

# Weak $p_T$ dependence of inclusive jet $R_{AA}$ and extraction of jet energy loss distributions

Yayun He (贺亚运)

Central China Normal University  
(华中师范大学)



第十七届全国核物理大会  
10月8-12日 2019

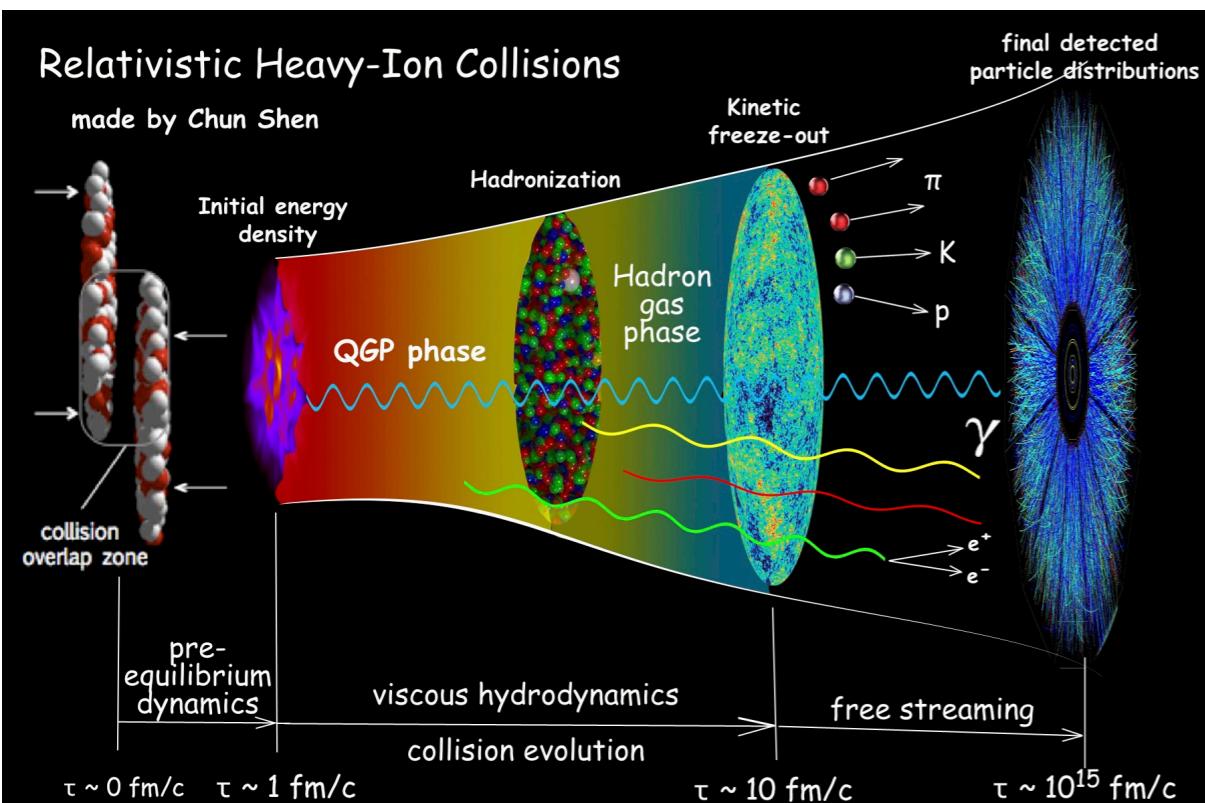


# Outline

- I. Motivation
- II. The Linear Boltzmann Transport (LBT) Model
- III. Results: suppression of inclusive jet,  
jet energy loss distributions
- IV. Summary



# Motivation



(made by Chun Shen, <https://u.osu.edu/vishnu/category/visualization/>)

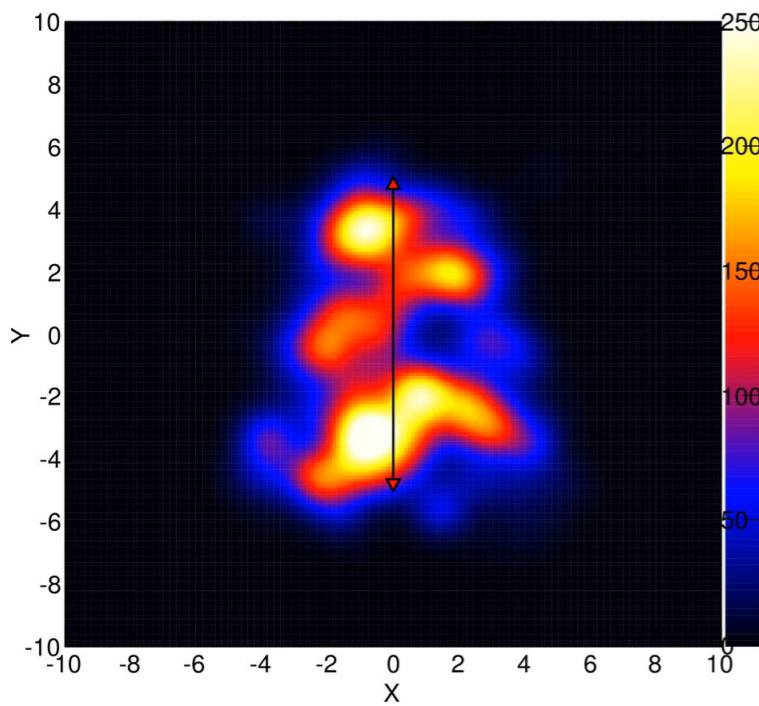
Two beams of nuclei colliding, large energy density deposits. Quark and gluon de-confine, “little bang” like early universe. QGP expands, cooling down to hadron phase. Hadrons re-scatter, and go free streaming, detected by the detector.

The quark-gluon plasma (QGP), predicted by QCD and confirmed at RHIC and LHC experiments, is created in high-energy heavy-ion collisions. It is a hot and dense medium.

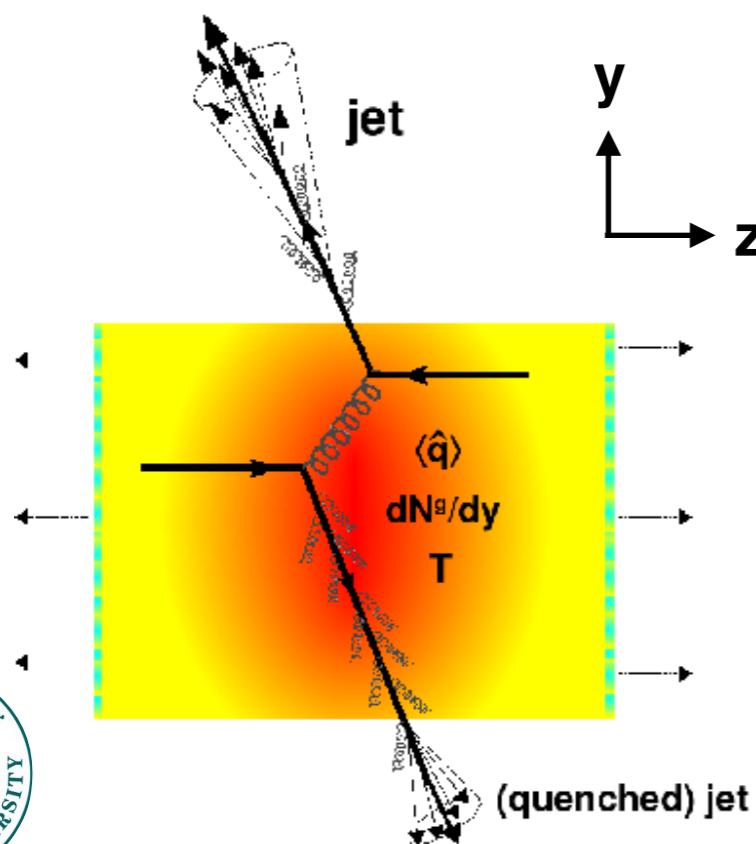


# Motivation

$E_d$  at  $\eta=0$  and  $t= 0.2$  fm



W. Chen, et al, Phys. Lett. B 777 (2018) 86–90



QGP Probes:

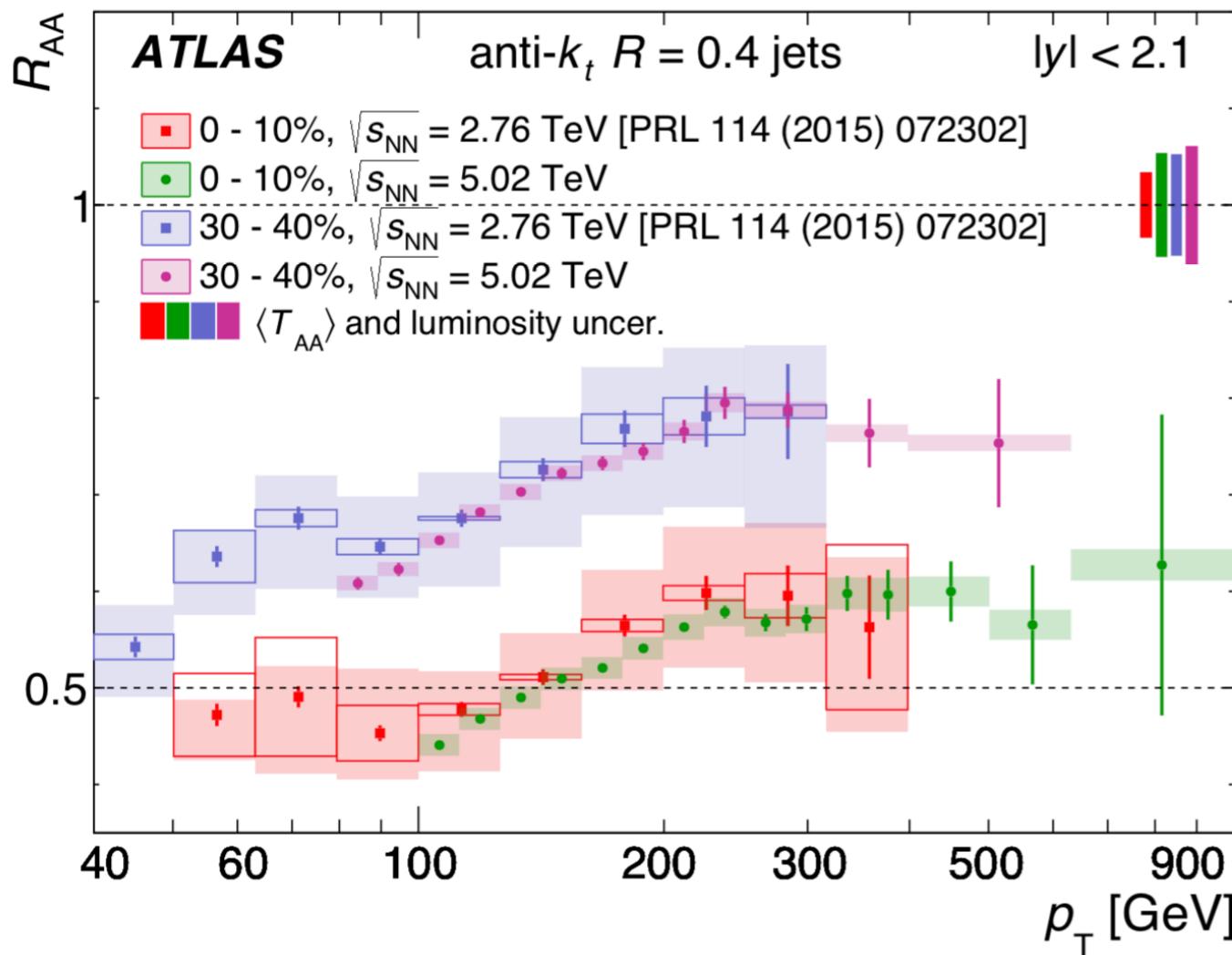
**hard probes**: large momentum or short distance, such as **jets**, high- $p_T$  hadrons, heavy quark.

jet: a spray of collimated hadrons with high transverse momentum

jet quenching:  
jet energy loss when a jet propagates in the medium



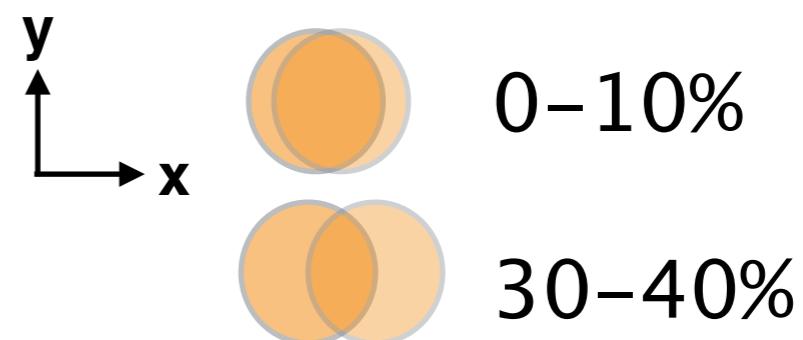
# Motivation



ATLAS, Phys. Rev. Lett. 114 (2015), 072302 arXiv:1411.2357,  
 ATLAS, Phys. Lett. B 790 (2019) 108, arXiv:1805.05635

$$R_{AA} = \frac{1}{\langle N_{coll} \rangle} \frac{d\sigma_{AA}^{jet}}{d\sigma_{pp}^{jet}}$$

$R_{AA} = 1$  No suppression;  
 $R_{AA} < 1$  suppression arises;  
 The smaller  $R_{AA}$  means  
 the stronger suppression.



Jet  $R_{AA}$  are almost the **same** and go **flat** for 2.76 TeV and 5.02 TeV. Why ?



# The LBT model

$$p_a \cdot \partial f_a = \int \sum_{bcd} \prod_{i=b,c,d} \frac{d^3 p_i}{2E_i(2\pi)^3} (f_c f_d - f_a f_b) |\mathcal{M}_{ab \rightarrow cd}|^2$$

$$\times \frac{\gamma_b}{2} S_2(\hat{s}, \hat{t}, \hat{u}) (2\pi)^4 \delta^4(p_a + p_b - p_c - p_d) + \text{inelastic}$$

$$S_2(\hat{s}, \hat{t}, \hat{u}) = \theta(\hat{s} \geq 2\mu_D^2) \theta(-\hat{s} + \mu_D^2 \leq \hat{t} \leq -\mu_D^2), \quad \mu_D^2 = \frac{3}{2} g^2 T^2$$

$$\Gamma_a^{\text{el}} \equiv \frac{p \cdot u}{p_0} \sum_{bcd} \rho_b(x) \sigma_{ab \rightarrow cd}$$

**LO perturbative QCD**

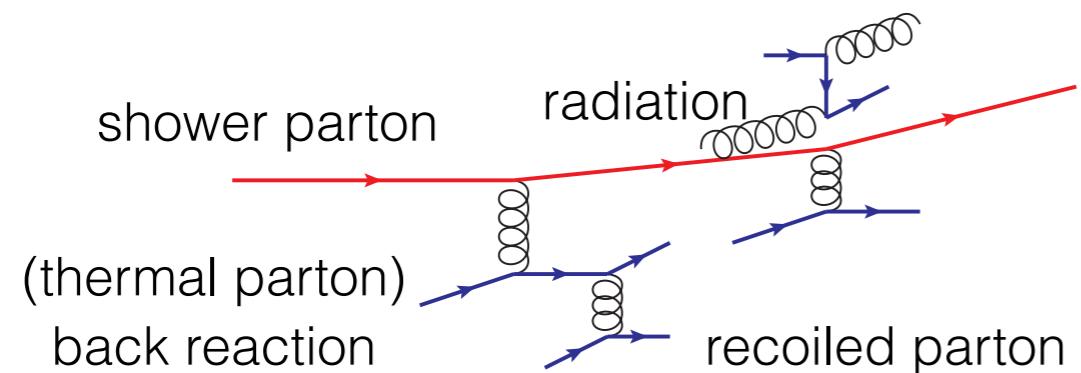
J. Auvinen et al, Phys. Rev. C 82(2010) 024906

$$\frac{d\Gamma_a^{\text{inel}}}{dz dk_\perp^2} = \frac{6\alpha_s P_a(z) k_\perp^4}{\pi(k_\perp^2 + z^2 m^2)^4} \frac{p \cdot u}{p_0} \hat{q}_a(x) \sin^2 \frac{\tau - \tau_i}{2\tau_f}$$

**LO+NLO twist-4**

Guo and Wang, PRL 85 (2000) 3591

Zhang, Wang and Wang, PRL 93 (2004) 072301



- ◆ re-scattering
- ◆ back reaction

- ◆ Linear approximation, and valid for  $\delta f \ll f$



# Framework

The inclusive jet shower partons from PYTHIA 8

T. Sjostrand, S. Mrenna, and P. Z. Skands, JHEP 05 (2006) 026.

Initial condition from AMPT

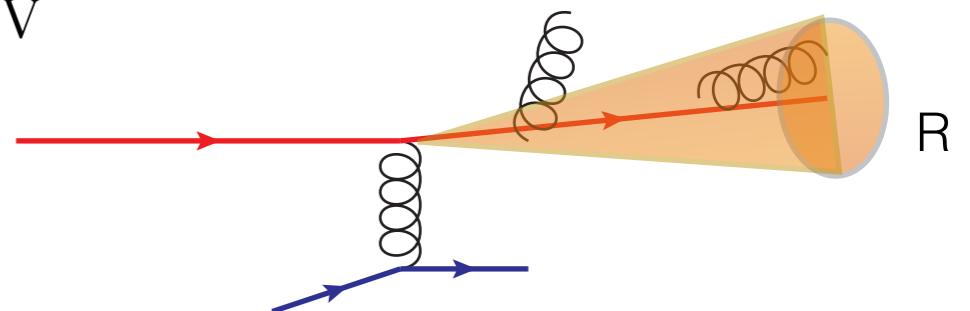
Z.-W. Lin, C. M. Ko, B.-A. Li, B. Zhang, and S. Pal,  
Phys. Rev. C 72, 064901 (2005).

**evolution with a hydro background:  
collisional + radiation in QGP phase,  
free streaming in hadron phase**

*out-of-cone  
jet energy loss*

freeze-out temperature:  $T_f = 137$  MeV

Final inclusive jet



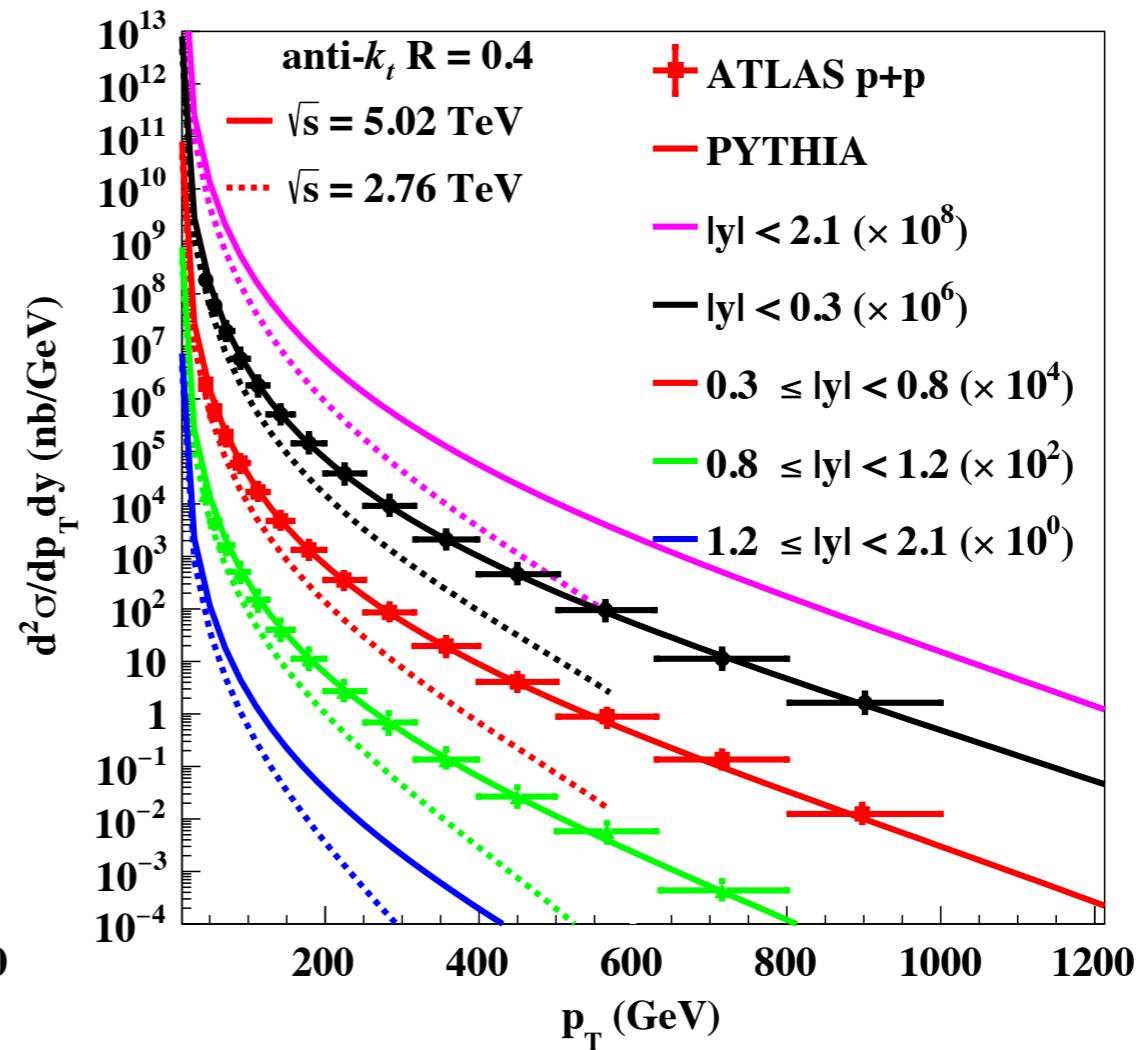
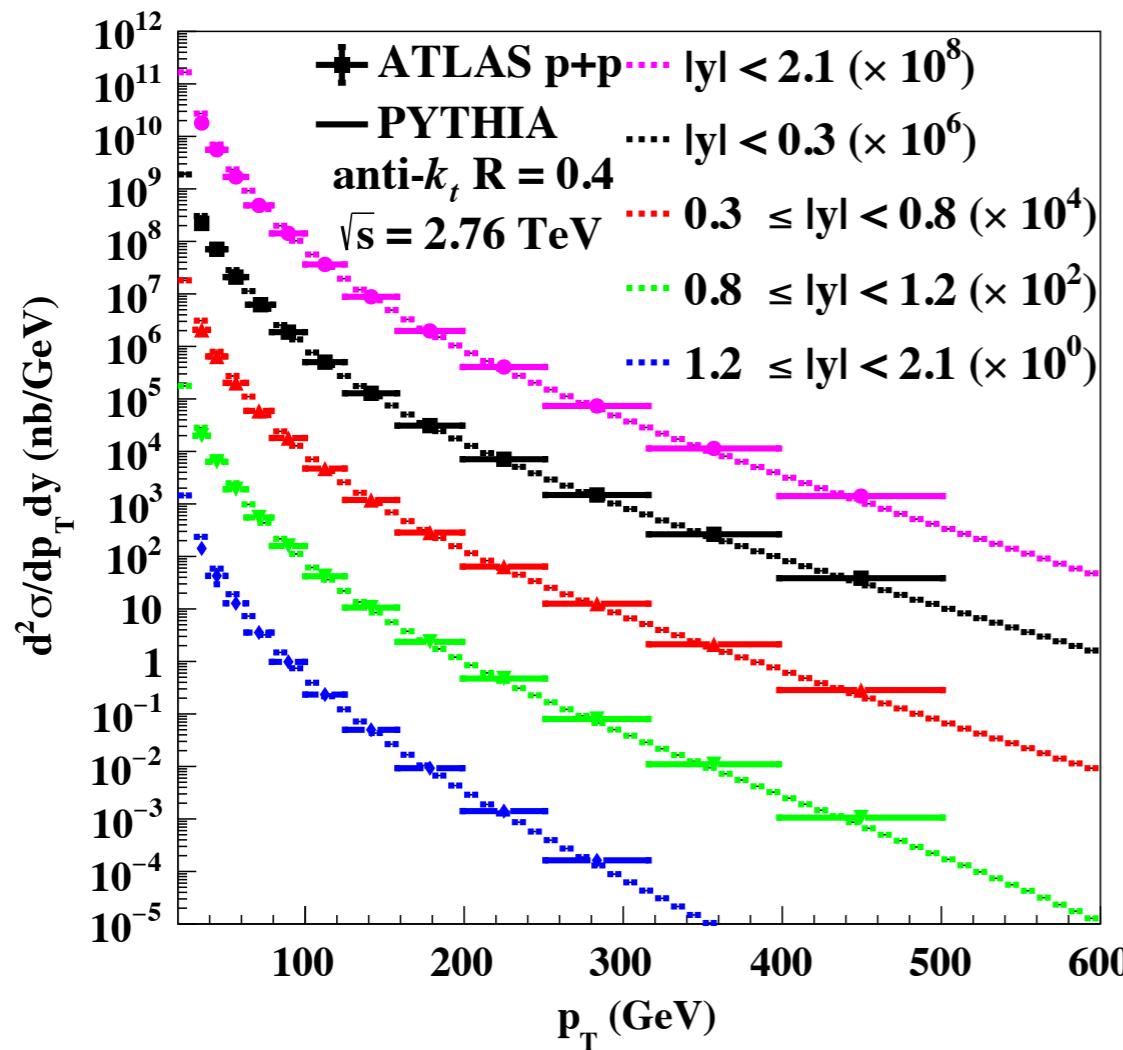
e-by-e 3+1D CLVisc: Pang, Wang & Wang, Phys. Rev. C86 (2012) 024911

Pang, Hatta, Wang & Xiao, Phys. Rev. D91 (2015) 074027



# The inclusive jet in pp collisions

$p_T$  distribution of  $pp$  collision within PYTHIA 8

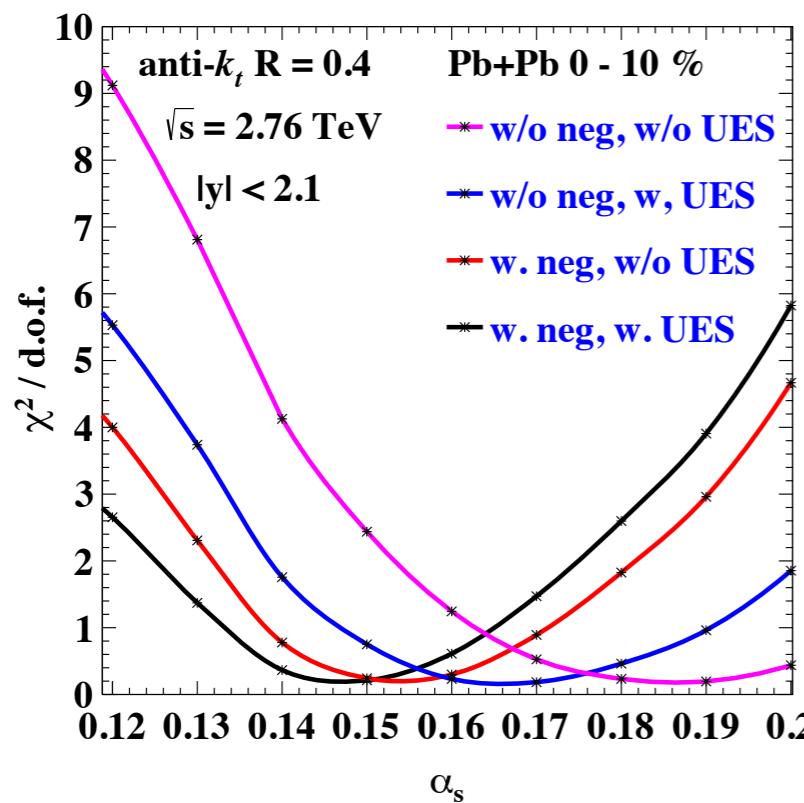


The spectrum at 5.02 TeV is higher and much flatter than at 2.76 TeV, which originates from PDFs.



# Fix strong coupling constant

Y. He et al, PRC 99 (2019) 054911

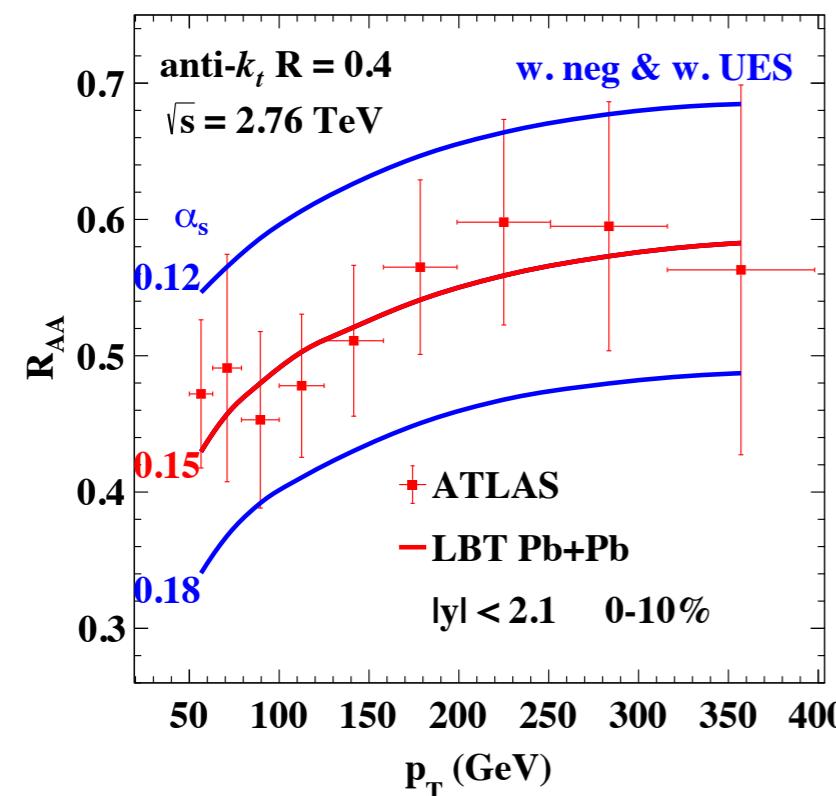


$$\chi^2 = \frac{(Theo. - Exp.)^2}{(\delta Exp.)^2}$$

neg.: “negative particles”, back reaction.

UES: underlying event subtraction.

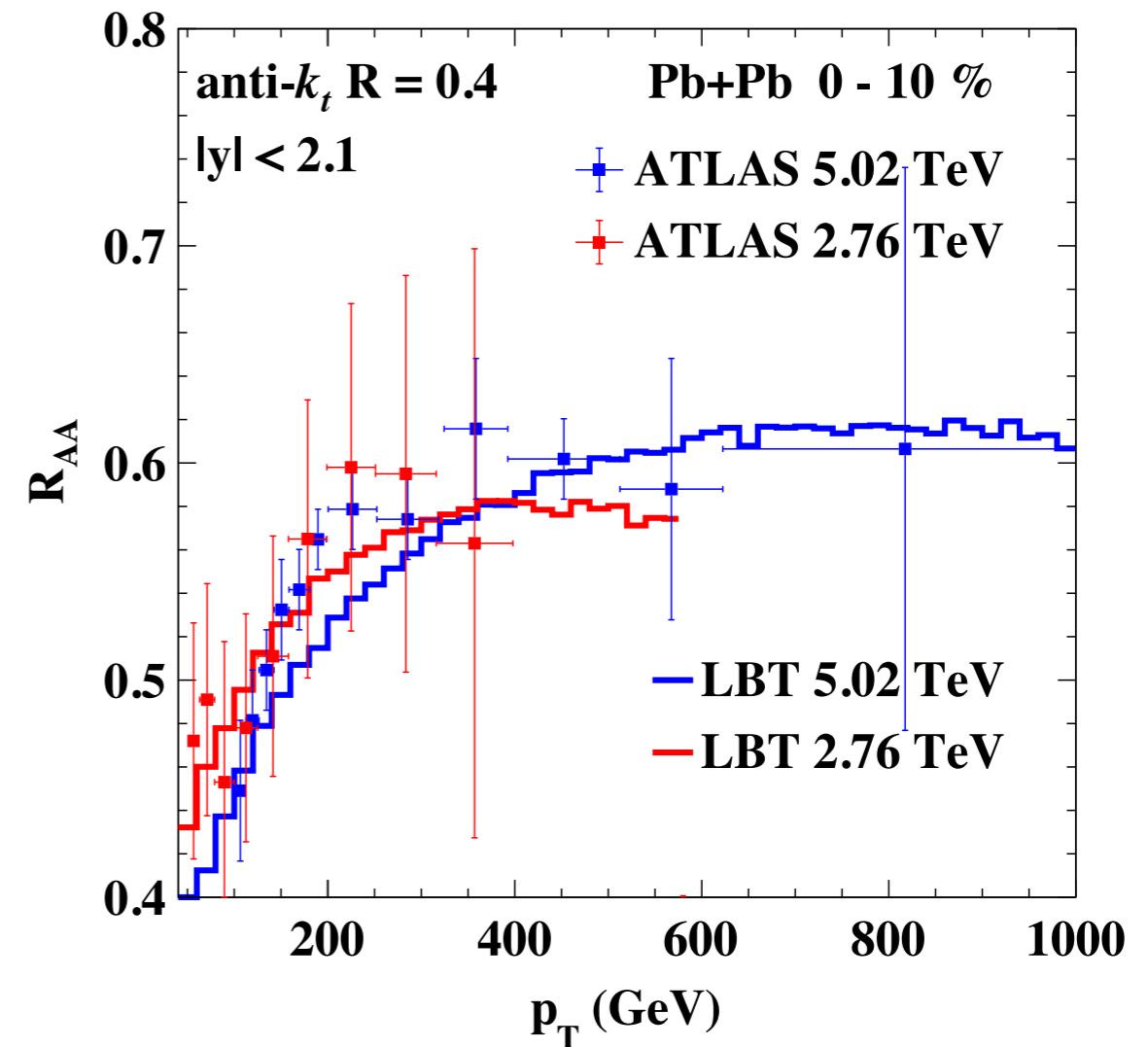
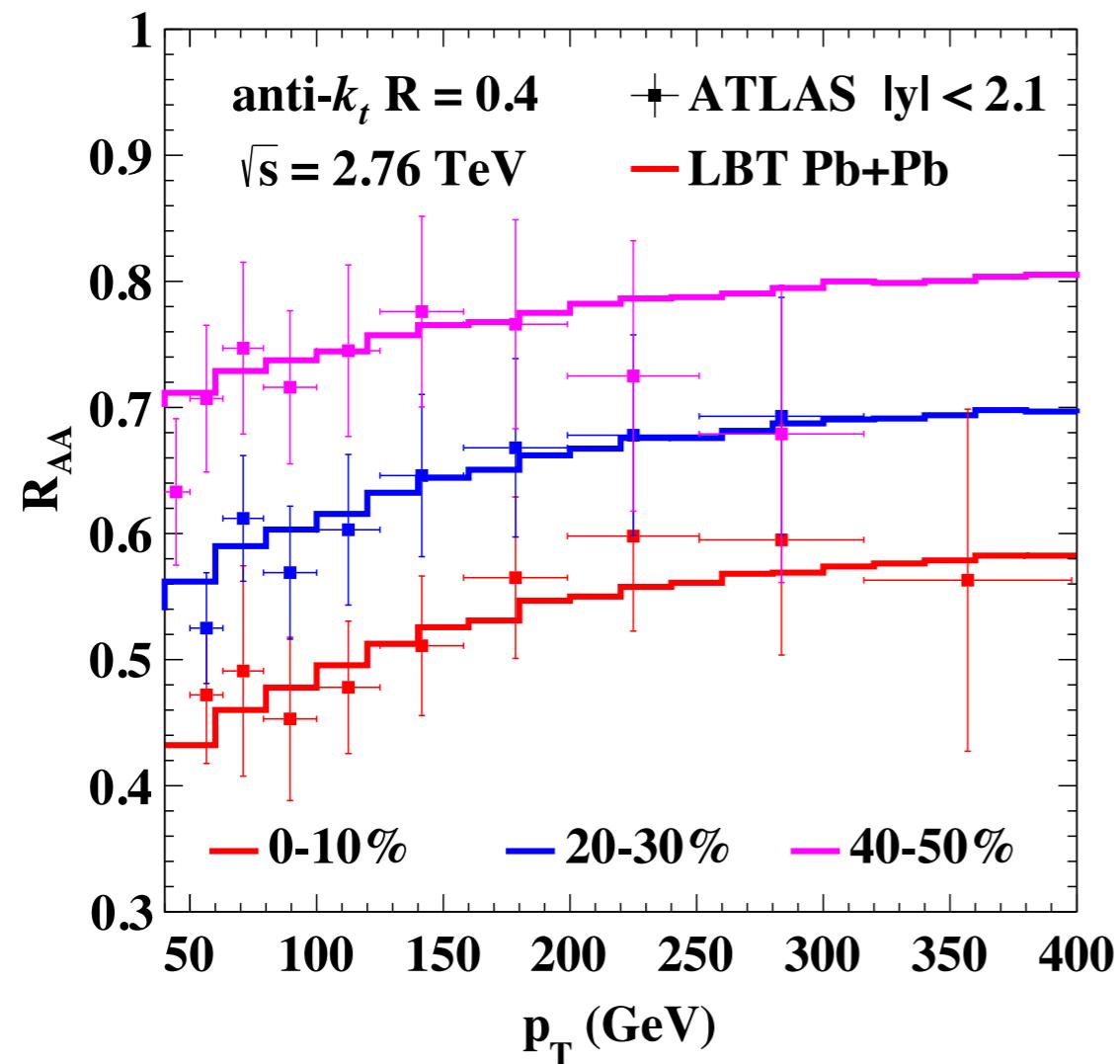
Inclusion of neg. or UES decreases jet energy



$$\Gamma_g \approx \sum_{b=g, q_i, \bar{q}_i} \Gamma_{gb \rightarrow gb} \approx 42 C_A \zeta(3) \frac{\alpha_s^2 T^3}{\pi \mu_D^2},$$

$$\alpha_s = 0.15$$

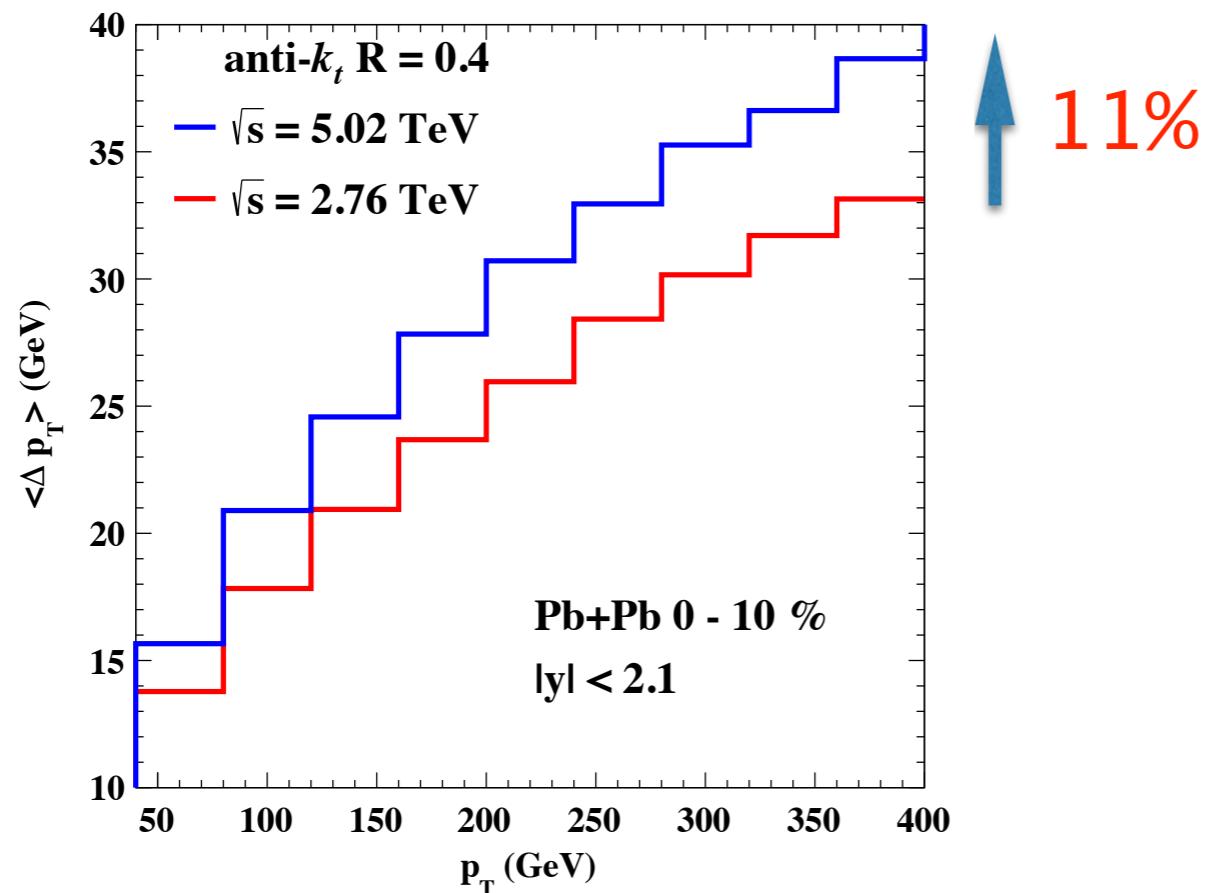
# Inclusive jet suppression



$R_{AA}$  slightly increases with jet  $p_T$  for 2.76 TeV and 5.02 TeV.



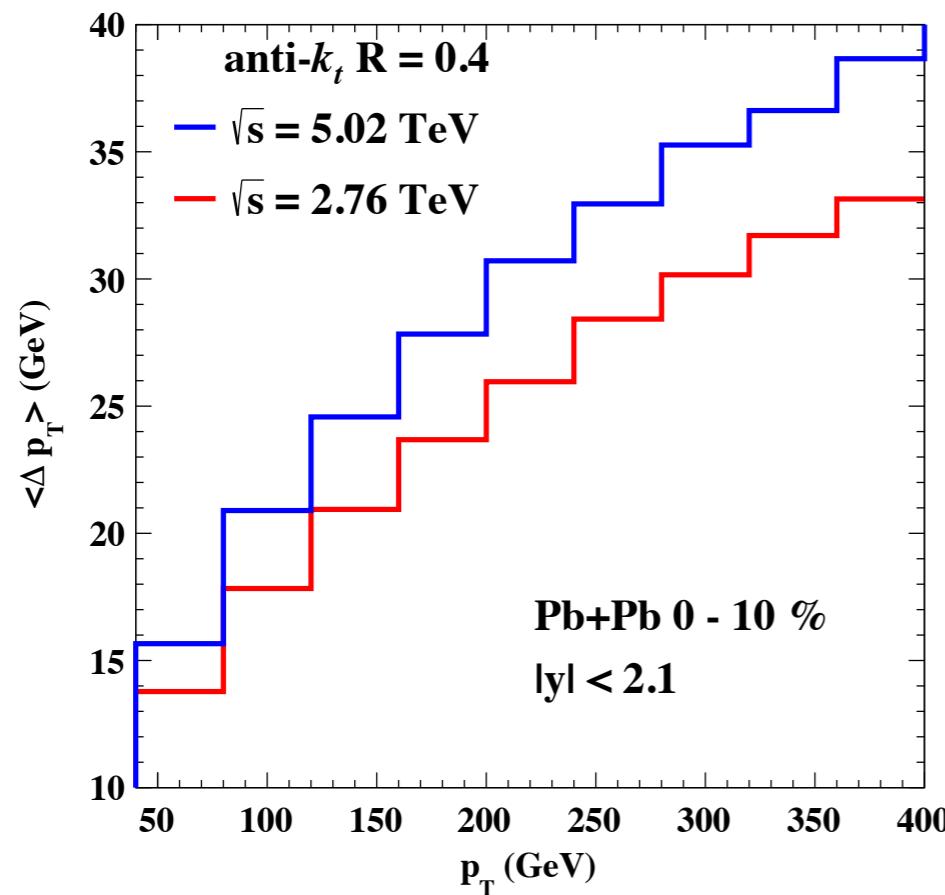
# Understanding jet $R_{AA}$



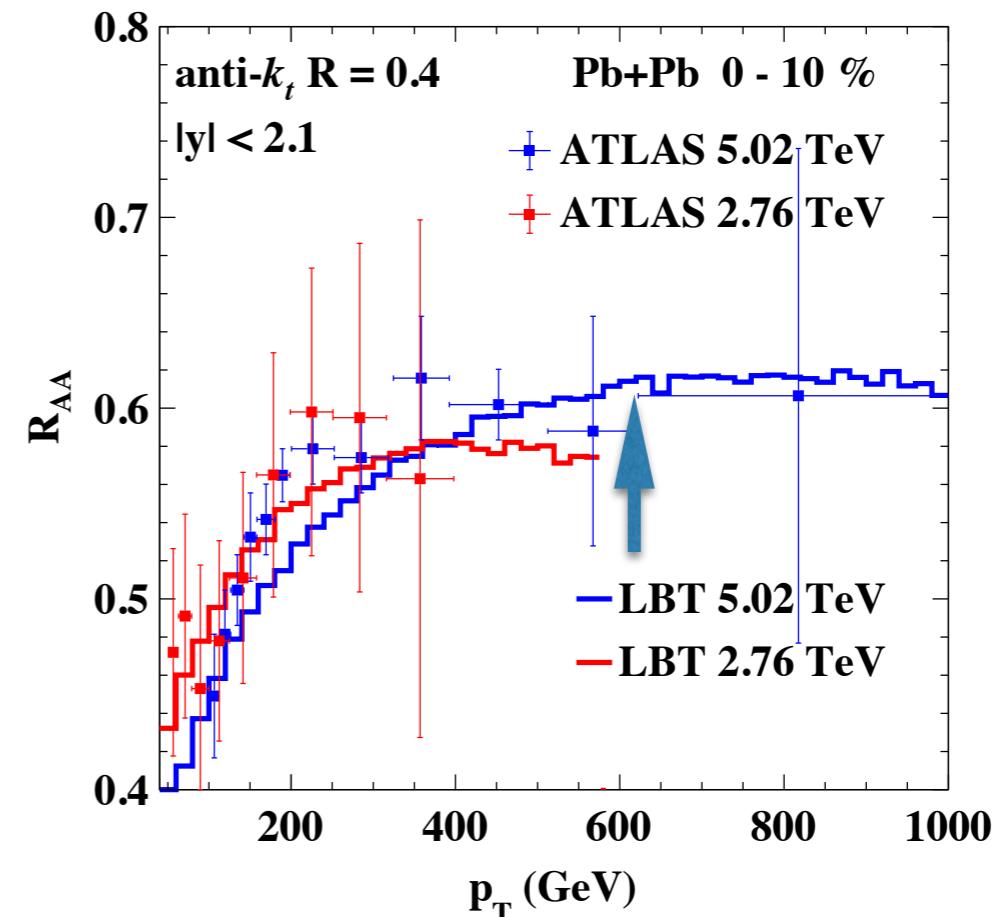
Jet energy loss at 5.02 TeV is indeed **larger** than at 2.76 TeV.



# Understanding jet $R_{AA}$



↑ 11%



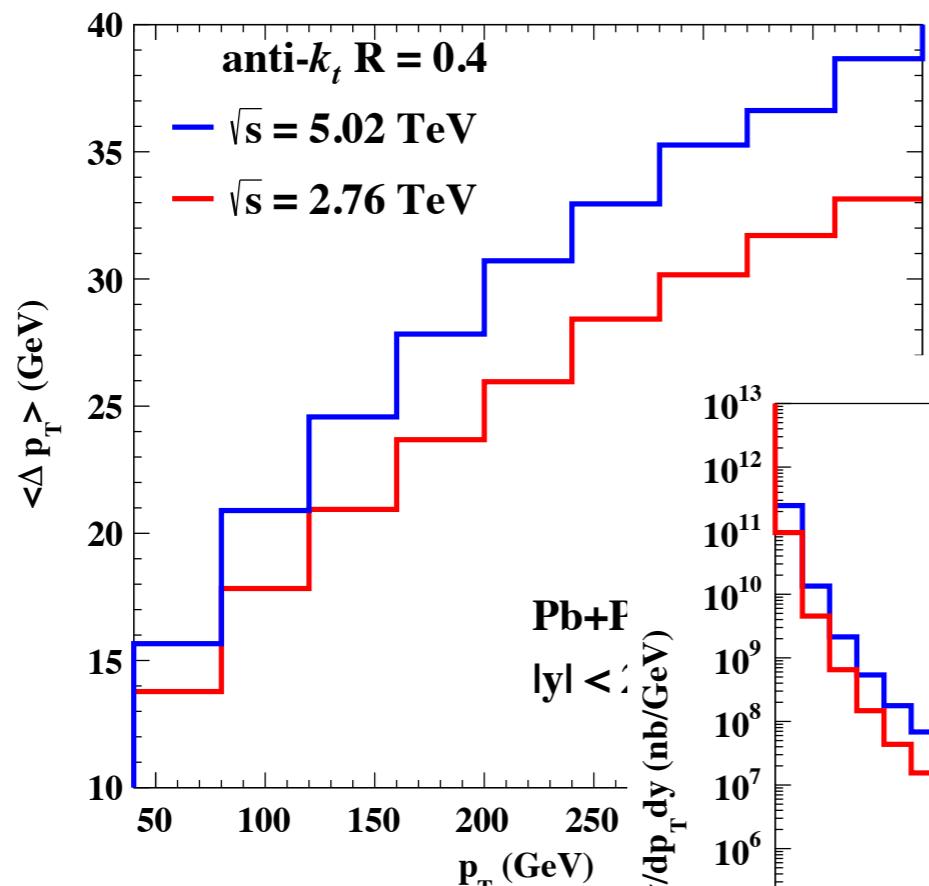
Jet energy loss at 5.02 TeV is indeed **larger** than at 2.76 TeV.

But jet R<sub>AA</sub> at 5.02 TeV is **higher** than at 2.76 TeV at large p<sub>T</sub> range

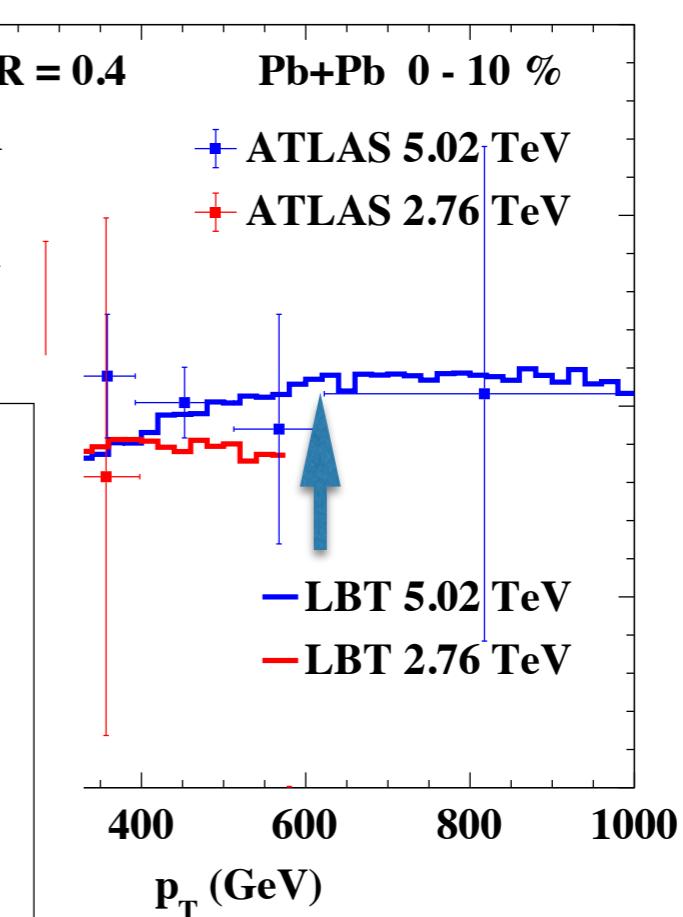
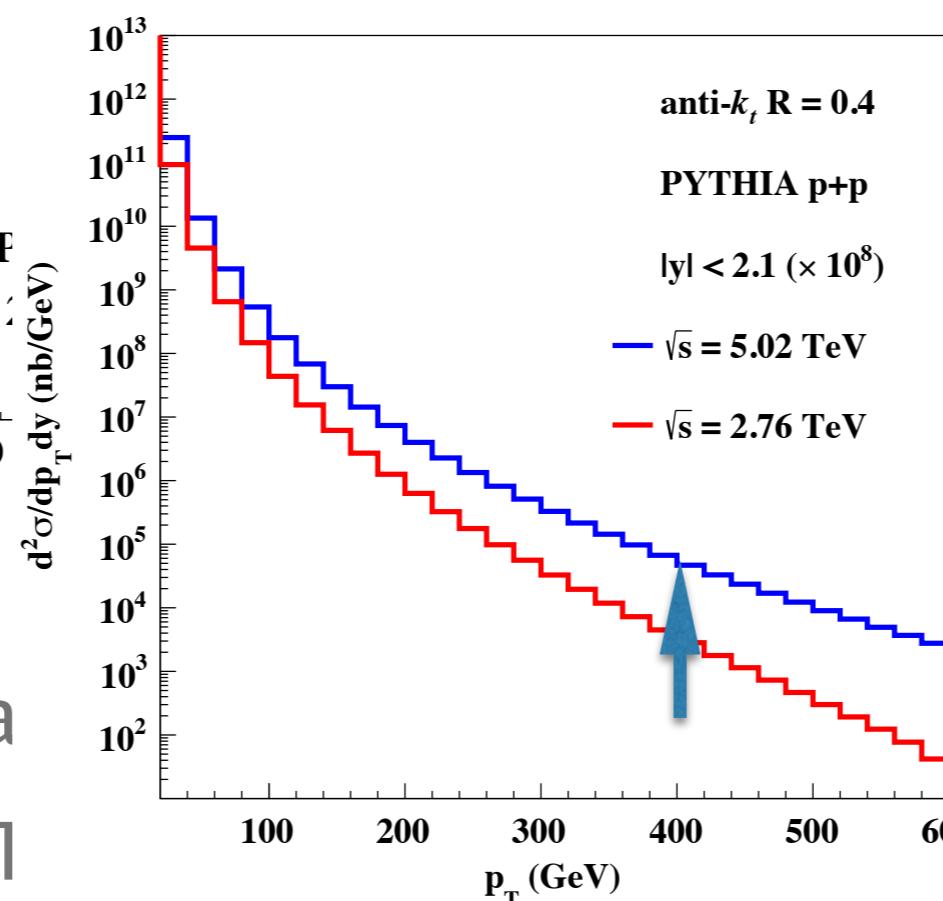
$$R_{AA} = \frac{1}{\langle N_{coll} \rangle} \frac{d\sigma_{AA}^{jet}}{d\sigma_{pp}^{jet}}$$



# Understanding jet $R_{AA}$



↑ 11%



Jet energy loss a

But Jet  $R_{AA}$  at 5.02 ↑

Because  $p_T$  spectrum at 5.02 TeV is much **flatter** than at 2.76 TeV.

r than at 2.76 TeV.

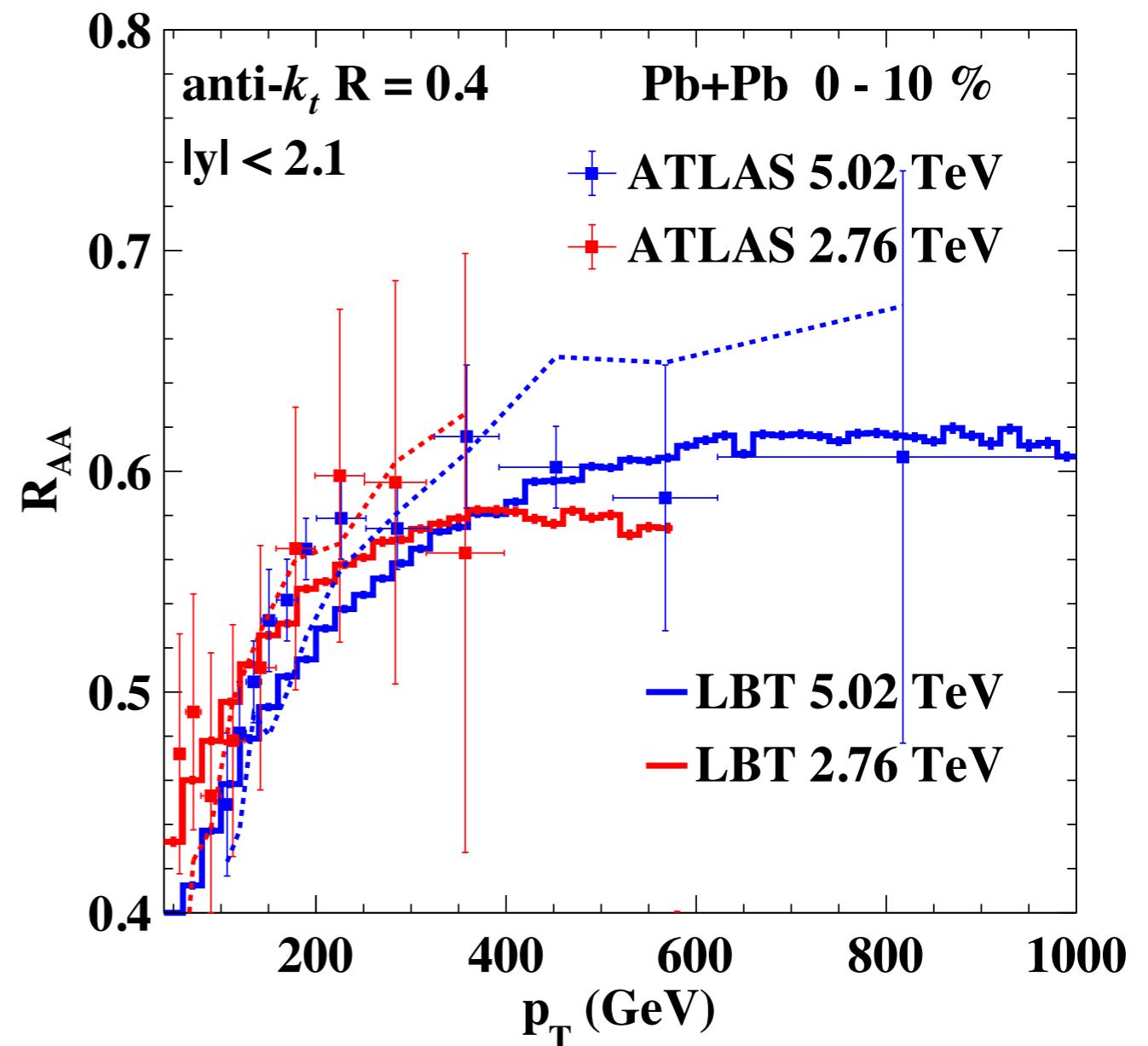
TeV. at large  $p_T$  range



# Understanding jet $R_{AA}$

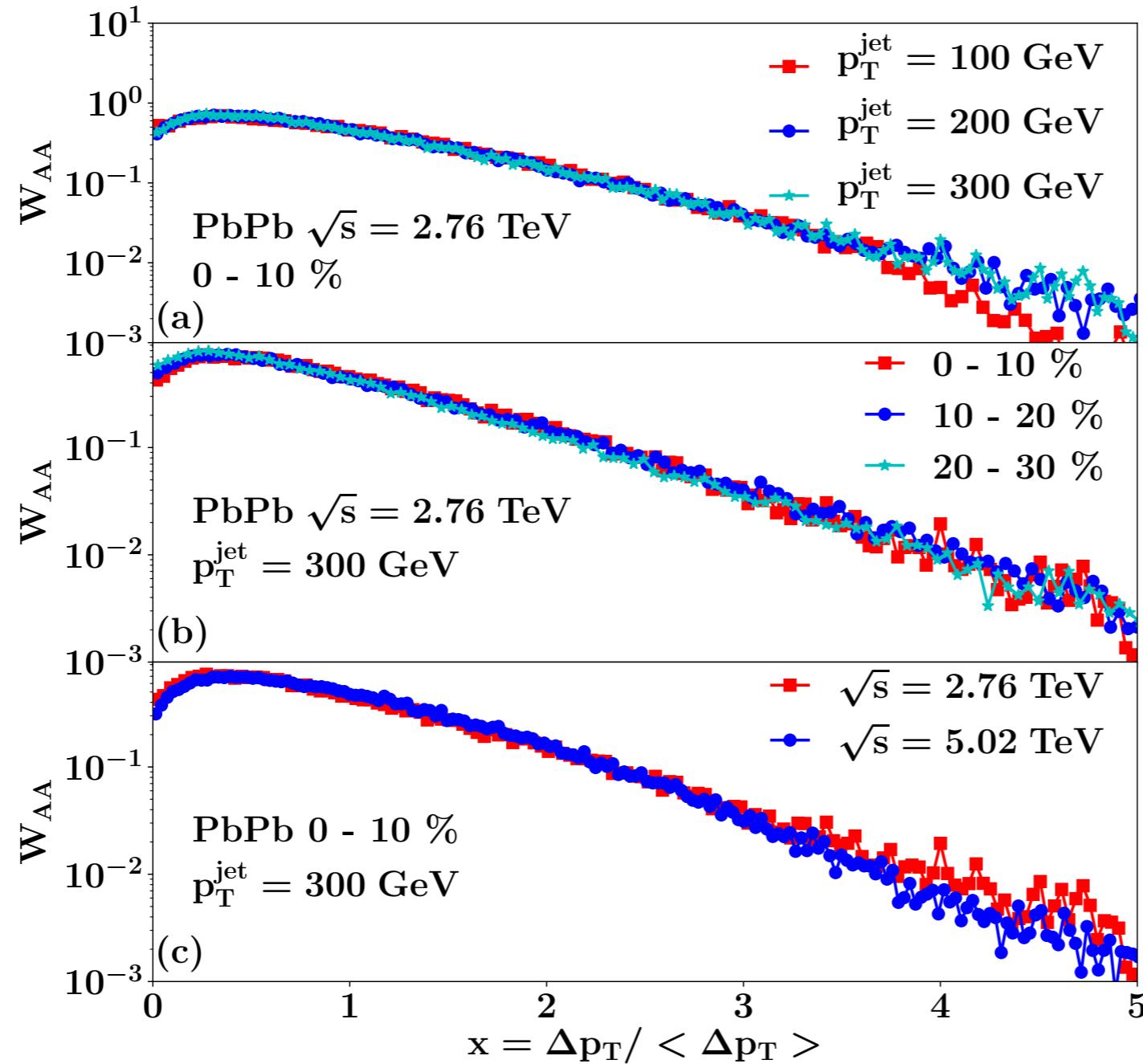
If  $\langle \Delta p_T \rangle / p_T$  is small,

$$R_{AA}(p_T) \approx \frac{d\sigma_{p+p}^{\text{jet}}(p_T + \langle \Delta p_T \rangle)}{d\sigma_{p+p}^{\text{jet}}(p_T)}$$



# Jet energy loss distribution

$$\frac{d\sigma_{jet}^{AA}}{dp_T dy}(p_T, R) = \int d\Delta p_T W_{AA}(\Delta p_T, p_T + \Delta p_T, R) \frac{d\sigma_{jet}^{pp}}{dp_T dy}(p_T + \Delta p_T, R)$$



$$x = \frac{\Delta p_T}{\langle \Delta p_T \rangle}$$

Scaling behavior at a given centrality class:

$$\langle \Delta p_T \rangle = \langle \Delta p_T \rangle(p_T, \sqrt{s})$$

leading jet energy loss distribution



# Bayesian extraction from experimental data

$$\frac{d\sigma_{jet}^{AA}}{dp_T dy}(p_T, R) = \int d\Delta p_T W_{AA}(\Delta p_T, p_T + \Delta p_T, R) \frac{d\sigma_{jet}^{pp}}{dp_T dy}(p_T + \Delta p_T, R)$$

Y. He, L-G Pang, X-N Wang, PRL 122 (2019) 252302

LBT model:

$$\left. \begin{array}{l} \sigma_{jet}^{pp}(p_T) \\ W_{AA}(p_T, \Delta p_T) \end{array} \right\} \Rightarrow \sigma_{jet}^{AA}(p_T)$$

Bayesian analysis:

$$\left. \begin{array}{l} \sigma_{jet}^{pp}(p_T) \\ \sigma_{jet}^{AA}(p_T) \end{array} \right\} \Rightarrow W_{AA}(p_T, \Delta p_T)$$

Data-driven,  
model independent

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$

$Y$  : data

$X$  :  $W_{AA}$

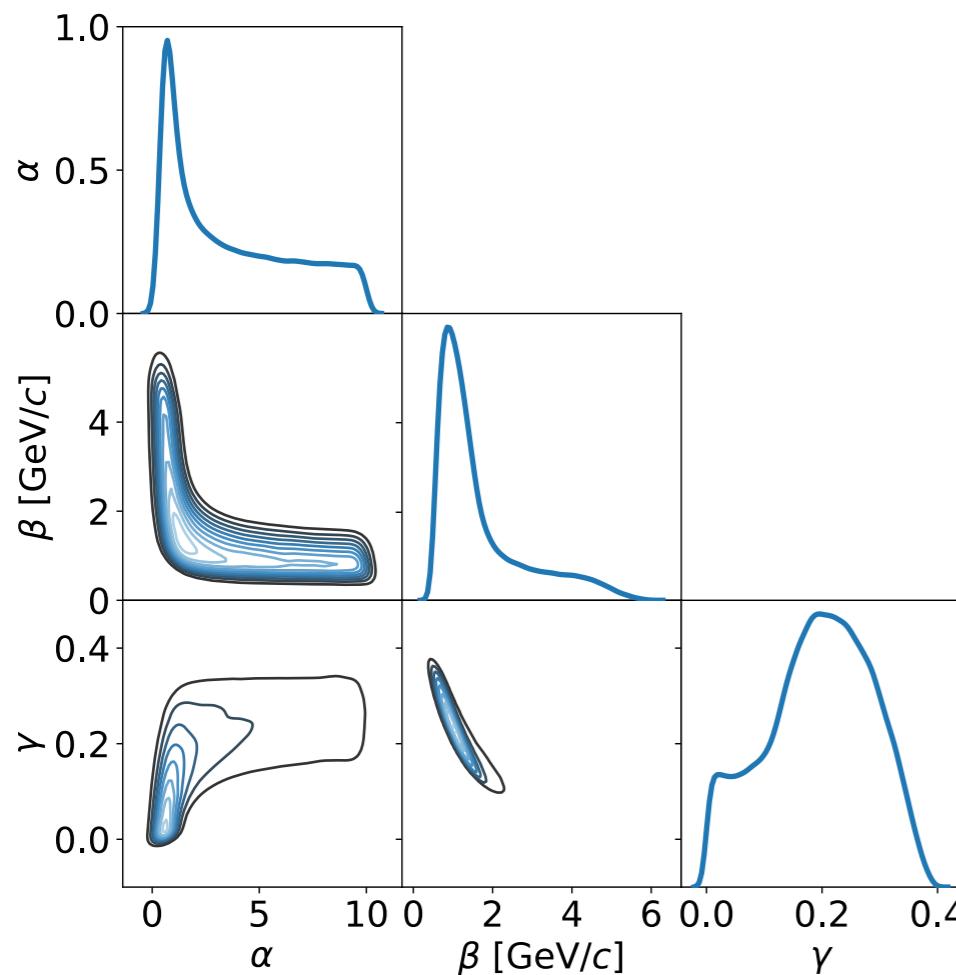


# Bayesian extraction from experimental data

Bayesian analysis:  
Markov Chain Monte Carlo

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$

8,000,000 samplings



$$\left. \begin{array}{l} \sigma_{jet}^{pp}(p_T) \\ \sigma_{jet}^{AA}(p_T) \end{array} \right\} \Rightarrow W_{AA}(p_T, \Delta p_T)$$

$$x = \frac{\Delta p_T}{\langle \Delta p_T \rangle}$$

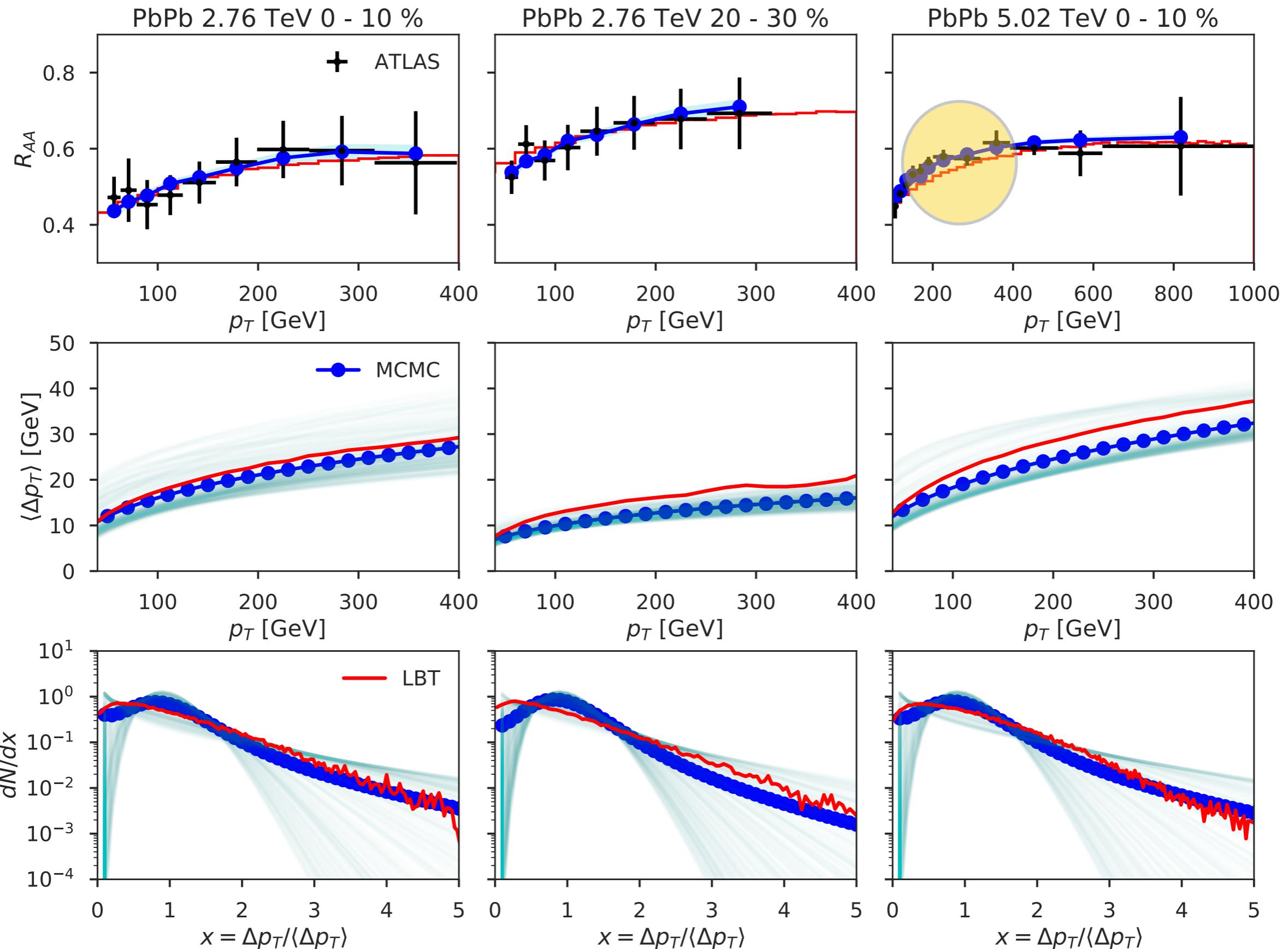
$$\begin{aligned} W_{AA}(x) &= \frac{\alpha^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\alpha x} \\ &\equiv \int \prod_{i=1}^a dx_i e^{-\sum_i^a x_i} \delta(x - \sum_{i=1}^a x_i) \end{aligned}$$

$$\langle \Delta p_T \rangle = \beta p_T^\gamma \log(p_T)$$

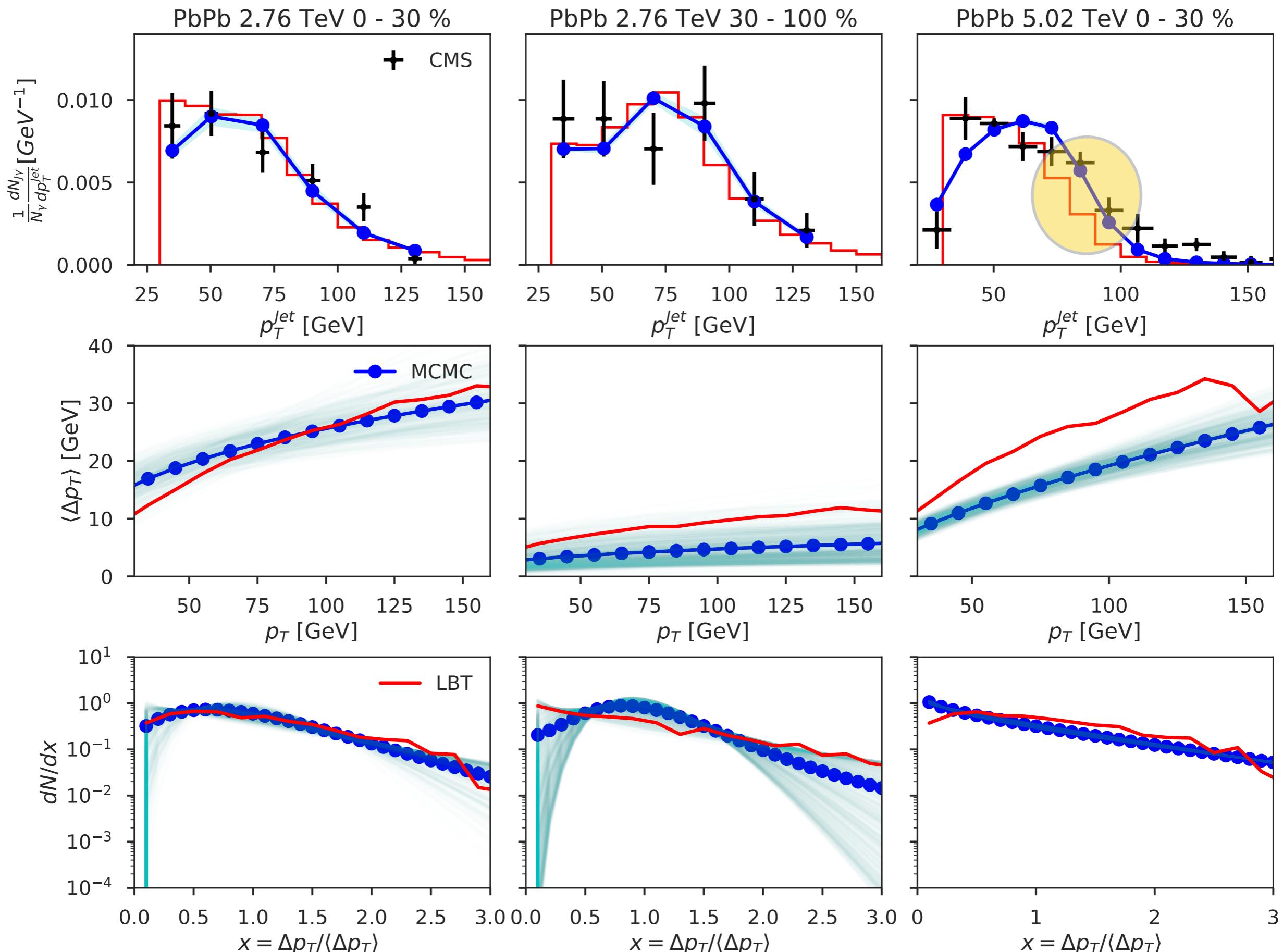
$\alpha$  : number of  
out-of-cone scatterings



# Bayesian extraction from experimental data



# Bayesian extraction from experimental data



# Bayesian extraction from experimental data

single inclusive jet in Pb+Pb			
	(0-10%)2.76 TeV	(20-30%)2.76 TeV	(0-10%)5.02 TeV
$\alpha$	$3.87 \pm 2.93$ $(1.45 \pm 0.01)$	$4.47 \pm 2.83$ $(1.33 \pm 0.02)$	$4.41 \pm 2.86$ $(1.58 \pm 0.02)$
$\beta$	$1.40 \pm 1.12$ $(1.39 \pm 0.06)$	$1.12 \pm 0.47$ $(1.08 \pm 0.07)$	$1.06 \pm 0.97$ $(1.56 \pm 0.06)$
$\gamma$	$0.21 \pm 0.09$ $(0.21 \pm 0.01)$	$0.15 \pm 0.07$ $(0.20 \pm 0.01)$	$0.26 \pm 0.06$ $(0.23 \pm 0.01)$
$\gamma$ -triggered jet in Pb+Pb			
	(0-30%)2.76 TeV	(30-100%)2.76 TeV	(0-30%)5.02 TeV
$\alpha$	$2.13 \pm 1.28$ $(1.95 \pm 0.12)$	$3.75 \pm 2.81$ $(1.04 \pm 0.06)$	$0.90 \pm 0.09$ $(1.84 \pm 0.13)$
$\beta$	$2.68 \pm 1.40$ $(0.72 \pm 0.06)$	$0.55 \pm 0.44$ $(0.53 \pm 0.04)$	$1.50 \pm 0.85$ $(0.50 \pm 0.04)$
$\gamma$	$0.16 \pm 0.14$ $(0.44 \pm 0.02)$	$0.13 \pm 0.18$ $(0.30 \pm 0.02)$	$0.21 \pm 0.12$ $(0.56 \pm 0.02)$

TABLE I. Parameters  $[\alpha, \beta, \gamma]$  of the jet energy loss distribution from Bayesian fits to single inclusive and  $\gamma$ -triggered jet spectra in Pb+Pb collisions at  $\sqrt{s} = 2.76$  and 5.02 TeV. Numbers in parentheses are from fits to LBT results.



# Summary

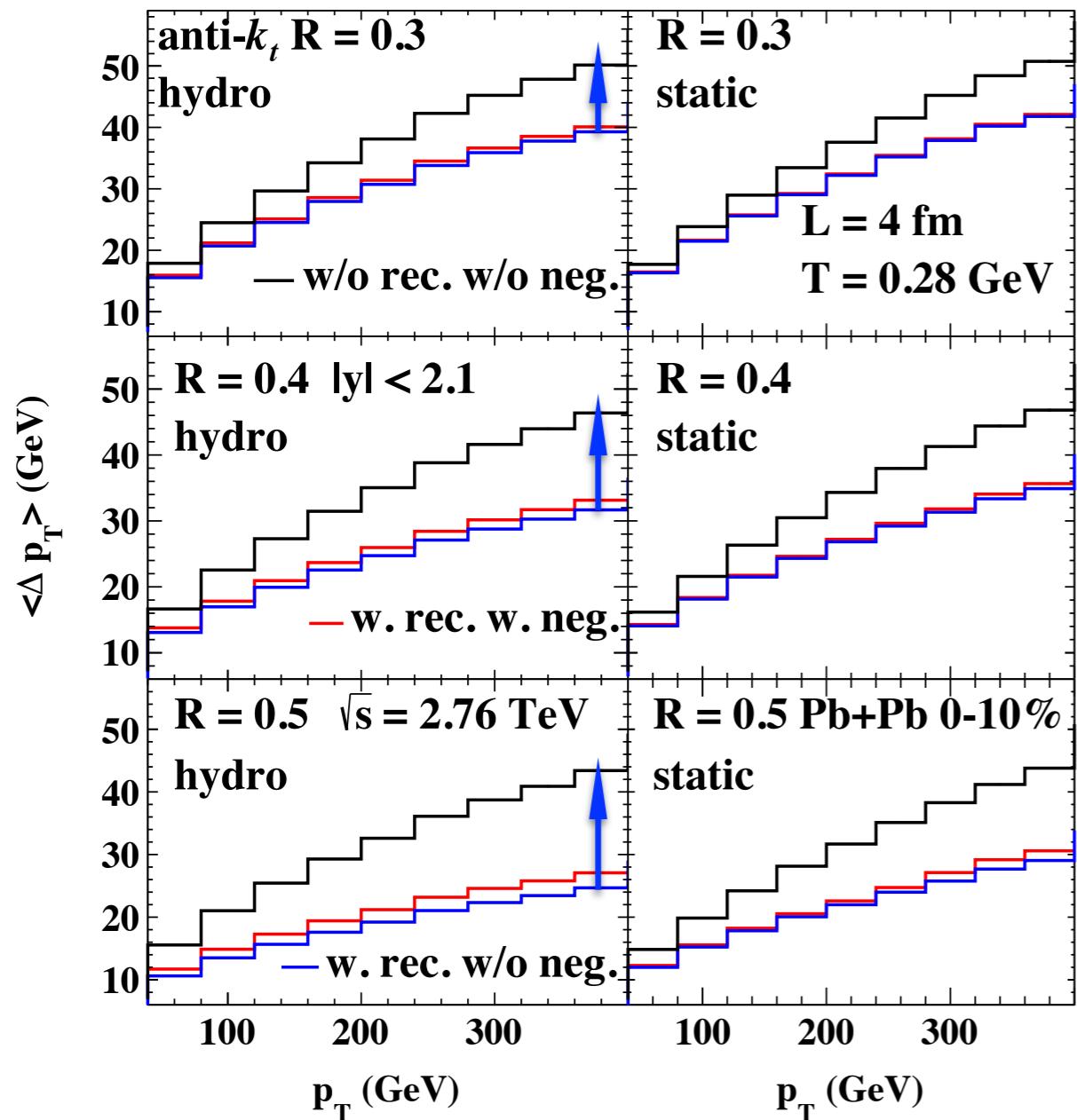
- The inclusive jet suppression is determined by the initial  $p\bar{p}$  spectrum and jet energy loss distribution.
- Jet energy loss distribution has a scaling behavior
- Bayesian analysis can extract jet energy loss distribution and averaged jet energy loss directly from experimental data.
- Jet energy loss is mainly caused by a few out-of cone scatterings in the hot and dense medium.



*Thanks!*



# Effects of medium response and radial expansion



medium recoil effect up to 15%

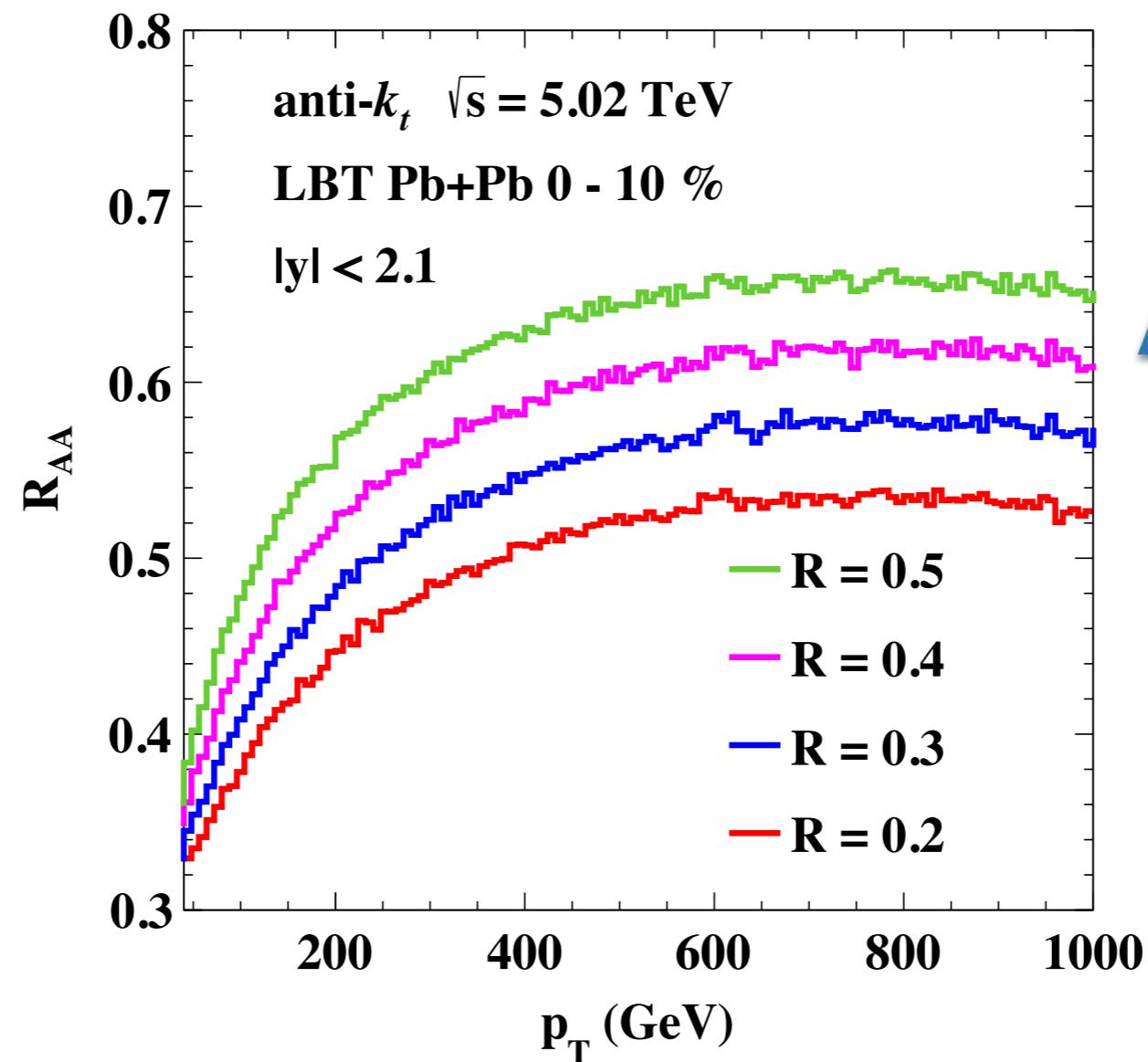
back reaction not negligible

larger cone size and radial expansion  
enlarges the effects above.

2.76 TeV



# Cone size dependence of $R_{AA}$

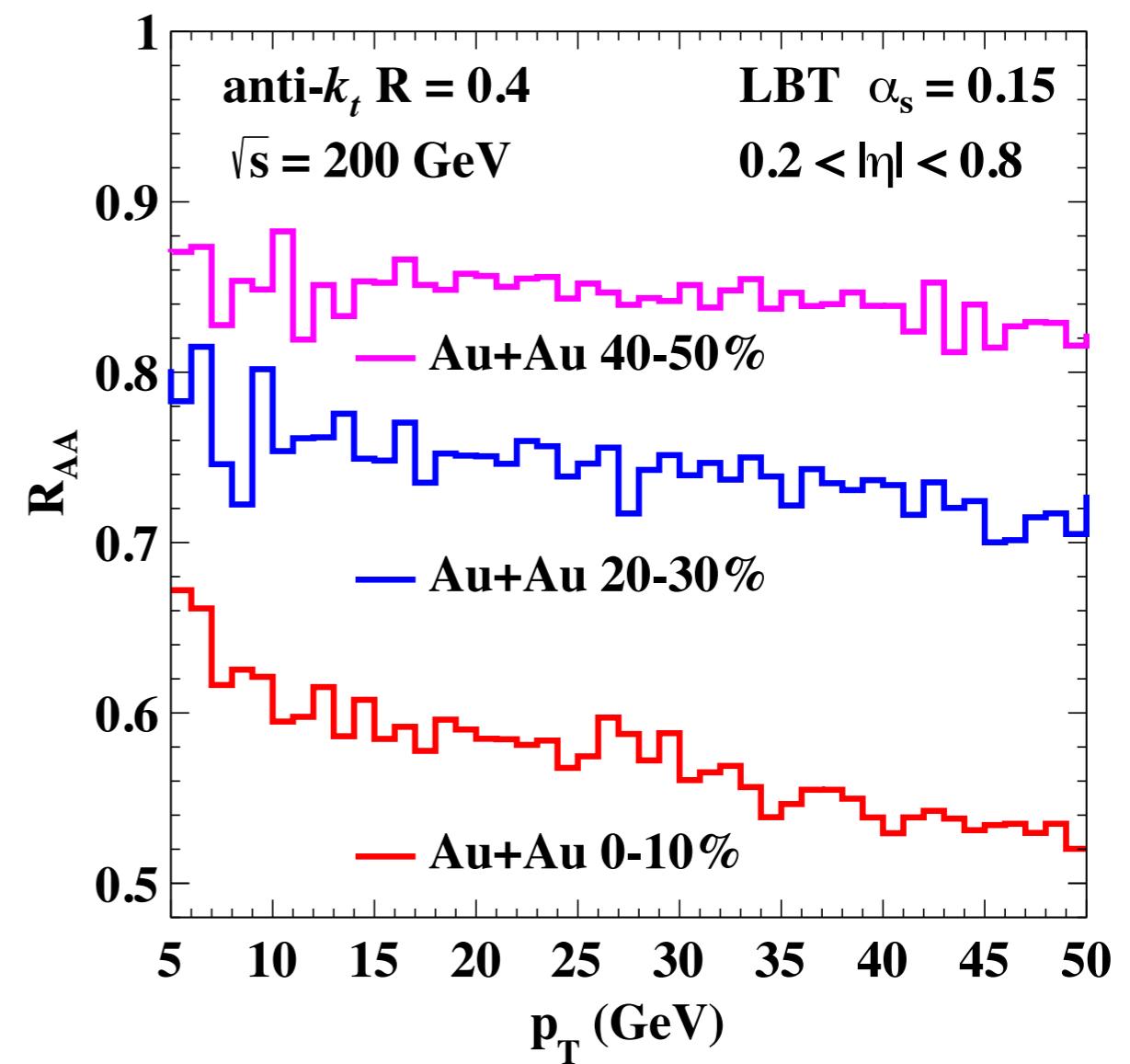
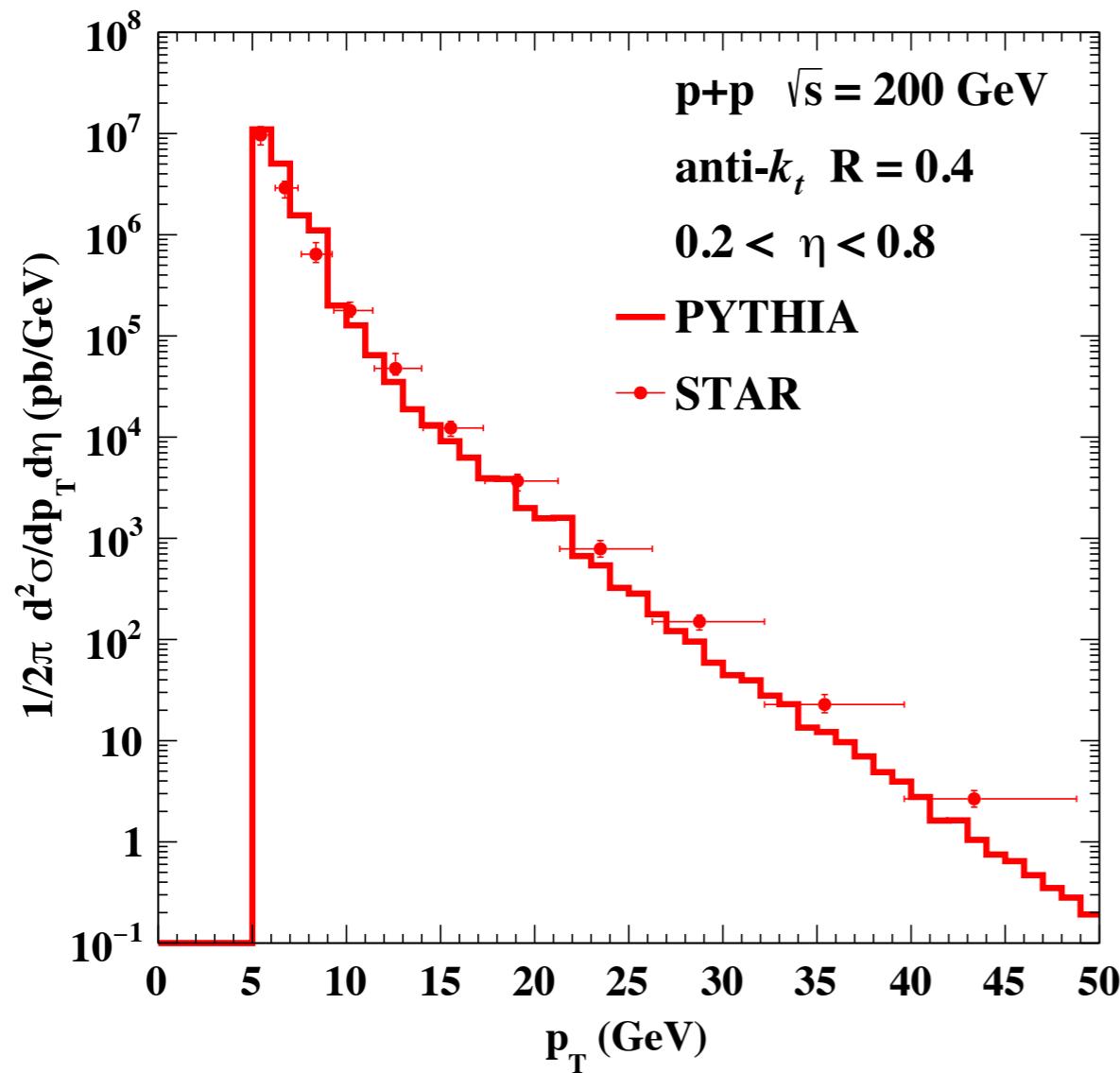


larger R: flatter initial spectrum + smaller energy loss  
-> less suppression

quantitatively relates to medium response



# $R_{AA}$ at RHIC energy

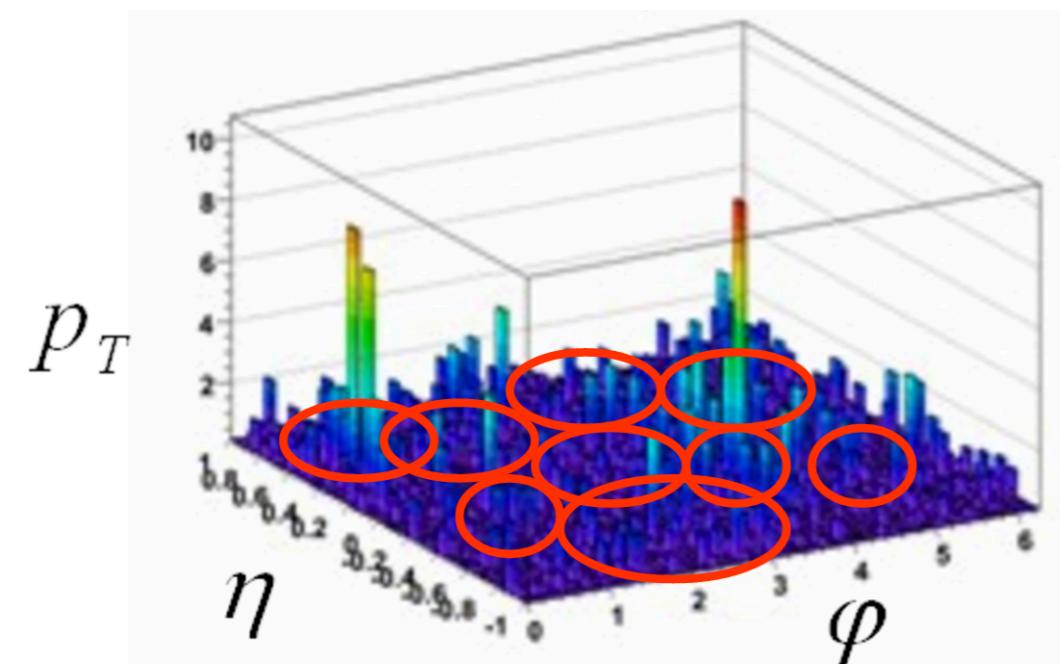


Slightly **decreases** with jet energy because of **steeper** initial spectrum, although the energy loss is **smaller** than at LHC energy.



# Underlying Event Subtraction (UES)

UE: collisions of beam remnant, fluctuation of the background, non-perturbative effects. Subtraction is needed to exclude the soft particles.



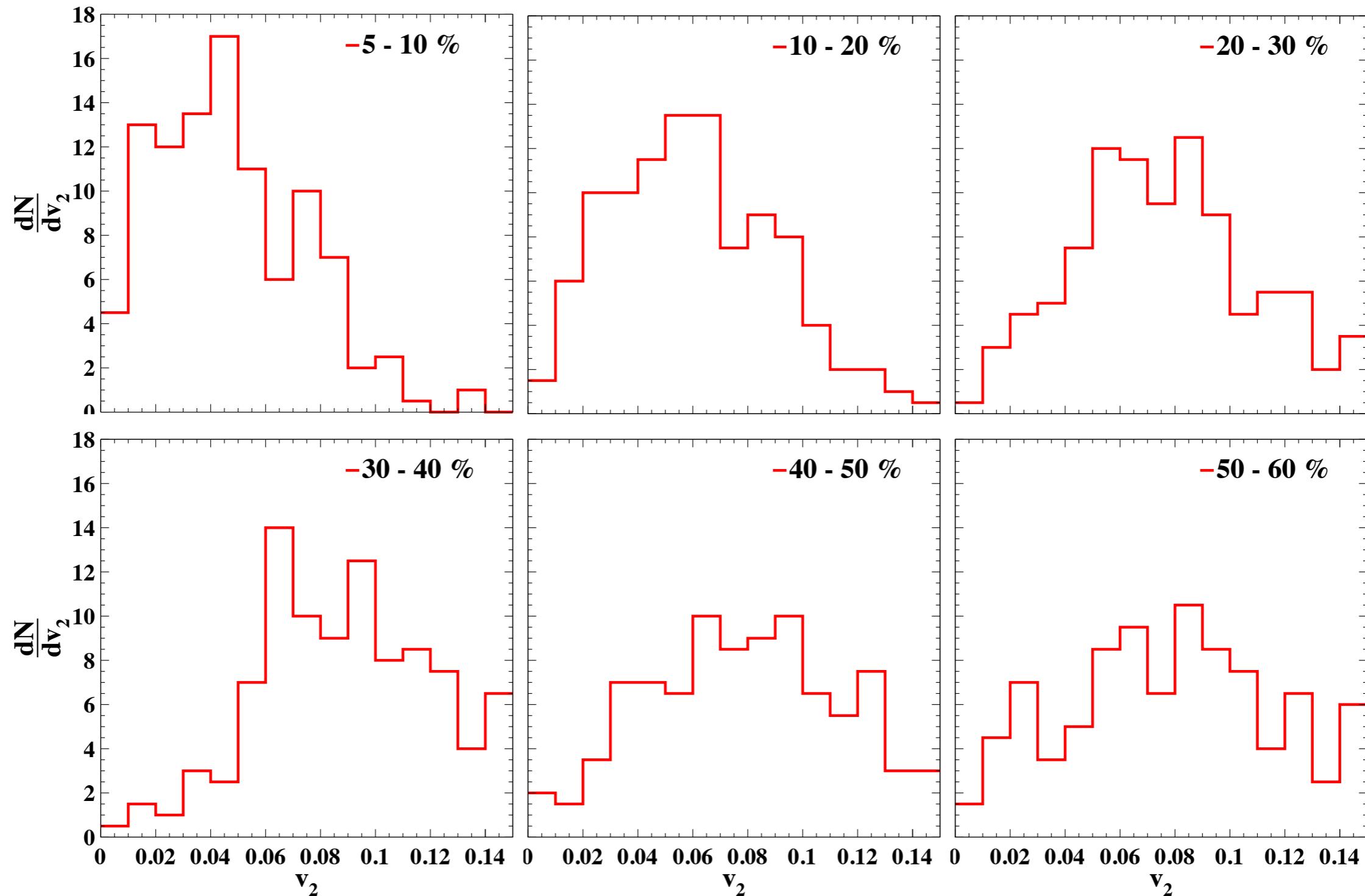
Seed jet:  $E_T > 3 \text{ GeV}$  for at least one parton, and  $E_T^{\max} / E_T^{\text{ave}} > 4$

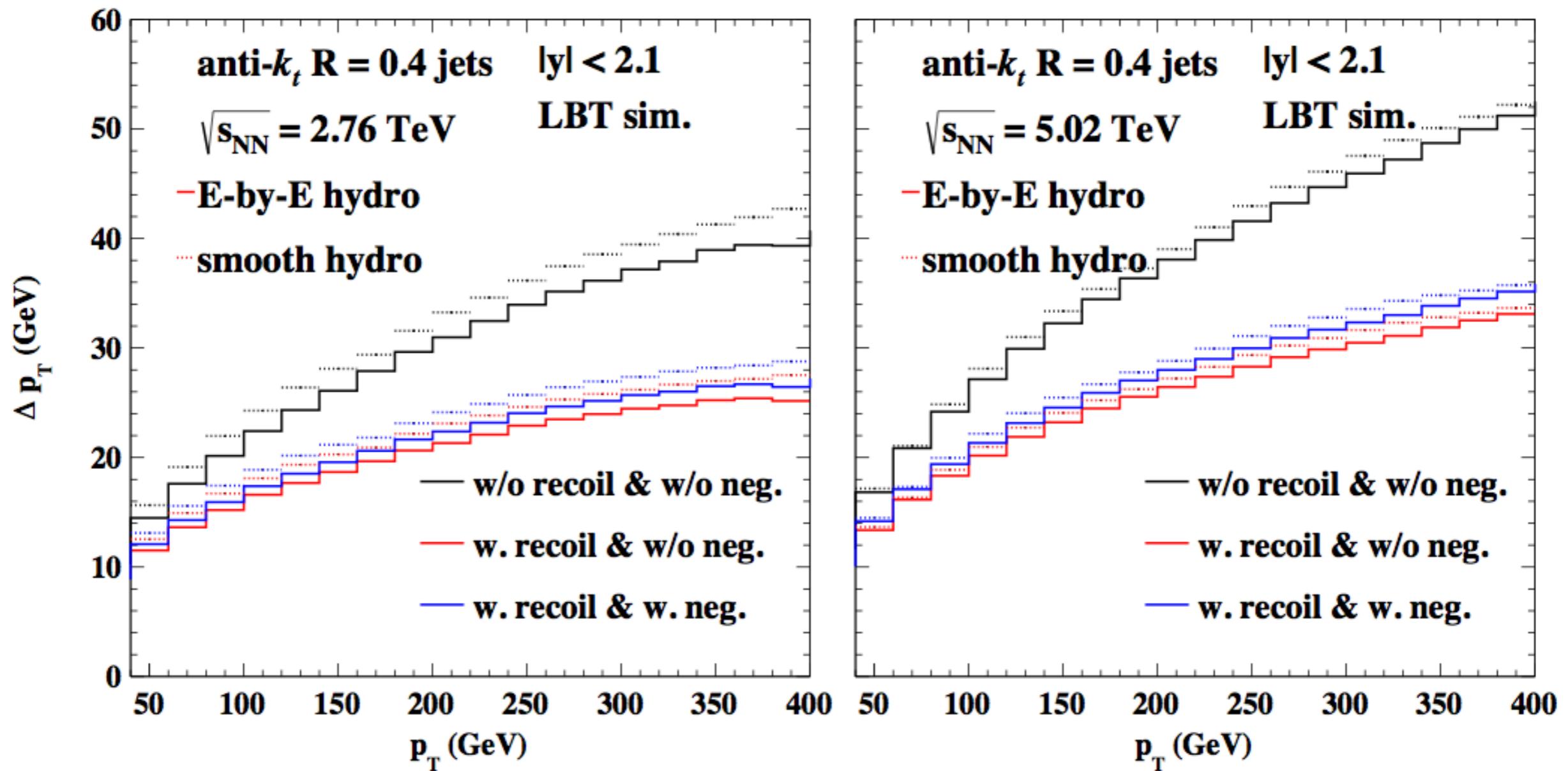
ATLAS Collaboration, Phys. Lett. B 719, 220 (2013).

$$E_T^{UES} = E_T^{\text{seedjet}} - A^{\text{seedjet}} \rho (1 + 2v_2 \cos[2(\phi_{\text{jet}} - \Psi_2)])$$

We only subtract the energy of seed jets,  
and count all the final jets!

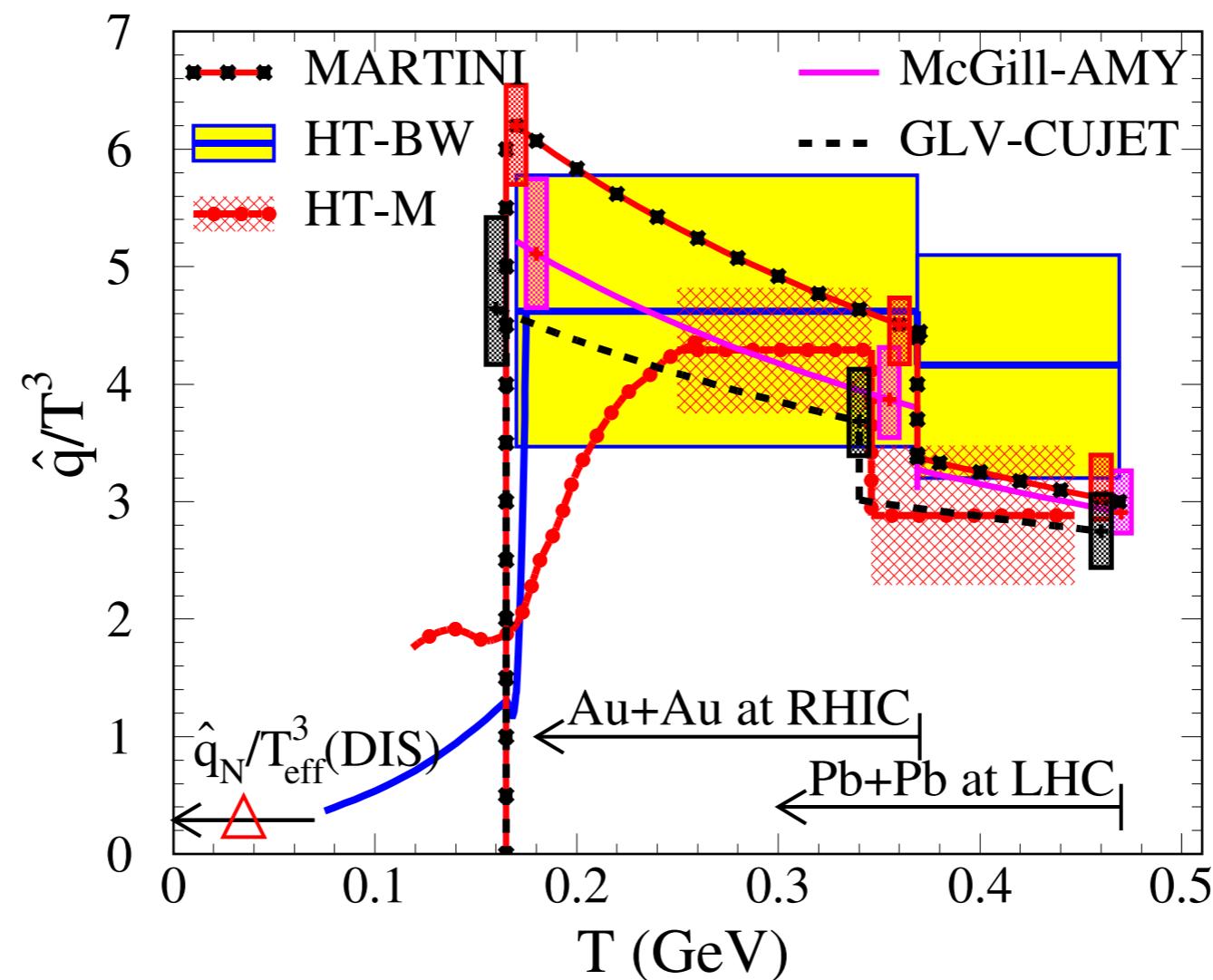
# $v_2$ of soft particles from hydro profiles





# jet-medium transport coefficient

$$\hat{q} = \frac{\langle \Delta p_T^2 \rangle}{\lambda}$$



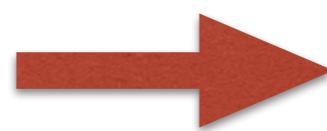
# Azimuthal Anisotropy $v_2$

$$\frac{dN}{d\phi} = C(1 + 2\sum_n v_n \cos[n(\phi - \Psi_n)])$$

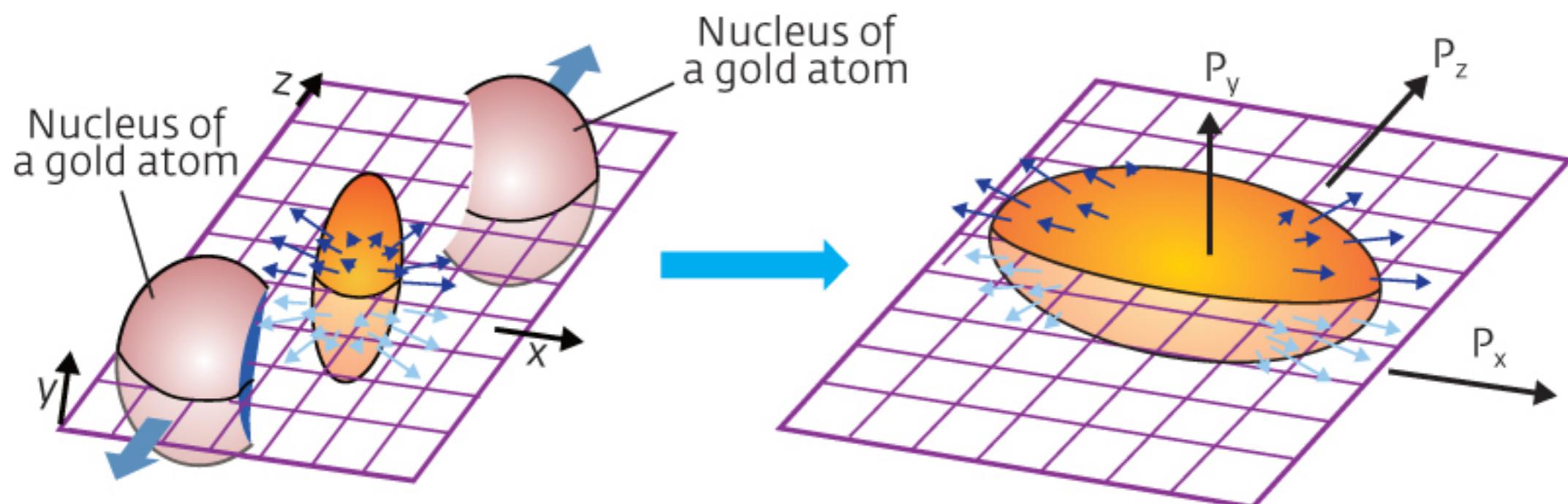
elliptic flow:  $n=2$

$$v_2 = \langle \cos[2(\phi - \Psi_2)] \rangle$$

Coordinate space:  
initial asymmetry



Momentum space:  
final asymmetry

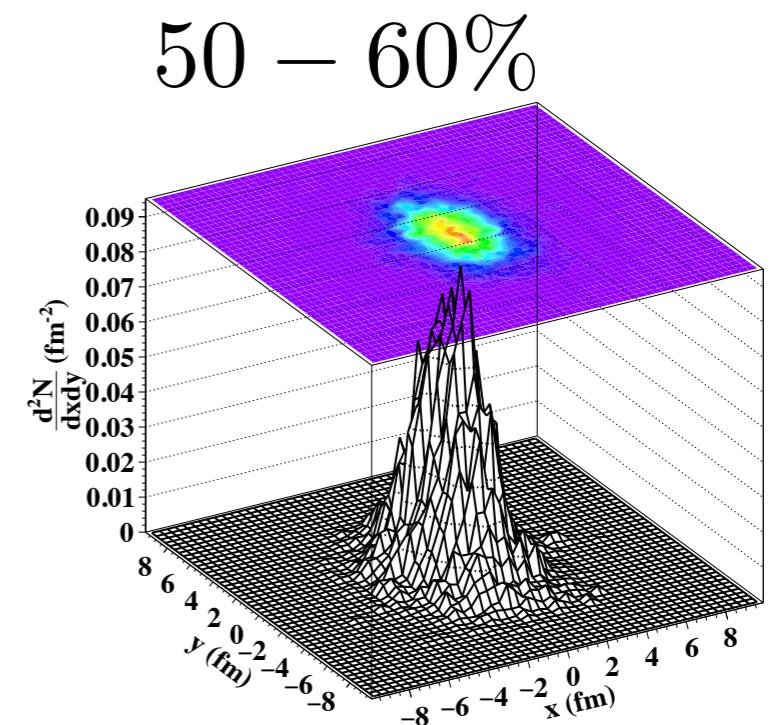
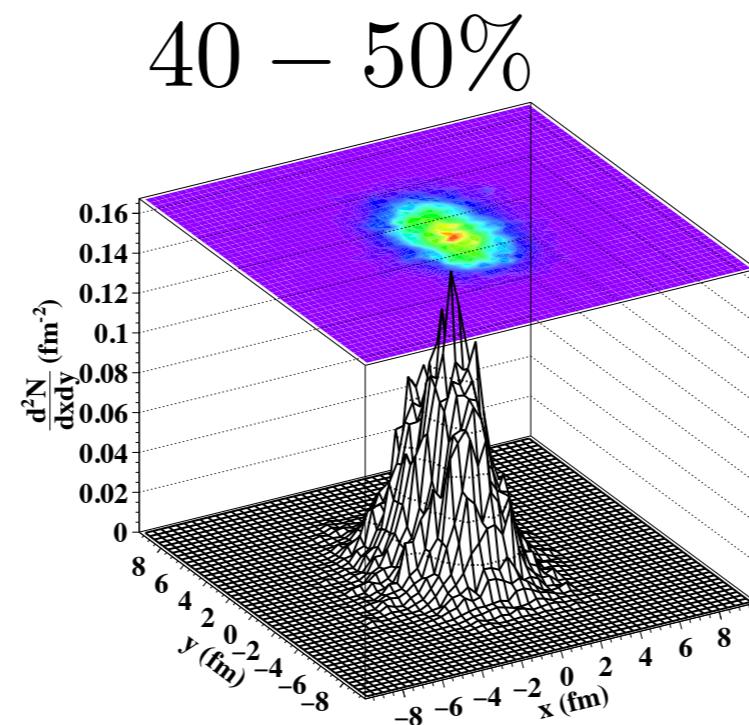
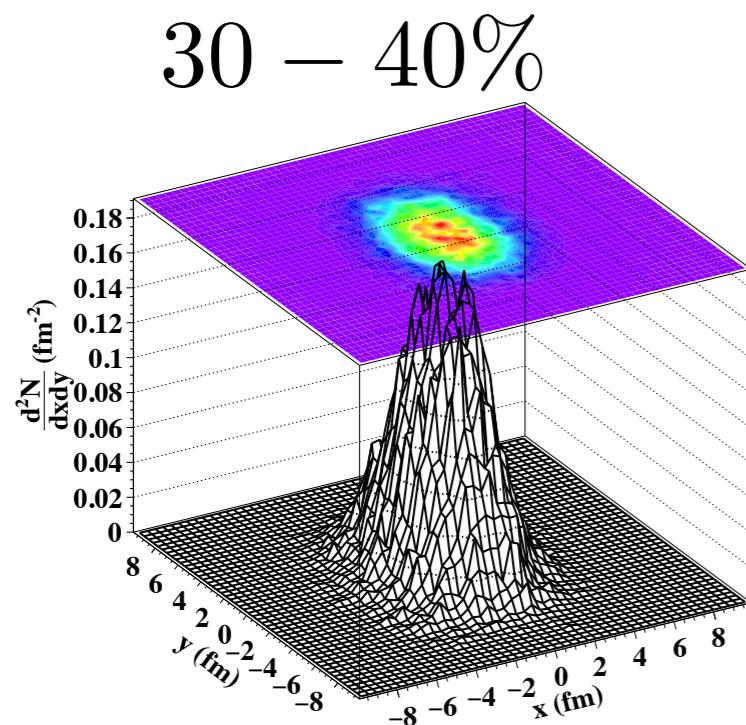
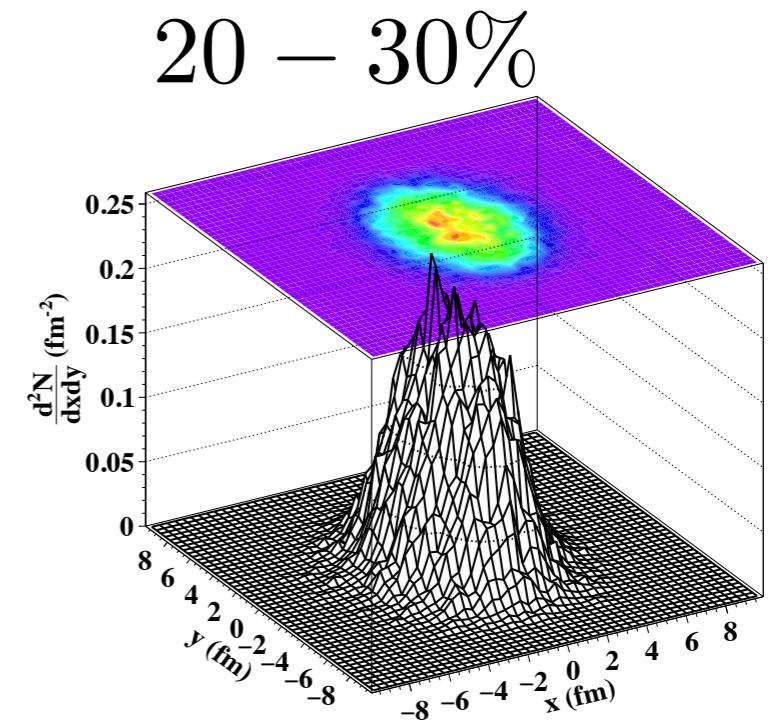
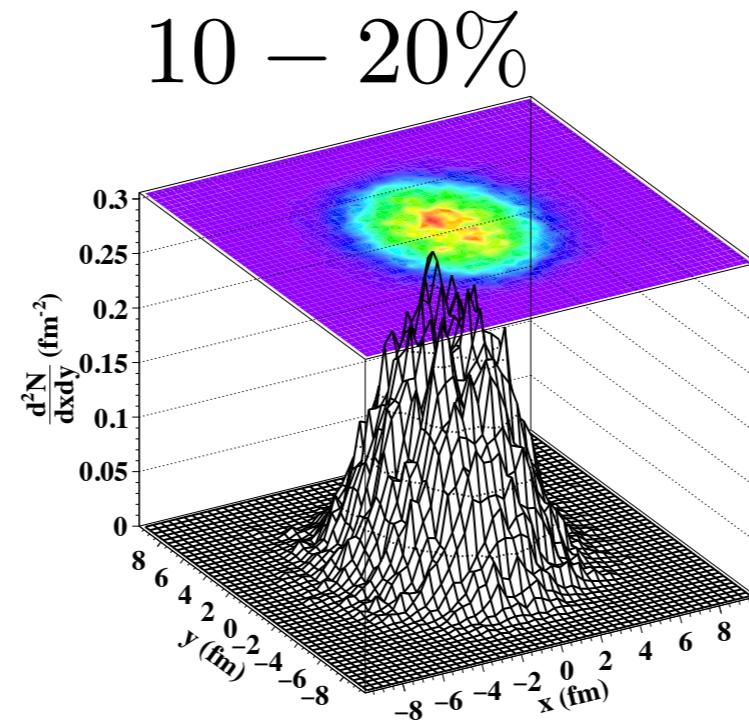
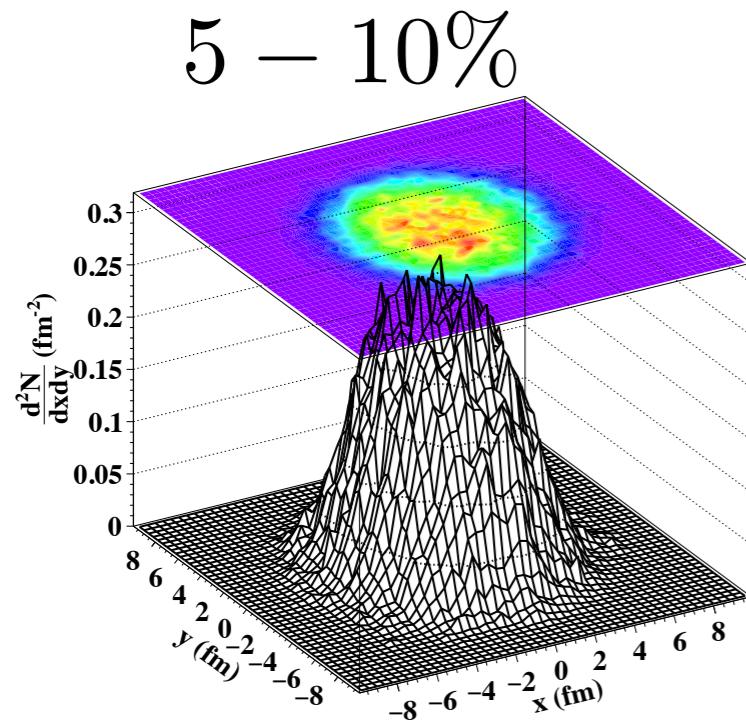


$$\epsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$



$$v_2 = \frac{\langle p_y^2 - p_x^2 \rangle}{\langle p_y^2 + p_x^2 \rangle}$$

# Initial Geometry at 2.76 TeV

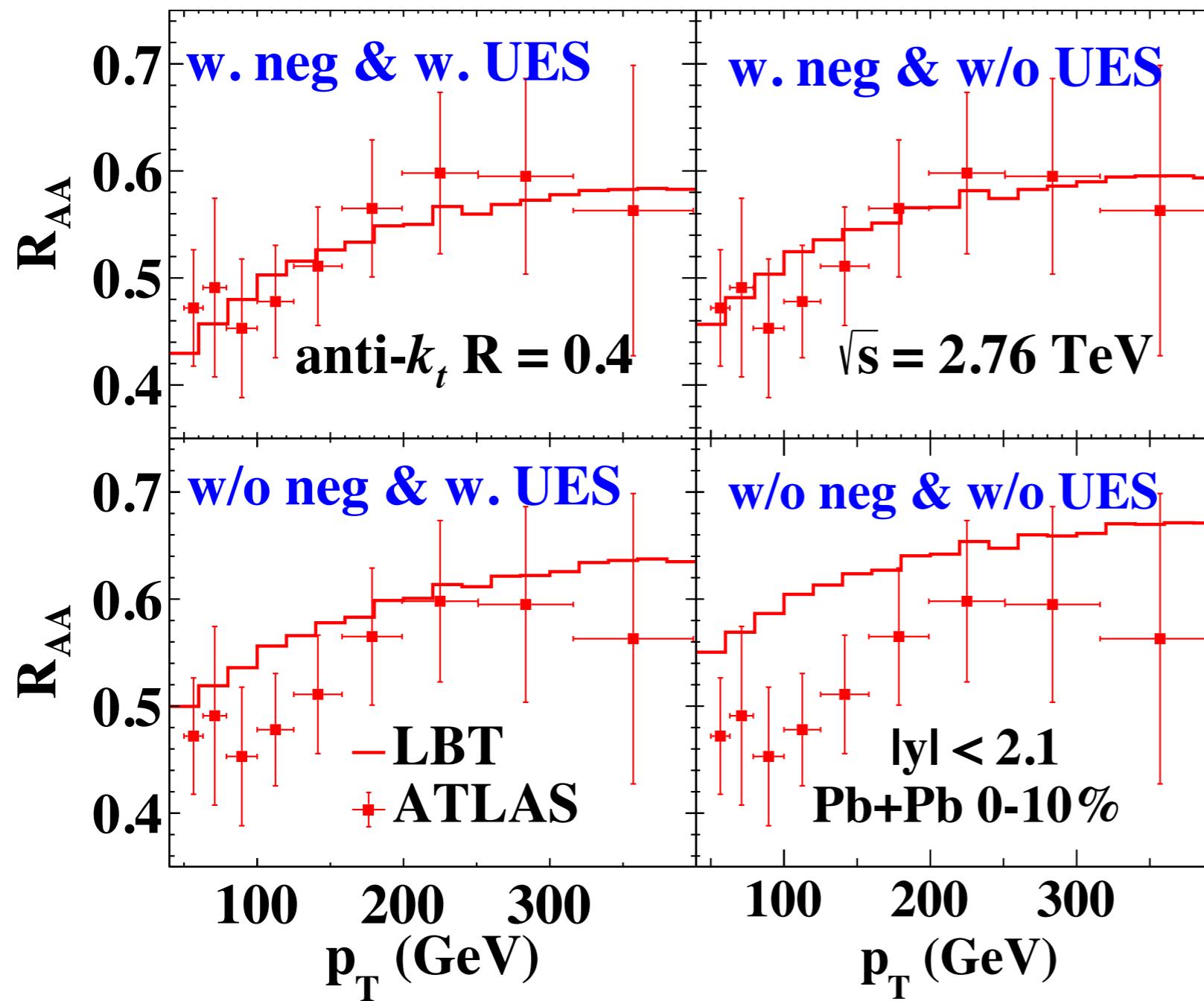


averaged over 200 3+1D event-by-event hydro profiles  
Pang, Wang & Wang, arXiv:1205.5019



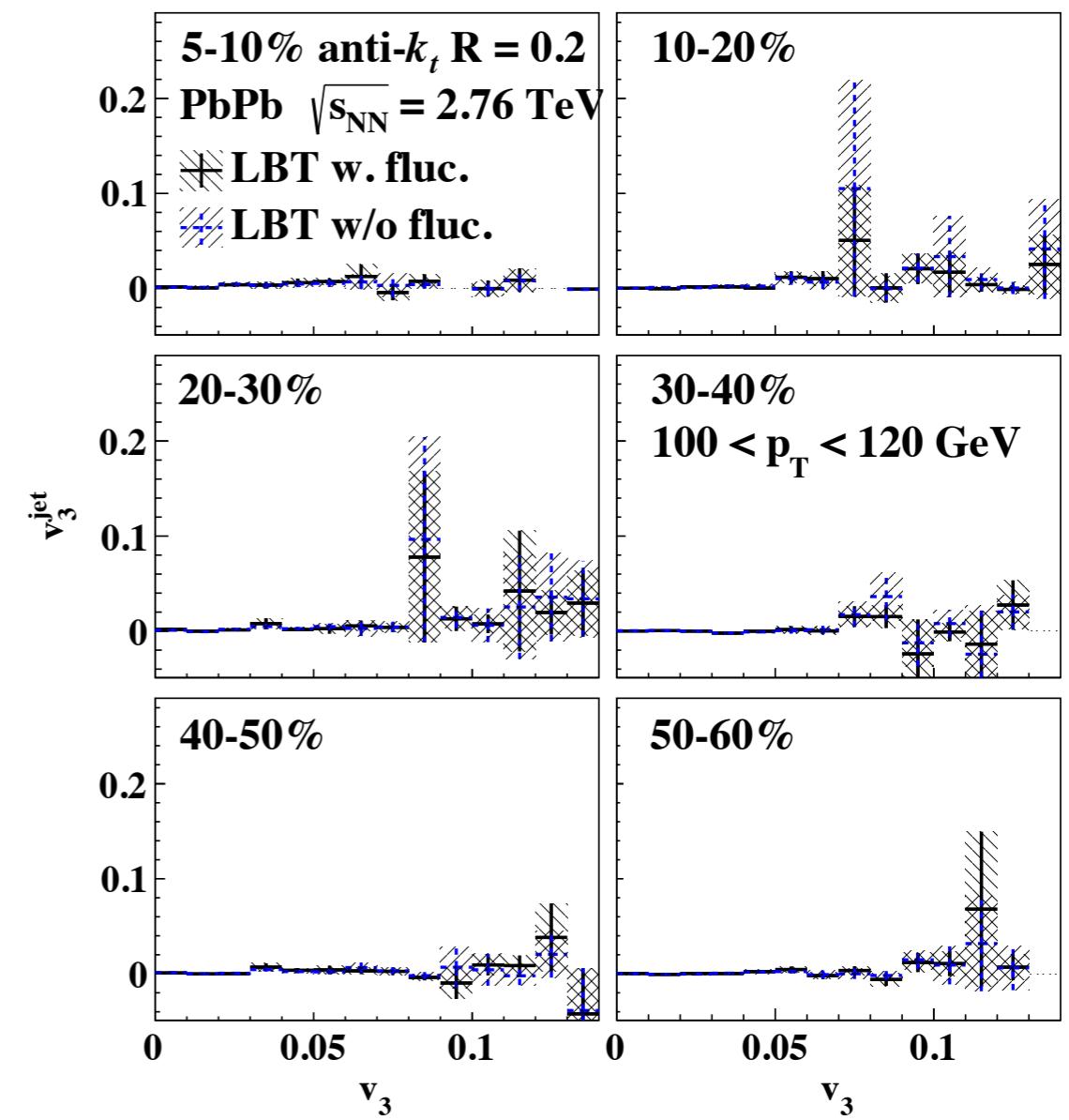
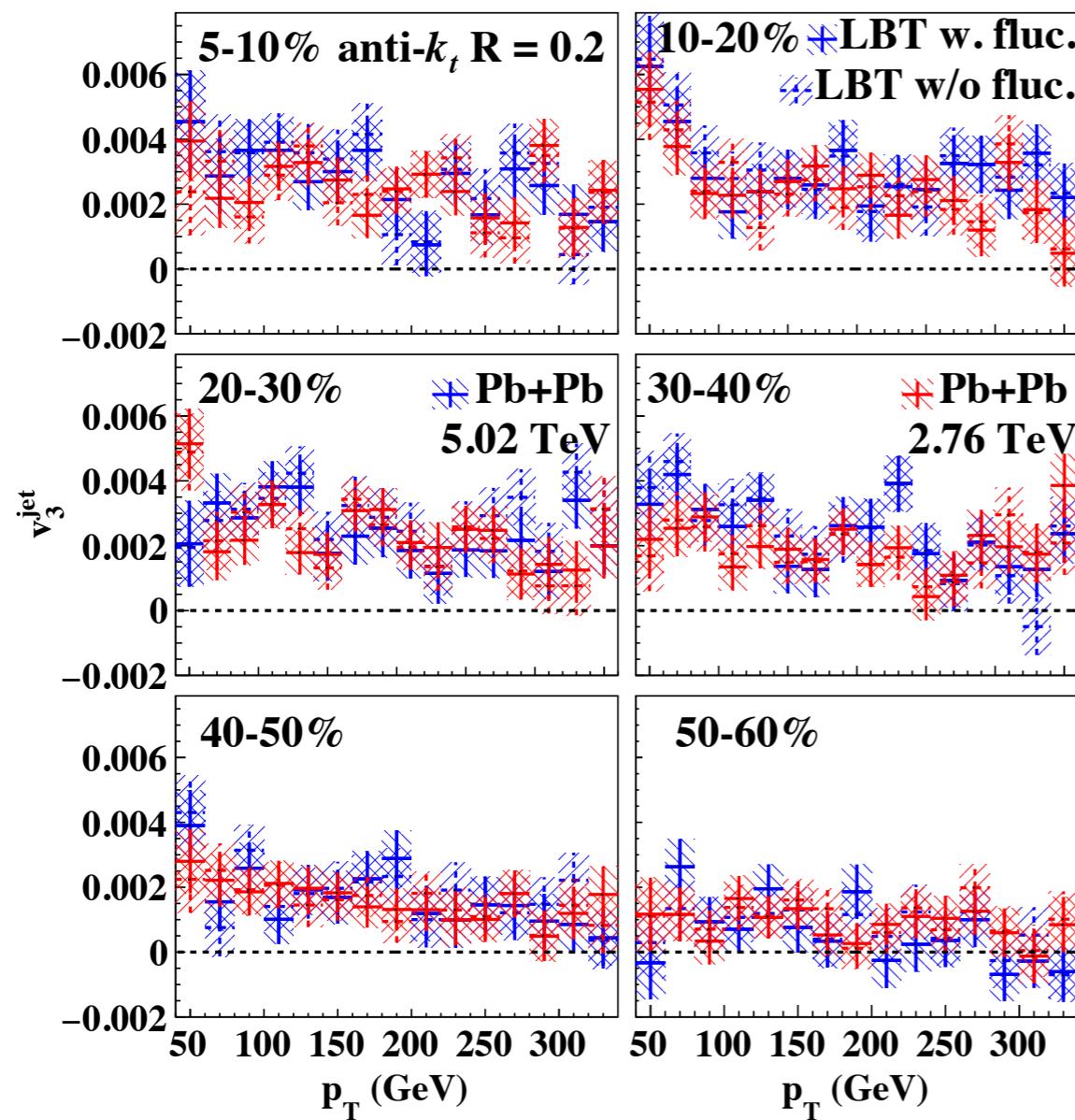
# Results: Inclusive jet suppression

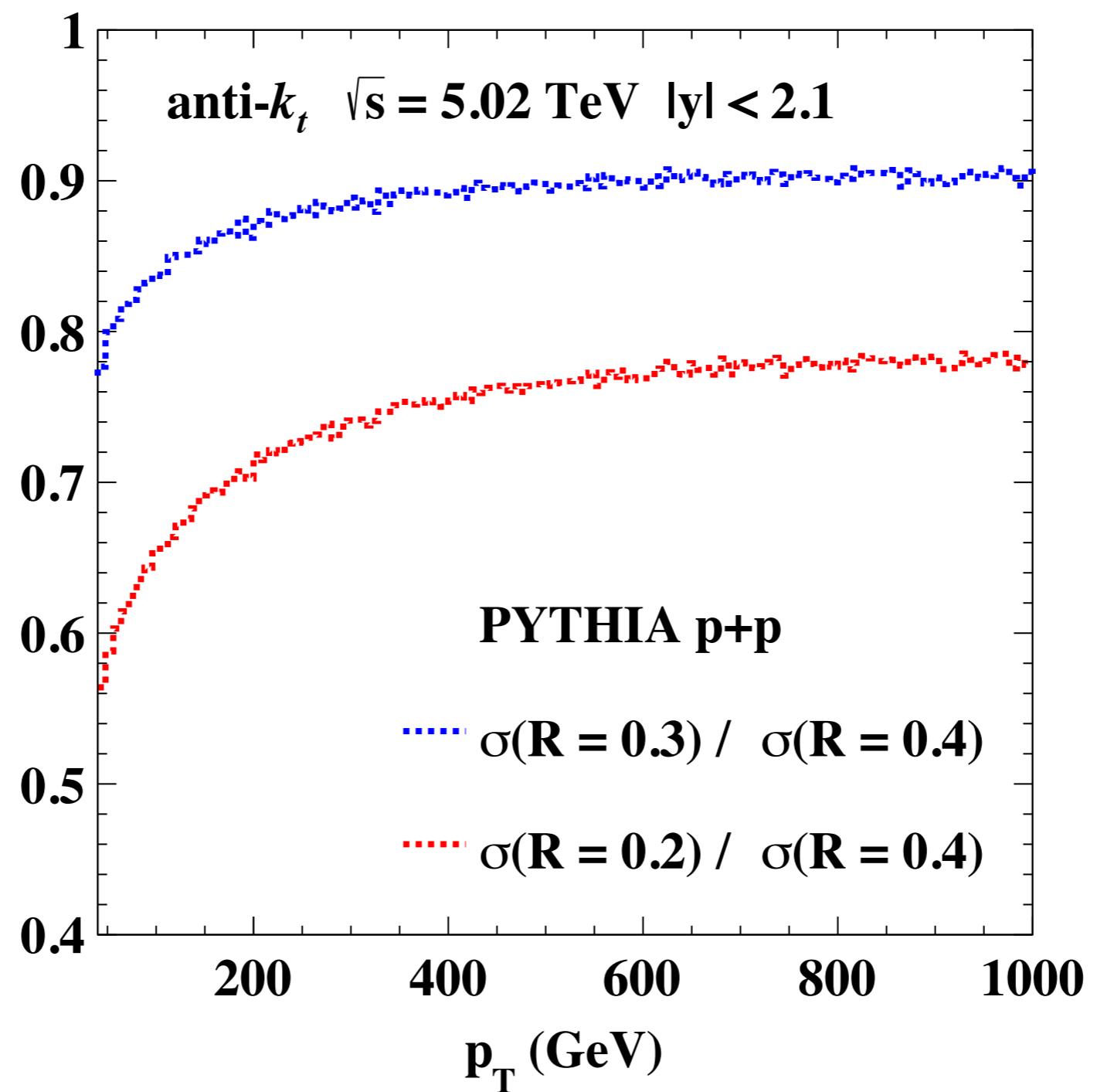
fixed  $\alpha_s = 0.15$



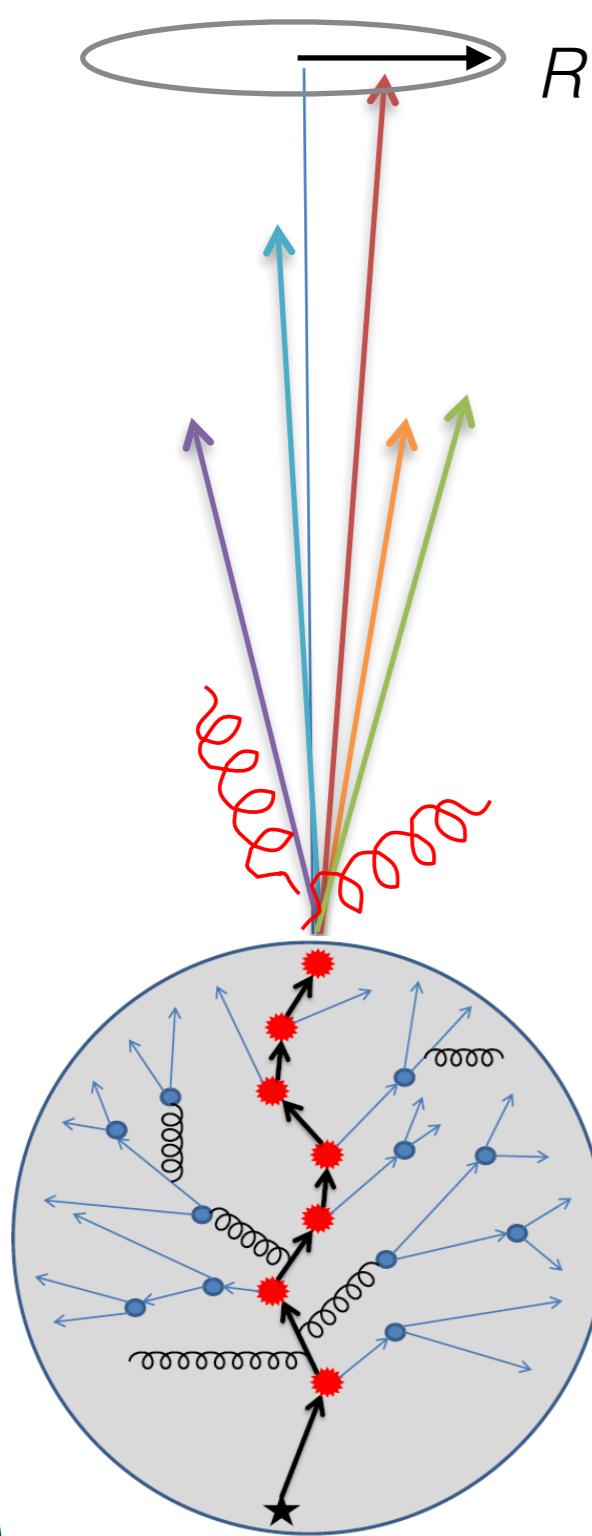
*Suppression!!!*  
*w. neg (whole  $p_T$  range);*  
*w. UES (low  $p_T$  range)*







# Jet reconstruction including medium recoils and back reaction



anti- $k_t$  algorithm in FASTJET package is used to reconstruct jets

$$\sqrt{(\eta - \eta_J)^2 + (\phi - \phi_J)^2} < R$$

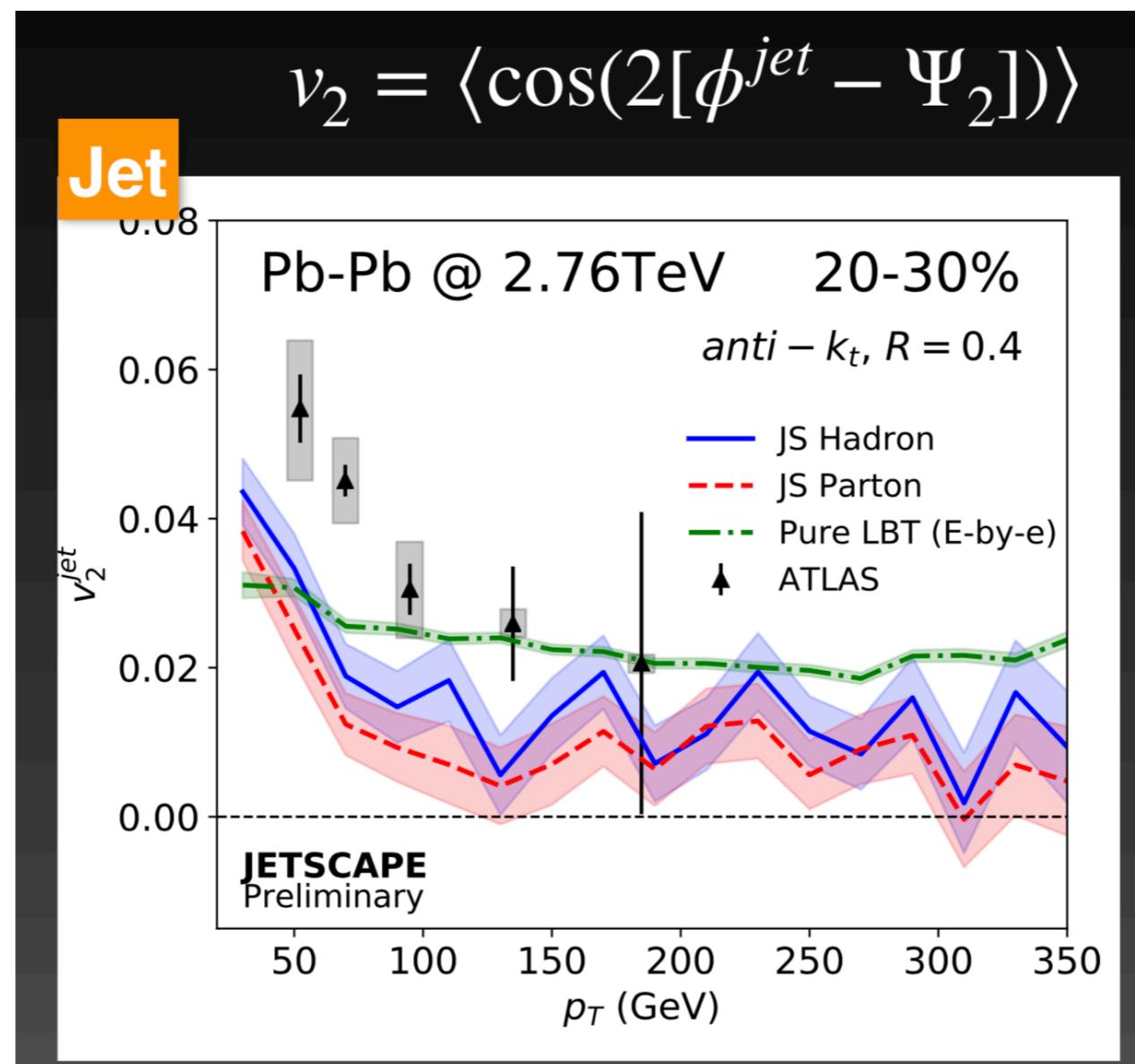
M. Cacciari, G. P. Salam and G. Soyez, Eur. Phys. J. C 72, 1896 (2012).

consider all the jets

modified FASTJET,  
**subtract** the “negative” particles

medium recoil re-scattering,  
back reaction (“negative particles”)

# Inclusive jet anisotropy



Multistage evolution, see: Chanwook Park, HP 2018



$$v_{\{2\}^{\text{jet}}} = \frac{\langle v_{\{2\}^{\text{soft}}} \cos(2[\phi^{\text{jet}} - \Psi_{\{2\}}]) \rangle}{\sqrt{\langle (v_{\{2\}^{\text{soft}}})^2 \rangle}}$$

$$\frac{d \sigma^{\text{AA}_{\text{jet}}}}{dp_T dy}(p_T, R) = \int d\Delta p_T W_{\text{AA}}(\Delta p_T, p_T + \Delta p_T, R) \frac{d\sigma^{\text{pp}_{\text{jet}}}}{dp_T dy}(p_T + \Delta p_T, R)$$

$$x = \frac{\Delta p_T}{\langle \Delta p_T \rangle}$$

$$W_{\text{AA}}(x) = \frac{\alpha^{\alpha}}{\Gamma(\alpha)} x^{\alpha-1} e^{-\alpha x}$$

$$\equiv \int \prod_{i=1}^a dx_i e^{-\sum_i a_i x_i} \delta(x - \sum_{i=1}^a x_i)$$

$$\sigma^{\text{pp}_{\text{jet}}}(p_T) + W_{\text{AA}}(p_T, \Delta p_T) \rightarrow \sigma^{\text{AA}_{\text{jet}}}(p_T)$$

$$\langle \Delta p_T \rangle = \beta p_T^{\gamma} \log(p_T)$$
