

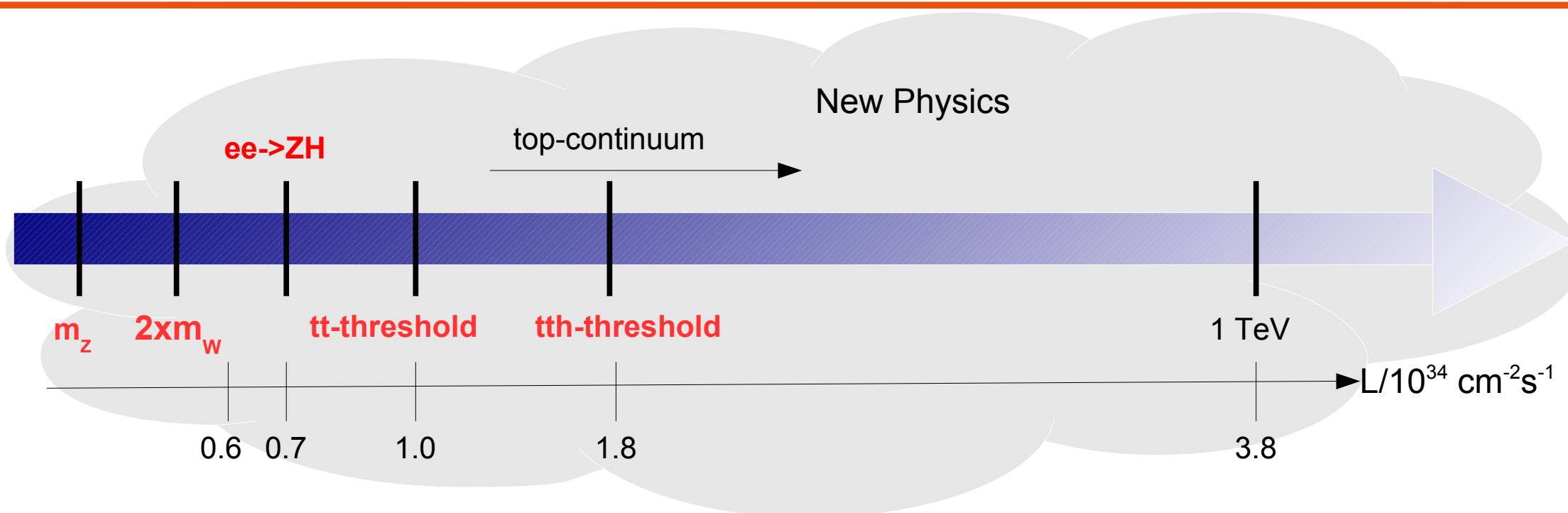
# ILC at the Z-Pole - GigaZ

Roman Pöschl



R.P. Is indebted to François Richard for most of the results presented here  
We reuse in part results of studies made by K. Moenig for TESLA report

CEPC 2019 Beijing China November 2019



All Standard Model particles within reach of planned  $e^+e^-$  colliders

High precision tests of Standard Model over wide range to detect onset of New Physics

Machine settings can be “tailored” for specific processes

- Centre-of-Mass energy
- Beam polarisation (straightforward at linear colliders)

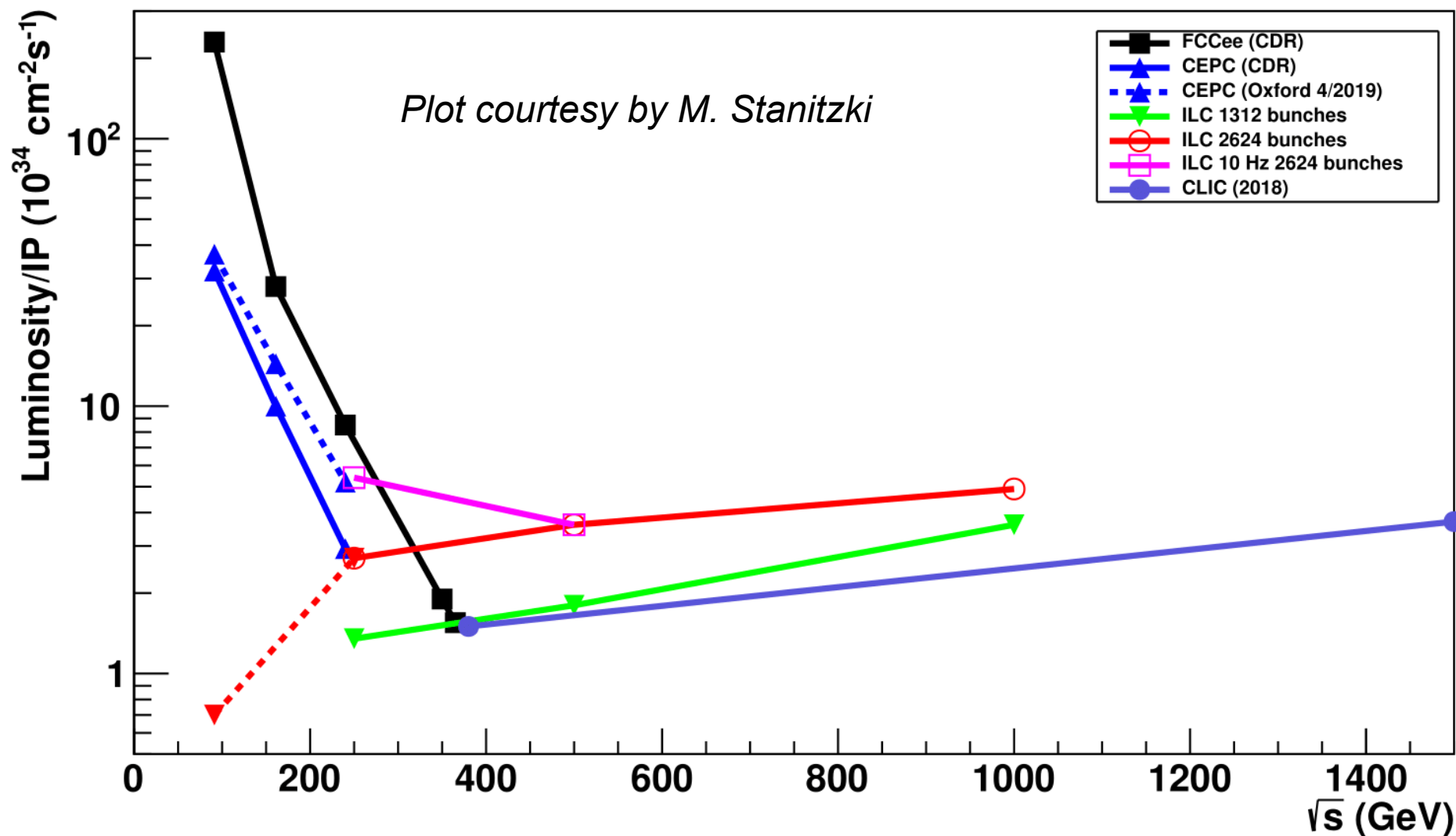
$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

**Background free** searches for BSM through beam polarisation

## e<sup>+</sup>e<sup>-</sup> Higgs Factory Luminosity Comparisons

Updated 15/04/2019

*Plot courtesy by M. Stanitzki*



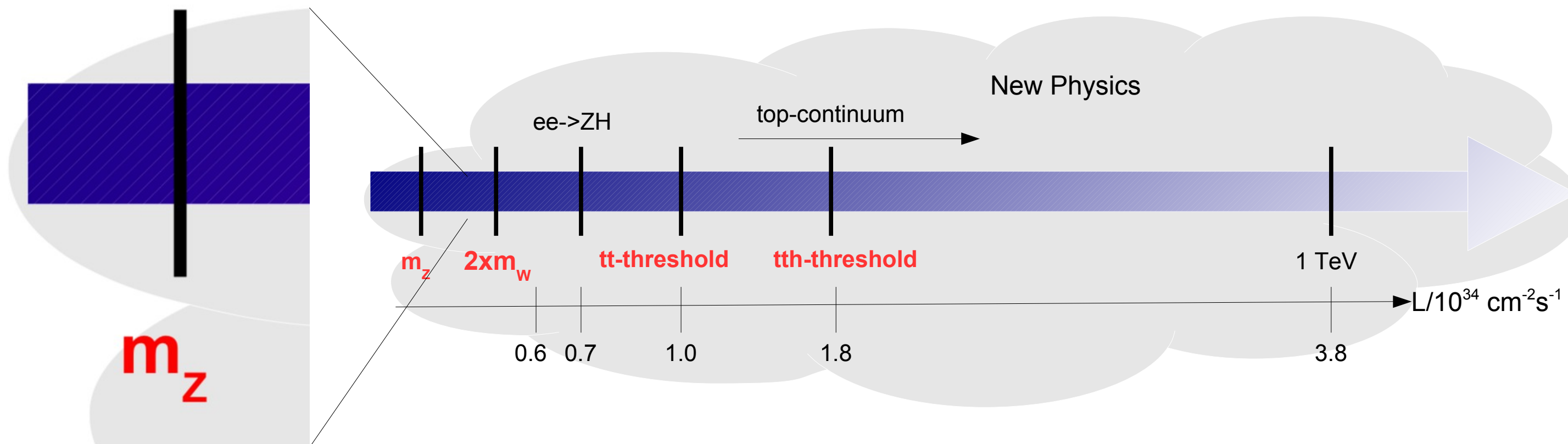
High energies ~above tt-threshold  
Domain of linear colliders

Low energies e.g. Z-pole  
Domain of circular machines  
•However, see later ...

Transition region, i.e. HZ threshold  
... not so clear

Comparable numbers for all proposals

Linear colliders are more versatile  
to test chiral theory due to polarised  
beams



- ILC is more than “just” a Higgs Factory
- Many new physics models have impact on electroweak processes e.g. 2f processes
- Z pole is “pure” Z => Therefore new physics (or not) due to Z has to be pinned down
- Many questions at Grenada to ILC capabilities on the pole
  - Some answers were at hand (arXiv: 1905.00220)

*arXiv:1506.07830*

	$\text{sgn}(P(e^-), P(e^+)) =$				sum
	$(-, +)$	$(+, -)$	$(-, -)$	$(+, +)$	
luminosity $[\text{fb}^{-1}]$	40	40	10	10	
$\sigma(P_{e^-}, P_{e^+})$ [nb]	83.5	63.7	50.0	40.6	
$Z$ events $[10^9]$	2.4	1.8	0.36	0.29	4.9
hadronic $Z$ events $[10^9]$	1.7	1.3	0.25	0.21	3.4

=230xLEP, 8500xSLC

- Accelerator scenario  $3.7\text{Hz}@M_Z/2 + 3.7 \text{ Hz}@125 \text{ GeV}$  to produce positrons
- With 2625 bunches an instantaneous luminosity of  $5 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1} \Rightarrow 100 \text{ fb}^{-1}$  in 1.3 years after lumi upgrade
- More possible by improved damping rings and BDS system
- See arxiv: 1908.08212 for a recent revision

Copied from deBlas, Higgs-Hunting 2016

Precise measurements of W&Z properties taken at e+e- colliders

$$M_Z, \Gamma_Z, \sigma_{had}^0, \sin^2 \theta_{eff}^{lept}, P_{\tau}^{Pol}, A_f, A_{FB}^{0,f}, R_f^0$$

Z-Pole observables  
SLD/LEP  
0.002 - O(1%)

$$M_W, \Gamma_W$$

W-observables  
LEP2  
0.02 - O(1%)

ILC (Wilson, Singer-Anguino@LCWS19):  
 $\Delta m_W (MeV) = 2.4(stat.) \oplus 3.2(syst.) \oplus 0.8(\sqrt{s}) \oplus \text{theory}$   
width:  $\Delta \Gamma_W = 3.2 MeV$

Tevatron/LHC but in future also from e+e- colliders

$$M_W, \Gamma_W$$

0.02-O(1%)

$$m_t$$

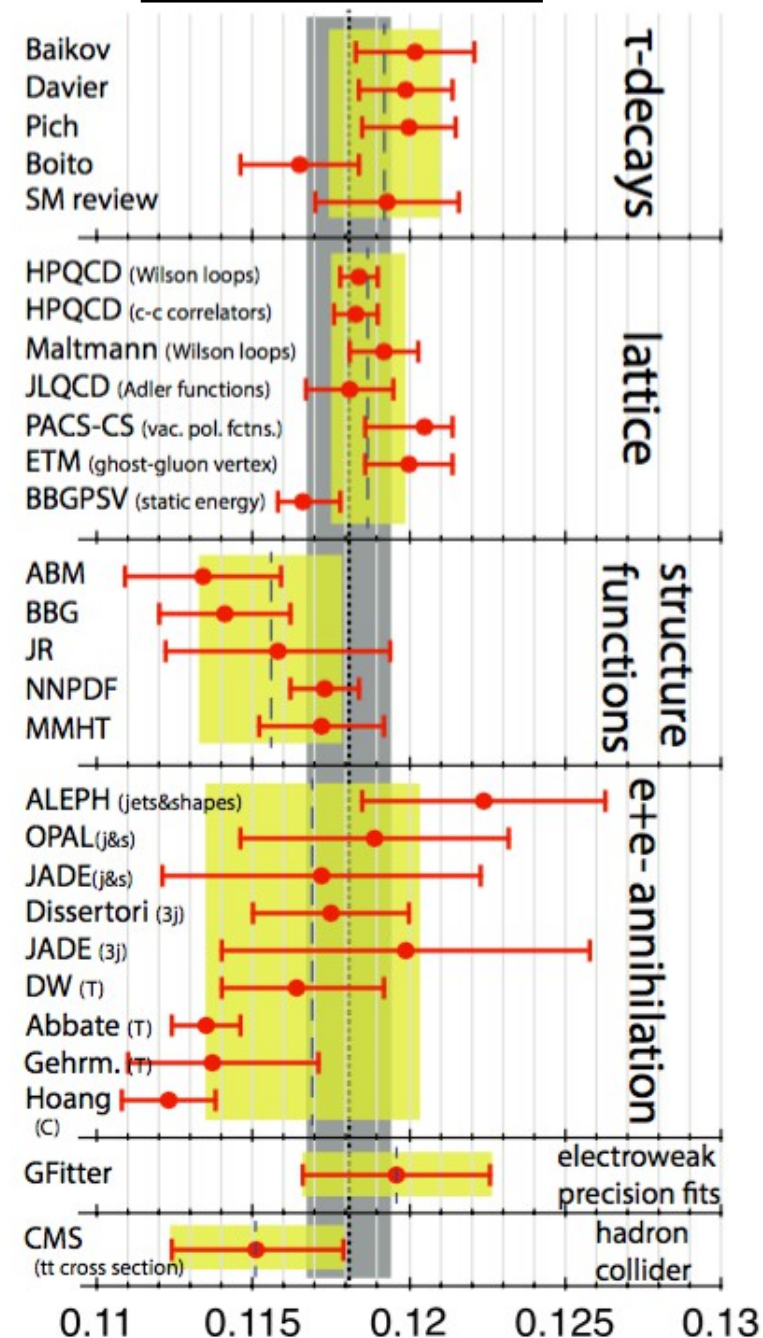
0.4%

$$M_H$$

0.2%

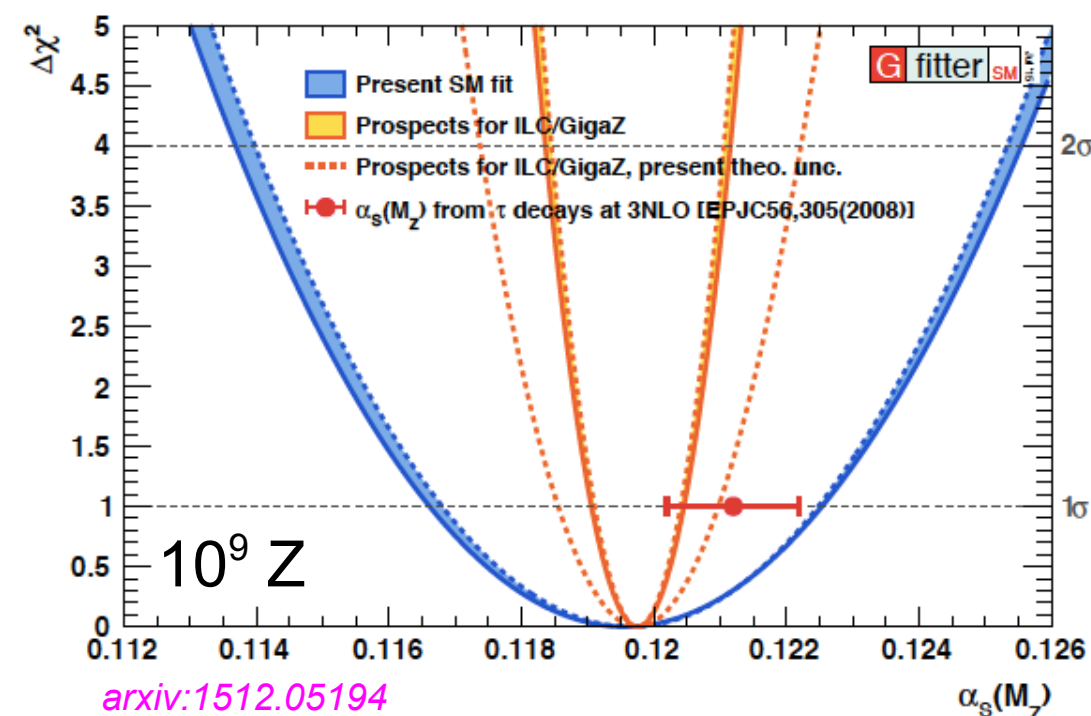


## Current status



Dominated by lattice QCD

## Prospects Z-running



Slide made  
in 2016!

Electroweak fit with updated EWPO and theory uncertainties

$$\delta \alpha_s(M_Z) \sim 0.0007 \text{ for } 10^9 Z$$

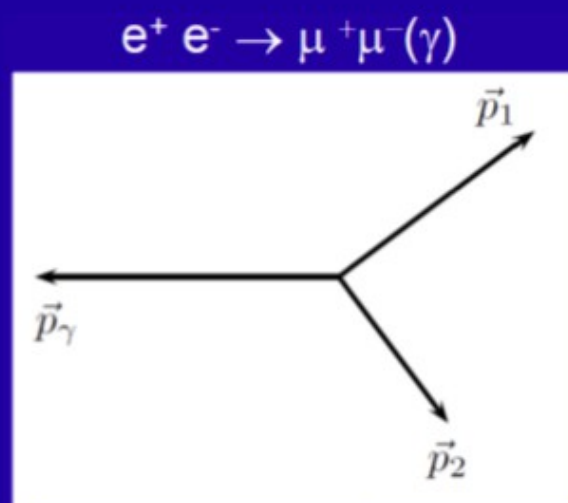
$$\delta \alpha_s(M_Z) \sim 0.0003(16) \text{ for } 10^{12} Z$$

## Prospects Lattice

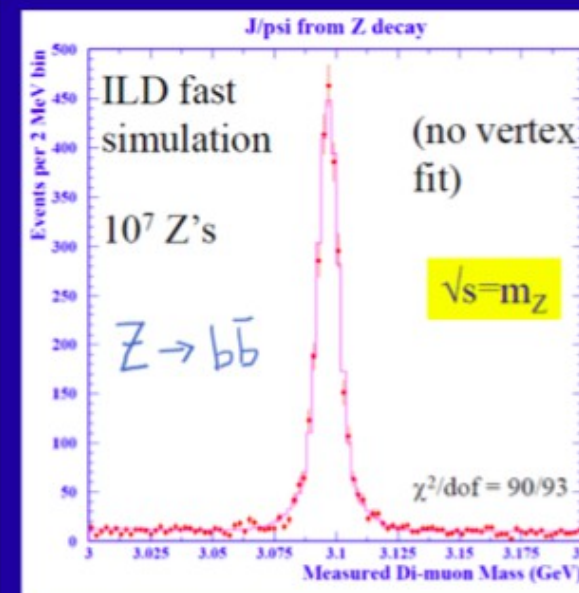
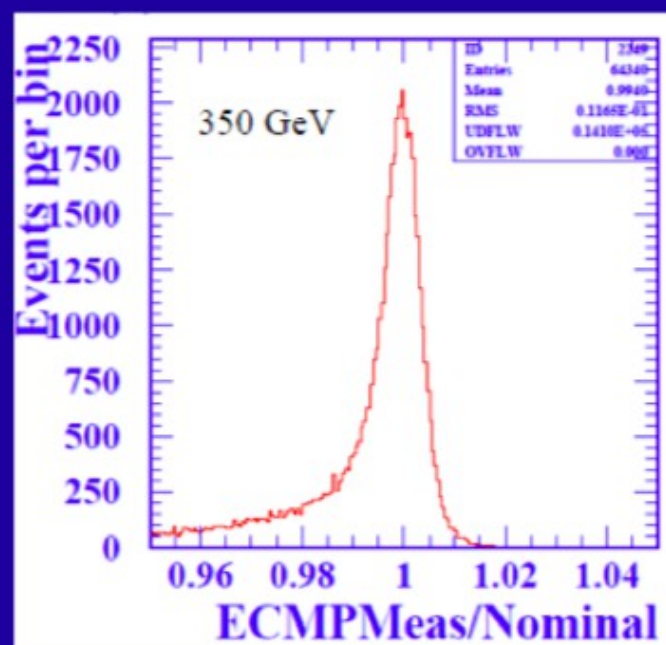
$$\delta \alpha_s(M_Z) \sim 0.0003$$

- 1) Scans around Z pole and measurement in upstream and downstream beam-spectrometers
- 2) In situ measurement using superb momentum resolution of ILC Detectors (G. Wilson)

- Critical input to measurements of  $m_t$ ,  $m_W$ ,  $m_H$ ,  $m_Z$ ,  $m_X$  using threshold scans.
- Standard precision  $O(10^{-4})$  for  $m_t$  straightforward.
- Targeting precision  $O(10^{-5})$  for  $m_W$ ,  $m_Z$ 
  - Muon momenta based strategy looks feasible



Use muon momenta.  
Measure  $E_1 + E_2 + |\mathbf{p}_{12}|$  as an  
estimator of  $\sqrt{s}$



$$\Rightarrow \Delta M_Z = 0.5 \text{ MeV}$$

*2.1 MeV currently*

$$\Delta \Gamma_Z = 0.33 \text{ MeV}$$

*2.3 MeV currently*

- The Z-mass and width is (as far as I can see) the among the few parameters on which a LC cannot compete with a CC
- Is this casted in stone?



$$\mathcal{A}_e = \frac{(g_{e_L}^Z)^2 - (g_{e_R}^Z)^2}{(g_{e_L}^Z)^2 + (g_{e_R}^Z)^2} = \frac{2g_{eV}/g_{eA}}{1 + (g_{eV}/g_{eA})^2} \quad \text{with } g_{eV}/g_{eA} = 1 - 4 \sin^2 \theta_{\text{eff}}^\ell.$$

## How to determine $\mathcal{A}_e$ ?

Left Right Asymmetry  
Requires polarised beams

$$A_{LR} = \frac{1}{|\mathcal{P}_{eff.}|} \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e$$

Available at LC

Using all hadronic decays of Z!!!

Forward backward asymmetry  
Has to assume lepton universality!!!

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \text{for } \mathcal{P}_e = 0.$$

Available at LC, CC  
Used e.g. in EPJC (2019) 79:474  
with  $f = \mu$

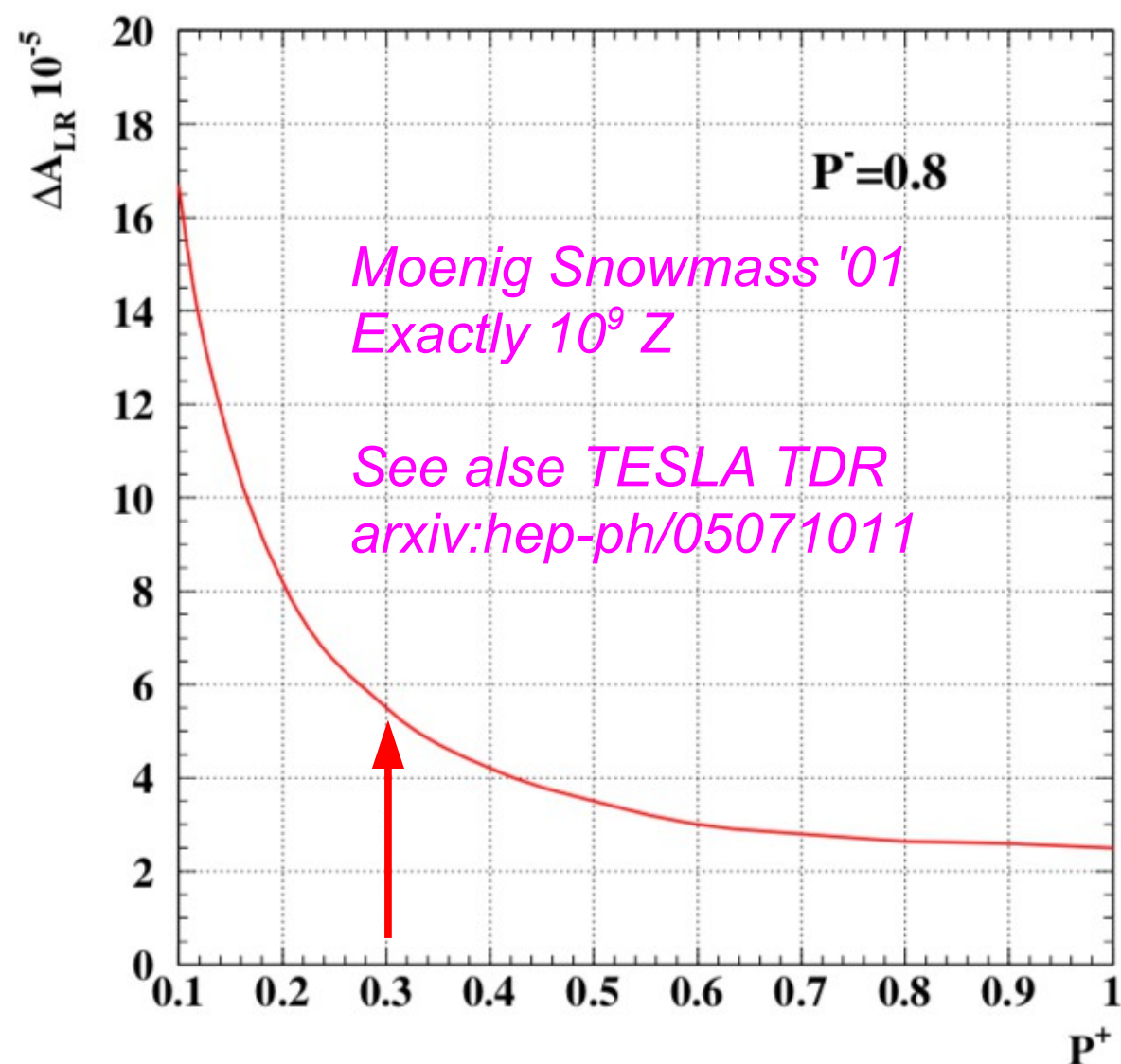
Final state polarisation (r,l)  
e.g. with  $\tau$

$$A_{FB}^{pol} = \frac{(\sigma_r - \sigma_l)_F - (\sigma_r - \sigma_l)_B}{(\sigma_r + \sigma_l)_F + (\sigma_r + \sigma_l)_B} = -\frac{3}{4} \mathcal{A}_e$$

Available at LC, CC

Beam polarisation is key: Remember SLC delivered most precise value of  $\sin^2 \theta_{\text{eff}}^\ell$  despite of 30 times less lumi

Blondel scheme: 
$$A_{LR} = \sqrt{\frac{(\sigma_{++} + \sigma_{-+} - \sigma_{+-} - \sigma_{--})(-\sigma_{++} + \sigma_{-+} - \sigma_{+-} + \sigma_{--})}{(\sigma_{++} + \sigma_{-+} + \sigma_{+-} + \sigma_{--})(-\sigma_{++} + \sigma_{-+} + \sigma_{+-} - \sigma_{--})}}$$



Blondel scheme independent of polarimeter precision

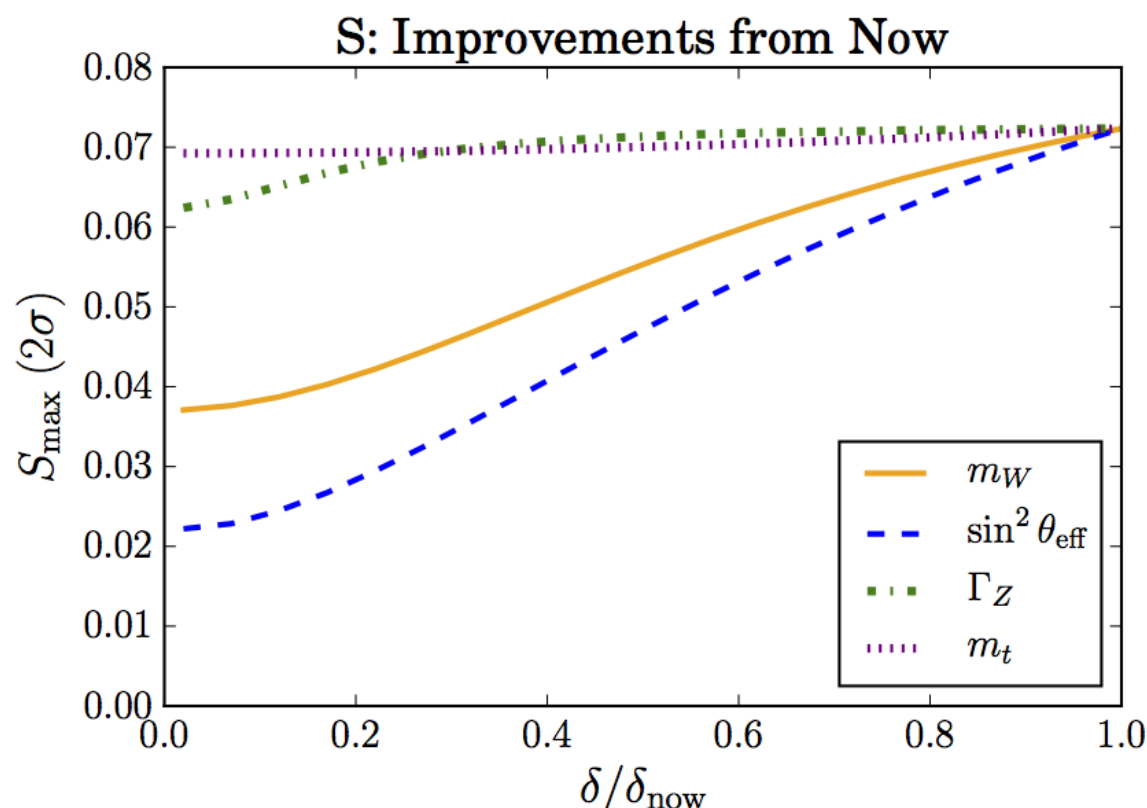
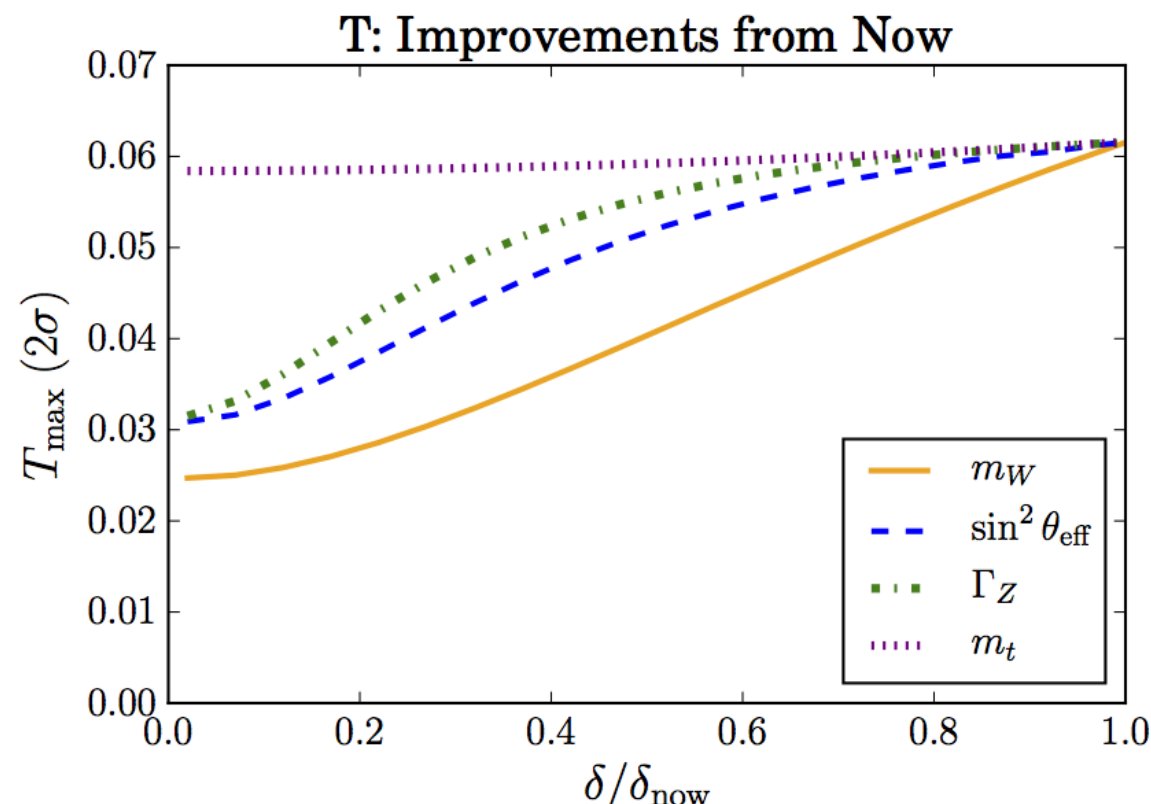
- Assumes perfect spin flip for polarised beams
- Residuals must be monitored by polarimeter
- Residual uncertainty of  $\Delta A_{LR} = 0.5 \times 10^{-4}$  seems possible
- The more positron polarisation the better (see backup)
- Don't forget energy dependency ( $dA_{LR}/d\sqrt{s} \sim 2 \times 10^{-5}/\text{MeV}$ )

Precision  $\Delta A_{LR} = 1 \times 10^{-4}$  is a realistic assumption for GigaZ

=>

$$\delta \sin^2 \theta_{\text{eff}}^{\ell} \sim 1.3 \cdot 10^{-5}$$

à la M. Reece 1609.03018

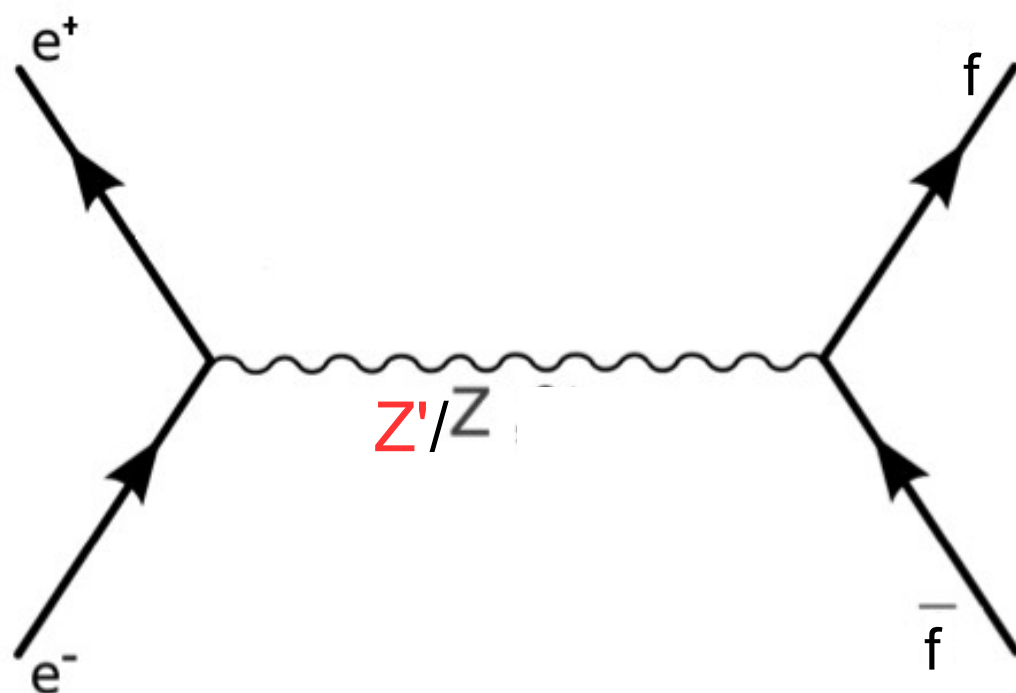


*Slide made  
in 2016!*

- T depends mainly on  $M_W$ 
  - Threshold scan around  $2M_W$  (with polarised beams), see above
- S depends mainly on  $\sin^2 \theta_{\text{eff}}^2$ .
  - Ultra-high statistics sample  $ee \rightarrow ff$  at Z-mass or smaller sample exploiting beam polarisation (Remember LEP and SLC times)

Precision on S and T seems to saturate at  $\delta/\delta_{\text{now}} \approx 0.1 - 0.2$

## On the Z-pole



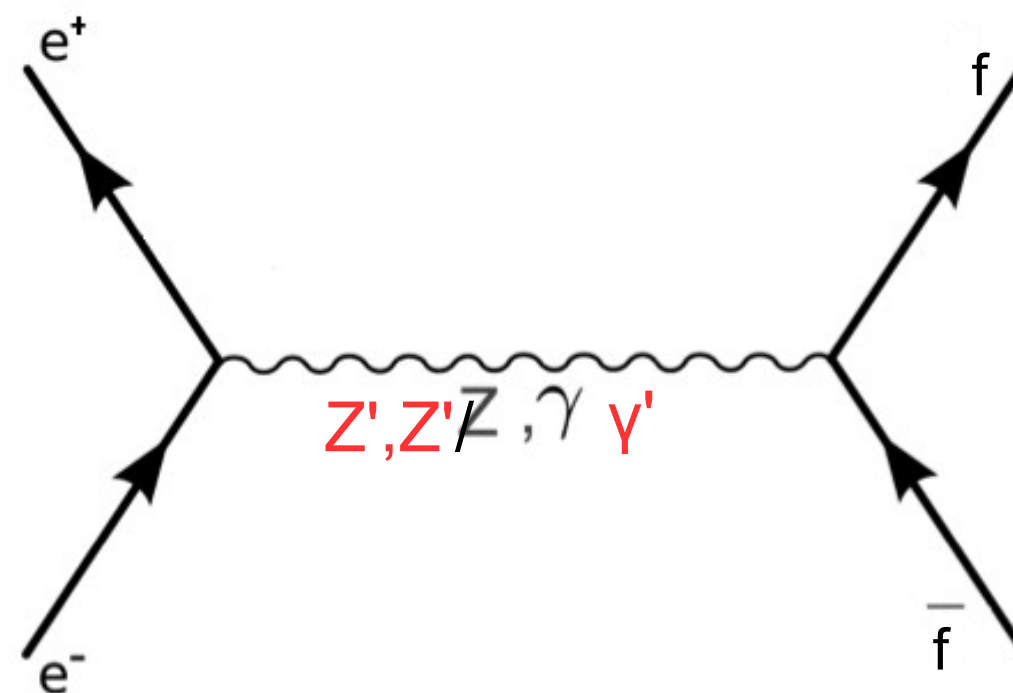
ILC/GigaZ with  $\sim 10^9$  Z

Sensitivity to Z/Z' mixing

Sensitivity to vector (and tensor)  
couplings of the Z

- the photon does not “disturb”

## Above the Z-pole



Sensitivity to interference effects of Z and photon!!

Measured couplings of photon and Z can be influenced  
by new physics effects

Interpretation of result is greatly supported by precise input  
from Z pole



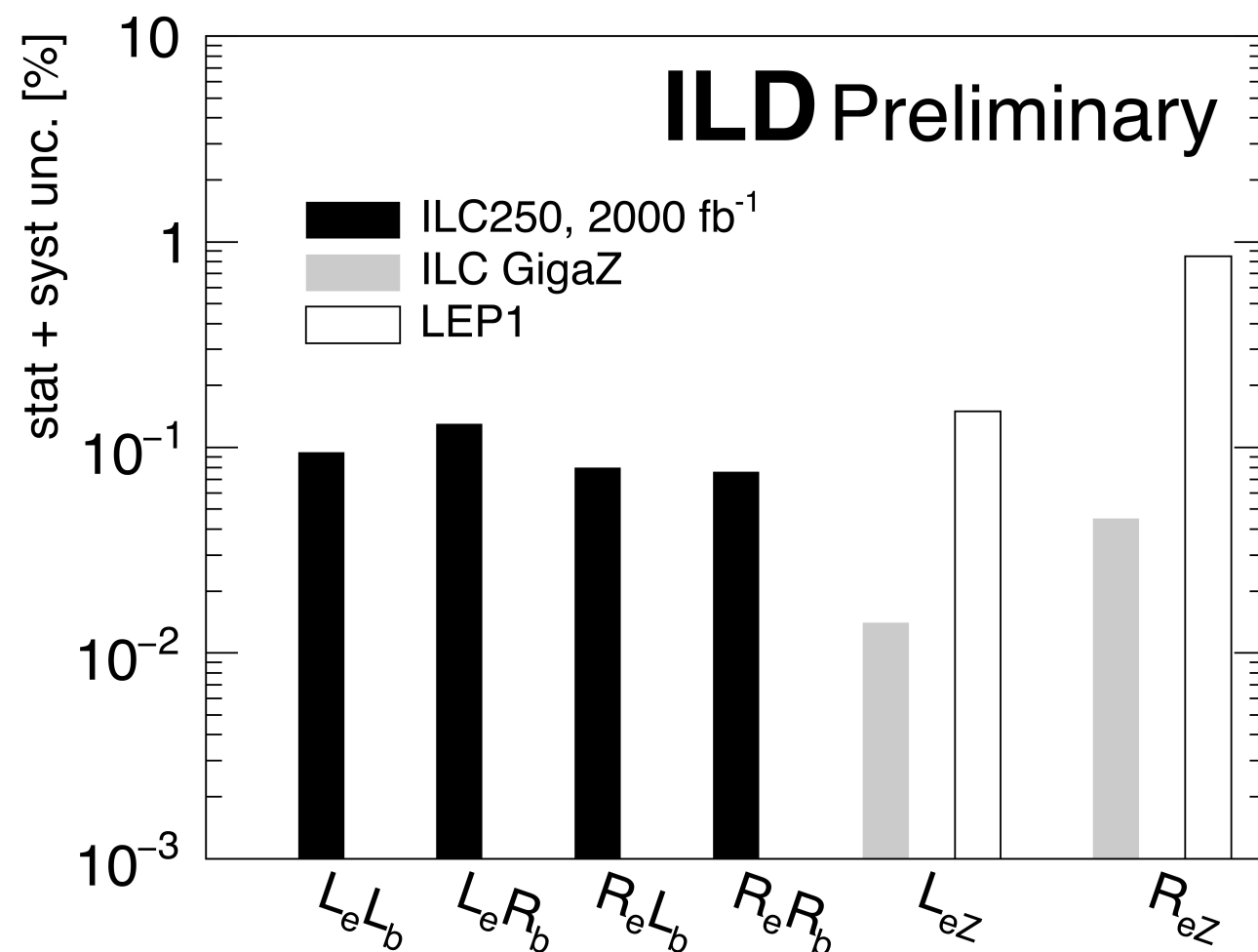


Figure: A. Irles

$$LeLb = QeQb + \frac{LeZLbZ}{s^2wc^2w}BWZ + \sum_{Z'} \frac{LeZ'LbZ'}{s^2wc^2w}BWZ'$$

$\downarrow$  ILC250       $\downarrow$  SM       $\downarrow$  GigaZ       $\downarrow$  New resonances

Couplings are order of magnitude better than at LEP

- In particular right handed couplings are much better constrained

New physics can also influence the Zee vertex

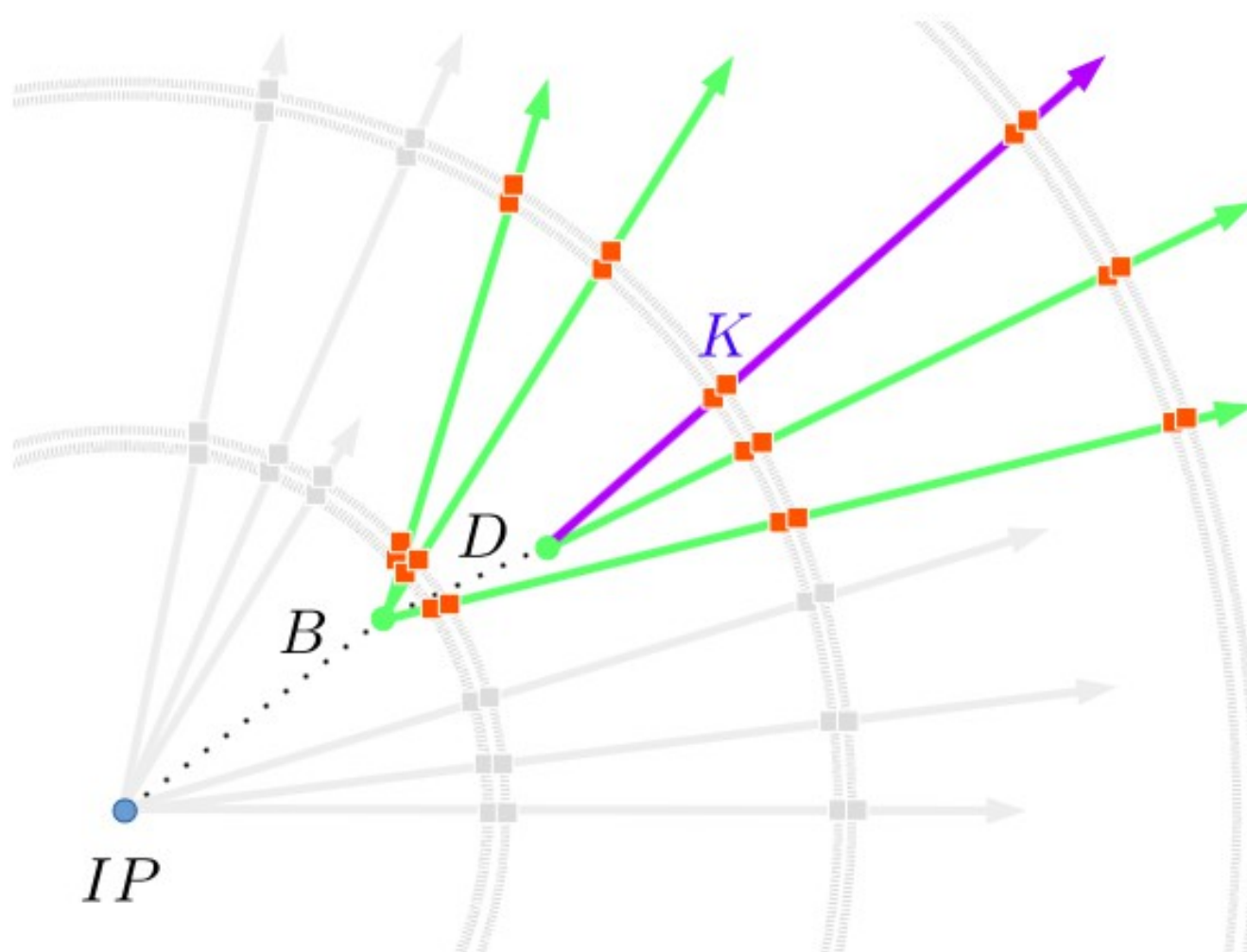
- in 'non top-philic' models

Full disentangling of helicity structure for all fermions  
only possible with polarised beams!!

- There is a strong motivation to measure electroweak heavy quark couplings at the ILC
- New physics models predict deviations and b and c quarks are at the cross roads between 'top-philic' and 'non-top-philic' models
- Remember also LEP anomaly on  $A_{FB}^b$
- ILC with GigaZ is a unique opportunity for a complete set of measurements and an unambiguous interpretation of the results
- Relevant observables at GigaZ are  $A_b$  (see above) and

$$R_q = \frac{N_q}{N_{had}} = \frac{\Gamma_q}{\Gamma_{had}} = \frac{(g_q^L)^2 + (g_q^R)^2}{\sum_{i=1}^{n_q} [(g_i^L)^2 + (g_i^R)^2]}$$

- Here  $\Gamma_{had}$  is constrained by the fact that all hadrons are produced from the known quark species i.e.  $R_b + R_c + R_{uds} = 1$  and has therefore no error, but the  $g_i$  are correlated to fulfill this constraint
- The measured  $\Gamma_{had}$ , which is sensitive to the experimental Z mass resolution has to be considered as a consistency check



- flavor tagging
- b-quark charge measurement
  - Important for top quark studies, indispensable for  $ee \rightarrow bb$
- Control of migrations:
  - Correct measurement of vertex charge
  - Kaon identification by  $dE/dx$  (and more)
- ILC/ILD can base the entire measurements on double Tagging and vertex charge
  - LEP/SLC had to include single tags and Semi-leptonic events

## Beam spot size



	FCCee	ILC	SLC	LEP
$\sigma_x$ [nm]	13700	516	1500	200000
$\sigma_y$ [nm]	36	7.7	500	2500

Source SLC, LEP, PDG

LEP

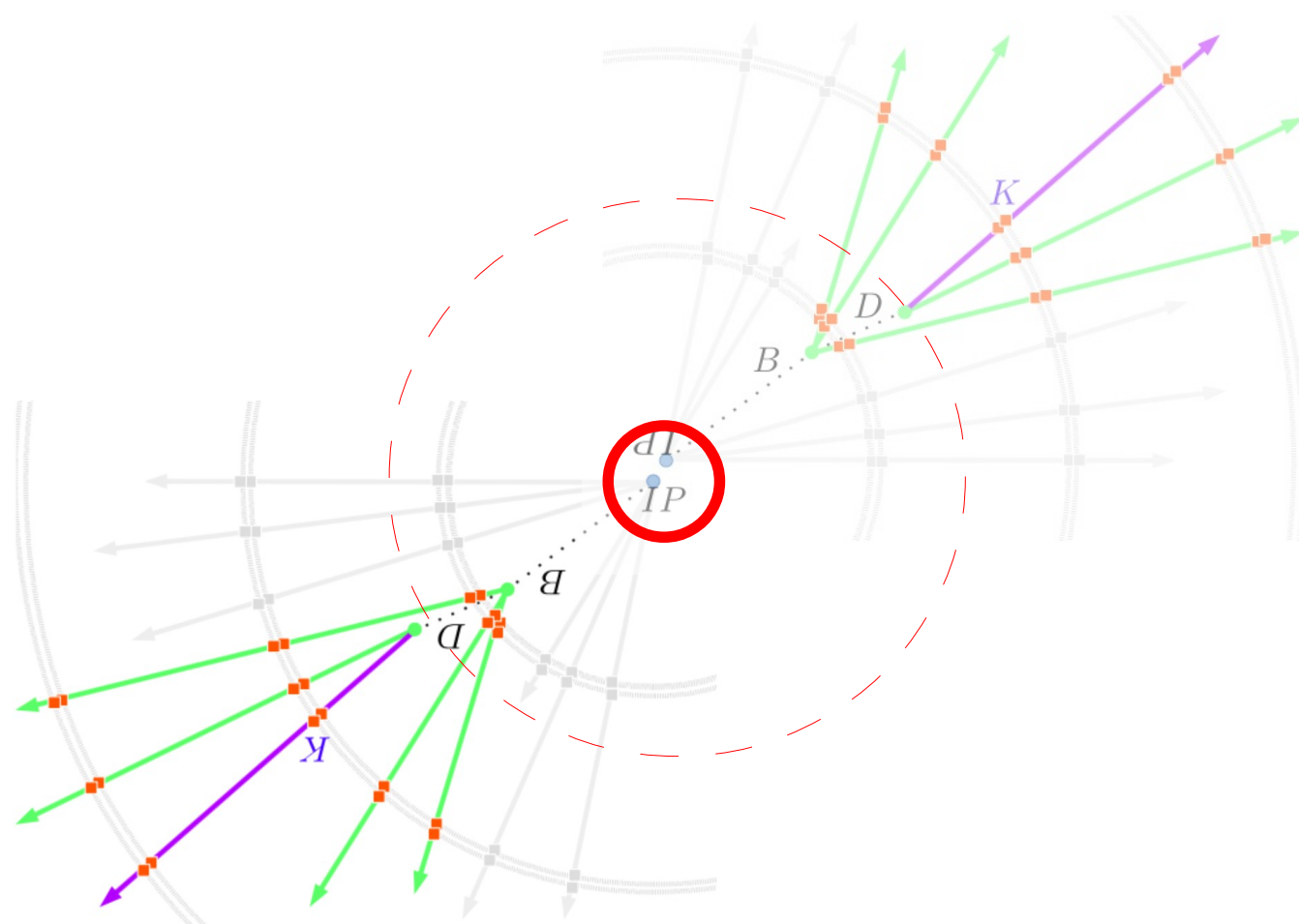
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SLC

>>

ILC





Important systematic error is knowledge of tagging efficiency  $\epsilon_q$

Can be derived from data if tagging is independent in two hemispheres, i.e. if

$$C_q = \frac{\epsilon_{double}}{\epsilon_q^2} \approx 1$$

If  $C_q \neq 1 \Rightarrow$  Hemisphere correlations  $\Rightarrow$  systematic error

For example:

LEP (large beam spot):  $C_q - 1 \approx 3\% \Rightarrow \Delta R_b \approx 0.2\%$

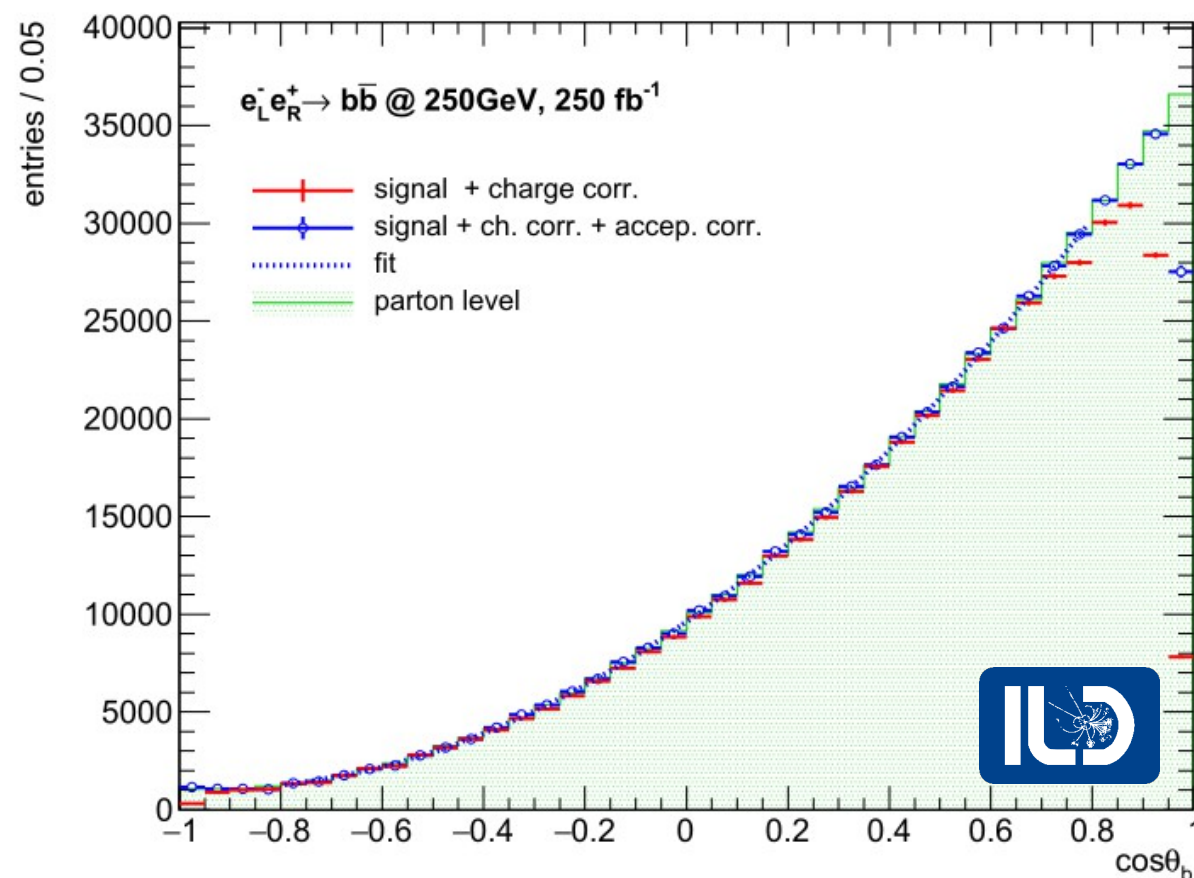
SLC (smaller beam spot):  $C_q - 1 < 1\% \Rightarrow \Delta R_b \approx 0.07\%$

ILC (tiny beam spot): Expect  $C_q - 1 = 0 \Rightarrow \Delta R_b \approx 0$

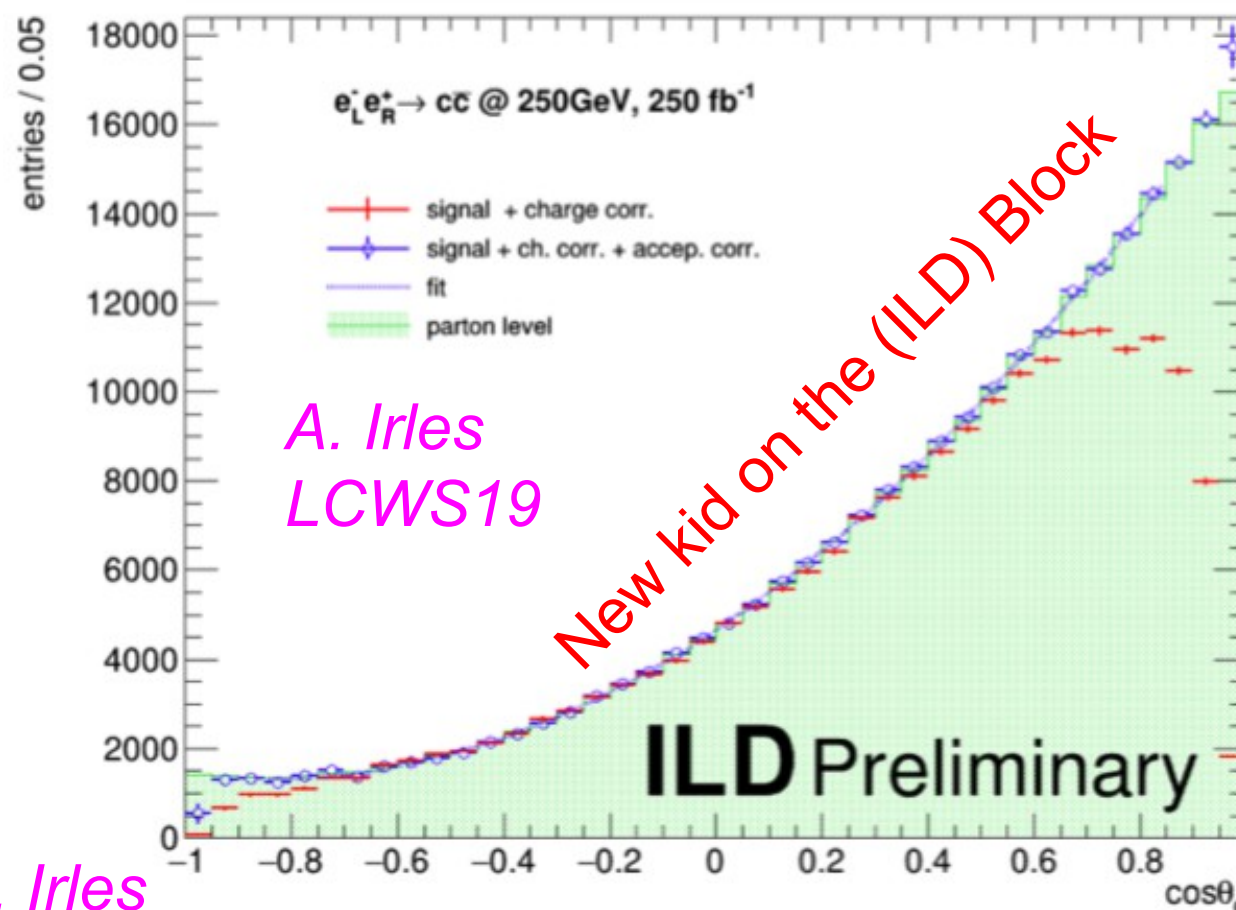
Full simulation studies for ILD confirm  $C_q - 1 = 0$

See talk at LCWS

## Excellent measurement of quark polar angle spectrum by double tagging track assignment



S. Bilokin, A. Irles



- Knowledge obtained at 250 GeV can be extrapolated to the Z-pole
- Relatively safe for b-quark case
  - To be verified for c-case (study for ILC in infancy state)
  - No show stopper observed by studying relevant SLC papers

- Create two samples
  - One with consistent charge measurement in both jets  $(-, +) \Rightarrow N_{acc.}$
  - One with inconsistent charge measurement  $(--, ++)\Rightarrow N_{rej.}$

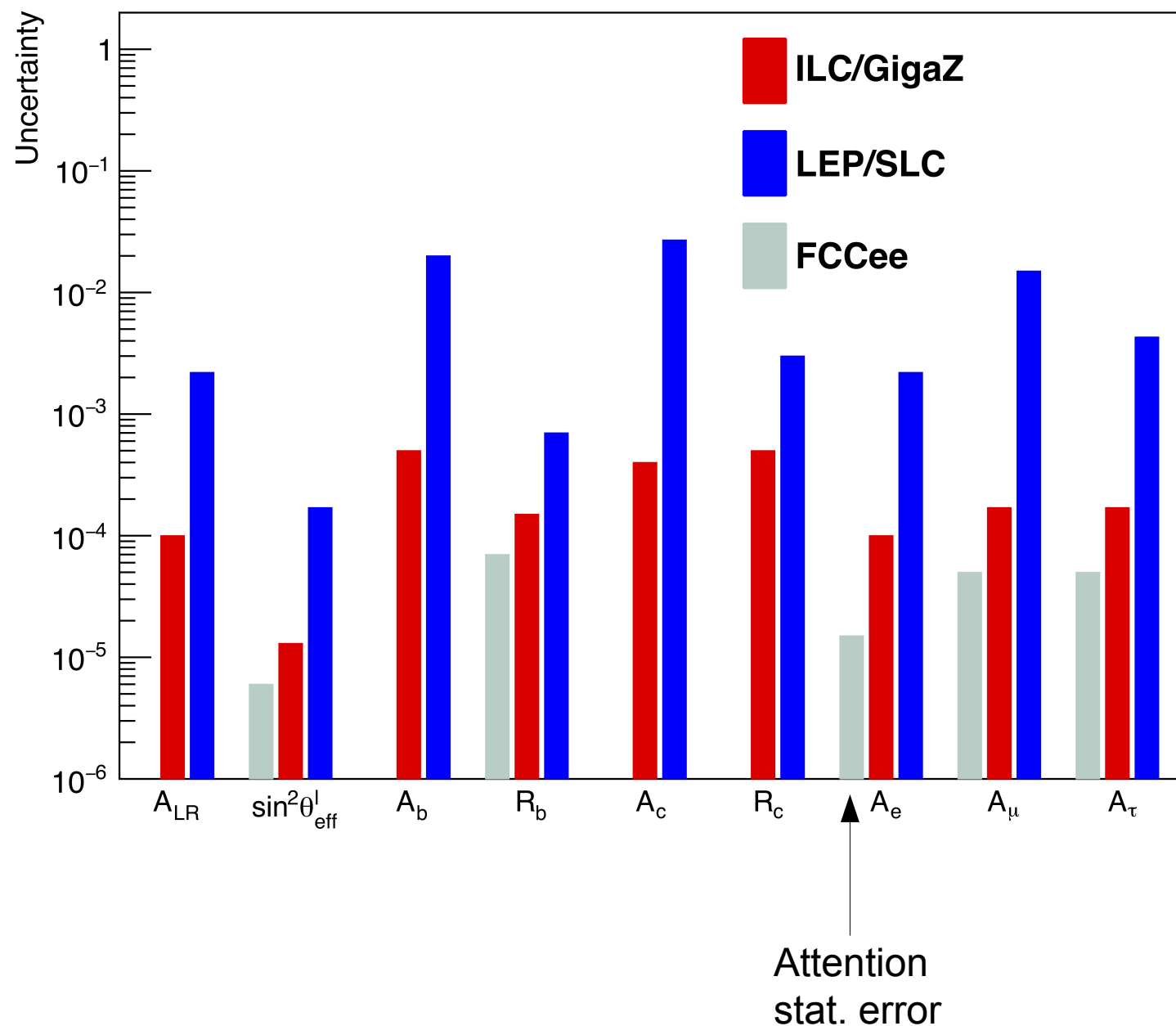
$$N_{acc} = Np^2 + Nq^2$$

$$N_{rej} = 2Npq$$

$$1 = p + q$$

$p$ : probability of a correct charge assignment  
 $q=1-p$ : probability of an incorrect charge assignment

- Two equations for two unknowns  
 $pq$ -formula allows for correcting for migrations and in particular for the last and ultimate migration (dilution) due to  $B^0$  oscillations
- Only possible since we always analyse quark and anti-quark
  - i.e. exclusive use of double tag events (was very limited at LEP and SLC)
  - All papers praise the usefulness of double tag and vertex charge measurements, well here it is!



Precise measurement of  $\sin^2 \theta_{\text{eff}}^l$ .

- Ten times better than LEP/SLD and competitive with FCC
- **Polarisation compensates for ~30 times luminosity**
- ... and  $A_{LR}$  at LC can benefit from hadronic Z decays
- **No assumption on lepton universality at LC**

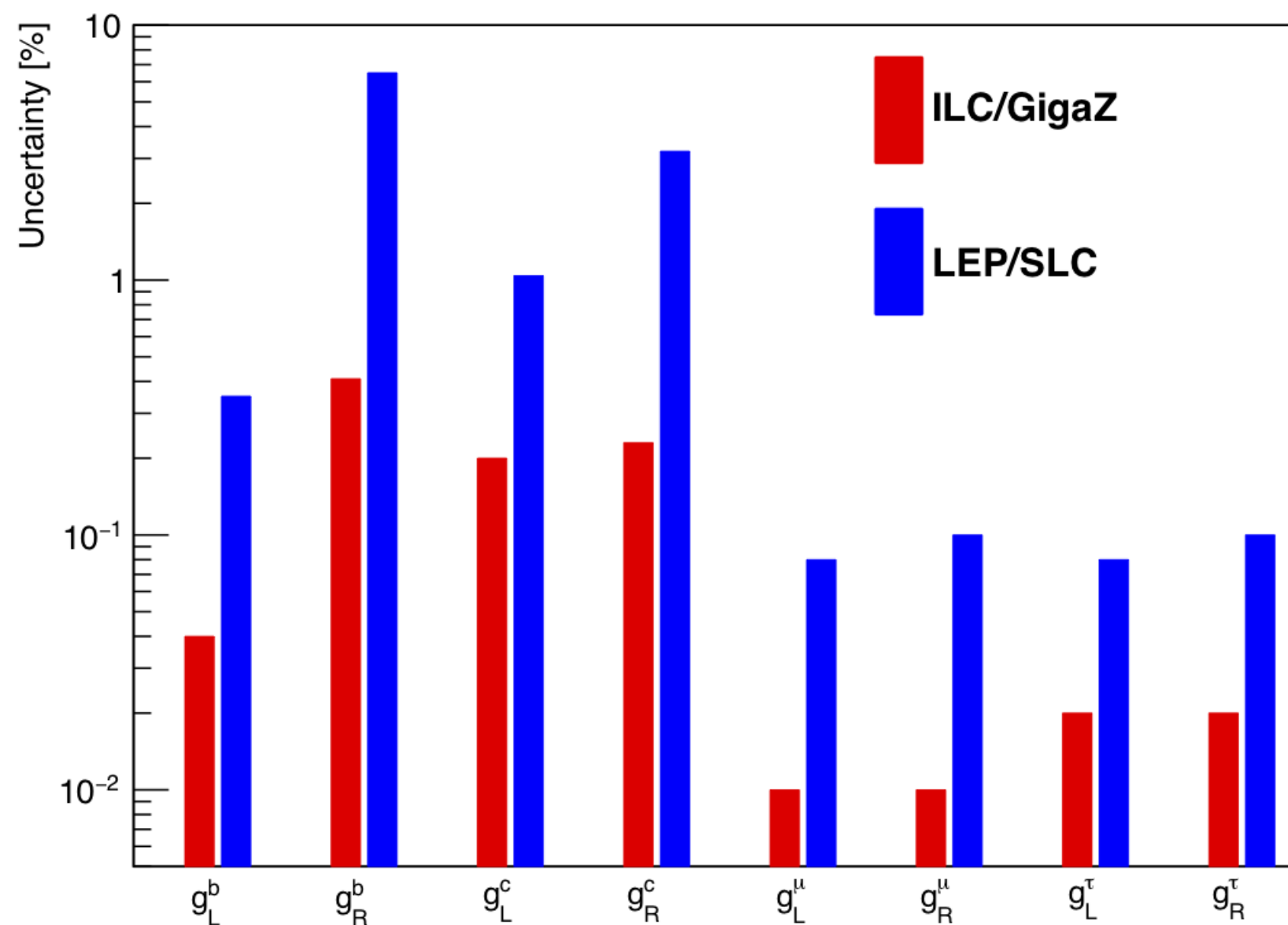
Complete test of lepton universality

- Precisions of order 0.05%

Note excellent measurement of quark asymmetries

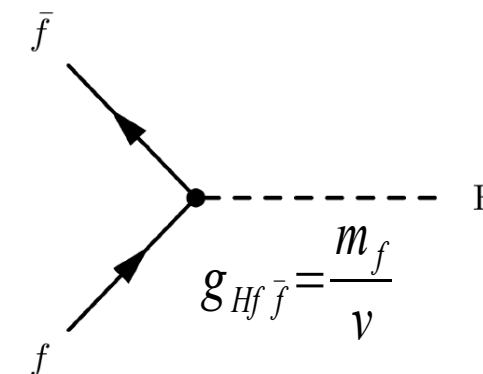
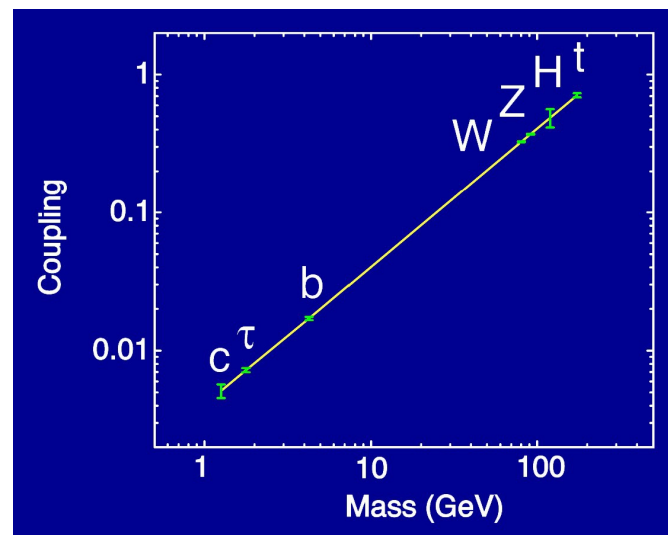
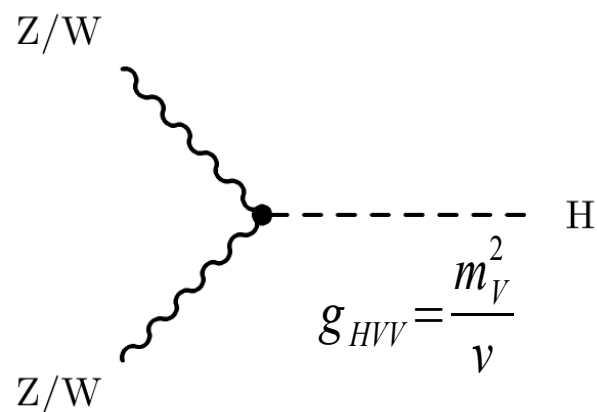
- See above for  $ee \rightarrow bb$  at 250 GeV
- *More details in talks by A. Irles and R.P. in parallel sessions*





What about the Higgs?

## Couplings to Higgs Boson in Standard Model



### Analysis using Kappa-fit:

Simple scaling of SM-couplings  
Implies that Higgs coupling to Z in production and decay are identical  
No new operators

$$\frac{\Gamma(h \rightarrow ZZ^*)}{SM} = \kappa_Z^2, \quad \frac{\sigma(e^+e^- \rightarrow Zh)}{SM} = \kappa_Z^2$$

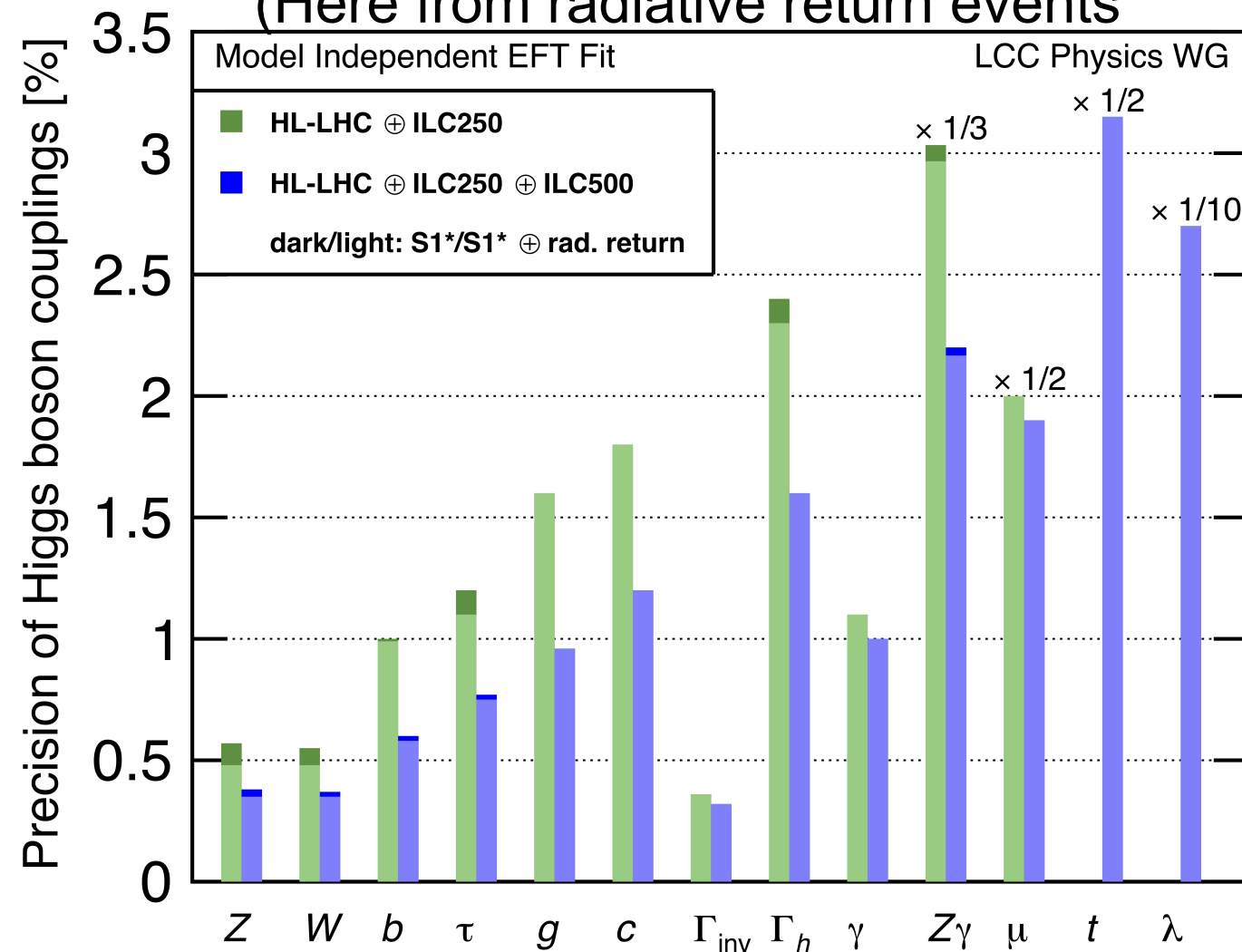
### Analysis using EFT-fit:

Introducing set of SU(2)xU(1) compatible operators  
e.g. breaks simple relation between Higgs production and decay  
Total width and Higgs to invisible as free parameters

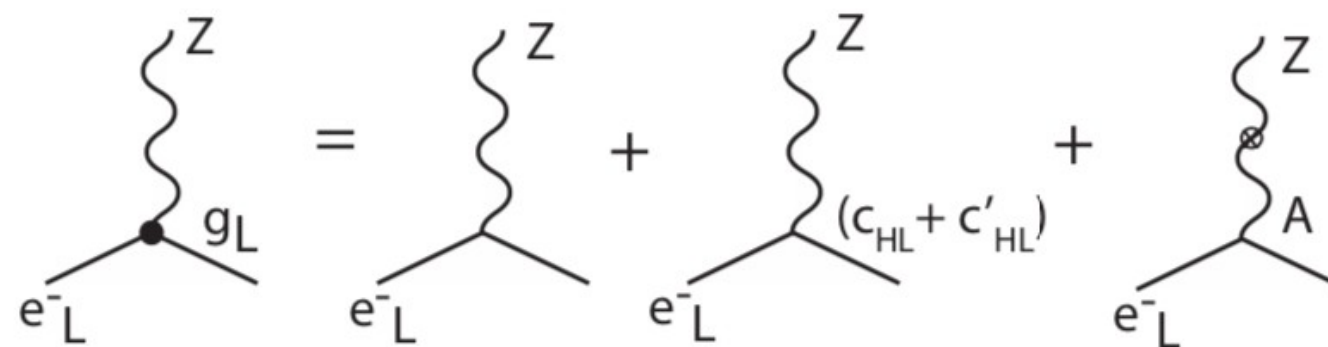
**Receives additional input from e.g. ee $\rightarrow$ WW and EWPO**

$$\begin{aligned} \Gamma(h \rightarrow ZZ^*)/SM &= (1 + 2\eta_Z - 0.50\zeta_Z) \\ \sigma(e^+e^- \rightarrow Zh)/SM &= (1 + 2\eta_Z + 5.7\zeta_Z) \end{aligned}$$

## Higgs couplings in EFT using $A_{LR}$ (Here from radiative return events)

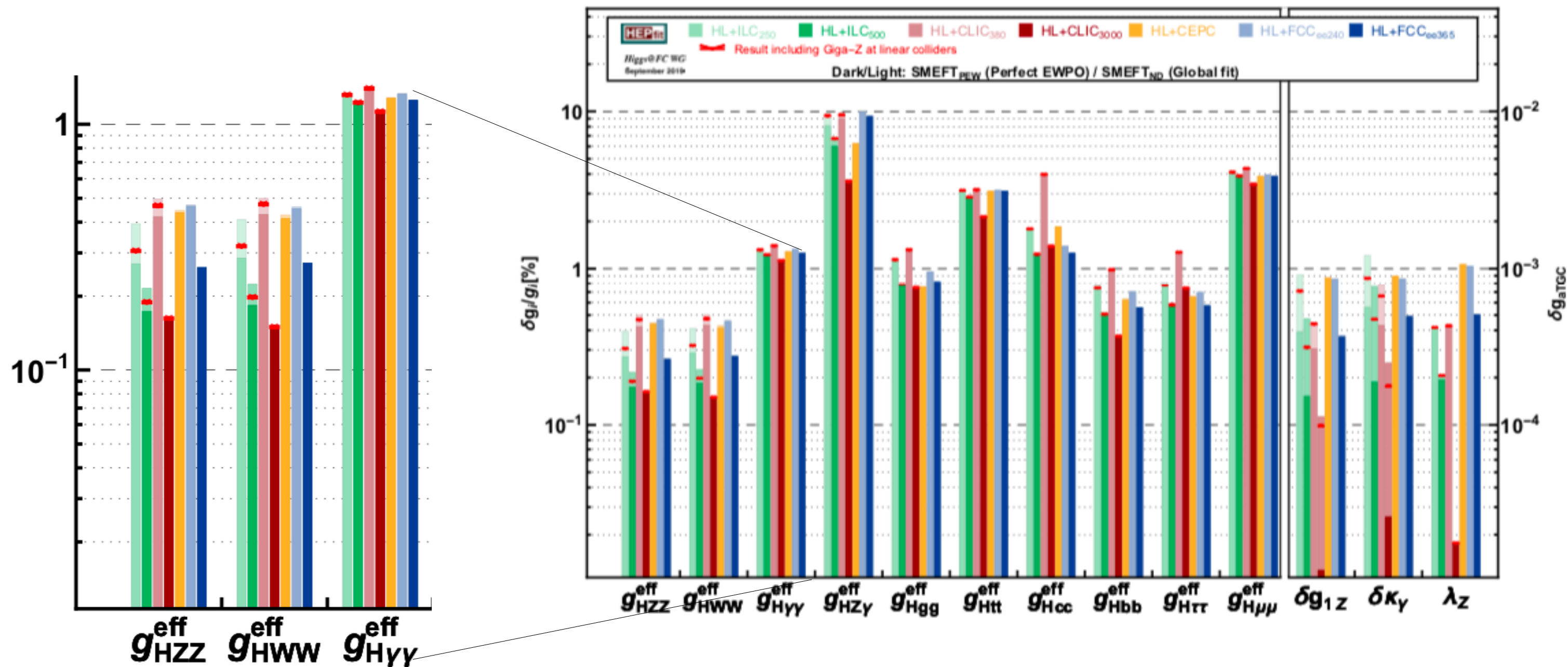


Corrections to Zee-vertex due to additional terms in EFT



- Model independent, clean  $A_e$  from  $A_{LR}$  and  $\Gamma_e$  from  $R_e$  to constrain EFT fit
  - (again) No assumption of Lepton Universality
- Mild but visible improvement on some Higgs couplings at 250 GeV
  - Effect stronger in fit presented in 1905.03764 (see next slide)

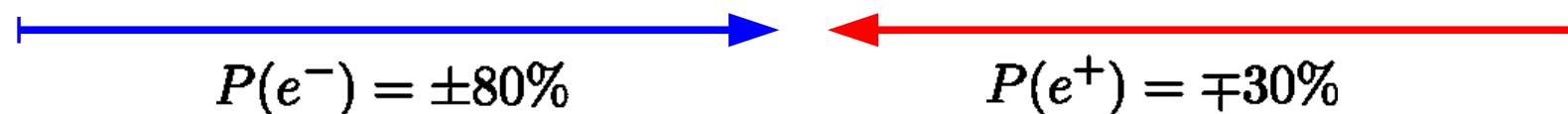




- GigaZ with polarised beams allows for including EWPO into ILC program
  - Polarisation compensates a great deal the lower luminosity
  - For comprehensive overviews see also hep-ph/0507011 and TESLA TDR
- “GigaZ Comeback” after Grenada
- Higher precision on relevant quantities (e.g.  $e\bar{e} \rightarrow b\bar{b}$  couplings) needed for correct interpretation of ILC results at all energies
- Machine can be set up to run on the Z-pole
  - May put additional challenges to detectors
- Heavy quark observables show nicely the progress that can be expected compared with LEP/SLC
- LCC Physics Group input for Physics Briefing Book of European Strategy arxiv:1908.1299

Backup

With two beam polarisation configurations



There exist a number of observables sensitive to chiral structure, e.g.

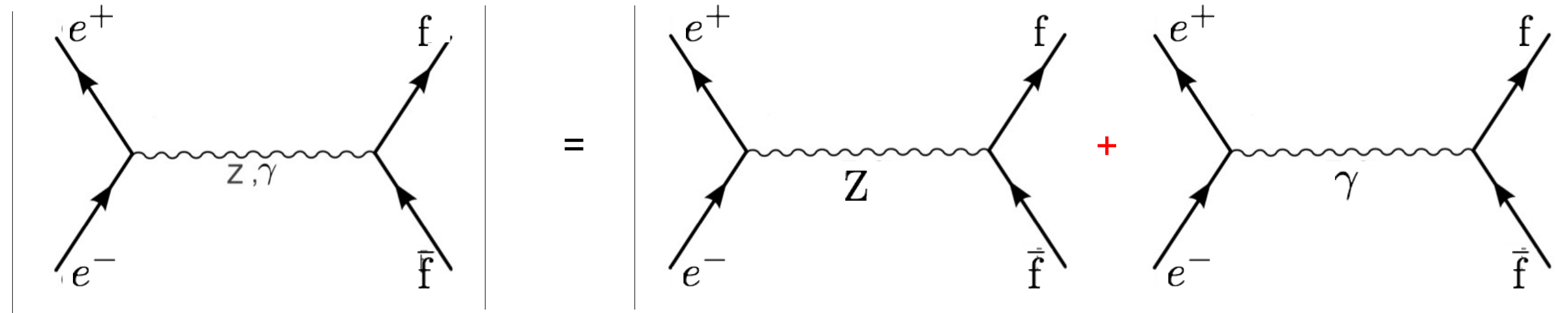
$\sigma_I$	$A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$	$(F_R)_I = \frac{(\sigma_{t_R})_I}{\sigma_I}$
x-section	Forward backward asymmetry	Fraction of right handed top quarks



Extraction of relevant unknowns

$$\begin{array}{c}
 F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \\
 F_{2V}^\gamma, F_{2V}^Z
 \end{array}
 \quad \text{or equivalently} \quad
 g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

# Cross section $e^+e^- \rightarrow f\bar{f}$



Interference between individual amplitudes of  $\gamma$  and  $Z$  exchange

$$\mathcal{M}_Z = -\frac{\sqrt{2}G_F M_Z^2}{s - M_Z^2} \left[ \bar{f} \gamma^\rho (c_V^f - c_A^f \gamma^5) f \right] g_{\rho\sigma} \left[ \bar{e} \gamma^\sigma (c_V^e - c_A^e \gamma^5) e \right]$$

$$\mathcal{M}_\gamma = -\frac{e^2}{s} (\bar{f} \gamma^\nu f) g_{\mu\nu} (\bar{e} \gamma^\mu e)$$

$$g_L^f = c_V^f + c_A^f$$

$$g_R^f = c_V^f - c_A^f$$

Differential cross section:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4s} \left[ A_0(1 + \cos^2\theta) + A_1 \cos\theta \right] \left\{ \begin{array}{ll} \sim (1 + \cos^2\theta) & \text{'Usual' Vector current, symmetric in } \cos\theta \\ \sim \cos\theta & \text{Axial Vector current, asymmetric in } \cos\theta \end{array} \right.$$

Weak interaction introduces forward backward asymmetry

=> Asymmetry is intrinsic to electroweak processes!!!



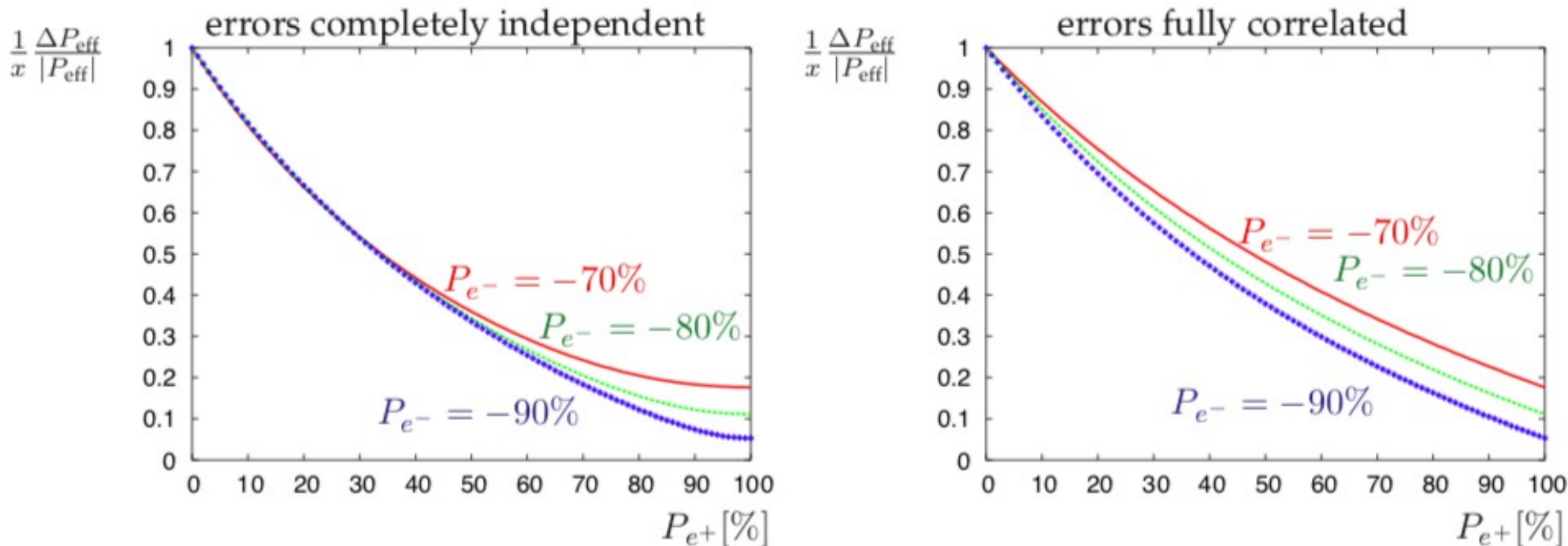
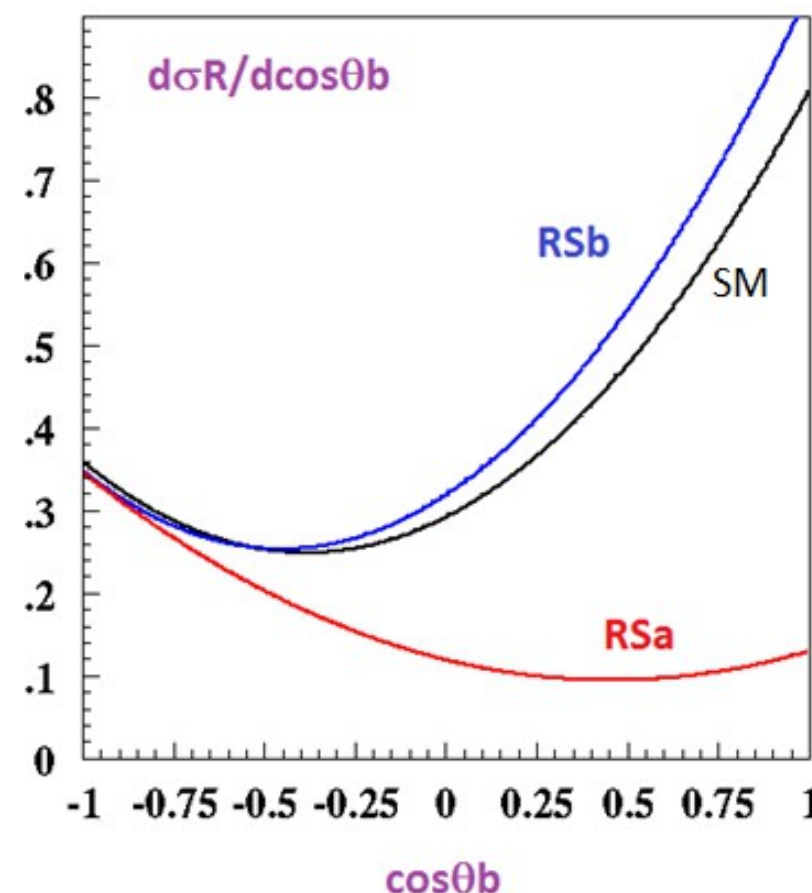
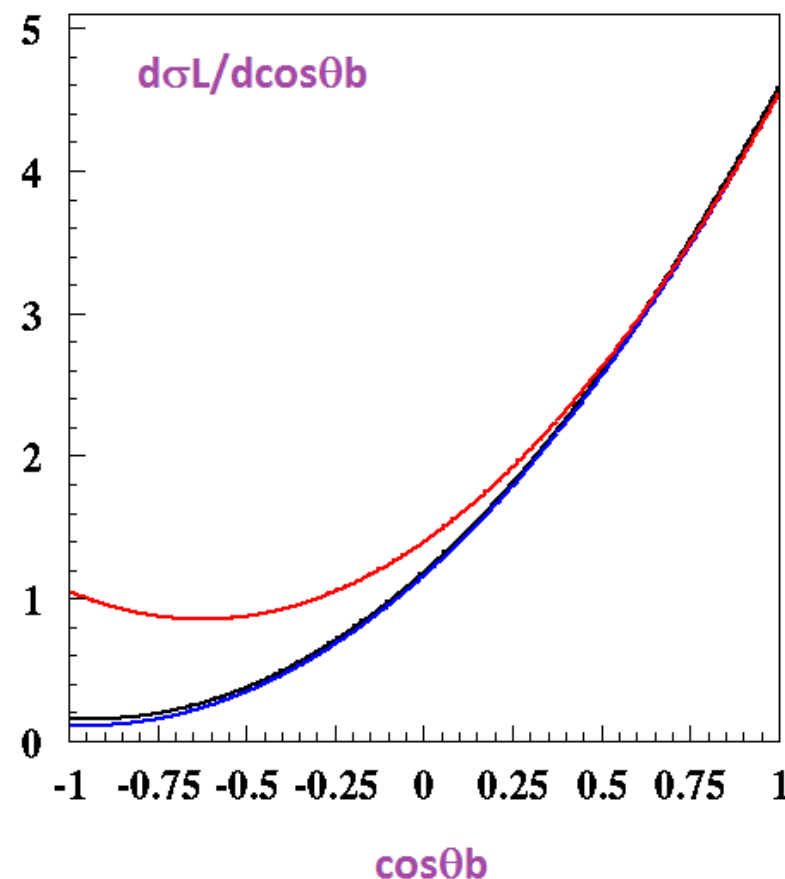
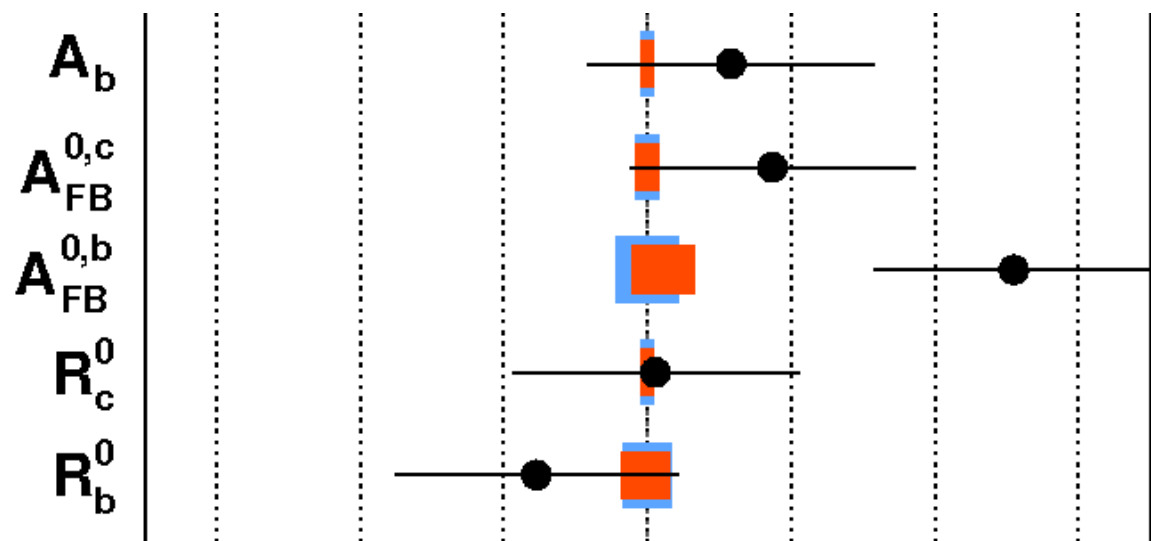


Figure 1.6: Relative uncertainty on the effective polarization,  $\Delta P_{\text{eff}}/|P_{\text{eff}}| \sim \Delta A_{\text{LR}}/A_{\text{LR}}$ , normalized to the relative polarimeter precision  $x = \Delta P_{e^-}/P_{e^-} = \Delta P_{e^+}/P_{e^+}$  for independent and correlated errors on  $P_{e^-}$  and  $P_{e^+}$ , see eqs. (1.25), (1.27).

$$A_{\text{LR}} = \frac{1}{P_{\text{eff}}} A_{\text{LR}}^{\text{obs}} = \frac{1}{P_{\text{eff}}} \frac{\sigma_{-+} - \sigma_{+-}}{\sigma_{-+} + \sigma_{+-}}, \quad (1.24)$$

$\sim 3\sigma$  in heavy quark observable  $A_{FB}^b$

ee- $\rightarrow$ bb@250 GeV



- Is tension due to underestimation of errors or due to new physics?

- High precision e<sup>+</sup>e<sup>-</sup> collider will give final word on anomaly

Randall Sundrum Models Djouadi/Richard '06

- In case it will persist polarised beams will allow for discrimination between effects on left and right handed couplings (Remember  $Zb_l b_l$  is protected by cross section)

- Note that also B-Factories report on anomalies LCWS 2019