

# Hyperon physics at a charm factory

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nature  
physics

LETTERS

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## Polarization and entanglement in baryon-antibaryon pair production in electron-positron annihilation

The BESIII Collaboration\*

$$e^+ e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda} \quad \text{Online: May 6}^{\text{th}}$$



BESIII

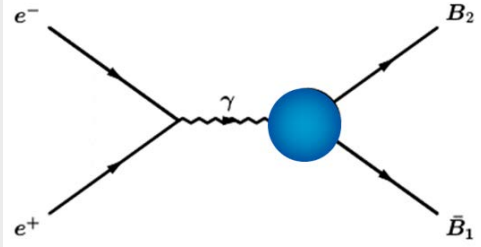
arXiv:1808.08917

## Prospects for hyperon physics at electron-positron collider

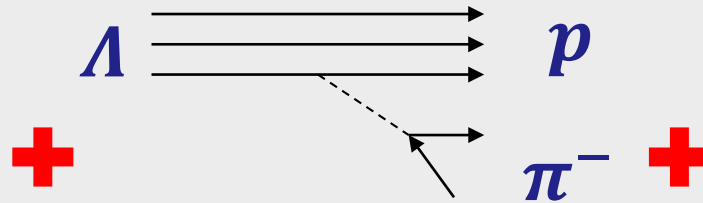
- ❑ Hyperon polarization
- ❑ Determination of hyperon decay parameters
- ❑ CP tests

E.Perotti,G.Fäldt,AK,S.Leupold,JJ.Song PRD99 (2019)056008,  
P.Adlarson,AK

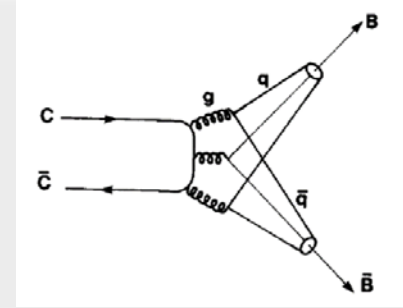
# Outline:



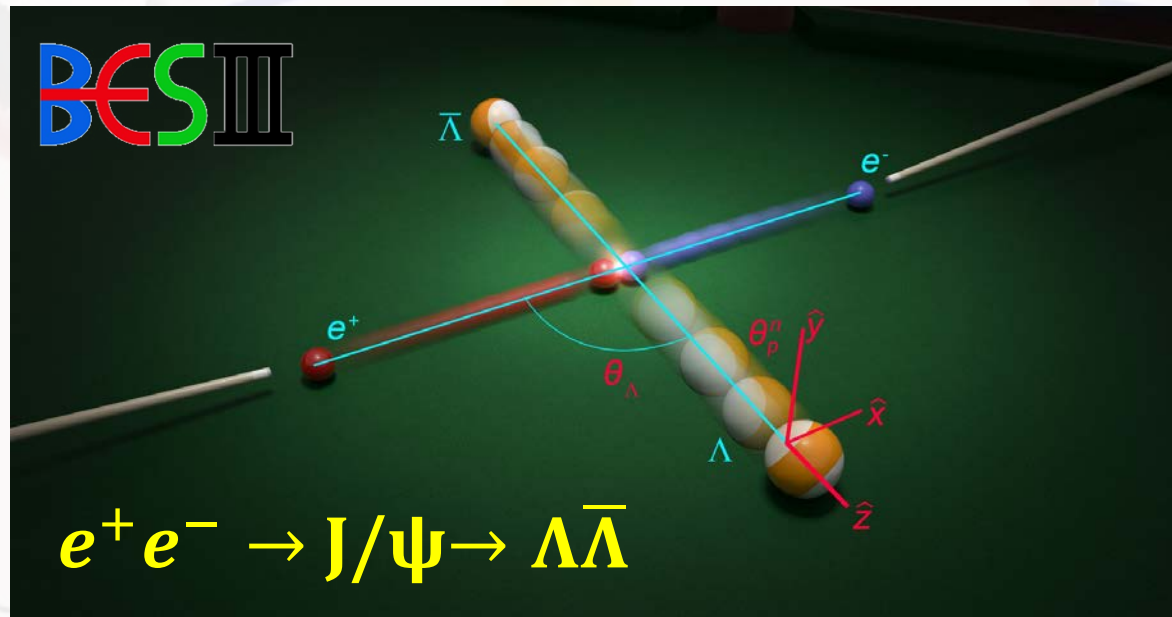
$$e^+ e^- \rightarrow f \bar{f}, B_1 \bar{B}_2$$



$$\Lambda \rightarrow p \pi^-$$



$$J/\psi \rightarrow B_1 \bar{B}_2$$

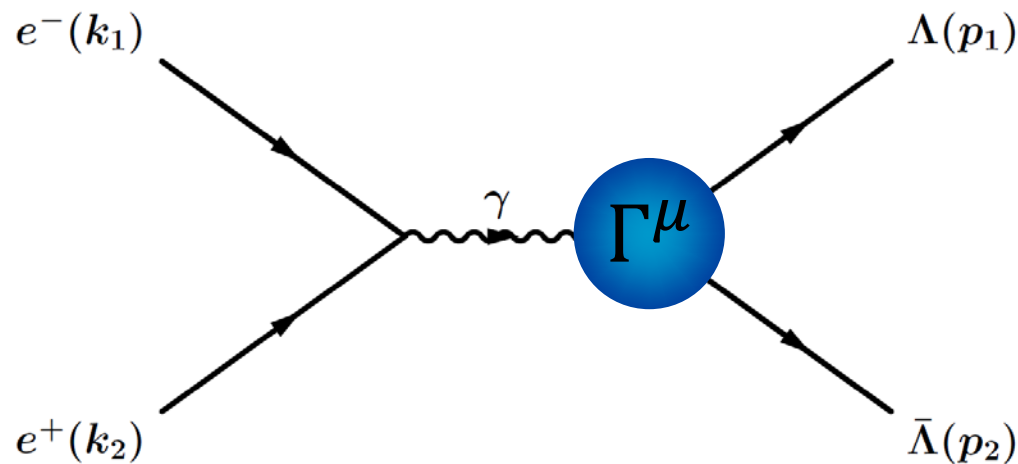


$$e^+ e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}$$

CP tests

$$e^+ e^- \rightarrow J/\psi \rightarrow \Xi \bar{\Xi}$$

# $e^+ e^- \rightarrow \gamma^* \rightarrow B\bar{B}$ (spin 1/2)



$$s = (p_1 + p_2)^2$$

$$q = p_1 - p_2$$

$$\Gamma^\mu(p_1, p_2) = -ie \left[ \gamma^\mu F_1(s) + i \frac{\sigma^{\mu\nu}}{2M_B} q_\nu F_2(s) \right]$$

$F_1$  (Dirac) and  $F_2$  (Pauli) Form Factors

Sachs Form Factors (FFs)  $\Leftrightarrow$  helicity amplitudes:

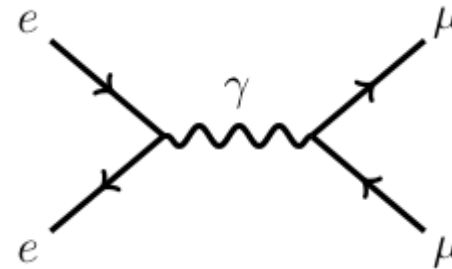
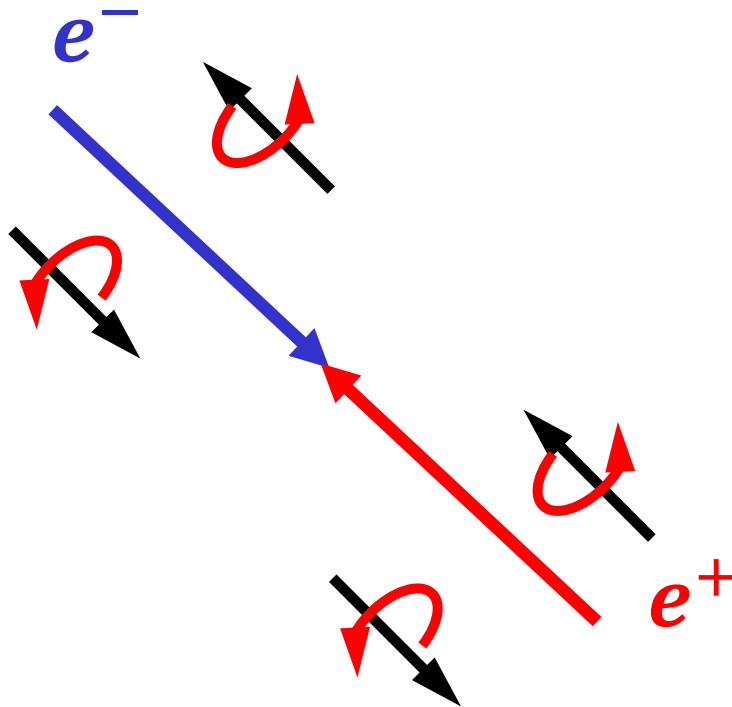
$$G_M(s) = F_1(s) + F_2(s), \quad G_E(s) = F_1(s) + \tau F_2(s)$$

helicity non-flip
helicity flip

$$\tau = \frac{s}{4M_B^2}$$

$$e^+e^- \rightarrow \mu^+\mu^-$$

At high energies annihilating  $e^+e^-$  have opposite helicities.



$$F_1(0) = 1, \quad F_2(0) = a_\mu$$

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4s}(1 + \cos^2\theta)$$

$\gamma^*$  has  $\pm 1$  helicity

$$\rho_1(\theta) = \begin{pmatrix} \frac{1+\cos^2\theta}{2} & -\frac{\cos\theta\sin\theta}{\sqrt{2}} & \frac{\sin^2\theta}{2} \\ -\frac{\cos\theta\sin\theta}{\sqrt{2}} & \sin^2\theta & \frac{\cos\theta\sin\theta}{\sqrt{2}} \\ \frac{\sin^2\theta}{2} & \frac{\cos\theta\sin\theta}{\sqrt{2}} & \frac{1+\cos^2\theta}{2} \end{pmatrix}$$

$$e^+ e^- \rightarrow \gamma^* \rightarrow B\bar{B}$$

For spin  $\frac{1}{2}$   $B\bar{B}$  production two complex FFs:  $G_M(s)$ ,  $G_E(s)$

$\Rightarrow$  process described by three parameters at fixed  $\sqrt{s}$  :

- cross section ( $\sigma$ )
- FFs ratio  $R$  or angular distribution parameter  $\alpha_\psi$
- relative phase between FFs ( $\Delta\Phi$ )

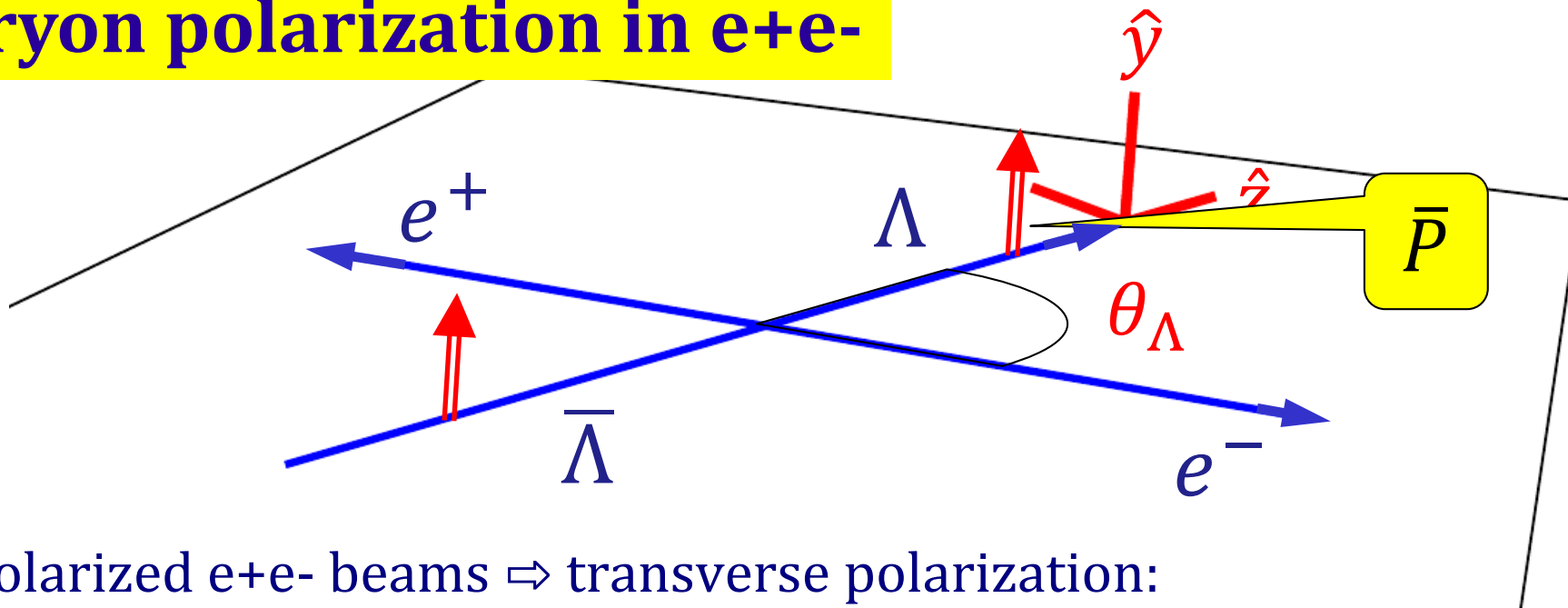
$$R = \left| \frac{G_E}{G_M} \right| \quad \left( \alpha_\psi = \frac{\tau - R^2}{\tau + R^2} \right) \quad G_E = R G_M e^{i\Delta\Phi} \quad \tau = \frac{s}{4M_B^2}$$

Angular distribution:

$$\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_\psi \cos^2\theta \quad -1 \leq \alpha_\psi \leq 1$$

Phase  $\Delta\Phi$  expected/predicted for continuum  
but neglected/not expected for the decays

# Baryon polarization in e+e-

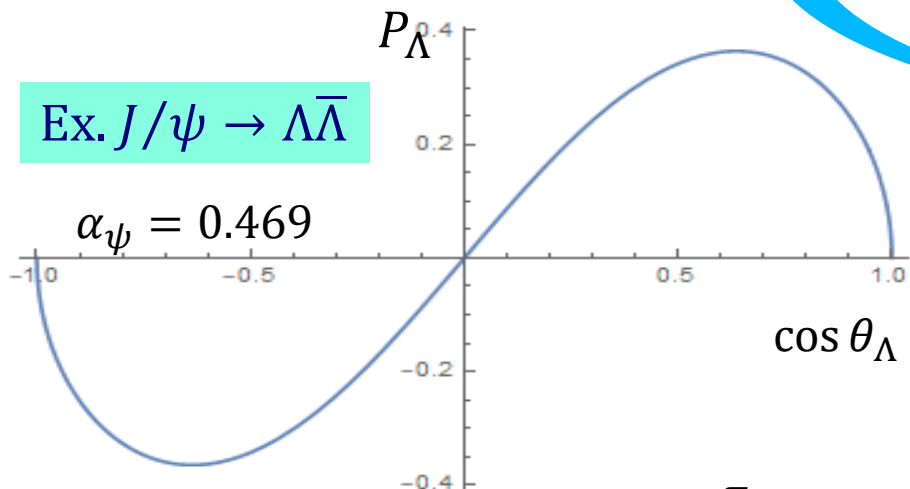


Unpolarized e+e- beams  $\Rightarrow$  transverse polarization:

$$P_y(\cos \theta_\Lambda) = \frac{\sqrt{1 - \alpha_\psi^2} \cos \theta_\Lambda \sin \theta_\Lambda}{1 + \alpha_\psi \cos^2 \theta_\Lambda} \sin(\Delta\Phi)$$

Ex.  $J/\psi \rightarrow \Lambda \bar{\Lambda}$

$\alpha_\psi = 0.469$

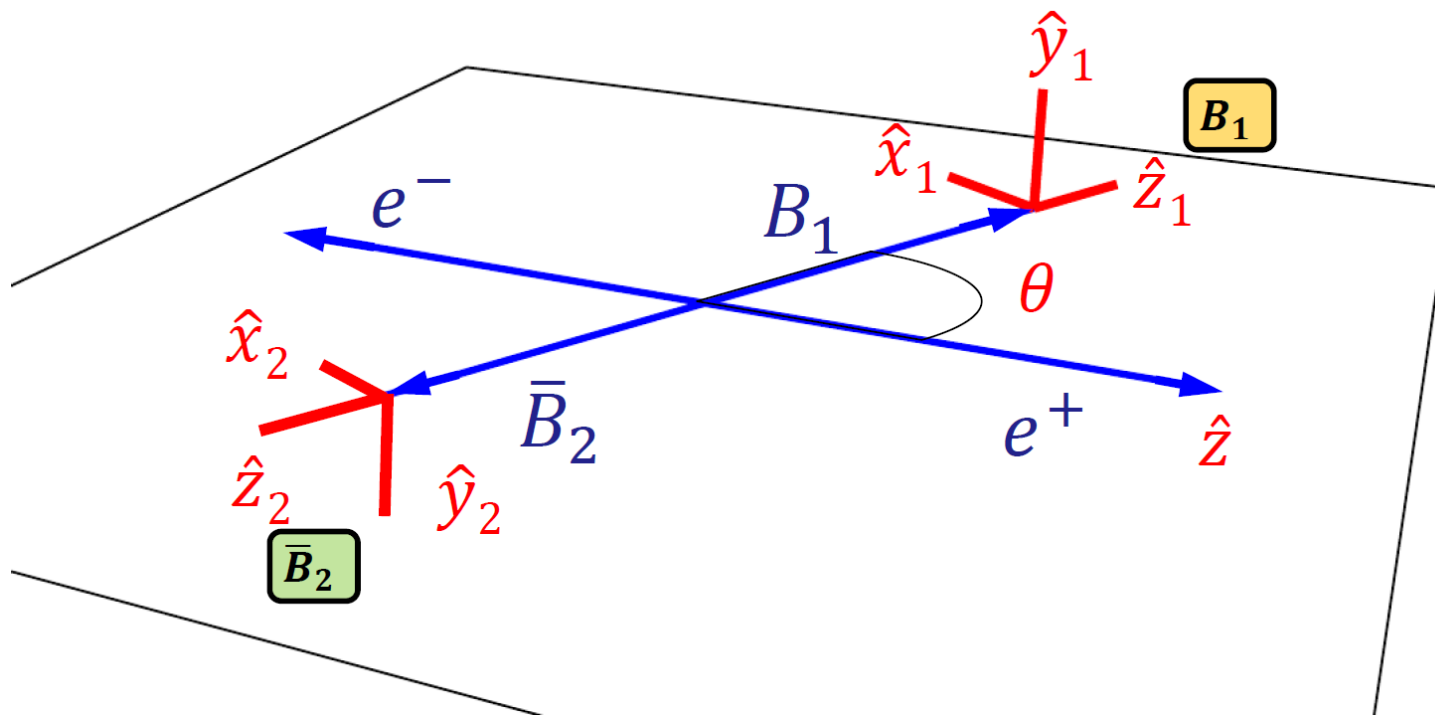


Max  $P_\Lambda = 36.4\%$

if  $\Delta\Phi = \frac{\pi}{2}$

$\Delta\Phi \neq 0$

$$e^+ e^- \rightarrow B_1 \bar{B}_2$$



# Baryon-antibaryon spin density matrix

$$e^+ e^- \rightarrow B_1 \bar{B}_2$$

General two spin 1/2 particle state:

$$\rho_{1/2,1/2} = \frac{1}{4} \sum_{\mu\bar{\nu}} C_{\mu\bar{\nu}} \sigma_{\mu}^{B_1} \otimes \sigma_{\bar{\nu}}^{\bar{B}_2}$$

$$(\sigma_0 = \mathbf{1}_2, \sigma_1 = \sigma_x, \sigma_2 = \sigma_y, \sigma_3 = \sigma_z)$$

$$C_{\mu\bar{\nu}} = \begin{pmatrix} 1 + \alpha_{\psi} \cos^2 \theta & 0 & \beta_{\psi} \sin \theta \cos \theta & 0 \\ 0 & \sin^2 \theta & 0 & \gamma_{\psi} \sin \theta \cos \theta \\ -\beta_{\psi} \sin \theta \cos \theta & 0 & \alpha_{\psi} \sin^2 \theta & 0 \\ 0 & -\gamma_{\psi} \sin \theta \cos \theta & 0 & -\alpha_{\psi} - \cos^2 \theta \end{pmatrix}$$

$P_y$

$$\beta_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \sin(\Delta\Phi) \quad \gamma_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \cos(\Delta\Phi)$$



# Polarization of daughter baryons:

$$Y \rightarrow B\pi$$

$$\mathbf{P}_B = \frac{(\alpha + \mathbf{P}_Y \cdot \hat{\mathbf{n}})\hat{\mathbf{n}} + \beta(\mathbf{P}_Y \times \hat{\mathbf{n}}) + \gamma\hat{\mathbf{n}} \times (\mathbf{P}_Y \times \hat{\mathbf{n}})}{1 + \alpha\mathbf{P}_Y \cdot \hat{\mathbf{n}}}$$

PDG

$$\mathbf{P}_Y = 0 \Rightarrow \mathbf{P}_B = \alpha \hat{\mathbf{n}}$$

Density matrix for a spin  $\frac{1}{2}$  particle  
in the rest frame:

$$\rho_{1/2} = \frac{1}{2} \sum_{\mu=0}^3 I_{\mu} \sigma_{\mu} = \frac{1}{2} I_0 \begin{pmatrix} 1 + P_z & P_x - iP_y \\ P_x + iP_y & 1 - P_z \end{pmatrix}$$

$$\sigma_0 = \mathbf{1}_2, \sigma_1 = \sigma_x, \sigma_2 = \sigma_y, \sigma_3 = \sigma_z$$

Transformation of base matrices:

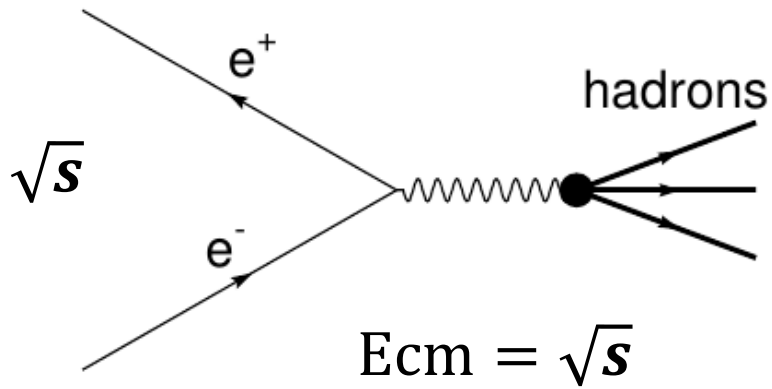
$$\frac{1^+}{2} \rightarrow \frac{1^+}{2} + 0^- \quad \text{e.g. } \Lambda \rightarrow p + \pi^-$$

Decay matrices

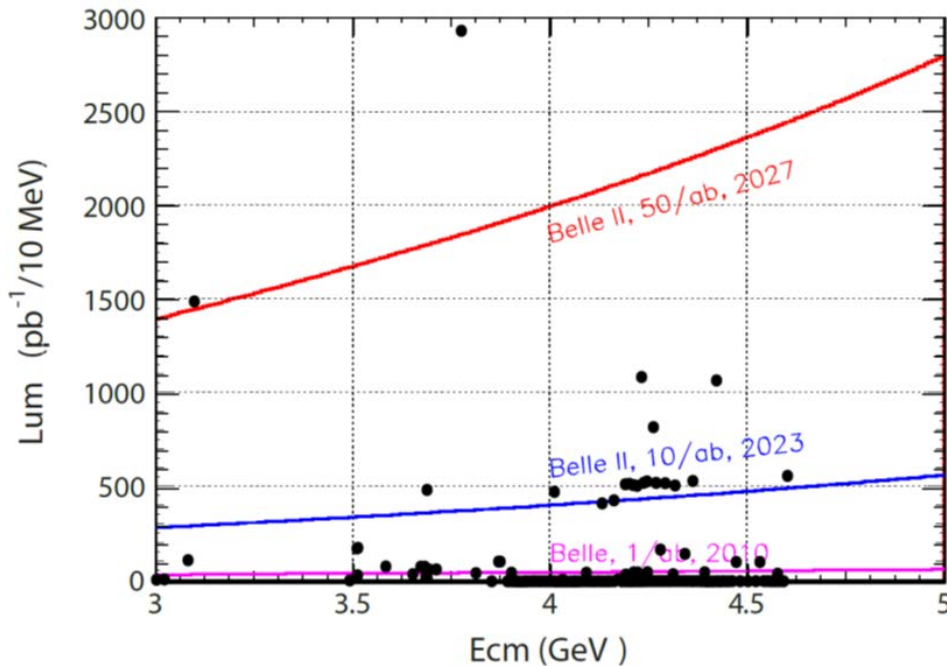
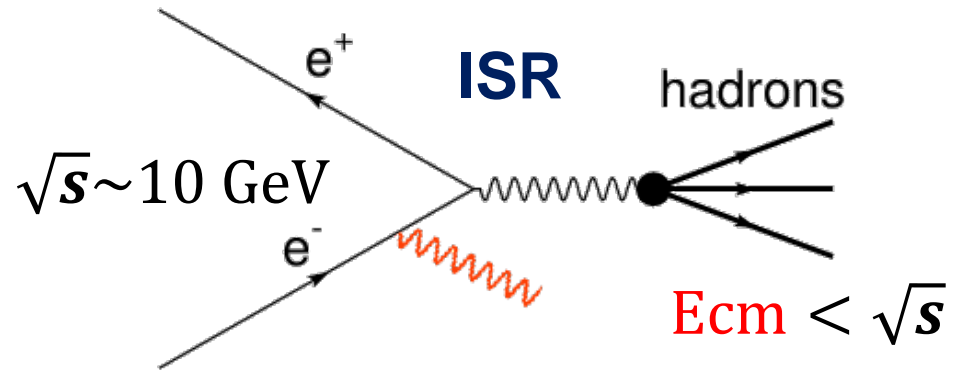
$$\sigma_{\mu} \rightarrow \sum_{\nu=0}^3 a_{\mu,\nu} \sigma_{\nu}^d$$

$4 \times 4$  decay matrix:  $a_{\mu,\nu}$

### Direct scan BESIII



### ISR BelleII



### Direct scan

- (very) high luminosity at selected c.m. energies
- better resolution: at  $J/\psi$  0.9 MeV:  $10^{10} J/\psi$

### ISR

- ISR: many  $E_{cm}$  simultaneously
- reduced point-to-point systematics
- mass resolution limited by detector
- boost of hadronic system may help efficiency

# Hyperon-hyperon pair production at BESIII

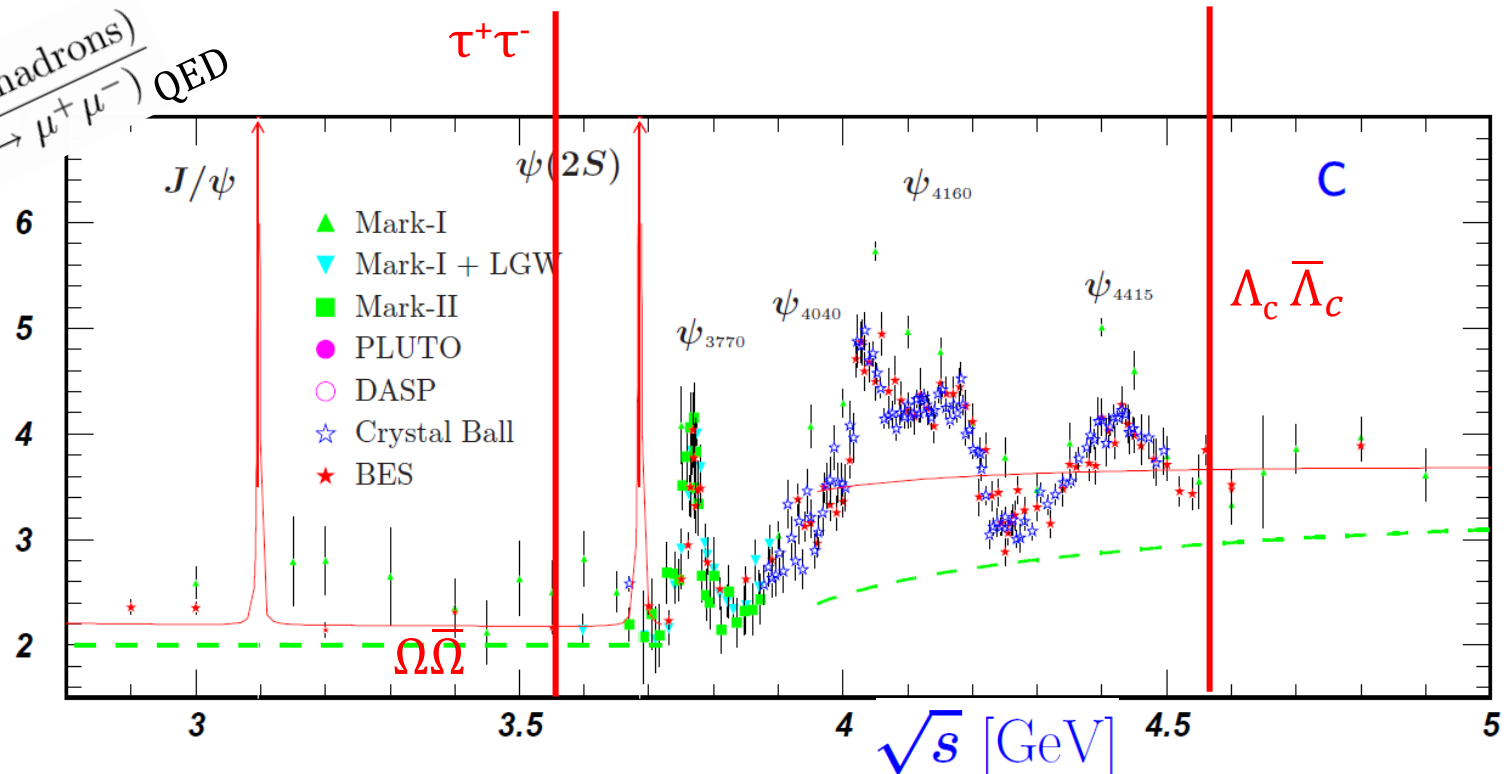
$$2.0 \text{ GeV} \leq \sqrt{s} \leq 4.6 \text{ GeV}$$

Thresholds:

|                          |           |                          |           |                        |           |
|--------------------------|-----------|--------------------------|-----------|------------------------|-----------|
| $\Lambda\bar{\Lambda}$   | 2.231 GeV | $\Sigma^+\bar{\Sigma}^-$ | 2.379 GeV | $(\Omega\bar{\Omega})$ | 3.345 GeV |
| $\Sigma^0\bar{\Sigma}^0$ | 2.385 GeV | $\Sigma^-\bar{\Sigma}^+$ | 2.395 GeV |                        |           |
| $\Xi^0\bar{\Xi}^0$       | 2.630 GeV | $\Xi^-\bar{\Xi}^+$       | 2.643 GeV |                        |           |
| $\Lambda\bar{\Sigma}^0$  | 2.308 GeV |                          |           |                        |           |

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \text{ QED}$$

$R$



# $J/\psi, \psi(2S) \rightarrow B\bar{B}$

$$\mathcal{B}(J/\psi \rightarrow p\bar{p}) = (21.21 \pm 0.29) \times 10^{-4}$$

| decay mode                                    | events |           | $\mathcal{B}(\text{units } 10^{-4})$ |
|---|--------|-----------|--------------------------------------|
| $J/\psi \rightarrow \Lambda\bar{\Lambda}$     | 440675 | $\pm 670$ | $19.43 \pm 0.03 \pm 0.33$            |
| $\psi(2S) \rightarrow \Lambda\bar{\Lambda}$   | 31119  | $\pm 187$ | $3.97 \pm 0.02 \pm 0.12$             |
| $J/\psi \rightarrow \Sigma^0\bar{\Sigma}^0$   | 111026 | $\pm 335$ | $11.64 \pm 0.04 \pm 0.23$            |
| $\psi(2S) \rightarrow \Sigma^0\bar{\Sigma}^0$ | 6612   | $\pm 82$  | $2.44 \pm 0.03 \pm 0.11$             |
| $J/\psi \rightarrow \Xi^0\bar{\Xi}^0$         | 134846 | $\pm 437$ | $11.65 \pm 0.04$                     |
| $\psi(2S) \rightarrow \Xi^0\bar{\Xi}^0$       | 10839  | $\pm 123$ | $2.73 \pm 0.03$                      |
| $J/\psi \rightarrow \Xi^-\bar{\Xi}^+$         | 42811  | $\pm 231$ | $10.40 \pm 0.06$                     |
| $\psi(2S) \rightarrow \Xi^-\bar{\Xi}^+$       | 5337   | $\pm 83$  | $2.78 \pm 0.05$                      |

PRD 93, 072003 (2016)  
PLB770,217 (2017)

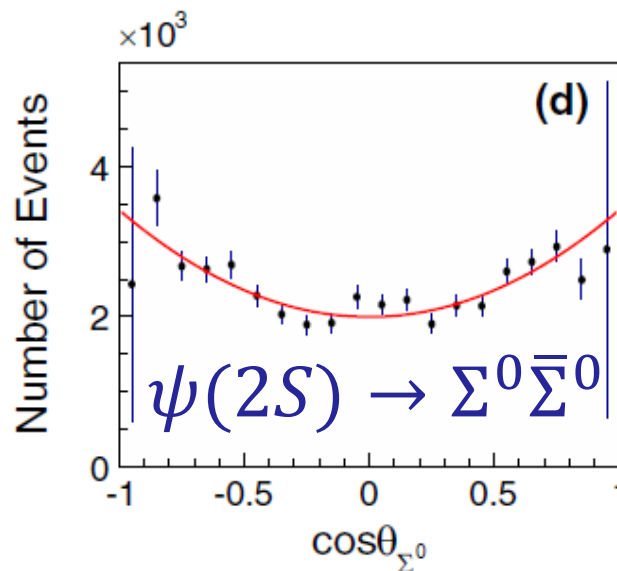
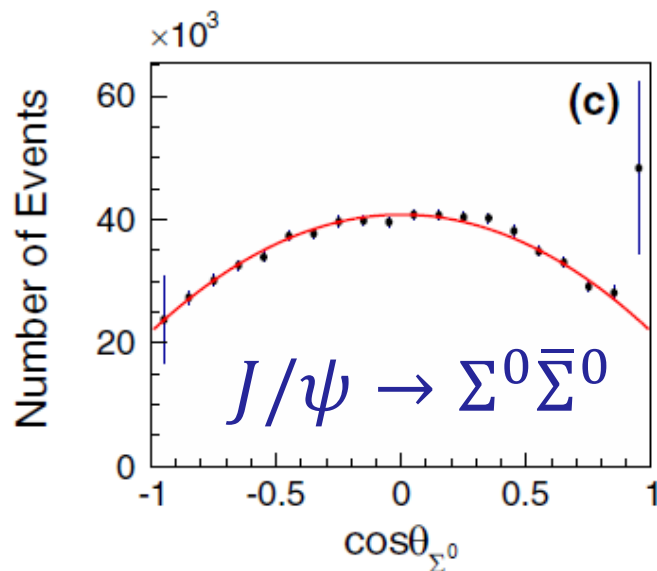
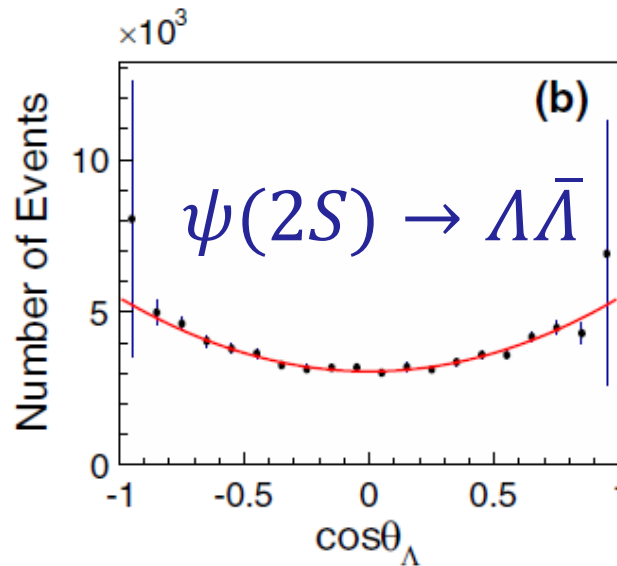
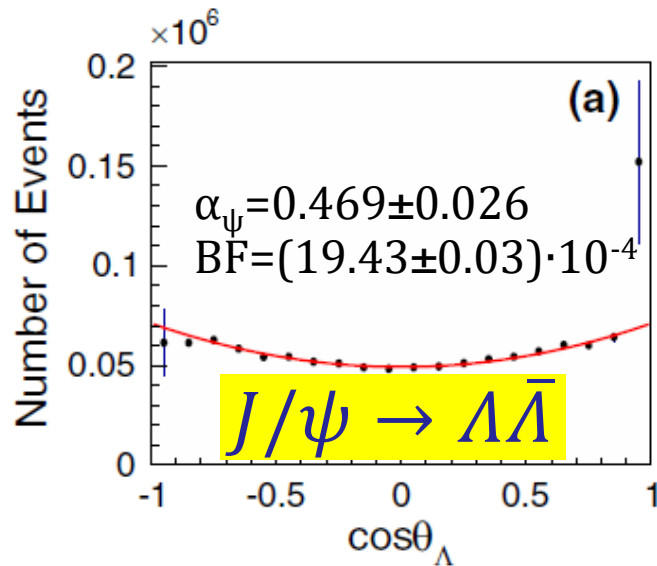
$1.31 \times 10^9 J/\psi$

$0.223 \times 10^9 J/\psi$

PRD 95, 052003 (2017)

$4.48 \times 10^8 \psi(2S)$

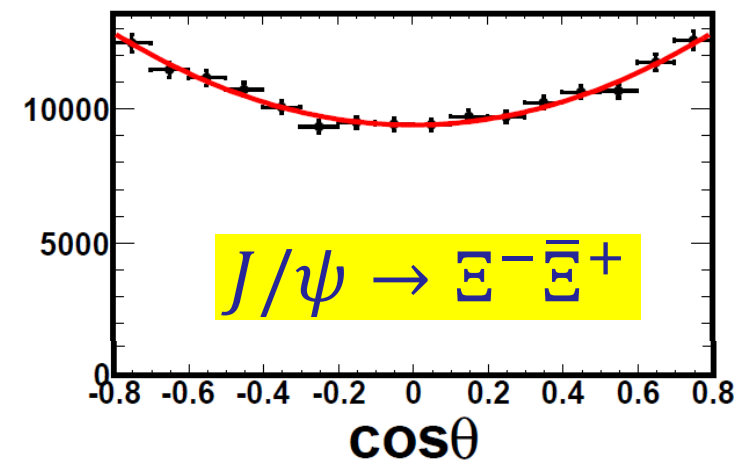
# Angular distributions in $J/\psi, \psi(2S) \rightarrow B\bar{B}$



$$1 + \alpha_\psi \cos^2 \theta_Y$$

$$\alpha_\psi = 0.58 \pm 0.04$$

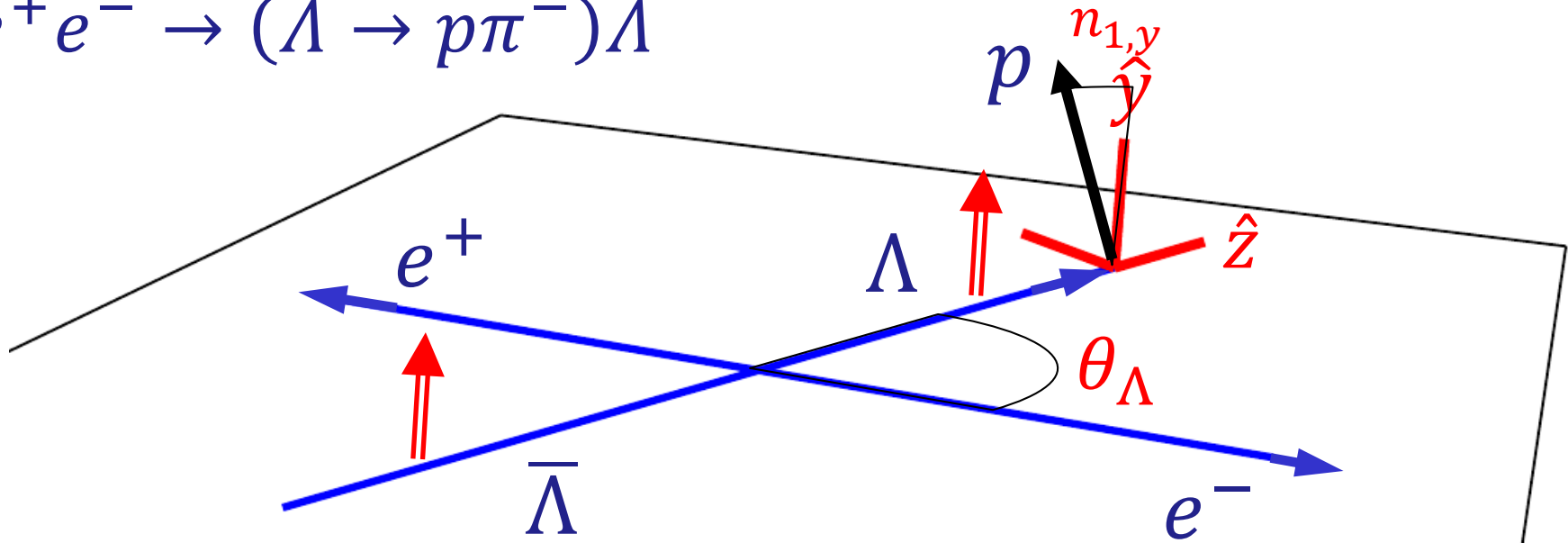
$$BF = (10.40 \pm 0.06) \cdot 10^{-4}$$



$\alpha_\psi$  measurements  
 at **BESIII**

# Inclusive decay angular distributions

$$e^+ e^- \rightarrow (\Lambda \rightarrow p \pi^-) \bar{\Lambda}$$



$$\frac{d\Gamma}{d \cos \theta_\Lambda d\Omega_1} \propto (1 + \alpha_\psi \cos^2 \theta_\Lambda) + \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda \alpha_- n_{1,y}$$

$$\Lambda \rightarrow p \pi^-: \hat{\mathbf{n}}_1 \rightarrow \Omega_1 = (\cos \theta_1, \phi_1) : \alpha_-$$

$\Rightarrow$  Determine product:  $\alpha_- P_y \sim \alpha_- \sin(\Delta\Phi)$

# Exclusive joint angular distribution

$$e^+ e^- \rightarrow (\Lambda \rightarrow p\pi^-) (\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

$$\Lambda \rightarrow p\pi^-: \hat{\mathbf{n}}_1 \rightarrow (\cos \theta_1, \phi_1) : \alpha_- \quad \bar{\Lambda} \rightarrow \bar{p}\pi^+: \hat{\mathbf{n}}_2 \rightarrow (\cos \theta_2, \phi_2) : \alpha_+$$

$$\xi : (\cos \theta_\Lambda, \hat{\mathbf{n}}_1, \hat{\mathbf{n}}_2) \quad \text{5D PhSp}$$

$$d\Gamma \propto W(\xi; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_+) =$$

$$1 + \alpha_\psi \cos^2 \theta_\Lambda \quad \text{Cross section}$$

$$+ \alpha_- \alpha_+ \left\{ \sin^2 \theta_\Lambda (n_{1,x} n_{2,x} - \alpha_\psi n_{1,y} n_{2,y}) + (\cos^2 \theta_\Lambda + \alpha_\psi) n_{1,z} n_{2,z} \right\} \quad \text{Spin correlations}$$

$$+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (n_{1,x} n_{2,z} + n_{1,z} n_{1,x})$$

$$+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y}) \quad \text{Polarization}$$

$\Delta\Phi \neq 0 \Rightarrow$  independent determination of  $\alpha_-$  and  $\alpha_+$

# Exclusive joint angular distribution (modular form)

$$e^+ e^- \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

General two spin  $\frac{1}{2}$  particle state:  $\rho_{1/2,1/2} = \frac{1}{4} \sum_{\mu\bar{\nu}} C_{\mu\bar{\nu}} \sigma_{\mu}^{\Lambda} \otimes \sigma_{\bar{\nu}}^{\bar{\Lambda}}$

( $\sigma_0 = \mathbf{1}_2, \sigma_1 = \sigma_x, \sigma_2 = \sigma_y, \sigma_3 = \sigma_z$ )

$$C_{\mu\bar{\nu}} = \begin{pmatrix} 1 + \alpha_{\psi} \cos^2 \theta & 0 & \beta_{\psi} \sin \theta \cos \theta & 0 \\ 0 & \sin^2 \theta & 0 & \gamma_{\psi} \sin \theta \cos \theta \\ -\beta_{\psi} \sin \theta \cos \theta & 0 & \alpha_{\psi} \sin^2 \theta & 0 \\ 0 & -\gamma_{\psi} \sin \theta \cos \theta & 0 & -\alpha_{\psi} - \cos^2 \theta \end{pmatrix}$$

$$\beta_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \sin(\Delta\Phi) \quad \gamma_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \cos(\Delta\Phi)$$

Apply decay matrices:

$$\sigma_{\mu}^{\Lambda} \rightarrow \sum_{\mu'=0}^3 a_{\mu,\mu'}^{\Lambda} \sigma_{\mu'}^p$$

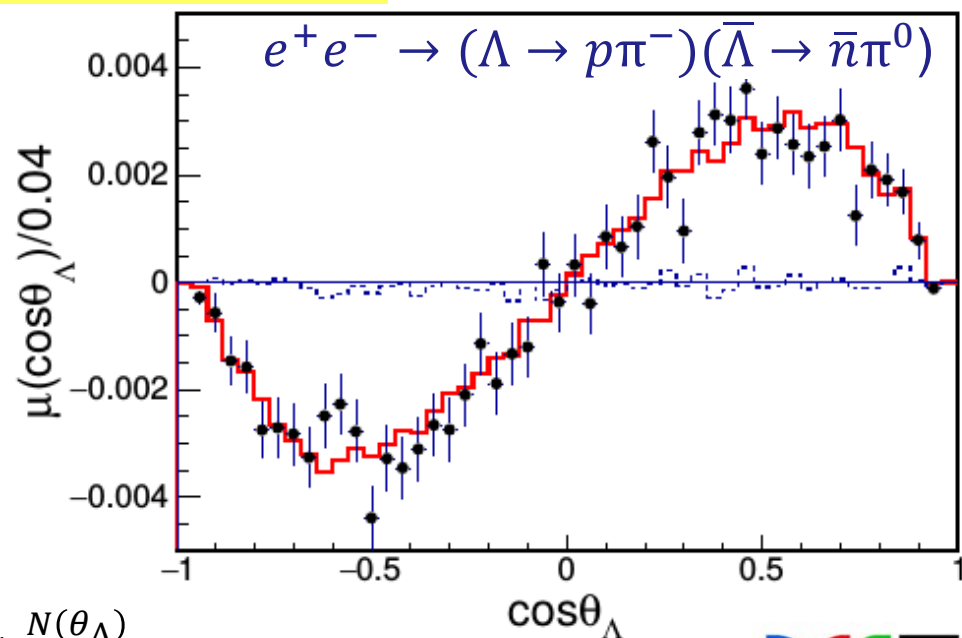
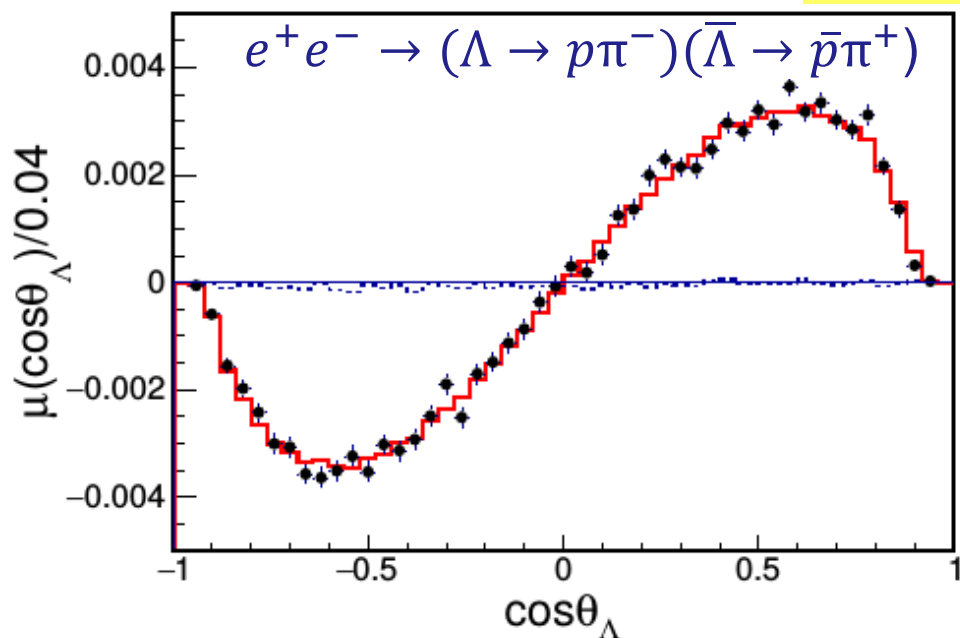
The result:

$$W = \text{Tr} \rho_{p,\bar{p}} = \sum_{\mu,\bar{\nu}=0}^3 C_{\mu\bar{\nu}} a_{\mu,0}^{\Lambda} a_{\bar{\nu},0}^{\bar{\Lambda}}$$



# Fit results

$$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$$



**moment:**

$$\mu(\cos\theta_\Lambda) = \frac{1}{N} \sum_{i=1}^{N(\theta_\Lambda)} (n_{1,y}^{(i)} - n_{2,y}^{(i)})$$

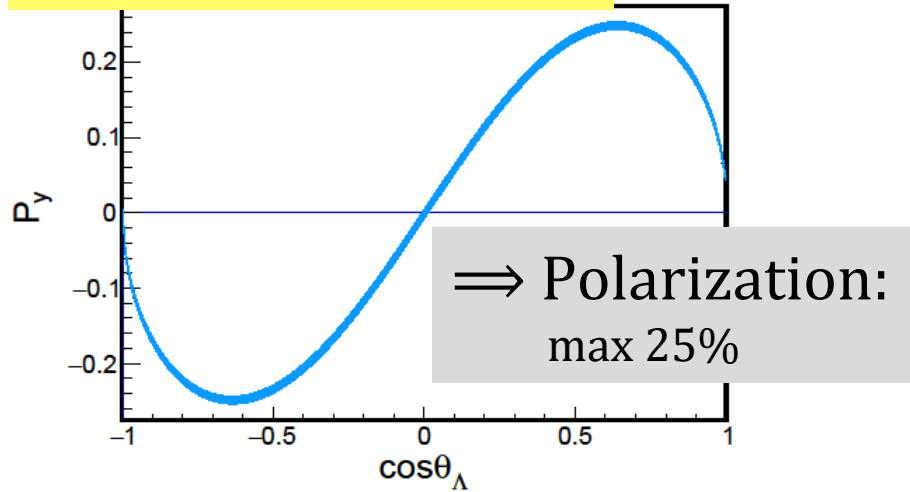
**(uncorrected for acceptance)**

**BESIII**

| Parameters         | This work                    | Previous results         |
|--------------------|------------------------------|--------------------------|
| $\alpha_\psi$      | $0.461 \pm 0.006 \pm 0.007$  | $0.469 \pm 0.027$ BESIII |
| $\Delta\Phi$ (rad) | $0.740 \pm 0.010 \pm 0.008$  | —                        |
| $\alpha_-$         | $0.750 \pm 0.009 \pm 0.004$  | $0.642 \pm 0.013$ PDG    |
| $\alpha_+$         | $-0.758 \pm 0.010 \pm 0.007$ | $-0.71 \pm 0.08$ PDG     |
| $\bar{\alpha}_0$   | $-0.692 \pm 0.016 \pm 0.006$ | —                        |
| $A_{CP}$           | $-0.006 \pm 0.012 \pm 0.007$ | $0.006 \pm 0.021$ PDG    |

# Implications of the $J/\psi \rightarrow \Lambda \bar{\Lambda}$ analysis

$$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$$



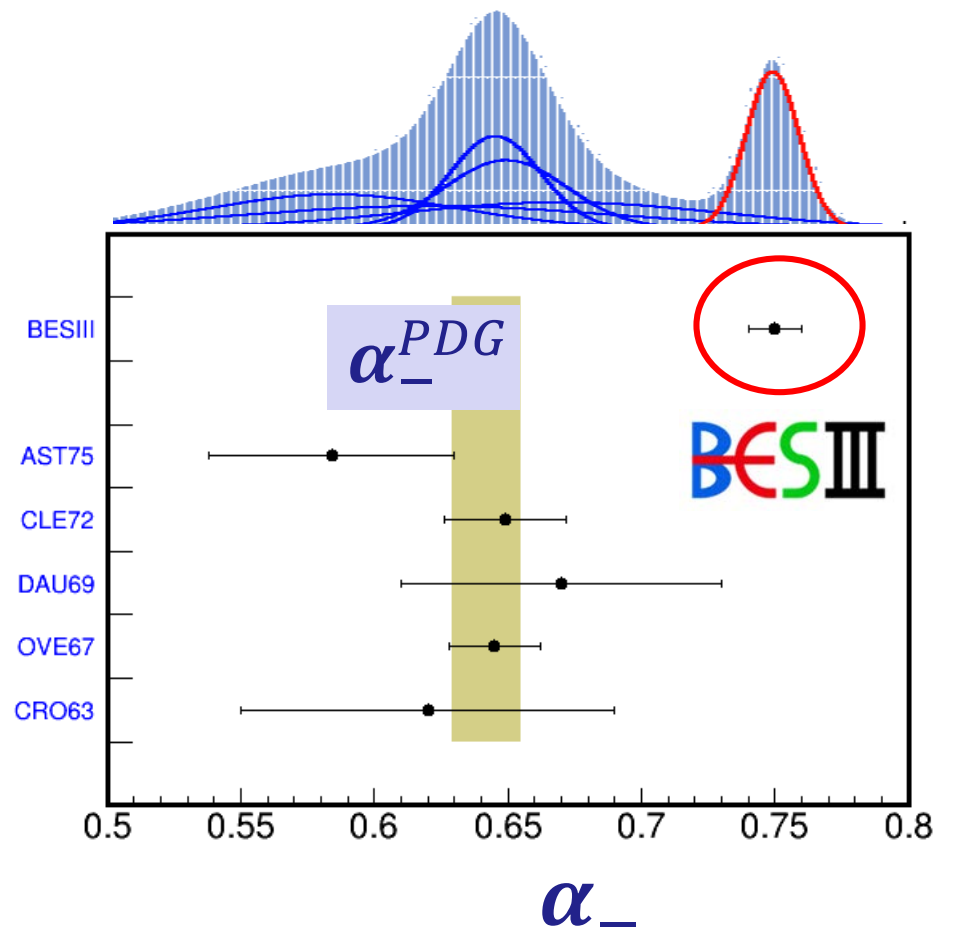
$$\langle \alpha_- \rangle_{\text{BESIII}} = \frac{\alpha_- - \alpha_+}{2} = 0.754(3)(2)$$

Since  $\rho = 0.82!$

$$\alpha_- = 0.721(6)(5)$$

D. Ireland et al arXiv:1904.07616

$$\Lambda \rightarrow p\pi^-: \alpha_- = 0.750 \pm 0.009 \pm 0.004$$



# PDG 2019 update

## $\alpha_-$ FOR $\Lambda \rightarrow p\pi^-$

[INSPIRE search](#)

| VALUE   | EVTS  | DOCUMENT ID                                    | TECN | COMMENT                            |
|---|-------|--|------|------------------------------------|
| $0.750 \pm 0.009 \pm 0.004$   | 420k  | <a href="#">ABLIKIM</a> <a href="#">2018AG</a> | BES3 | $J/\psi$ to $\Lambda\bar{\Lambda}$ |
| ... We do not use the following data for averages, fits, limits, etc. ... |       |  |      |                                    |
| $0.584 \pm 0.046$   | 8500  | <a href="#">ASTBURY</a> <a href="#">1975</a>   | SPEC |                                    |
| $0.649 \pm 0.023$   | 10325 | <a href="#">CLELAND</a> <a href="#">1972</a>   | OSPK |                                    |
| $0.67 \pm 0.06$   | 3520  | <a href="#">DAUBER</a> <a href="#">1969</a>    | HBC  | From $\Xi$ decay                   |
| $0.645 \pm 0.017$   | 10130 | <a href="#">OVERSETH</a> <a href="#">1967</a>  | OSPK | $\Lambda$ from $\pi^- p$           |
| $0.62 \pm 0.07$   | 1156  | <a href="#">CRONIN</a> <a href="#">1963</a>    | CNTR | $\Lambda$ from $\pi^- p$           |

### References:

|  |                  |  |  |  |
|--|------------------|--|--|--|
| <a href="#">ABLIKIM</a> <a href="#">2018AG</a> | arXiv:1808.08917 |  |  |  |
| <a href="#">ASTBURY</a> <a href="#">1975</a>   | NP B99 30        | Measurement of the Differential Cross Section and the Spin Correlation Parameters $P$ , $A$ , and $R$ in the Backward Peak of $\pi^- p \rightarrow K^0 \Lambda$ at 5 GeV/c |  |  |
| <a href="#">CLELAND</a> <a href="#">1972</a>   | NP B40 221       | A Measurement of the $\beta$ -Parameter in the Charged Nonleptonic Decay of the $\Lambda^0$ Hyperon  |  |  |
| <a href="#">DAUBER</a> <a href="#">1969</a>    | PR 179 1262      | Production and Decay of Cascade Hyperons   |  |  |
| <a href="#">OVERSETH</a> <a href="#">1967</a>  | PRL 19 391       | Time Reversal Invariance in $\Lambda$ Decay  |  |  |
| <a href="#">CRONIN</a> <a href="#">1963</a>    | PR 129 1795      | Measurement of the Decay Parameters of the $\Lambda$ Particle  |  |  |

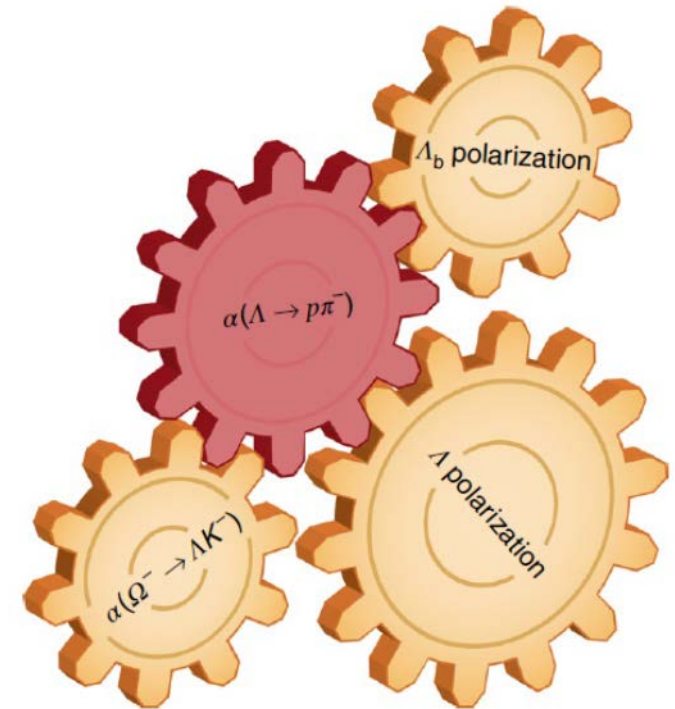
## $\alpha_+$ FOR $\bar{\Lambda} \rightarrow \bar{p}\pi^+$

[INSPIRE search](#)

| VALUE   | EVTS           | DOCUMENT ID                                    | TECN | COMMENT                                   |
|---|----------------|--|------|---|
| $-0.758 \pm 0.010 \pm 0.007$  | 420k           | <a href="#">ABLIKIM</a> <a href="#">2018AG</a> | BES3 | $J/\psi$ to $\Lambda\bar{\Lambda}$        |
| ... We do not use the following data for averages, fits, limits, etc. ... |                |  |      |   |
| $-0.755 \pm 0.083 \pm 0.063$  | $\approx 8.7k$ | <a href="#">ABLIKIM</a> <a href="#">2010</a>   | BES  | $J/\psi \rightarrow \Lambda\bar{\Lambda}$ |
| $-0.63 \pm 0.13$  | 770            | <a href="#">TIXIER</a> <a href="#">1988</a>    | DM2  | $J/\psi \rightarrow \Lambda\bar{\Lambda}$ |

### References:

|  |                  |   |  |  |
|--|------------------|---|--|--|
| <a href="#">ABLIKIM</a> <a href="#">2018AG</a> | arXiv:1808.08917 |   |  |  |
| <a href="#">ABLIKIM</a> <a href="#">2010</a>   | PR D81 012003    | Measurement of the Asymmetry Parameter for the Decay $\bar{\Lambda} \rightarrow \bar{p}\pi^+$       |  |  |
| <a href="#">TIXIER</a> <a href="#">1988</a>    | PL B212 523      | Looking at $CP$ Invariance and Quantum Mechanics in $J/\psi \rightarrow \Lambda\bar{\Lambda}$ Decay |  |  |

[news & views](#)

## PARTICLE PHYSICS

# Anomalous asymmetry

A measurement based on quantum entanglement of the parameter describing the asymmetry of the  $\Lambda$  hyperon decay is inconsistent with the current world average. This shows that relying on previous measurements can be hazardous.

Ulrik Egede

# CP violation in hyperon decays?

CP test:  $A_\Lambda = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+}$

$A_\Lambda = -0.006 \pm 0.012 \pm 0.007$

Previous result:

$A_\Lambda = 0.013 \pm 0.021$   
PS185 PRC54(96)1877

BESIII



|                                       | Events           | Error $A_\Lambda$   |  |
|---------------------------------------|------------------|---------------------|--|
| BESIII(2018)                          | $4.2 \cdot 10^5$ | $1.2 \cdot 10^{-2}$ | $1.31 \cdot 10^9$ J/ $\psi$  |
| BESIII                                | $3 \cdot 10^6$   | $5 \cdot 10^{-3}$   | $10^{10}$ J/ $\psi$<br>$L=0.47 \cdot 10^{33}$ $\Delta E = 0.9$ MeV                               |
| SuperTauCharm                         | $6 \cdot 10^8$   | $3 \cdot 10^{-4}$   | $L=10^{35}$ cm <sup>-2</sup> s <sup>-1</sup><br>$2 \cdot 10^{12}$ J/ $\psi$ $\Delta E = 0.9$ MeV |
| SuperTauCharm<br>+ reduced $\Delta E$ | $3 \cdot 10^9$   | $1.4 \cdot 10^{-4}$ | $L=10^{35}$ cm <sup>-2</sup> s <sup>-1</sup><br>$10^{13}$ J/ $\psi$ $\Delta E < 0.9$ MeV??       |

a guess

$-3 \times 10^{-5} \leq A_\Lambda \leq 4 \times 10^{-5}$   
 $-2 \times 10^{-5} \leq A_{\Xi} \leq 1 \times 10^{-5}$   
 $-5 \times 10^{-5} \leq A_{\Xi\Lambda} \leq 5 \times 10^{-5}$

CKM

$$\sigma(A_\Lambda) = \frac{\sqrt{1 + \rho}}{\sqrt{2}\alpha_\Lambda} \sigma(\alpha_\Lambda)$$

$$e^+ e^- \rightarrow J/\psi \rightarrow \Xi^- \bar{\Xi}^+ \rightarrow \Lambda \pi^- \bar{\Lambda} \pi^+ \rightarrow p \pi^- \pi^- \bar{p} \pi^+ \pi^+$$

$$d\Gamma \propto W(\xi; \omega) \quad \xi \quad 9 \text{ kinematical variables } 9\text{D PhSp}$$

Parameters: 2 production + 6 for decay chains

$$\omega = (\alpha_\psi, \Delta\Phi, \underbrace{\alpha_\Xi, \phi_\Xi, \alpha_\Lambda, \bar{\alpha}_\Xi, \bar{\phi}_\Xi, \bar{\alpha}_\Lambda}_{\text{red bracket}})$$

$$W = \sum_{\mu, \bar{\nu}} C_{\mu\bar{\nu}} \sum_{\mu', \bar{\nu}'} a_{\mu, \mu'}^\Xi a_{\bar{\nu}, \bar{\nu}'}^{\bar{\Xi}} a_{\mu', 0}^\Lambda a_{\bar{\nu}', 0}^{\bar{\Lambda}}$$

$\Delta\Phi \neq 0$  is not needed!

Variables and parameters  
factorize:

$$W(\xi; \omega) = \sum_{k=1}^M f_k(\omega) T_k(\xi)$$

$$\Delta\Phi \neq 0 : \quad M = 72 \quad \begin{matrix} \Xi^- \bar{\Xi}^+ \\ \Lambda \bar{\Lambda} \end{matrix} \quad (7)$$

$$\Delta\Phi = 0 : \quad M = 56 \quad (5)$$

# Expected number of events in BESIII

| decay mode                                   | Events published | $\mathcal{B}(\text{units } 10^{-4})$ | $\alpha_\psi$     | Events proposal    |
|--|------------------|--------------------------------------|-------------------|--------------------|
| $J/\psi \rightarrow \Lambda \bar{\Lambda}$   | $440675 \pm 670$ | $19.43 \pm 0.03 \pm 0.33$            | $0.469 \pm 0.026$ | $3400 \times 10^3$ |
| $\psi(2S) \rightarrow \Lambda \bar{\Lambda}$ | $31119 \pm 187$  | $3.97 \pm 0.02 \pm 0.12$             | $0.824 \pm 0.074$ | $220 \times 10^3$  |
| $J/\psi \rightarrow \Xi^0 \bar{\Xi}^0$       | $134846 \pm 437$ | $11.65 \pm 0.04$                     | $0.66 \pm 0.03$   | $790 \times 10^3$  |
| $\psi(2S) \rightarrow \Xi^0 \bar{\Xi}^0$     | $10839 \pm 123$  | $2.73 \pm 0.03$                      | $0.65 \pm 0.09$   | $84 \times 10^3$   |
| $J/\psi \rightarrow \Xi^- \bar{\Xi}^+$       | $42811 \pm 231$  | $10.40 \pm 0.06$                     | $0.58 \pm 0.04$   | $1900 \times 10^3$ |
| $\psi(2S) \rightarrow \Xi^- \bar{\Xi}^+$     | $5337 \pm 83$    | $2.78 \pm 0.05$                      | $0.91 \pm 0.13$   | $160 \times 10^3$  |

*scaled to*

Feb 2019:  $10^{10} J/\psi$

BESIII Phys book  $3.2 \times 10^9 \psi(2S)$

# Sensitivity estimate

detection efficiency constant

validation

$$e^+ e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}$$

|                        | $\bar{\alpha}_\Lambda$ | $\alpha_\psi$ | $\Delta\Phi$ |
|------------------------|------------------------|---------------|--------------|
| $\alpha_\Lambda$       | 0.87                   | -0.05         | -0.07        |
| $\bar{\alpha}_\Lambda$ |                        | 0.05          | 0.07         |
| $\alpha_\psi$          |                        |               | 0.28         |

$$\sigma(\alpha_\Lambda) = \frac{7}{\sqrt{N}} \quad (0.011)$$

$$\sigma(A_\Lambda) = \frac{9}{\sqrt{N}} \quad (0.014)$$

$e^+ e^- \rightarrow J/\psi \rightarrow \Xi \bar{\Xi}$

Correlation matrix:

|                        | $\bar{\alpha}_E$ | $\alpha_\Lambda$ | $\bar{\alpha}_\Lambda$ | $\phi_E$ | $\bar{\phi}_E$ | $\alpha_\psi$ | $\Delta\Phi$ |
|------------------------|------------------|------------------|------------------------|----------|----------------|---------------|--------------|
| $\alpha_E$             | 0.03             | 0.37             | 0.11                   | 0.0      | 0.0            | 0.0           | 0.0          |
| $\bar{\alpha}_E$       |                  | 0.11             | 0.37                   | 0.0      | 0.0            | 0.0           | 0.0          |
| $\alpha_\Lambda$       |                  |                  | 0.43                   | 0.0      | 0.0            | -0.1          | 0.0          |
| $\bar{\alpha}_\Lambda$ |                  |                  |                        | 0.0      | 0.0            | 0.1           | 0.0          |
| $\phi_E$               |                  |                  |                        |          | -0.15          | 0.0           | 0.0          |
| $\bar{\phi}_E$         |                  |                  |                        |          |                | 0.0           | 0.0          |
| $\alpha_\psi$          |                  |                  |                        |          |                |               | 0.0          |

$\Delta\Phi = 0$

$$\sigma(\alpha_E) = \frac{2}{\sqrt{N}}$$

$$\sigma(\phi_E) = \frac{6}{\sqrt{N}}$$

$$\sigma(\alpha_\Lambda) = \frac{3}{\sqrt{N}}$$

$$\sigma(A_\Lambda) = \frac{3.3}{\sqrt{N}}$$



$e^+ e^- \rightarrow J/\psi \rightarrow \Xi \bar{\Xi}$

Correlation matrix:

$$\sigma(\alpha_{\Xi}) = \frac{2}{\sqrt{N}}$$

$$\sigma(\phi_{\Xi}) = \frac{6}{\sqrt{N}}$$

$$\sigma(\alpha_{\Lambda}) = \frac{3}{\sqrt{N}}$$

|                          | $\bar{\alpha}_{\Xi}$ | $\alpha_{\Lambda}$ | $\bar{\alpha}_{\Lambda}$ | $\phi_{\Xi}$ | $\bar{\phi}_{\Xi}$ | $\alpha_{\psi}$ | $\Delta\Phi$ |
|--------------------------|----------------------|--------------------|--------------------------|--------------|--------------------|-----------------|--------------|
| $\alpha_{\Xi}$           | 0.03                 | 0.37               | 0.11                     | 0.0          | 0.0                | 0.0             | 0.0          |
| $\bar{\alpha}_{\Xi}$     |                      | 0.11               | 0.37                     | 0.0          | 0.0                | 0.0             | 0.0          |
| $\alpha_{\Lambda}$       |                      |                    | 0.43                     | 0.0          | 0.0                | -0.1            | 0.0          |
| $\bar{\alpha}_{\Lambda}$ |                      |                    |                          | 0.0          | 0.0                | 0.1             | 0.0          |
| $\phi_{\Xi}$             |                      |                    |                          |              |                    | -0.15           | 0.0          |
| $\bar{\phi}_{\Xi}$       |                      |                    |                          |              |                    | 0.0             | 0.0          |
| $\alpha_{\psi}$          |                      |                    |                          |              |                    |                 | 0.0          |
|                          | $\bar{\alpha}_{\Xi}$ | $\alpha_{\Lambda}$ | $\bar{\alpha}_{\Lambda}$ |              |                    |                 |              |
| $\alpha_{\Xi}$           | 0.01                 | 0.31               | 0.07                     |              |                    |                 |              |
| $\bar{\alpha}_{\Xi}$     |                      | 0.07               | 0.31                     |              |                    |                 |              |
| $\alpha_{\Lambda}$       |                      |                    | 0.39                     |              |                    |                 |              |

$\Delta\Phi = 0$

$\Delta\Phi = \frac{\pi}{2}$

$$\sigma(A_{\Lambda}) = \frac{3.3}{\sqrt{N}}$$

# Conclusions:

Polarization in  $e^+e^- \rightarrow \Lambda\bar{\Lambda}$  observed at  $J/\psi$  [phase close to  $40^\circ$ ]

$J/\psi$  and  $\psi'$  decays into hyperon-antihyperon:  
unique spin entangled system for CP tests and for determination of  
(anti-)hyperon decay parameters

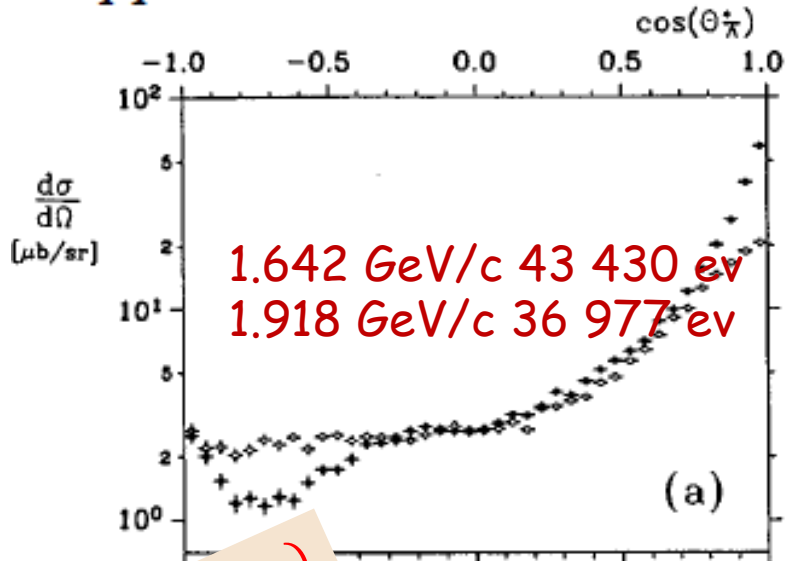
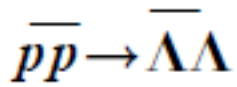
**In progress:** analysis using  $10^{10}$   $J/\psi$  collected, more  $\psi'$  data ...

Prospect for a CP violation signal at Super Tau Charm Factories

$\alpha_-: 0.642 \pm 0.012$  (PDG1978-2018)  $\Rightarrow 0.750 \pm 0.009 \pm 0.004$

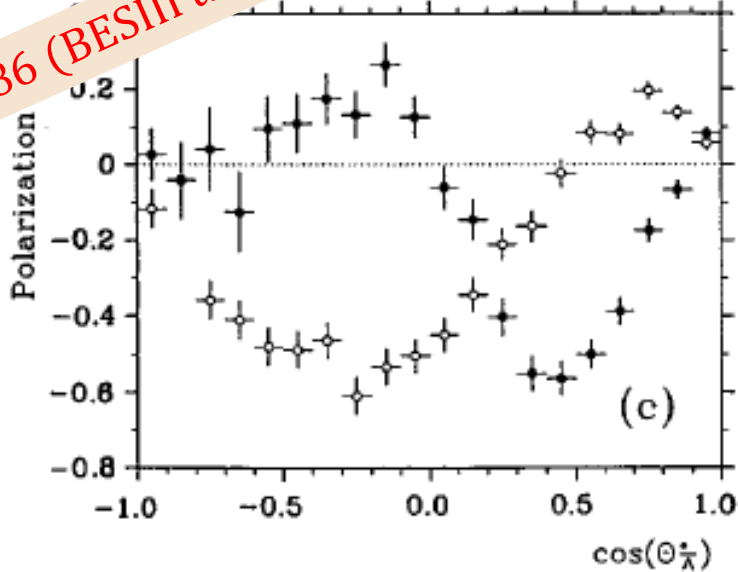
Reset of  $\alpha_-$  values in PDG 2019

Thank you!



(a)

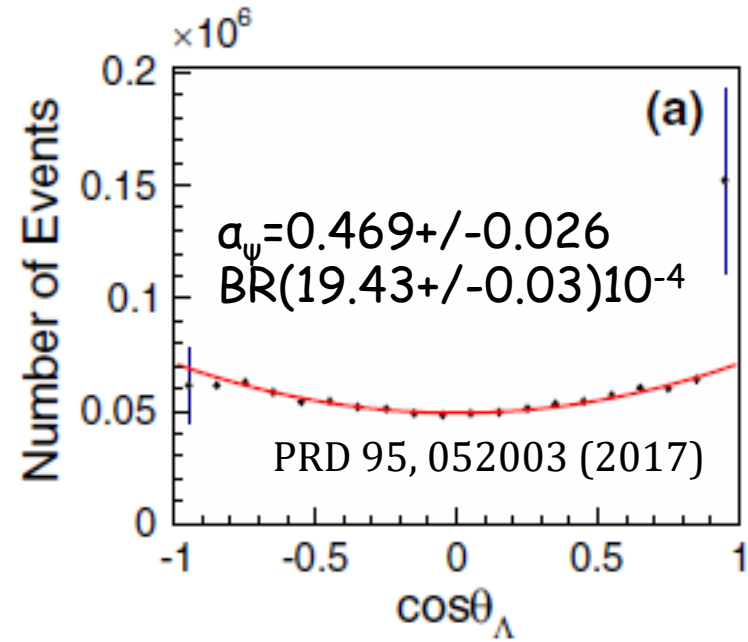
$\times 0.86$  (BESIII  $\alpha_-$ )



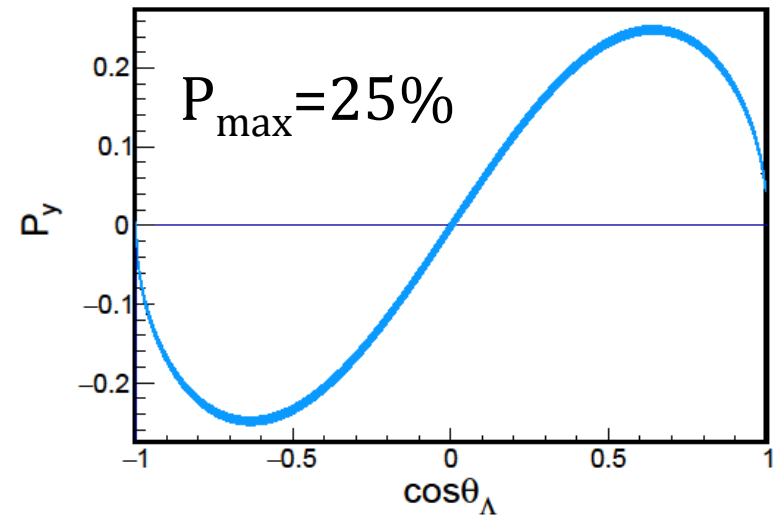
(c)

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5 parameters at each  $\theta_\Lambda$



(a)



2 global parameters