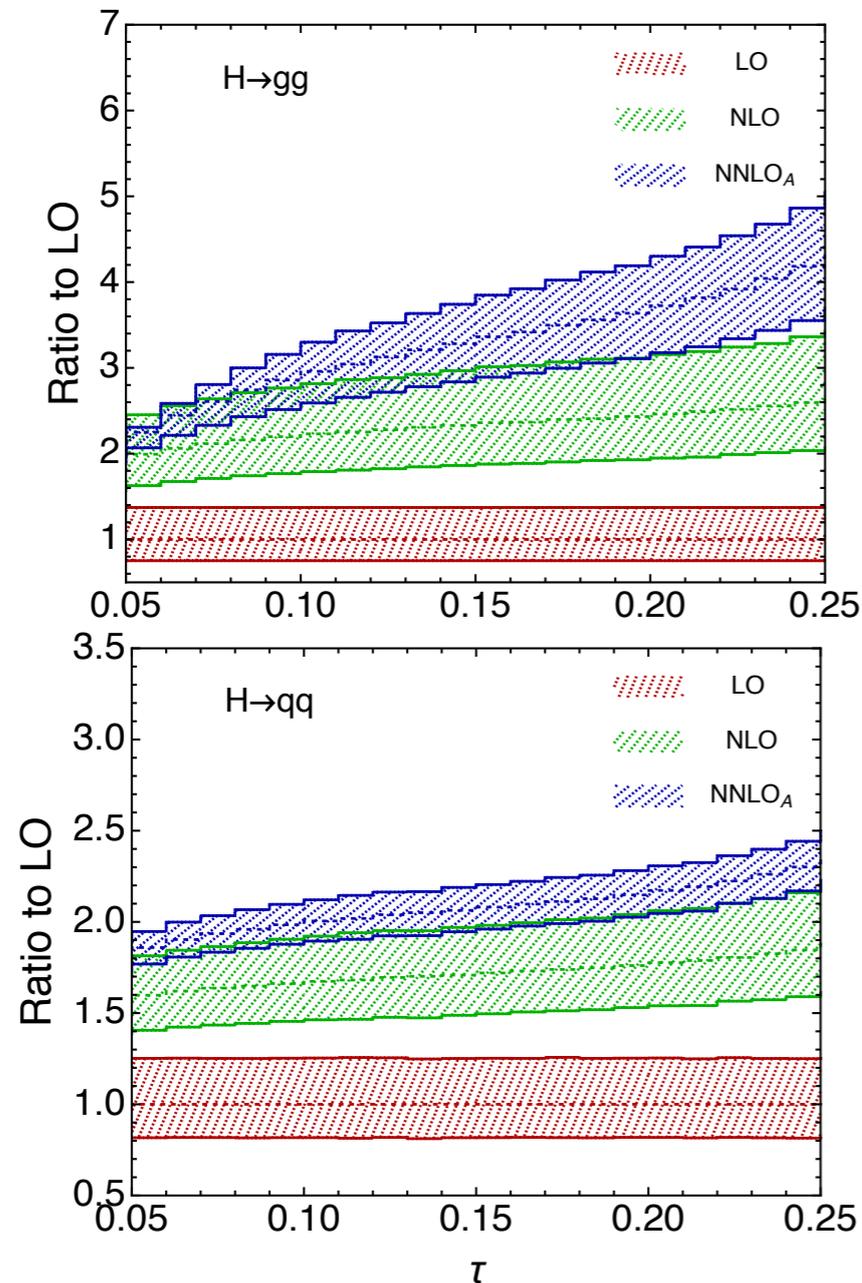


**from various event shapes**

# Improving theoretical prediction

- Works are in progress on improving theoretical predictions on event shapes in Higgs decay, NLO and beyond [JG, Gong, Ju, Yang, 2019]

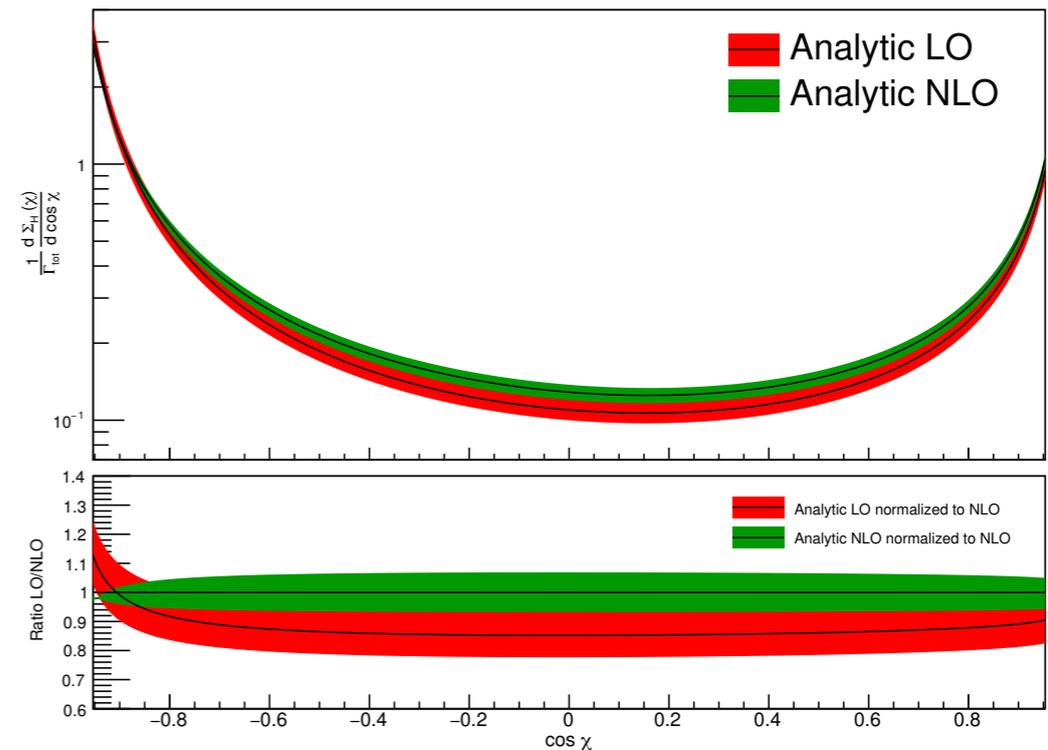
## thrust distribution



- ★ large QCD corrections similar to the inclusive decay

## energy-energy correlations

$$\frac{1}{\Gamma_{\text{tot}}} \frac{d\Sigma_H(\chi)}{d\cos\chi} = \sum_{a,b} \int \frac{2E_a E_b}{m_H^2} \delta(\cos\theta_{ab} - \cos\chi) d\Gamma_{a+b+X}$$



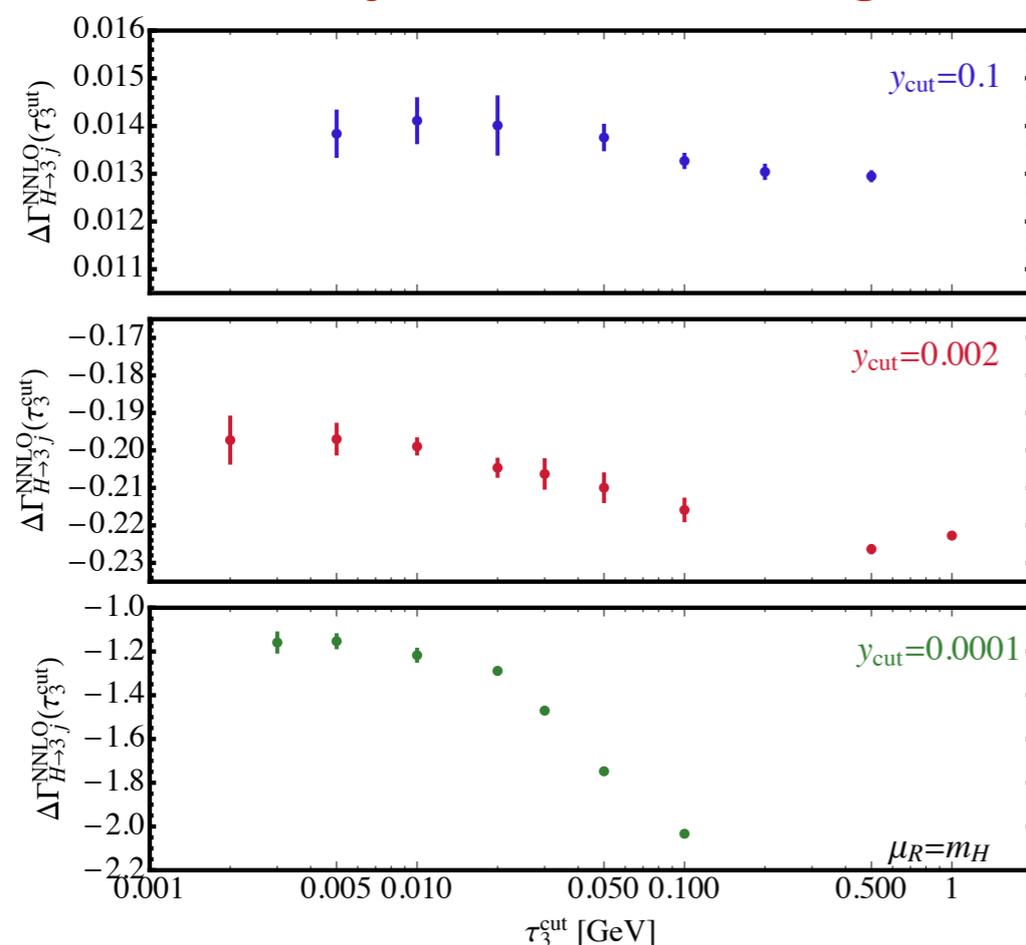
[Luo, Shtabovenko, Yang, Zhu, 2019]

- ★ NLO predictions in a compact analytic form, only di-gluon channel yet

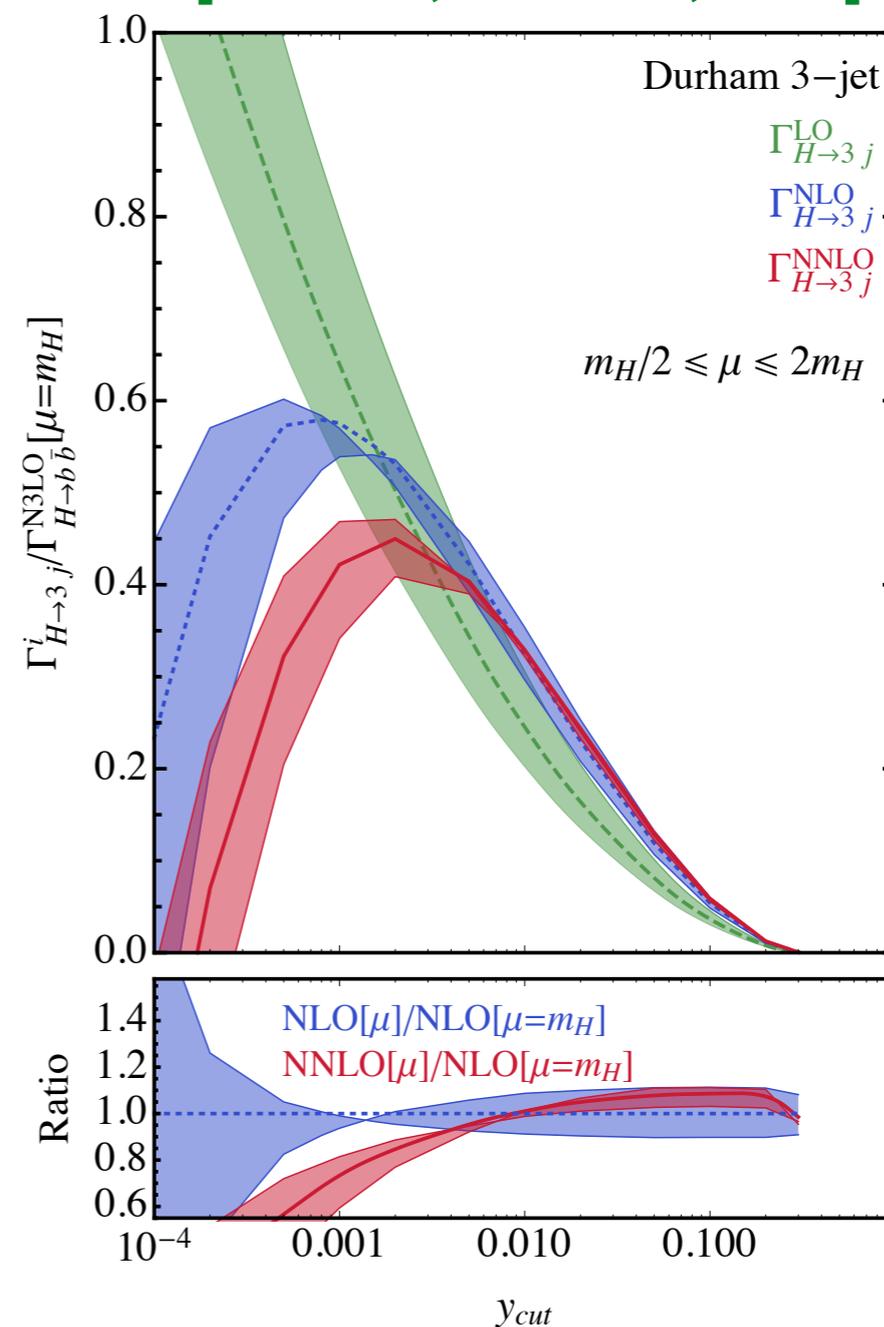
# Improving theoretical prediction

- Exact NNLO QCD corrections have been recently carried out for Higgs decaying into three-jet for the (massless) bottom quark channel

## 3-jettiness for slicing



[Mondini, Williams, 2019]



- phase space slicing method is now widely used for NNLO calculations in QCD

[Catani, Grazzini, 2007]

[JG, Li, Zhu, 2012]

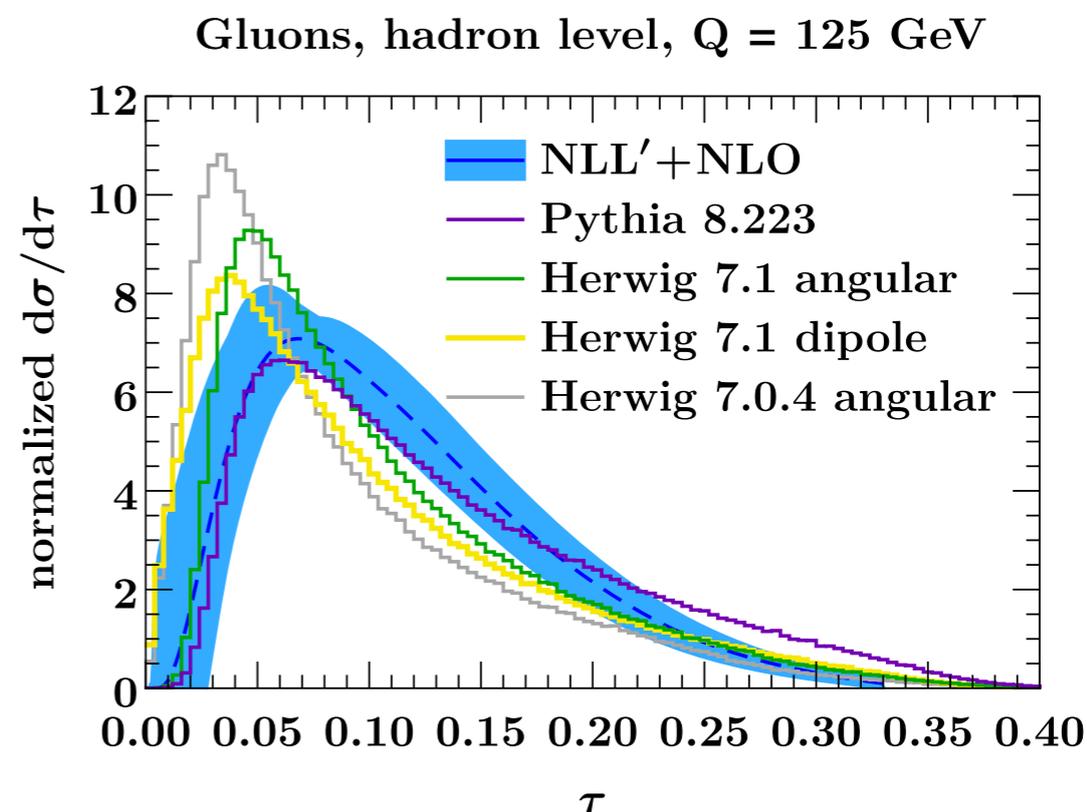
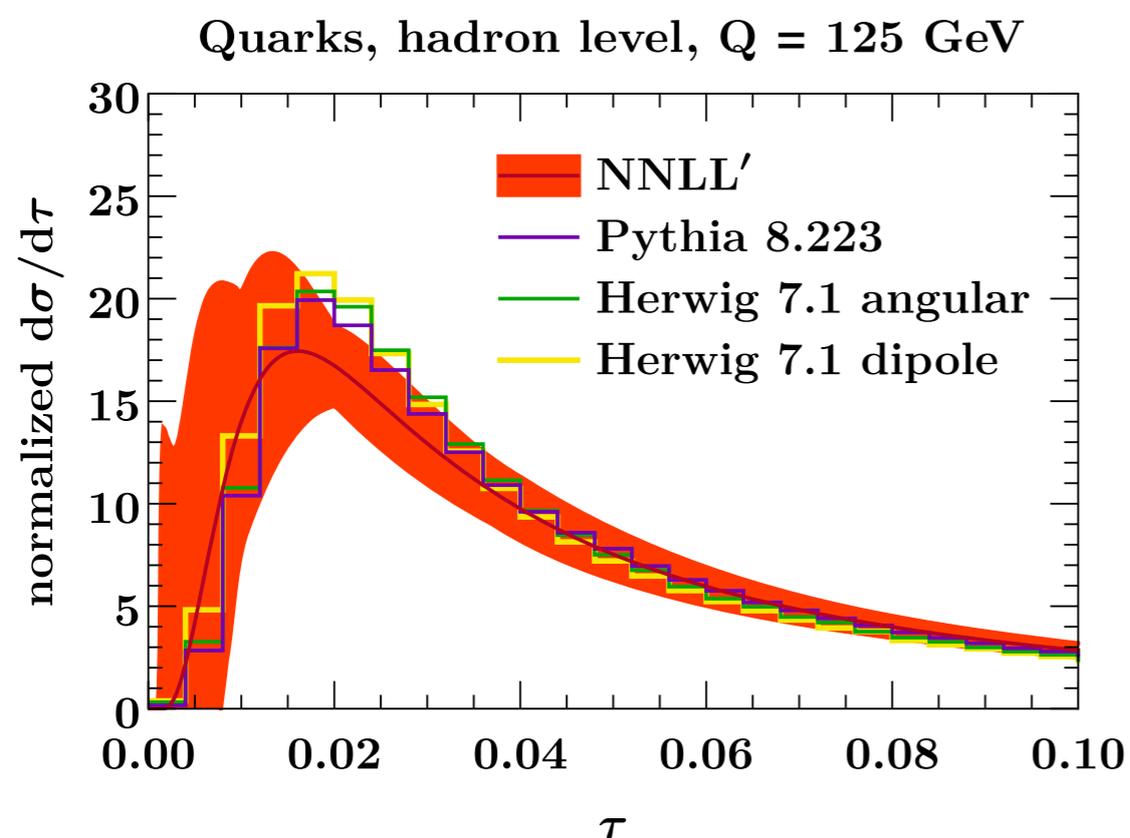
[Boughezal, Focke, Liu, Petriello, 2015]

- scale variations largely reduced at NNLO

# Improving theoretical prediction

- ◆ Dependence of the event shape distributions on hadronization effects via either MC or analytic models

[Mo, Tackmann, Waalewijn, 2017]



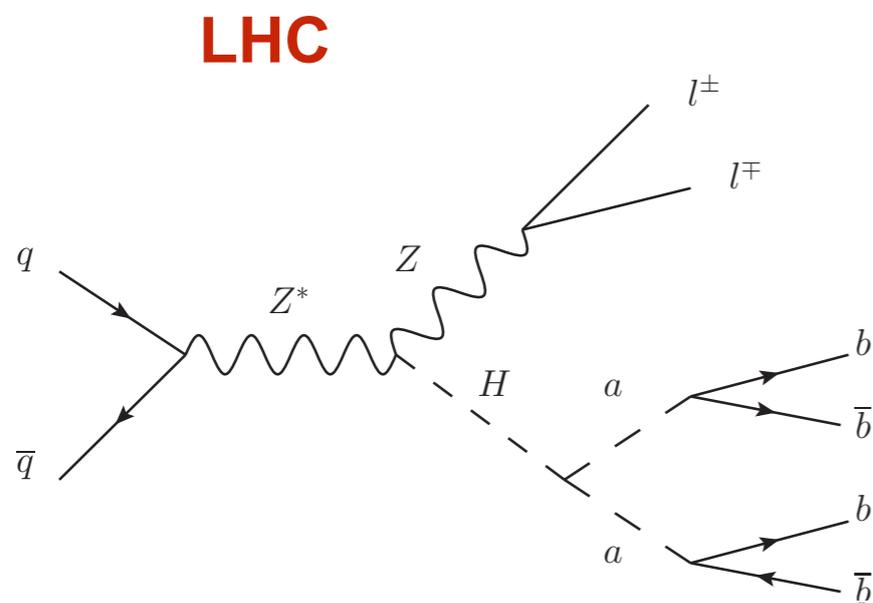
**thrust distribution (hadron level)**

- ★ Non-perturbative corrections are not well understood in general for case of quark-gluon jet discrimination

# Exotic hadronic decays

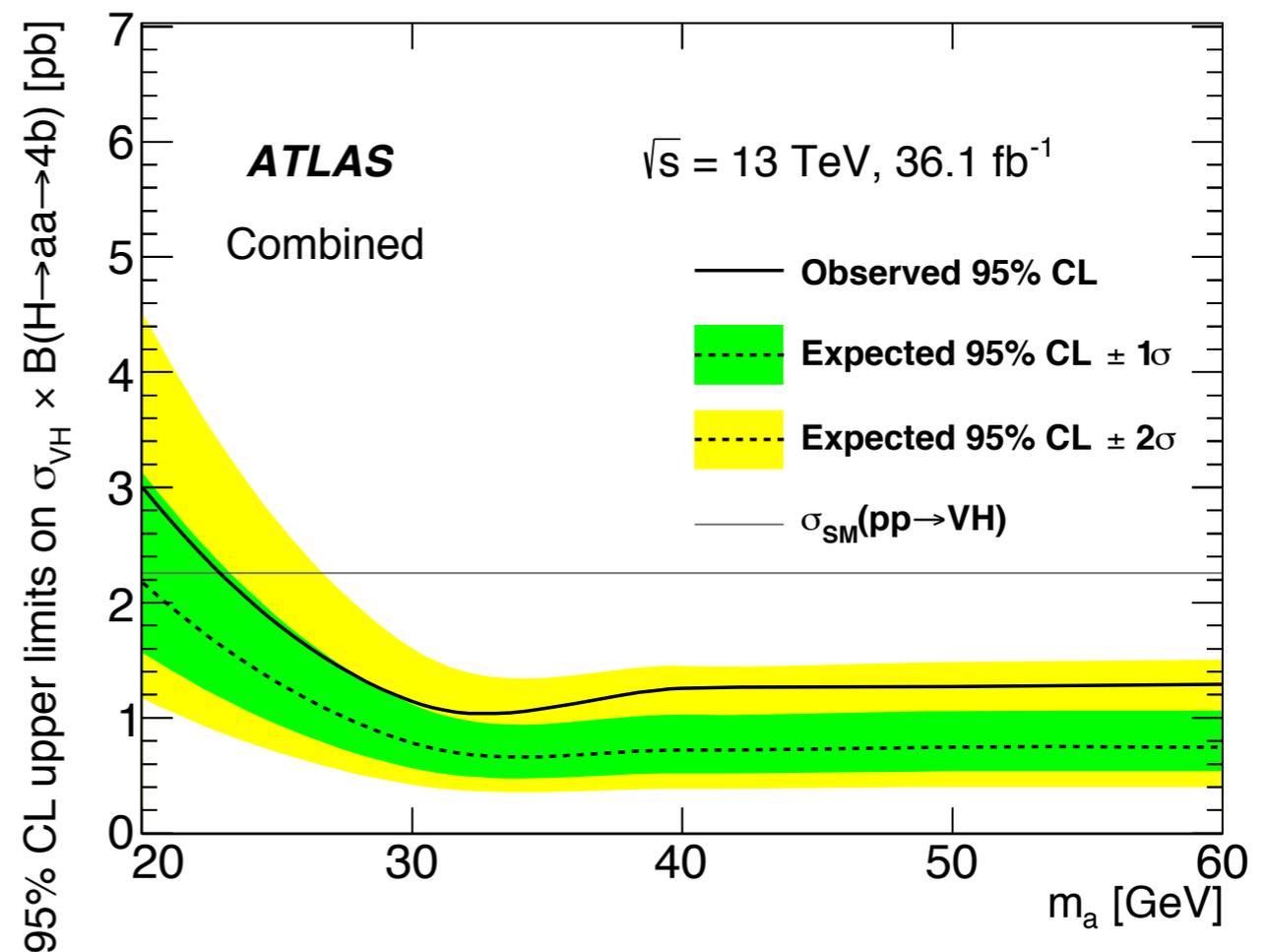
- Exotic hadronic decay modes can be explored directly at future electron-positron colliders, e.g., Higgs boson to four bottom quarks

## direct search of new light scalars



- ★ current LHC limit on BRs ( $H \rightarrow aa \rightarrow 4b$ ) at  $\sim 50\%$

[ATLAS, 1806.07355]



# Higgs boson to four bottom quarks in SM

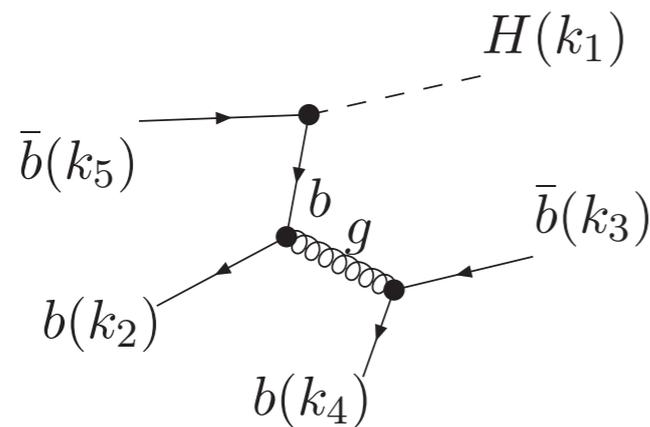
- ◆ A complete next-to-leading order calculation including both Yukawa and EW couplings with full bottom quark mass dependences

**exotic decay in the SM**

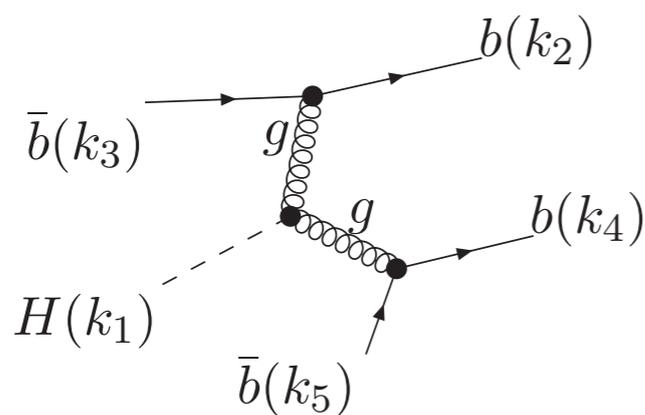
**[JG, 1905.04865]**

**Yukawa**

$$\Gamma_{4b,yuk} = \left( \frac{\alpha_S(\mu)}{2\pi} \right)^2 \left\{ A_{b\bar{b}} [\Delta_{b\bar{b}}(x)(1 + \delta_{b\bar{b}}(x)) C_2^2 + \Delta_{bg}(x)(1 + \delta_{bg}(x)) C_1 C_2] + A_{gg} [\Delta_{gg}(x)(1 + \delta_{gg}(x)) C_1^2] \right\},$$



$$A_{b\bar{b}} = \frac{3M_H}{8\pi v^2} \overline{m}_b^2(\mu), \quad A_{gg} = \frac{4M_H^3}{2\pi v^2}, \quad x = m_b^2/M_H^2,$$



$$\delta_{b\bar{b}}(x) = \frac{\alpha_S(\mu)}{2\pi} [(2\beta_0 + 3C_F) \ln(4\mu^2/M_H^2) + a_{b\bar{b}}(x)],$$

$$\delta_{bg}(x) = \frac{\alpha_S(\mu)}{2\pi} [(3\beta_0 + 3C_F) \ln(4\mu^2/M_H^2) + a_{bg}(x)],$$

$$\delta_{gg}(x) = \frac{\alpha_S(\mu)}{2\pi} [(4\beta_0) \ln(4\mu^2/M_H^2) + a_{gg}(x)].$$

- ★ mixing of operator  $O_1$  and  $O_2$

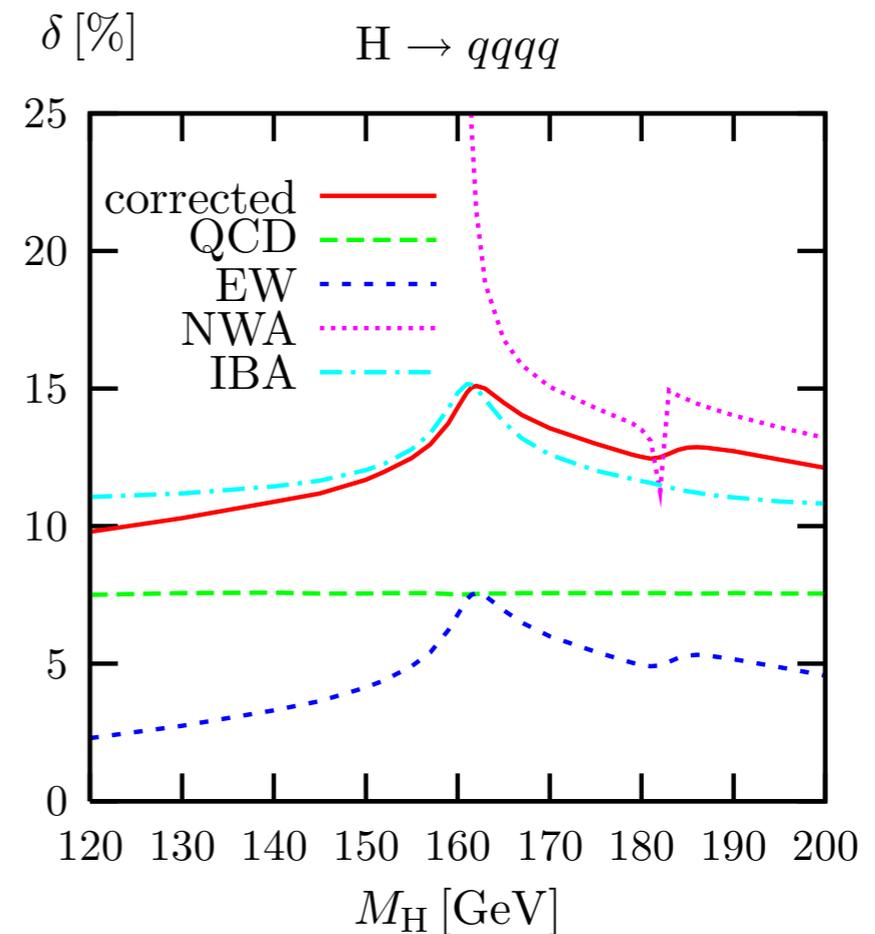
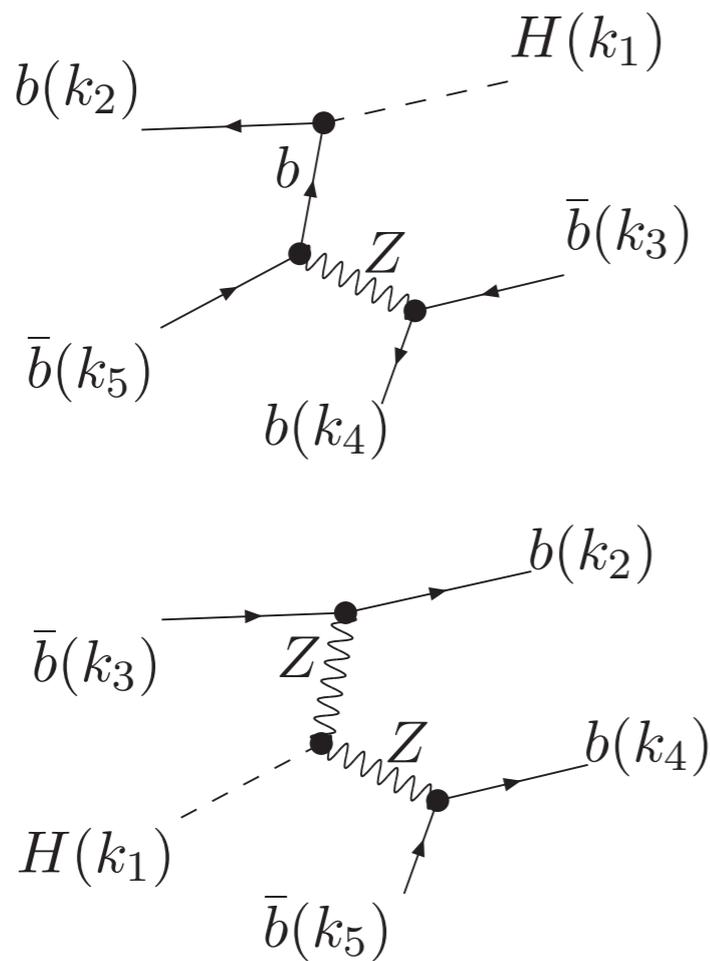
# Higgs boson to four bottom quarks in SM

- ◆ A complete next-to-leading order calculation including both Yukawa and EW couplings with full bottom quark mass dependences

**exotic decay in the SM**

**[JG, 1905.04865]**

**EW**  $\Gamma_{4b,ew} = A_{ZZ} \Delta_{ZZ}(x)(1 + \delta_{ZZ}(x)), \quad A_{ZZ} = \frac{32M_Z^4 M_H}{\pi^3 v^4}, \quad \delta_{ZZ} = \frac{\alpha_S(\mu)}{2\pi} [a_{ZZ}(x)].$



- ★ complex mass scheme  
**[Denner, Dittmaier+, 2005]**

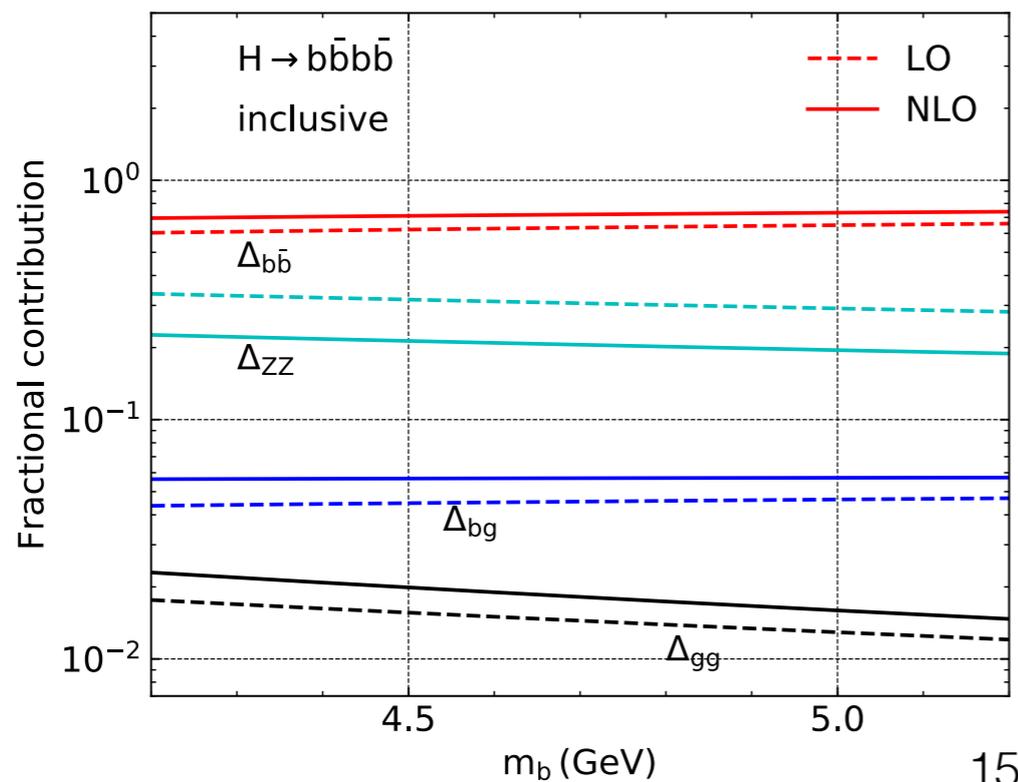
- ★ NLO QCD correction for massless quarks from PROPHECY4F **[Denner, Dittmaier+, 2006]**

# Higgs boson to four bottom quarks in SM

- ◆ A complete next-to-leading order calculation including both Yukawa and EW couplings with full bottom quark mass dependences

| $m_b$ (GeV) | $x$ ( $10^{-3}$ ) | $\Delta_{b\bar{b}}$ | $\Delta_{bg}$ | $\Delta_{gg}$ | $a_{b\bar{b}}$ | $a_{bg}$ | $a_{gg}$ | $\Delta_{ZZ}$ | $a_{ZZ}$ |
|-------------|-------------------|---------------------|---------------|---------------|----------------|----------|----------|---------------|----------|
| 4.2         | 1.129             | 7.32                | -144.0        | 1.160         | 45.2           | 56.9     | 57.8     | 0.1222        | 5.64     |
| 4.4         | 1.239             | 6.80                | -133.3        | 1.094         | 45.2           | 56.0     | 56.7     | 0.1205        | 5.80     |
| 4.6         | 1.354             | 6.32                | -123.4        | 1.032         | 45.1           | 55.2     | 55.7     | 0.1188        | 5.97     |
| 4.8         | 1.474             | 5.89                | -114.7        | 0.976         | 45.0           | 54.5     | 54.8     | 0.1170        | 6.14     |
| 5.0         | 1.600             | 5.49                | -106.7        | 0.922         | 44.9           | 53.8     | 53.9     | 0.1152        | 6.32     |
| 5.2         | 1.730             | 5.13                | -99.4         | 0.873         | 44.9           | 53.2     | 53.2     | 0.1133        | 6.50     |

- ★ Bottom mass (pole) dependence, at LO and for the NLO QCD corrections

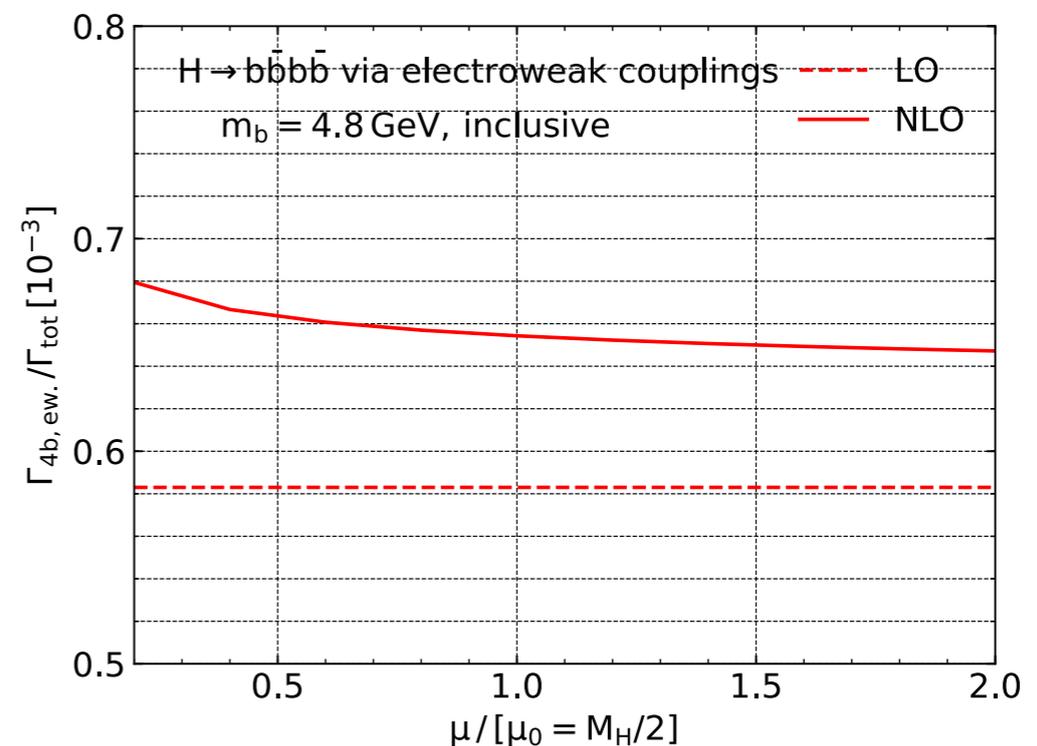
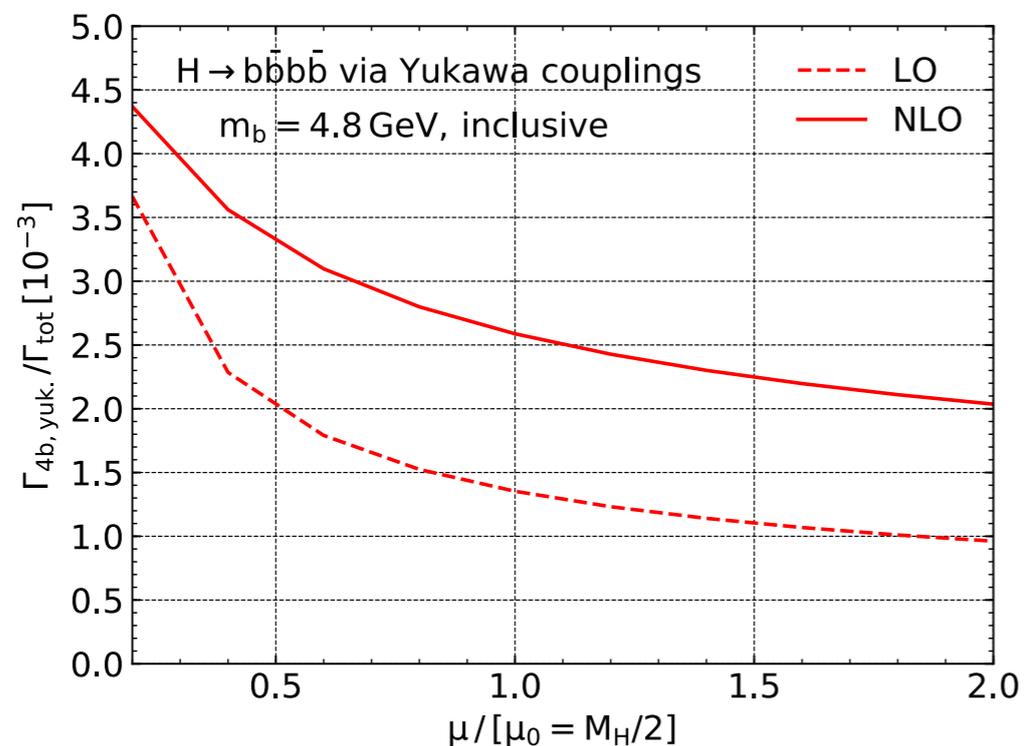


- ★ SM predictions on BRs( $H \rightarrow 4b$ ) at  $\sim 0.3\%$  with large QCD corrections; and dominated by Yukawa interactions

# Higgs boson to four bottom quarks in SM

- ◆ A complete next-to-leading order calculation including both Yukawa and EW couplings with full bottom quark mass dependences

## QCD scale variations



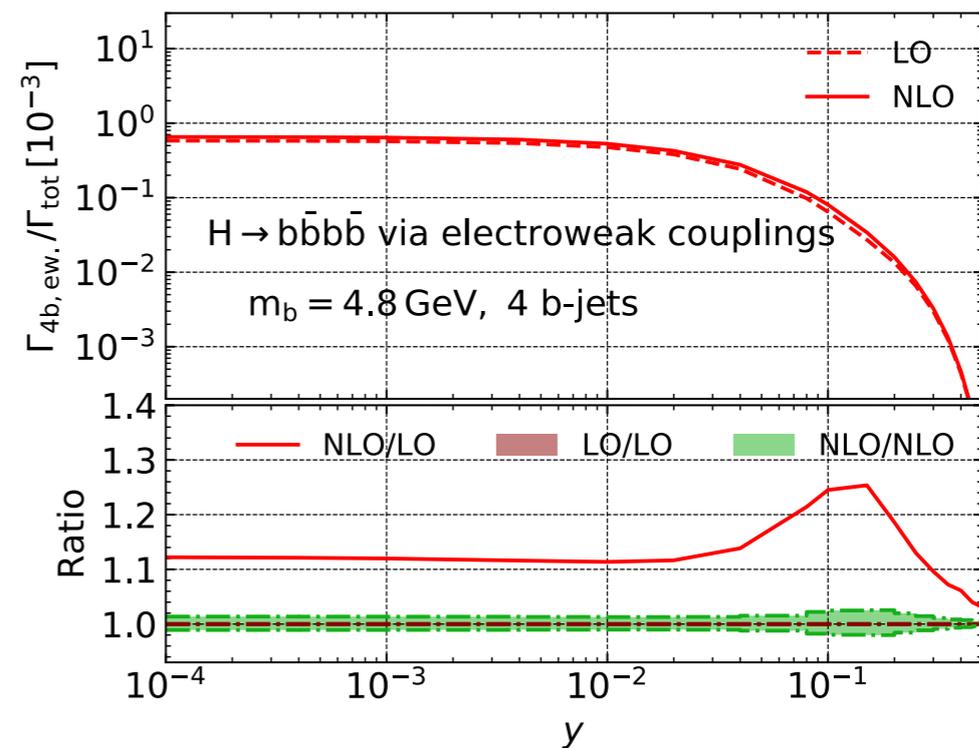
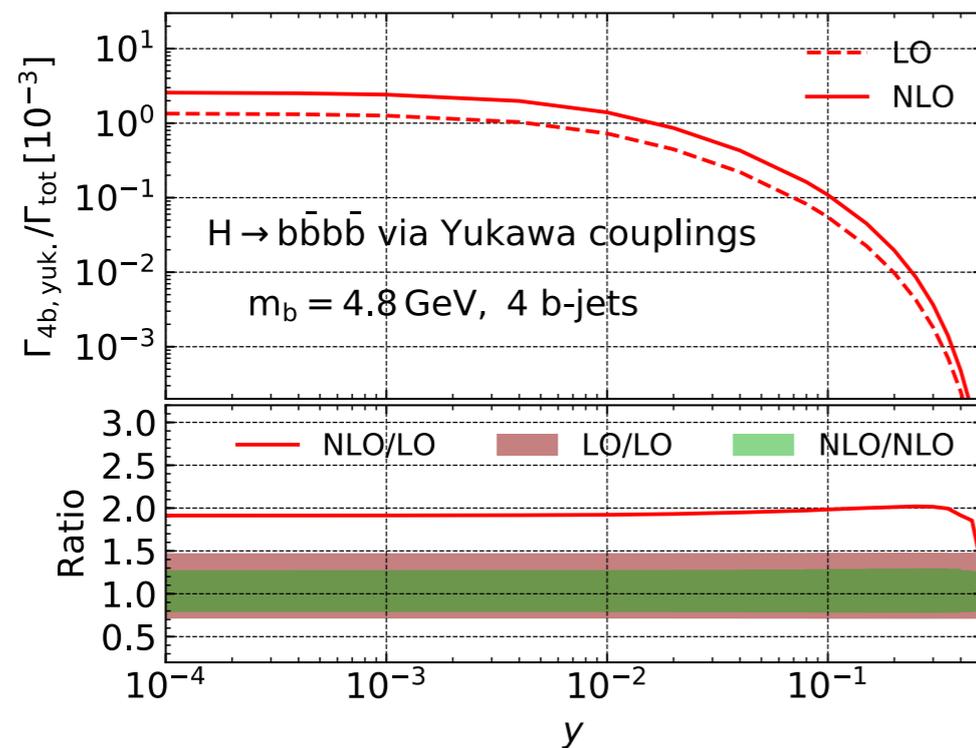
- ★ QCD scale dependence is reduced though still significant for decay via Yukawa interactions,  $\sim 25\%$

# Jet cross sections

- ✦ Jet cross sections by requiring at least four b-tagged jets in the final state with e+e- k<sub>T</sub> algorithm

**k<sub>T</sub> algorithm**

$$d_{ij} = \frac{2 \min(E_i^2, E_j^2)}{Q^2} (1 - \cos \theta_{ij}) \quad Q^2 = M_H^2/4$$

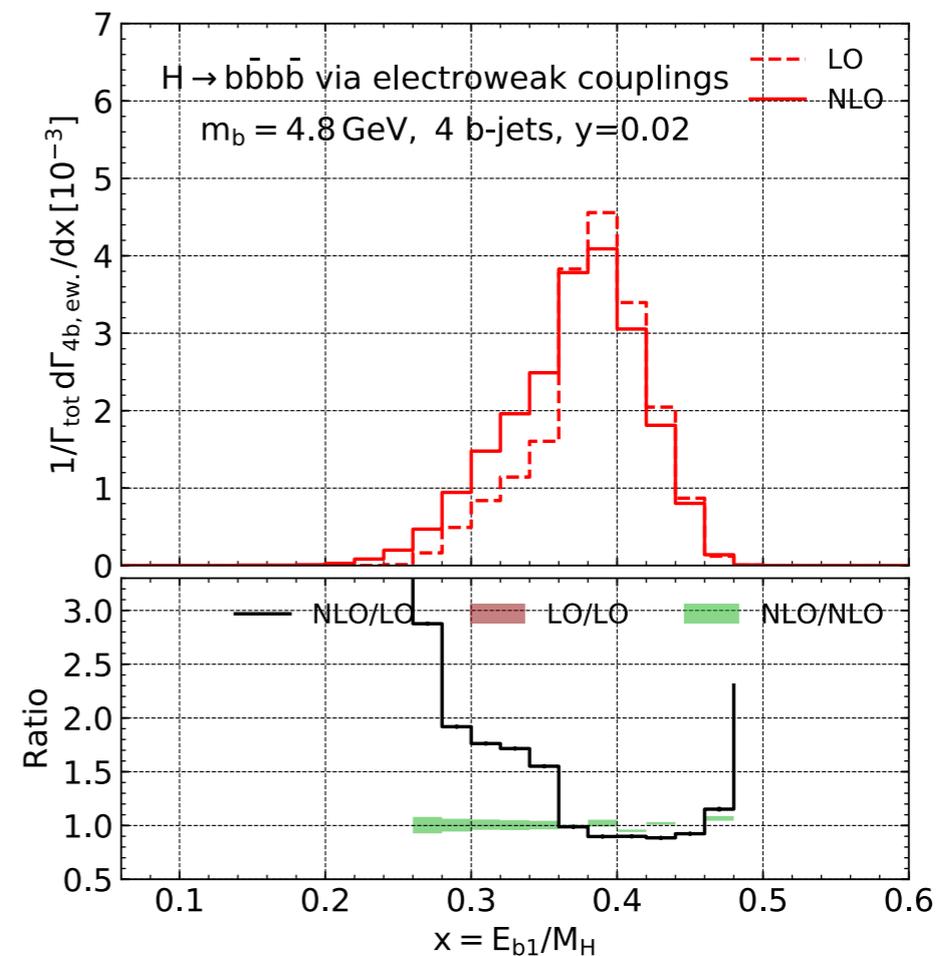
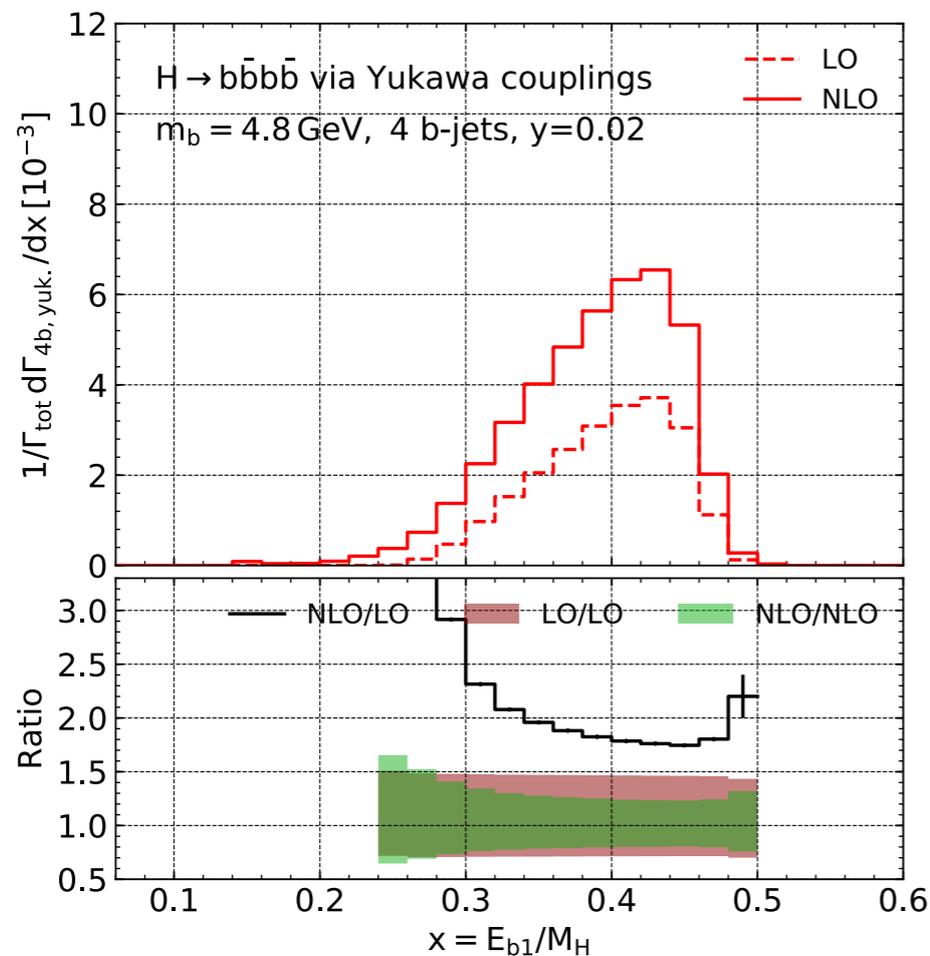


- ★ partial width as a function of the jet resolution parameter  $y$ ;  $y=0.02$  corresponds to an opening angle of about 0.3(17 degrees)

# Event topology

- Four b-jets are ordered by energy; kinematic distributions are constructed for individual jet and jet pairs

## energy of the leading b-jet

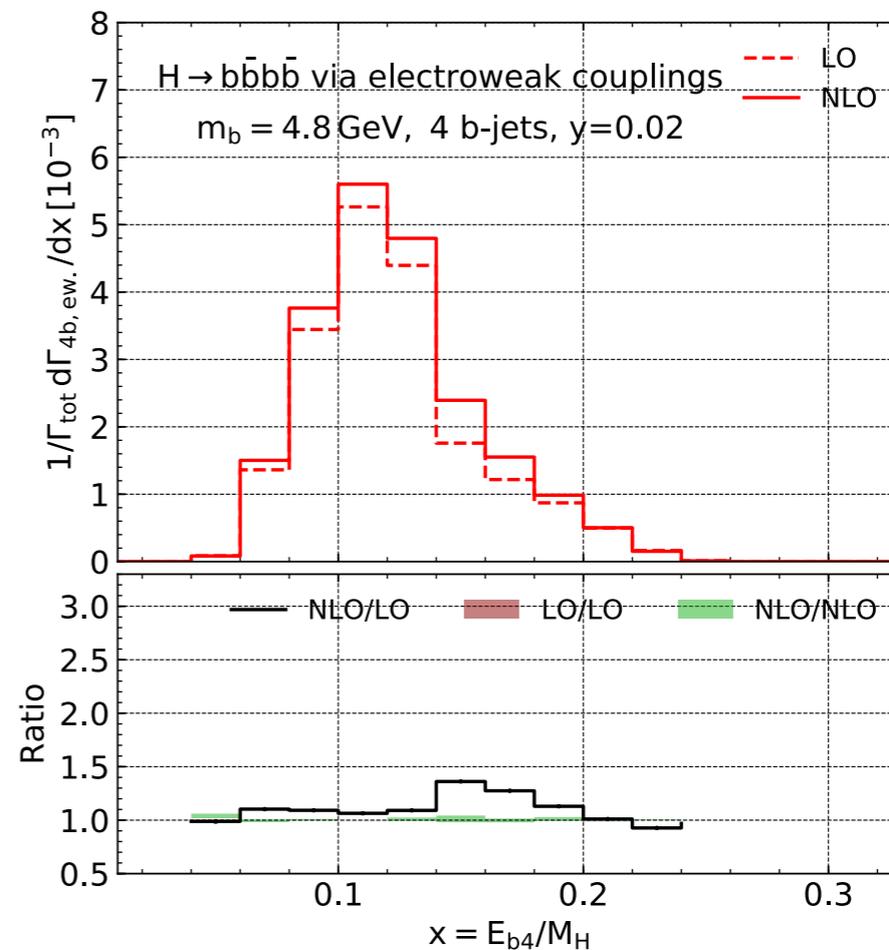
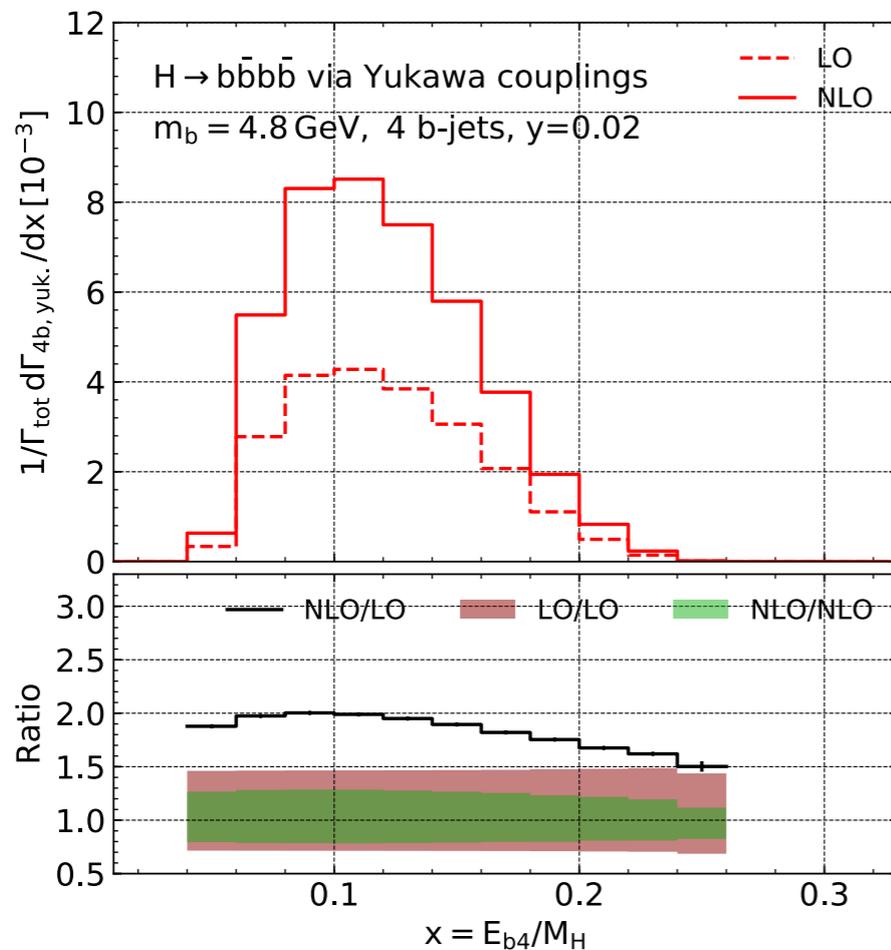


- ★ spectrum are harder and broader for decay via Yukawa couplings; QCD corrections change the shapes in different ways

# Event topology

- Four b-jets are ordered by energy; kinematic distributions are constructed for individual jet and jet pairs

## energy of the softest b-jet

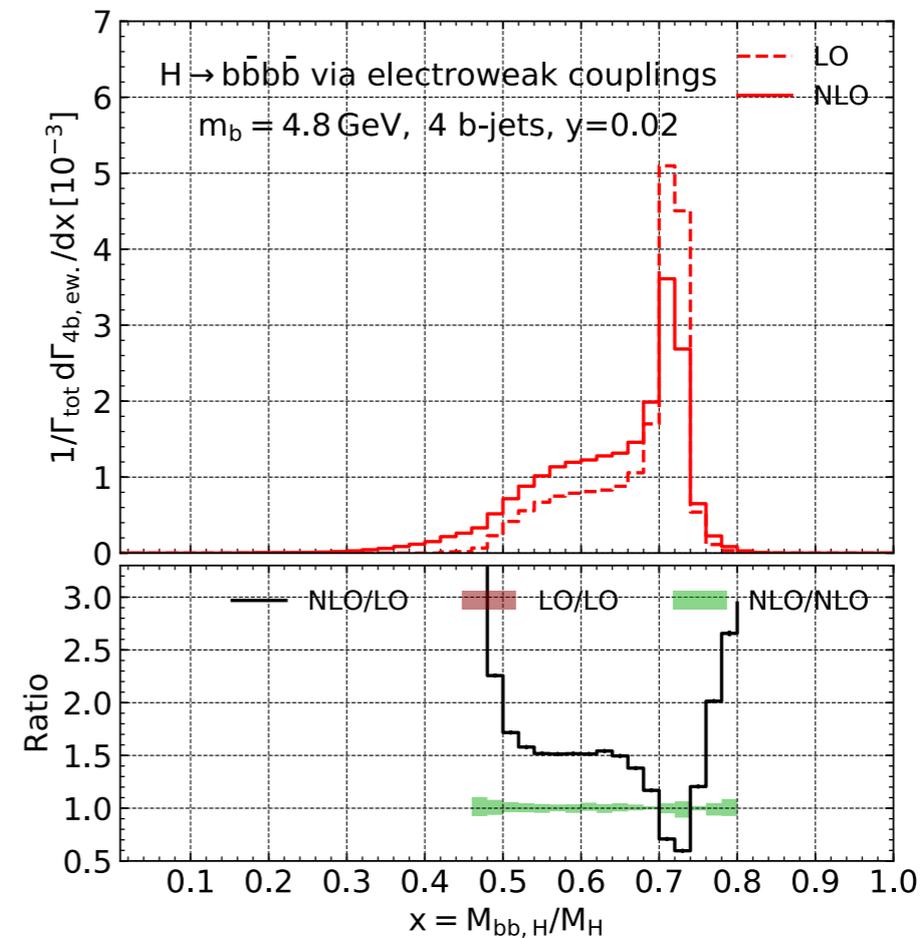
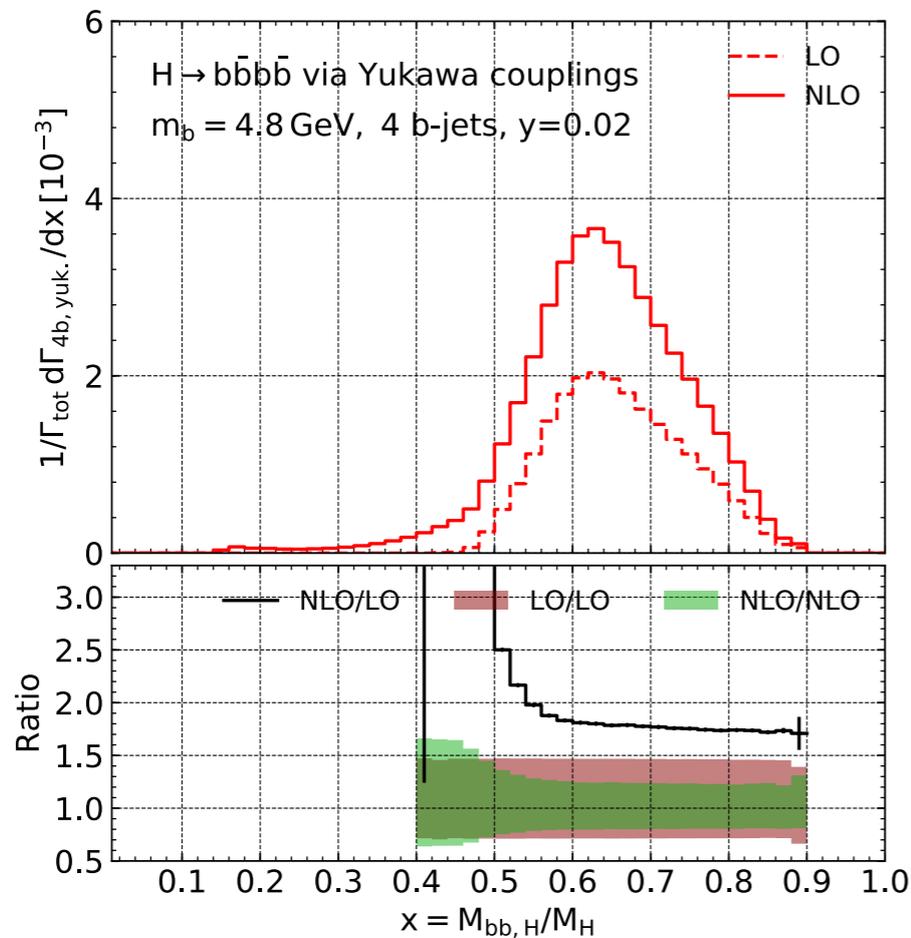


- softest b-jet peaked at  $E \sim 15 \text{ GeV}$  and are broader for decay via Yukawa couplings; QCD corrections show less dependence on energy

# Event topology

- Four b-jets are ordered by energy; kinematic distributions are constructed for individual jet and jet pairs

## highest b-jet pair invariant mass

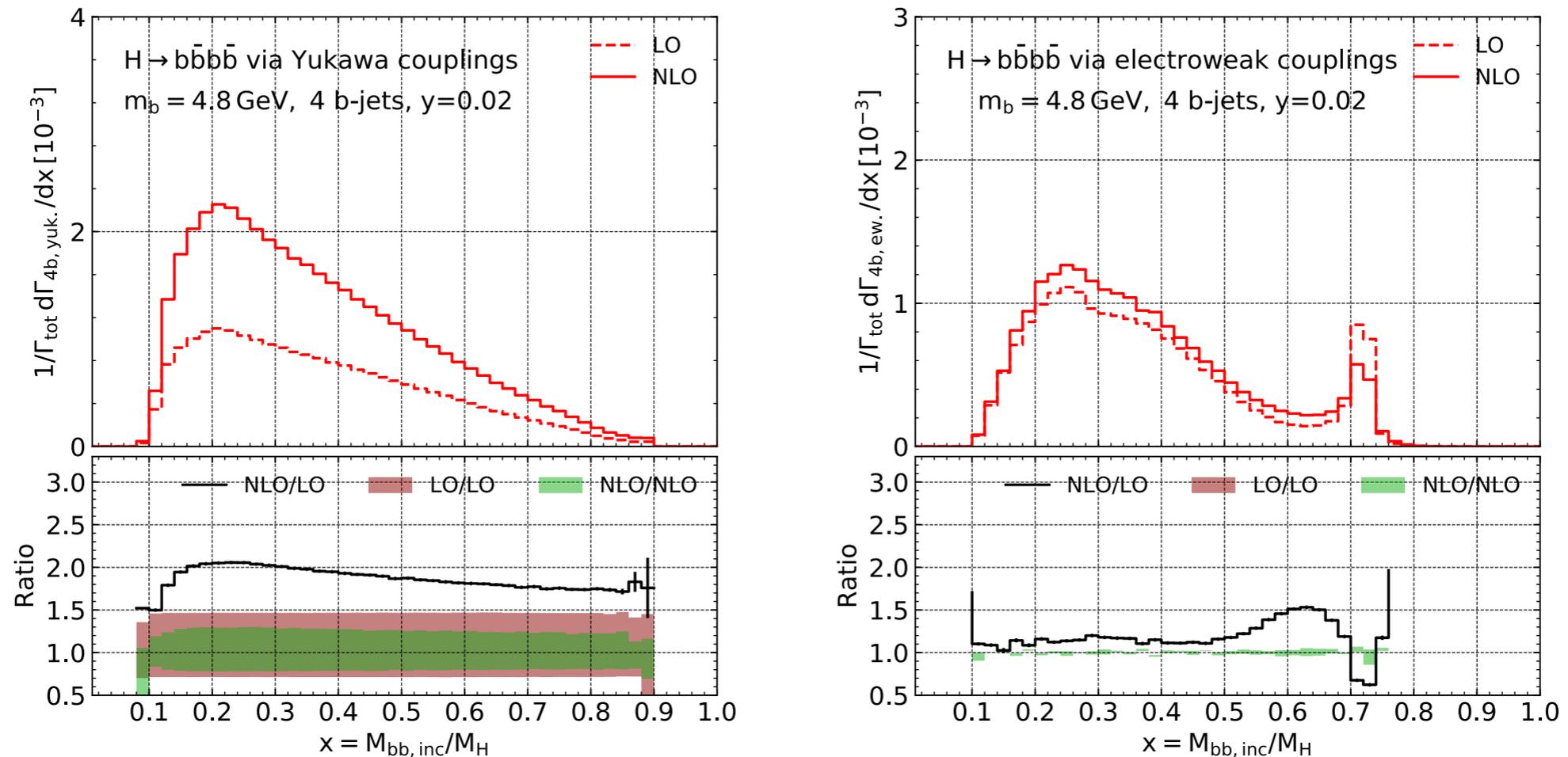


- clear Z mass peak in decay via EW coupling, while much broader for decay via Yukawa couplings; QCD corrections are quite different in two cases

# Event topology

- Four b-jets are ordered by energy; kinematic distributions are constructed for individual jet and jet pairs

## inclusive b-jet pair invariant mass

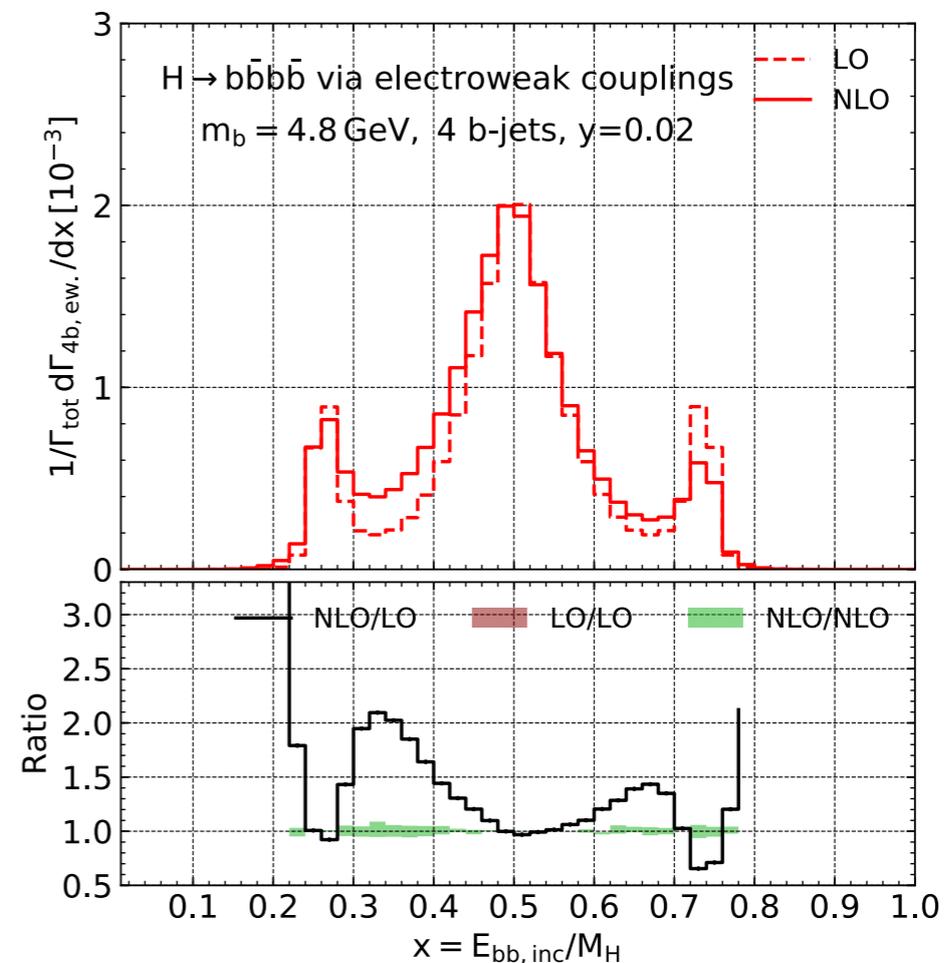
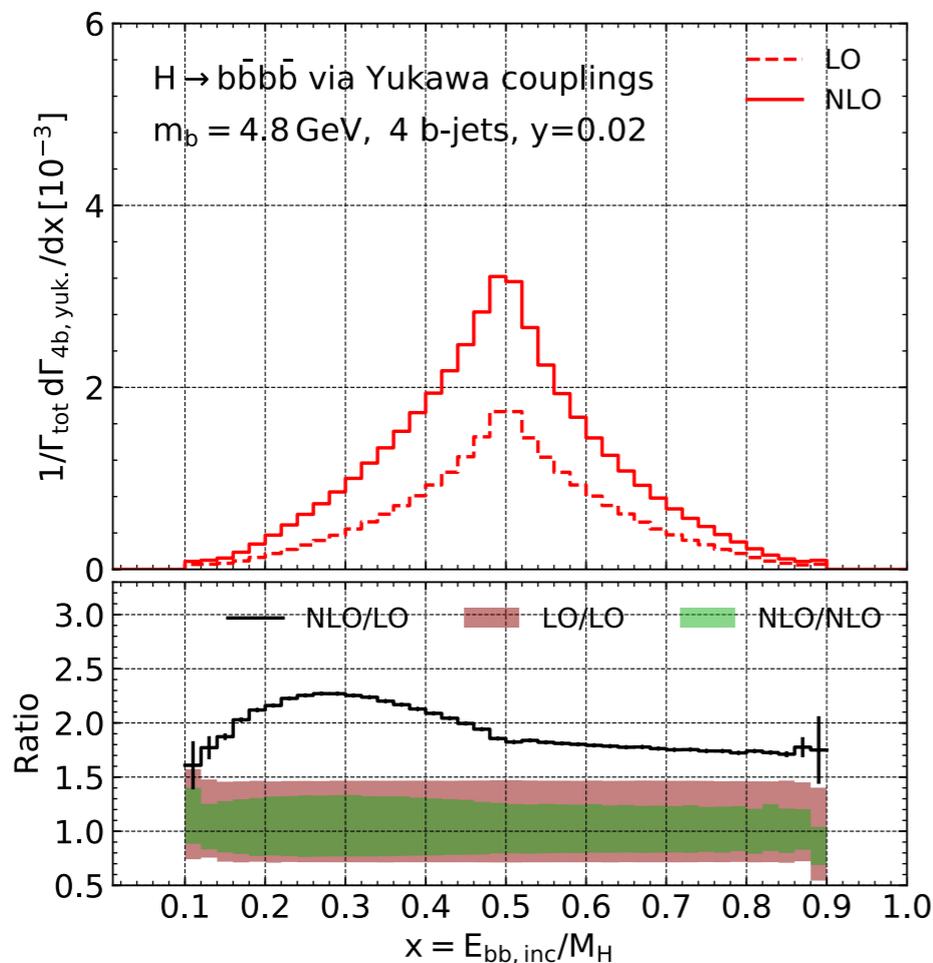


- ★ Z mass peak is diluted for decay via EW coupling and another peak arises for  $M \sim 0.2 M_H$ ; QCD corrections are almost flat except close to Z mass region

# Event topology

- Four b-jets are ordered by energy; kinematic distributions are constructed for individual jet and jet pairs

## inclusive b-jet pair energy

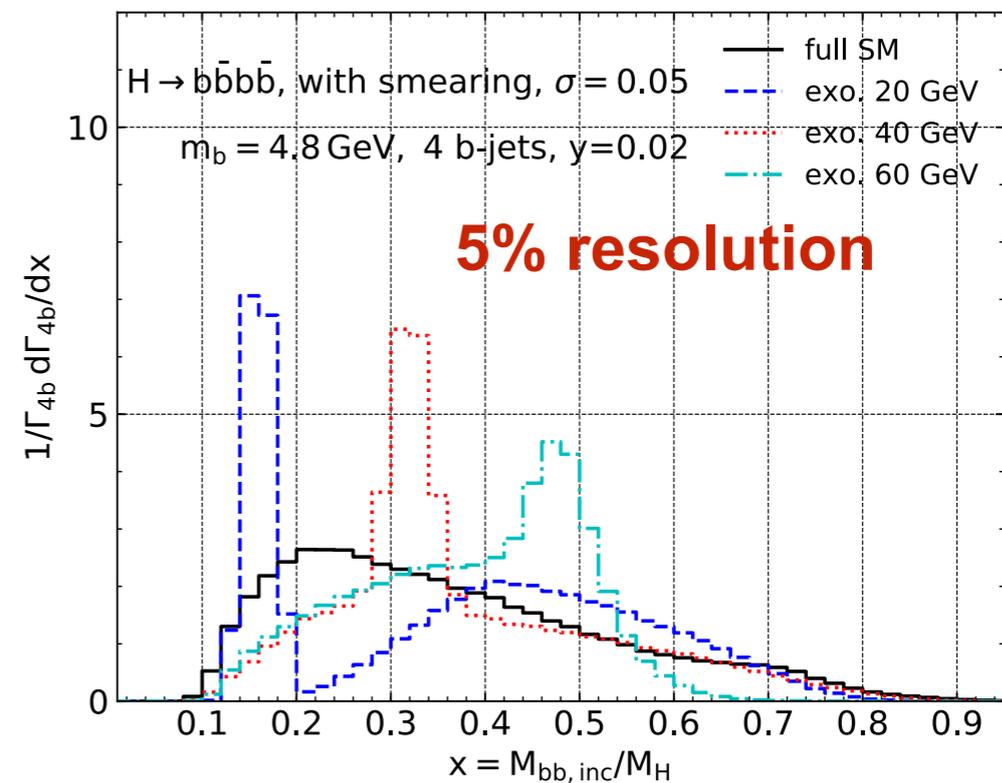
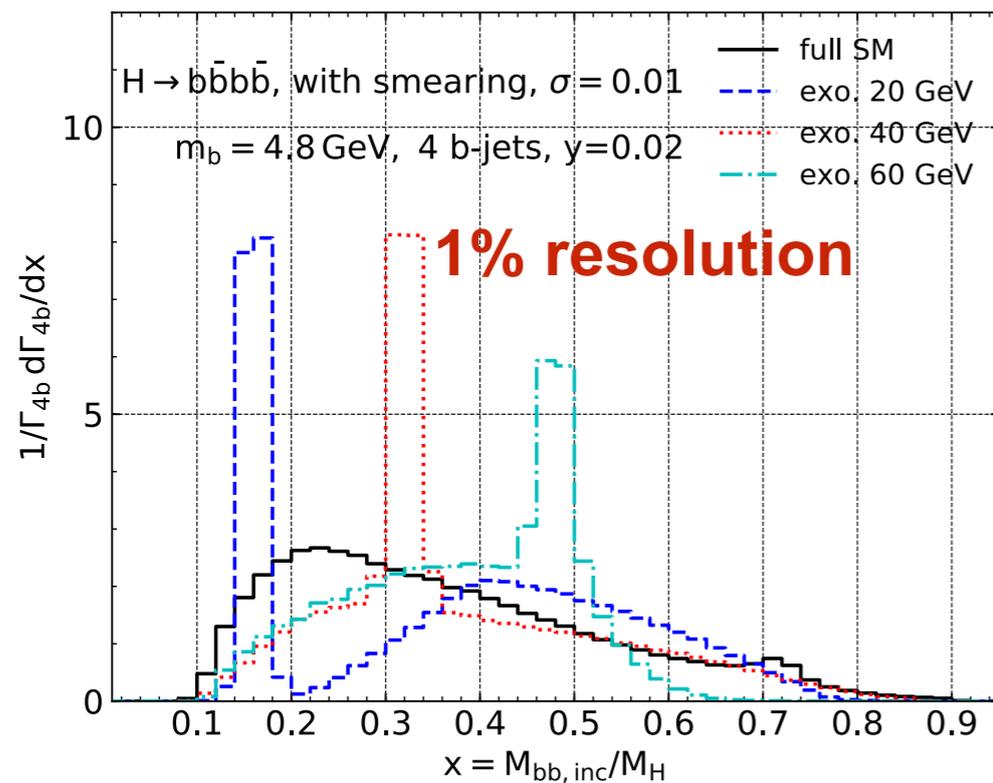


- ★ Symmetric at LO, asymmetries driven by unclustered gluon in QCD real radiations; triple peak structure expected for decay via EW couplings

# SM vs BSM to four bottom quarks

- ◆ A comparison of the four bottom quark decay mode in SM and induced by two light scalars for normalized distributions

## inclusive b-jet pair mass



- ★ all calculated at NLO in QCD and assuming narrow width case for the light scalars; Gaussian smearing are applied with different energy resolutions

# Summary

- ◆ Precision test of the Higgs couplings will be one of the most imperative tasks in the next few decades
- ◆ Better understanding on hadronic decays of the Higgs boson, on both perturbative and non-perturbative QCD aspects, will be important for extraction of the relevant Higgs couplings
- ◆ Rare or exotic hadronic decay modes can also be explored at future Higgs factories, for instance, decay to light quarks or to multiple heavy-quarks

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**Thank you for your attention!**