

# MCSANC<sub>ee</sub> – Monte Carlo Generator for polarized $e^+e^-$ scattering at one-loop EW

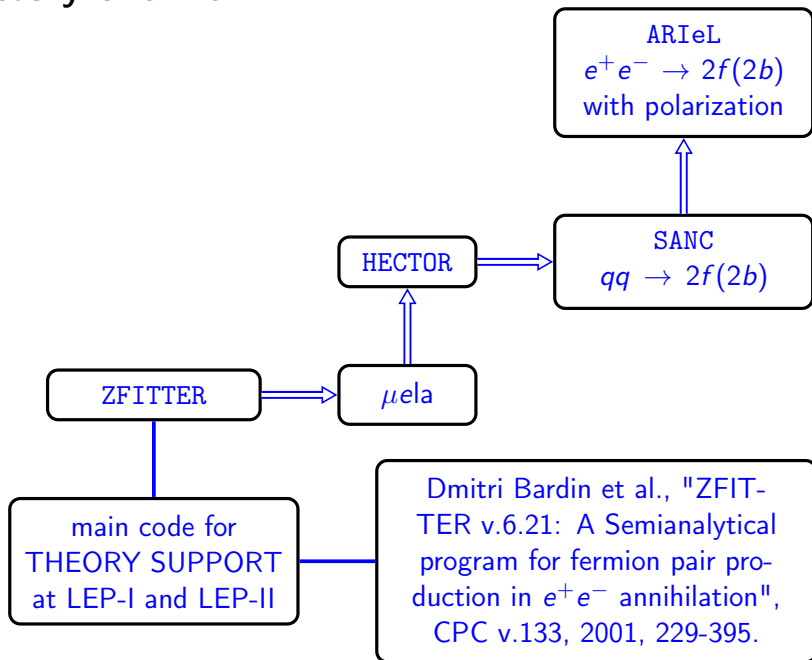
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# Outline

- History overview
- ARLeL project
- Polarization effects
- Cross section at one-loop
- High order (HA) corrections through  $\Delta\rho$
- Results
- Conclusions and plans
- Demonstration of the generator for  $e^+e^- \rightarrow ZH$

# History overview



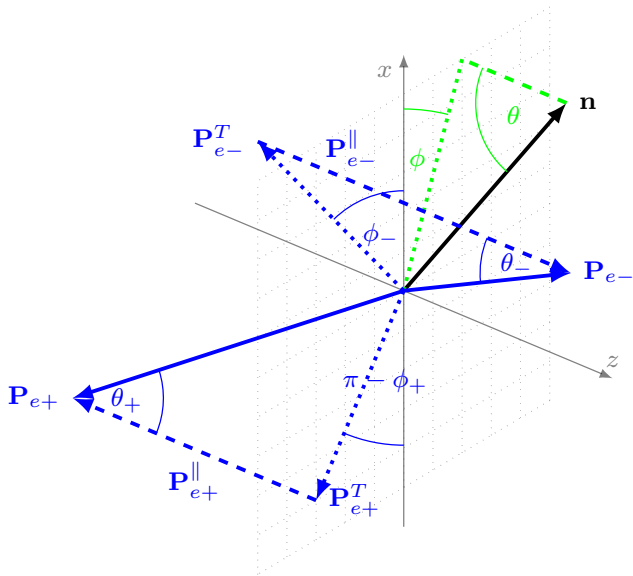
# Why ARIeL?

- **A**dvanced
- **R**esearch of
- **I**nteractions in
- $e^+e^-$
- **coL**lisions

# Goals

- Preparation of research program for future  $e^+e^-$  colliders:
  - Precision study of  $e^+e^- \rightarrow \gamma\gamma$  and setting limits on the NP models
  - Precision measurement of the Higgs boson mass  $M_H$
  - Determination of top quark polarization
  - Measurement of  $\gamma\gamma \rightarrow W^+W^-$  and  $\gamma\gamma \rightarrow ZZ$  and search for anomalous quartic coupling
- Theoretical support:
  - Create  $e^+e^-$  Monte Carlo generator with polarization at **complete one-loop EW** and **leading multiloop** for processes  $e^+e^- \rightarrow e^+e^-$  ( $\mu\mu, \tau\tau, tt, HZ, H\gamma, Z\gamma, ZZ, H\nu\nu, H\mu\mu, f\bar{f}\gamma, \gamma\gamma$ )
  - Interface to parton shower MC (PYTHIA8 etc.)
  - Implement a single-resonance approach to complex processes
  - Elaborate the standard procedure for  $2 \rightarrow 3, 4$  helicity amplitudes
  - Create building blocks for complete EW 2-loops and QCD 3-loops, plus leading EW 3-loops and QCD 4-loops

# Decomposition of the $e^\pm$ polarization vectors



# Matrix element squared

$$\begin{aligned}
 |\mathcal{M}|^2 = & L_{e-}'' R_{e+}'' |\mathcal{H}_{-+}|^2 + R_{e-}'' L_{e+}'' |\mathcal{H}_{+-}|^2 + L_{e-}'' L_{e+}'' |\mathcal{H}_{--}|^2 + R_{e-}'' R_{e+}'' |\mathcal{H}_{++}|^2 \\
 & - \frac{1}{2} P_{e-}^\perp P_{e+}^\perp \operatorname{Re} \left[ e^{i(\Phi_+ - \Phi_-)} \mathcal{H}_{++} \mathcal{H}_{--}^* + e^{i(\Phi_+ + \Phi_-)} \mathcal{H}_{+-} \mathcal{H}_{-+}^* \right] \\
 & + P_{e-}^\perp \operatorname{Re} \left[ e^{i\Phi_-} \left( L_{e+}'' \mathcal{H}_{+-} \mathcal{H}_{--}^* + R_{e+}'' \mathcal{H}_{++} \mathcal{H}_{-+}^* \right) \right] \\
 & - P_{e+}^\perp \operatorname{Re} \left[ e^{i\Phi_+} \left( L_{e-}'' \mathcal{H}_{-+} \mathcal{H}_{--}^* + R_{e-}'' \mathcal{H}_{++} \mathcal{H}_{+-}^* \right) \right],
 \end{aligned}$$

where

$$L_{e\pm}'' = \frac{1}{2}(1 - P_{e\pm}''), \quad R_{e\pm}'' = \frac{1}{2}(1 + P_{e\pm}''), \quad \Phi_\pm = \phi_\pm - \phi,$$

$\mathcal{H}_{--}, \mathcal{H}_{++}, \mathcal{H}_{-+}, \mathcal{H}_{+-}$  — helicity amplitudes.

Moortgat-Pick, G. et al. Phys.Rept. 460 (2008) 131-243

# Scheme of FF calculation

- One-loop accuracy level with using the renormalization scheme on the mass surface in  $R_\xi$  calibration with three calibration parameters  $\xi_A$ ,  $\xi_Z$  and  $\xi \equiv \xi_W$
- Dimensional regularization to parameterize the ultraviolet divergences
- Loop integrals are expressed in terms of standard scalar Passarino-Veltman functions:  $A_0$ ,  $B_0$ ,  $C_0$ ,  $D_0$
- The error criterion is the absence of  $\xi$  dependencies



# Cross-section structure

The cross-section of these processes at one-loop can be divided into four parts:

$$\sigma^{1\text{-loop}} = \sigma^{\text{Born}} + \sigma^{\text{virt}}(\lambda) + \sigma^{\text{soft}}(\lambda, \omega) + \sigma^{\text{hard}}(\omega),$$

Contributions due to:

$\sigma^{\text{Born}}$  — Born level cross-section,

$\sigma^{\text{virt}}$  — virtual(loop) corrections,

$\sigma^{\text{soft}}$  — soft photon emission,

$\sigma^{\text{hard}}$  — hard photon emission (with energy  $E_\gamma > \omega$ ).

Auxiliary parameters  $\lambda$  ("photon mass") and  $\omega$  cancel out after summation.

# Helicity Amplitudes (HA) approach

We count all contributions through HA approach.

The cross section of the generic  $2 \rightarrow 2(\gamma)$  process  $e^+e^- \rightarrow X_3X_4(\gamma)$   
( $X_3X_4 = e^-e^+, \mu^-\mu^+, ZH, \gamma Z, \gamma\gamma, \dots$ )

$$\sigma_{P_{e^-}P_{e^+}} = \frac{1}{4} \sum_{\chi_1, \chi_2} (1 + \chi_1 P_{e^-})(1 + \chi_2 P_{e^+}) \sigma_{\chi_1 \chi_2},$$

where  $\chi_i = -1(+1)$  corresponds to lepton with left (right) helicity state.

The virt(Born) cross section:

$$\frac{d\sigma_{\chi_1 \chi_2}^{\text{virt(Born)}}}{d \cos \theta} = \frac{\sqrt{\lambda(s, M_3^2, M_4^2)}}{2^5 \pi s^2} \left| \mathcal{H}_{\chi_1 \chi_2}^{\text{virt(Born)}} \right|^2,$$

where

$$\left| \mathcal{H}_{\chi_1 \chi_2}^{\text{virt(Born)}} \right|^2 = \sum_{\chi_3, \chi_4} \left| \mathcal{H}_{\chi_1 \chi_2 \chi_3 \chi_4}^{\text{virt(Born)}} \right|^2.$$

# Helicity Amplitudes (HA) approach

The soft term is factorized to Born-level cross section:

$$\frac{d\sigma_{\chi_1\chi_2}^{\text{soft}}}{d\cos\theta} = \frac{d\sigma_{\chi_1\chi_2}^{\text{Born}}}{d\cos\theta} \cdot \frac{\alpha}{2\pi} K^{\text{soft}}(\omega, \lambda).$$

The cross section for hard Bremsstrahlung

$$\frac{d\sigma_{\chi_1\chi_2}^{\text{hard}}}{ds' d\cos\theta_4 d\phi_4 d\cos\theta_5} = \frac{s-s'}{8(4\pi)^4 ss'} \frac{\sqrt{\lambda(s', M_3^2, M_4^2)}}{\sqrt{\lambda(s, m_e^2, m_e^2)}} \left| \mathcal{H}_{\chi_1\chi_2}^{\text{hard}} \right|^2,$$

where  $s = (p_1 + p_2)^2$ ,  $s' = (p_3 + p_4)^2$  and

$$\left| \mathcal{H}_{\chi_1\chi_2}^{\text{hard}} \right|^2 = \sum_{\chi_3, \chi_4, \chi_5} \left| \mathcal{H}_{\chi_1\chi_2\chi_3\chi_4\chi_5}^{\text{hard}} \right|^2.$$

# HA for Bhabha

At one-loop level we have six non-zero HAs (four independent):

$$\begin{aligned} \mathcal{H}_{++++} &= \mathcal{H}_{----} = -2e^2 \frac{s}{t} \left( \mathcal{F}_{QQ}^{(\gamma,Z)}(t, s, u) - \chi_Z^t \delta_e \mathcal{F}_{QL}^Z(t, s, u) \right), \\ \mathcal{H}_{+--+} &= \mathcal{H}_{-++-} = -2e^2 \frac{t}{s} \left( \mathcal{F}_{QQ}^{(\gamma,Z)}(s, t, u) - \chi_Z^s \delta_e \mathcal{F}_{QL}^Z(s, t, u) \right), \\ \mathcal{H}_{+---} &= 2e^2 \left( \frac{u}{s} \left[ \mathcal{F}_{QQ}^{(\gamma,Z)}(s, t, u) + \chi_Z^s (\mathcal{F}_{LL}^Z(s, t, u) - 2\delta_e \mathcal{F}_{QL}^Z(s, t, u)) \right] \right. \\ &\quad \left. + \frac{u}{t} \left[ \mathcal{F}_{QQ}^{(\gamma,Z)}(t, s, u) + \chi_Z^t (\mathcal{F}_{LL}^Z(t, s, u) - 2\delta_e \mathcal{F}_{QL}^Z(t, s, u)) \right] \right), \\ \mathcal{H}_{-++-} &= 2e^2 \left( \frac{u}{s} \mathcal{F}_{QQ}^{(\gamma,Z)}(s, t, u) + \frac{u}{t} \mathcal{F}_{QQ}^{(\gamma,Z)}(t, s, u) \right), \end{aligned}$$

where

$$\chi_Z^s = \frac{1}{4s_W^2 c_W^2} \frac{s}{s - M_Z^2 + iM_Z \Gamma_Z}, \quad \chi_Z^t = \frac{1}{4s_W^2 c_W^2} \frac{t}{t - M_Z^2}, \quad \delta_e = v_e - a_e = 2s_W^2,$$

$$\mathcal{F}_{QQ}^{(\gamma,Z)}(a, b, c) = \mathcal{F}_{QQ}^\gamma(a, b, c) + \chi_Z^a \delta_e^2 \mathcal{F}_{QQ}^Z(a, b, c).$$

We get the Born level HAs by replacing  $\mathcal{F}_{LL}^Z \rightarrow 1$ ,  $\mathcal{F}_{QL}^Z \rightarrow 1$ ,  $\mathcal{F}_{QQ}^Z \rightarrow 1$  and  $\mathcal{F}_{QQ}^\gamma \rightarrow 1$ .

# HO corrections through $\Delta\rho$

We follow the recipe introduced in [J. Fleischer et al. Phys.Lett. B319 \(1993\) 249-256](#).

The  $\rho$  parameter is defined as the ratio of the neutral current to charged current amplitudes at zero momentum transfer:

$$\rho = \frac{G_{NC}(0)}{G_{CC}(0)} = \frac{1}{1 - \Delta\rho},$$

where  $G_{CC}(0) = G_\mu$  is the Fermi constant defined from the  $\mu$ -decay width.

Perturbatively

$$\Delta\rho = \Delta\rho^{(1)} + \Delta\rho^{(2)} + \dots$$

Expanding  $\rho$  up to quadratic terms  $\Delta\rho^2$ , we have

$$\rho = 1 + \Delta\rho + \Delta\rho^2.$$

# HO corrections through $\Delta\rho$

The leading in  $G_\mu m_t^2$  NLO EW contribution to  $\Delta\rho$  is explicitly given by

$$\Delta\rho^{(1)}\Big|^{G_\mu} = 3x_t = \frac{3\sqrt{2}G_\mu m_t^2}{16\pi^2}.$$

At the two-loop level, quantity  $\Delta\rho$  contains two contributions:

$$\Delta\rho = 3x_t \left[ 1 + \rho^{(2)} \left( M_H^2/m_t^2 \right) x_t \right] \left[ 1 - \frac{2\alpha_s(M_Z^2)}{9\pi} (\pi^2 + 3) \right].$$

They consist of the following:

- two-loop EW part at  $\mathcal{O}(G_\mu^2)$ .
- mixed two-loop EW $\otimes$ QCD at  $\mathcal{O}(G_\mu\alpha_s)$

# HO corrections through $\Delta\rho$

The leading in  $G_\mu m_t^2$  universal higher order (h.o.) corrections may be taken into account via the replacements, [Dittmaier et al., JHEP 1001 (2010) 060]:

$$\begin{aligned}s_W^2 &\rightarrow \bar{s}_W^2 \equiv s_W^2 + \Delta\rho c_W^2, \\c_W^2 &\rightarrow \bar{c}_W^2 \equiv 1 - \bar{s}_W^2 = (1 - \Delta\rho) c_W^2, \\ \alpha_{G_\mu} &\rightarrow \alpha_{G_\mu} \frac{\bar{s}_W^2}{s_W^2}\end{aligned}$$

in the LO expression for the cross section.

This approach correctly reproduces terms up to  $\mathcal{O}(\Delta\rho^2)$ .

Given these replacements, we get the contributions of h.o. corrections to the scalar form factors of the invariant amplitude

# HO corrections through $\Delta\rho$

A large group of dominant radiative corrections can be absorbed into the shift of the  $\rho$  parameter from its lowest order value  $\rho_{Born} = 1$ .

These groups of radiative corrections are:

$$\begin{aligned}\Delta\rho = & \Delta\rho_{x_t} + \Delta\rho_{\alpha\alpha_s} + \Delta\rho_{x_t\alpha_s} + \Delta\rho_{x_t^3+x_t^2\alpha_s} \\ & + \Delta\rho_{x_t\alpha_s^2} + \Delta\rho_{x_t^2} + \Delta\rho_{x_t\alpha_s^3} + \Delta\rho_{x_t^2(bos)} + \Delta\rho_{x_t^3}.\end{aligned}$$

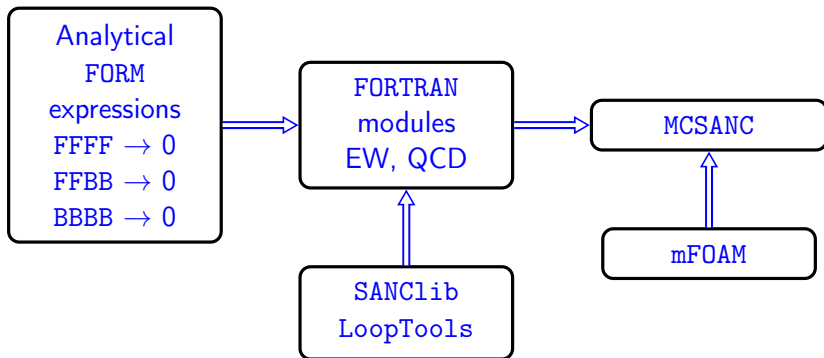


# HO corrections through $\Delta\rho$

- $\Delta\rho_{x_t}$  — 1-loop EW at  $\mathcal{O}(x_t)$
- $\Delta\rho_{\alpha\alpha_s}$  — 2-loop mixed QCD-EW at  $\mathcal{O}(\alpha\alpha_s)$
- $\Delta\rho_{x_t\alpha_s}$  — 2-loop large top-mass at  $\mathcal{O}(x_t\alpha_s)$
- $\Delta\rho_{x_t^3+x_t^2\alpha_s}$  — leading 3-loop large top-mass contributions
- $\Delta\rho_{x_t\alpha_s^2}$  — 3-loop mixed at  $\mathcal{O}(x_t\alpha_s^2)$
- $\Delta\rho_{x_t^2}$  — 2-loop EW at  $\mathcal{O}(x_t^2)$
- $\Delta\rho_{x_t\alpha_s^3}$  — 4-loop mixed at  $\mathcal{O}(x_t\alpha_s^3)$
- $\Delta\rho_{x_t^2(bos)}$  — 2-loop EW bosonic corrections at  $\mathcal{O}(x_t^2)$
- $\Delta\rho_{x_t^3(bos)}$  — 3-loop EW corrections at  $\mathcal{O}(x_t^3)$

All of these corrections that were computed by different groups in the past will be included in the generator

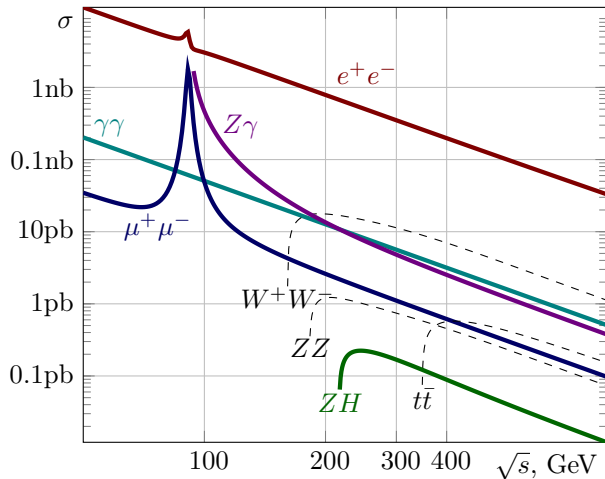
# MCSANC<sub>ee</sub> generator



We created Monte Carlo generator of unweighted events for the polarized  $e^+e^-$  scattering with complete one-loop EW corrections.

This generator uses adaptive Monte Carlo algorithm **mFOAM** [S. Jadach and P. Sawicki. CPC 177:441-458,2007] which is a part of **ROOT** [<https://root.cern.ch>] program.

# Basic processes of SM for $e^+e^-$ annihilation



The cross sections are given for polar angles between  $10^\circ < \theta < 170^\circ$  in the final state

# Setup for tuned comparison

Input parameters:

$$\alpha^{-1}(0) = 137.03599976,$$

$$M_W = 80.4514958 \text{ GeV}, \quad M_Z = 91.1876 \text{ GeV}, \quad \Gamma_Z = 2.49977 \text{ GeV},$$

$$m_e = 0.51099907 \text{ MeV}, \quad m_\mu = 0.105658389 \text{ GeV}, \quad m_\tau = 1.77705 \text{ GeV},$$

$$m_d = 0.083 \text{ GeV}, \quad m_s = 0.215 \text{ GeV}, \quad m_b = 4.7 \text{ GeV},$$

$$m_u = 0.062 \text{ GeV}, \quad m_c = 1.5 \text{ GeV}, \quad m_t = 173.8 \text{ GeV}.$$

Cuts:

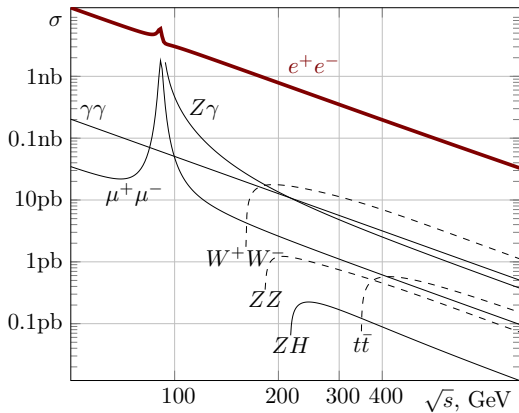
$$|\cos \theta| < 0.9,$$

$$E_\gamma > 1 \text{ GeV} \quad (\text{for comparison of hard Bremsstrahlung}).$$

Tuned comparison of our results for polarized Born and hard Bremsstrahlung with the results **WHIZARD** [Eur.Phys.J.C71 (2011) 1742] and **CalcHEP** [CPC 184(2013) 1729-1769] programs shows agreement within statistical errors.

Unpolarized Soft + virtual contribution agree with the results of **a1TALC** [CPC 174 (2006) 71-82] (for  $e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, \tau^+\tau^-$ ) and **Grace-Loop** [Phys.Rept. 430 (2006) 117-209] (for  $e^+e^- \rightarrow ZH$ )

$$e^+e^- \rightarrow e^+e^-$$



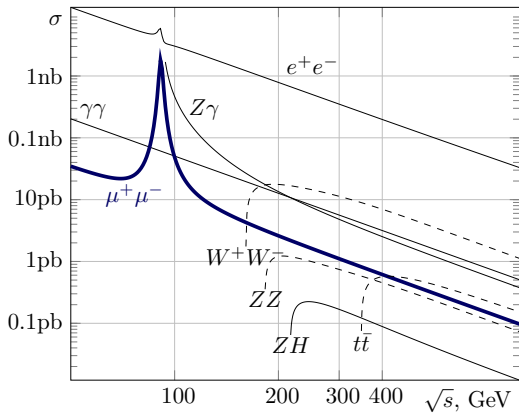
For details, see the talk by [Andrej Arbuzov](#)

$e^+e^- \rightarrow e^+e^-$ : Born vs 1-loop

$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250 \text{ GeV}$				
$\sigma_{e^+e^-}^{\text{Born}}$ , pb	56.676(1)	57.774(1)	56.273(1)	59.275(1)
$\sigma_{e^+e^-}^{\text{1-loop}}$ , pb	61.73(1)	62.59(1)	61.88(1)	63.29(1)
$\delta$ , %	8.92(1)	8.33(1)	9.96(1)	6.77(1)
$\sqrt{s} = 500 \text{ GeV}$				
$\sigma_{e^+e^-}^{\text{Born}}$ , pb	14.379(1)	15.031(1)	12.706(1)	17.355(1)
$\sigma_{e^+e^-}^{\text{1-loop}}$ , pb	15.47(1)	15.87(1)	13.86(1)	17.88(1)
$\delta$ , %	7.56(1)	5.59(1)	9.09(1)	3.05(1)
$\sqrt{s} = 1000 \text{ GeV}$				
$\sigma_{e^+e^-}^{\text{Born}}$ , pb	3.6792(1)	3.9057(1)	3.0358(1)	4.7756(1)
$\sigma_{e^+e^-}^{\text{1-loop}}$ , pb	3.864(1)	3.945(1)	3.233(1)	4.654(1)
$\delta$ , %	5.02(1)	0.99(1)	6.50(1)	-2.54(1)

$$e^+e^- \rightarrow \mu^-\mu^+$$

$$e^+e^- \rightarrow \tau^-\tau^+$$



$e^+e^- \rightarrow \mu^+\mu^-$ : Born vs 1-loop

$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250 \text{ GeV}$				
$\sigma_{\mu^+\mu^-}^{\text{Born}}$ , pb	1.417(1)	1.546(1)	0.7690(2)	2.323(1)
$\sigma_{\mu^+\mu^-}^{1\text{-loop}}$ , pb	2.397(1)	2.614(1)	1.301(1)	3.927(1)
$\delta, \%$	69.1(1)	69.1(1)	69.2(1)	69.1(1)
$\sqrt{s} = 500 \text{ GeV}$				
$\sigma_{\mu^+\mu^-}^{\text{Born}}$ , pb	0.3436(1)	0.3716(1)	0.1857(1)	0.5575(1)
$\sigma_{\mu^+\mu^-}^{1\text{-loop}}$ , pb	0.4696(1)	0.4953(1)	0.2506(1)	0.7399(1)
$\delta, \%$	36.7(1)	33.3(1)	35.0(1)	32.7(1)
$\sqrt{s} = 1000 \text{ GeV}$				
$\sigma_{\mu^+\mu^-}^{\text{Born}}$ , pb	0.08535(1)	0.09213(1)	0.04608(1)	0.1382(1)
$\sigma_{\mu^+\mu^-}^{1\text{-loop}}$ , pb	0.1163(1)	0.1212(1)	0.06169(1)	0.1807(1)
$\delta, \%$	36.2(1)	31.6(1)	33.9(1)	30.8(1)



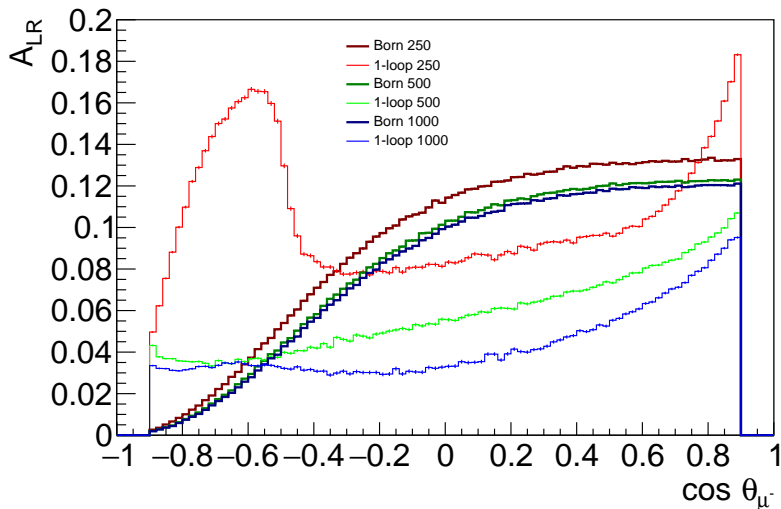
# $e^+e^- \rightarrow \tau^+\tau^-$ : Born vs 1-loop

$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250 \text{ GeV}$				
$\sigma_{\tau^+\tau^-}^{\text{Born}}, \text{ pb}$	1.417(1)	1.546(1)	0.7692(1)	2.324(1)
$\sigma_{\tau^+\tau^-}^{1\text{-loop}}, \text{ pb}$	2.360(1)	2.575(1)	1.298(1)	3.850(1)
$\delta, \%$	66.5(1)	66.5(1)	68.8(1)	65.7(1)
$\sqrt{s} = 500 \text{ GeV}$				
$\sigma_{\tau^+\tau^-}^{\text{Born}}, \text{ pb}$	0.3436(1)	0.3715(1)	0.1857(1)	0.5575(1)
$\sigma_{\tau^+\tau^-}^{1\text{-loop}}, \text{ pb}$	0.4606(1)	0.4861(1)	0.2466(1)	0.7257(1)
$\delta, \%$	34.0(3)	30.8(1)	32.8(1)	30.1(1)
$\sqrt{s} = 1000 \text{ GeV}$				
$\sigma_{\tau^+\tau^-}^{\text{Born}}, \text{ pb}$	0.08534(2)	0.09213(1)	0.04608(1)	0.1382(1)
$\sigma_{\tau^+\tau^-}^{1\text{-loop}}, \text{ pb}$	0.1134(1)	0.11885(2)	0.06067(1)	0.1770(1)
$\delta, \%$	33.6(1)	29.0(1)	31.7(1)	28.1(1)

$e^+e^- \rightarrow \mu^+\mu^-$ :  $A_{LR}$  distributions in  $\cos\theta$

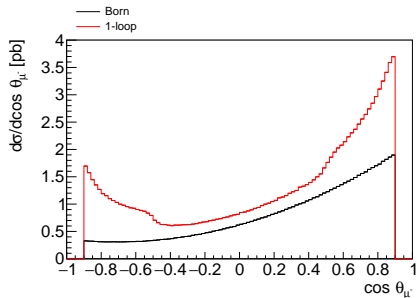
$$A_{LR} = \frac{\sigma_{LR} - \sigma_{RL}}{\sigma_{LR} + \sigma_{RL}}$$

$e^+e^- \rightarrow \mu^+\mu^-$

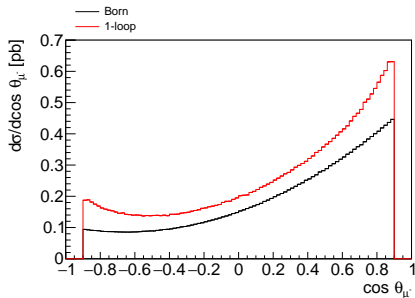


# $e^+e^- \rightarrow \mu^+\mu^-$ : distributions in $\cos\theta$

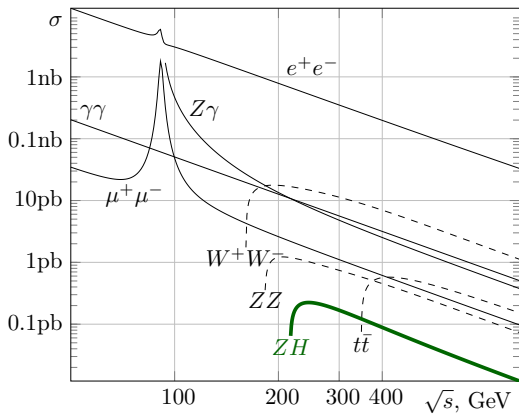
250 GeV:



500 GeV:



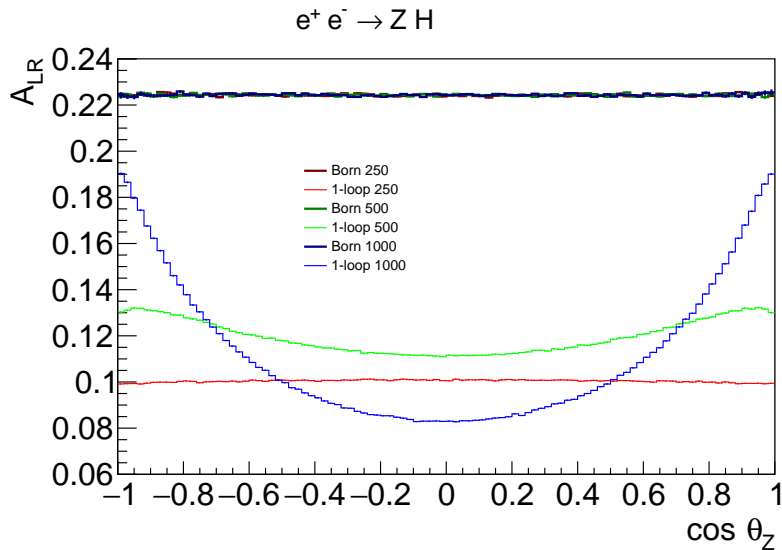
$$e^+ e^- \rightarrow ZH$$



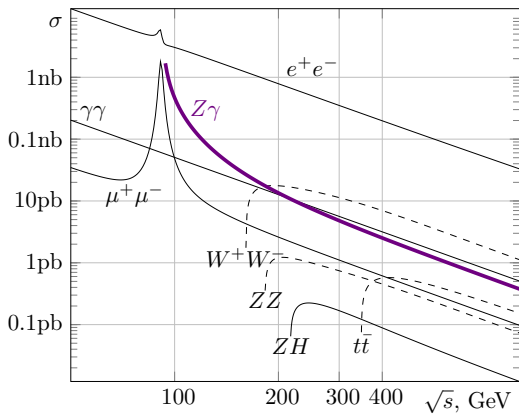
# $e^+e^- \rightarrow ZH$ : Born vs 1-loop

$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250 \text{ GeV}$				
$\sigma^{\text{Born}}, \text{fb}$	205.64(1)	242.55(1)	116.16(1)	368.93(1)
$\sigma^{1\text{-loop}}, \text{fb}$	186.6(1)	201.5(1)	100.8(1)	302.2(1)
$\delta, \%$	-9.24(1)	-16.94(1)	-13.25(1)	-18.10(1)
$\sqrt{s} = 500 \text{ GeV}$				
$\sigma^{\text{Born}}, \text{fb}$	51.447(1)	60.680(1)	29.061(1)	92.299(1)
$\sigma^{1\text{-loop}}, \text{fb}$	57.44(1)	62.71(1)	31.25(1)	94.17(2)
$\delta, \%$	11.65(1)	3.35(2)	7.54(1)	2.03(2)
$\sqrt{s} = 1000 \text{ GeV}$				
$\sigma^{\text{Born}}, \text{fb}$	11.783(1)	13.898(1)	6.6559(1)	21.140(1)
$\sigma^{1\text{-loop}}, \text{fb}$	12.92(1)	13.91(1)	6.995(1)	20.83(1)
$\delta, \%$	9.68(1)	0.10(2)	5.09(2)	-1.47(2)

$e^+e^- \rightarrow ZH$ :  $A_{LR}$  distributions in  $\cos\theta$



$$e^+e^- \rightarrow Z\gamma$$



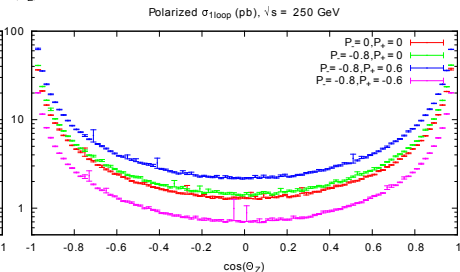
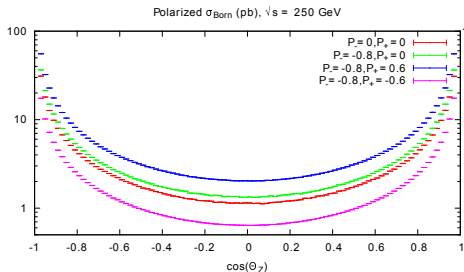
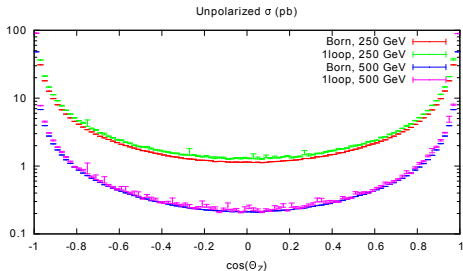
# $e^+e^- \rightarrow Z\gamma$ : Born vs 1-loop (preliminary)

$\sqrt{s}$ , GeV	250	500	1000
$\sigma_{Z\gamma}^{\text{Born}}$ , pb	15.7038(6)	3.3858(3)	0.81958(3)
$\sigma_{Z\gamma}^{\text{1-loop}}$ , pb	24.37(1)	5.23(6)	1.237(3)
$\delta$ , %	55.20(6)	54.4(2)	50.9(4)

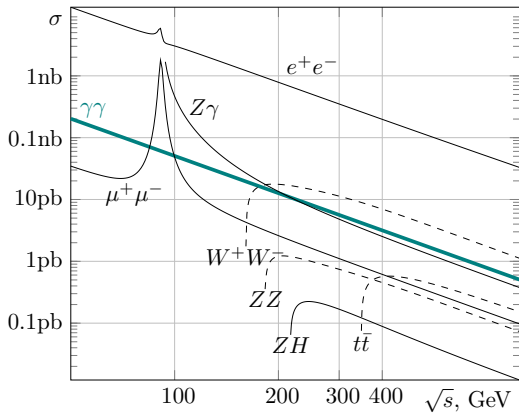
$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250$ GeV				
$\sigma_{Z\gamma}^{\text{Born}}$ , pb	15.7038(6)	18.520(4)	8.870(3)	28.174(2)
$\sigma_{Z\gamma}^{\text{1-loop}}$ , pb	24.37(1)	28.00(1)	13.53(1)	42.13(2)
$\delta$ , %	55.20(6)	51.11(8)	52.57(9)	49.55(7)



# $e^+e^- \rightarrow Z\gamma$ : distributions in $\cos\theta_Z$ (preliminary)



$$e^+ e^- \rightarrow \gamma\gamma$$

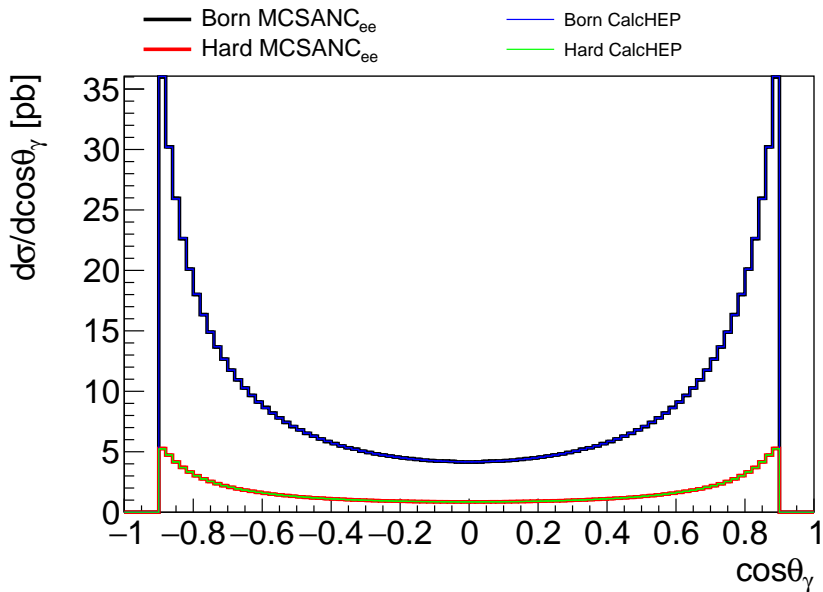


$e^+e^- \rightarrow \gamma\gamma$ : WHIZARD vs CalcHEP vs MCSAN Cee

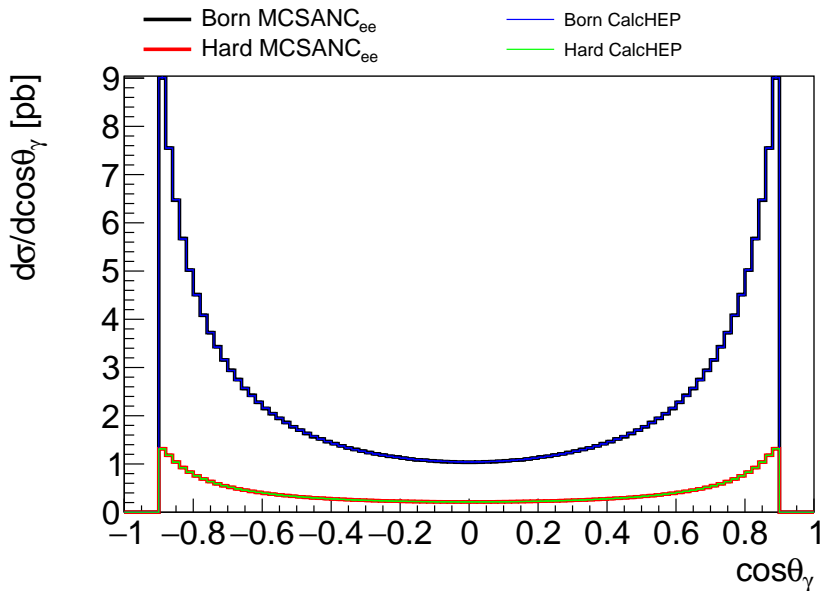
$P_{e^-}, P_{e^+}$	0, 0	-0.8, 0	-0.8, -0.6	-0.8, 0.6
$\sqrt{s} = 250 \text{ GeV}$				
$\sigma^{\text{hard}}, \text{fb}$	594.1(1)	594.1(1)	308.9(1)	879.2(1)
$\sigma^{\text{hard}}, \text{fb}$	594.0(1)	593.8(1)	308.8(1)	879.2(1)
$\sigma^{\text{hard}}, \text{fb}$	594.0(1)	594.2(1)	308.9(1)	879.1(1)
$\sqrt{s} = 500 \text{ GeV}$				
$\sigma^{\text{hard}}, \text{fb}$	158.6(1)	158.5(1)	82.50(1)	234.5(1)
$\sigma^{\text{hard}}, \text{fb}$	158.7(1)	158.6(1)	82.50(1)	234.8(1)
$\sigma^{\text{hard}}, \text{fb}$	158.7(1)	158.7(1)	82.50(1)	234.8(1)
$\sqrt{s} = 1000 \text{ GeV}$				
$\sigma^{\text{hard}}, \text{fb}$	42.18(1)	42.20(1)	21.95(1)	62.43(1)
$\sigma^{\text{hard}}, \text{fb}$	42.19(1)	42.18(1)	21.94(1)	62.45(1)
$\sigma^{\text{hard}}, \text{fb}$	42.17(1)	42.20(1)	21.94(1)	62.44(1)

Cuts:  $|\cos\theta_\gamma| < 0.9$ ,  $E_\gamma > 0.0025 \text{ GeV}$  for each of the final photons

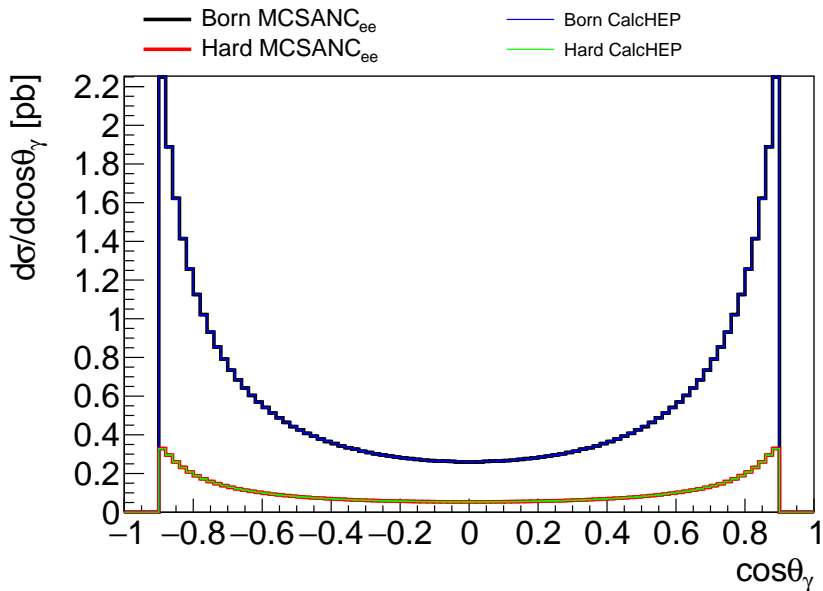
$e^+e^- \rightarrow \gamma\gamma$ : distribution in  $\cos\theta$ ,  $\sqrt{s}=250$  GeV



$e^+e^- \rightarrow \gamma\gamma$ : distribution in  $\cos\theta$ ,  $\sqrt{s}=500$  GeV



$e^+e^- \rightarrow \gamma\gamma$ : distribution in  $\cos\theta$ ,  $\sqrt{s}=1000\text{GeV}$



# Summary

- We created Monte Carlo generator of unweighted events  $\text{MCSANC}_{ee}$  for polarized  $e^+e^-$  scattering with complete one-loop EW corrections
- Now it includes the following processes:
  - $e^+e^- \rightarrow e^+e^-$  ([Phys.Rev.D 98, 013001](#))
  - $e^+e^- \rightarrow ZH$  ([arXiv:1812.10965](#))
  - $e^+e^- \rightarrow \mu^+\mu^-$  (or  $\tau^+\tau^-$ ) ([preliminary](#))
  - $e^+e^- \rightarrow Z\gamma$  ([preliminary](#))
  - $e^+e^- \rightarrow \gamma\gamma$  ([preliminary](#))
- Support of Les Houches format for events

# Plans

- to include in **MCSANC<sub>ee</sub>** the following processes:
  - $e^+e^- \rightarrow t\bar{t}$
  - $e^+e^- \rightarrow ZZ$
  - $e^+e^- \rightarrow H\gamma$
  - $e^+e^- \rightarrow f\bar{f}\gamma$
  - $e^+e^- \rightarrow f\bar{f}H$
  - $\gamma\gamma \rightarrow \gamma\gamma, \gamma\gamma \rightarrow e^+e^-, \gamma\gamma \rightarrow HZ, \gamma\gamma \rightarrow Z\gamma, \gamma\gamma \rightarrow ZZ$
  - $e^\pm\gamma \rightarrow e^\pm\gamma$
- to extend the functionality of the generator with actual energy spectrum of initial particles, leading multi-loop corrections, and with transverse polarization
- Public pre-release: **June 2019**