

# Some concerns on CPV measurements in $J/\psi \rightarrow \Lambda \bar{\Lambda}$

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# Introduction

- BESIII modified the decay parameter of  $\Lambda$  and improve the precision of CP asymmetry

$$\alpha_-^{PDG} = 0.642 \pm 0.013 \Rightarrow 0.750 \pm 0.009 \pm 0.004$$

$$A_{CP} = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+} = 0.006 \pm 0.012 \pm 0.007$$

- We believe there is still something wrong with this measurement!

# Outline

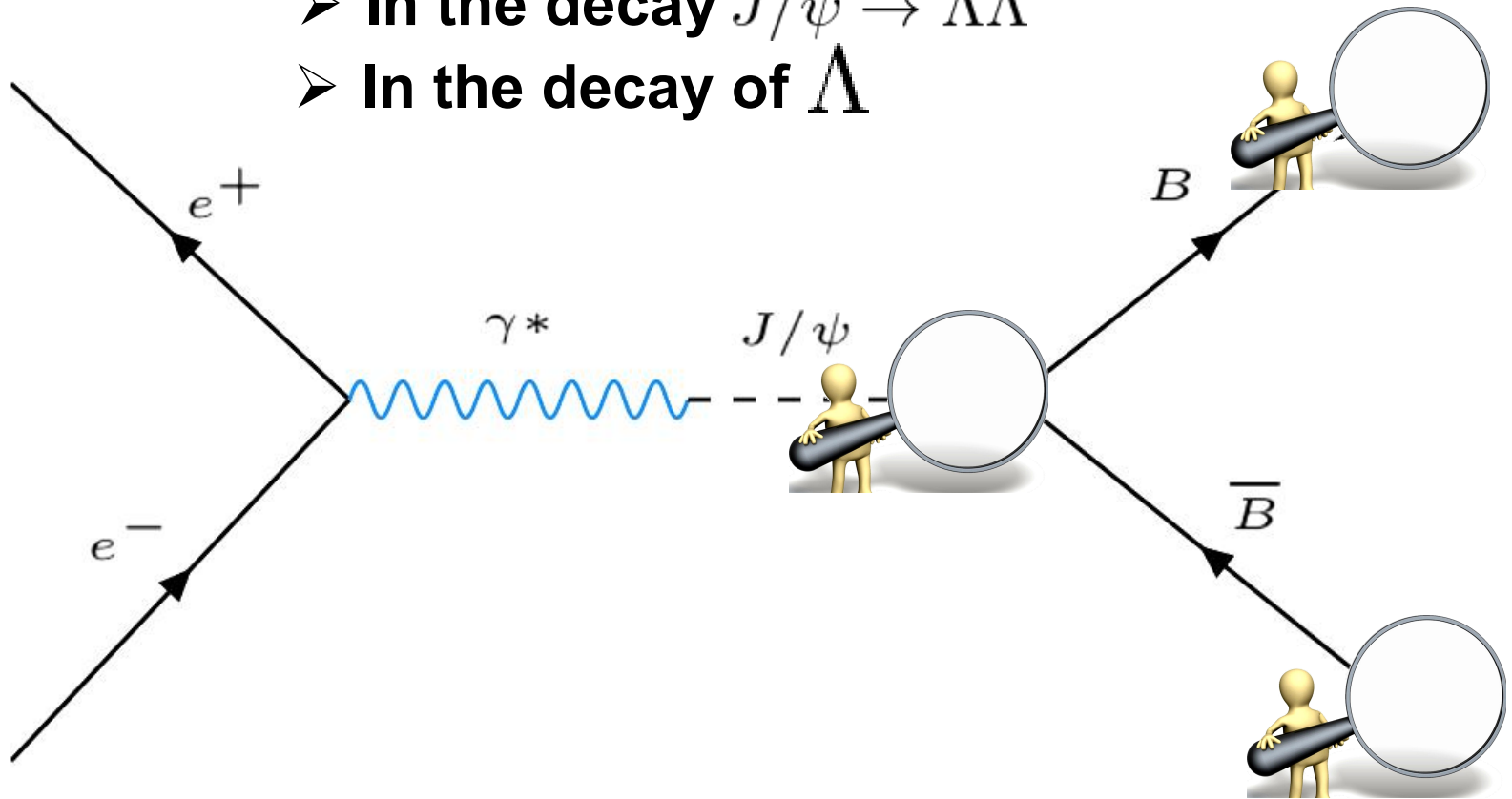
- The sources of CPV
- Methods for CPV measurement
- Challenge and Opportunity

# Outline

- The sources of CPV
- Methods for CPV measurement
- Challenge and Opportunity

# Where is the CPV?

- In the decay  $J/\psi \rightarrow \Lambda \bar{\Lambda}$
- In the decay of  $\Lambda$



# Where is the CPV?

-In the decay of  $J/\psi$  (type I-A)

The amplitude is

$$M = j_\mu K_\mu$$

with harmonic current

$$K_\mu = \bar{u}(p_1) \left[ F_1 \gamma_\mu - \frac{F_2}{4M} (\gamma_\mu \cdot Q - Q \cdot \gamma_\mu) + (p_{1\mu} - p_{2\mu}) \eta \frac{G_M}{p_B} \gamma_5 \right] v(p_2)$$

The **red term** violates CP, caused by electric dipole moment, CP violating Z- $\Lambda$  coupling etc. [Phys.Rev.D 47 (1993)]

$$L_{c-\Lambda} = -\frac{2}{3} \frac{g_V}{M^2} ed_\Lambda (p_1^\mu - p_2^\mu) \bar{c} \gamma_\mu c \bar{\Lambda} i \gamma_5 \quad \eta = i \frac{2}{3} \frac{p_B}{G_M} \frac{g_V}{M^2} ed_\Lambda$$

# Where is the CPV?

-In the decay of  $\Lambda$  (type I-B)

The decay parameters

$$\Gamma_{\Lambda} \propto 1 - \alpha_- \vec{s}_{\Lambda} \cdot \vec{p}_{\pi} \quad \Gamma_{\bar{\Lambda}} \propto 1 - \alpha_+ \vec{s}_{\bar{\Lambda}} \cdot \vec{p}_{\pi}$$

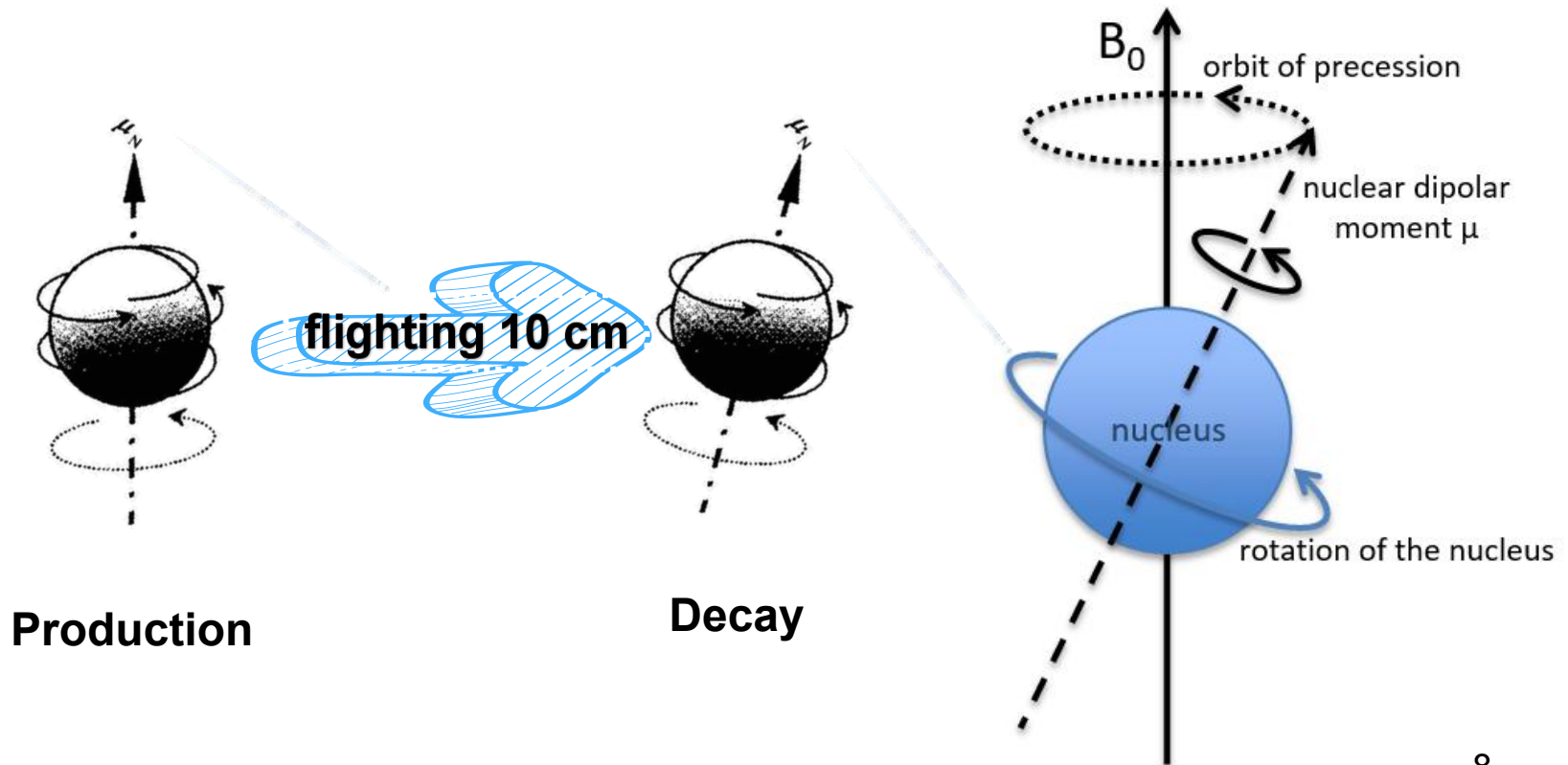
Defination of Acp

$$A_{CP} = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+} \quad \Delta = \frac{\Gamma_{\Lambda} - \Gamma_{\bar{\Lambda}}}{\Gamma_{\Lambda} + \Gamma_{\bar{\Lambda}}} \quad A = \frac{\Gamma_{\Lambda} \alpha_- - \Gamma_{\bar{\Lambda}} \alpha_+}{\Gamma_{\Lambda} \alpha_- + \Gamma_{\bar{\Lambda}} \alpha_+}$$

The **Acp** is  $4 \times 10^{-5}$  in SM [Phys. Rev. D 34, 833 (1986), Phys. Rev. D 67, 056001 (2003)]

# Where is the CPV?

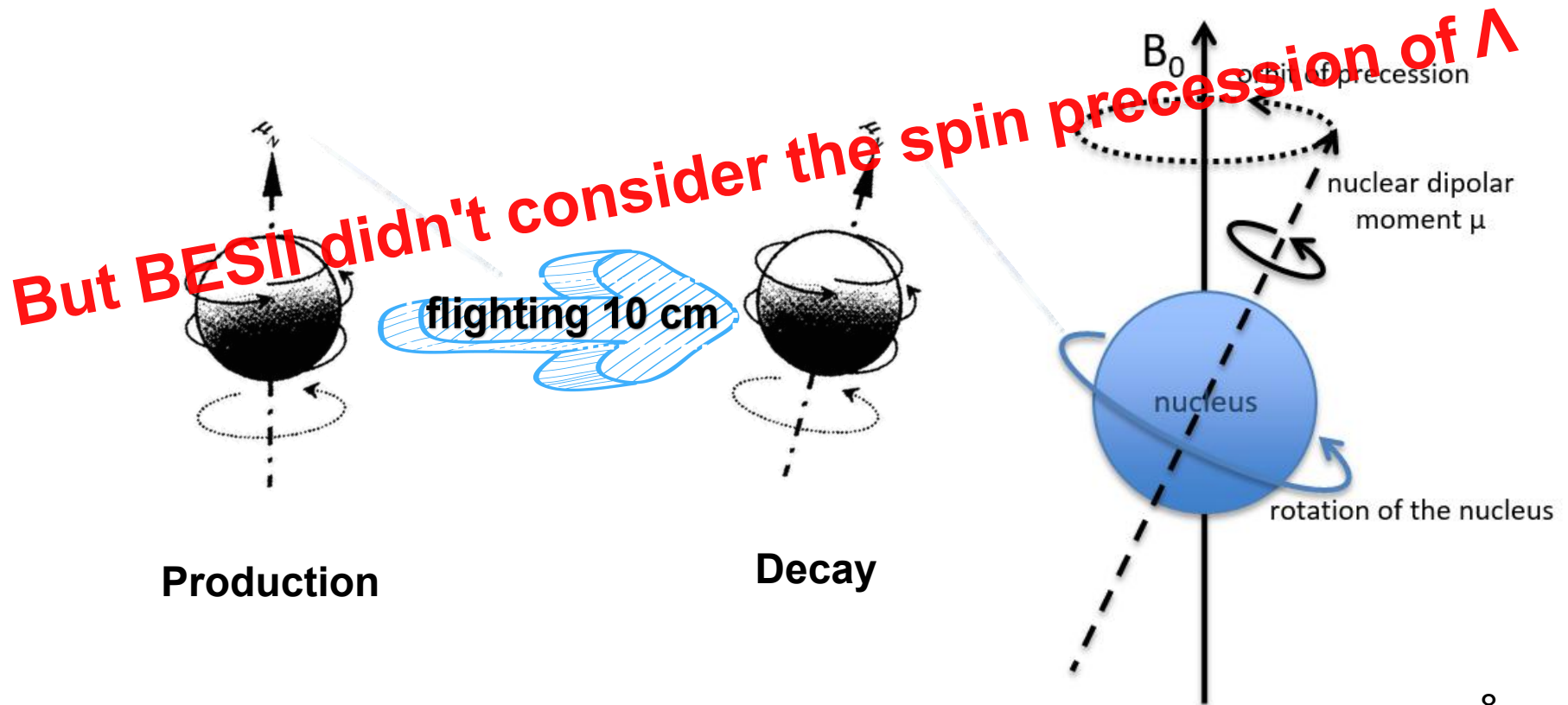
-experiment bias (type II)





# Where is the CPV?

-experiment bias (type II)



# Spin precession

## The change of spin direction

$$\begin{pmatrix} \hat{s}_1^{x'} \\ \hat{s}_1^{y'} \\ \hat{s}_1^{z'} \end{pmatrix} = \begin{pmatrix} 1 & -\omega t \hat{B}'_z & \omega t \hat{B}'_y \\ \omega t \hat{B}'_z & 1 & -\omega t \hat{B}'_x \\ -\omega t \hat{B}'_y & \omega t \hat{B}'_x & 1 \end{pmatrix} \begin{pmatrix} \hat{s}_1^x \\ \hat{s}_1^y \\ \hat{s}_1^z \end{pmatrix}$$

$$\omega = -\frac{2\mu_\Lambda B}{\hbar}$$

precession angle is about 0.017 rad

- $B=1.0\text{T}$
- $s_1$  is the spin direction of  $\Lambda$
- $t = 2 \times 10^{-10}\text{s}$
- $\mu_\Lambda = -0.613 \pm 0.04\mu_N$

# Spin precession(2)

## The cross-section for the production of $\Lambda\bar{\Lambda}$

NuovoCim. A109, 241 (1996)

Nucl. Phys. A771, 169 (2006) [hep-ph/0511240]

Phys. Rev. D75, 074026(2007) [hep-ph/0702122]

$$\frac{d\sigma}{d\cos\theta} \sim 1 + \alpha_\psi \cos^2\theta + \sin^2\theta \hat{s}_1^x \hat{s}_2^x + \alpha_\psi \sin^2\theta \hat{s}_1^y \hat{s}_2^y - (\alpha_\psi + \cos^2\theta) \hat{s}_1^z \hat{s}_2^z + \sqrt{1 - \alpha_\psi^2} \cos\Phi \sin\theta \cos\theta (\hat{s}_1^x \hat{s}_2^z - \hat{s}_1^z \hat{s}_2^x) + \sqrt{1 - \alpha_\psi^2} \sin\Phi \sin\theta \cos\theta (\hat{s}_1^y - \hat{s}_2^y),$$

- $\theta$  is the angle between  $\Lambda$  and  $e^+$
- $\alpha_\psi$  decay parameter of  $J/\psi$
- $\Phi = \text{Arg}[G_E/G_M]$

# Spin precession(3)

Consider the spin precession

$$\begin{aligned}
 \frac{d\sigma}{d\cos\theta d\Omega_1 d\Omega_2} &\sim 1 + \alpha_\psi \alpha_- \alpha_+ \cos^2\theta n_p^x n_{\bar{p}}^x + \alpha_\psi \alpha_- \alpha_+ \sin^2\theta n_p^y n_{\bar{p}}^y - \alpha_- \alpha_+ (\alpha_\psi + \cos^2\theta) n_p^z n_{\bar{p}}^z \\
 &+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos\Phi \sin\theta \cos\theta (n_p^x n_{\bar{p}}^z - n_p^z n_{\bar{p}}^x) + \sqrt{1 - \alpha_\psi^2} \sin\Phi \sin\theta \cos\theta (\alpha_- n_p^y - \alpha_+ n_{\bar{p}}^y) \\
 &+ \omega t \alpha_- \alpha_+ \sin^2\theta \left( \hat{B}'_z (\hat{n}_p^x \hat{n}_p^y - \hat{n}_p^y \hat{n}_p^x) - \hat{B}'_y (\hat{n}_p^x \hat{n}_p^z + \hat{n}_p^z \hat{n}_p^x) \right) \\
 &+ \omega t \alpha_\psi \alpha_- \alpha_+ \sin^2\theta \left( -\hat{B}'_z \hat{n}_p^x \hat{n}_p^y + \hat{B}'_z \hat{n}_p^x \hat{n}_p^y - \hat{B}'_x \hat{n}_p^y \hat{n}_p^z + \hat{B}'_x \hat{n}_p^y \hat{n}_p^z \right) - \omega t \alpha_- \alpha_+ (\alpha_\psi + \cos^2\theta) (\hat{B}'_y \hat{n}_p^x \hat{n}_p^z \\
 &- \hat{B}'_x \hat{n}_p^y \hat{n}_p^z + \hat{B}'_y \hat{n}_p^x \hat{n}_p^z + \hat{B}'_x \hat{n}_p^y \hat{n}_p^z) + \omega t \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos\Phi \sin\theta \cos\theta \left( \hat{B}'_x \hat{n}_p^x \hat{n}_p^y + \hat{B}'_x \hat{n}_p^x \hat{n}_p^y + \hat{B}'_z \hat{n}_p^y \hat{n}_p^z \right. \\
 &\left. + \hat{B}'_z \hat{n}_p^y \hat{n}_p^z \right) + \omega t \sqrt{1 - \alpha_\psi^2} \sin\Phi \sin\theta \cos\theta \left( -\alpha_- \hat{B}'_z \hat{n}_p^x + \alpha_- \hat{B}'_x \hat{n}_p^z - \alpha_+ \hat{B}'_z \hat{n}_p^x + \alpha_+ \hat{B}'_x \hat{n}_p^z \right),
 \end{aligned}$$

- $n_{p,\bar{p}}$  is the direction of proton (anti-proton) in the rest frame of  $\Lambda(\bar{\Lambda})$
- $\omega$  the precession frequency
- $t$  the average lifetime of  $\Lambda$

# Outline

- The sources of CPV
- **Methods for CPV measurement**
- Challenge and Opportunity

# Difference Methods

- Define CP-odd observable

$$A_{CP} = \frac{N_+ - N_-}{N_+ + N_-}$$

- Maximum Likelihood Fit to the over-all distribution
- Others

# Difference Methods

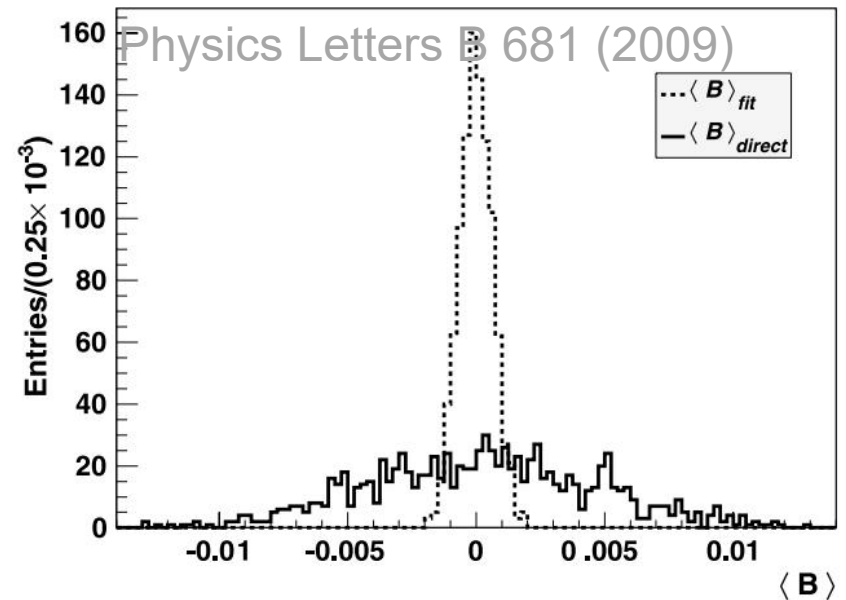
- Define CP-odd observable Phys. Rev. D 49 (1994) 4548

$$B = \hat{\mathbf{P}} \cdot (\hat{\mathbf{q}}_1 \times \hat{\mathbf{q}}_2)$$

$\mathbf{P}$  is the direction of the momentum of  $\Lambda$

and  $\mathbf{q}_{1,2}$  are the directions of the momenta of  $p$  and  $\bar{p}$  in the rest frames of  $\Lambda$  and  $\bar{\Lambda}$  respectively

The ML fit is better



# Spin precession(4)

**We choose the ML fit**

The probability distribution function is defined

$$\mathcal{P} = \frac{1}{N} \frac{d\sigma}{d \cos \theta d\Omega_1 d\Omega_2},$$
$$-\ln \mathcal{L} = -\sum_{i=1}^n \ln \mathcal{P}_i,$$



# Spin precession(5)

Toy MC: No CPV

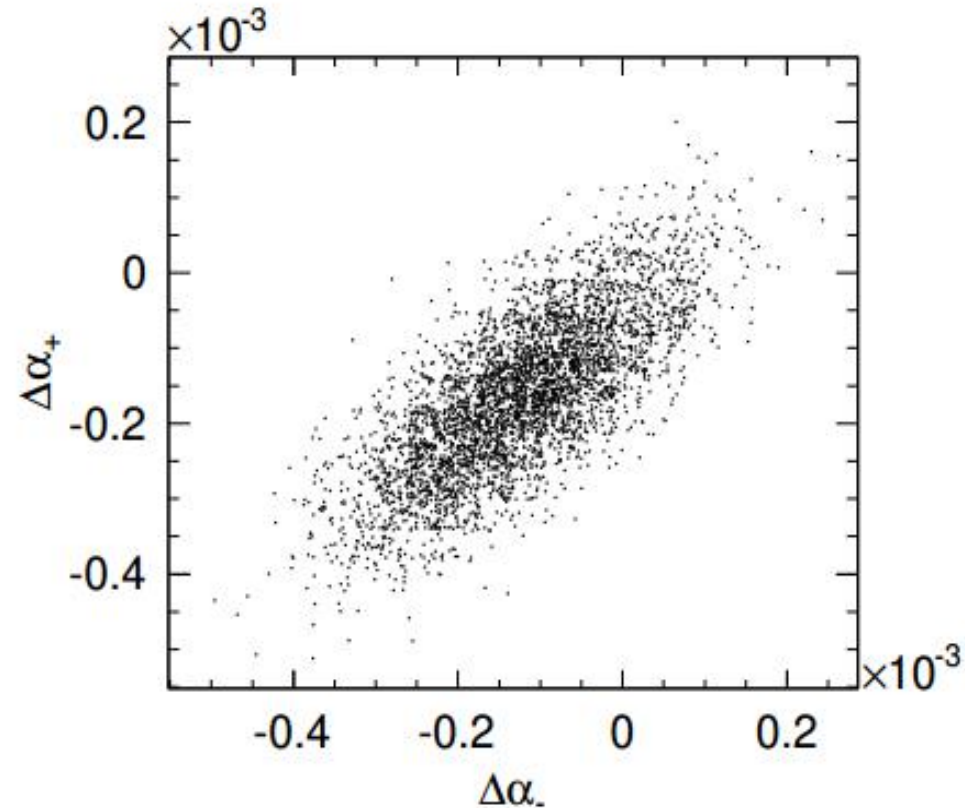
$$\Delta\alpha_{\pm} = \alpha_{\pm}^{\text{corr}} - \alpha_{\pm}^{\text{exp}}$$

exp : PDF without spin precession

corr: PDF with spin precession

**Additional "CP" asymmetry will be caused**

$$A_{CP} = \frac{\Delta\alpha_{-} + \Delta\alpha_{+}}{\alpha_{-} - \alpha_{+}} = -2 \times 10^{-5}$$



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# Opportunity and Challenge

- How well does SU(3) favor symmetry work ?

	$p$	$\Lambda$	$\Sigma^+$	$\Sigma^0$	$\Xi^-$
Branching fraction ( $10^{-3}$ )	$2.121 \pm 0.029$	$1.89 \pm 0.09$	$1.50 \pm 0.24$	$1.172 \pm 0.032$	$0.97 \pm 0.08$
$\alpha_{J/\psi}$	$0.595 \pm 0.019$	$0.461 \pm 0.009$	刮奖区	$-0.449 \pm 0.020$	刮奖区
$\Phi(^{\circ})$	$42.4 \pm 0.8$	刮奖区	刮奖区	刮奖区	刮奖区

# Opportunity and Challenge

- BEPCII have produced  $10^{10}$  J/ $\psi$  sample
- The Super J/ $\psi$  factory will produce 1000 times data of BEPCII's
  - 400 000  $\Lambda\bar{\Lambda}$  will be reconstructed by BESIII
  - About 400 000 000  $\Lambda\bar{\Lambda}$  will be reconstructed by Super-Charm factor
  - $A_{cp}$  could reach  $10^{-4}\sim 10^{-5}$

## Challenge

- Reduce Systemtic uncertainty (understudying)
- Enough CPU/GPU for ML fit (understudying)
- Any Potential effecton that may bring bias

# Summary

- We discuss the spin precession effect on the CP asymmetry measurement
- An additional CP asymmetry of order  $10^{-5}$  will be caused

**Thanks!**

# The $A_{cp}$ v.s. $B$

