

# Kinematic reconstruction of the $W$ mass and width at FCC-ee

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On behalf of the FCC-ee WG2 working group  
CEPC workshop

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FCC-ee  
FCC-hh : 100 TeV  
Option : FCC-he

Z	WW	HZ	$t\bar{t}$
$\sim 91$ GeV	$\sim 160$ GeV	$\sim 240$ GeV	$\sim 350-365$ GeV



Detectors  $e^+e^-$ : **CLD** and **IDEA**

# WW factory

$$\sqrt{s} = 160 \text{ GeV}, L = 12 \text{ ab}^{-1}$$

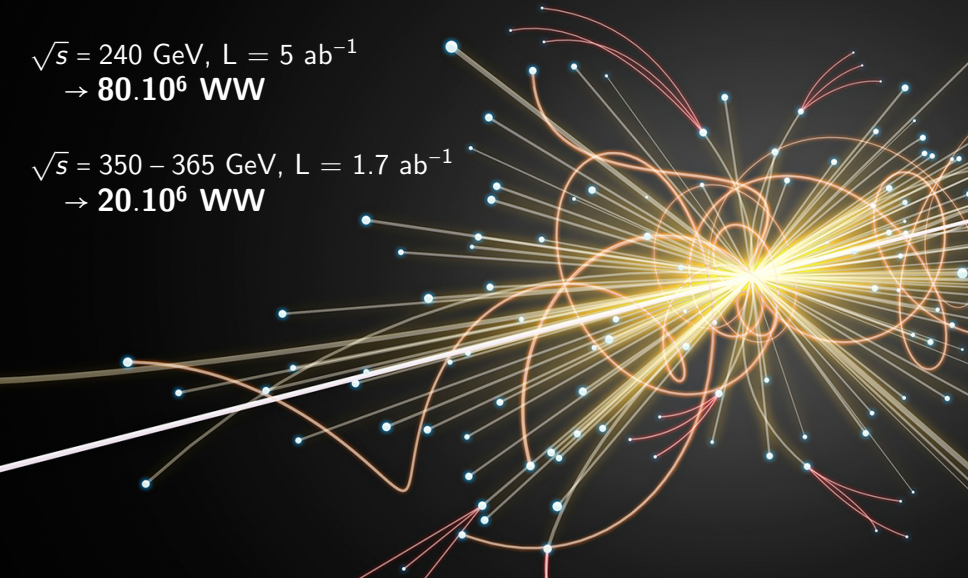
→ **60.10<sup>6</sup> WW**

$$\sqrt{s} = 240 \text{ GeV}, L = 5 \text{ ab}^{-1}$$

→ **80.10<sup>6</sup> WW**

$$\sqrt{s} = 350 - 365 \text{ GeV}, L = 1.7 \text{ ab}^{-1}$$

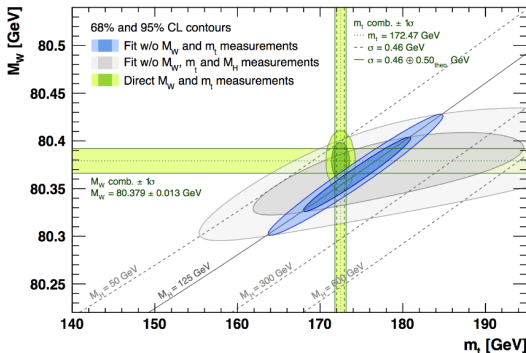
→ **20.10<sup>6</sup> WW**



## WW diboson physics at FCC-ee

- Measurements of the **W mass and width** directly and with threshold scan;
  - W partial widths;
  - Strong coupling constant;
  - CKM matrix;
  - Gauge self-couplings ...
- ... **with unprecedented accuracy**

# W mass measurement

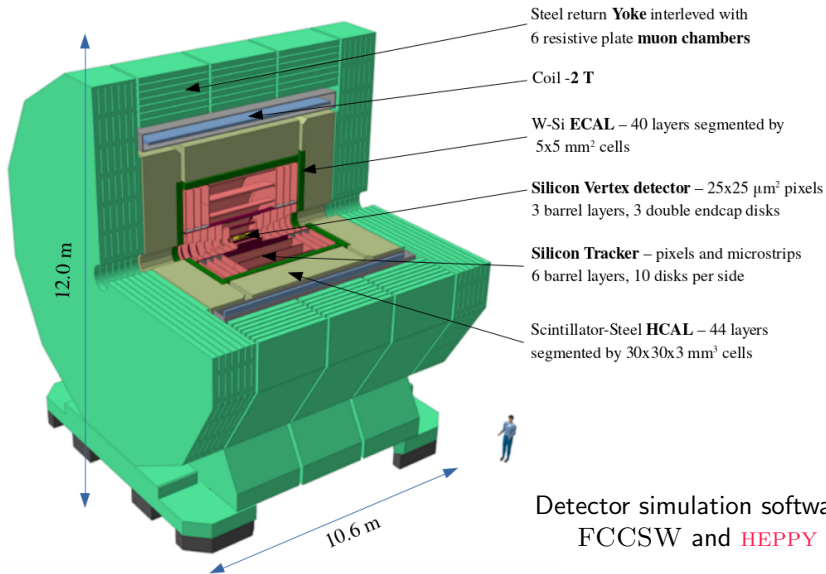


Precise relation between  $M_W$ ,  $M_H$ ,  $M_t$  is a **crucial test** of the internal consistency of SM and failure might reveal **new physics**.

## Methods

- At WW threshold;
- **Direct determination**

# CLIC-Like Detector: CLD



More information in: [FCC CDR v2](#)

# Direct reconstruction of $M_W$ and $\Gamma_W$

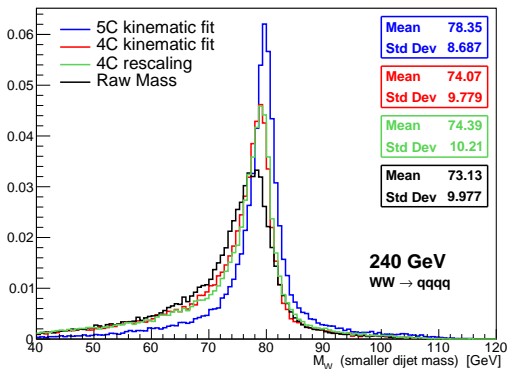
## Hadronic decay channel $WW \rightarrow q\bar{q}q\bar{q}$

Study at 162.6 GeV, 240 GeV and 365 GeV

- PYTHIA v8.24 simulation
- Reconstruction with HEPPY (CLD detector, DURHAM algorithm)

W mass estimators :

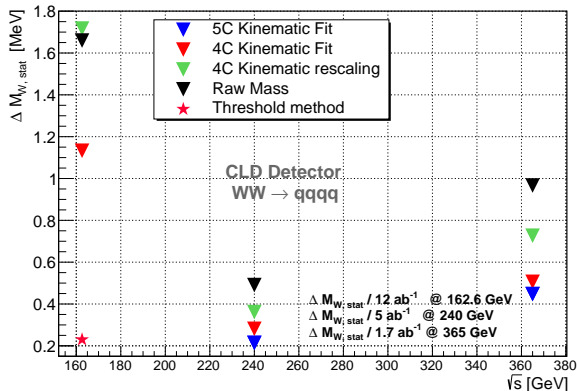
- **Raw mass**
- **4C jets momenta rescaling**
- **Kinematic fit** with energy-momentum conservation (4C) and W masses equality (5C)



# Direct reconstruction of $M_W$ and $\Gamma_W$

## Hadronic decay channel $WW \rightarrow q\bar{q}q\bar{q}$

Statistical uncertainty estimated with a **binned maximum likelihood fit** on the reconstructed  $M_W$  distributions, using **templates** with different nominal W mass (width) values.



@162.6 GeV  
 $\Delta\Gamma_W(4C) = 1.1 \text{ MeV}$

@240 GeV  
 $\Delta\Gamma_W(5C) = 0.47 \text{ MeV}$

@365 GeV  
 $\Delta\Gamma_W(5C) = 1 \text{ MeV}$

Mass and width uncertainties  
evaluated **independently**

Full FCC-ee luminosity

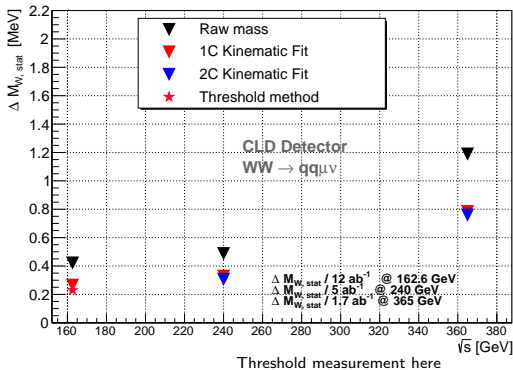
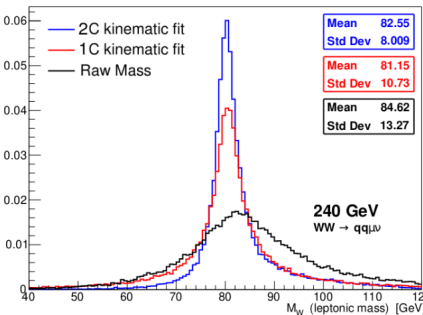


# Direct reconstruction of $M_W$ and $\Gamma_W$

## Semi-leptonic decay channel $WW \rightarrow q\bar{q}l\nu$

Study at 162.6 GeV, 240 GeV and 365 GeV

Only the muon decay



@162.6 GeV  $\Delta\Gamma_W(1C) = 0.35 \text{ MeV}$

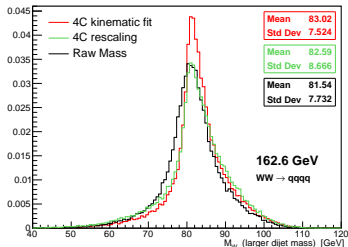
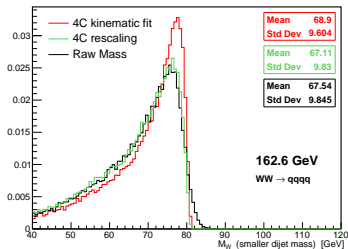
@240 GeV  $\Delta\Gamma_W(2C) = 0.68 \text{ MeV}$

@365 GeV  $\Delta\Gamma_W(2C) = 1.56 \text{ MeV}$

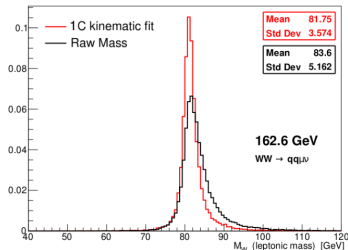
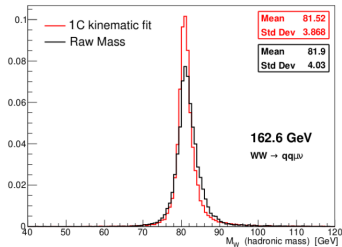
Full FCC-ee luminosity

# Direct reconstruction of $M_W$ and $\Gamma_W$ at threshold

Hadronic channel



Semi-leptonic channel



Direct reconstruction can be used to extract  $W$  mass and width at threshold

# W mass and width statistical uncertainties

Table: Hadronic decay

$\sqrt{s}$ [GeV]	$\sigma_{M_W}$ [MeV/c <sup>2</sup> ]			$\sigma_{\Gamma_W}$ [MeV/c <sup>2</sup> ]		
	162.6	240	365	162.6	240	365
Luminosity ( $ab^{-1}$ )	12	5	1.7	12	5	1.7
Raw Mass	1.66	0.49	0.97	1.44	1.10	1.71
4C rescaling	1.72	0.36	0.73	1.53	0.77	1.48
4C fit	<b>1.13</b>	0.28	0.5	<b>1.1</b>	0.58	<b>0.95</b>
5C fit		<b>0.21</b>	<b>0.44</b>		<b>0.47</b>	1.0

With threshold method  $\sigma_{M_W} = \mathbf{0.23}$  MeV

Threshold measurement [here](#)

Full FCC-ee luminosity

Table: Semi-leptonic decay

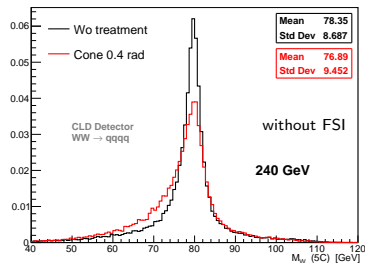
$\sqrt{s}$ [GeV]	$\sigma_{M_W}$ [MeV/c <sup>2</sup> ]			$\sigma_{\Gamma_W}$ [MeV/c <sup>2</sup> ]		
	162.6	240	365	162.6	240	365
Luminosity ( $ab^{-1}$ )	12	5	1.7	12	5	1.7
Raw Mass	0.42	0.49	1.19	0.39	0.87	1.94
1C fit	<b>0.26</b>	0.33	0.78	<b>0.35</b>	<b>0.59</b>	<b>1.36</b>
2C fit		<b>0.31</b>	<b>0.75</b>		0.68	1.56

# Systematic uncertainties

Main sources of systematic uncertainties at LEP2:  
arXiv:1302.3415

Source	Systematic Uncertainty in MeV			
	on $m_W$			on $\Gamma_W$
	$q\bar{q}\ell\nu_\ell$	$q\bar{q}q\bar{q}$	Combined	
ISR/FSR	8	5	7	6
Hadronisation	13	19	14	40
Detector effects	10	8	9	23
LEP energy	9	9	9	5
Colour reconnection	—	35	8	27
Bose-Einstein Correlations	—	7	2	3
Other	3	10	3	12
Total systematic	21	44	22	55
Statistical	30	40	25	63
Statistical in absence of systematics	30	31	22	48
Total	36	59	34	83

FSI simulated with PYTHIA (SKI/SKII).  
 $\delta M_{W,FSI}$  reduced using a cone  
(0.4 rad) on jets



$\sqrt{s}$ [GeV]	162.6		240		365	
$\delta M_{FSI}$ [MeV]	standard	cone	standard	cone	standard	cone
SKI	14.6	7.5	23.9	11.5	32.2	17.5
SKII	7.9	3.8	12.1	6.0	14.7	8.3
BEC	3.1	1.8	5.9	2.1	9.9	5.5

$\Delta M_{W,stat}$  is degraded with the cone by a few percents at threshold and 10-15% above.

Background processes studied at **162.6 GeV, 240 GeV and 365 GeV** (if possible):

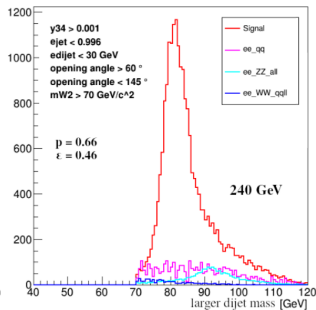
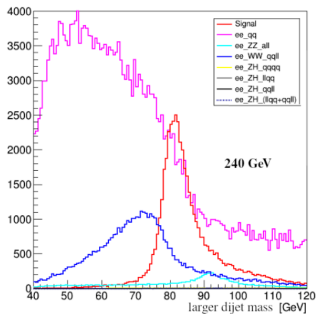
$$e^+e^- \rightarrow q\bar{q}(\gamma),$$

$$e^+e^- \rightarrow WW \rightarrow q\bar{q}ll,$$

$$e^+e^- \rightarrow ZZ \rightarrow 4f,$$

$$e^+e^- \rightarrow ZH \rightarrow q\bar{q}q\bar{q},$$

$$e^+e^- \rightarrow ZH \rightarrow q\bar{q}ll.$$



▷ Effective background rejection above threshold

▷  $\Delta M_W(5C) = 0.27 \text{ MeV}$  @240 GeV ( $5ab^{-1}$ ) in presence of background (0.21 MeV without)

Bkg rejection increases with energy:

@162.6 GeV:  $p = 0.41$ ,  $\epsilon = 0.37$ ;

@365 GeV:  $p = 0.85$ ,  $\epsilon = 0.36$

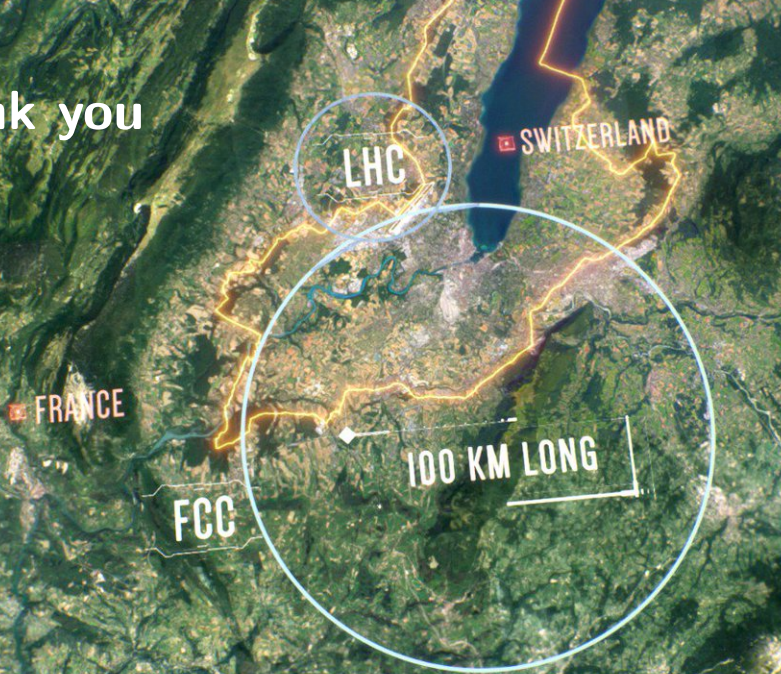
Sofiane Lablack, Precise measurement of the W boson mass at the  $e^+e^-$  future circular collider (FCC-ee), Master Thesis, 2019

# Conclusion

The **amount of W-pairs** at different centre-of-mass energies planned at **FCC-ee** presents a huge potential for the W physics measurements.

- Direct  $M_W$  and  $\Gamma_W$  measurements at threshold and above is possible at FCC-ee. Yielding to statistical **precision below MeV-level** ( $\Delta M_W = 210 \text{ keV}$  @240 GeV for hadronic channel and  $\Delta M_W = 260 \text{ keV}$  @162.6 GeV for semi-leptonic channel).
- Measurement of the centre-of-mass energy with **good precision** (2 MeV @365 GeV) for energies above the WW threshold, where the resonant depolarisation cannot be used (more information [here](#)).
- Ultimately a simultaneous fit of WW, ZZ and  $Z\gamma$  events could be performed to extract  $m_W/m_Z$  with potential **large cancellations of systematic uncertainties**

Thank you  
谢谢

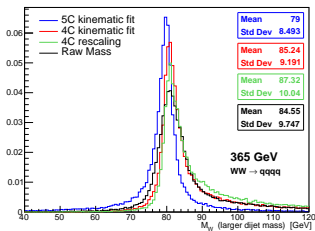
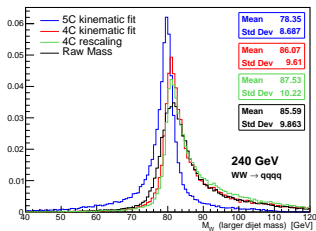
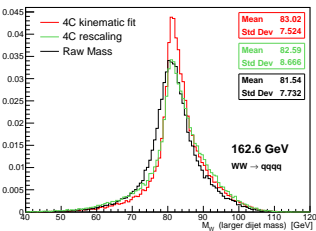
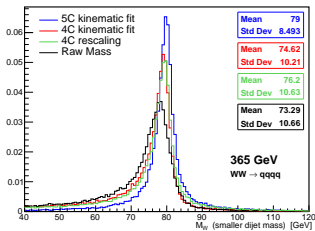
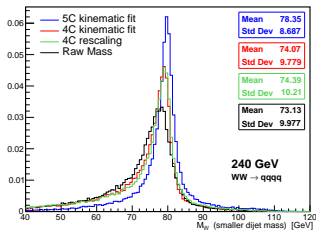
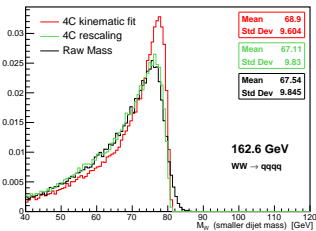


A close-up photograph of a condensation-covered light bulb. The bulb is the central focus, its glass surface glistening with droplets of water. It is positioned in the lower right quadrant of the frame. The background is a soft, out-of-focus bokeh of warm, golden-yellow lights, likely from a string of Christmas lights. The overall mood is cozy and evocative. The text "BACK-UP" is overlaid in the upper right area in a clean, white, sans-serif font.

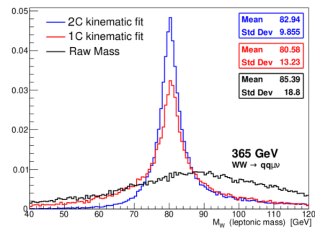
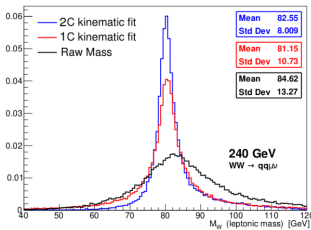
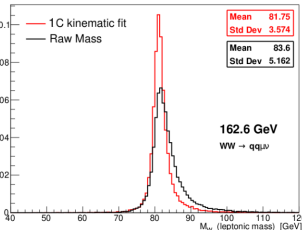
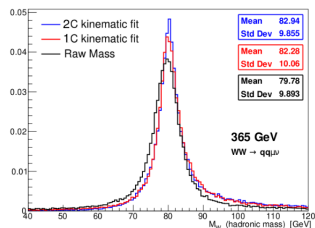
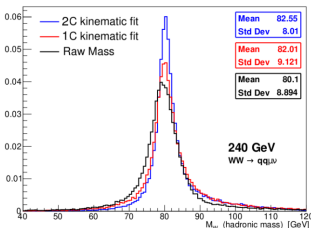
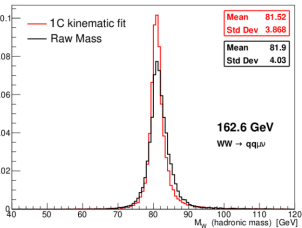
BACK-UP



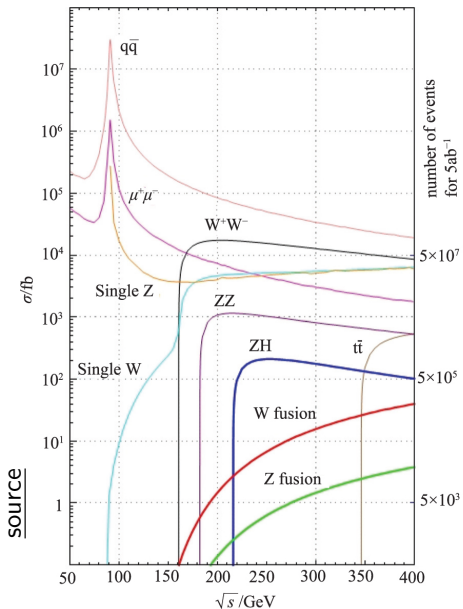
# W mass distributions - Hadronic channel



# W mass distributions - Semi leptonic channel



# Cross-section for different processes in lepton collisions

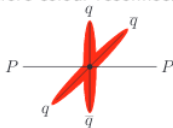


All processes with larger or relatively close cross-section to the WW cross-section are potential backgrounds for the WW decay study.

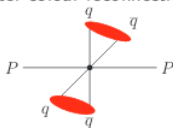
# Colour Reconnection - Models

$$e^+ e^- \rightarrow WW \rightarrow q_1 \bar{q}_2 q_3 \bar{q}_4$$

Before colour reconnection



After colour reconnection?



Jesper Roy Christiansen, July 23, 2015,  
EPS HEP, Vienna

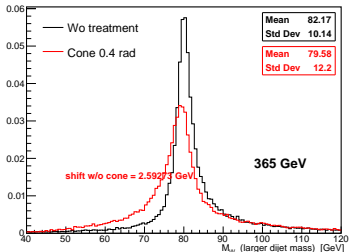
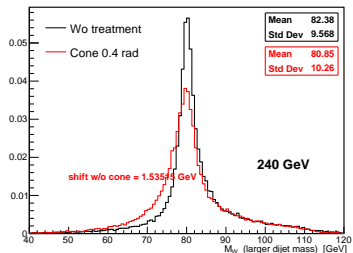
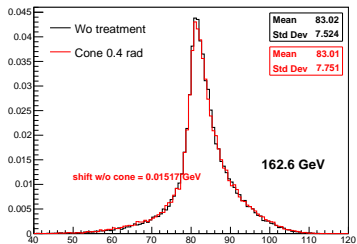
Color Reconnection (CR) : interaction between partons of the two  $W$ s

Because  $WW$  separation in phase-space is smaller than the typical distance scale of hadronisation:  $(q_1 \bar{q}_4)$  and  $(q_3 \bar{q}_2)$

Models in PYTHIA for  $e^+ e^-$  collisions are based on string hadronisation.

- SK1 : string = cylindrical bag. Colour reconnection probability proportional to the integrated overlap between cylinders.
- SK2 : string = vortex line. Colour reconnection if the cores are crossing.

# Cone reconstruction effect on W mass resolution



The loss of particle information degrades the resolution by 2.9% at 162.6 GeV, 6.7% at 240 GeV and 16.9% at 365 GeV

# Cone effect on $\Delta M_{W,stat}$

## Full FCC-ee luminosity

$\sqrt{s}$ [GeV]	162.6		240		365	
$\Delta M_{W,stat}$ [MeV]	standard	cone	standard	cone	standard	cone
woFSI	1.14	1.18	0.215	0.228	0.463	0.564
SKI	1.18	1.21	0.225	0.244	0.478	0.55
SKII	1.17	1.19	0.218	0.237	0.467	0.539
BEC	1.17	1.18	0.224	0.236	0.461	0.58

$\Delta M_{W,stat}$  is degraded with the cone by few percent at threshold and 10-15% above.