

Measurement of the branching fraction of $J/\psi \rightarrow \phi\eta$

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June 2019

Motivation I

Improved estimation of the mixing angle between strong and electromagnetic amplitudes in $J/\psi \rightarrow \phi\eta$ decay

Formulas of cross section for lineshape fit of $J/\psi \rightarrow \phi\eta$

$$\begin{aligned}\sigma_{\text{born}}(s) &= |\mathcal{A}_{\text{cont.}} + \mathcal{A}_\gamma + \mathcal{A}_{3g}|^2 \\ &= \frac{\sigma_0}{s^2} \left| 1 + \frac{3/\alpha \sqrt{s} \Gamma_e \Gamma_\mu}{(s - M^2) + i \sqrt{s} \Gamma} \cdot (1 + A e^{i\varphi}) \right|^2 \times \left[\frac{|P|}{\sqrt{s}} \right]^3\end{aligned}$$

where σ_0 can be expressed through the $Br(J/\psi \rightarrow \phi\eta)$:

$$\sigma_0 = \frac{4\pi\alpha^2 s}{3} \cdot \frac{Br(J/\psi \rightarrow \phi\eta)}{Br(J/\psi \rightarrow \mu\mu)} \cdot \frac{1}{|1 + A e^{i\varphi}|^2} \left[\frac{\sqrt{s}}{|P|} \right]^3$$

- ✓ The value of the $Br(J/\psi \rightarrow \phi\eta)$ is obtained directly from the fit

Motivation I

Fit result:

$$Br = (10.5 \pm 0.5) \times 10^{-4}$$

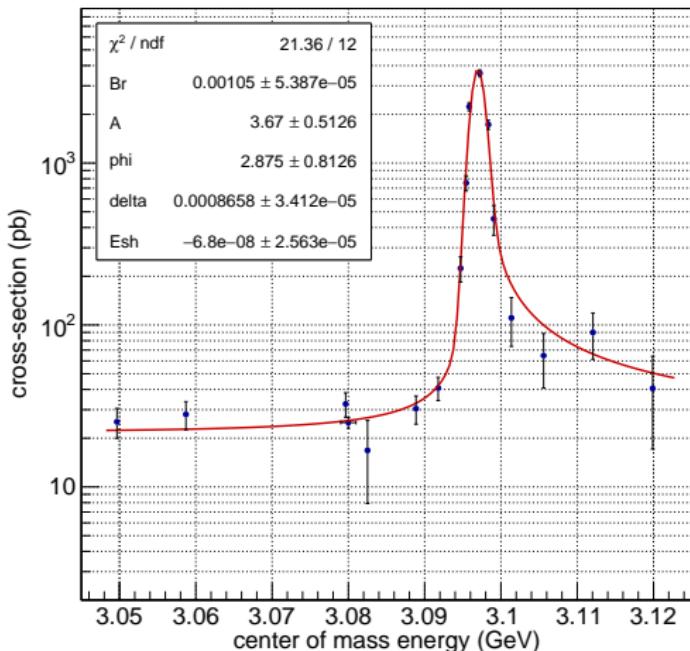
$$\varphi = 2.88 \pm 0.81$$

PDG weighted average:

$$(7.5 \pm 0.8) \times 10^{-4}$$

BES-2 measurement:

$$(8.99 \pm 0.18 \pm 0.89) \times 10^{-4}$$



Motivation I

Include PDG val. in fit

$$\chi^2(\text{new}) = \chi^2(\text{old}) +$$

$$\frac{|Br(\text{fit}) - Br(\text{PDG})|^2}{\sigma^2(\text{PDG})}$$

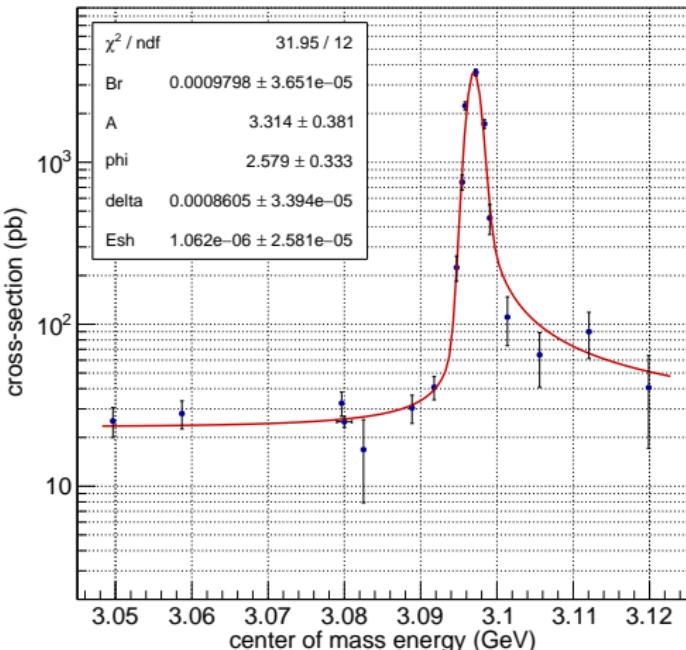
$$Br(\text{PDG}) = (7.5 \pm 0.8) \times 10^{-4}$$

Fit result:

$$Br = (9.8 \pm 0.4) \times 10^{-4}$$

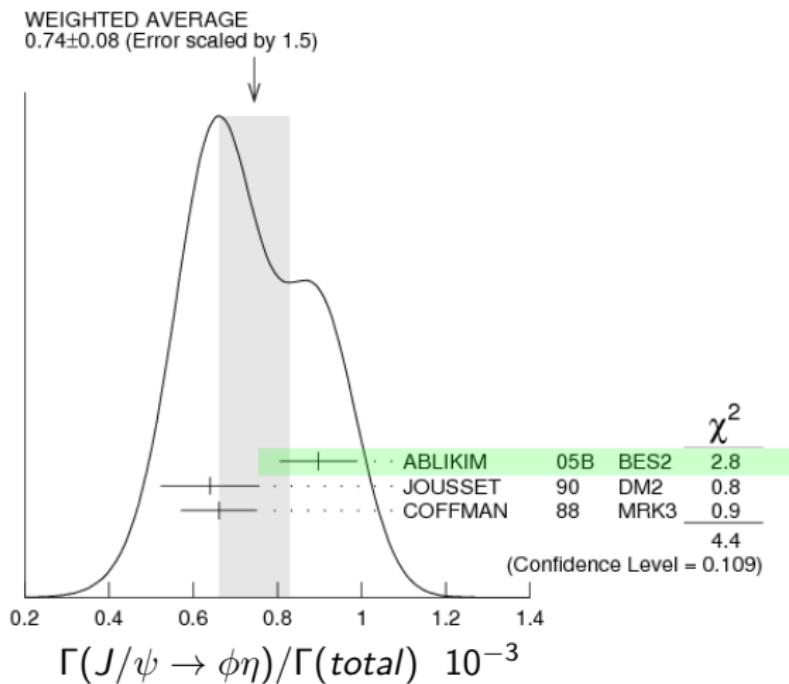
$$\varphi = 2.58 \pm 0.33$$

✓ Error on φ is reduced by factor 2.5



Motivation II

The existing measurements of $Br(J/\psi \rightarrow \phi\eta)$ are ambiguous (PDG-2019)



Data & Monte-Carlo samples

Measurements are performed in the decay chain:

$$\psi(3686) \rightarrow \pi^+ \pi^- J/\psi, \quad J/\psi \rightarrow \phi \eta, \quad \phi \rightarrow K^+ K^-, \quad \eta \rightarrow \gamma\gamma.$$

- We used DST for $\psi(3686)$ 2009 and 2012.
- We used a continuum sample at 3.65 GeV to estimate the background from non resonant production.
- We used $\psi(3686)$ inclusive Monte Carlo simulated data for 2009 and 2012 (official samples).
- We generated signal MC data with BesEvenGen.
- We used two versions of the BOSS software
 - ▶ **6.6.4p1** for 2009: data, MC and continuum sample
 - ▶ **6.6.4p3** for 2012: data and MC

Event Selection I: $\psi(3686) \rightarrow \pi^+ \pi^- J/\psi$

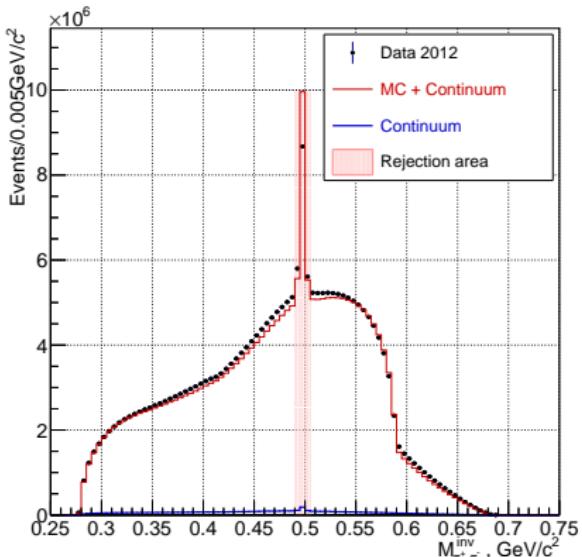
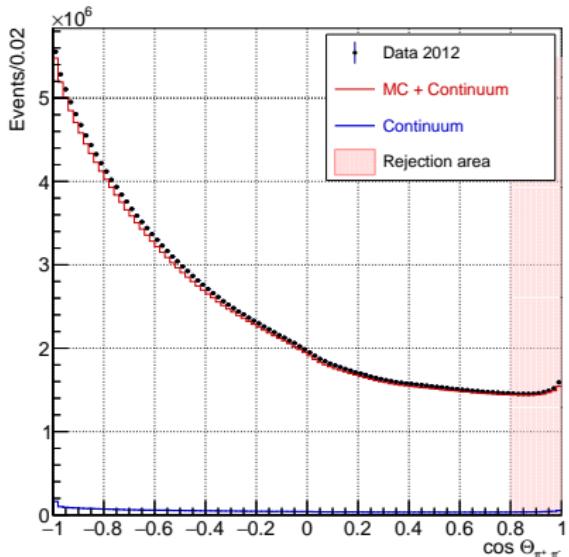
At least two opposite charged soft pions:

- $|R_{xy}| \leq 1 \text{ cm}; |R_z| \leq 10 \text{ cm}$
- $\cos(\Theta) \leq 0.80$
- PID: $\text{Prob}(\pi) > \max(\text{Prob}(K), \text{Prob}(\text{proton}), 0.001)$
- $P_\pi < 0.45 \text{ GeV}/c$

We consider a good pair of $\pi^+ \pi^-$ if:

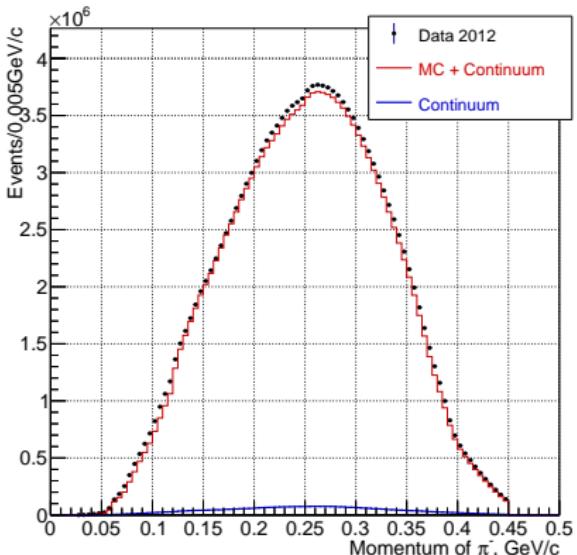
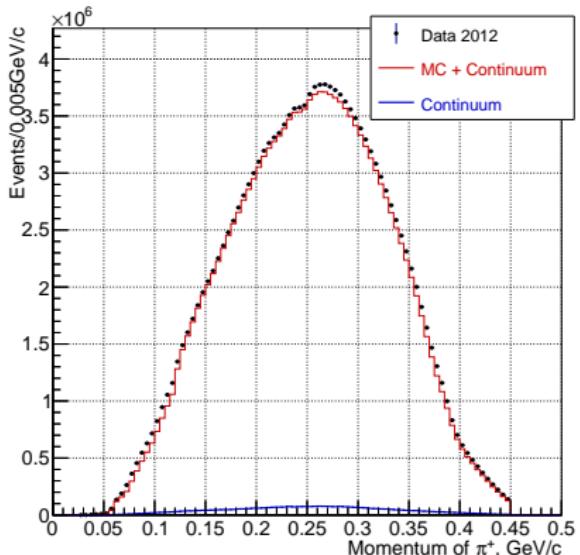
- $\cos(\Theta_{\pi^+ \pi^-}) < 0.80$ (to suppress pions flying in one direction)
- $|M_{\pi^+ \pi^-}^{inv} - M(K_S^0)| > 0.008 \text{ GeV}/c^2$ (to suppress pions from K_S^0)
- $3.0 \leq M_{\pi^+ \pi^-}^{rec} \leq 3.2 \text{ GeV}/c^2$
where the recoil mass is: $M_{\pi^+ \pi^-}^{rec} = \sqrt{(P_{ecm} - p_{\pi^+} - p_{\pi^-})^2}$

Selection $\pi^+\pi^-$: data vs MC



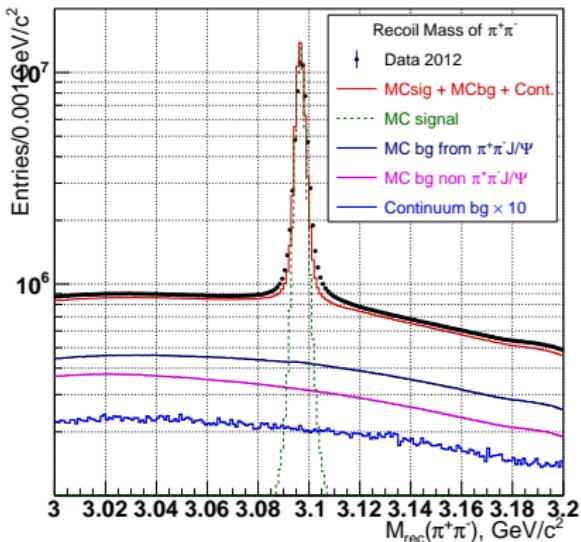
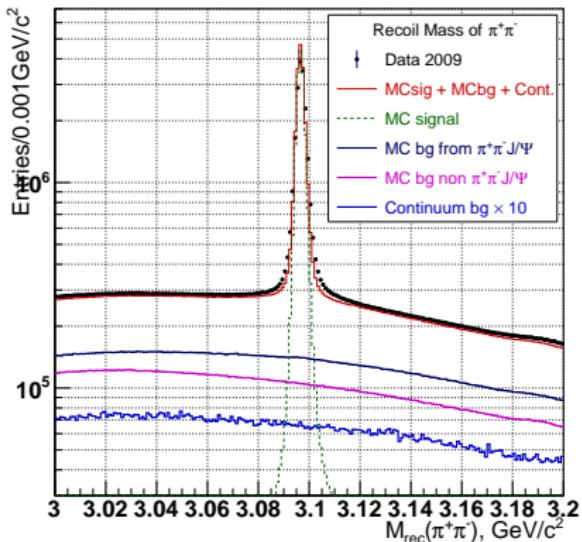
- Good agreement between data and inclusive MC
- The 2009 distributions are almost identical

Selection $\pi^+\pi^-$: data vs MC



- Good agreement between data and inclusive MC
- The 2009 distributions are almost identical

Recoil mass of $\pi^+\pi^-$: data vs MC



- These distributions were used to estimate the number of J/ψ in our selection

Estimation of the number of J/ψ

Side-Band Method

- Fit data in the region far from the J/ψ peak:

$$M_{\pi^+\pi^-}^{rec} \in [3.00; 3.06] \cup [3.14; 3.20] \text{ GeV}/c^2$$

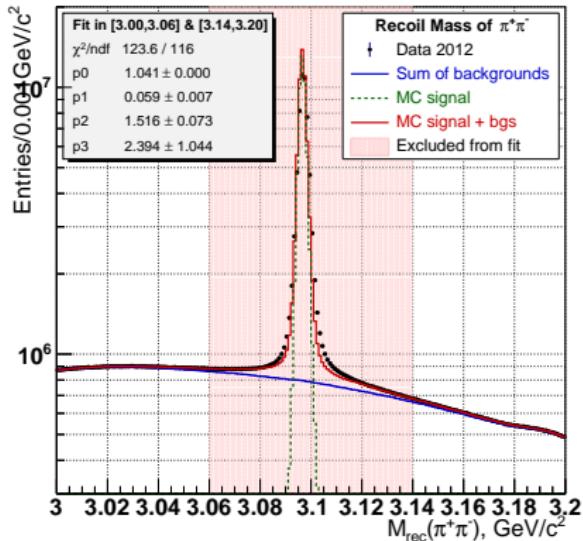
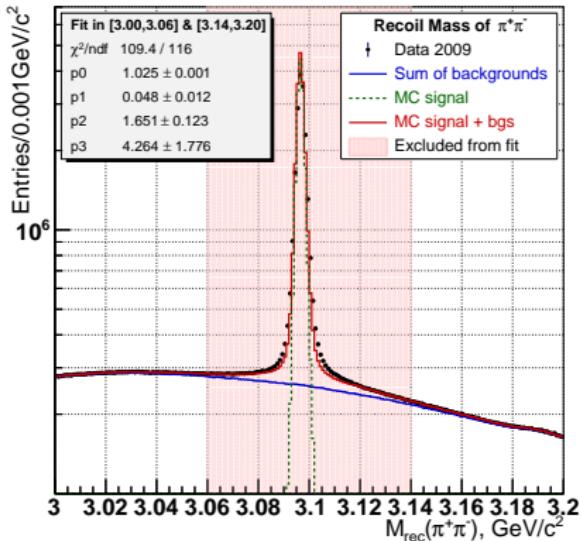
- The fitting function is:

$$MC(Bkg) \times P_3(M_{\pi^+\pi^-}^{rec} - 3.1) + Cont + MC(Sig),$$

- $MC(Bkg)$ is the sum of the background distributions
- $P_3(x)$ is the third order polynomial
- $Cont$ is the non-resonance production
- $MC(Sig)$ is the signal distribution

- The number of J/ψ is calculated as the number of data minus the fitted background

The side-band fit of $M_{\pi^+\pi^-}^{rec}$



$M_{\pi^+\pi^-}^{rec}$ (GeV/c ²)	$N(J/\psi)$ in 2009	$N(J/\psi)$ in 2012
[3.055, 3.145]	17839834 ± 8108	55383311 ± 14357
[3.092, 3.102]	15738304 ± 4603	48669687 ± 8111

Systematic uncertainties in the side-band fit

Variation of polynomial order (P-degree) and fit range

	P-degree	fit range (GeV/c^2)	χ^2/ndf	$N_{J/\psi}$	$\delta(\%)$
2009	3	[3.00,3.06] \cup [3.14,3.20]	109/116	17839834	—
	2	[3.00,3.06] \cup [3.14,3.20]	115/117	17834768	0.03
	4	[3.00,3.06] \cup [3.14,3.20]	107/115	17805529	0.19
	3	[3.00,3.05] \cup [3.15,3.20]	91/96	17850882	0.06
	3	[3.00,3.07] \cup [3.13,3.20]	140/136	17818151	0.12
2012	3	[3.00,3.06] \cup [3.14,3.20]	124/116	55383311	—
	2	[3.00,3.06] \cup [3.14,3.20]	129/117	55373982	0.02
	4	[3.00,3.06] \cup [3.14,3.20]	122/115	55340269	0.08
	3	[3.00,3.05] \cup [3.15,3.20]	104/96	55415283	0.06
	3	[3.00,3.07] \cup [3.13,3.20]	177/136	55330721	0.09

- numbers are given for «wide interval» $M_{\pi^+\pi^-}^{\text{rec}} \in [3.055, 3.145]\text{GeV}/c^2$
- for a narrower interval the error is much smaller

Second method for estimation of the number of J/ψ

Fit method

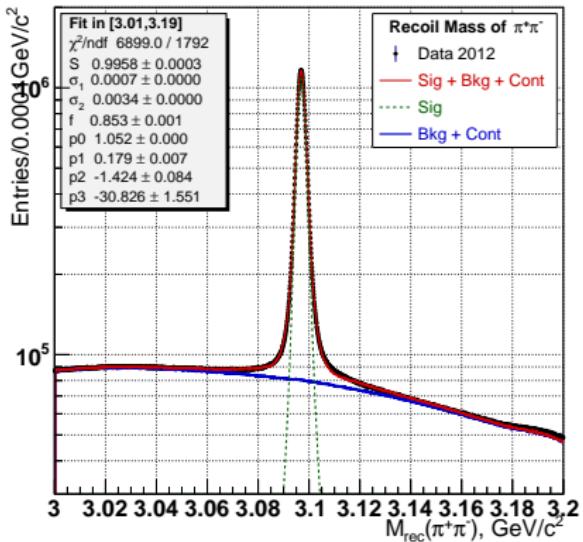
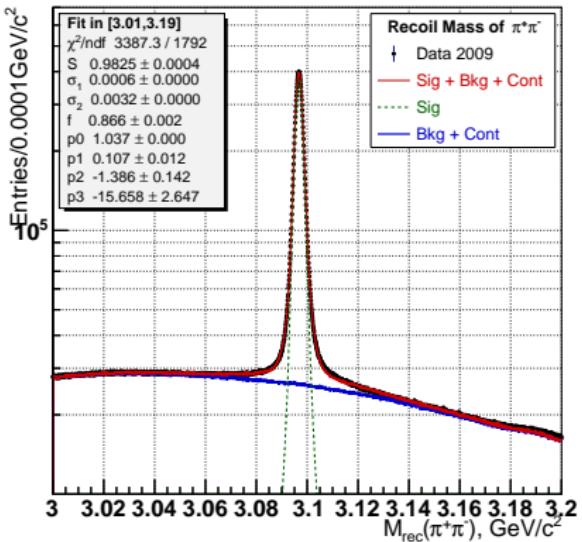
- Fit data in the entire range of $M_{\pi^+\pi^-}^{rec}$
- The fitting function is:

$$MC(Bkg) \times P_3(M_{\pi^+\pi^-}^{rec} - 3.1) + Cont + Sig(M_{\pi^+\pi^-}^{rec})$$

$$Sig(m) = S \times MC(Sig) \otimes (f \cdot \mathcal{G}(m, \sigma_1) + (1 - f) \cdot \mathcal{G}(m, \sigma_2))$$

- ▶ $MC(Sig)$ is the signal distribution convolving with the sum of two Gaussian functions $\mathcal{G}(m, \sigma)$
- ▶ σ_1 , σ_2 , f and S are the parameters of the fit
- The number of J/ψ is calculated as the integral of $Sig(M_{\pi^+\pi^-}^{rec})$ in the corresponding window

The fit of $M_{\pi^+\pi^-}^{rec}$ in the entire range



$M_{\pi^+\pi^-}^{rec}$ (GeV/c ²)	$N(J/\psi)$ in 2009	$\delta(\%)$	$N(J/\psi)$ in 2012	$\delta(\%)$
[3.055, 3.145]	17603315 ± 4161	1.3	54740554 ± 6751	1.2
[3.092, 3.102]	15703865 ± 3929	0.22	48560298 ± 6357	0.22

- δ is the difference from side-band method

Number of $\psi(3686) \rightarrow \pi^+\pi^- J/\psi$ events

Summary: $Br \equiv Br(\psi' \rightarrow \pi^+\pi^- J/\psi)$

	$M_{\pi^+\pi^-}^{rec}$ (GeV/c ²)	N(J/ ψ)	δ_{sys} (%)	ε (%)	Br (%)
2009	[3.055, 3.145] [3.092, 3.102]	17839834 15738304	1.3 0.22	47.80 \pm 0.28 42.65 \pm 0.26	34.9 \pm 0.5 34.5 \pm 0.3
2012	[3.055, 3.145] [3.092, 3.102]	55383311 48669687	1.2 0.22	45.99 \pm 0.28 40.80 \pm 0.24	35.3 \pm 0.5 35.0 \pm 0.3

- Numbers will be used in the rest of this presentation
- Selection efficiency ε was obtained from inclusive MC with corrections on pion tracking efficiency

Notes on branching ratio $Br(\psi' \rightarrow \pi^+ \pi^- J/\psi)$

- ✓ The systematic errors are dominant
- ✓ Good agreement of branching obtained in wide and narrow intervals:
errors are fully correlated and therefore $\sigma_{\Delta} = \sqrt{|\sigma_1^2 - \sigma_2^2|} = 0.4\%$
- ✓ Good agreement between 2009 and 2012
- ✓ Good agreement with previous BES-3 result based on the same 2009 data: $B(\psi' \rightarrow \pi^+ \pi^- J/\psi) = (34.98 \pm 0.02 \pm 0.45)\%$

Event Selection: $J/\psi \rightarrow \phi\eta$ ($\phi \rightarrow K^+K^-$; $\eta \rightarrow \gamma\gamma$)

Charged tracks

- We choose $\pi^+\pi^-$ with $M_{\pi^+\pi^-}^{rec}$ closest to the mass of J/ψ
- $M_{\pi^+\pi^-}^{rec} \in [3.092, 3.102] \text{ GeV}/c^2$
- In addition to the selected pions there must be two opposite charged kaons:
 - ▶ $|R_{xy}| \leq 1 \text{ cm}; |R_z| \leq 10 \text{ cm}$
 - ▶ $\cos(\Theta) \leq 0.80$
 - ▶ PID: $Prob(K) > \max(Prob(\pi), Prob(\text{proton}), 0.001)$

At least two photons:

- $E_\gamma > 25 \text{ MeV}$ (barrel EMC) or $E_\gamma > 50 \text{ MeV}$ (end-cap EMC)
- $\alpha_\gamma > 10^\circ$ for the angle relative to the nearest charged track

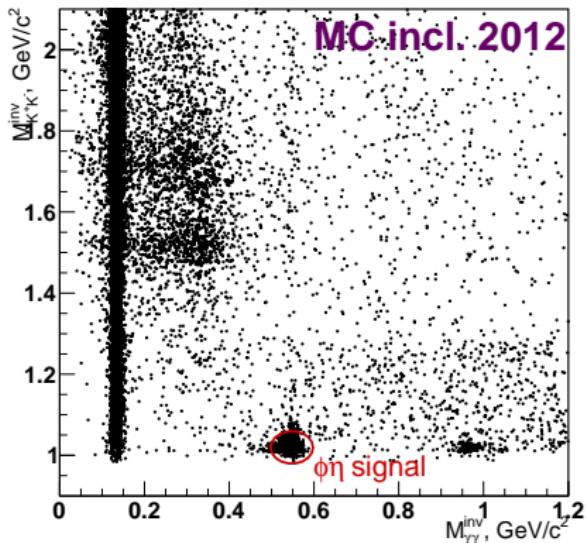
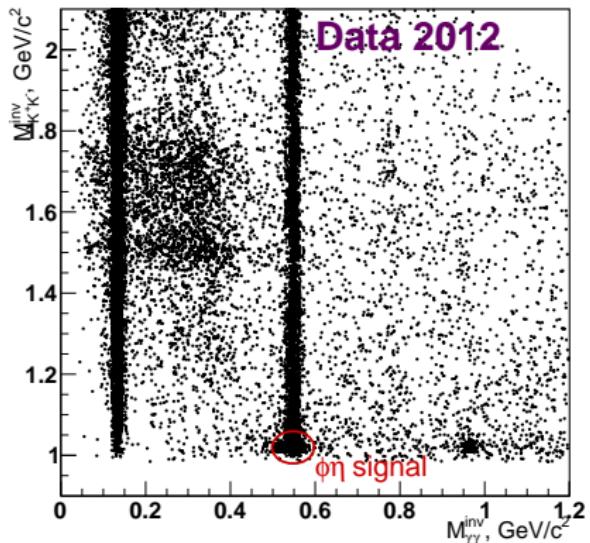
Event Selection: $\psi' \rightarrow \pi^+ \pi^- J/\psi$, $J/\psi \rightarrow \phi \eta$

5C kinematic constraints

- the 4-momentum of the system $\pi^+ \pi^- K^+ K^- 2\gamma$ should be P_{ecm}
- the invariant mass $M^{inv}(K^+ K^- 2\gamma)$ should be $M_{J/\psi}$
- we choose two photons with minimal χ^2_{5C}
- the event is discarded if $\chi^2_{5C} > 80$
- the event is discarded if there is a third photon such that:

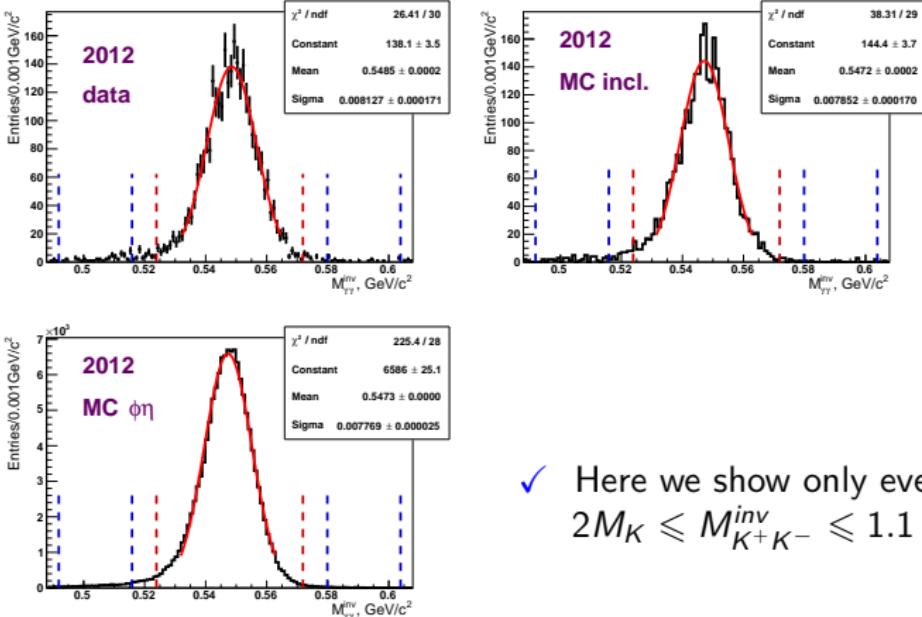
$$\chi^2_{5C}(\pi^+ \pi^- K^+ K^- 3\gamma) < \chi^2_{5C}(\pi^+ \pi^- K^+ K^- 2\gamma)$$

Invariant masses $M_{K^+K^-}^{inv}$ vs $M_{\gamma\gamma}^{inv}$; Data and MC



- Inclusive MC does not contain $K^+K^-\eta$ events above M_ϕ
- We generated MC data with final state $K^+K^-\eta$ (background MC) using BesEvenGen

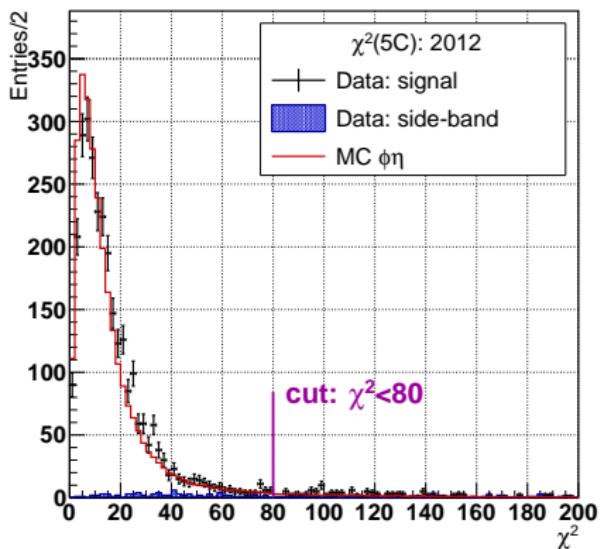
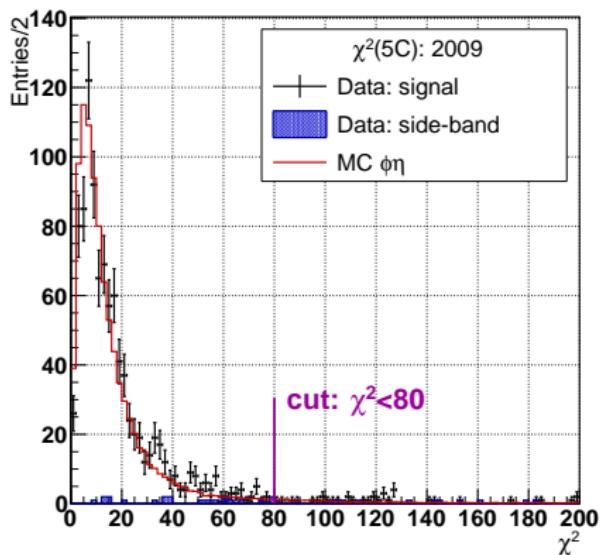
Invariant mass of $\eta \rightarrow \gamma\gamma$



✓ Here we show only events with $2M_K \leq M_{K^+K^-}^{inv} \leq 1.1$ GeV/c²

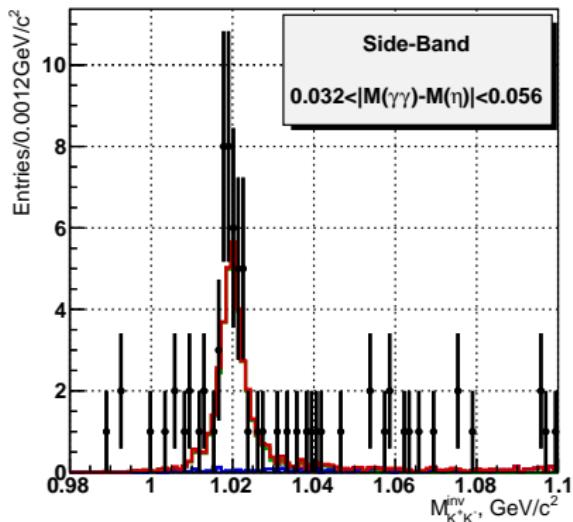
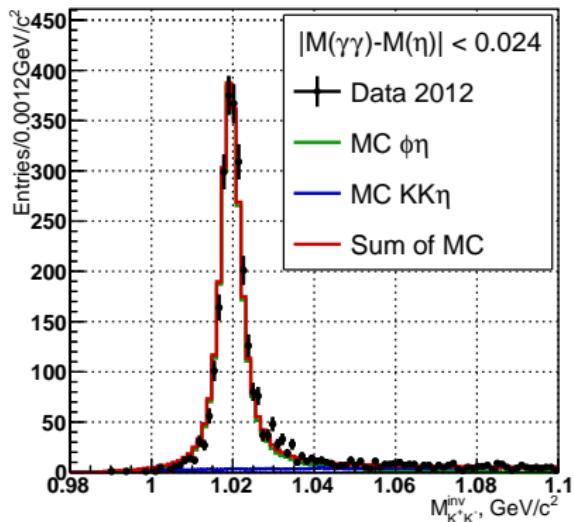
- The distributions fit with Gauss: $\sigma(\eta) \sim 8$ MeV
- The dashed lines show the selection window and side bands

$\chi^2(5C)$ for signal and side-band events



- Good agreement between data and signal MC

Invariant mass of $\phi \rightarrow K^+K^-$



- The data appears to be shifted to the right relative of the MC curve
- This is consistent with interference of $KK(\phi) - KK(\text{non resonant})$
- The effect was ignored in all previous measurements
- BESIII precision is so high that we must take into account the interference effect

Fit of $M_{K^+K^-}^{inv}$

Resonant part

- the relativistic Breit-Wigner corrected for the phase space:

$$\mathcal{BW}_\phi(m) = \frac{\kappa f^2(m)}{(m^2 - M_\phi^2)^2 + m^2 \Gamma^2(m)},$$

where energy dependant width $\Gamma(m)$ is

$$\Gamma(m) = \Gamma_\phi \left(\frac{p_K(m)}{p_K(M_\phi)} \right)^3 \frac{M_\phi}{m} \frac{B(p_K(m))}{B(p_K(M_\phi))},$$

$f(m)$ is correction factor and $B(p)$ is Blatt-Weisskopf penetration form factor:

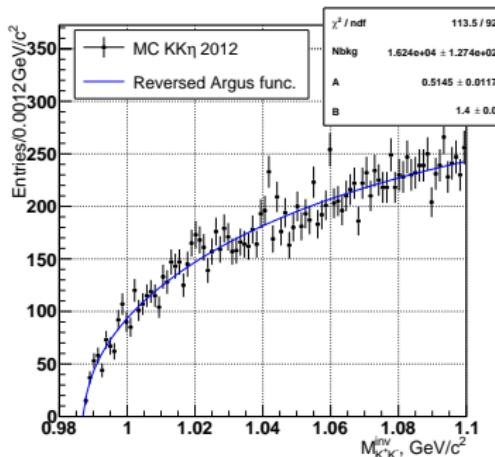
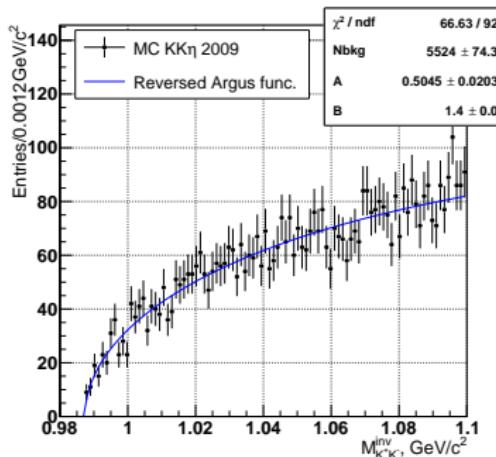
$$f(m) = \frac{p_\phi(m)}{p_\phi(M_\phi)} \frac{p_K(m)}{p_K(M_\phi)} \frac{B(p_\phi(m))}{B(p_\phi(M_\phi))} \frac{B(p_K(m))}{B(p_K(M_\phi))}, \quad B(p) = \frac{1}{\sqrt{1 + (rp)^2}}.$$

Fit of $M_{K^+K^-}^{inv}$

Background:

- reversed Argus function:

$$\mathcal{AR}(m) = m \cdot \exp(A \cdot \log(v) - B \cdot v), \quad v = 1 - \left(1 - \frac{m - L}{U}\right)^2$$

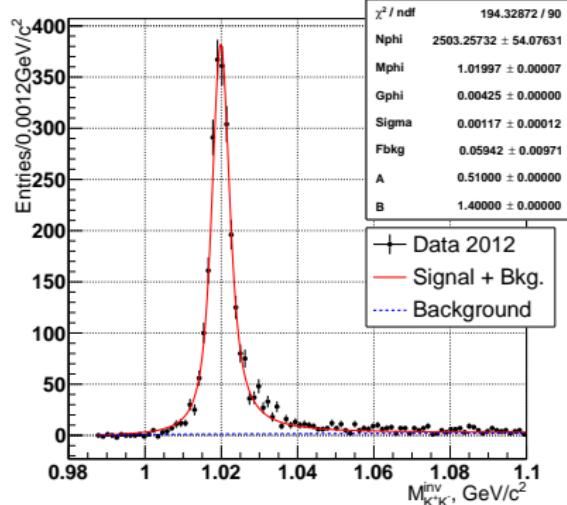
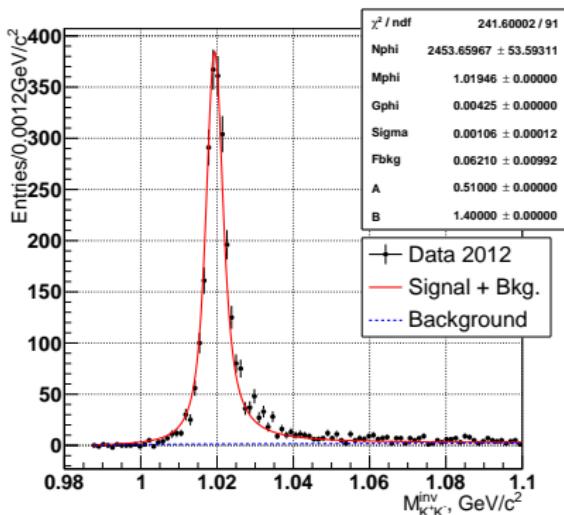


- Fit of MC $K^+K^-\eta$ background with Argus function

Fit of $M_{K^+K^-}^{inv}$ data by incoherent sum

- The incoherent sum of the Breit-Wigner convoluted with Gauss and Argus function:

$$\mathcal{BW}_\phi(m) \otimes \mathcal{G}(m) + \mathcal{AR}(m)$$



M_ϕ is fixed at the PDG value

M_ϕ is a free parameter

In general the data are described poorly: $\sim 0.5\text{MeV}$ shift relative to the PDG M_ϕ

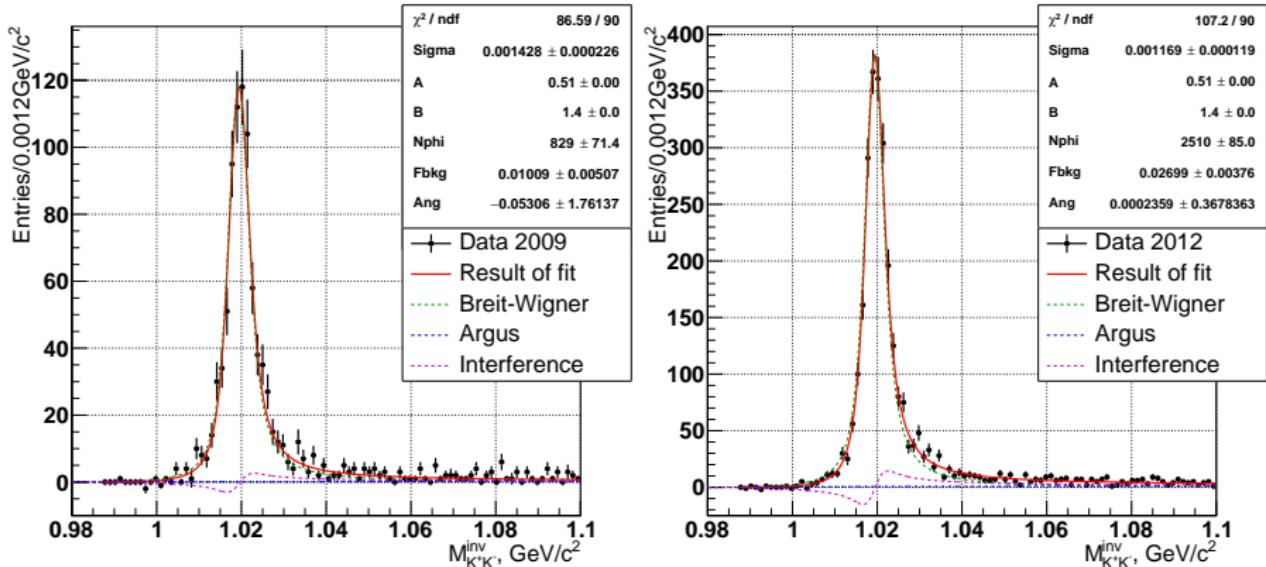
Fit of $M_{K^+K^-}^{inv}$ data, the interference

- The interference between $\phi\eta$ and $K^+K^-\eta$ final states:

$$\left| \mathcal{A}_{BW}(m) \times N_R \exp(i\vartheta) + \sqrt{\mathcal{AR}(m)} \right|^2 \otimes \mathcal{G}(m)$$

- $\mathcal{A}_{BW}(m)$ is the Breit-Wigner amplitude
- N_R is the magnitude of the ϕ resonance
- ϑ is the mixing angle
- $\mathcal{AR}(m)$ is the Argus function

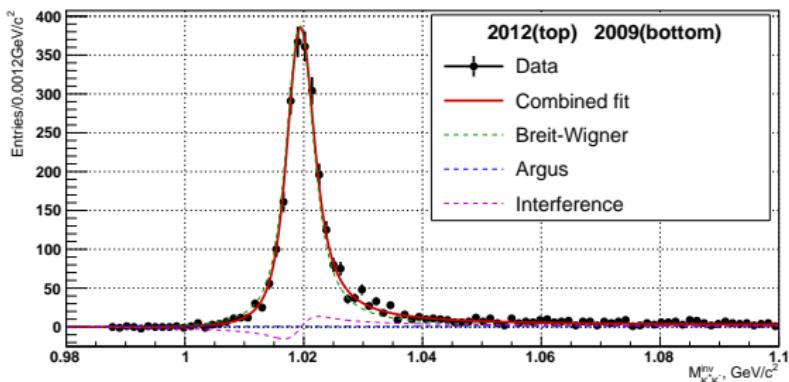
Fit of $M_{K^+K^-}^{inv}$ data, the interference



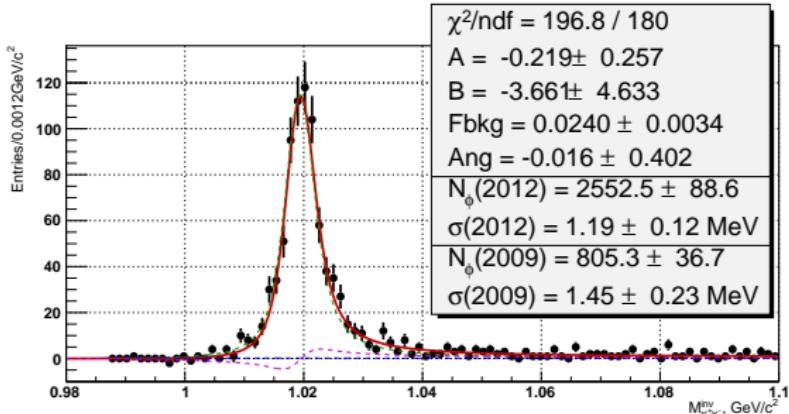
- $\chi^2/ndf = 0.96$ for 2009 and 1.2 for 2012
- If M_ϕ is a free fit parameter then the fitted value is consistent with the PDG value within the fit error
- Both results are compatible to the zero mixing angle

Combined fit of $M_{K^+K^-}^{inv}$ data

- Both data periods are fitted at the same time
- Background parameters (A , B , F_{bkg}) and mixing angle are common



- Taking into account the interference changes the N_ϕ by $3 \div 4\%$, which is $\sim (1. \div 1.5) \times \sigma(\text{stat})$
- This effect was ignored in all past measurements



Branching fraction of $J/\psi \rightarrow \phi\eta$

Summary

	$N(K^+K^-\gamma\gamma)$	$\varepsilon(\%)$	$N(J/\psi)$	$Br(J/\psi \rightarrow \phi\eta)$
2009	805.3 ± 36.7	32.79 ± 0.17	15738304	$(8.1 \pm 0.4) \times 10^{-4}$
2012	2552.5 ± 88.6	31.90 ± 0.10	48669687	$(8.5 \pm 0.3) \times 10^{-4}$

- Selection efficiency ε was obtained from signal MC with corrections on kaon tracking efficiency
- We used the following branchings from PDG 2018:
 $Br(\eta \rightarrow \gamma\gamma) = (39.41 \pm 0.20)\%$
 $Br(\phi \rightarrow K^+K^-) = (49.2 \pm 0.5)\%$
- The errors are statistical only

PDG 2018: $Br(J/\psi \rightarrow \phi\eta) = (7.5 \pm 0.8) \times 10^{-4}$

Systematic uncertainties

- Number of J/ψ :
 - ▶ we estimated $\delta_{sys}(N_{J/\psi}) = 0.22\%$ for interval $M_{\pi^+\pi^-}^{rec} \in [3.092, 3.102]$
- Branching fractions (PDG):
 - ▶ $\delta Br(\phi \rightarrow K^+K^-) \oplus \delta Br(\eta \rightarrow \gamma\gamma) = 1.1\%$
- Track reconstruction efficiency:
 - ▶ the standard value $2 \times 1\%$ looks too big for this analysis, so we performed additional study to estimate difference in reconstruction efficiencies of kaons in data and MC (see the next slide)
- Photon reconstruction efficiency:
 - ▶ $2 \times 1\%$
here we are also trying to do additional study to reduce this error
The analysis is not yet complete
- Varying selection critiria:
this part is not complete yet
 - ▶ varying χ^2 cut
 - ▶ varying side-band criteria

Difference of tracking efficiency: Data vs MC

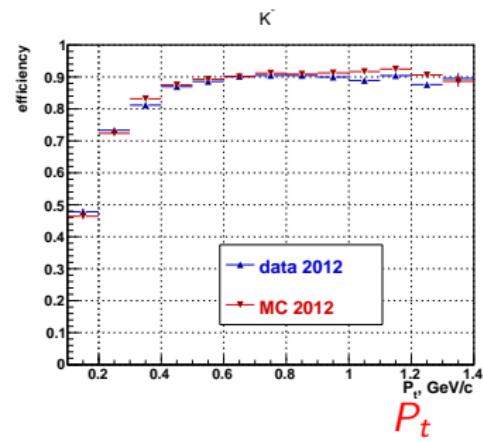
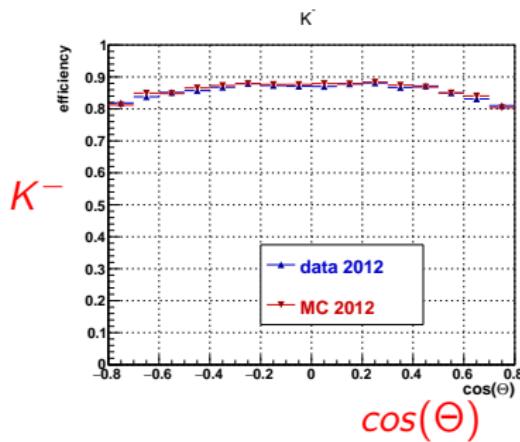
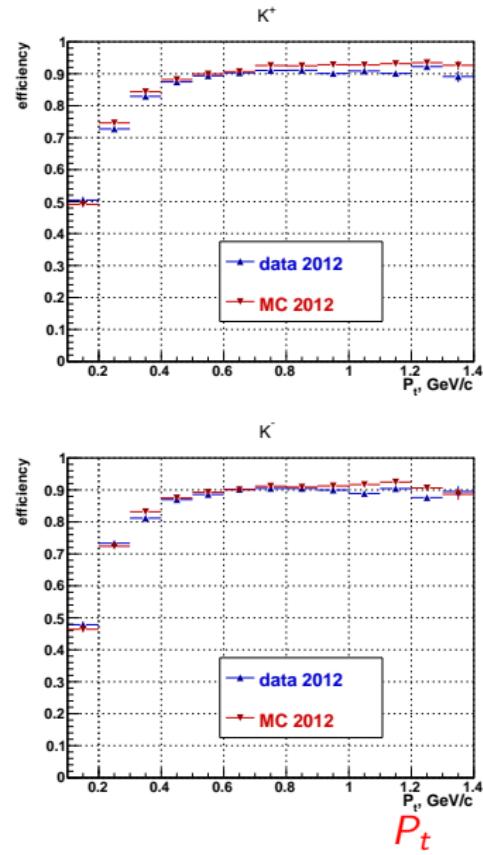
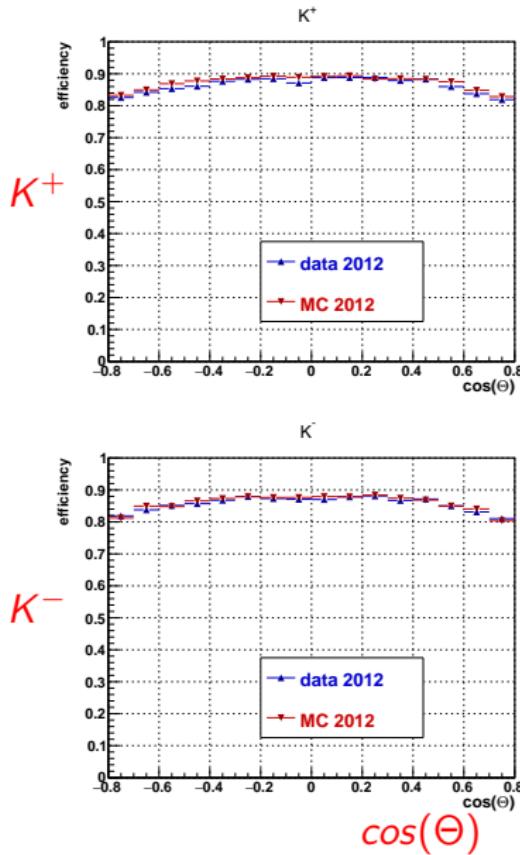
- We used process: $\psi' \rightarrow \pi^+ \pi^- J/\psi$, $J/\psi \rightarrow \pi^+ \pi^- K^+ K^-$ to measure the track efficiencies of pions and kaons
- For kaons:
 - ▶ $\pi^+ \pi^-$ pair was selected as described in «Event Selection I»
 $M_{\pi^+ \pi^-}^{rec} \in [3.095, 3.099] \text{ GeV}/c^2$
 - ▶ “tag” a J/ψ decay by $\pi^+ \pi^- K^{(\pm)}$ with a missing mass about M_K
 - ▶ we checked whether $K^{(\mp)}$ was reconstructed or not
- For pions:
 - ▶ “tag” a J/ψ event by $\pi^+ \pi^- K^+ K^-$ with invariant mass:
 $M^{inv} \in [3.087, 3.105] \text{ GeV}/c^2$
 - ▶ we search for additional $\pi^{(\pm)}$ and the missing mass is about M_π
 - ▶ we checked whether $\pi^{(\mp)}$ was reconstructed or not

definition of track reconstruction efficiency ϵ

$$\epsilon = \frac{N_6}{N_6 + N_5}$$

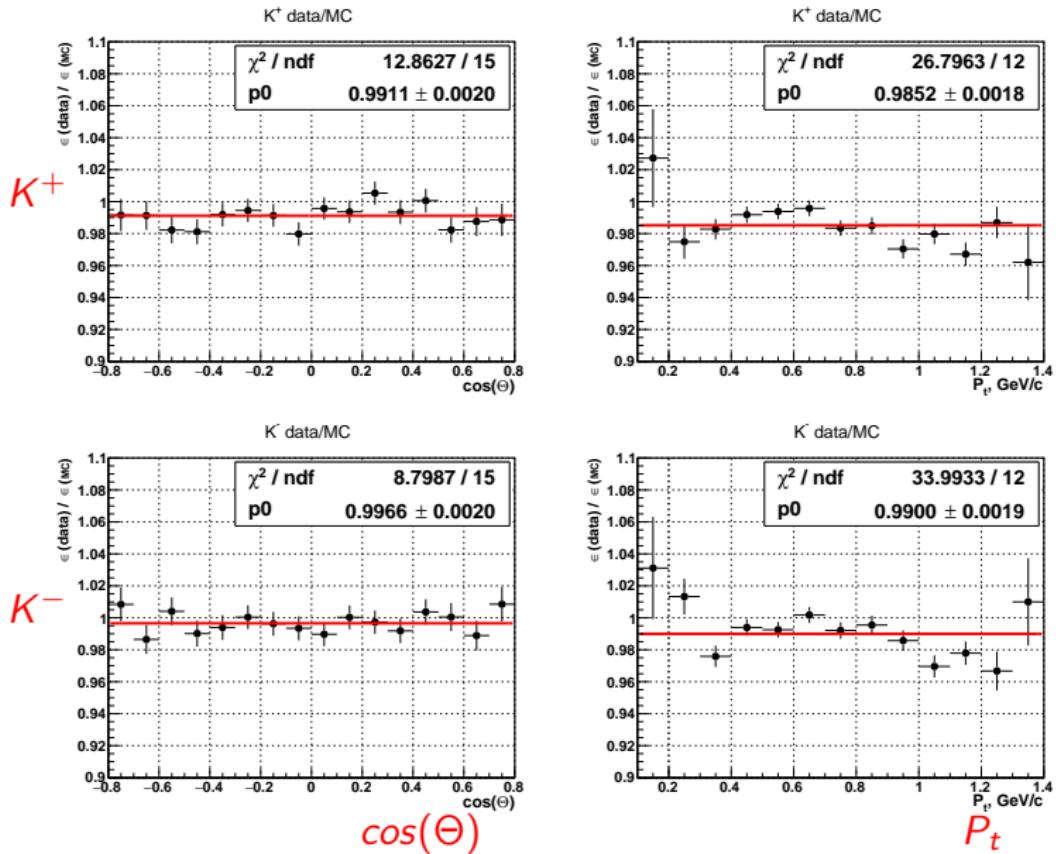
N_6 — all six tracks reconstructed
 N_5 — one track (π or K) is missing

Kaons: reconstruction track efficiency in 2012



P_t

Kaons: $\epsilon_{DATA}/\epsilon_{MC}$ in 2012

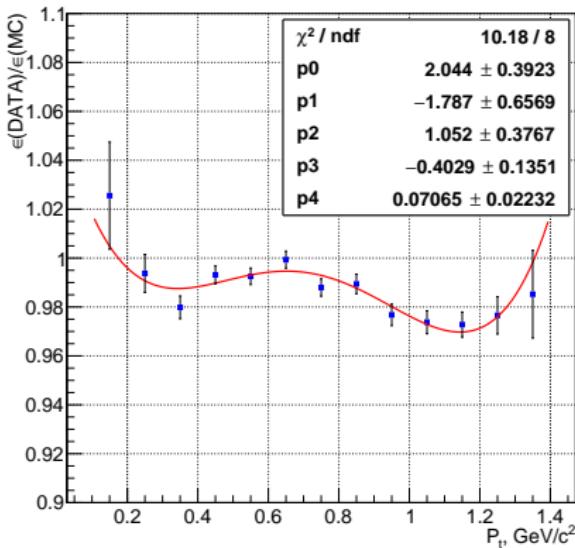


Efficiency corrections

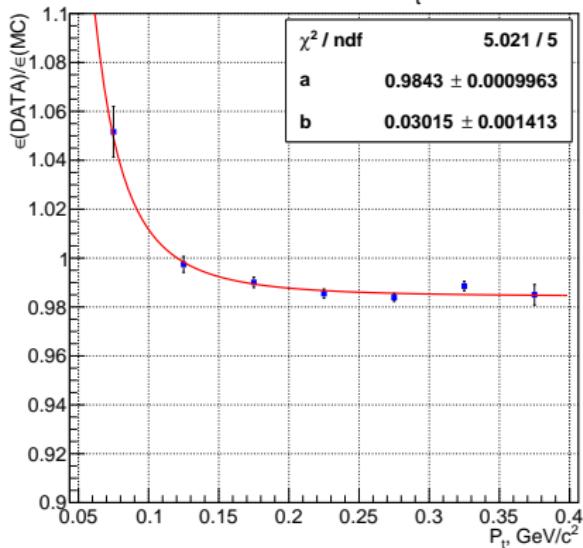
- To improve consistency between data and MC we used re-weighting for $\pi^+\pi^-$ and K^+K^- in MC
- Kolmogorov–Smirnov test showed that ratios of efficiencies for K^+ and K^- have the same distribution (the same fact for π^+ and π^-)
- There is no dependence on the polar angle of kaons and pions
- Efficiency corrections were obtained as a function on transverse momentum P_t

Efficiency corrections in 2012

Kaons: chebyshev polynomials

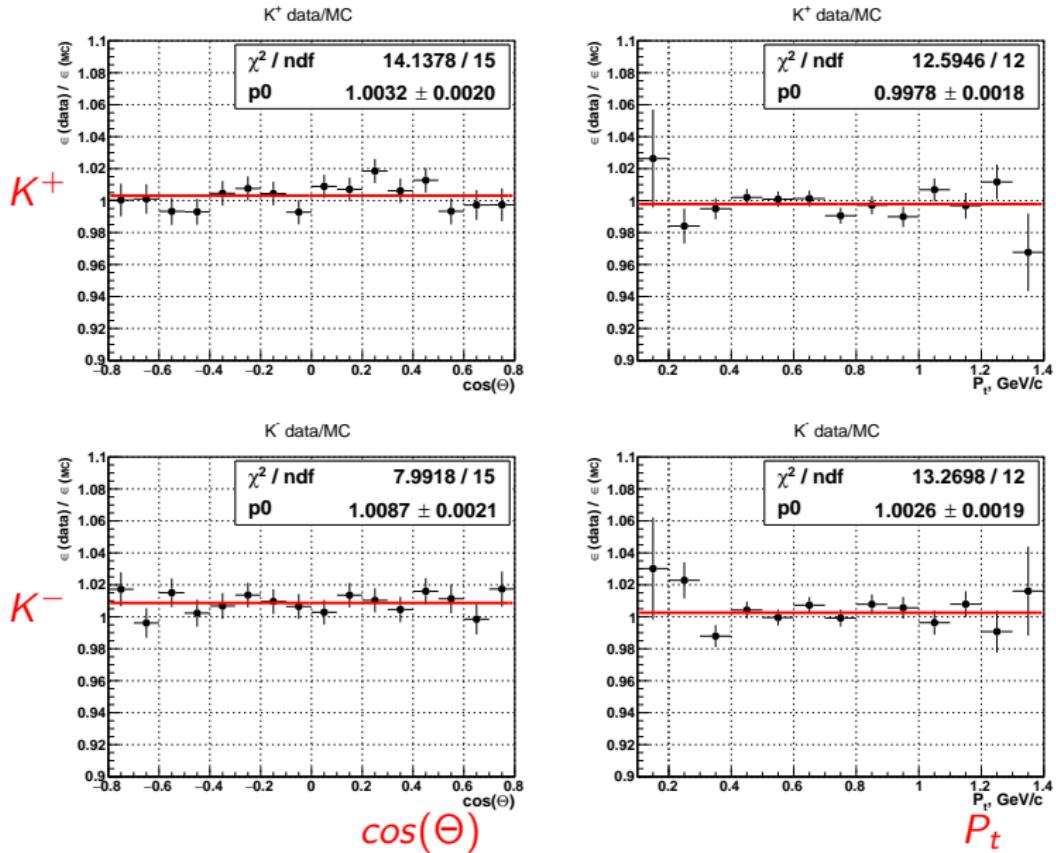


Pions: $a + (b/P_t)^3$



- ✓ These corrections have been already applied for calculations of selection efficiencies for $\psi(3686) \rightarrow \pi^+ \pi^- J/\psi$ and $J/\psi \rightarrow \phi \eta$ shown above

Kaons: $\epsilon_{DATA}/\epsilon_{MC}$ in 2012 after corrections



Conclusion

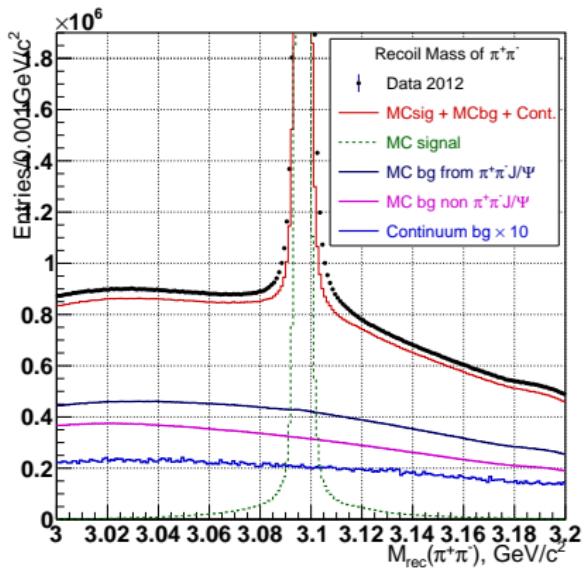
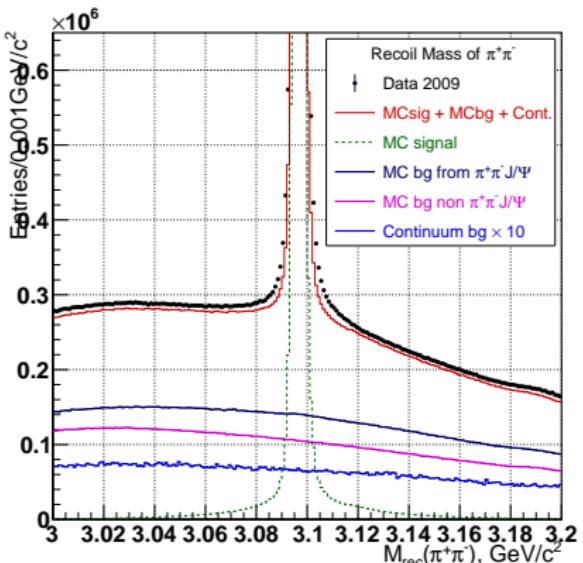
- We measured the branching fraction of $J/\psi \rightarrow \phi\eta$:
 $(8.1 \pm 0.4) \times 10^{-4}$ for data 2009
 $(8.5 \pm 0.3) \times 10^{-4}$ for data 2012
- We continue the work for estimation of systematic uncertainties
- Memo in the process of preparation

prospective result

- We got 0.24×10^{-4} cumulative statistical error
- We expect $\sim 0.2 \times 10^{-4}$ systematic error
- Total error will be $\sim 0.31 \times 10^{-4}$ (current PDG average is 0.8×10^{-4})

Backup slides

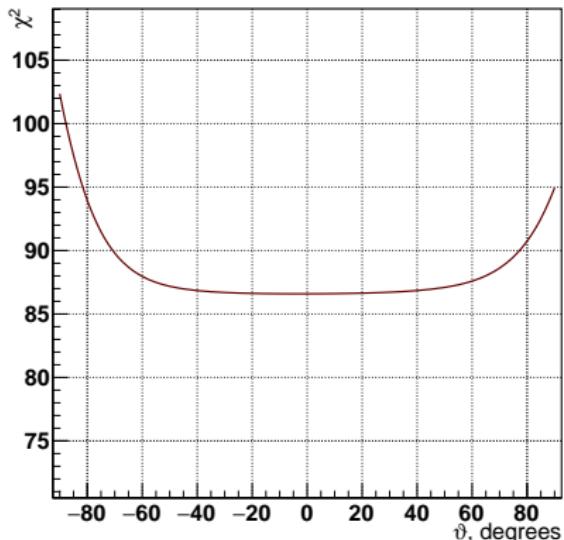
Recoil mass of $\pi^+\pi^-$: data vs MC



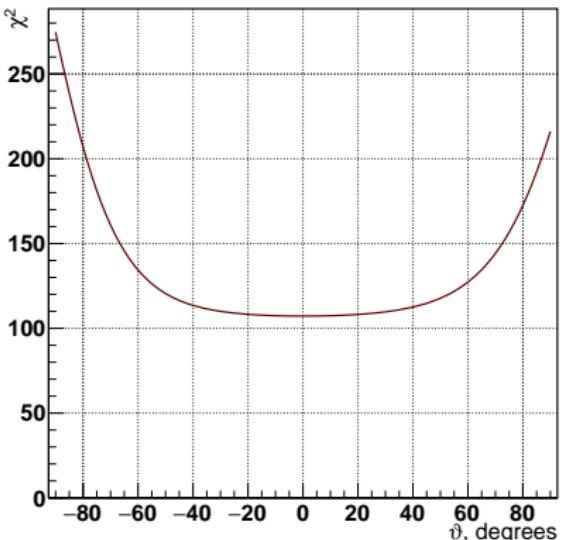
- The pictures are in linear scale and zoomed to show the tails of MC signal distribution J/ψ in our selection

Scan for mixing angle

Data 2009



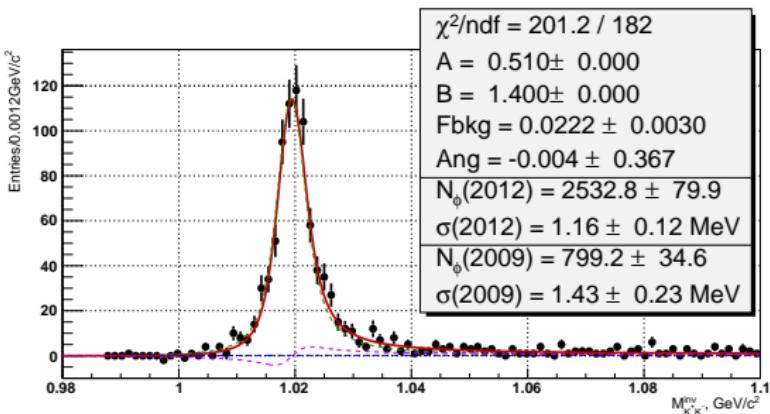
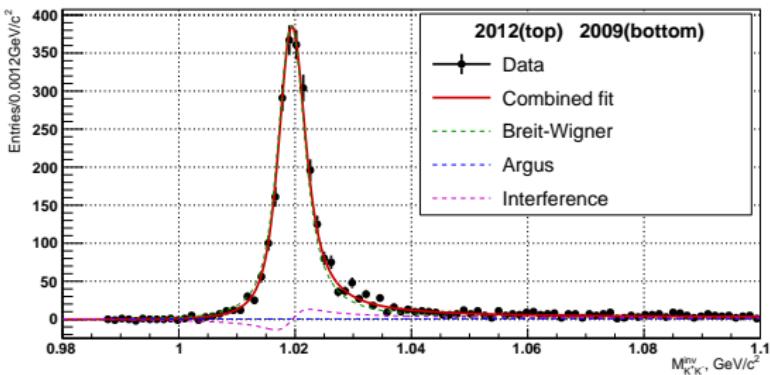
Data 2012



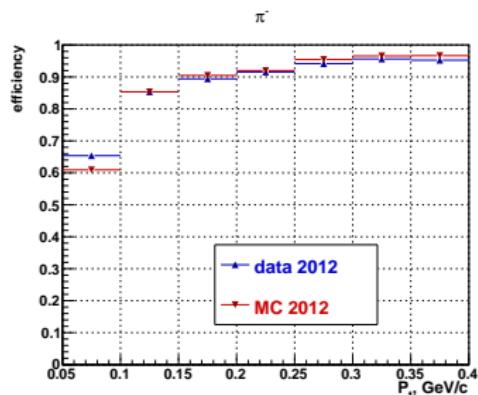
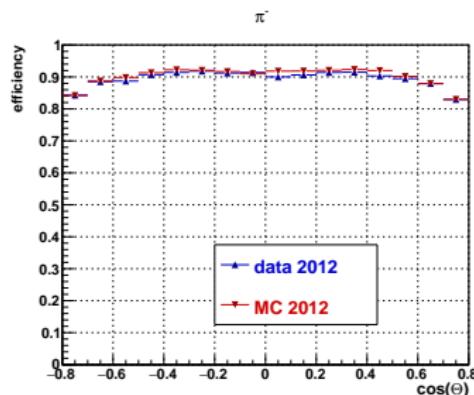
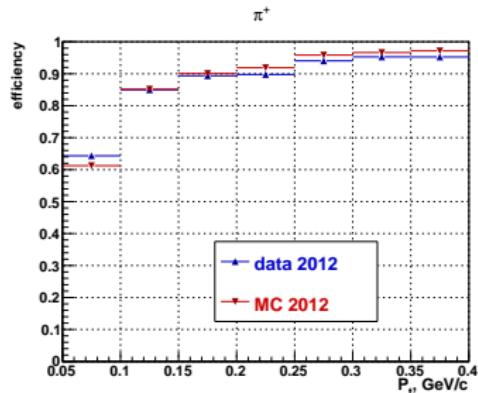
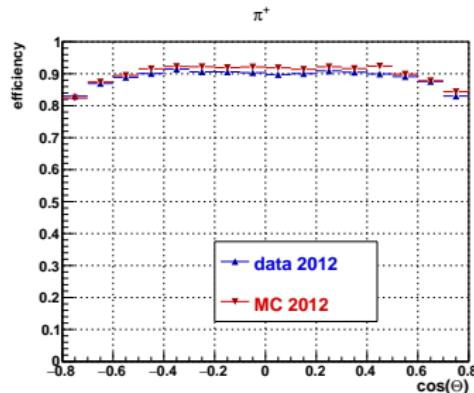
- the angle is fixed at a specific value, a fit was performed and the χ^2 of the fit is displayed
- zero angle is preferred for both data periods

Combined fit of $M_{K^+K^-}^{inv}$ data

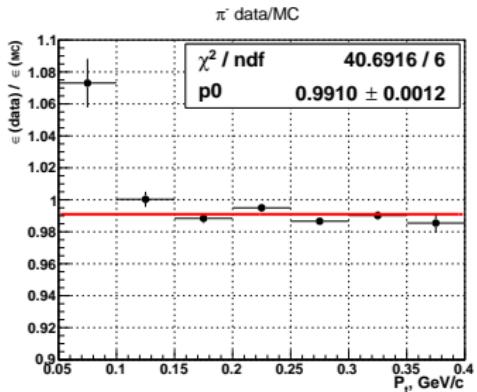
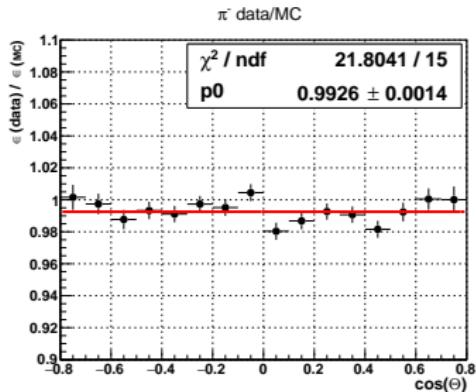
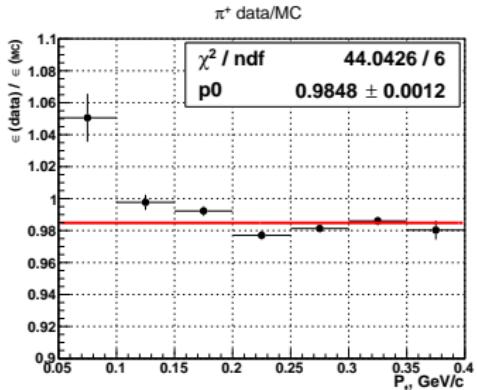
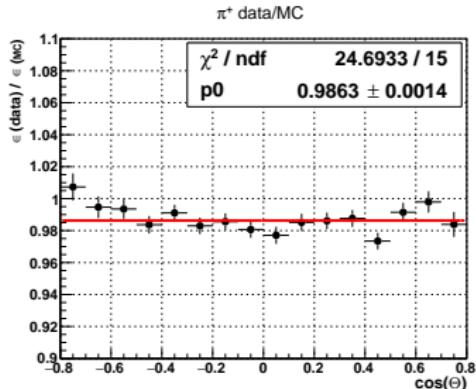
- parameters A and B are fixed
- almost the same quality of the fit:
 $\chi^2/ndf = 1.1$
- errors of N_ϕ reduced by $\sim 10\%$



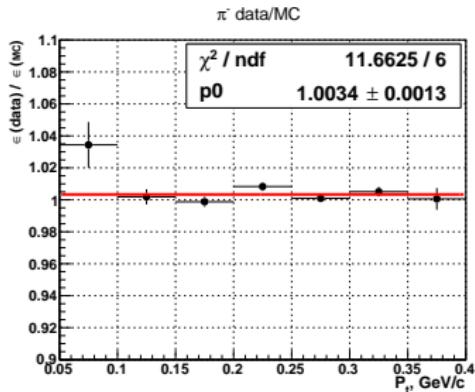
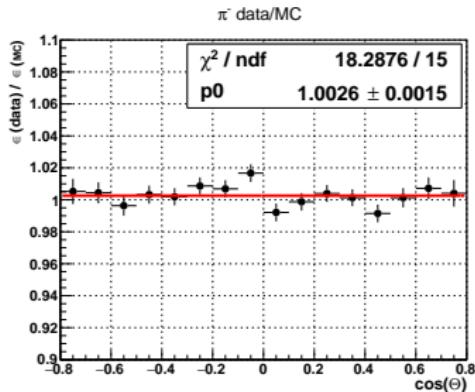
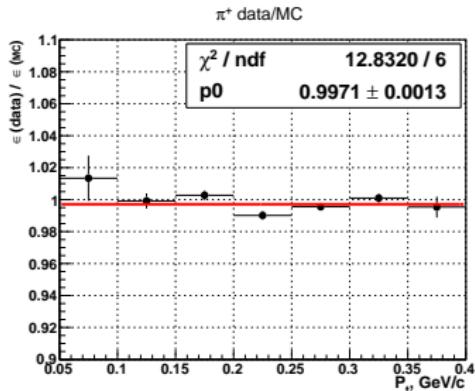
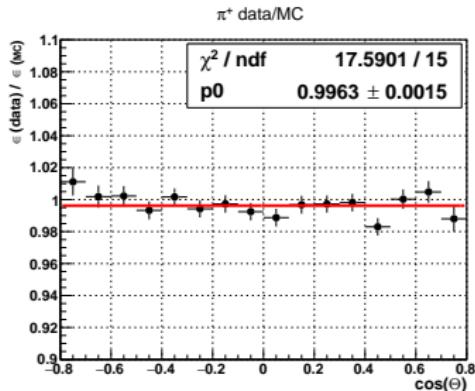
Pions: reconstruction track efficiency in 2012



Pions: $\epsilon_{DATA}/\epsilon_{MC}$ in 2012

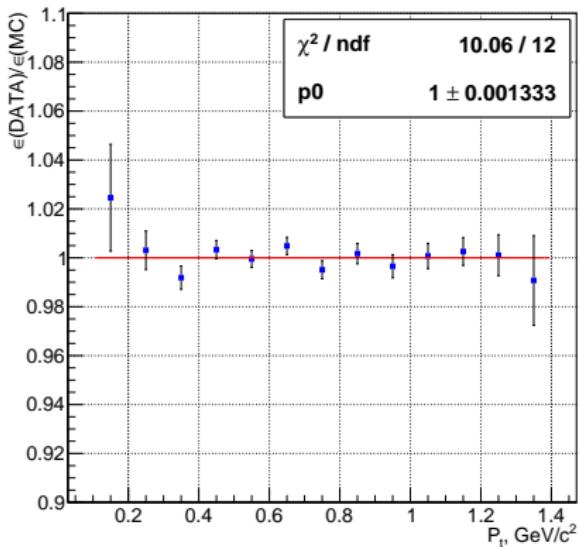


Pions: $\epsilon_{\text{DATA}}/\epsilon_{\text{MC}}$ in 2012 after corrections



Check after efficiency corrections in 2012

Kaons: chebyshev polynomials



Pions

